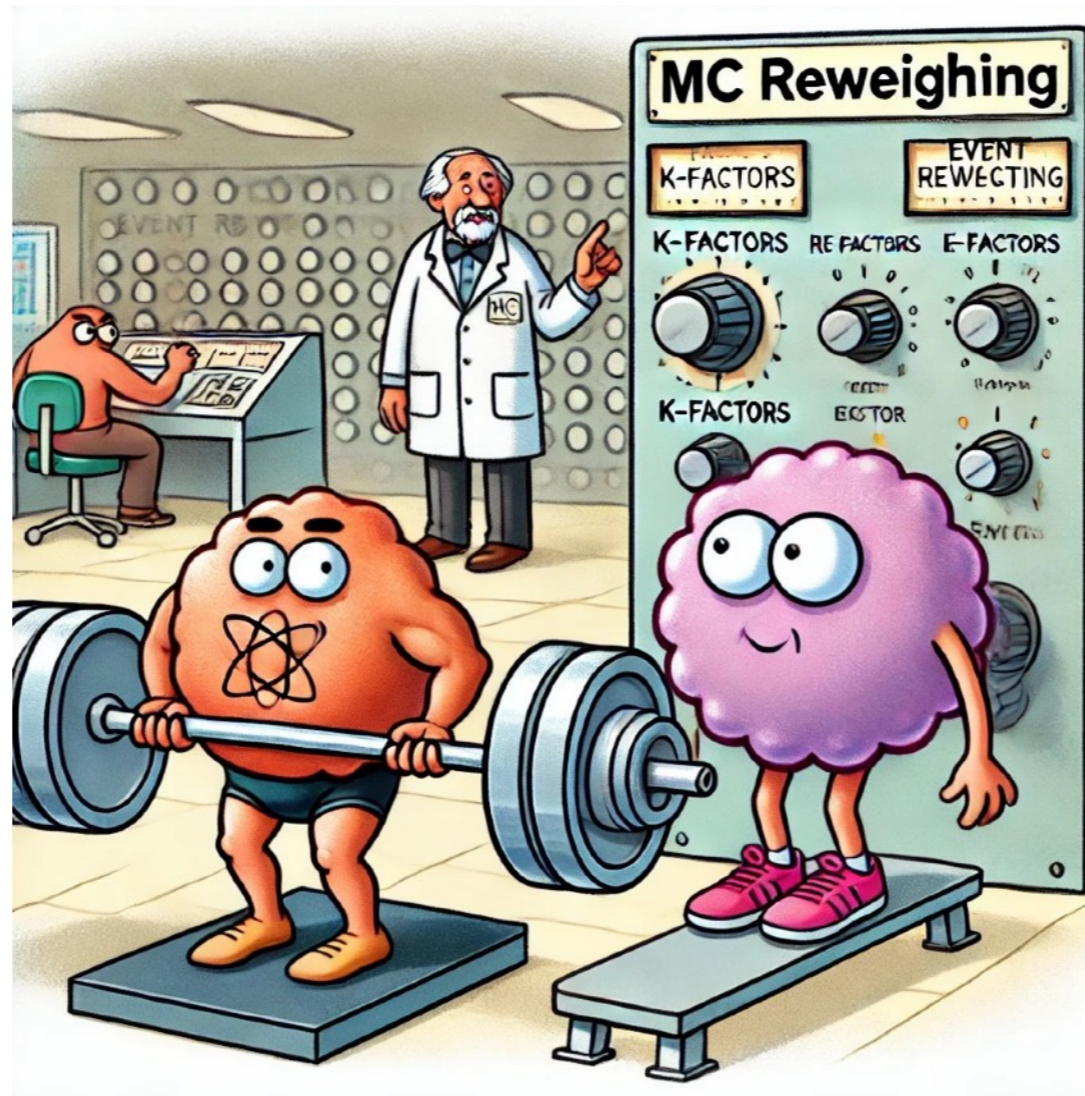


# IMPERIAL

## Di-Higgs reweighing tutorial



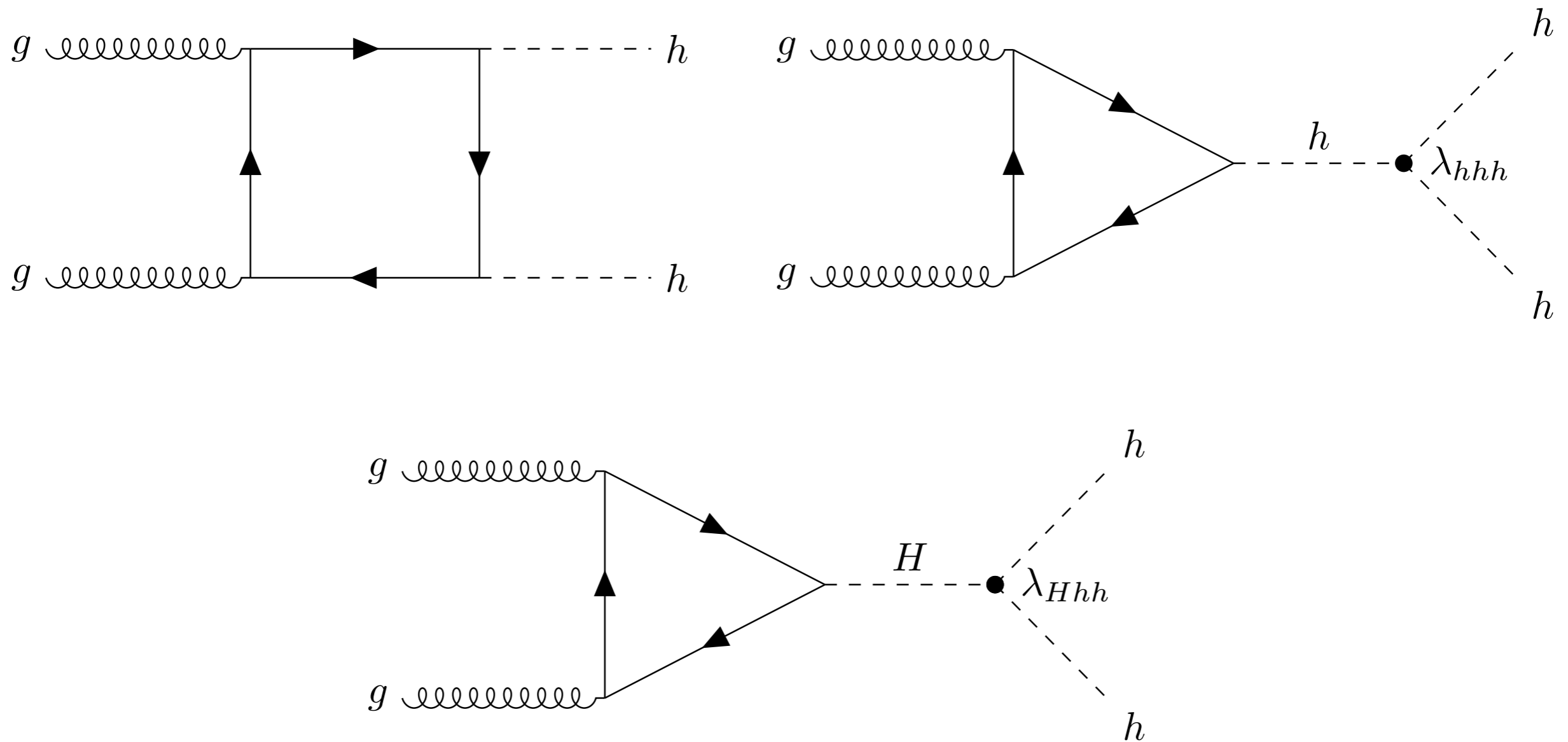
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LHC WG4 meeting March 12  
[d.winterbottom15@imperial.ac.uk](mailto:d.winterbottom15@imperial.ac.uk)

