



Standard PMNS oscillations and physics beyond PMNS

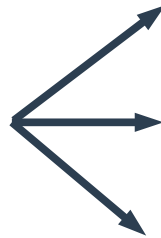
(a model builder point of view)

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Dipartimento di Matematica e Fisica, Roma Tre

Disclaimer

Going to present the point of view of a Model Builder



discussion about neutrino properties form oscillation data only

1. PMNS now and in the near future

2. some aspect of New Physics in the oscillation domain

What we know: flavor mixing

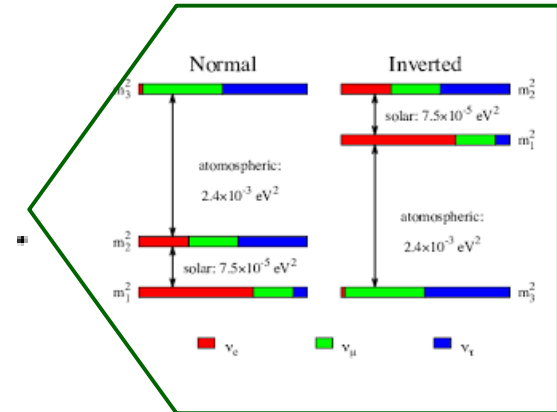
Standard Model states

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L, \quad \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L, \quad \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$$

PMNS matrix

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

Neutrino mass states



What we know: flavor mixing

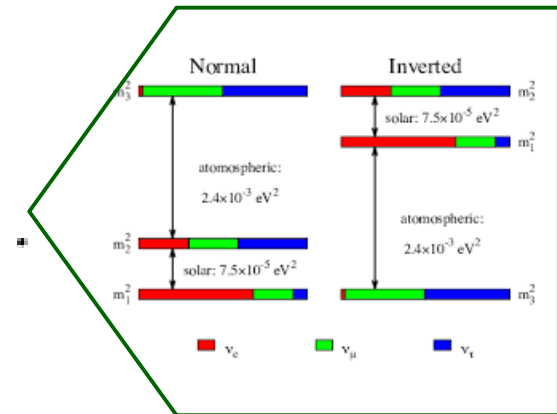
Standard Model states

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$$

PMNS matrix

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

Neutrino mass states



$$U_{\text{PMNS}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

atmospheric

reactor

solar

2 mass differences + 3 angles + 1 phase = 6 new parameters for SM

PMNS some years ago

$$T_{BM} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{\sqrt{2}} \\ -\frac{1}{2} & -\frac{1}{2} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

Bi-maximal mixing

$$T_{TBM} = \begin{pmatrix} \sqrt{\frac{2}{3}} & \frac{1}{\sqrt{3}} & 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{6}} & -\frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

Tri-Bi-maximal mixing

$$T_{GR} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ \frac{s_{12}}{\sqrt{2}} & -\frac{c_{12}}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{s_{12}}{\sqrt{2}} & -\frac{c_{12}}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix}$$

Golden Ratio

$$\tan \theta_{12} = 1/\phi, \text{ with } \phi = (1 + \sqrt{5})/2$$

PMNS some years ago

$$\begin{array}{l}
 T_{BM} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{\sqrt{2}} \\ -\frac{1}{2} & -\frac{1}{2} & \frac{1}{\sqrt{2}} \end{pmatrix} \\
 \text{Bi-maximal} \\
 \text{mixing}
 \end{array}
 \quad
 \begin{array}{l}
 T_{TBM} = \begin{pmatrix} \sqrt{\frac{2}{3}} & \frac{1}{\sqrt{3}} & 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{6}} & -\frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{pmatrix} \\
 \text{Tri-Bi-} \\
 \text{maximal} \\
 \text{mixing}
 \end{array}
 \quad
 \begin{array}{l}
 T_{GR} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ s_{12}/\sqrt{2} & -c_{12}/\sqrt{2} & 1/\sqrt{2} \\ s_{12}/\sqrt{2} & -c_{12}/\sqrt{2} & -1/\sqrt{2} \end{pmatrix} \\
 \text{Golden} \\
 \text{Ratio}
 \end{array}
 \quad
 \tan \theta_{12} = 1/\phi, \text{ with } \phi = (1 + \sqrt{5})/2$$

CP conserving patterns

$$\tan(\theta_{12}) = 1$$

$$\tan(\theta_{12}) = \frac{1}{\sqrt{2}}$$

$$\tan(\theta_{12}) = \frac{2\sqrt{5}}{\sqrt{5+\sqrt{5}}}$$

nice

$$\tan(\theta_{23}) = 1$$

$$\tan(\theta_{23}) = 1$$

$$\tan(\theta_{23}) = 1$$

acceptable

$$\sin(\theta_{13}) = 0$$

$$\sin(\theta_{13}) = 0$$

$$\sin(\theta_{13}) = 0$$

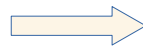
bad

What we know: the solar sector

before 2012

solar ν_e disappearance, large θ_{12} (H/S, Ga, SK) (02)

solar ν_e are converted to $\nu_\mu + \nu_\tau$ (SNO) (02)



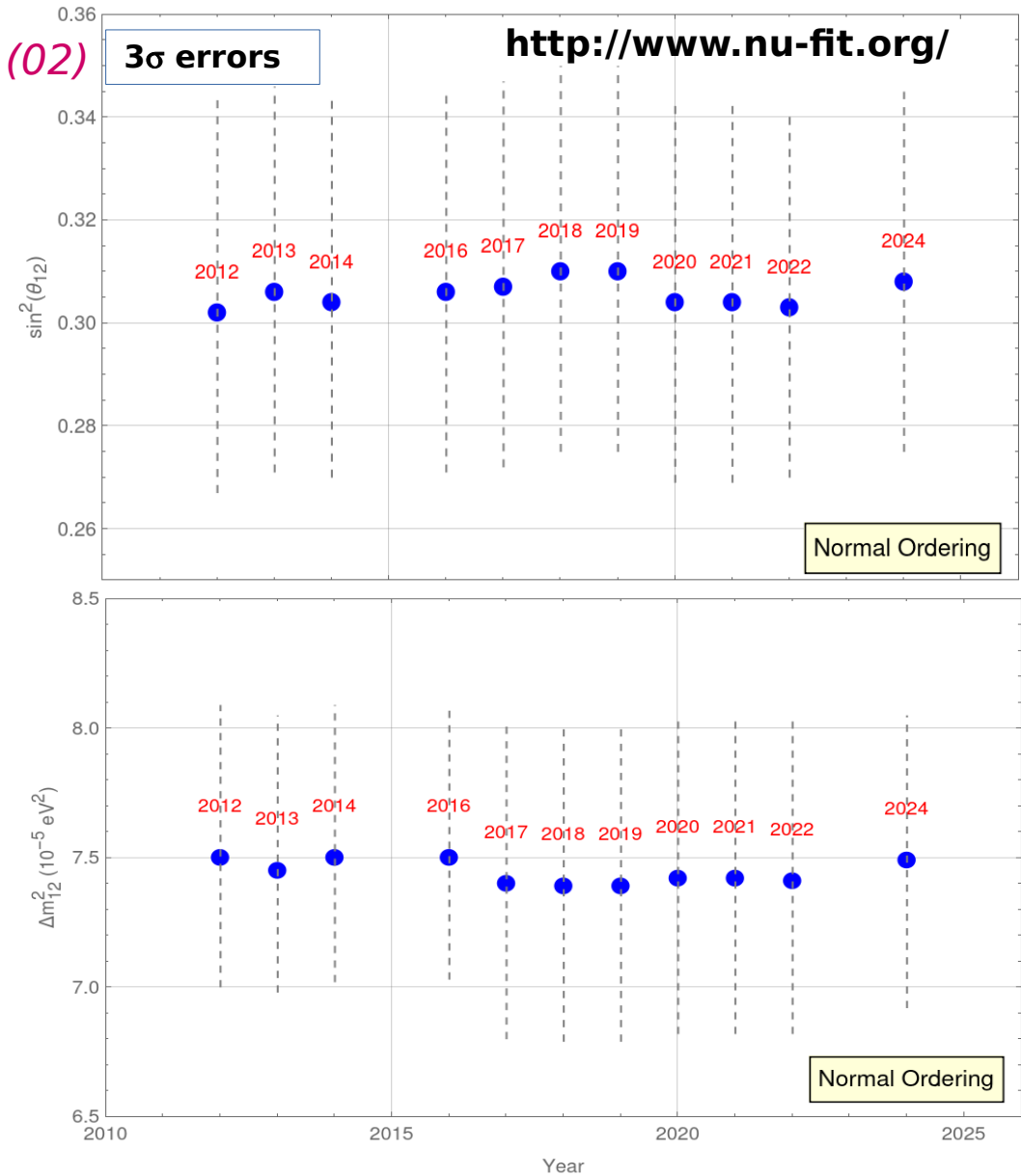
not useful for distinguishing
among different patterns

What we know: the solar sector

before 2012

solar ν_e disappearance, large θ_{12} (H/S,Ga,SK) (02)
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from 2012 to 2024



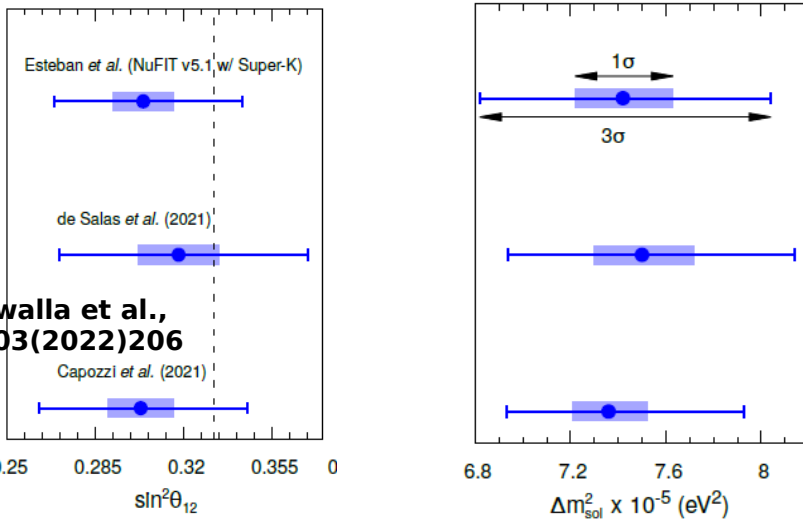
What we know: the solar sector

before 2012

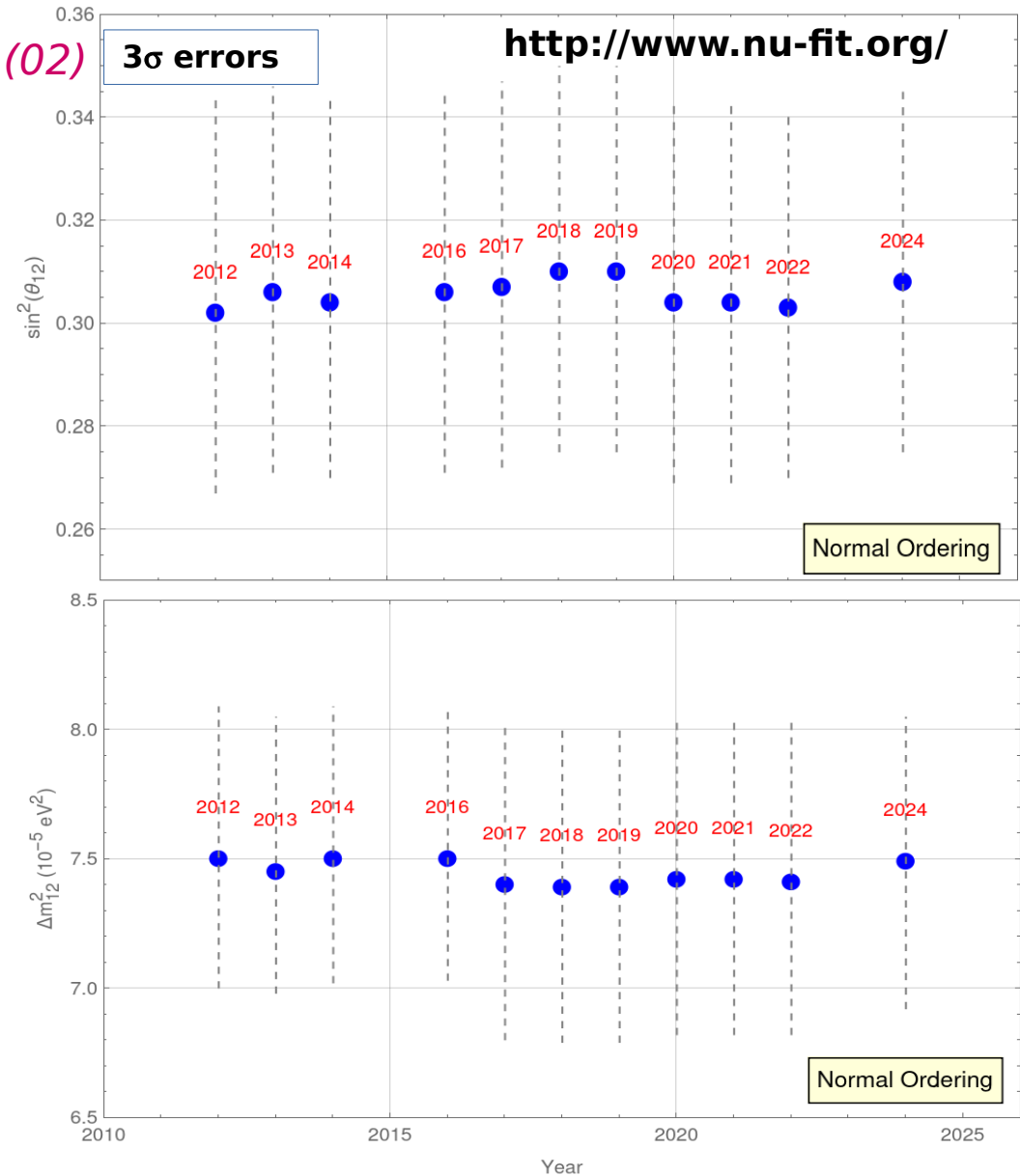
solar ν_e disappearance, large θ_{12} (H/S, Ga, SK) (02)
solar ν_e are converted to $\nu_\mu + \nu_\tau$ (SNO) (02)

Relevant features:

- central values almost constant
- not large improvements on errors
- precisely determined by solar and KamLAND constraints
- no significant best-fit difference between the NO and IO cases.



from 2012 to 2024



3 σ errors

<http://www.nu-fit.org/>

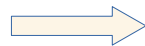
Normal Ordering

Normal Ordering

What we know: the atmospheric sector

before 2012

atmospheric ν_μ disappear, large θ_{23} (SK) (98)
accelerator ν_μ disappear (K2K 04 , MINOS 06)
accelerator ν_μ converted to ν_τ (OPERA 10)



All consistent among
different patterns

What we know: the atmospheric sector

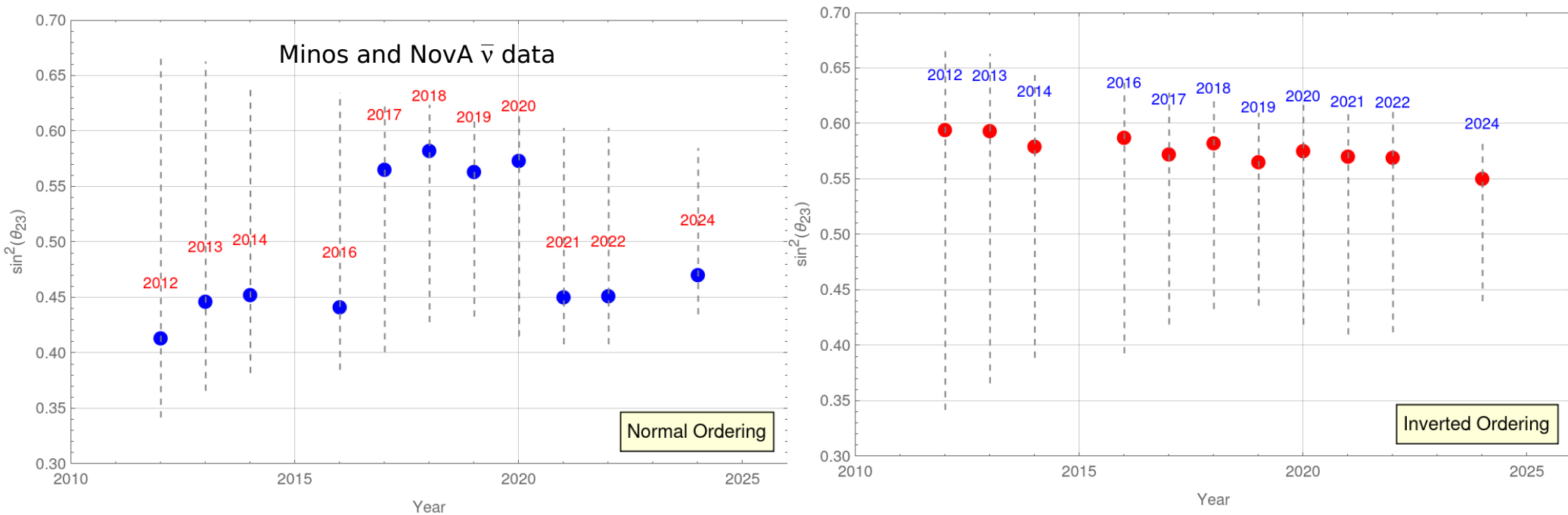
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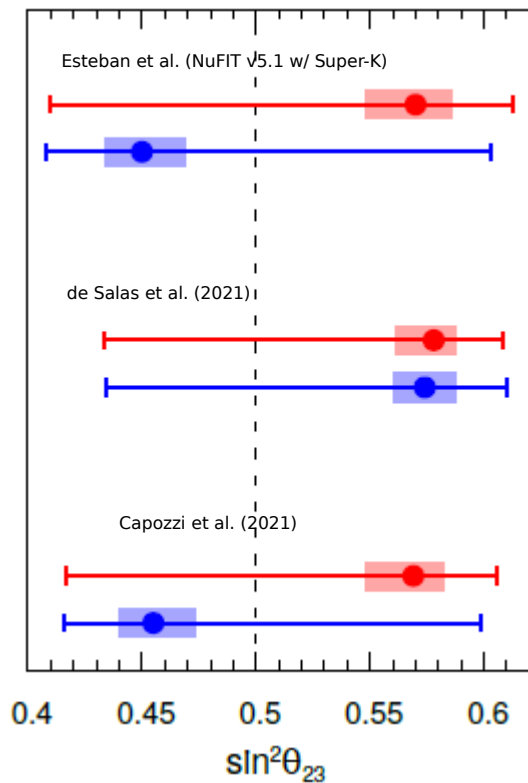
from 2012 to 2024



Quite a puzzling situation !

