

Correlations and fluctuations from lattice QCD

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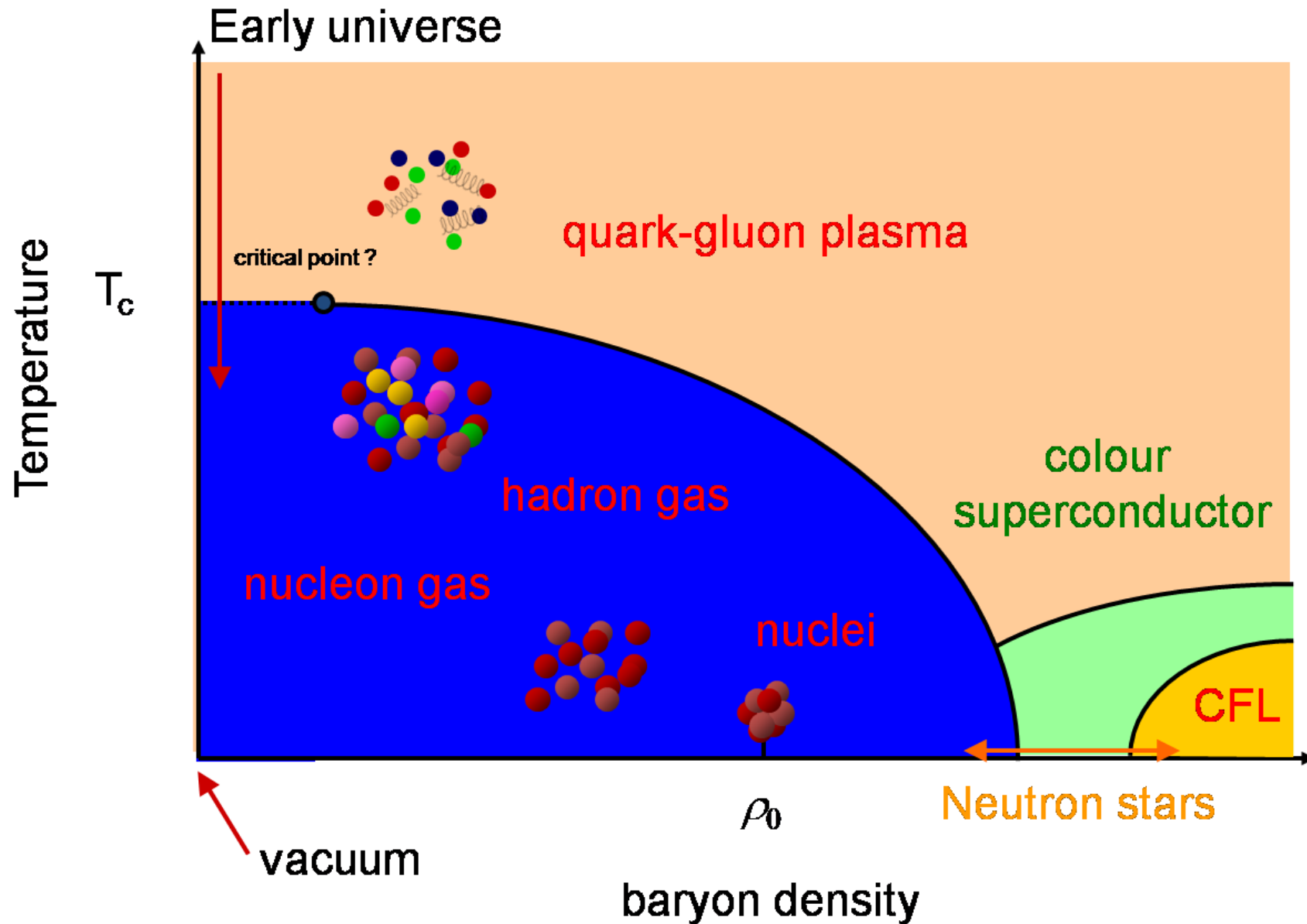
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In collaboration with: S. Borsanyi, Z. Fodor, S. Katz, S. Krieg, K. Szabó
(Wuppertal-Budapest collaboration); arXiv: 1112.4416 (JHEP 2012)