# Overview

- The material shown today based on the paper “**Interference effects in resonant di-Higgs production at the LHC in the Higgs singlet extension**”, in collaboration with F. Feuerstake, E. Fuchs, and T. Robens
  - [arXiv:2409.06651](https://arxiv.org/abs/2409.06651)
- Today I will focus on the method we used for reweighing di-Higgs events to account for interference effects between resonant and non-resonant di-Higgs processes
- If there is time I will also show how to generate di-Higgs nonresonant and resonant MC events using Madgraph
- These slides will give a quick introduction then we will move to Google Colab notebooks

# di-Higgs production at the LHC

- Dominant diagrams contributing to di-Higgs spectrum
- Interference between diagrams as well!



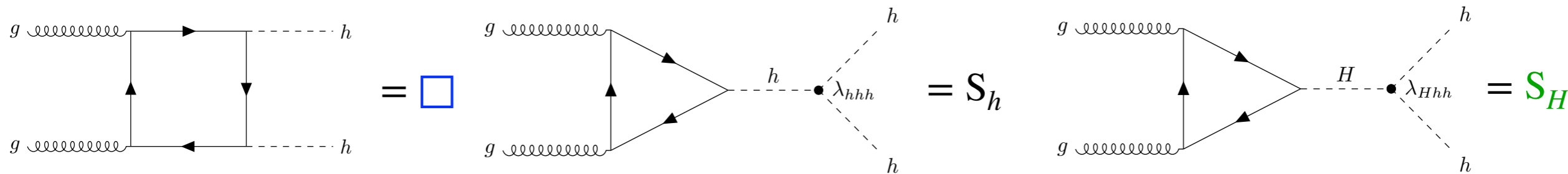
# ME reweighing method

- ME reweighing reweighs events using:

$$w = \frac{|\mathcal{M}_{\text{target}}|^2}{|\mathcal{M}_{\text{ref}}|^2}$$

- $\mathcal{M}_{\text{ref}}$  is ME for the MC you are reweighing and  $\mathcal{M}_{\text{target}}$  is the ME for the process/parameters you want to model
  - $\mathcal{M}_{\text{target}}$  in general model dependent, many options for process and parameters
  - In our method we decompose  $\mathcal{M}_{\text{target}}$  into minimal set of contributions that can scaled and combined to obtain distributions in any model
- Matrix elements computed using MadGraph with TRSM ([A Papaefstathiou, T Robens and G Tetlalmatzi-Xolocotzi JHEP05\(2021\)193](#))

# Decomposing the ME

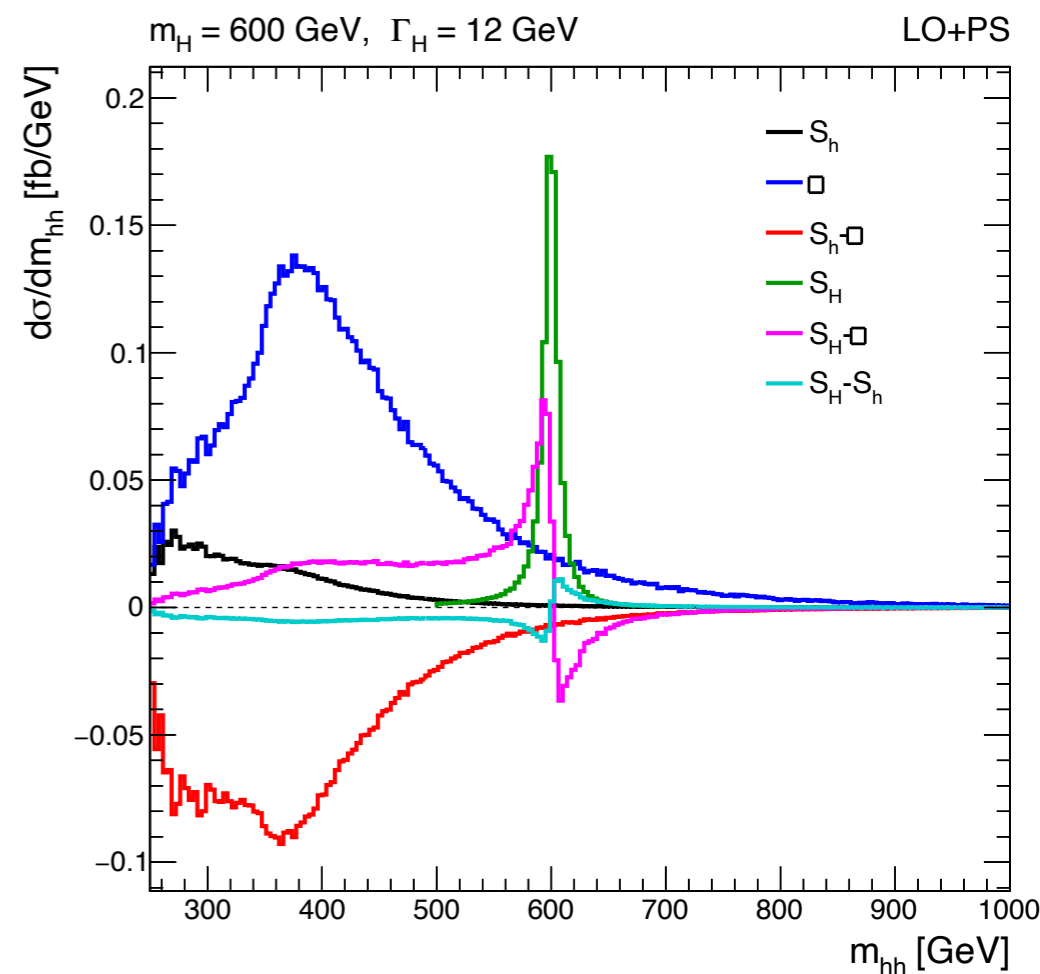


Parameterise using:  $\lambda_{hhh}, \lambda_{Hhh}, y_q^h, y_q^H, \Gamma_H, m_H$  ( $\kappa_p = p/p_{\text{SM}}$ )

$$\begin{aligned}
 |\mathcal{M}_{\text{total}}|^2 &= \mathcal{M}_{\square}^2 \cdot (\kappa_q^h)^4 \\
 &+ \mathcal{M}_{S_h}^2 \cdot (\kappa_q^h)^2 \kappa_{\lambda_{hhh}}^2 \\
 &+ \mathcal{M}_{S_H}^2(m_H, \Gamma_H) \cdot (\kappa_q^H)^2 \kappa_{\lambda_{Hhh}}^2
 \end{aligned}$$

