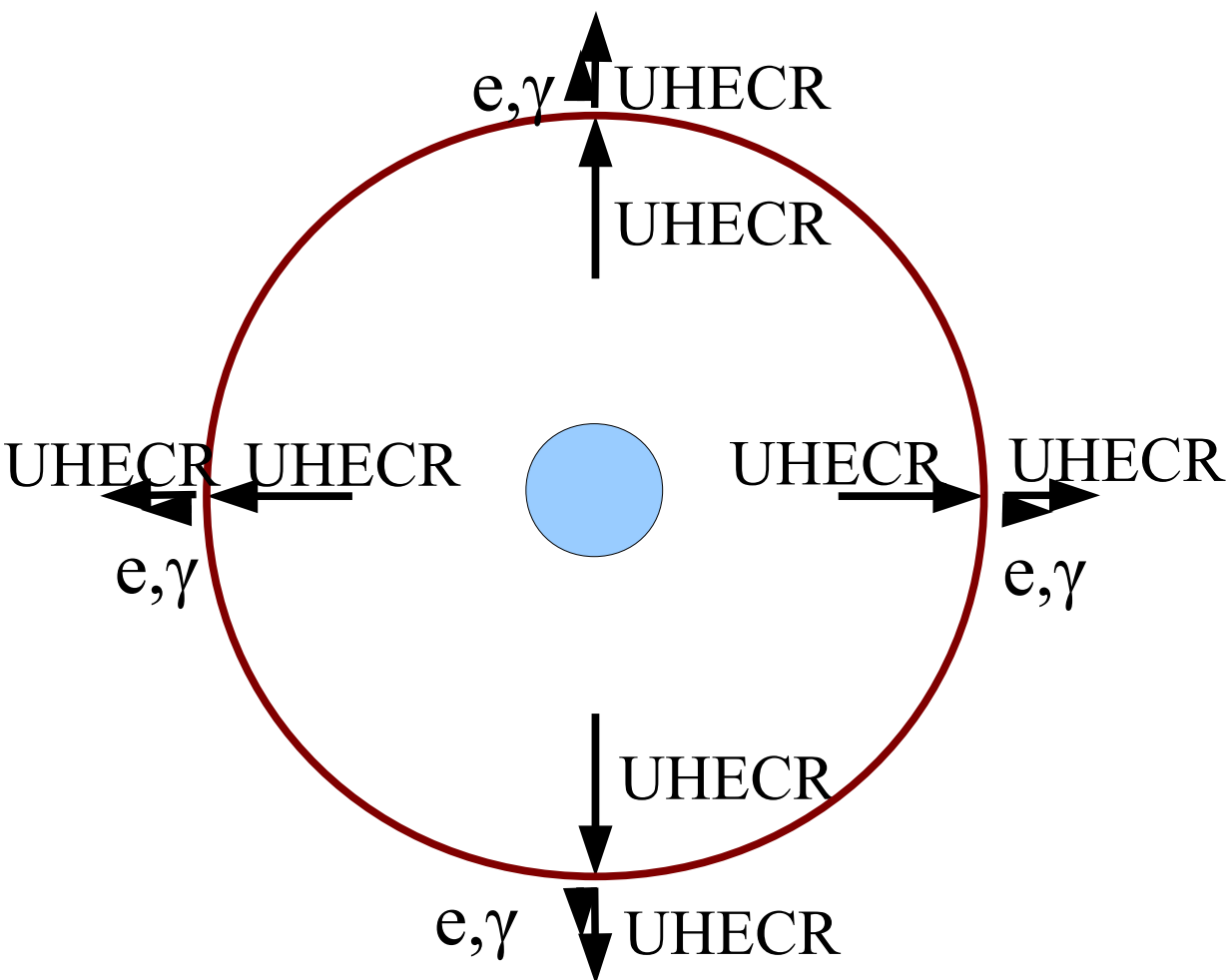


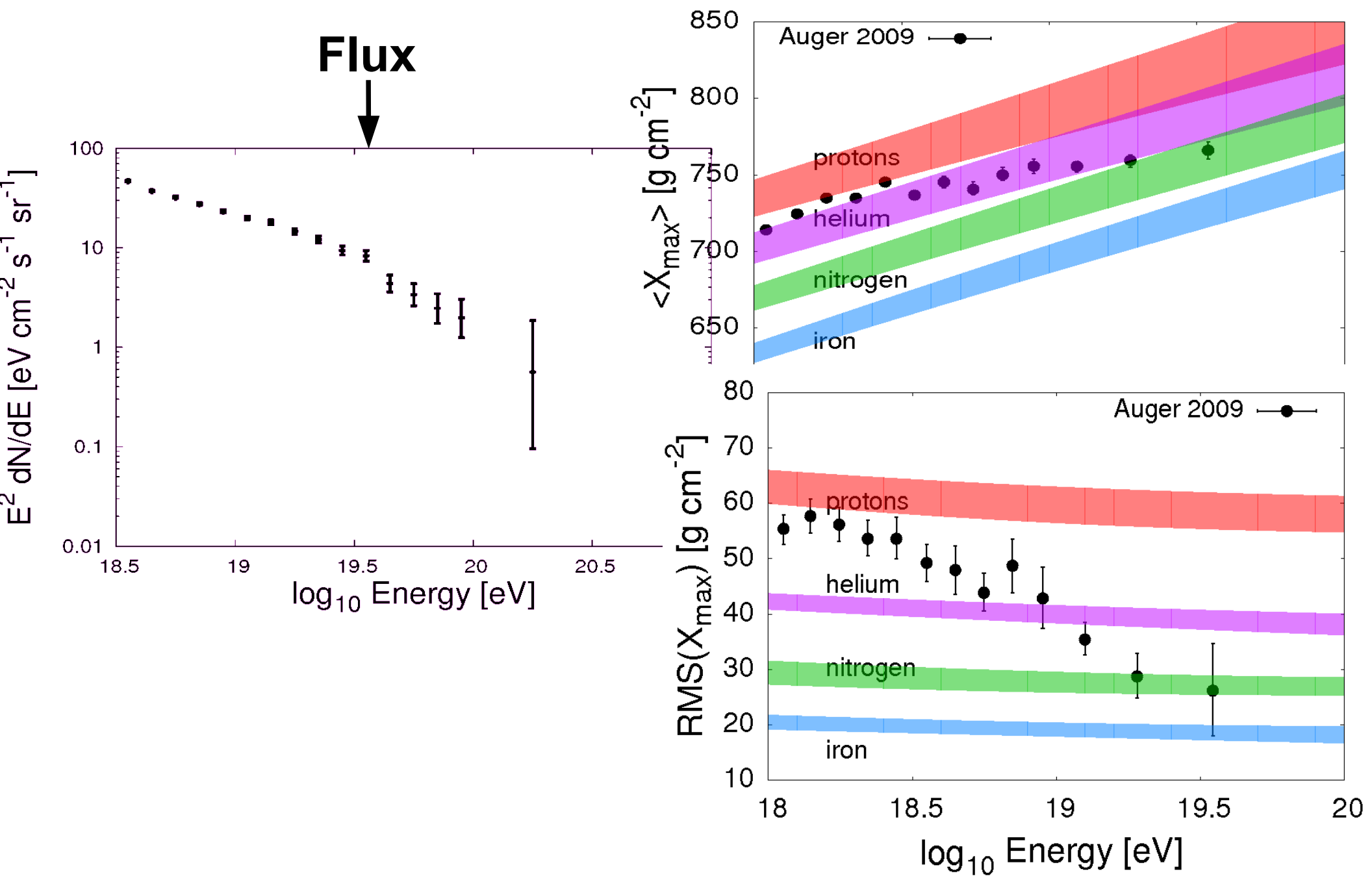
The Need For Hard Spectra Sources of Nearby Heavy Cosmic Rays