What we know: the atmospheric sector

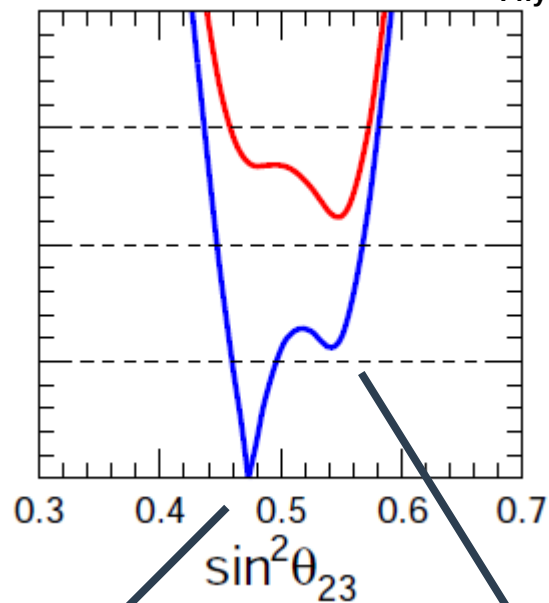
Agarwalla et al.,
JHEP03(2022)206



Octant degeneracy problem:
 θ_{23} smaller or larger than 45°

$$P_{\mu\mu} \sim \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)$$

Capozzi et al.
Phys.Rev.D111 (2025) no.9, 093006



lower octant

higher octant

What we know: the atmospheric sector

All patterns predict maximal mixing

$$T_{BM} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{\sqrt{2}} \\ -\frac{1}{2} & -\frac{1}{2} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

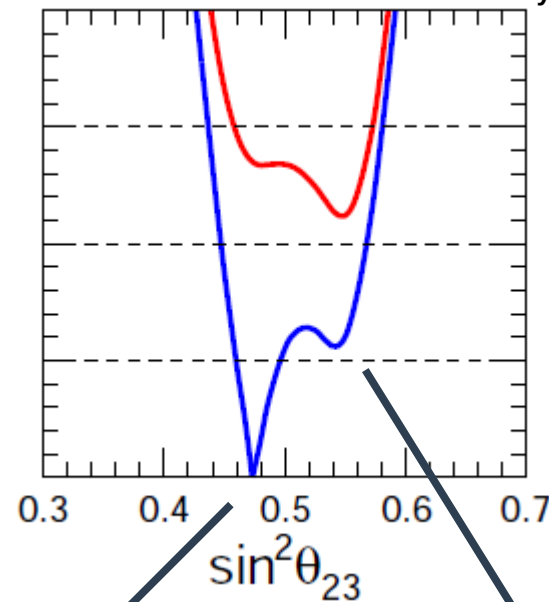


Corrections must be added to describe the correct octant, once found...

Octant degeneracy problem:
 θ_{23} smaller or larger than 45°

$$P_{\mu\mu} \sim \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)$$

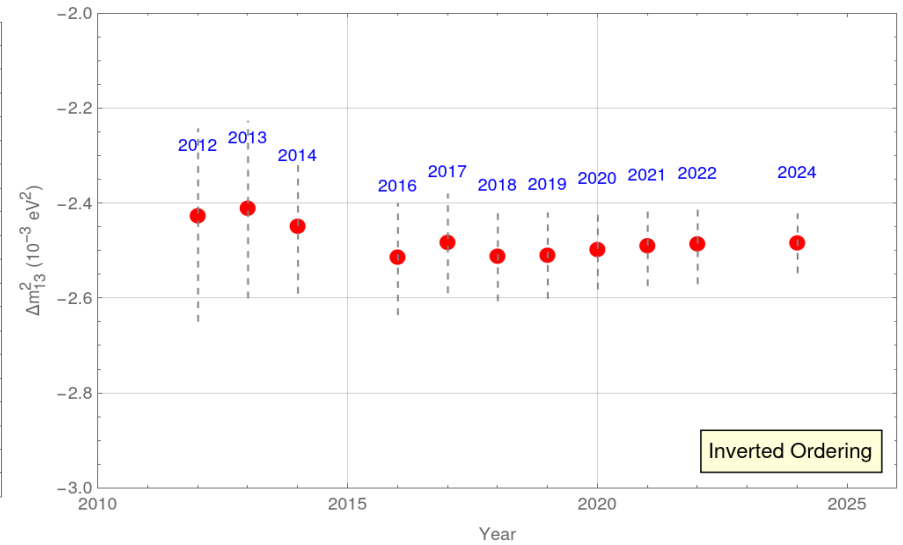
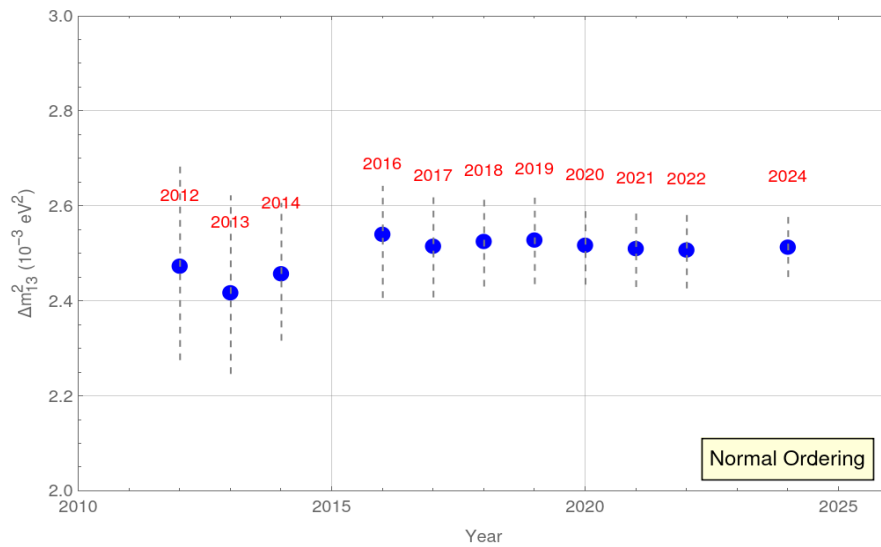
Capozzi et al.
Phys.Rev.D111 (2025) no.9, 093006



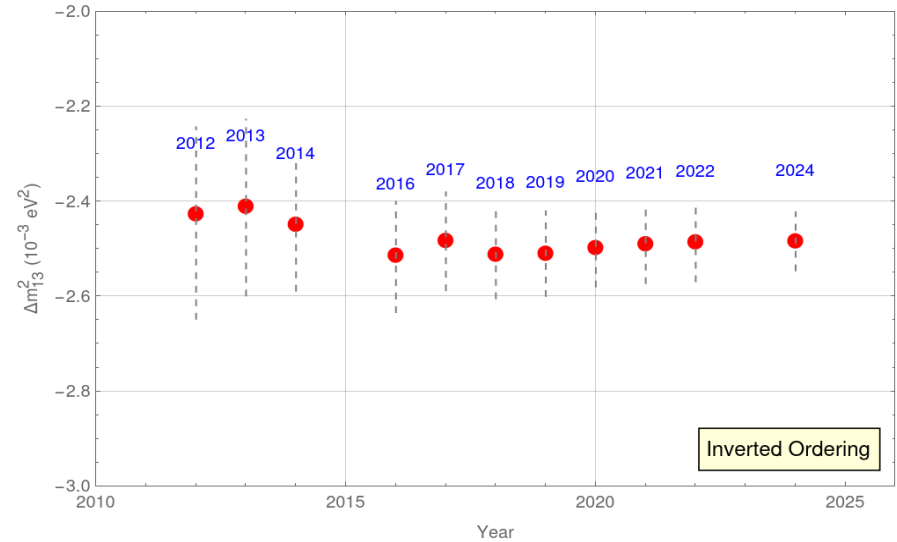
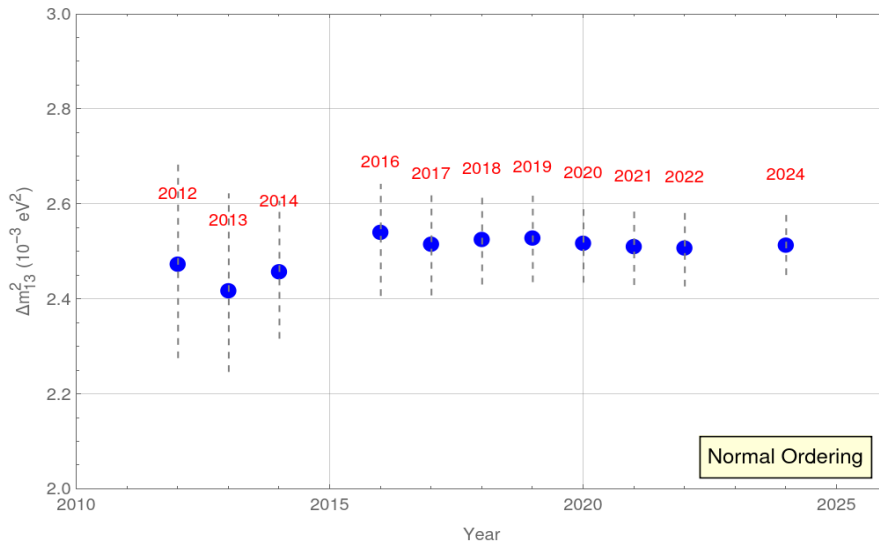
lower octant

higher octant

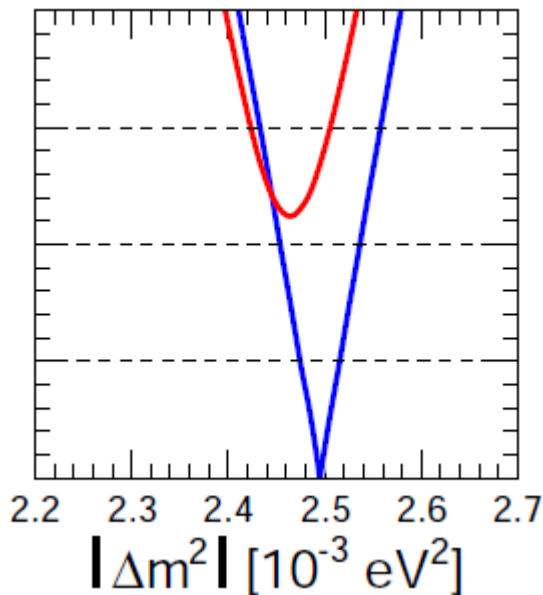
What we know: the atmospheric sector



What we know: the atmospheric sector



Capozzi et al.
Phys. Rev. D111 (2025) no. 9, 093006



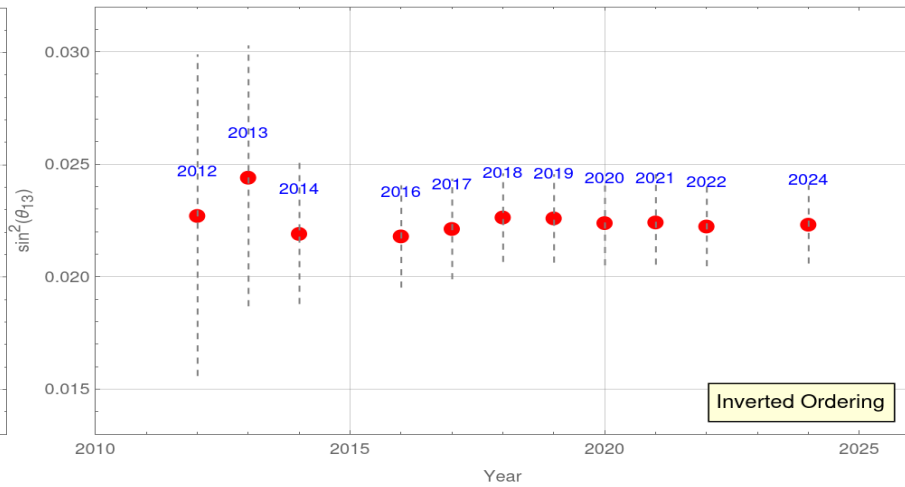
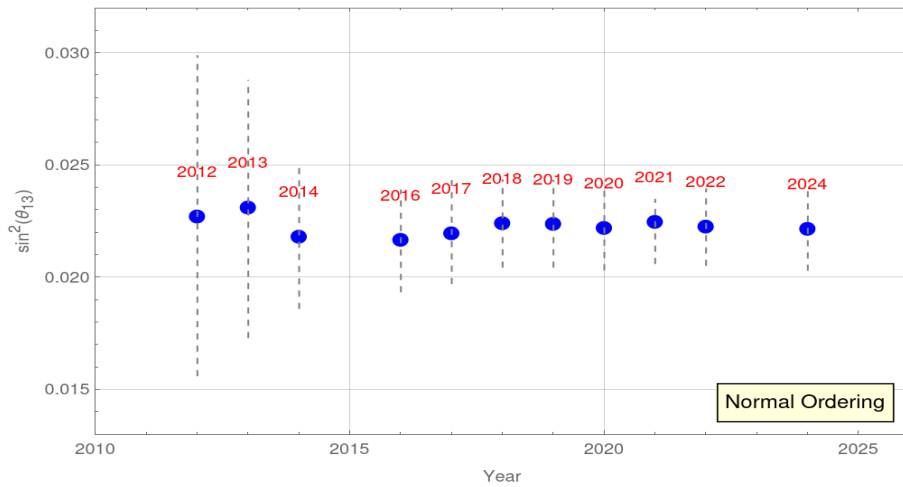
Parameter	Ordering	Best fit	1 σ range	2 σ range	3 σ range	"1 σ " (%)
$ \Delta m^2 /10^{-3} \text{ eV}^2$	NO	2.495	2.475 – 2.515	2.454 – 2.536	2.433 – 2.558	0.8
	IO	2.465	2.444 – 2.485	2.423 – 2.506	2.403 – 2.527	0.8

- Δm^2_{atm} entering the subpercent precision era

- NO favoured at 2.2 sigma (2.5 in 2021)

(preference for IO by combined LBL accelerator data first reduced by SBL reactor data and then flipped to NO by atmospheric data)

What we know: the reactor sector

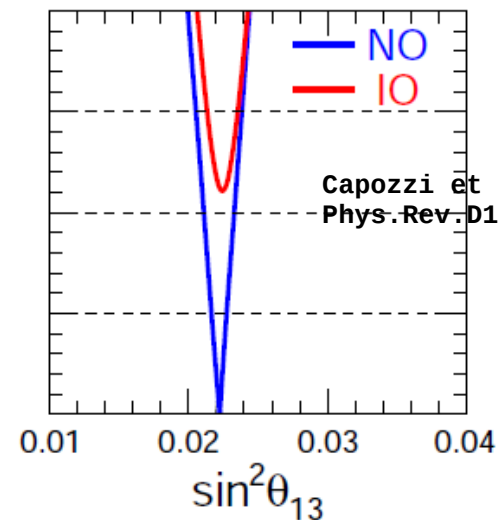


Very clear situation:

converging hints about nonzero values from the global analysis of solar, KamLAND, atmospheric and LBL accelerator data that consistently reached a cumulative statistical above 3sigma before its discovery and precise measurement by SBL reactor experiments

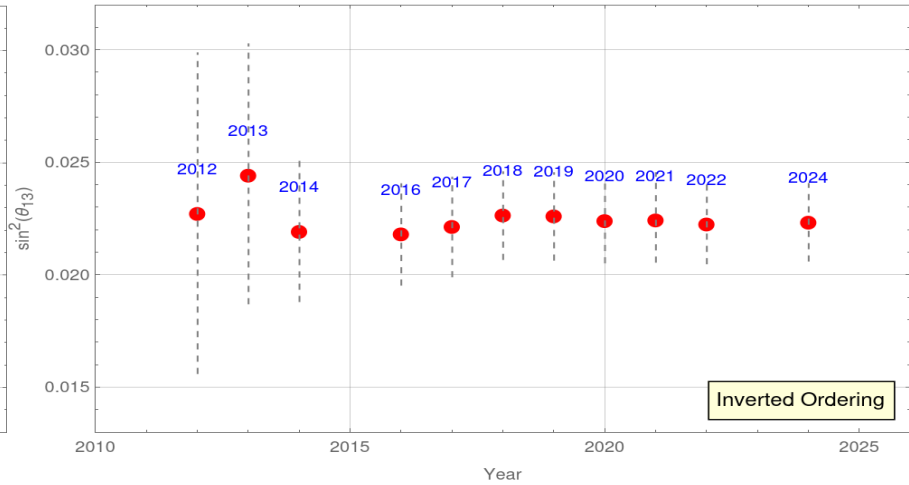
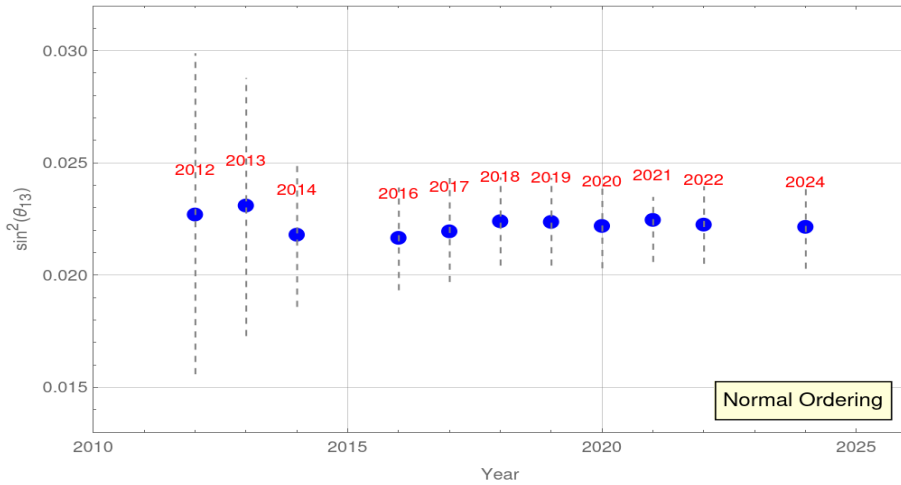
1 sigma error at the level of 4-5%