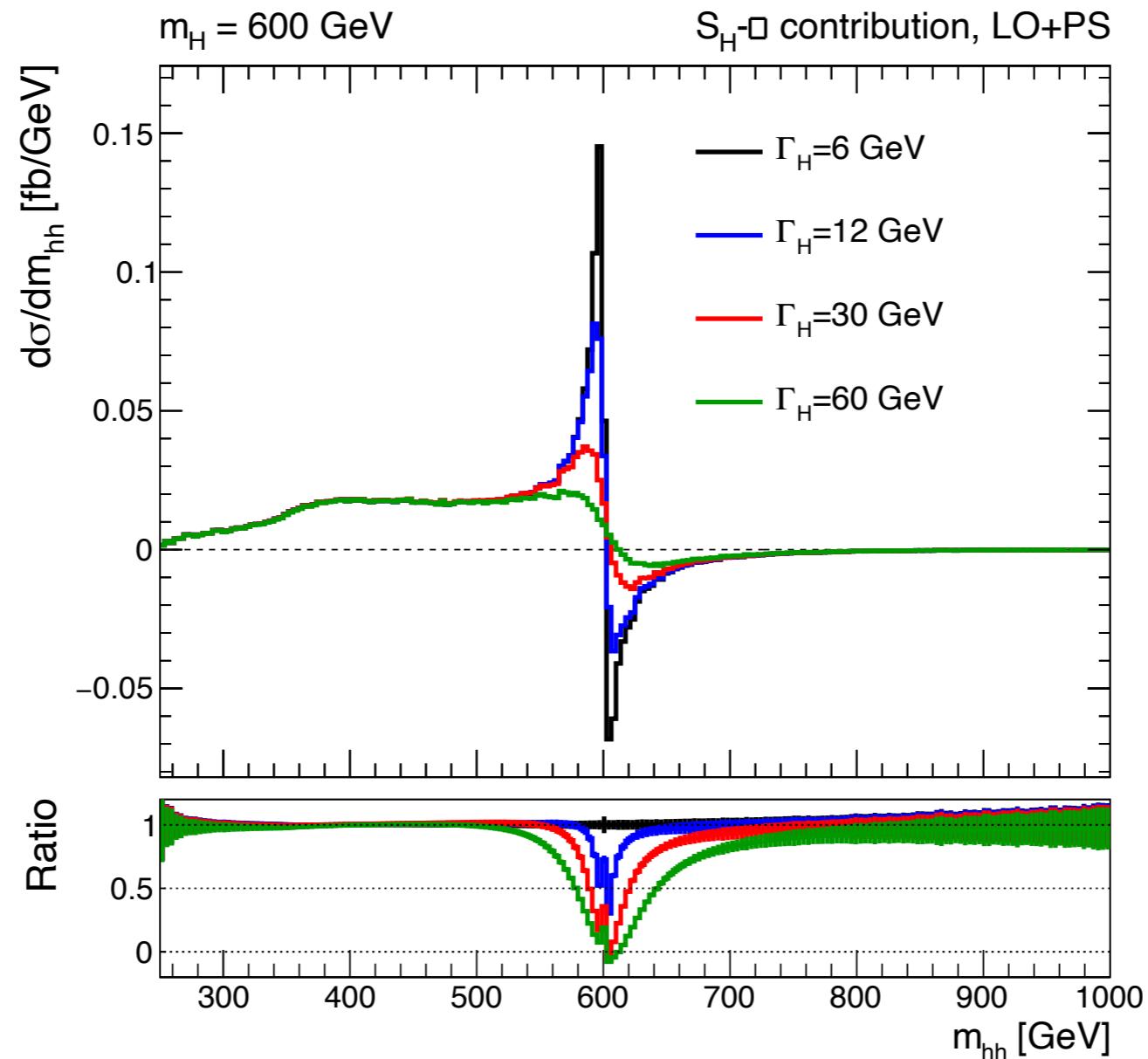
$$\begin{aligned}
 &+ \widetilde{\mathcal{M}}_{S_h-\square}^2 \cdot (\kappa_q^h)^3 \kappa_{\lambda_{hhh}} \\
 &+ \widetilde{\mathcal{M}}_{S_H-\square}^2(m_H, \Gamma_H) \cdot (\kappa_q^h)^2 \kappa_q^H \kappa_{\lambda_{Hhh}} \\
 &+ \widetilde{\mathcal{M}}_{S_H-S_h}^2(m_H, \Gamma_H) \cdot \kappa_q^h \kappa_q^H \kappa_{\lambda_{hhh}} \kappa_{\lambda_{Hhh}},
 \end{aligned}$$