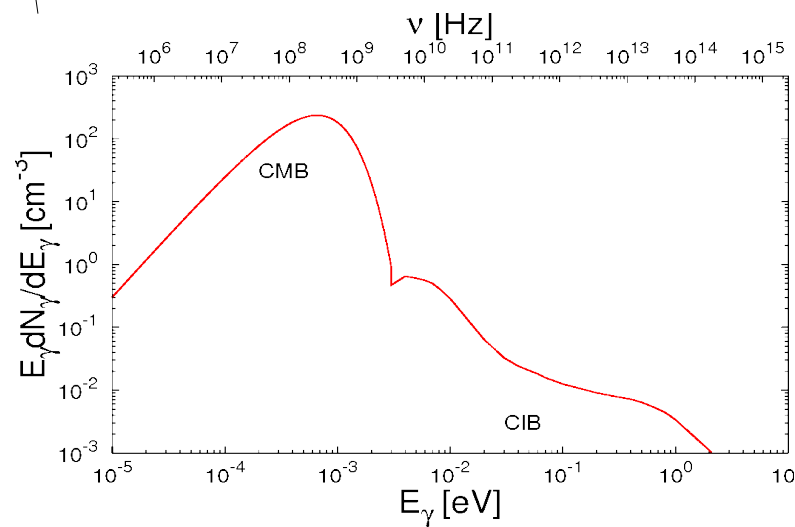
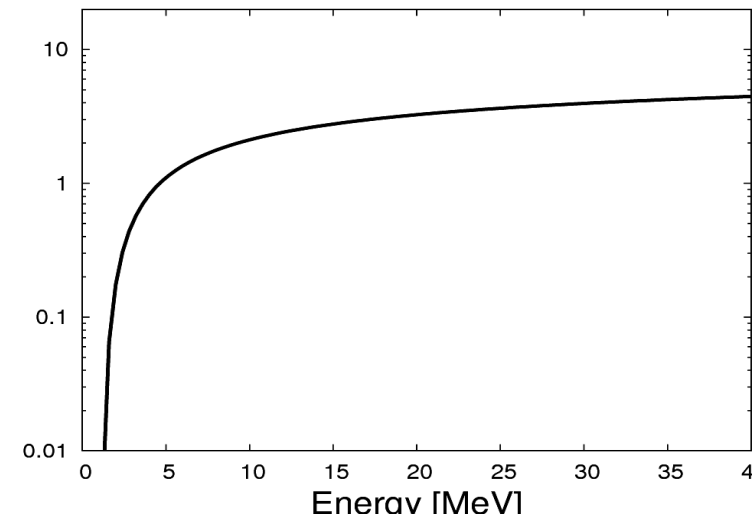
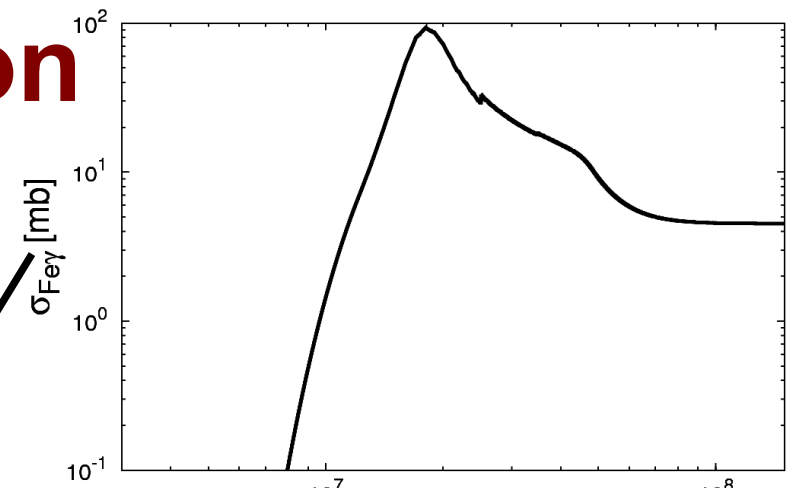
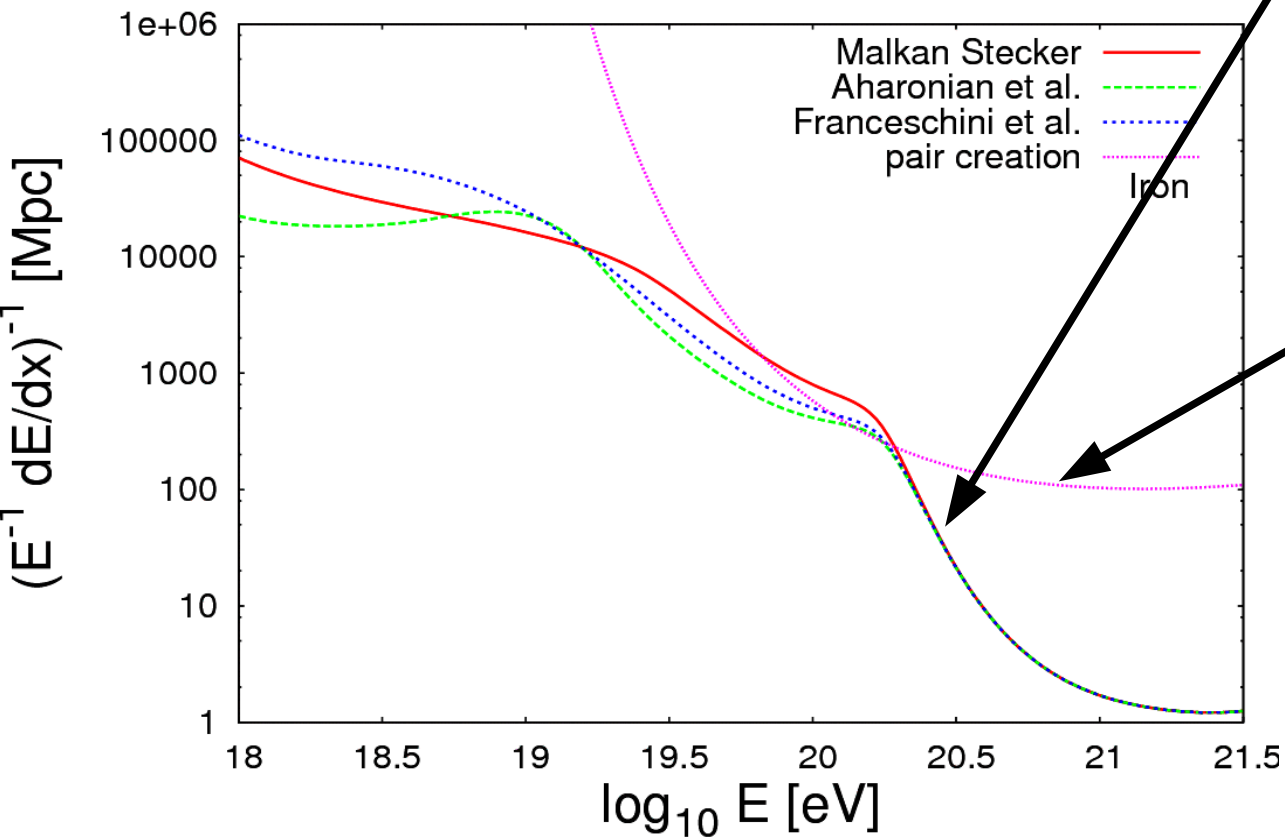
1) What source injection spectra + composition is consistent with Auger results?