$$\sin(\theta_{13}) = (2.23 \pm 0.06) 10^{-2}$$



Capozzi et al.
Phys. Rev. D111 (2025) no.9, 093006

What we know: the reactor sector



Major breakthrough in the model building industry

Corrections are needed from charged lepton diagonalization

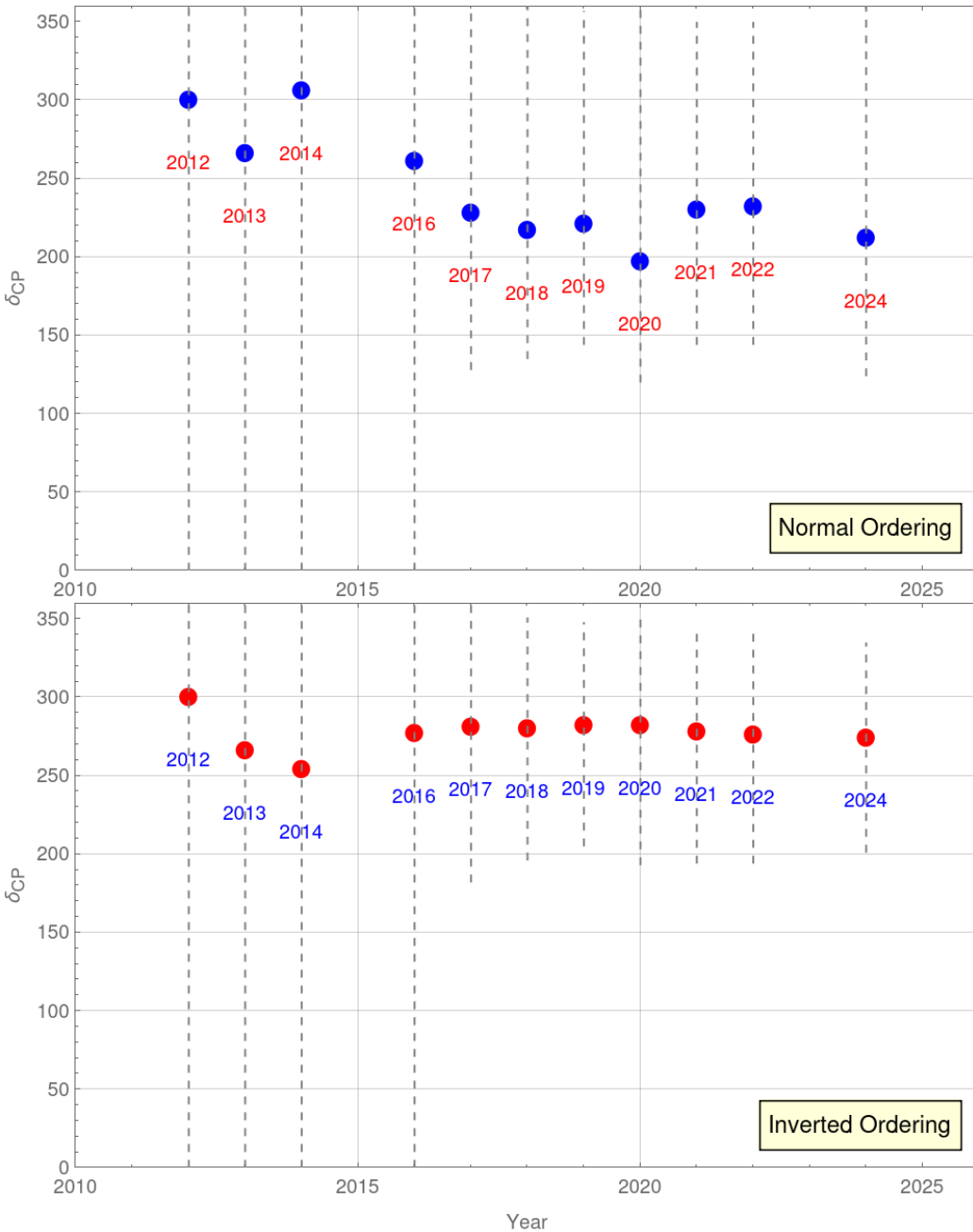
$$U^{PMNS} = U_{cl}^+ \cdot T_{BM} \quad U_{cl} \sim \begin{pmatrix} 1 & \lambda_C & \lambda_C \\ \lambda_C & 1 & 0 \\ \lambda_C & 0 & 1 \end{pmatrix} \quad \text{Altarelli et al., 0903.1940}$$

good results:

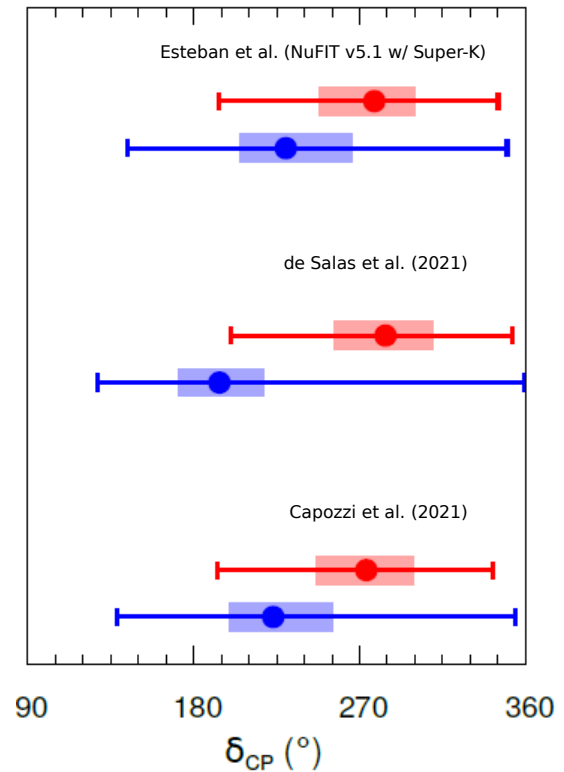
$$\begin{cases} \sin^2 \theta_{12} = \frac{1}{2} - O(\lambda_C) \\ \sin^2 \theta_{23} = \frac{1}{2} \\ \sin \theta_{13} = \frac{1}{\sqrt{2}} O(\lambda_C) \end{cases}$$

$$[\theta_{13}^{PMNS} = O(1) \cdot \theta_{12}^{CKM}]$$

What we know: δ_{CP}



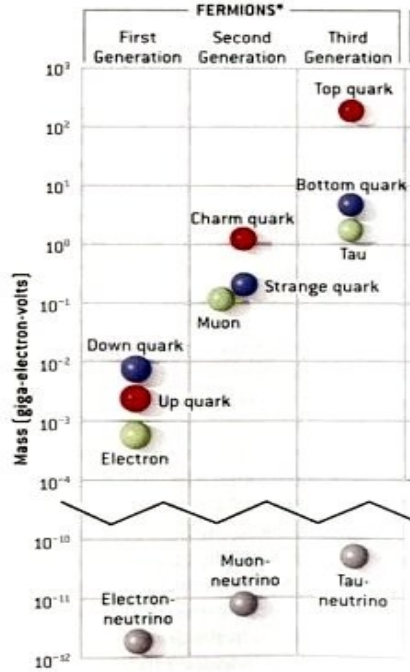
$$P_{\alpha\beta}^{CPV} \sim \sin(\theta_{13}) \left(\frac{\Delta m_{sol}^2}{\Delta m_{atm}^2} \right) \sin \delta_{CP}$$



- weak indications:
 IO **seems** to prefer maximal CP violation while NO a CP conserving solution

The Flavor Problem (I)

Mass hierarchies



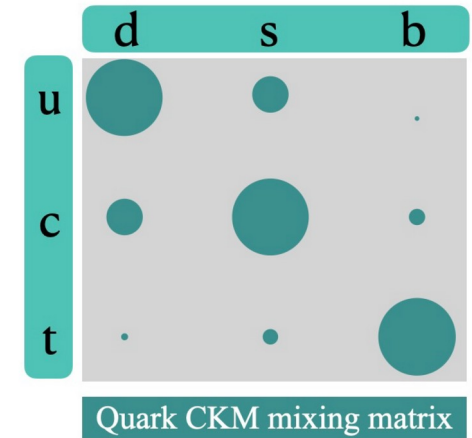
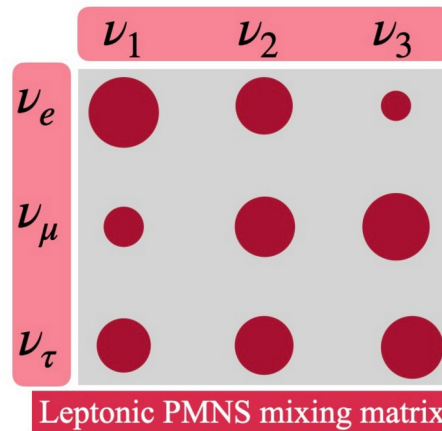
$$m_d \ll m_s \ll m_b, \quad \frac{m_d}{m_s} = 5.02 \times 10^{-2},$$

$$m_u \ll m_c \ll m_t, \quad \frac{m_u}{m_c} = 1.7 \times 10^{-3},$$

$$\frac{m_s}{m_b} = 2.22 \times 10^{-2}, \quad m_b = 4.18 \text{ GeV};$$

$$\frac{m_c}{m_t} = 7.3 \times 10^{-3}, \quad m_t = 172.9 \text{ GeV};$$

Fermion mixing



all mixing are large but the 13 element

almost a diagonal matrix

Why are they so different?

Approach

Discrete Non-Abelian Symmetries

Advantages

Flexibility: Wide choice of groups (e.g., A_4 , S_4) and representations to fit data.

Established Precedents: Well-studied and widely applied

Intuitive Structure: Directly imposes order on mass matrices via group invariants.

Disadvantages

Complexity: Requires additional scalar fields and non-trivial vacuum alignment.

Free Parameters: Many degrees of freedom (flavon VEVs, coupling constants) reduce predictivity.

Ad Hoc: Phenomenologically motivated, less tied to fundamental theories.

Modular Forms

Elegance: Reduces the number of fields (only τ as a 'flavon-like' field), simplifying the model.

Predictivity: Yukawa couplings constrained by modular forms, with fewer free parameters.

Theoretical Foundation: Naturally arises from string theory or extra-dimensional geometries.

τ Stabilization: Determining the modulus τ 's value is challenging.

Limited Flexibility: The form of couplings is fixed by modular weight and level.

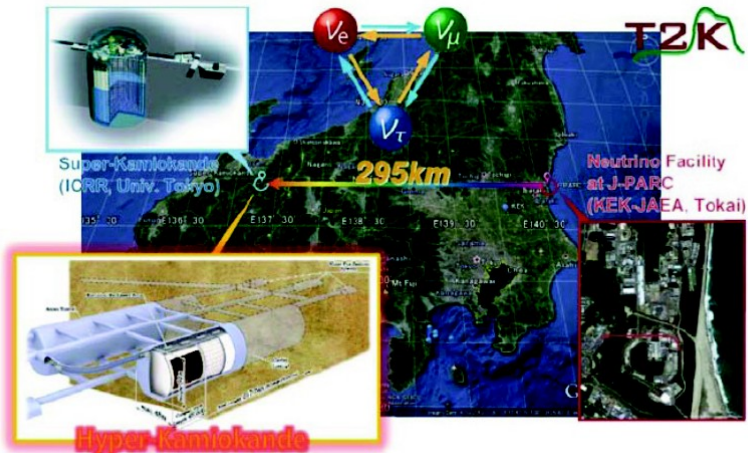
Mathematical Complexity: Requires familiarity with modular forms and the $SL(2, \mathbb{Z})$ group.

Future measurements can help in discarding some approaches to the flavor problem

Future perspectives

T2HK

T2K



WC 374 kt
295 km

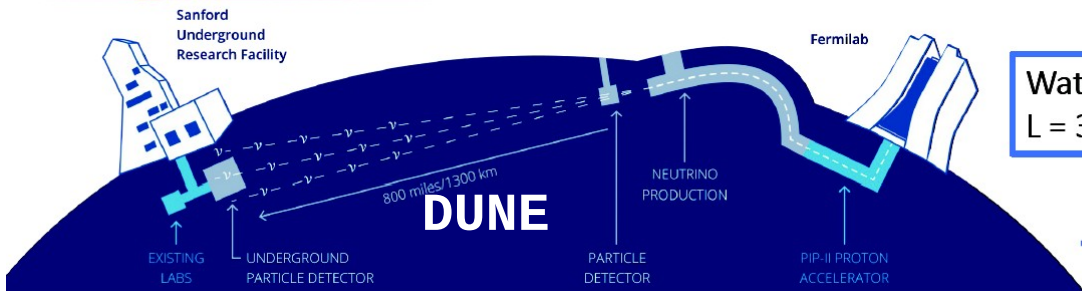
ESSnuSB – talk by Eric Baussan



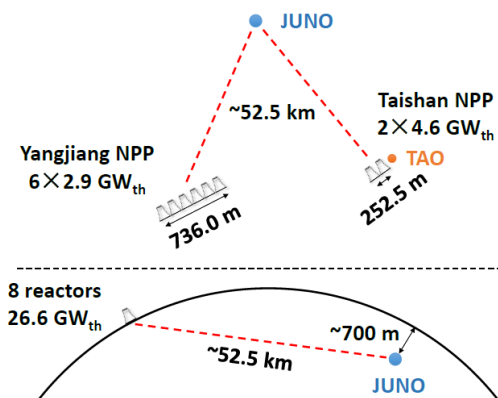
Image Credit –
Monojit Ghosh

Water Cerenkov (WC) Far detector of 540 kt
L = 360 km

Liquid argon TPC of 40 kt
L = 1300 km

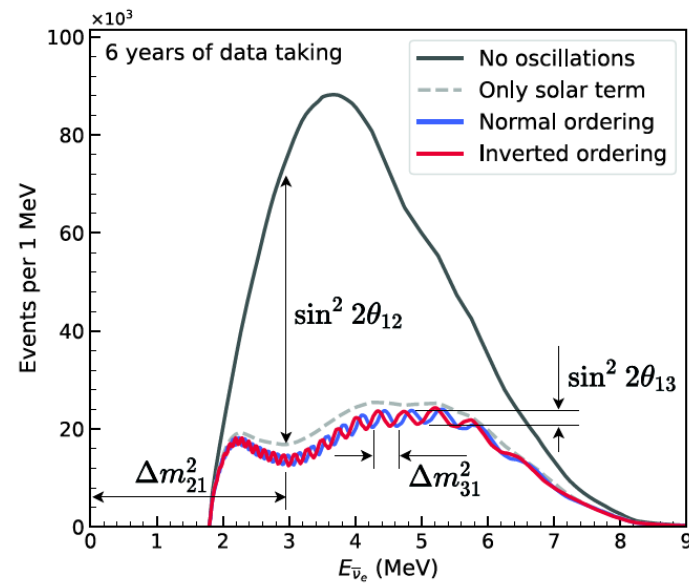


KNO

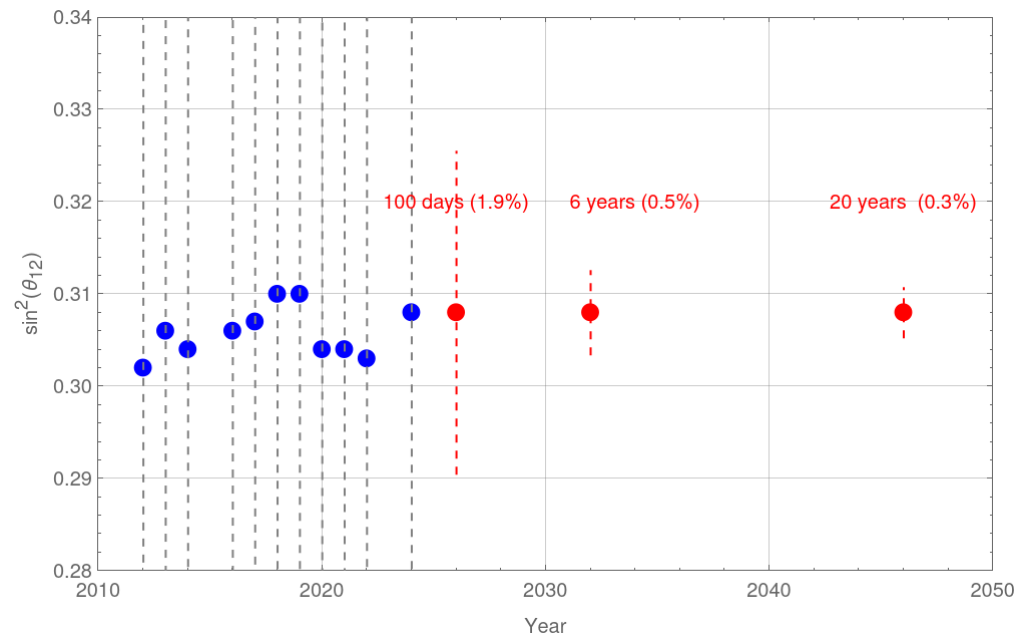
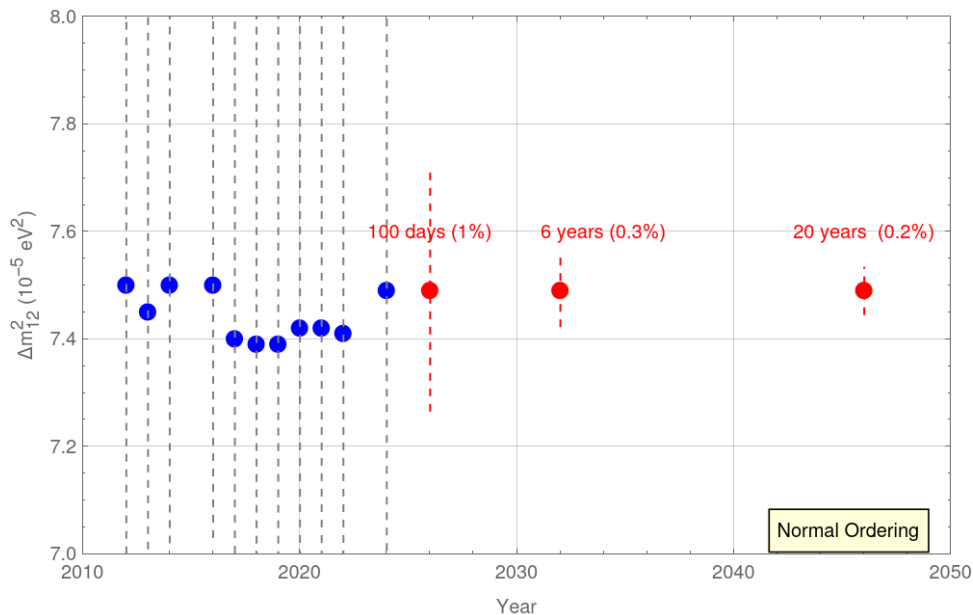