**Interference terms!**



# Dependence on the width

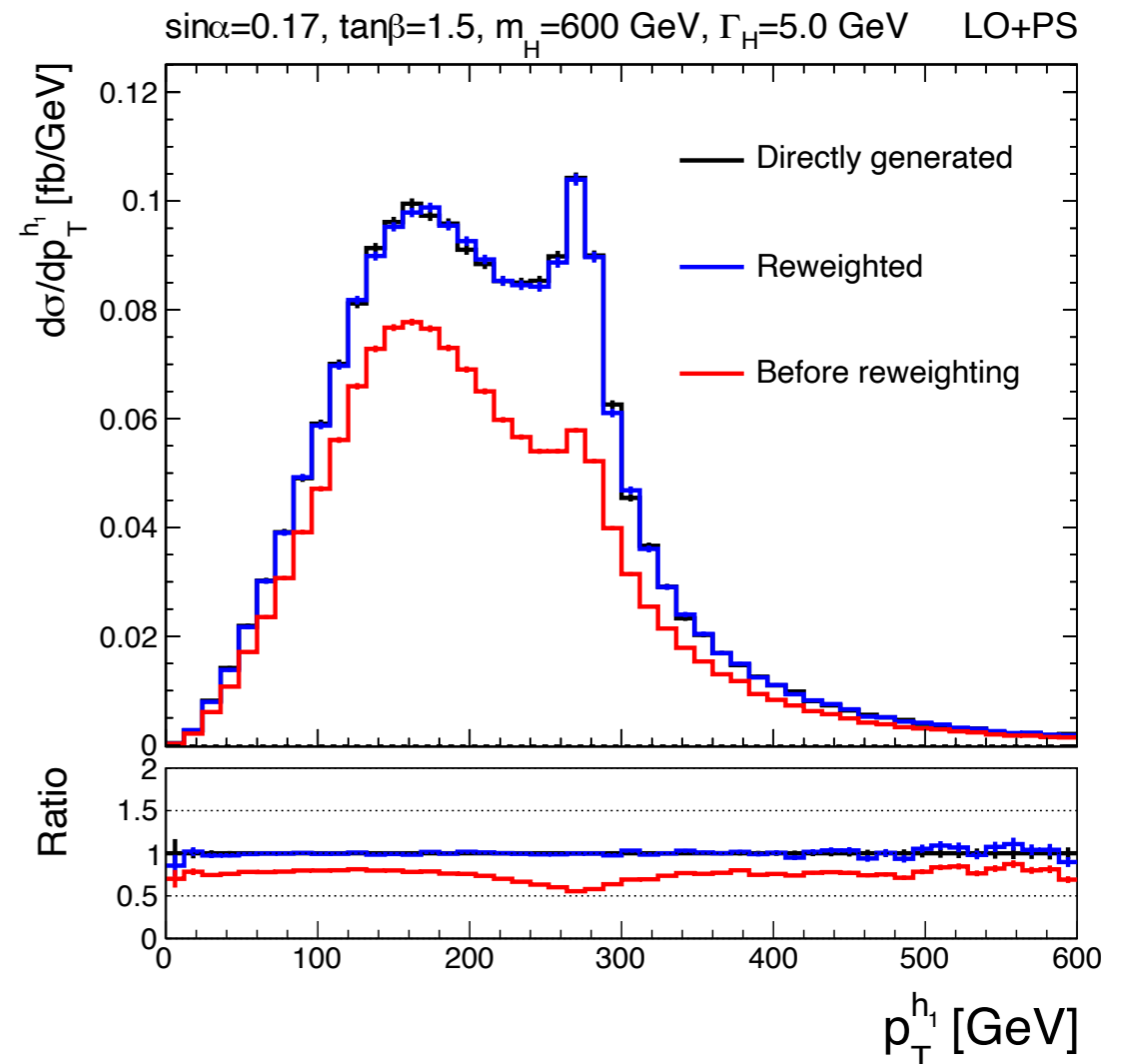
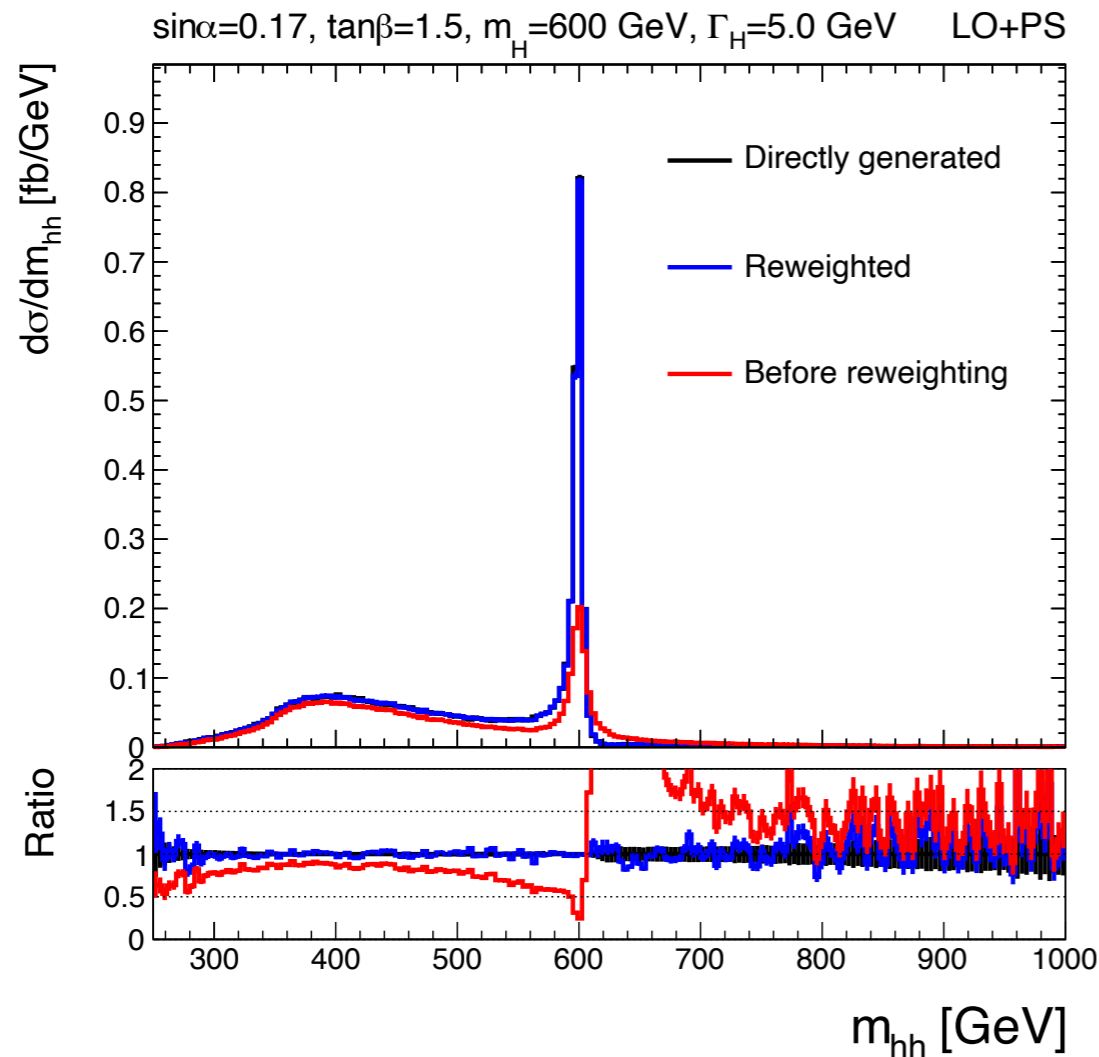
- $S_H$ ,  $\square - S_H$ , and  $S_H - S_h$  depend on the mass and the width of the H



- With ME reweighting you need to make sure your chosen reference sample is populated in all phase-space regions where  $\mathcal{M}_{\text{target}}$  is non-vanishing
- For the  $\square$ ,  $S_h$ ,  $\square - S_h$ ,  $\square - S_H$ , and  $S_H - S_h$  contributions we use a SM di-Higgs sample (non-resonant only)
- For  $S_H$  we use a MC samples of the same  $m_H$  and a width not too far from the target ( $\sim 0.5\text{--}2 \times \text{target } \Gamma_H$ )

# Validating the reweighting method

- Applying reweighting to LO MC samples give ~perfect agreement with samples generated for a set of model points!