2) What constraints do these fits place on the local source distribution?

Reminder- The Composition that Arrives at Earth



UHECR Nuclei Propagation From Source to Earth



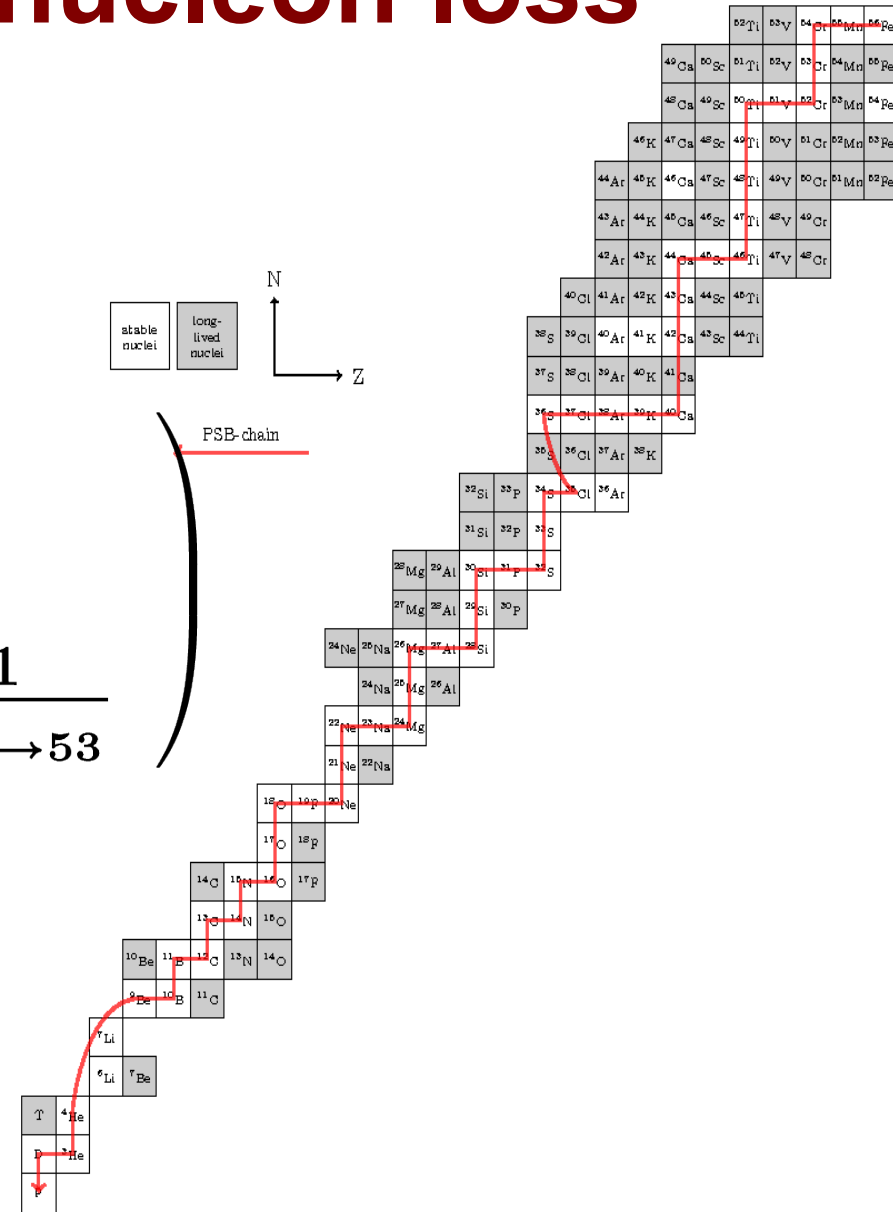
1st Order: Cascade of Nuclei Through Species- single nucleon loss

$$\frac{d}{dt} \begin{pmatrix} f_{56} \\ f_{55} \\ f_{54} \end{pmatrix} = \Lambda \begin{pmatrix} f_{56} \\ f_{55} \\ f_{54} \end{pmatrix}$$

$$\Lambda = \begin{pmatrix} -\frac{1}{\tau_{56 \rightarrow 55}} & 0 & 0 \\ \frac{1}{\tau_{56 \rightarrow 55}} & -\frac{1}{\tau_{55 \rightarrow 54}} & 0 \\ 0 & \frac{1}{\tau_{55 \rightarrow 54}} & -\frac{1}{\tau_{54 \rightarrow 53}} \end{pmatrix}$$