Better determination of solar parameters

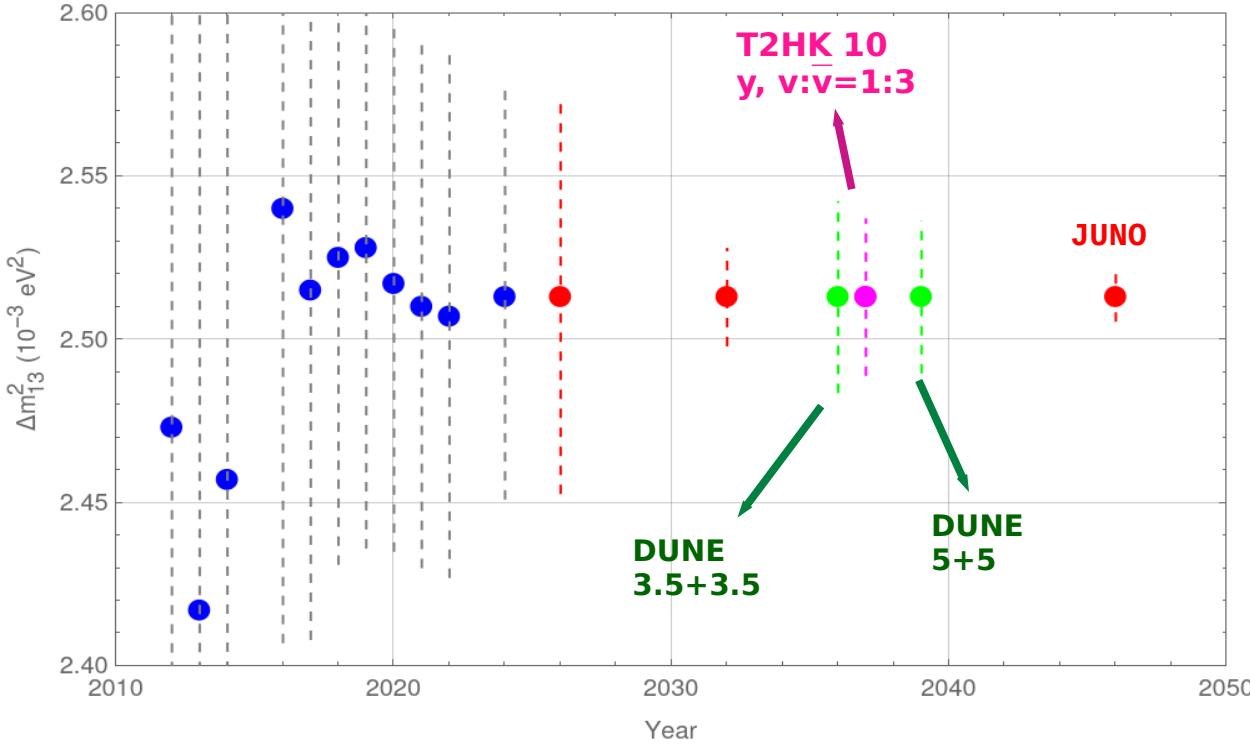
A. Abusleme et al. [JUNO],
Chin. Phys. C46 (2022) no. 12, 123001



sensitive to both solar and atmospheric oscillations



Atmospheric mass precision & ordering

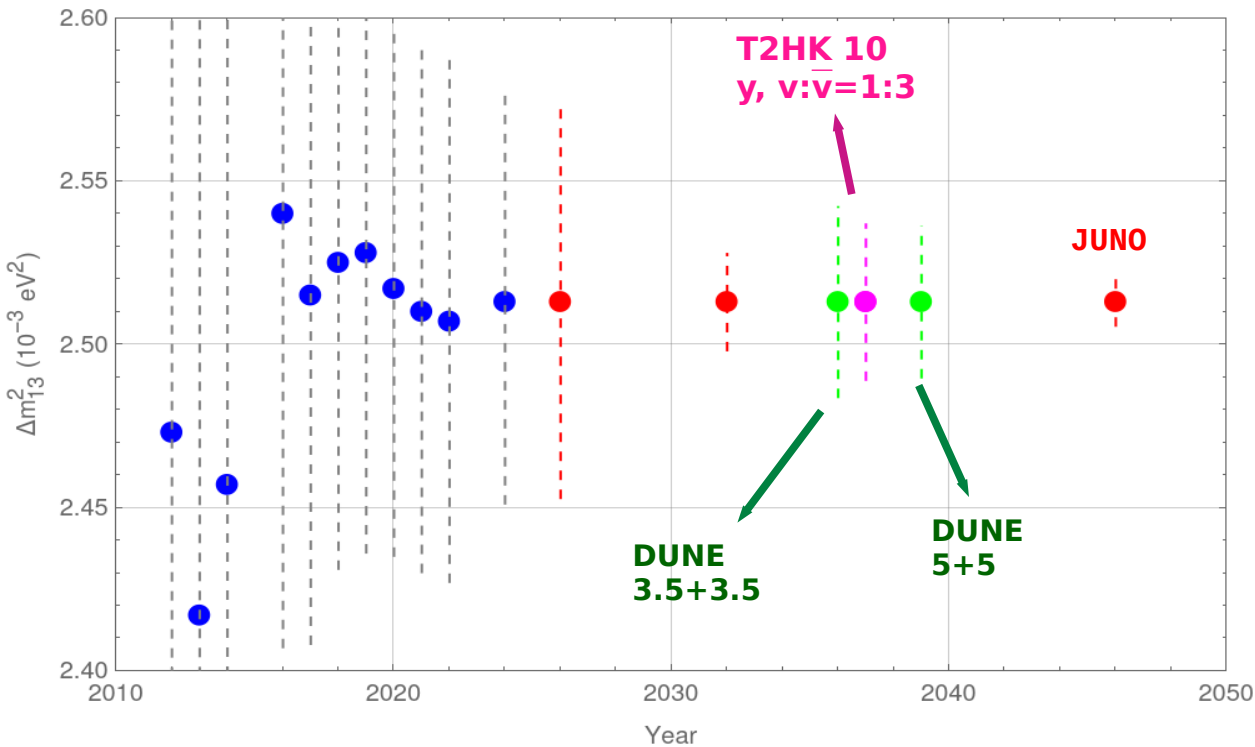


Jeanne Wilson, T2HK, NOW24

Marshall, DUNE, Neutrino24
 Agarwalla et al., JHEP03(2022)206

A.Abusleme et al. [JUNO],
 Chin.Phys.C46 (2022)no.12,123001

Atmospheric mass precision & ordering



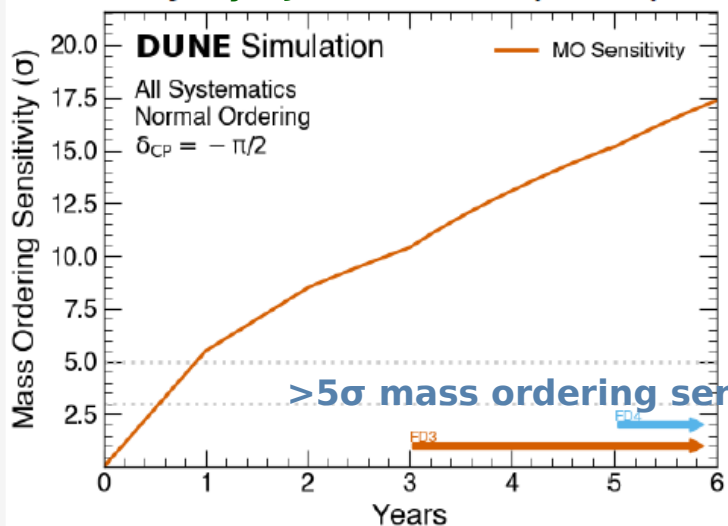
Jeanne Wilson, T2HK, NOW24

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Agarwalla et al., JHEP03(2022)206

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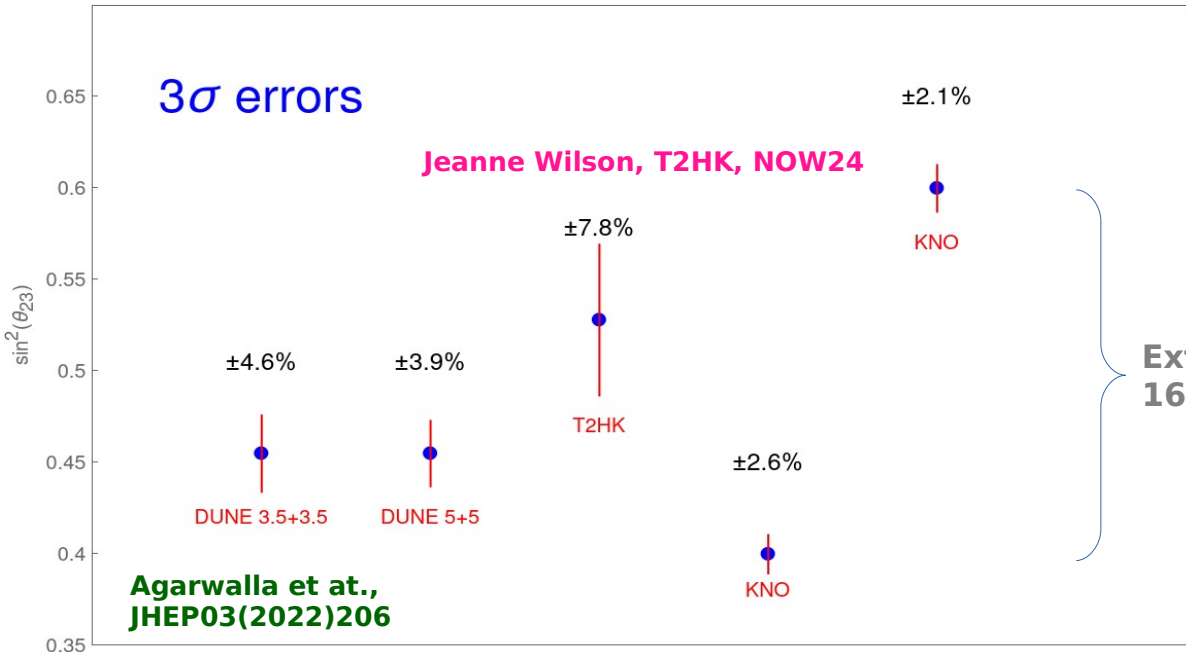
DUNE, Eur. Phys. J. C 80, 978 (2020)

Snowmass: NF01 Topical Group Report



		Atmospheric Mass Ordering
JUNO	Optimistic	2030: 3σ
	Conservative	2030: 2.5σ
DUNE	Optimistic	2030: 5σ
	Conservative	2032: 5σ
HK	Optimistic	2033: 5σ
	Conservative	2032: 3σ

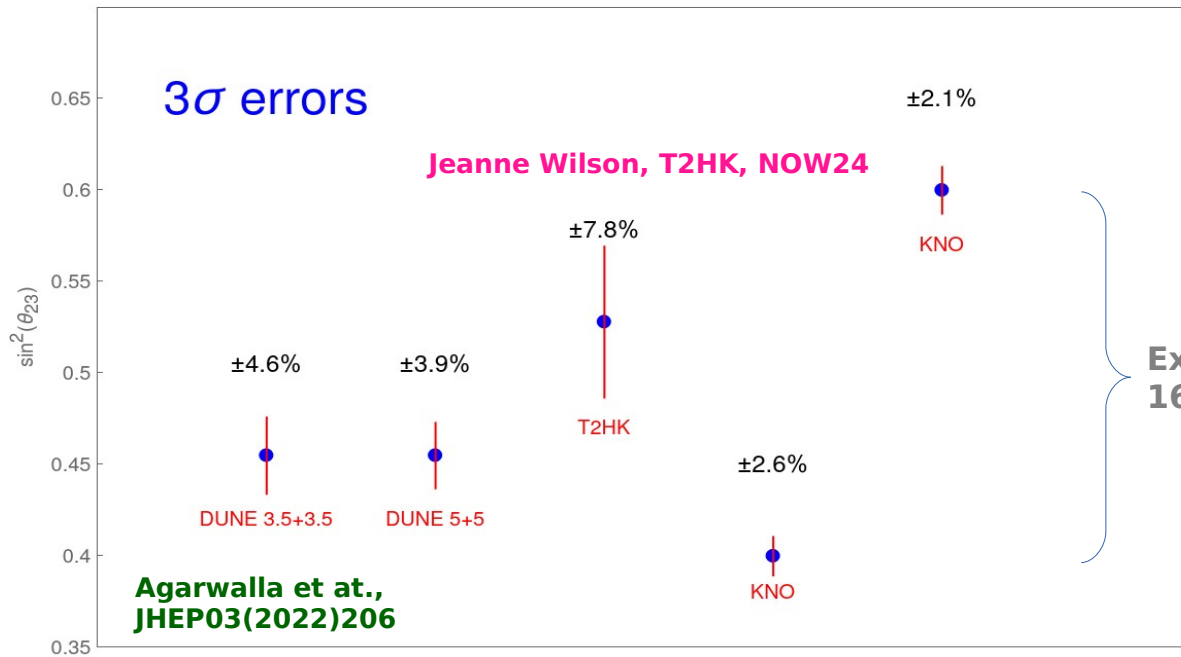
Atmospheric angle precision & octant degeneracy



some representative points for different true octants

Extrapolated from 1611.06118v3 [hep-ex]

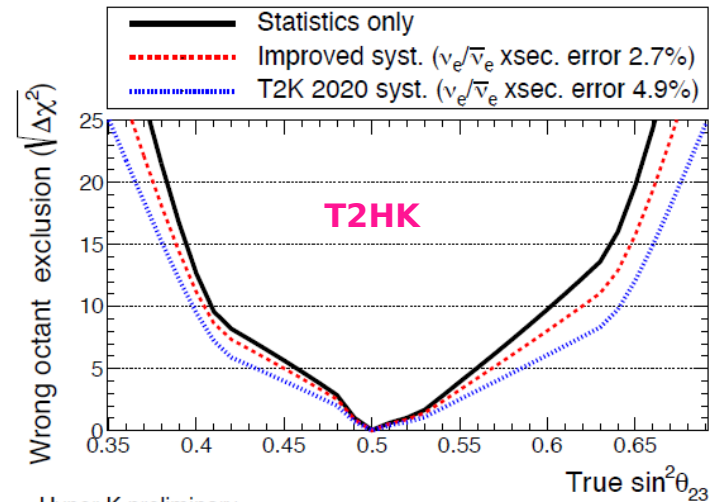
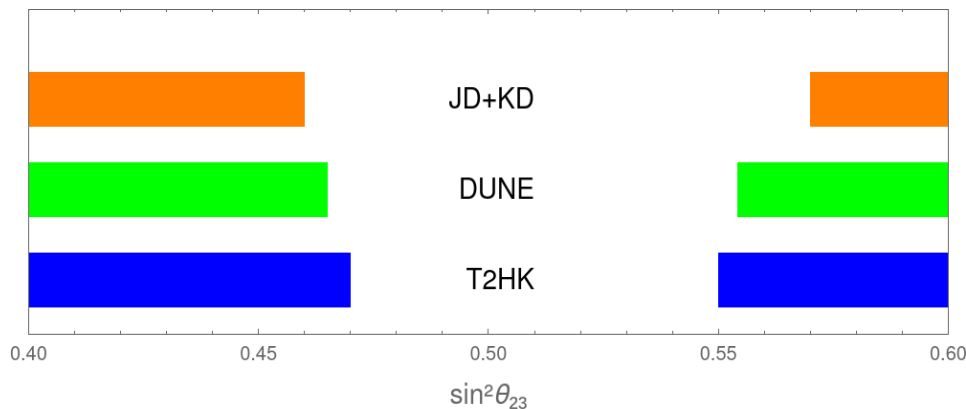
Atmospheric angle precision & octant degeneracy



some representative points for different true octants

EPJ Web of Conferences 312, 02005 (2024)

excluding the wrong octant at 3 σ

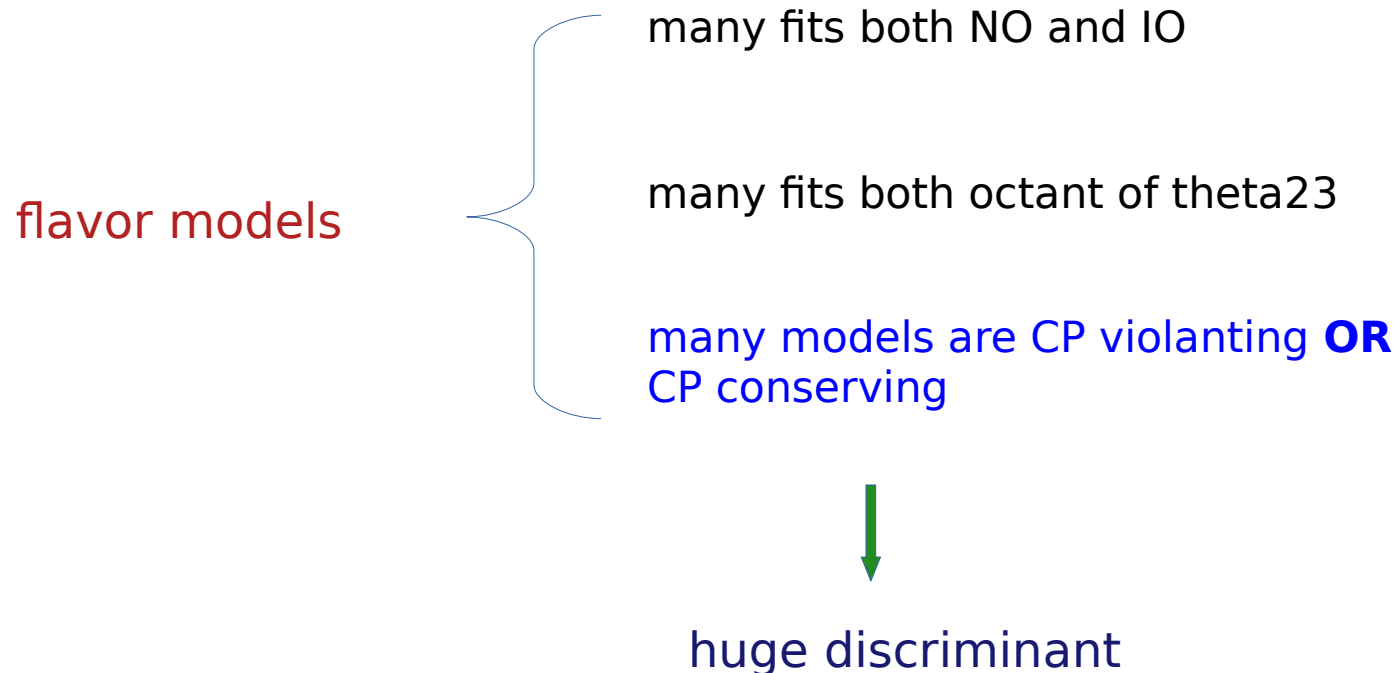


Hyper-K preliminary

True normal ordering (known), 10 years (2.7×10^{22} POT 1:3 $\nu\bar{\nu}$)
 $\sin^2\theta_{13}=0.0218\pm 0.0007$, $\delta_{CP}=-1.601$, $\Delta m_{32}^2=2.509 \times 10^{-3} eV^2/c^4$

Discovery of CP violation

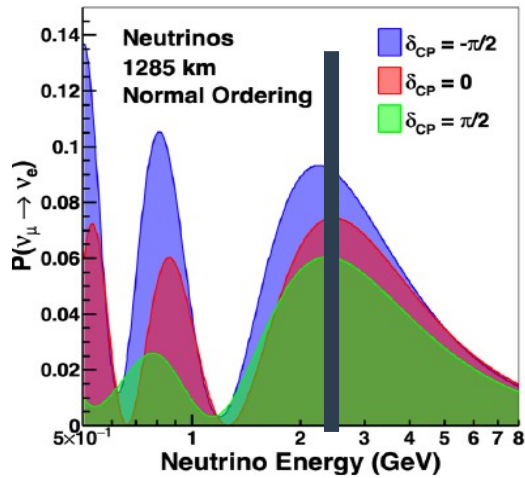
Personal point of view: delta CP is the most important Standard Model parameter to be determined.