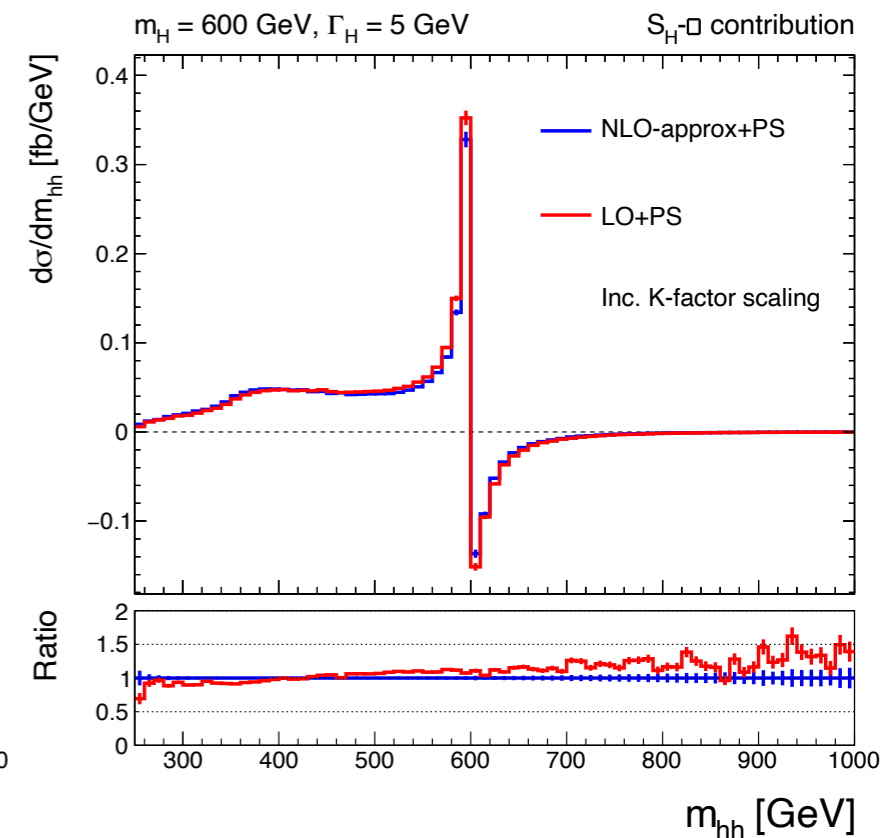
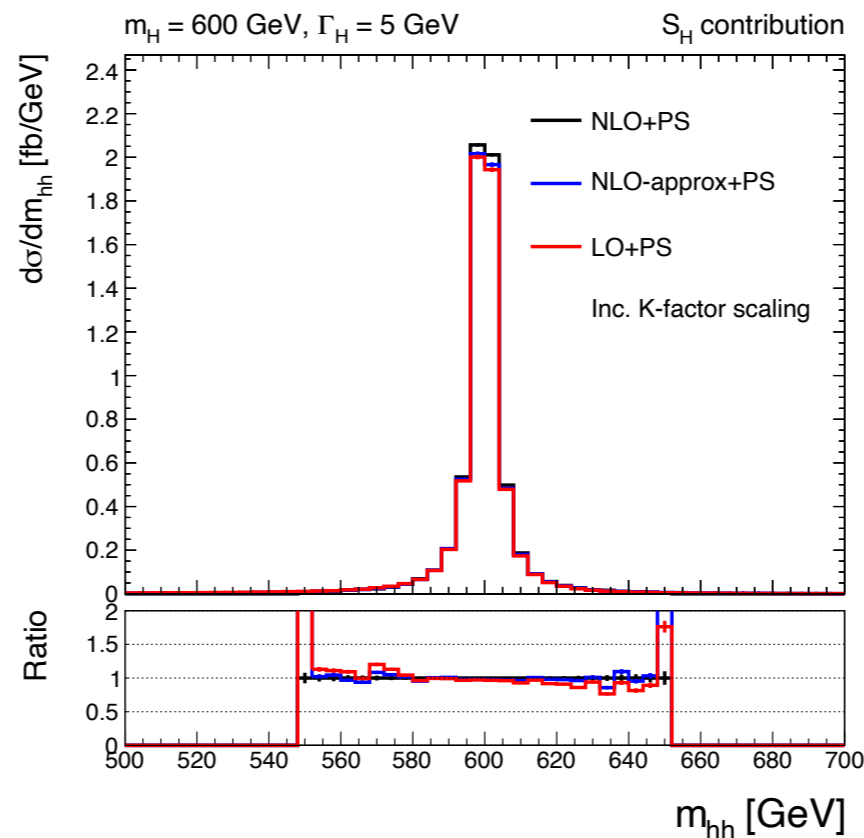
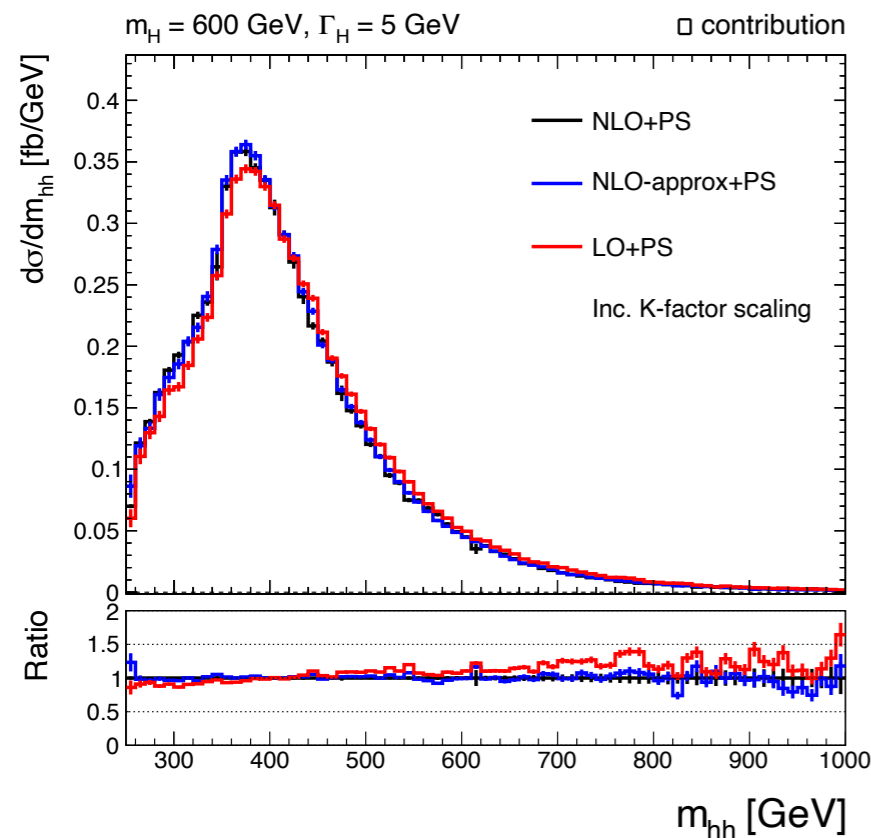


- Now lets move to some examples in Google Colab
- Example using reweighing tool: <https://colab.research.google.com/drive/1kqu-9ouFCXNKJFB8dC0OHUdpsk1BxtiR?usp=sharing>
- Example generating MC using Madgraph: [https://colab.research.google.com/drive/1SGzp8BiuV9XGM\\_9QKUOLrsar3-LYvN4-?usp=sharing](https://colab.research.google.com/drive/1SGzp8BiuV9XGM_9QKUOLrsar3-LYvN4-?usp=sharing)
- Reweighing tool available on Gitlab: <https://gitlab.com/danielwinterbottom/HHReweigher>