Whose eigenvalues are

$$f_q = \sum_{n=q}^{56} \frac{\tau_q \tau_n^{56-q-1}}{\prod_{p=q}^{56} (\tau_n - \tau_p)} e^{-t/\tau_n}$$



Cascade of Nuclei Through Species- single nucleon loss

Since nuclei Lorentz factor remains
~conserved, and cross-section varies mildly
with A (nuclear mass)

$$\tau_{56 \rightarrow 55} \approx \tau_{55 \rightarrow 54} \dots$$

For the case $\tau_{56 \rightarrow 55} = \tau_{55 \rightarrow 54} \dots$

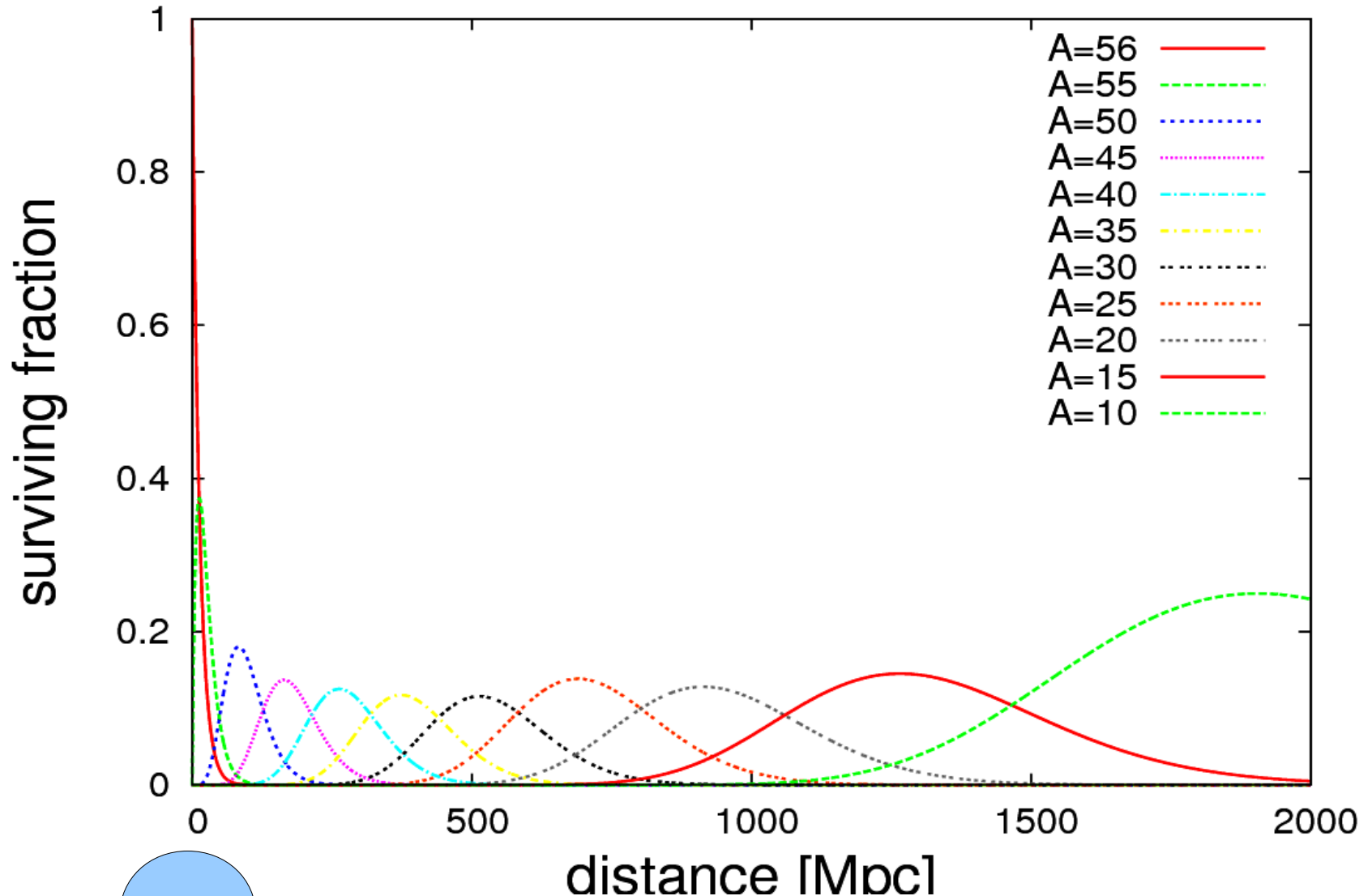
$$f_q = \frac{t^{(q_{max} - q)}}{\tau_q (q_{max} - q)!} e^{-t/\tau_q}$$

ie. Gaisser-Hillas
type function!

(used to describe air showers)