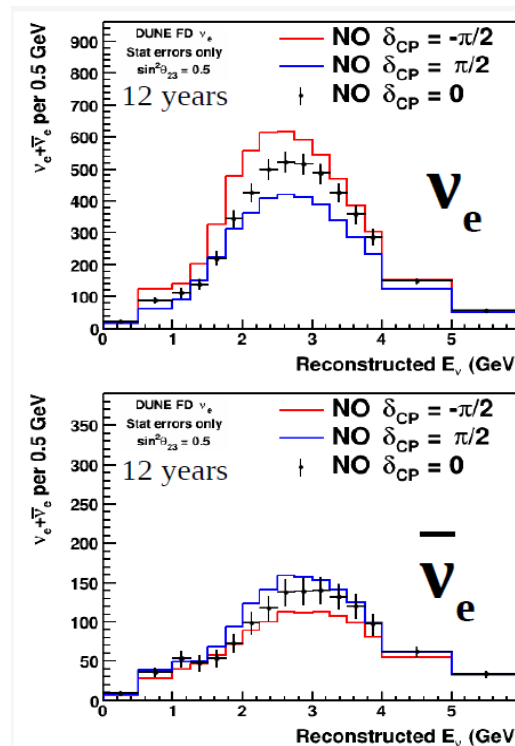
let us focus on ability to discriminate $\delta=0,\pi$ vs $\delta=\pi/2,3/2\pi$

Discovery of CP violation: DUNE and T2HK

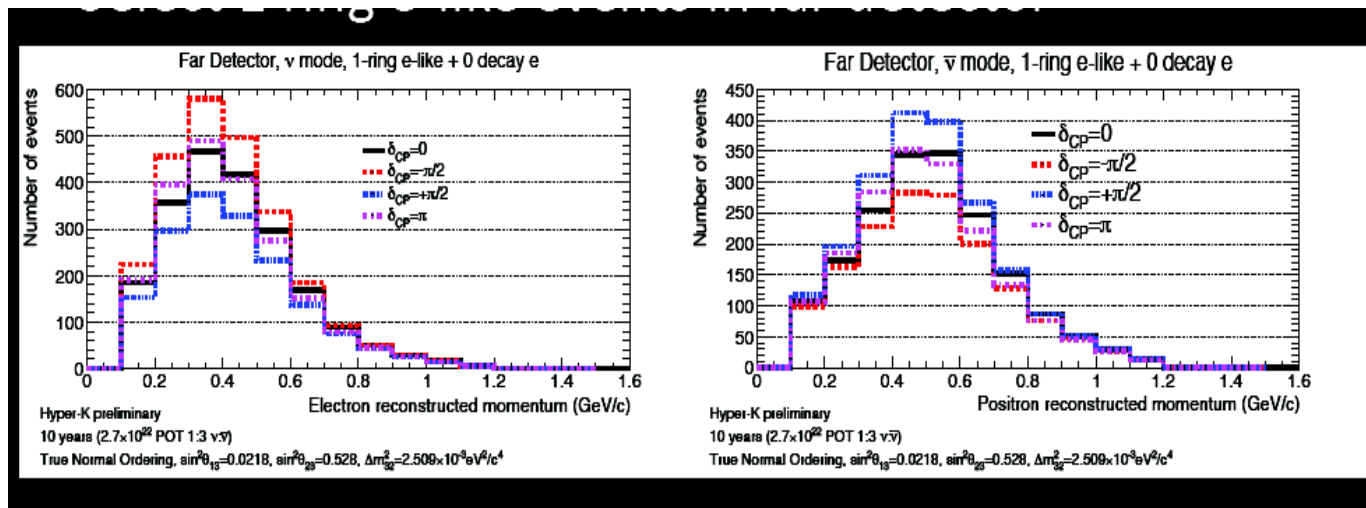
DUNE



T2HK

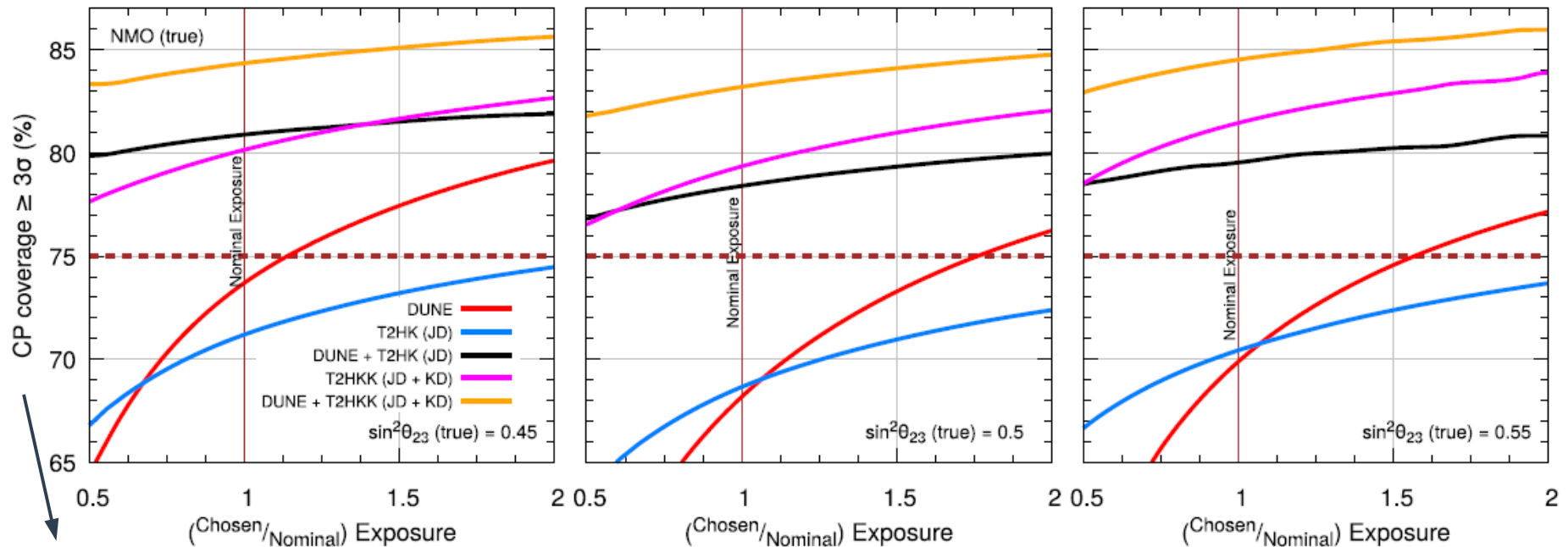


$|\delta| = +\pi/2$ max changes
in ν_e appearance



Discovery of CP violation: DUNE, T2HK and KNO

Agarwalla et al. Eur. Phys. J. C (2023) 83:694



denotes the values of true dCP (in %) in its entire range for which leptonic CPV can be established at $\geq 3\sigma$ confidence level.

differences among panels given by $\delta\text{-}\theta_{23}$ degeneracy

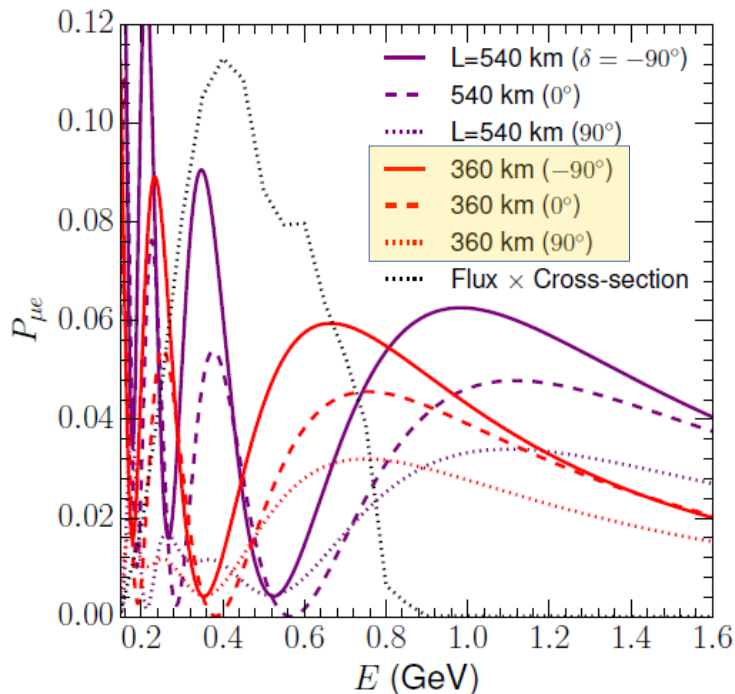
Relevant feature: at nominal exposure KNO always exceeds DUNE and T2HK

Discovery of CP violation: ESSνSB

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = \underbrace{s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{\tilde{B}_\mp}\right)^2 \sin^2\left(\frac{\tilde{B}_\mp L}{2}\right)}_{\text{atmospheric term}} + \underbrace{c_{23}^2 \sin^2 2\theta_{12} \left(\frac{\Delta_{21}}{A}\right)^2 \sin^2\left(\frac{AL}{2}\right)}_{\text{solar term}} + \underbrace{\tilde{J} \frac{\Delta_{21}}{A} \frac{\Delta_{31}}{\tilde{B}_\mp} \sin\left(\frac{AL}{2}\right) \sin\left(\frac{\tilde{B}_\mp L}{2}\right) \cos\left(\frac{\Delta_{31}L}{2} \pm \delta\right)}_{\text{interference term}}, \quad \tilde{B}_\mp = |A \mp \Delta_{13}|$$

First oscillation peak: $\Delta_{12}L/2 \sim 0.05$ and the “atmospheric” term tends to dominate

Second oscillation maximum: $\Delta_{12}L/2 \sim 0.14$ and the dependence on δ is much more important



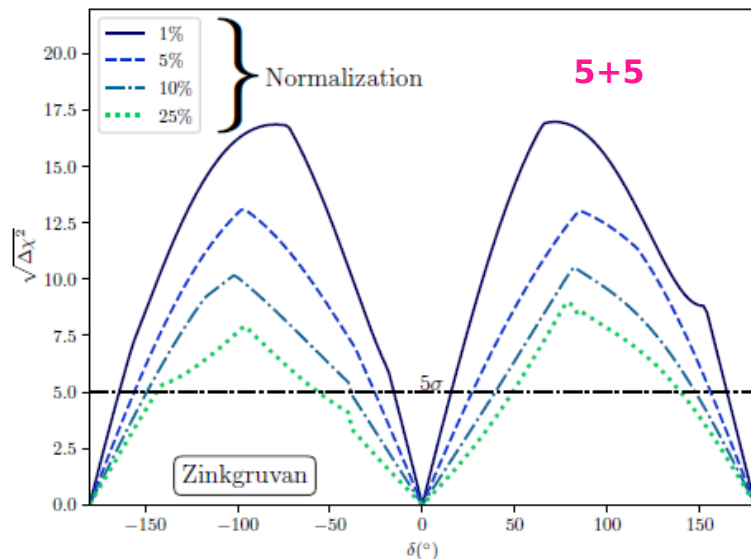
Discovery of CP violation: ESSνSB

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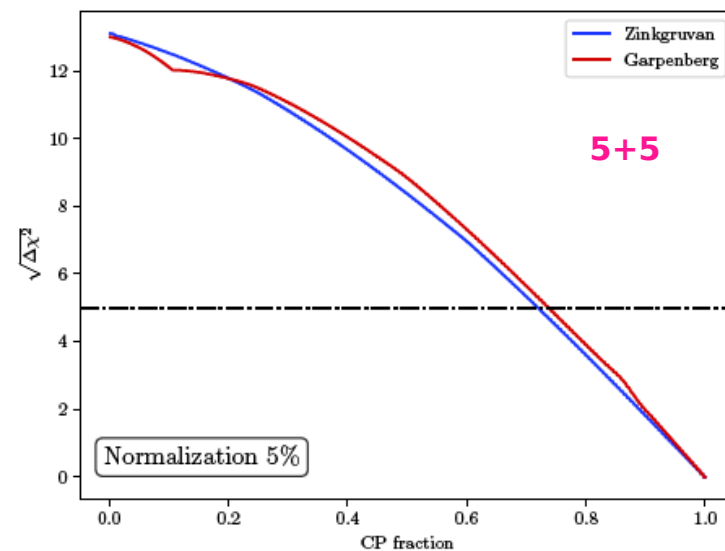
First oscillation peak: $\Delta_{12}L/2 \sim 0.05$ and the “atmospheric” term tends to dominate

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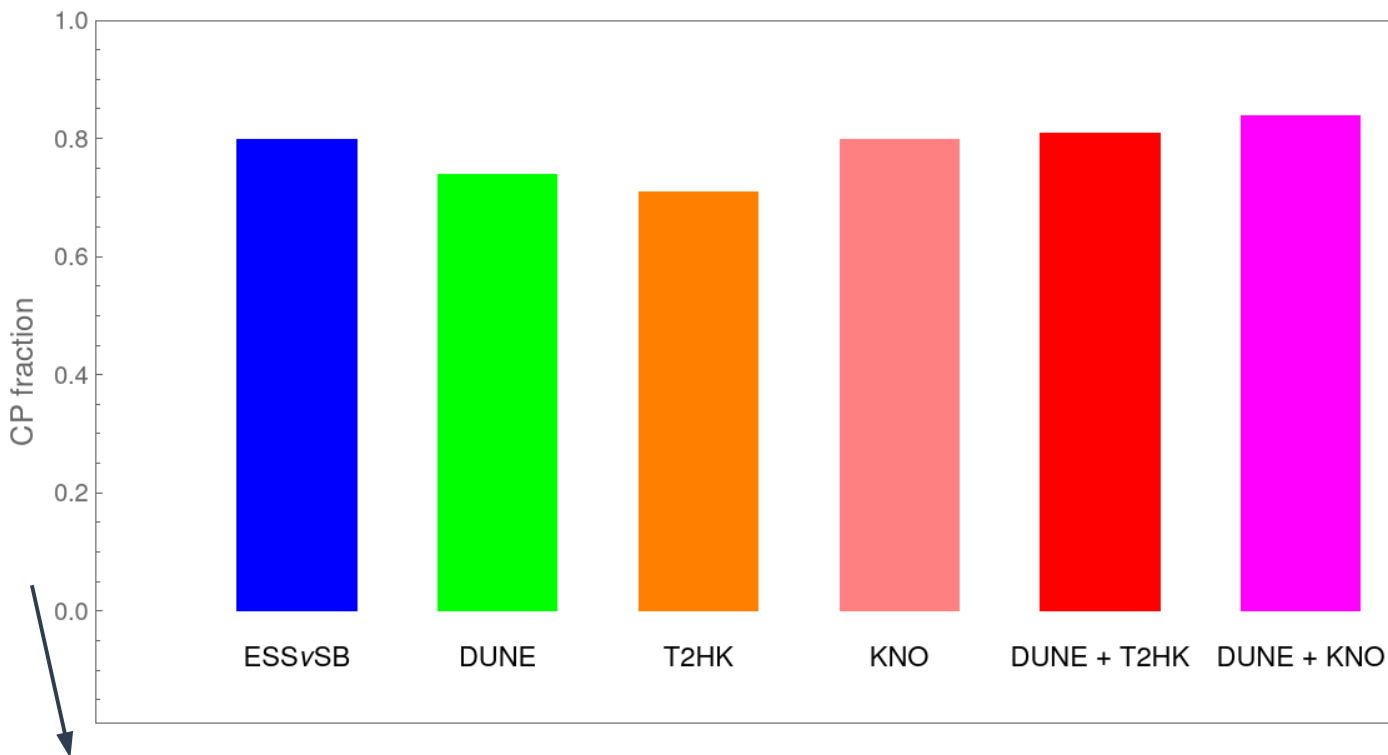
significance with which ESSnuSB would be able to disfavour CP-conservation



Significance with which CP violation could be established as a function of the fraction of values for which it would be possible.