# Backup

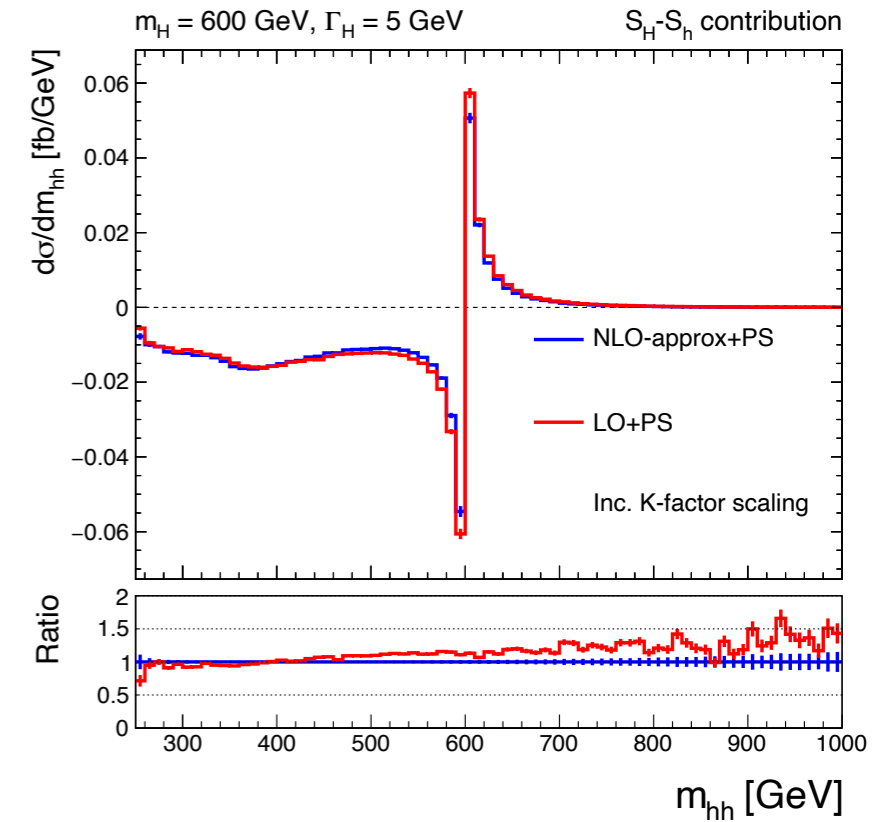
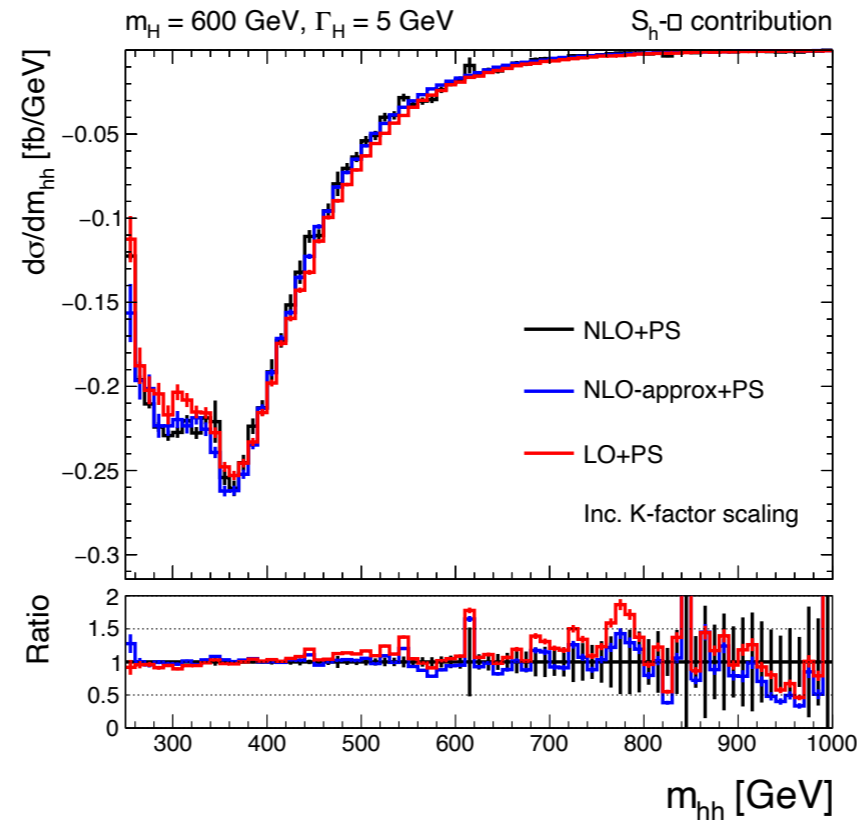
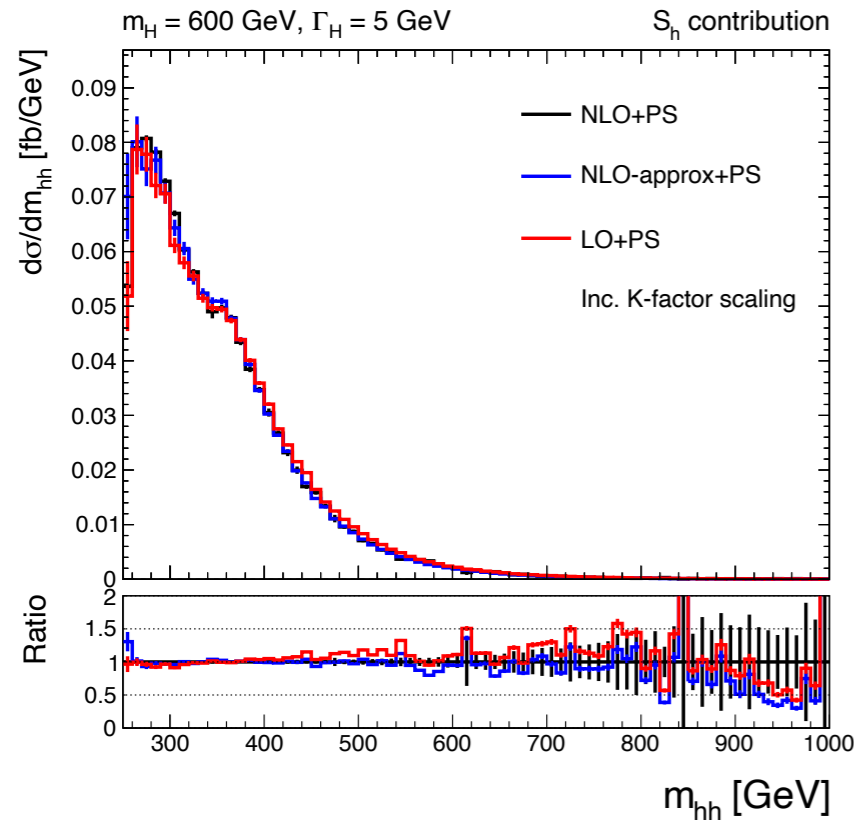
# Including higher order corrections