Nuclei Propagation Away from their Source + their Transmutation

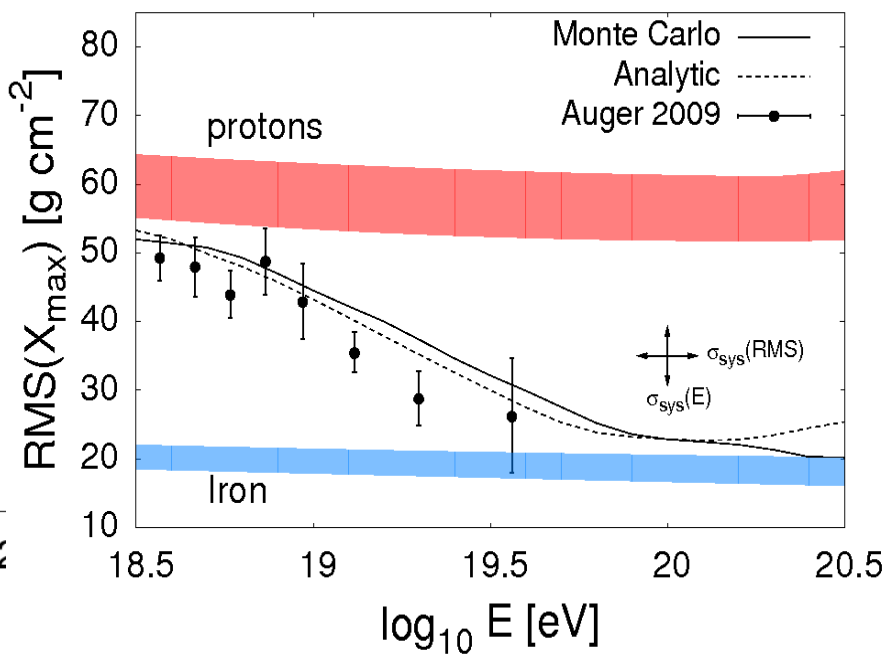
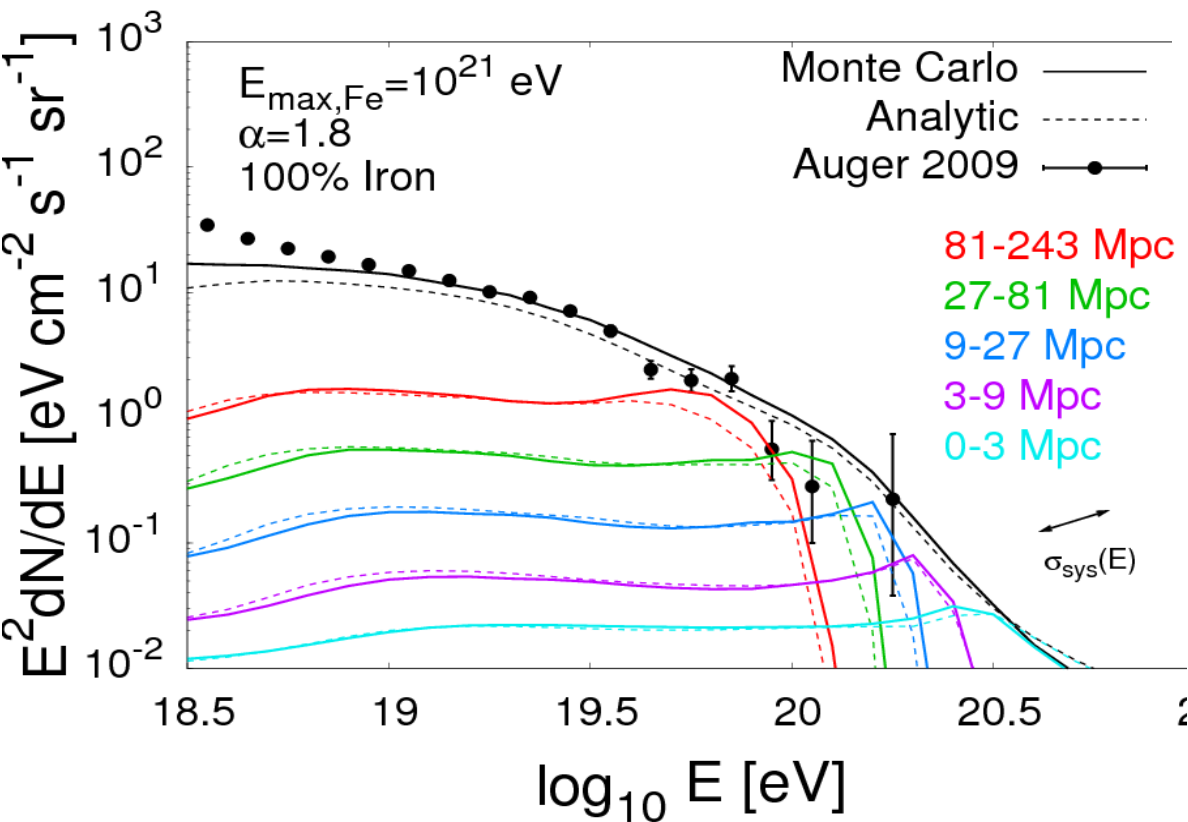
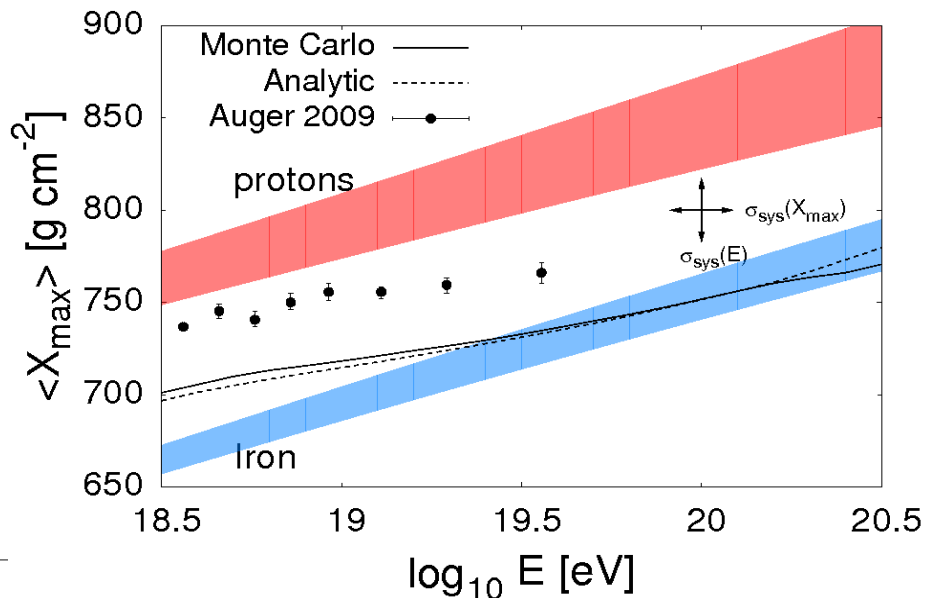
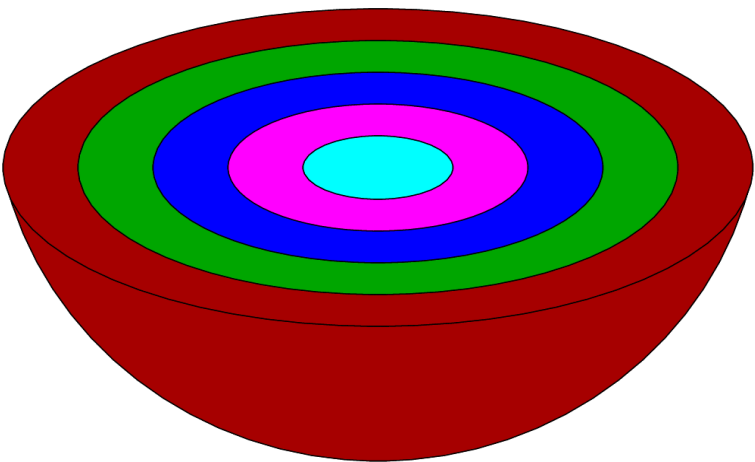
For 10^{20} eV Iron Nuclei at source-



Local Scales Effect Highest Energies

0 3 9 27 81 243 Mpc

(logarithmic scale)



What is the Source Composition?