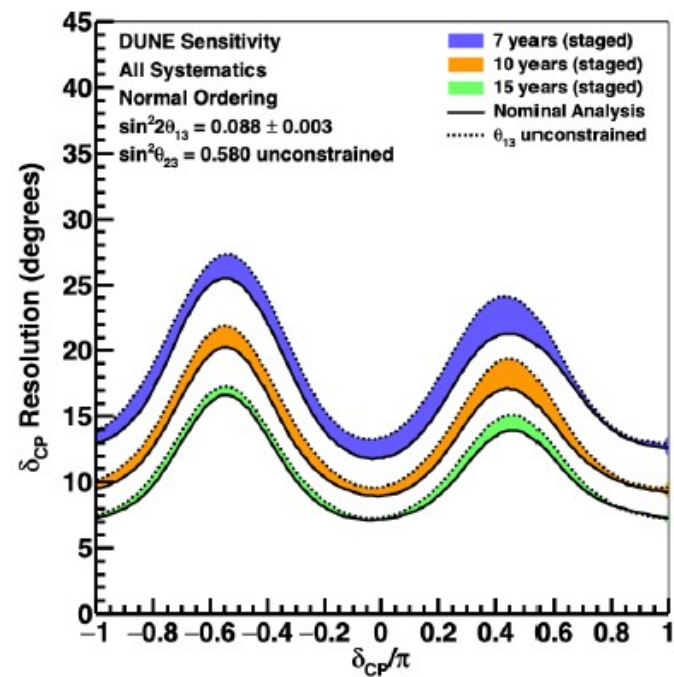


Discovery of CP violation: a summary



Significance with which CP violation could be established as a function of the fraction of values for which it would be possible.

typical error of δ measurement $\geq 10^\circ$



New Physics

plethora of NP signatures at
future Long Baseline Experiments



not going to revise them

Non-Standard Interactions

Neutrino Self-Interactions

Neutrino Decay

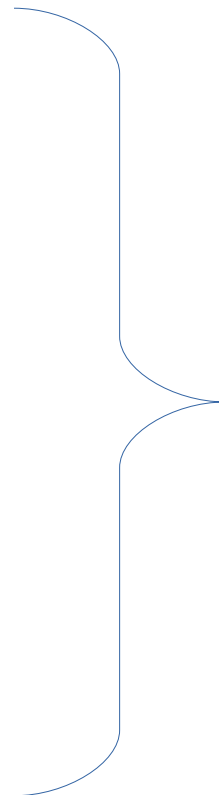
Decoherence

Unitarity Violation

Large Extra Dimensions

CPT Violation

Lorentz Invariance Violation



many of them have new sources
of CP violation



how to get info on them

New sources of CP violation

main ingredient:
Asymmetries

A.Giarnetti, D.Meloni,
Universe 7 (2021) no.7, 240

G.Altarelli, D.Meloni
Nucl. Phys. B809 (2009), 158-182

$$A_{\alpha\beta} \equiv \frac{P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)}{P(\nu_\alpha \rightarrow \nu_\beta) + P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)}$$

$$A_{\mu e}^{SM_0} = -\frac{12}{f_1} r \alpha \Delta_{31} \sin \delta \sin^2 \Delta_{31}$$

vacuum case

$$A_{\mu\tau}^{SM_0} = \frac{4}{3} r \alpha \Delta_{31} \sin \delta$$

$$s_{13} = \frac{r}{\sqrt{2}},$$
$$\alpha = \Delta m_{21}^2 / \Delta m_{31}^2$$

New sources of CP violation

Main ingredient:
Asymmetries

A.Giarnetti, D.Meloni,
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$$\left\{ \begin{array}{l} A_{\mu e}^{SM_0} = -\frac{12}{f_1} r \alpha \Delta_{31} \sin \delta \sin^2 \Delta_{31} \\ A_{\mu\tau}^{SM_0} = \frac{4}{3} r \alpha \Delta_{31} \sin \delta \end{array} \right. \quad \text{vacuum case}$$

$$s_{13} = \frac{r}{\sqrt{2}}, \quad \alpha = \Delta m_{21}^2 / \Delta m_{31}^2$$

matter case

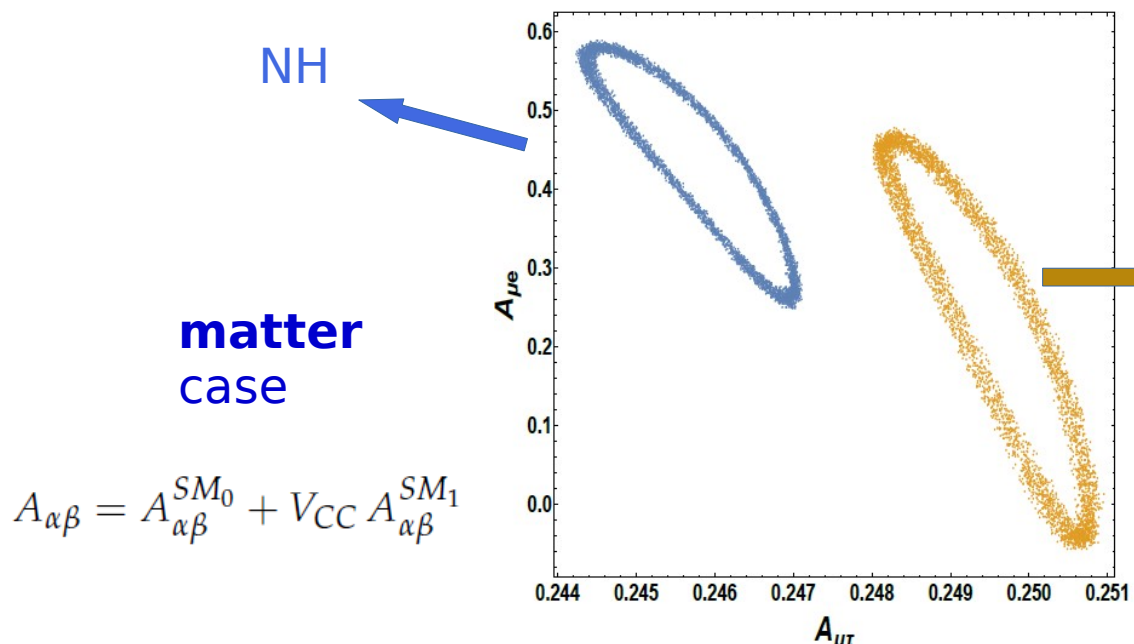
$$A_{\alpha\beta} = A_{\alpha\beta}^{SM_0} + V_{CC} A_{\alpha\beta}^{SM_1}$$

$$\left\{ \begin{array}{l} A_{\mu e}^{SM_1} = -\frac{6}{f_1} r (\Delta_{31} \cos \Delta_{31} - \sin \Delta_{31}) [2\alpha \Delta_{31} \cos \delta \cos \Delta_{31} + 3r \sin \Delta_{31} + \\ - \frac{24}{f_1} r \alpha^2 \sin^2 \delta \Delta_{31}^2 \sin^3 \Delta_{31}] , \\ A_{\mu\tau}^{SM_1} = -2r^2 (1 - \Delta_{31} \cot \Delta_{31}) + \frac{8}{27} \alpha^2 \Delta_{31}^3 \cot \Delta_{31} , \\ A_{\mu\mu}^{SM_1} = \frac{4}{3} r \alpha \Delta_{31} \cos \delta (\Delta_{31} - \tan \Delta_{31}) - \frac{8}{27} \alpha^2 \Delta_{31}^3 \tan \Delta_{31} . \end{array} \right.$$

See also:

J.Kopp et al., Phys.Rev.D77:013007,2008, T.Kikuchi et al.,JHEP 0903:114,2009, D.Meloni et al.,JHEP0904:033,2009, J.Liao et al., Phys.Rev.D93,093016(2016), P.Coloma, JHEP03(2016)016

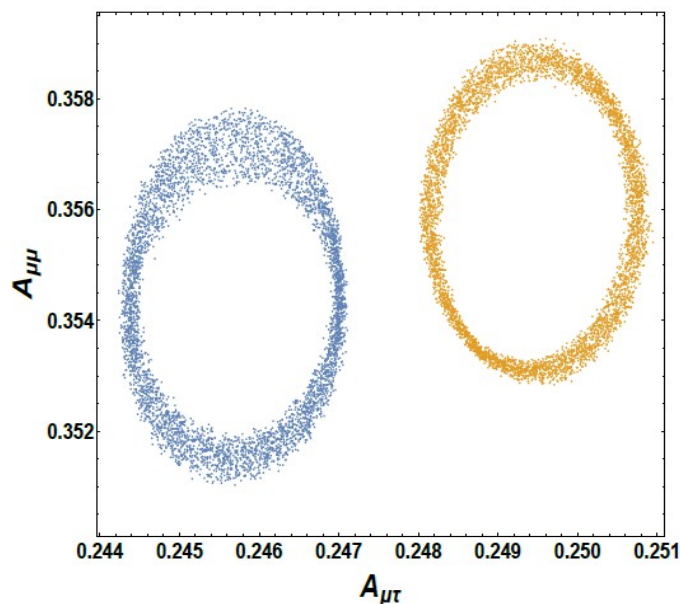
New sources of CP violation



a single sources
of CP violation:
closed curves

IH
Spread due to
experimental
uncertainties


Largest variation on $A_{\mu e}$



very small variation on $A_{\mu\mu}$
driven by matter effects

New sources of CP violation in NSI

modified matter potential

$$A_{CC} \begin{pmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}$$


3 more CP phases: $\varepsilon_{\mu\tau}$, $\varepsilon_{e\tau}$, $\varepsilon_{e\mu}$

$$A_{\alpha\beta} = A_{\alpha\beta}^{SM_0} + V_{CC}(A_{\alpha\beta}^{SM_1} + A_{\alpha\beta}^{NSI})$$



leading contribution from $\varepsilon_{\mu\tau}$

New sources of CP violation in NSI

modified matter potential

$$A_{CC} \begin{pmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}$$

$$A_{\alpha\beta} = A_{\alpha\beta}^{SM_0} + V_{CC}(A_{\alpha\beta}^{SM_1} + A_{\alpha\beta}^{NSI})$$

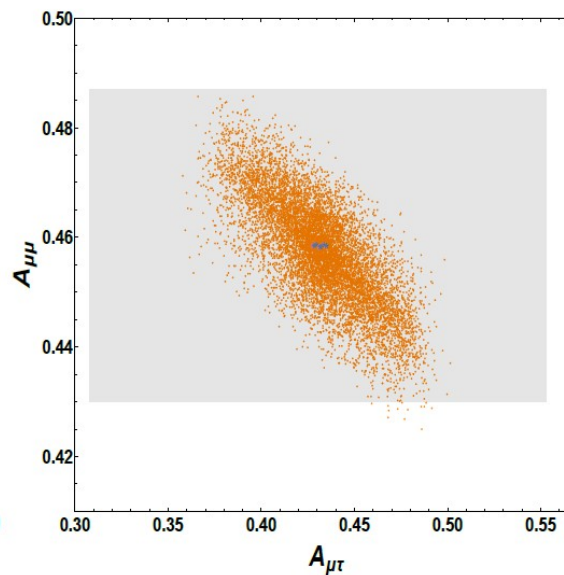
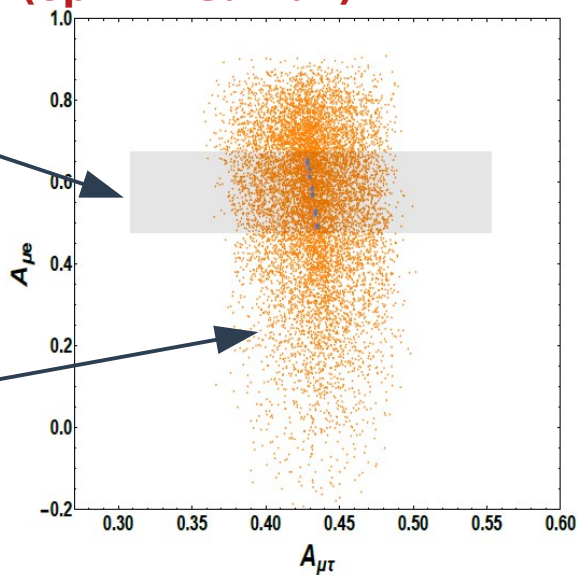
leading contribution from $\varepsilon_{\mu\tau}$

3 more CP phases: $\varepsilon_{\mu\tau}$, $\varepsilon_{e\tau}$, $\varepsilon_{e\mu}$

Now using integrated asymmetries in DUNE (optimized flux)

statistical errors on SM asy.

values in the NSI scenario



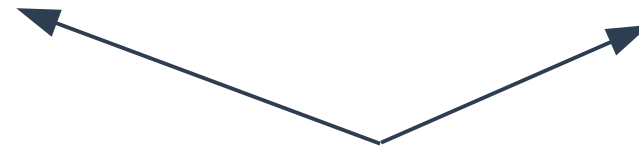
$A_{\mu e}$ is the most promising

and

more resolution on tau detection

New sources of CP violation in 3+1 scheme

$$U = R(\theta_{34})R(\theta_{24})R(\theta_{23}, \delta_3)R(\theta_{14})R(\theta_{13}, \delta_2)R(\theta_{12}, \delta_1)$$



two new sources of CP violation

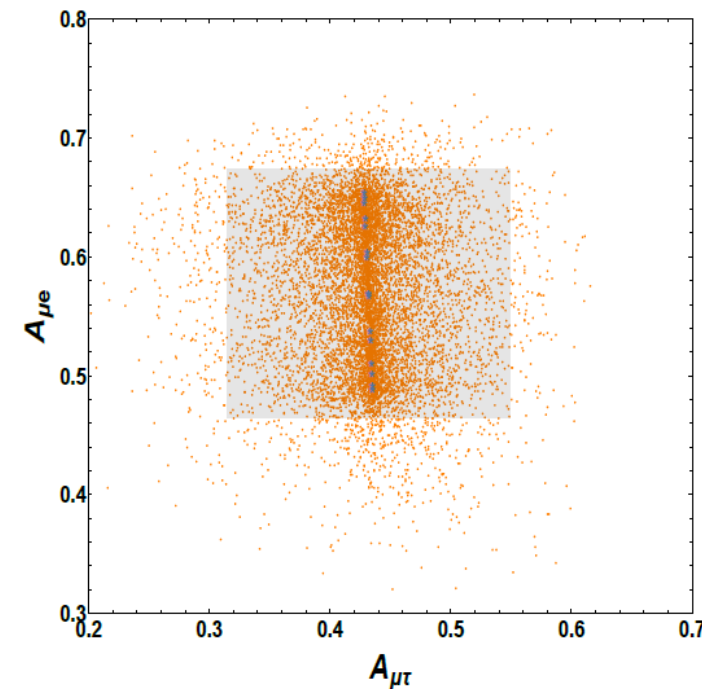
$$A_{\mu e}^{3+1} \sim \frac{s_{14}s_{24}}{f_1} \left\{ -6[2\alpha\Delta_{31} \sin \delta_1 + 3r \cos \Delta_{31} \sin(\delta_2 - \delta_3) \sin \Delta_{31}] \right\} +$$

$$\frac{s_{14}s_{24}}{f_1^2} \left\{ 216r^2\alpha\Delta_{31} \cos(\delta_2 - \delta_3) \sin(\delta_1 - \delta_2 + \delta_3) \sin^4 \Delta_{31} \right\},$$

$$A_{\mu\tau}^{3+1} = 2s_{24}s_{34} \cot \Delta_{31} (\sin \delta_3 - 2V_{NC}\Delta_{31} \cos \delta_3),$$

$$A_{\mu\mu}^{3+1} = 4s_{24}s_{34}V_{NC}\Delta_{31} \cos \delta_3 \tan \Delta_{31}.$$

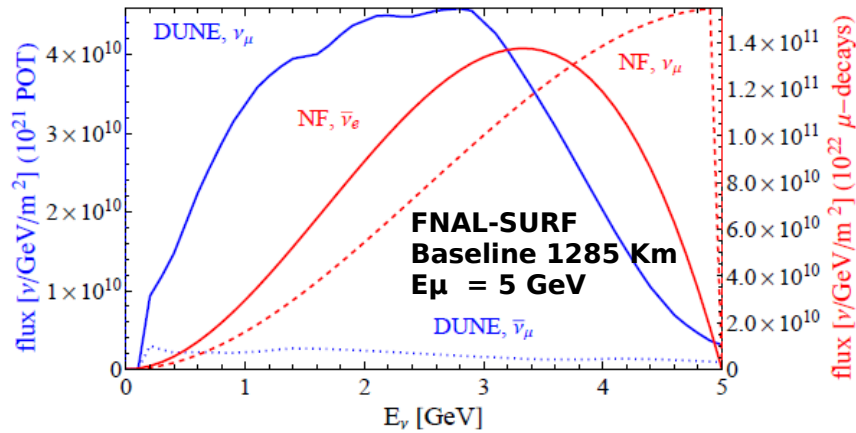
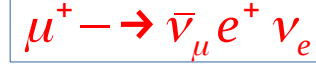
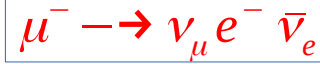
$A_{\mu e}$ and $A_{\mu\tau}$ are good candidates



Neutrino Factory & NSI

Denton et al.,
Nucl. Phys. B 1018 (2025), 117040

Nucl. Phys. B 1012 (2025), 116818



- neutrino energies reach higher energies than a fixed target
- spectrum is different with part of it rising to the maximum
- the composition and the expected energy of the neutrino beam is a 3 body decay
- no $\nu\tau$ get produced in the source, allowing for cleaner searches for $\nu\tau$ appearance

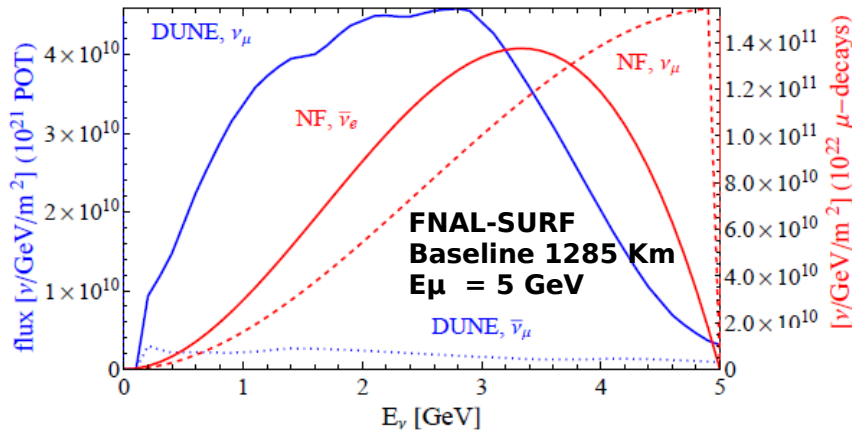
Neutrino Factory & NSI

Denton et al.,
 Nucl. Phys. B 1018 (2025), 117040
 Nucl. Phys. B 1012 (2025), 116818

$$\mu^- \rightarrow \nu_\mu e^- \bar{\nu}_e$$

$$\mu^+ \rightarrow \bar{\nu}_\mu e^+ \nu_e$$

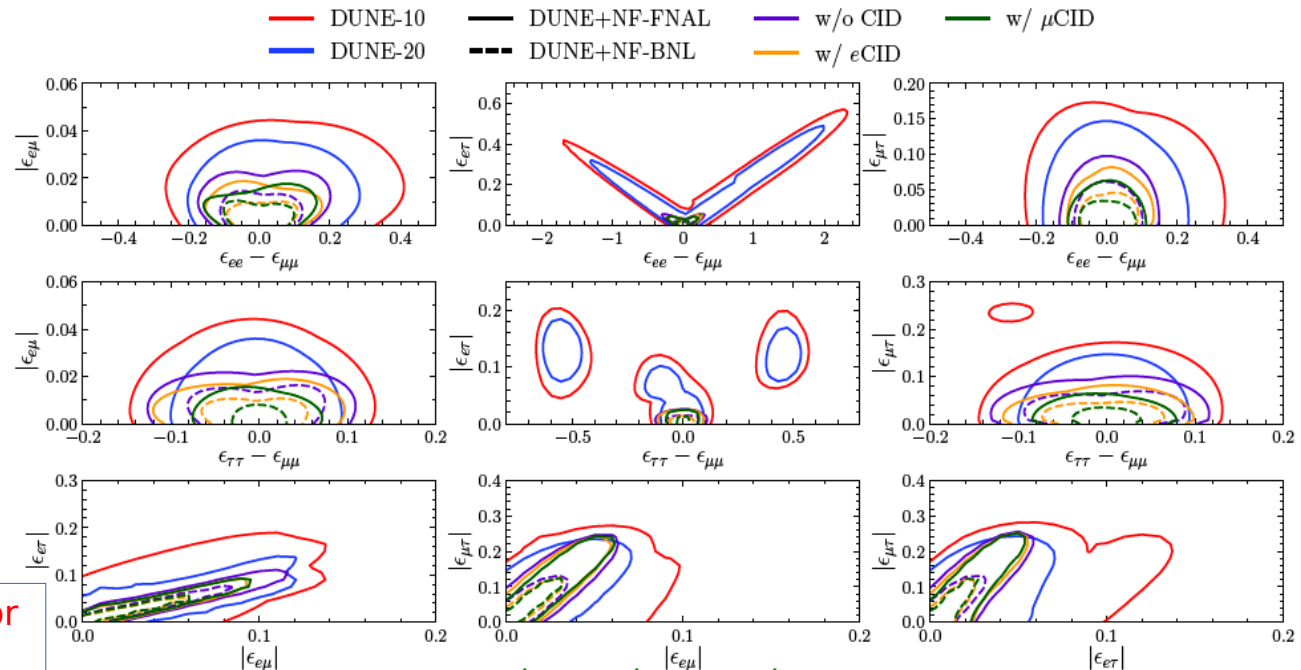
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- spectrum is different with part of it rising to the maximum
- the composition and the expected energy of the neutrino beam is a 3 body decay
- no $\nu\tau$ get produced in the source, allowing for cleaner searches for $\nu\tau$ appearance