- Define approximate-method for reweighting NLO samples
  - Ignore additional radiation and compute MEs at LO
- NLO samples generated using POWHEG
  - No model currently available that can generate nonresonant+resonant di-Higgs with interference
  - We generate  $\square$ ,  $S_h$ ,  $\square - S_h$  for non-resonant, and  $S_H$  resonant samples and compare to reweighting where possible
  - We can also use reweighting to obtain approximate  $\square - S_H$ , and  $S_H - S_h$  predictions - agree well with LO, to be checked once proper NLO MC is available



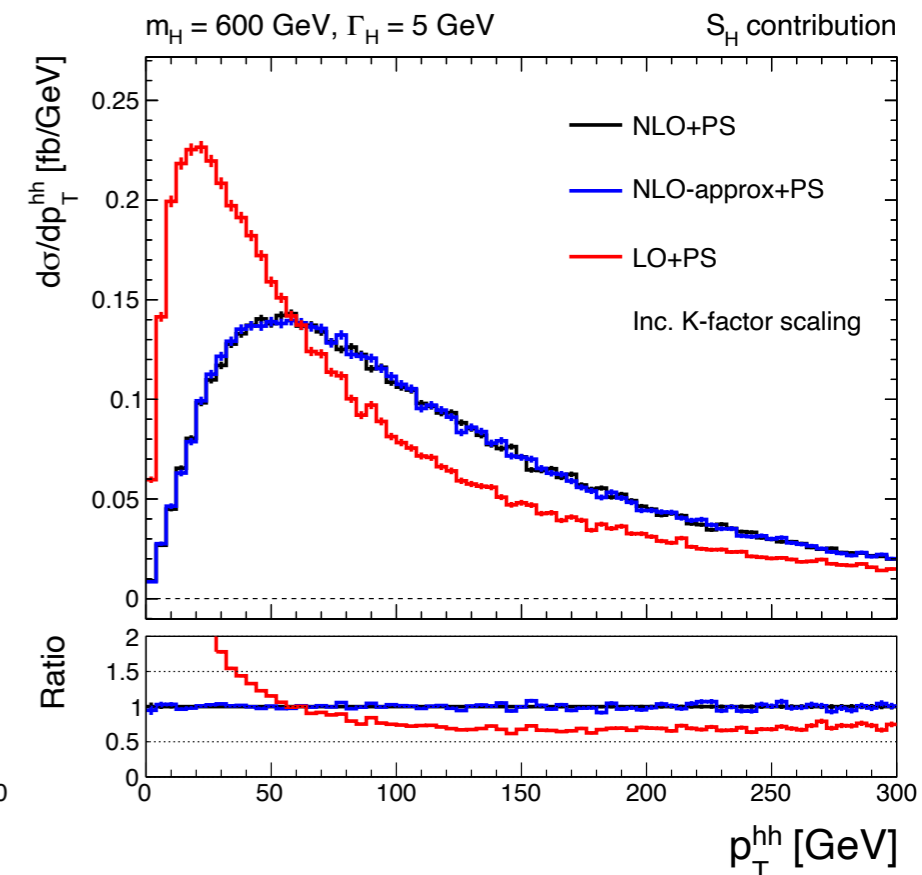
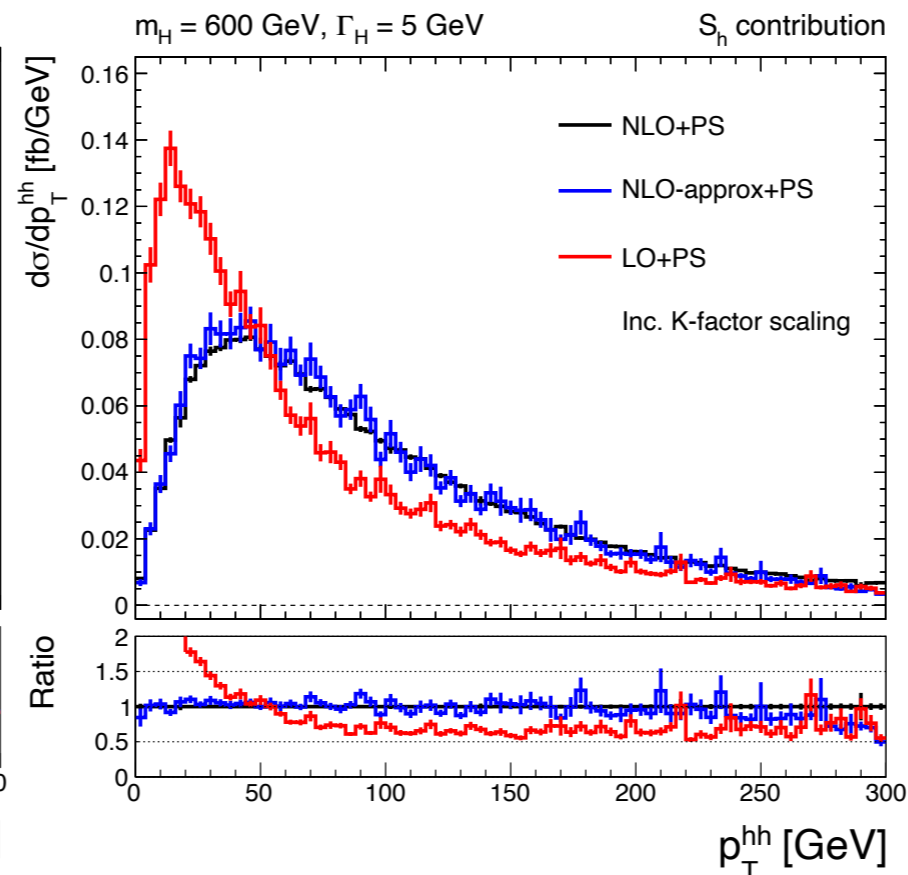
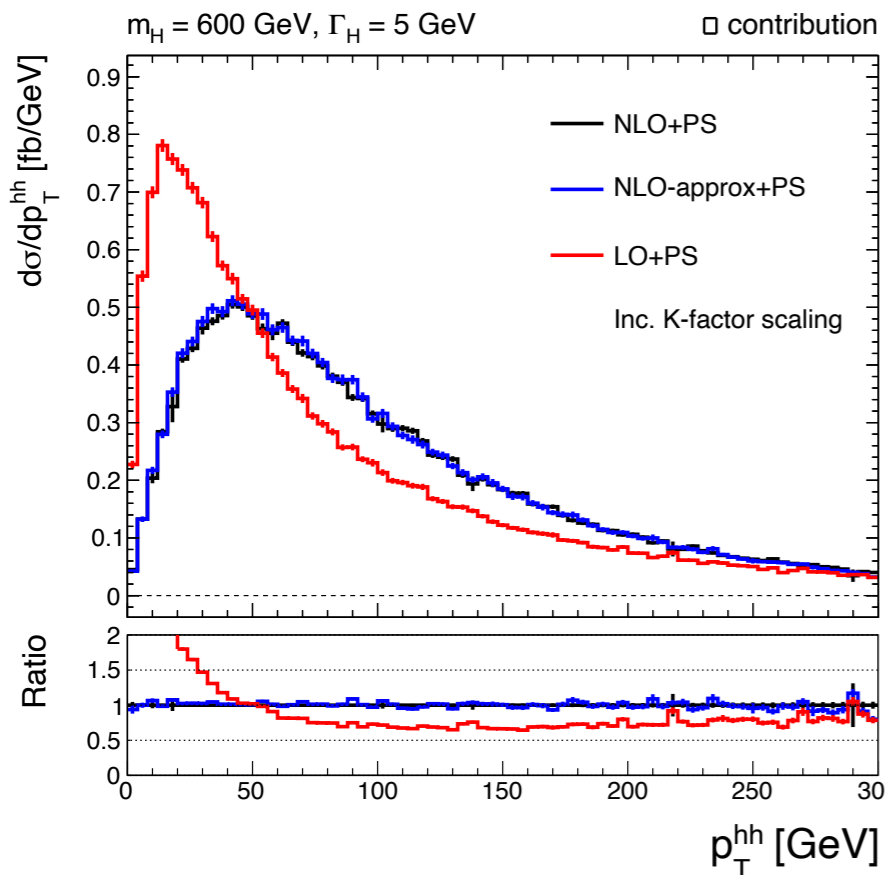
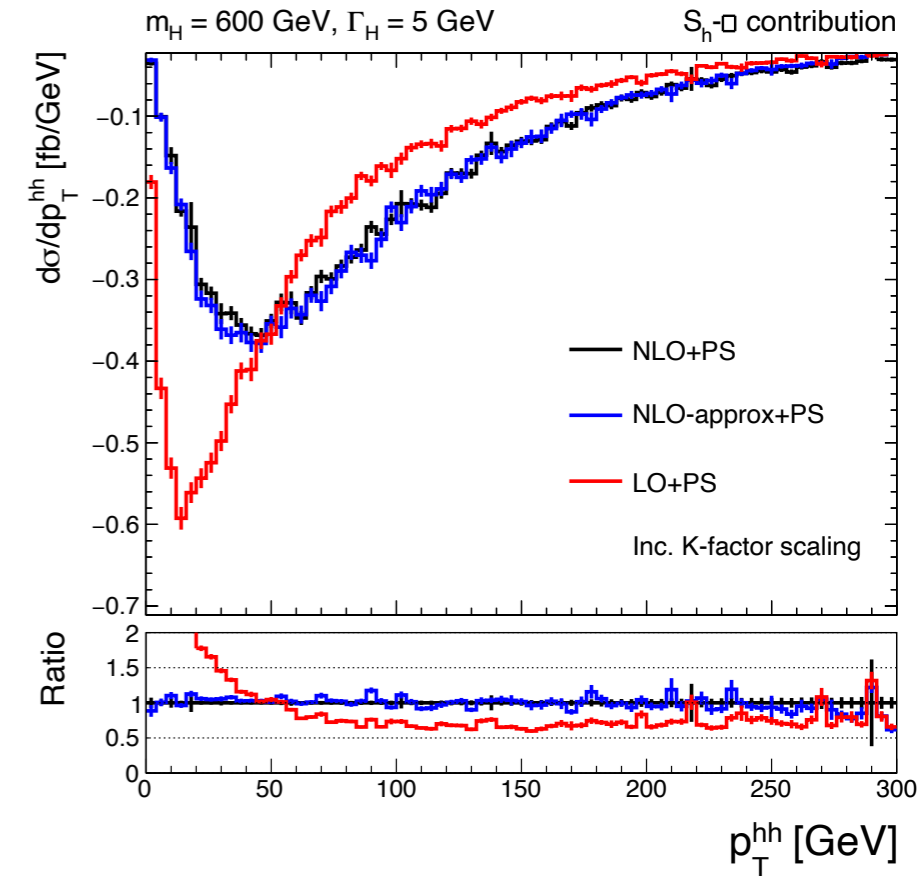
# Additional plots of NLO validations