Keep It Simple

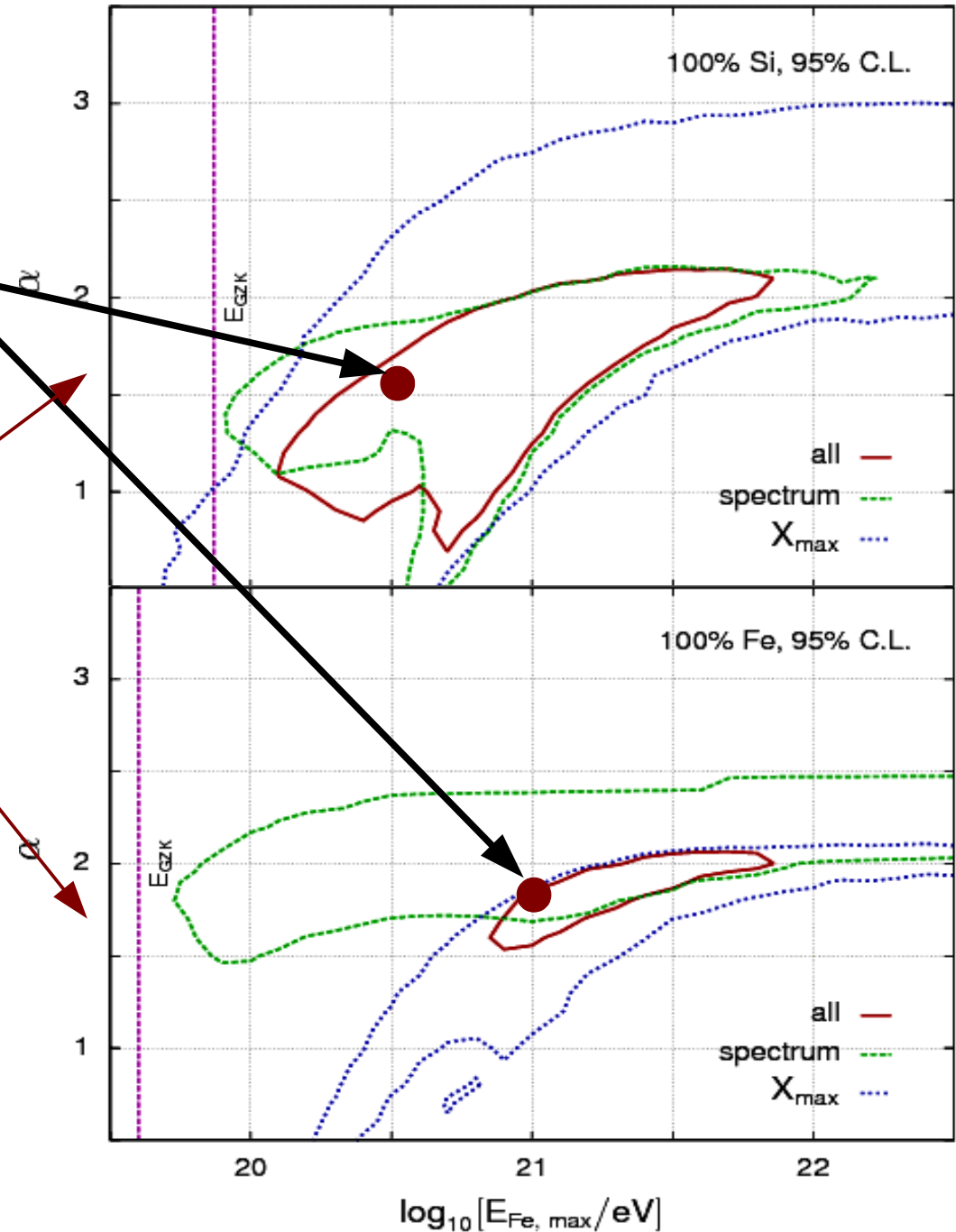
- **Single Composition**

Example Best-Fit Models

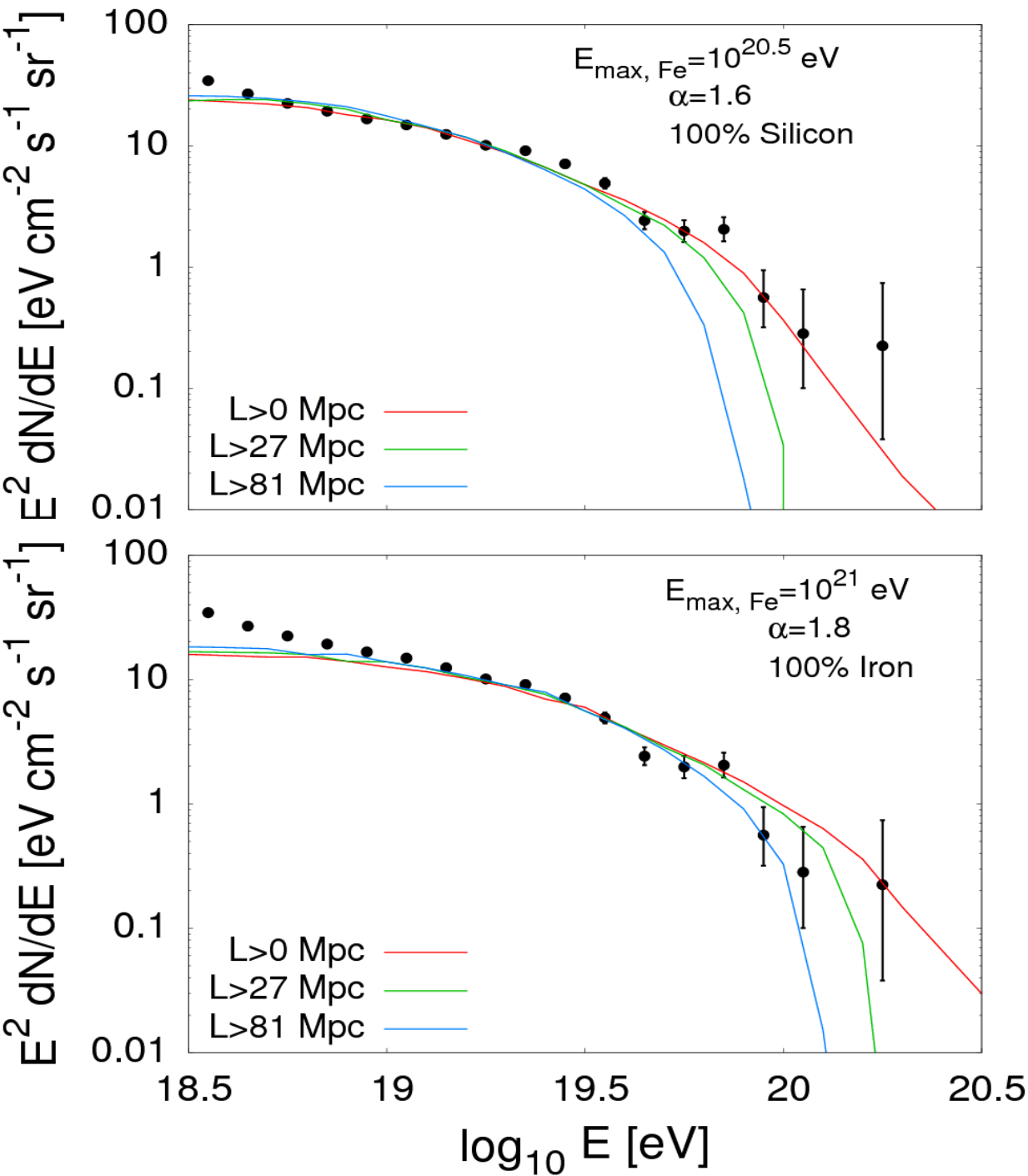
Silicon →

Hard Spectra preferred