Motivation

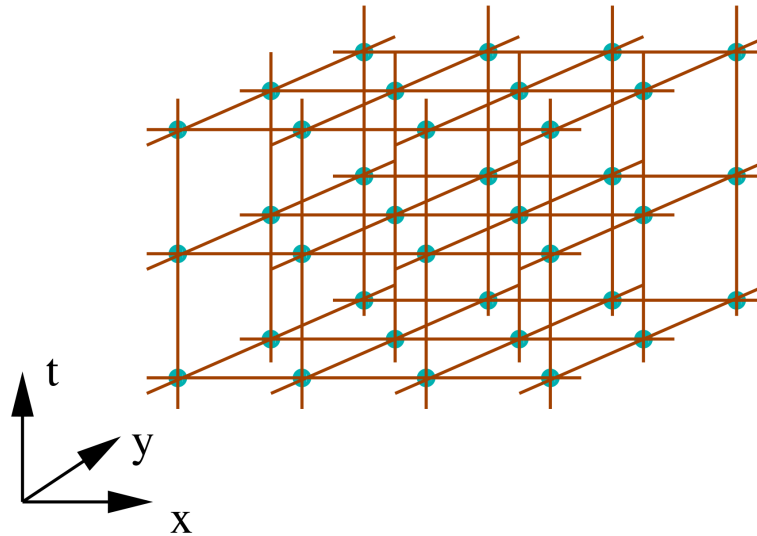
- ❖ We live in a **very exciting era** to understand the fundamental constituents of matter and the evolution of the Universe
- ❖ We can create the **deconfined phase of QCD** in the laboratory
- ❖ Lattice QCD simulations have reached unprecedented levels of accuracy
 - ➡ physical quark masses
 - ➡ several lattice spacings → continuum limit
- ❖ The joint information between **theory** and **experiment** can help us to shed light on QCD

The QCD phase diagram



Discretization of space-time

- ❖ Simplest: isotropic hypercubic grid with spacing $a = a_S = a_T$ and size $N_S \times N_S \times N_S \times N_T$.



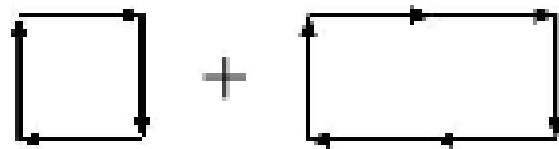
- ❖ Physical size of the lattice: $L = N_S a$
- ❖ Temperature: $T = \frac{1}{N_T a}$
- ❖ N_T large $\Rightarrow a$ small: closer to continuum limit but **computationally expensive**

Choice of the action

- ❖ **no consensus**: which action offers the most cost effective approach

Aoki, Fodor, Katz, Szabo, JHEP 0601, 089 (2006)

- ❖ **our choice** tree-level $O(a^2)$ -improved Symanzik gauge action



2-level (stout) smeared improved staggered fermions

$$V = P \left[\longrightarrow + \rho \left(\begin{array}{c} \nearrow \\ \searrow \end{array} + \begin{array}{c} \nwarrow \\ \swarrow \end{array} + \begin{array}{c} \uparrow \\ \downarrow \end{array} + \begin{array}{c} \leftarrow \\ \rightarrow \end{array} \right) \right]$$

Quark number susceptibilities

- ❖ The **deconfined phase** of QCD can be reached in the laboratory
- ❖ Need for **unambiguous observables** to identify the phase transition
 - ❖ susceptibilities of conserved charges (baryon number, electric charge, strangeness)
S. Jeon and V. Koch (2000), M. Asakawa, U. Heinz, B. Müller (2000)
- ❖ A rapid change of these observables in the vicinity of T_c provides an unambiguous signal for **deconfinement**
- ❖ These observables are sensitive to the **microscopic structure of the matter**
 - ➡ non-diagonal correlators give information about **presence of bound states** in the QGP
- ❖ They can be measured **on the lattice** as combinations of **quark number susceptibilities**

The observables under study

❖ The chemical potentials are related:

$$\begin{aligned}\mu_u &= \frac{1}{3}\mu_B + \frac{2}{3}\mu_Q; \\ \mu_d &= \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q; \\ \mu_s &= \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q - \mu_S.\end{aligned}$$

❖ susceptibilities are defined as follows:

$$\chi_{lmn}^{BSQ} = \frac{\partial^{l+m+n} p / T^4}{\partial(\mu_B/T)^l \partial(\mu_S/T)^m \partial(\mu_Q/T)^n}.$$