- Plots of di-Higgs mass for other terms



# Additional plots of NLO validations

- Plots of di-Higgs  $p_T$



# More details on approximate NLO reweighting

When reweighting NLO samples we “ignore” the additional radiation if there is any as follows:

- We take the two outgoing  $h$  four-momenta from the ME and boost to the di-Higgs rest frame
- We then obtain the four-momenta for the incoming gluons by requiring both gluons to have zero transverse momentum, and equal and opposite longitudinal momentum, also requiring four-momentum conservation between incoming and outgoing particles
- When estimating the MEs we also average over all possible spin-states of the incoming gluons
- If there is no radiation, then we compute ME in the usual way as if the event is from a LO generator

# The Higgs singlet model

- Simplest extension of the Standard model (SM) that can provide resonance-enhanced di-Higgs production = Higgs singlet model with softly broken  $\mathbb{Z}_2$  symmetry
- Potential:  $V(\Phi, S) = -m^2\Phi^\dagger\Phi - \mu^2S^2 + \lambda_1(\Phi^\dagger\Phi)^2 + \lambda_2S^4 + \lambda_3\Phi^\dagger\Phi S^2$
- 5 free parameters
  - 2 of them fixed by experiments:  $v$  and  $m_h=125$  GeV
  - 3 remaining parameters chosen as:  $m_H, \sin\alpha, \tan\beta = v/v_S$
  - $\alpha$  is mixing angle that rotates gauge into mass eigenstates, define  $m_H > m_h$
- SM-like  $h$  couplings to fermions and weak gauge bosons modified by  $\cos\alpha$
- Heavy Higgs  $H$  behaves like SM-Higgs with couplings to fermions and gauge bosons scaled by  $\sin\alpha$ , with additional decay channel (if  $m_H > 2m_h$ ):  $H \rightarrow hh$

- Coupling modifiers (wrt SM couplings) in the singlet model

$$\kappa_{f/V}^h = \cos \alpha,$$

$$\kappa_{f/V}^H = \sin \alpha,$$

$$\kappa_{\lambda_{hhh}} = \cos^3 \alpha - \tan \beta \sin^3 \alpha,$$

$$\kappa_{\lambda_{Hhh}} = \frac{2m_h^2 + m_H^2}{m_h^2} \frac{\sin(2\alpha)}{2} (\cos \alpha + \tan \beta \sin \alpha),$$

$$\Gamma_H = \sin^2 \alpha \Gamma_{\text{SM}}(m_H) + \frac{\kappa_{\lambda_{Hhh}}^2 \sqrt{1 - 4m_h^2/m_H^2}}{8\pi m_H}$$