10^{21} muon (or anti-muon) decays per year

far detector is a LArTPC configuration with a total fiducial target mass of 40 kT

the sensitivity can be improved by a factor of ~ 2 compared to DUNE with 20 years running time



experimental constraint on different combinations of two NSI

Distinguishing New Physics models at DUNE

Strategy: assume that one of the benchmark new physics points represents reality and then attempt to reconstruct it in a different new physics scenario

$\Delta\chi^2$		scalar NSI						sterile
	SM	$\eta_{e\mu}$	$\eta_{e\tau}$	$\eta_{\mu\tau}$	$\epsilon_{e\mu}$	$\epsilon_{e\tau}$	$\epsilon_{\mu\tau}$	3+1
$\epsilon_{e\mu}$ NO	200	140	140	170	/	180	160	80
$\epsilon_{e\tau}$ NO	60	48	50	45	50	/	50	40
$\epsilon_{\mu\tau}$ NO	200	180	170	180	160	180	/	80
$\epsilon_{e\mu}$ IO	170	80	75	90	/	10	13	3
$\epsilon_{e\tau}$ IO	70	50	50	45	45	/	60	20
$\epsilon_{\mu\tau}$ IO	500	400	400	400	300	350	/	160

data could not be well fit with a different New Physics model

Reality: vector NSI from Nova and T2K

Distinguishing New Physics models at DUNE

Strategy: assume that one of the benchmark new physics points represents reality and then attempt to reconstruct it in a different new physics scenario

$\Delta\chi^2$	SM	$\eta_{e\mu}$	$\eta_{e\tau}$	$\eta_{\mu\tau}$	vector NSI			sterile
					$\epsilon_{e\mu}$	$\epsilon_{e\tau}$	$\epsilon_{\mu\tau}$	3+1
$\eta_{e\mu}$ NO	0.14	/	0.005	0.088	0.071	0.033	0.055	0.02
$\eta_{e\tau}$ NO	0.08	0.003	/	0.041	SM	SM	SM	0.01
$\eta_{\mu\tau}$ NO	0.60	0.48	0.48	/	SM	SM	SM	0.02
$\eta_{e\mu}$ IO	100	/	4.7	6.3	80	70	90	21
$\eta_{e\tau}$ IO	60	1.0	/	1.5	44	38	50	11
$\eta_{\mu\tau}$ IO	30	4.6	4.8	/	23	20	29	12

there is some confusions for particular choices

Reality: scalar NSI from Nova and T2K

Conclusions

- about the “current” PMNS parameters known with sufficient precision but the θ_{23} & CP phase
- about the “future” PMNS improvements on the measure of CP phase crucial for model building
- about “new physics” in 20 years from now, either we discern small variations from the standard picture or the SM is likely to be valid up to the Planck scale

Neutrino Factory & CPT violation

Denton et al.,
Nucl. Phys. B 1018 (2025), 117040

neutrinos are
described by $x \in \{\theta_{ij}, \delta_{CP}, \Delta m_{ij}^2\}$

anti-neutrinos are
associated with $\bar{x} \in \{\bar{\theta}_{ij}, \bar{\delta}_{CP}, \Delta \bar{m}_{ij}^2\}$

CPT conserved \rightarrow all parameters are
the same but a“-” sign on the phase

limits on CPT violation are
obtained by evaluating

$$\chi^2(|\Delta x|) = \chi^2(|x - \bar{x}|) = \chi_\nu^2(x) + \chi_{\bar{\nu}}^2(\bar{x})$$

Neutrino Factory & CPT violation

Denton et al.,
Nucl. Phys. B 1018 (2025), 117040

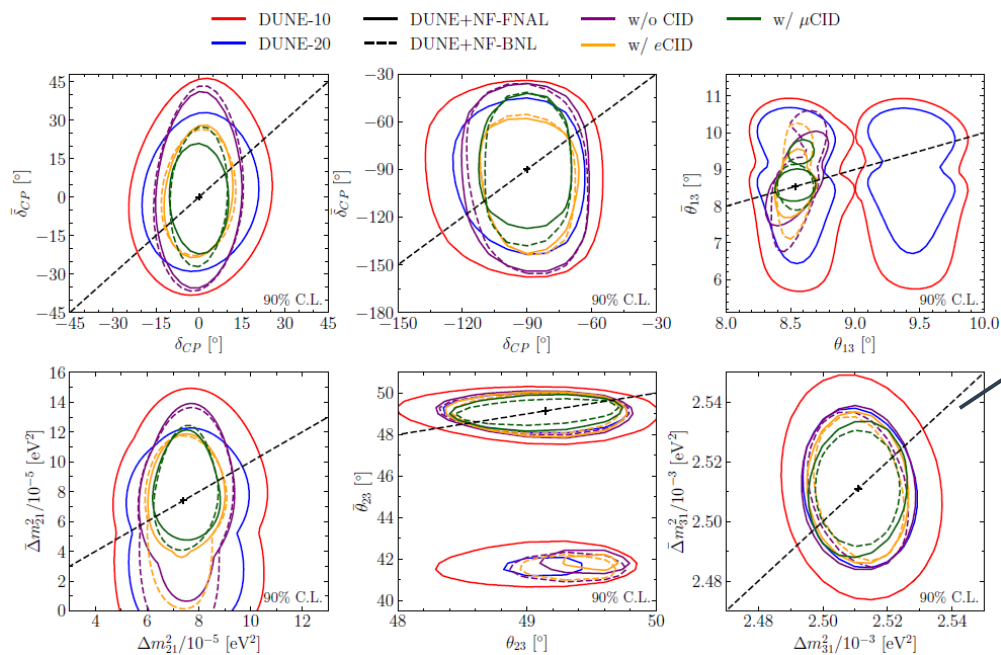
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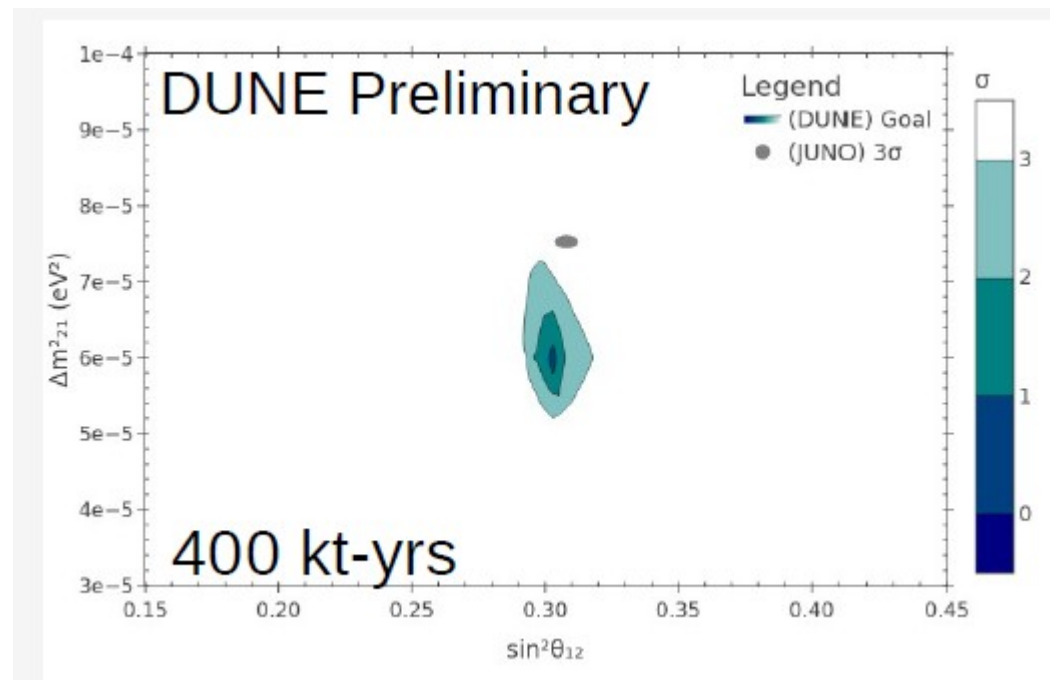
experimental sensitivity to the difference between the oscillation parameters for neutrino and anti neutrinos

CPT conserving line

the addition of a NF to DUNE improves the precision on the oscillation parameters for neutrinos and antineutrinos simultaneously

Dune & solar neutrinos

DUNE sensitivity to solar neutrinos



Some experimental setup

Agarwalla et al. Eur. Phys. J. C (2023) 83:694

Table 2 Essential experimental features of various long-baseline experiments considered in our analysis. The first column characterizes DUNE, while the second column depicts aspects of JD and KD

Characteristics	DUNE	JD/KD
Baseline (km)	1285	295 (1100)
ρ_{avg} (g/cm ³)	2.848	2.7 (2.8)
Beam	LBNF [16]	J-PARC [57]
Beam type	Wide-band, on-axis	Narrow-band, 2.5° off-axis
Beam power	1.2 MW	1.3 MW
Proton energy	120 GeV	30 GeV
P.O.T./year	1.1×10^{21}	2.7×10^{22}
Flux peaks at (GeV)	2.5	0.6
1st (2nd) oscillation maxima for appearance channel (GeV)	2.6 (0.87)	0.6 (0.2)/1.8 (0.6)
Detector mass (kt)	40, LArTPC	187 each, water Cherenkov
Runtime ($\nu + \bar{\nu}$) yrs	5 + 5	2.5 + 7.5
Exposure (kt·MW·yrs)	480	2431
Signal norm. error (App.)	2%	5%
Signal norm. error (Disapp.)	5%	3.5%
Binned-events matched with	[19]	[23]

Table 3 Total appearance event rates (signal + background) in neutrino, antineutrino modes, and $\mathcal{N}_{\text{CP}}^{\mu e}$ for DUNE (JD) corresponding to different sets of $\delta_{\text{CP}} : 0^\circ, 90^\circ, -90^\circ$ and $\theta_{23} : 40^\circ, 45^\circ, \text{ and } 50^\circ$ are shown in the second (third) set of rows, respectively

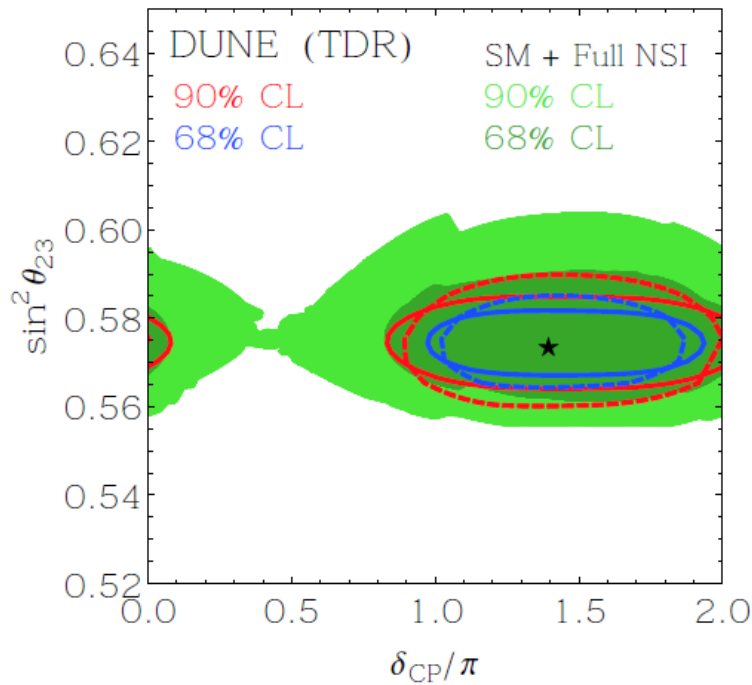
Experiment	Parameter	$\mathcal{N}_{\text{CP}}^{\mu e}$		
		θ_{23}	$\delta_{\text{CP}} = 0^\circ (\nu_e, \bar{\nu}_e, \mathcal{N}_{\text{CP}}^{\mu e})$	$\delta_{\text{CP}} = 90^\circ (\nu_e, \bar{\nu}_e, \mathcal{N}_{\text{CP}}^{\mu e})$
DUNE	40°	1965, 812, 0.41	1657, 857, 0.31	2303, 728, 0.52
	45°	2215, 875, 0.43	1902, 920, 0.34	2558, 790, 0.53
	50°	2470, 938, 0.45	2161, 982, 0.37	2807, 854, 0.53
JD	40°	1644, 1420, 0.074	1277, 1687, -0.14	2024, 1113, 0.29
	45°	1890, 1594, 0.085	1517, 1868, -0.1	2276, 1286, 0.28
	50°	2137, 1770, 0.093	1770, 2041, -0.07	2518, 1476, 0.26

Limits on NC NSI and correlation with the SM

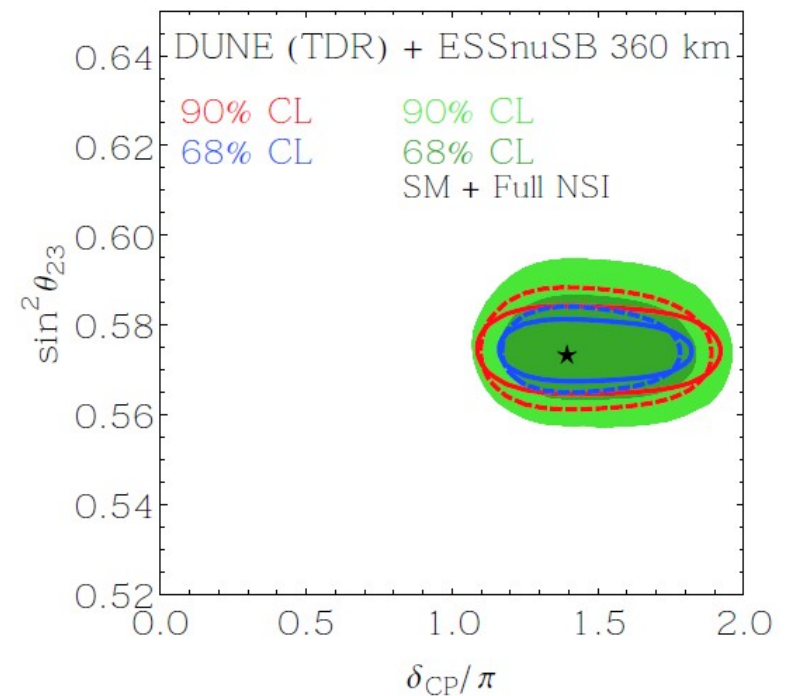
Singha et al. 2112.04876

$$\left(\begin{array}{l} |\epsilon_{ee}| < 4 \times 10^0 \quad |\epsilon_{e\mu}| < 3 \times 10^{-1} \quad |\epsilon_{e\tau}| < 3 \times 10^0 \\ \quad \quad \quad |\epsilon_{\mu\mu}| < 7 \times 10^{-2} \quad |\epsilon_{\mu\tau}| < 3 \times 10^{-1} \\ \quad \quad \quad \quad \quad \quad |\epsilon_{\tau\tau}| < 2 \times 10^1 \end{array} \right)$$

L.A. Delgadillo and O.G.Miranda
PRD108 (095024)

