

# Black holes with torsion

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# Torsion and curvature

- Definition of the torsion tensor (contains 24 dof):

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$$\begin{aligned}\tilde{R}^\lambda{}_{[\mu\nu\rho]} &= \tilde{\nabla}_{[\mu}T^\lambda{}_{\rho\nu]} + T^\sigma{}_{[\mu\rho}T^\lambda{}_{\nu]\sigma}, \\ \tilde{\nabla}_{[\sigma|}\tilde{R}^\lambda{}_{\rho|\mu\nu]} &= T^\omega{}_{[\sigma\mu|}\tilde{R}^\lambda{}_{\rho\omega|\nu]}.\end{aligned}$$

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- Just one independent trace, the generalised Ricci tensor

$$\tilde{R}_{\mu\nu} = \tilde{R}^\lambda{}_{\mu\lambda\nu},$$

- Unique scalar and pseudoscalar curvatures:

$$\tilde{R} = g^{\mu\nu} \tilde{R}_{\mu\nu}, \quad * \tilde{R} = \varepsilon^{\lambda\rho\mu\nu} \tilde{R}_{\lambda\rho\mu\nu}.$$

# Dynamics in theories with torsion

- One can write down an action of the form

$$S = \int d^4x \sqrt{-g} \left[ \mathcal{L}_m - \frac{1}{2\kappa^2} \mathcal{L}_g(\tilde{\mathcal{R}}, \mathcal{T}) \right].$$

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- Correspondence between geometry and matter:

$$\frac{1}{\sqrt{-g}} \frac{\delta(\mathcal{L}_g \sqrt{-g})}{\delta e^a{}_\nu} = 2\kappa^2 \theta_a{}^\nu,$$
$$\frac{1}{\sqrt{-g}} \frac{\delta(\mathcal{L}_g \sqrt{-g})}{\delta \omega^a{}_{b\nu}} = 2\kappa^2 \Delta_a{}^{b\nu},$$

where we have two matter sources:

$$\theta_\mu{}^\nu = \frac{e^a{}_\mu}{\sqrt{-g}} \frac{\delta(\sqrt{-g} \mathcal{L}_m)}{\delta e^a{}_\nu},$$
$$\Delta^{\lambda\mu\nu} = \frac{e^{a\lambda} e_b{}^\mu}{\sqrt{-g}} \frac{\delta(\sqrt{-g} \mathcal{L}_m)}{\delta \omega^a{}_{b\nu}}.$$

# Poincaré gauge theory

- $ISO(1, 3) = T^4 \rtimes SO(1, 3)$  gauge connection<sup>1</sup>:

$$A_\mu = e^a{}_\mu P_a + \omega^a{}_{b\mu} J_a{}^b, \quad g_{\mu\nu} = e^a{}_\mu e^b{}_\nu \eta_{ab},$$

where

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- Generators of the Poincaré group  $ISO(1, 3)$ :

$$[P_a, P_b] = 0, \quad [P_a, J_{bc}] = i \eta_{a[b} P_{c]},$$

$$[J_{ab}, J_{cd}] = \frac{i}{2} (\eta_{ad} J_{bc} + \eta_{cb} J_{ad} - \eta_{db} J_{ac} - \eta_{ac} J_{bd}).$$

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- $ISO(1, 3)$  translational and rotational field strength tensors:

$$F_{\mu\nu} = F^a{}_{\mu\nu} P_a + F^a{}_{b\mu\nu} J_a{}^b,$$

where

$$F^a{}_{\mu\nu} = \partial_\mu e^a{}_\nu - \partial_\nu e^a{}_\mu + \omega^a{}_{b\mu} e^b{}_\nu - \omega^a{}_{b\nu} e^b{}_\mu,$$

$$F^a{}_{b\mu\nu} = \partial_\mu \omega^a{}_{b\nu} - \partial_\nu \omega^a{}_{b\mu} + \omega^a{}_{c\mu} \omega^c{}_{b\nu} - \omega^a{}_{c\nu} \omega^c{}_{b\mu}.$$

# Quadratic Poincaré gauge theory - ghost issue

- Convenient to decompose torsion as

$$T^\lambda{}_{\mu\nu} = \frac{1}{3} (\delta^\lambda{}_\nu T_\mu - \delta^\lambda{}_\mu T_\nu) + \frac{1}{6} \varepsilon^\lambda{}_{\rho\mu\nu} S^\rho + t^\lambda{}_{\mu\nu}.$$

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- The most general class of quadratic Poincaré gauge models that are reduced to General Relativity in the absence of torsion is:

$$S_g = \frac{1}{16\pi} \int \left[ -R + c_2 \tilde{R}_{\lambda\rho\mu\nu} \tilde{R}^{\lambda\mu\rho\nu} - \frac{1}{2} (2c_1 + c_2) \tilde{R}_{\lambda\rho\mu\nu} \tilde{R}^{\mu\nu\lambda\rho} + c_1 \tilde{R}_{\lambda\rho\mu\nu} \tilde{R}^{\lambda\rho\mu\nu} \right. \\ \left. + d_1 \tilde{R}_{\mu\nu} (\tilde{R}^{\mu\nu} - \tilde{R}^{\nu\mu}) + \frac{1}{2} (m_T^2 T_\mu T^\mu + m_S^2 S_\mu S^\mu + m_t^2 t_{\lambda\mu\nu} t^{\lambda\mu\nu}) \right] \sqrt{-g} d^4x.$$

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- It is not possible to have a stable propagating torsion tensor in quadratic Poincaré gauge theory for general backgrounds. Kinetic part of vectors  $T_\mu$  and  $S_\mu$  propagate a ghost.