Iron →



How Far is the Nearest Source?



$L > 0 \text{ Mpc}$

$L > 27 \text{ Mpc}$

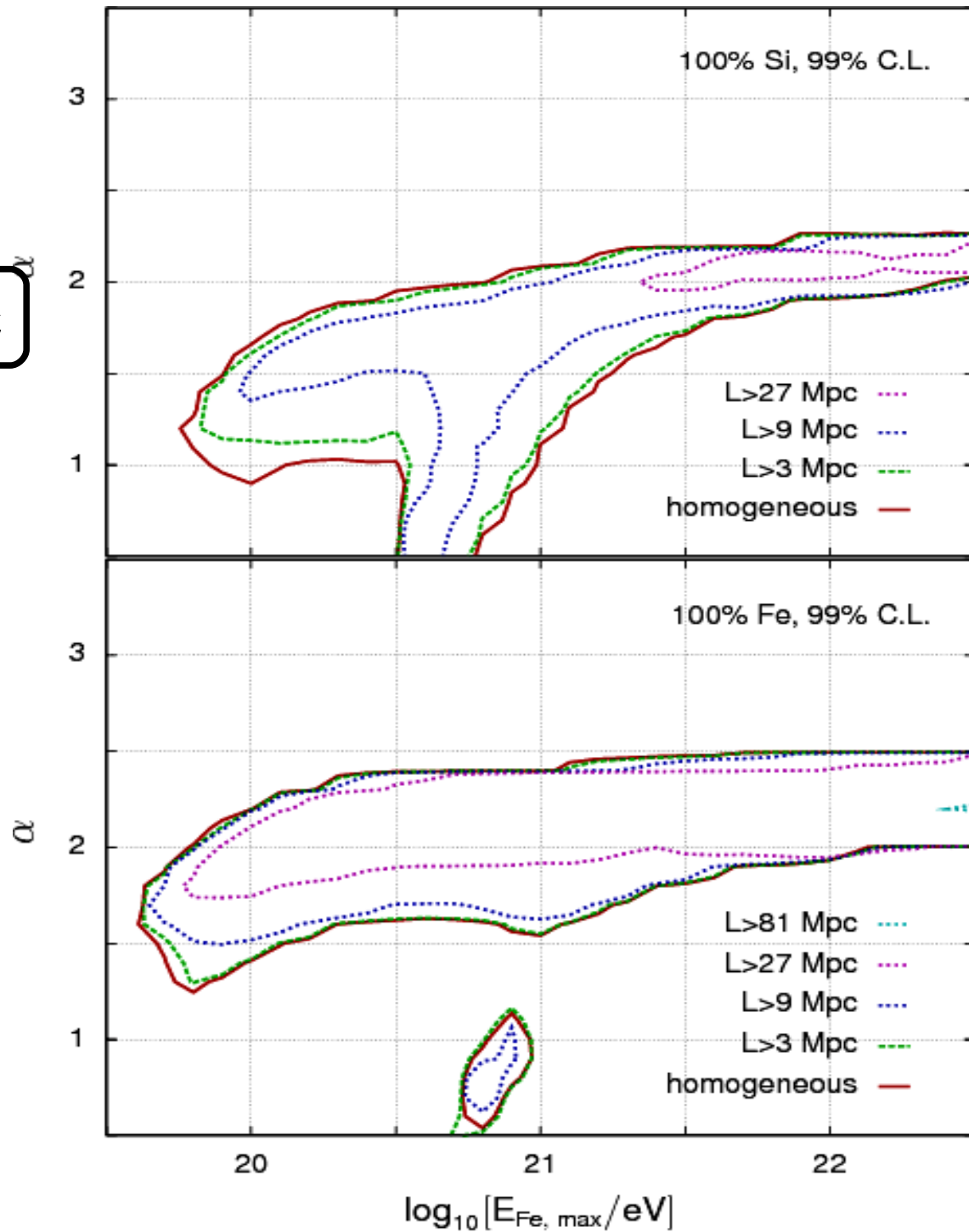
$L > 81 \text{ Mpc}$

How Far is the Nearest Source?