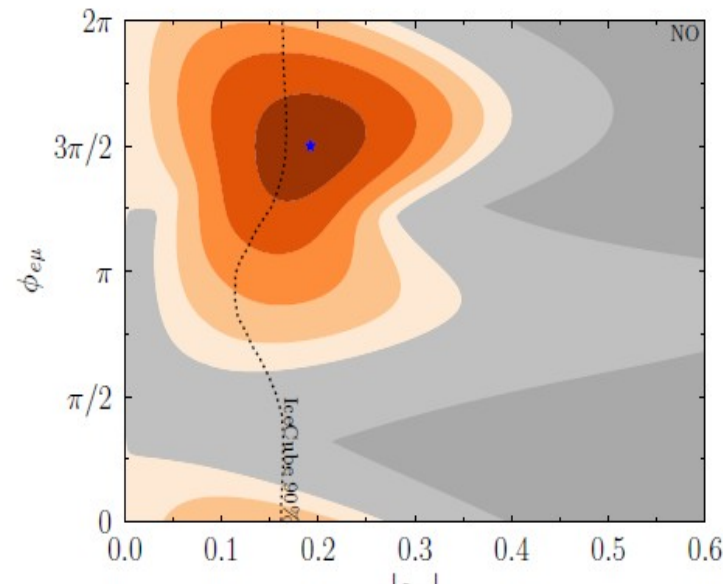


synergy



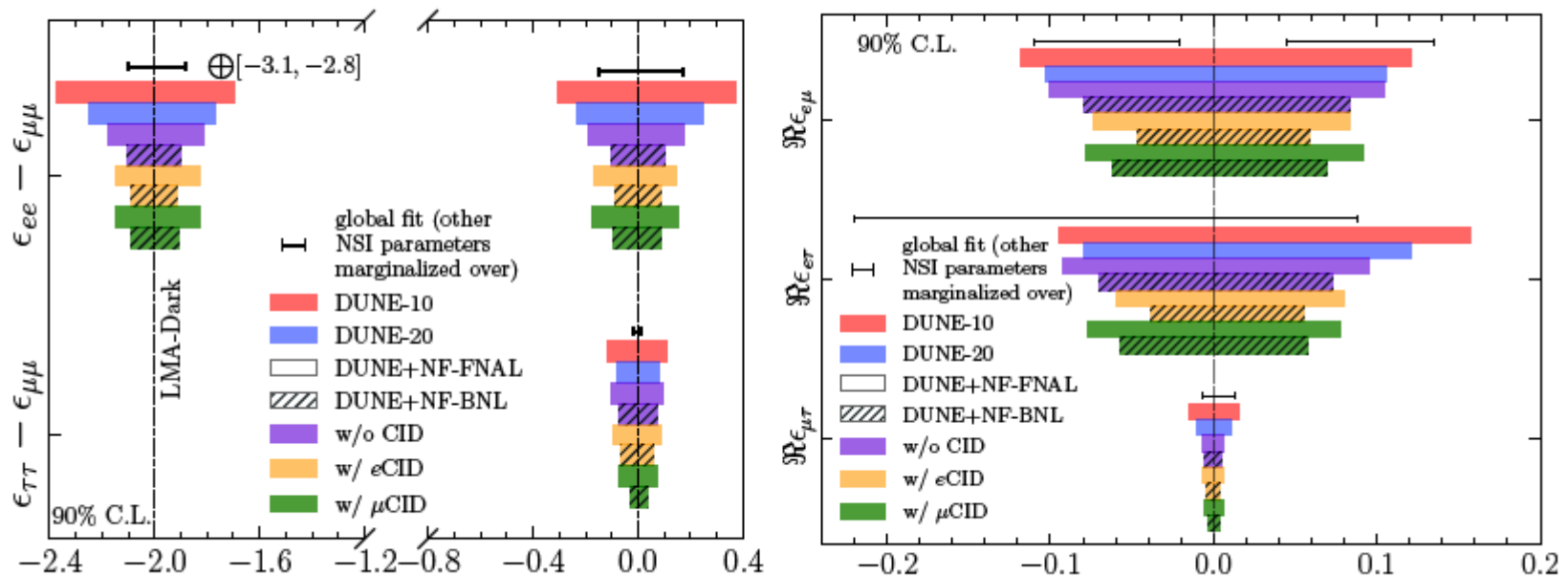
NoVA-T2K tension on delta CP

Denton et al.,
PhysRevLett.126.051801



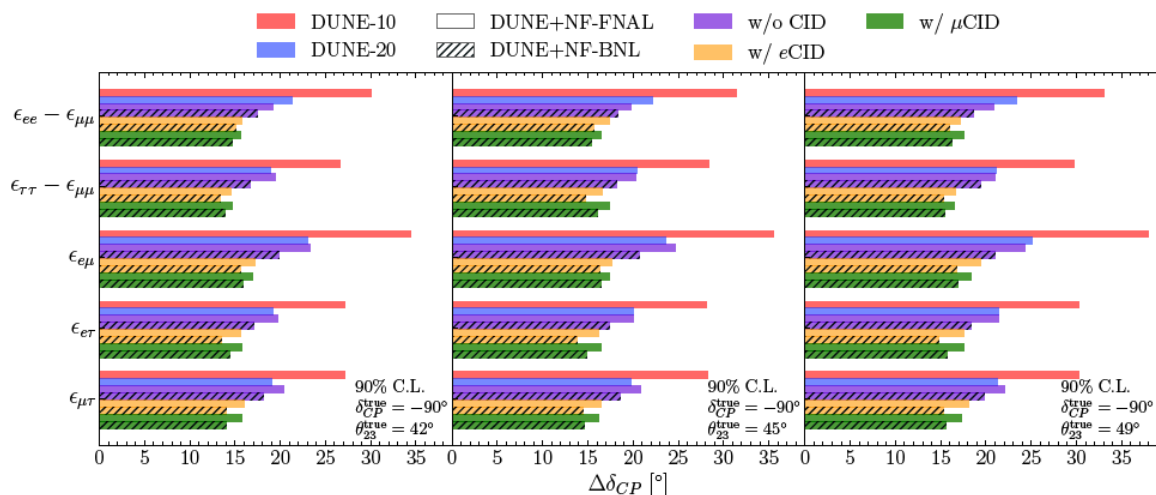
tension in the recent
NOvA and T2K data
solved by complex
NSI

Denton et al.,2502.14027,
NSI at NuFact

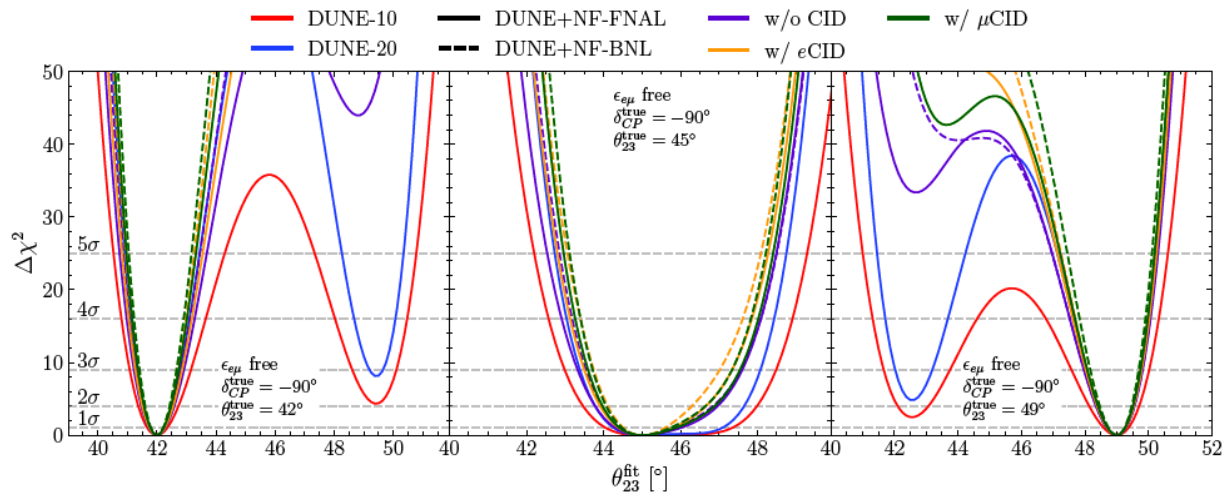


Effects of NSI on delta CP measurement

Denton et al., 2502.14027,
NSI at NuFact

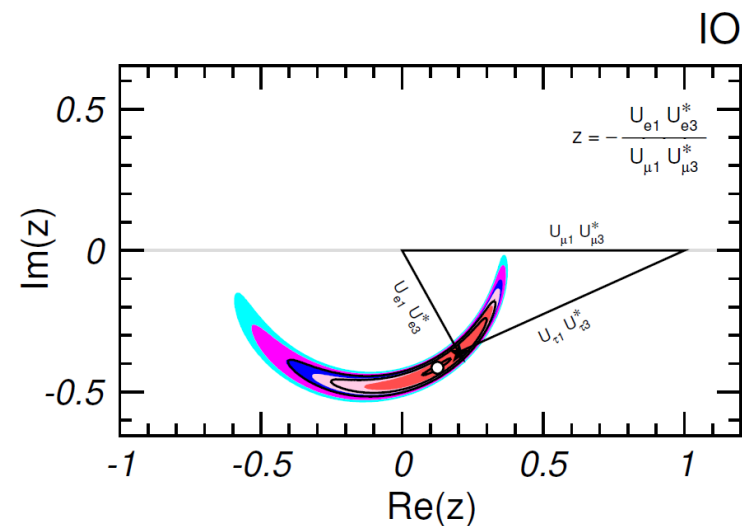
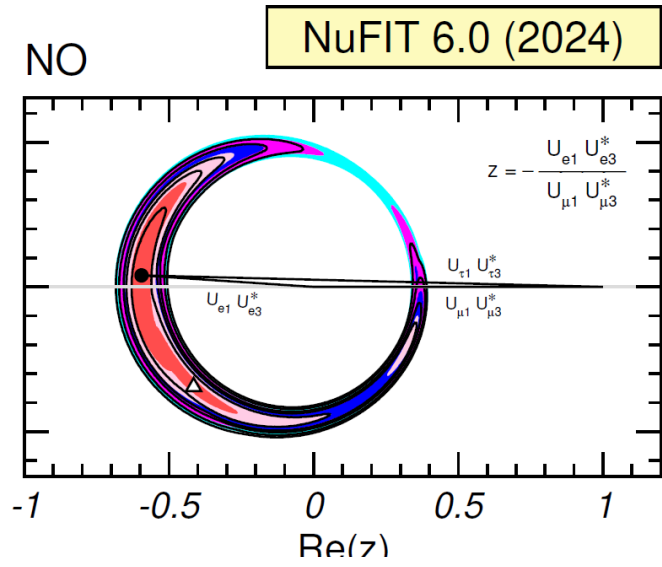
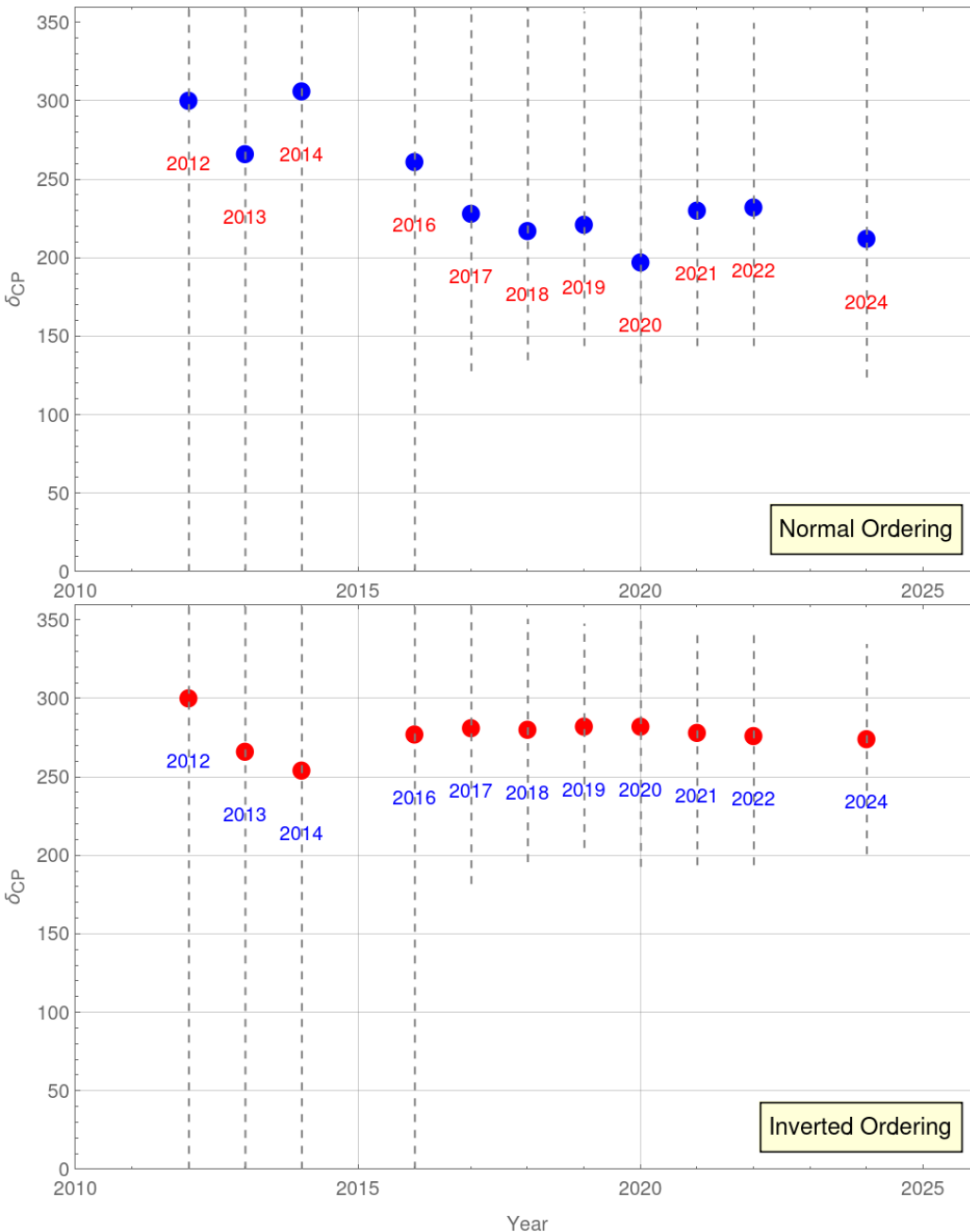


Expected sensitivity
on deltaCP



experimental
sensitivity to theta23

What we know: δ_{CP}

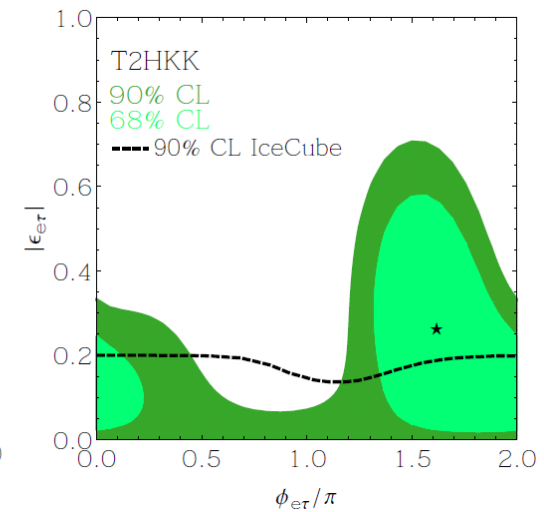
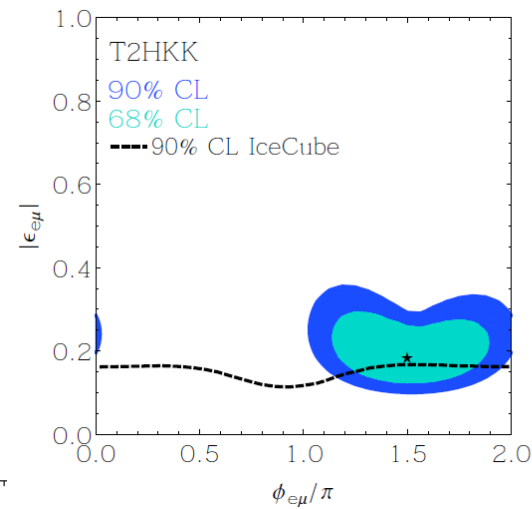
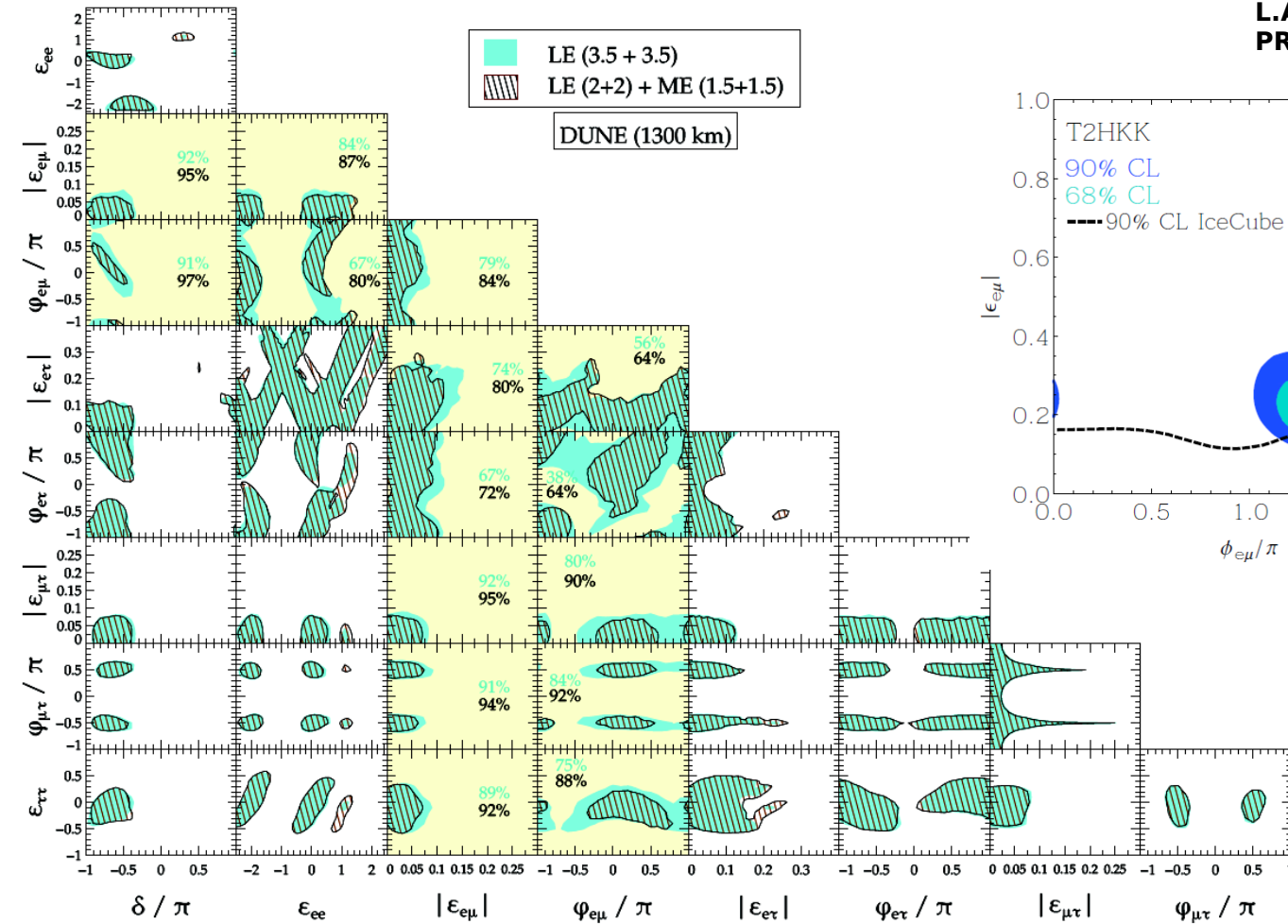


- weak indications:
 IO seems to prefer maximal CP violation
 while NO a CP conserving solution

New sources of CP violation in NSI

M.Masud, S.Roy and P.Mehta,
Phys. Rev. D99 (2019) no.11, 115032

L.A. Delgadillo and O.G.Miranda
PRD108 (095024)



difficult to strongly
constrain CP phases