# Cubic Poincaré gauge theory

- Cubic parity preserving branch with mixing terms:<sup>2</sup>

$$\mathcal{L}_{\text{curv-tors}}^{(3)} = \mathcal{L}_{\tilde{R}TT}^{(3)} + \mathcal{L}_{\tilde{R}SS}^{(3)} + \mathcal{L}_{\tilde{R}tt}^{(3)} + \mathcal{L}_{\tilde{R}TS}^{(3)} + \mathcal{L}_{\tilde{R}Tt}^{(3)} + \mathcal{L}_{\tilde{R}St}^{(3)},$$

$$\mathcal{L}_{\tilde{R}TT}^{(3)} = h_1 \tilde{R}_{\mu\nu} T^\mu T^\nu + h_2 \tilde{R} T_\mu T^\mu, \quad \mathcal{L}_{\tilde{R}SS}^{(3)} = h_3 \tilde{R}_{\mu\nu} S^\mu S^\nu + h_4 \tilde{R} S_\mu S^\mu,$$

$$\begin{aligned} \mathcal{L}_{\tilde{R}tt}^{(3)} &= h_5 \tilde{R}_{\lambda\rho\mu\nu} t_\sigma^{\lambda\rho} t^{\sigma\mu\nu} + h_6 \tilde{R}_{\lambda\rho\mu\nu} t_\sigma^{\lambda\mu} t^{\sigma\rho\nu} + h_7 \tilde{R}_{\lambda\rho\mu\nu} t^{\lambda\rho} t^{\sigma\mu\nu} \\ &+ h_8 \tilde{R}_{\lambda\rho\mu\nu} t^{\lambda\mu} t^{\sigma\rho\nu} + h_9 \tilde{R}_{\lambda\rho\mu\nu} t^{\lambda\mu} t^{\rho\nu\sigma} + h_{10} \tilde{R}_{\lambda\rho} t_{\mu\nu}^{\lambda} t^{\rho\mu\nu} \\ &+ h_{11} \tilde{R}_{\lambda\rho} t_{\mu\nu}^{\lambda} t^{\mu\nu\rho} + h_{12} \tilde{R} t_{\lambda\rho\mu}^{\lambda} t^{\rho\mu}, \end{aligned}$$

$$\mathcal{L}_{\tilde{R}TS}^{(3)} = h_{13} \varepsilon^{\lambda\rho\mu\nu} \tilde{R}_{\lambda\rho\mu\nu} T_\sigma S^\sigma + h_{14} \varepsilon_{\nu}^{\lambda\rho\sigma} \tilde{R}_{\lambda\rho\mu\sigma} T^\mu S^\nu + h_{15} \varepsilon^{\lambda\rho\mu\nu} \tilde{R}_{\lambda\rho} T_\mu S_\nu,$$

$$\mathcal{L}_{\tilde{R}Tt}^{(3)} = h_{16} \tilde{R}_{\lambda\rho\mu\nu} T^\nu t^{\lambda\rho\mu} + h_{17} \tilde{R}_{\lambda\rho\mu\nu} T^\rho t^{\lambda\mu\nu} + h_{18} \tilde{R}_{\lambda\rho} T_\mu t^{\mu\lambda\rho} + h_{19} \tilde{R}_{\lambda\rho} T_\mu t^{\lambda\rho\mu},$$

$$\begin{aligned} \mathcal{L}_{\tilde{R}St}^{(3)} &= h_{20} \varepsilon_{\alpha\rho\mu\nu} \tilde{R}_\tau^{\rho\mu\nu} S^\gamma t^{\alpha\tau}{}_\gamma + h_{21} \varepsilon_{\alpha\rho\mu\nu} \tilde{R}_\tau^{\rho\mu\nu} S^\gamma t_\gamma{}^{\alpha\tau} \\ &+ h_{22} \varepsilon_{\alpha\rho}{}^{\mu\nu} \tilde{R}^\rho{}_{\mu\tau\nu} S^\gamma t_\gamma{}^{\alpha\tau} + h_{23} \varepsilon_{\alpha\rho}{}^{\mu\nu} \tilde{R}_{\gamma\mu\tau\nu} S^\alpha t^{\gamma\rho\tau} \\ &+ h_{24} \varepsilon_{\alpha\rho}{}^{\mu\nu} \tilde{R}_{\gamma\mu\tau\nu} S^\alpha t^{\rho\tau\gamma} + h_{25} \varepsilon_{\alpha\rho\tau\mu} \tilde{R}^\mu{}_\gamma S^\alpha t^{\rho\tau\gamma} + h_{26} \varepsilon_{\lambda\rho\mu\nu} \tilde{R}^{\lambda\rho} S_\sigma t^{\sigma\mu\nu}. \end{aligned}$$

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- We showed that by including these Poincare gauge invariants, ghost issue is solved!