If $E_{\text{max}} < 10^{22} \text{ eV}$

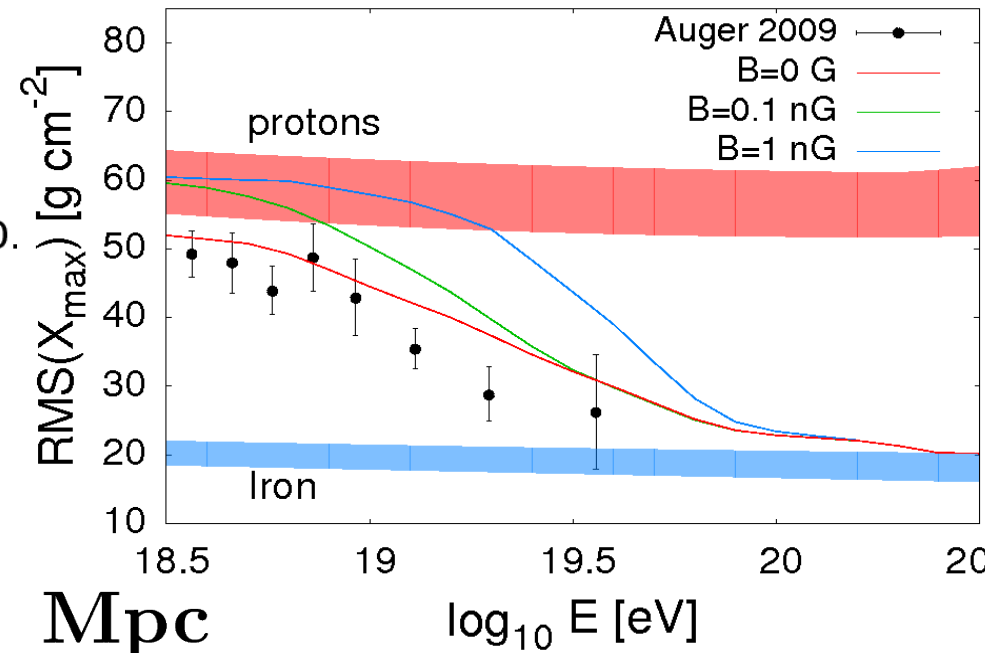
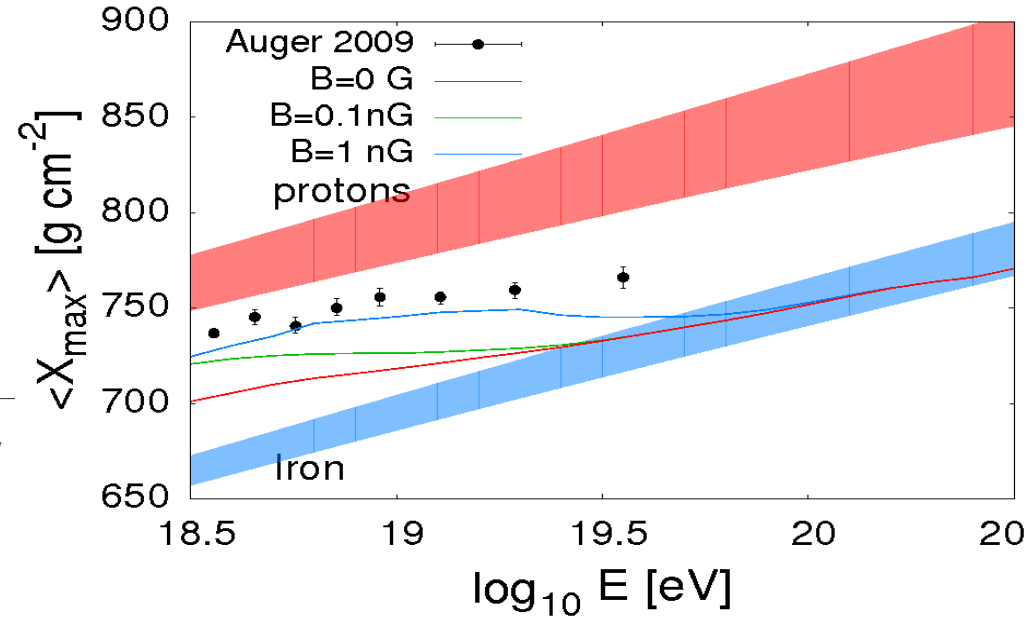
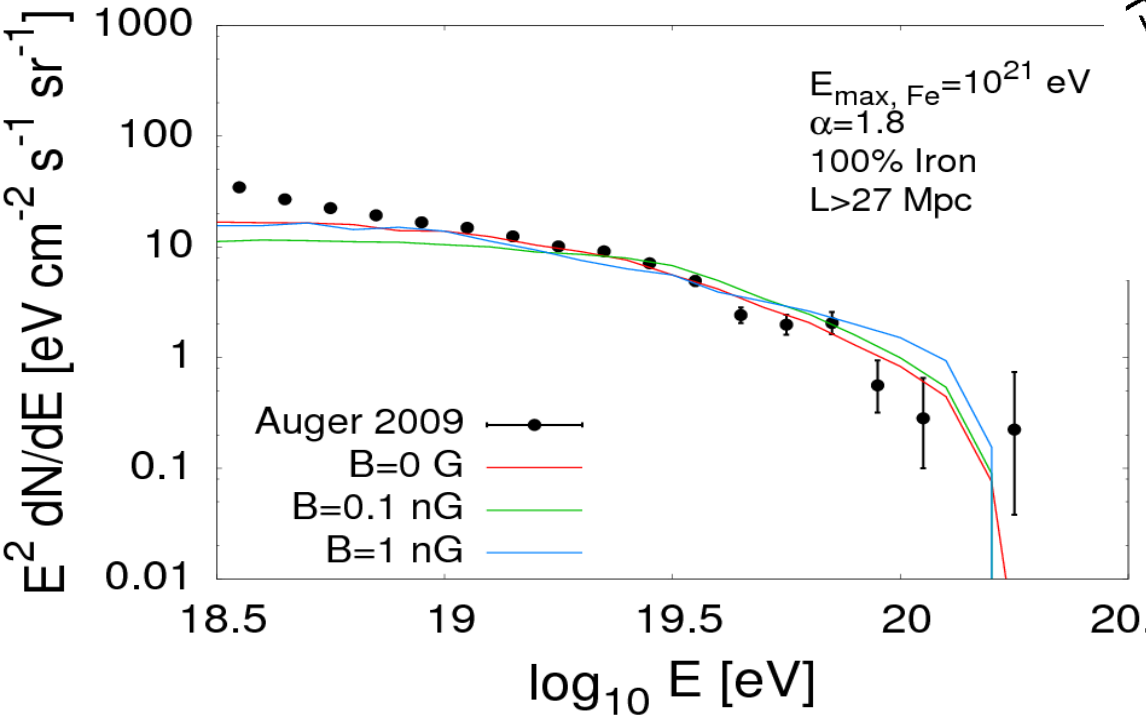
Silicon- $D < 60 \text{ Mpc}$

Iron- $D < 80 \text{ Mpc}$



Extragalactic Magnetic Fields

L > 27 Mpc



$$R_{\text{Larmor}} \approx 4 \left(\frac{E}{10^{20} \text{ eV}} \right) \left(\frac{\text{nG}}{B} \right) \left(\frac{26}{Z} \right) \text{ Mpc}$$

Conclusion

The dominance of nuclei at the high energies provides useful new information about the proximity of UHECR sources

Analytic calculations can be used to describe with reasonable accuracy the spectrum and the composition results

Agreement with both the spectral and composition information require that local sources exist which produce hard spectra