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# Spherically symmetric black holes

- Explicit symmetries on the metric, torsion and nonmetricity tensors:

$$\mathcal{L}_\xi g_{\mu\nu} = \mathcal{L}_\xi T^\lambda{}_{\mu\nu} = 0 \implies \mathcal{L}_\xi \tilde{R}^\lambda{}_{\rho\mu\nu} = 0.$$

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- Static and spherically symmetric space-times:

$$\#10 \rightarrow \#2 \left\{ ds^2 = \Psi_1(r) dt^2 - \frac{dr^2}{\Psi_2(r)} - r^2 (d\vartheta^2 + \sin^2 \vartheta d\varphi^2) \right. ;$$

$$\#24 \rightarrow \#8 \left\{ \begin{array}{ccc} T^t{}_{tr} & T^r{}_{tr} & T^\vartheta{}_{t\vartheta} \\ T^\vartheta{}_{r\vartheta} & T^\vartheta{}_{t\varphi} & T^\vartheta{}_{r\varphi} \\ T^t{}_{\vartheta\varphi} & T^r{}_{\vartheta\varphi} & \end{array} \right.$$

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- First one needs to solve the connection eqs (8 eqs+8 dof of torsion) and then the metric eqs (2 eqs+2 dof).

- By solving the equations in Cubic Poincare we find an exact BH solution:

$$T^t{}_{tr} = \frac{\Psi'(r)}{2\Psi(r)} + \frac{wr}{\Psi(r)}, \quad T^r{}_{tr} = T^t{}_{tr}\Psi(r),$$

$$T^\vartheta{}_{t\vartheta} = -T^\vartheta{}_{r\vartheta}\Psi(r), \quad T^\vartheta{}_{r\vartheta} = -\frac{1}{2r} - \frac{wr}{2\Psi(r)},$$

$$T^\vartheta{}_{t\varphi} = -T^\vartheta{}_{r\varphi}\Psi(r), \quad T^\vartheta{}_{r\varphi} = \frac{N_1\kappa_s}{r\Psi(r)}\sin\vartheta,$$

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# Reissner-Nordström-like black holes in Cubic Poincare

- By solving the equations in Cubic Poincare we find an exact BH solution:

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- The metric sector behaves as:

$$\Psi = 1 - \frac{2m}{r} + (2N_1 - N_2)(N_1 + N_2) \left[ \frac{2N_1 + N_2}{4N_1 + N_2} d_1 + 2h_{25} \right] \frac{\kappa_s^2}{3r^2}.$$

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- This solution has a dynamical torsion with its spin-2 part being massive and is related to the constant  $w$ .

# Electrodynamics coupled with torsion

- Let us consider a theory with couplings between the electromagnetic field strength  $F_{\mu\nu} = \partial_{[\mu}A_{\nu]}$  and  $\tilde{R}^\lambda{}_{\rho\mu\nu}$ :

$$\mathcal{L} = -R - 4k_1 F_{\mu\nu} F^{\mu\nu} + k_2 \tilde{R}^2 + k_3 F^{\mu\nu} \tilde{R}_{\mu\nu} .$$

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- With the following metric and electric potential

$$\Psi(r) = 1 - \frac{2m}{r} + \frac{k_1 q^2}{r^2} - \frac{k_3 \kappa_s q}{4r^2} - \frac{k_3^2 q^2}{128 k_2 r^2},$$
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- New coupling between spin charge  $\kappa_s$  and electric charge  $q$ .
- Different charges would give rise to different phenomenology.

# What does this charge $\kappa_S$ represent?

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- 4 We expect that the spin charge might be important in certain astrophysical scenarios such as: highly magnetized neutron stars; supermassive black holes with endowed spin.

# Axially symmetric black holes

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- We recently found a solution in the non-dynamical part and with that part, we are investigating the dynamical part.
- In spherical symmetry we obtained RN, but in axial symmetry we expect to have an extension of Kerr-Newman with new interactions between  $\kappa_s$  (intrinsic spin) and macroscopic spin  $a$ .

## Spin-Orbit Interaction in Atomic Physics

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- The spin-orbit interaction increases the energy gap between certain nuclear energy levels, making nuclei with magic numbers more stable.

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- We are now trying to find the dynamical part as well.

# Conclusions

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- Quadratic Poincare gauge gravity contains ghosts but we cure this issue with cubic interactions of the form  $\tilde{R}TT$ .
- We found new exact spherically symmetric solutions with dynamical torsion with a charge (intrinsic spin) that enters the metric as RN.
- We are now investigating axial symmetry where we observe the emergence of a potentially new physical interaction within our theory: a gravitational spin-orbit coupling  $a\kappa_s$ .

# Thank You for Listening!

*Questions? Comments?*

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