❖ Here we concentrate on the **quadratic susceptibilities**

$$\chi_2^X = \frac{1}{VT^3} \langle N_X^2 \rangle$$

❖ and on the correlators between different charges

$$\chi_{11}^{XY} = \frac{1}{VT^3} \langle N_X N_Y \rangle.$$

diagonal and non-diagonal

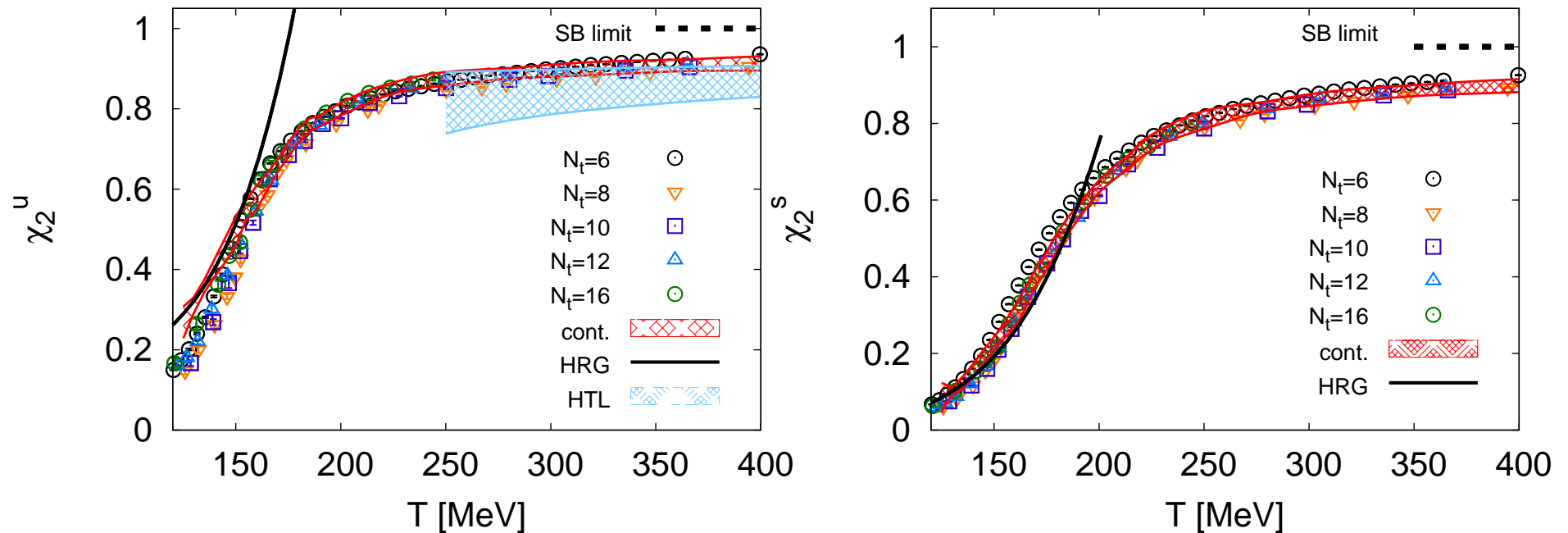
quark number susceptibilities

$N_f = 2 + 1$ dynamical quark flavors

$$m_s/m_{u,d} = 28.15$$

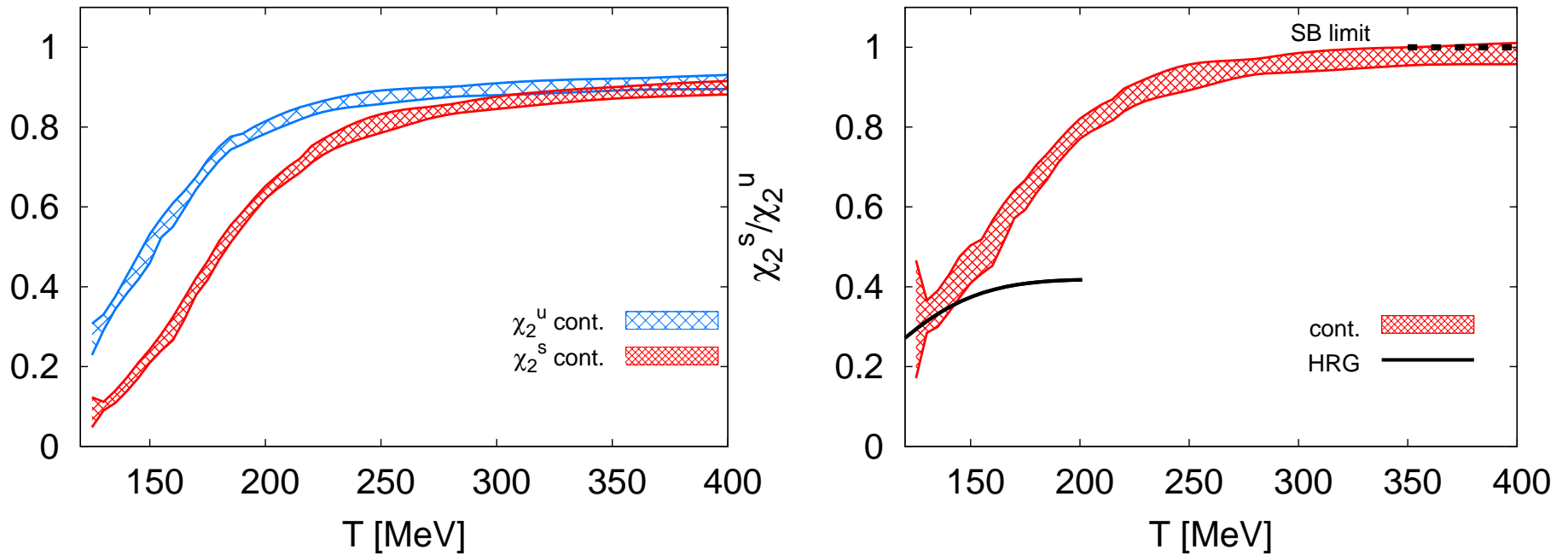
Results: light and strange quark susceptibilities

$$\chi_2^u = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_u \partial \mu_u} \Big|_{\mu_i=0} \quad \chi_2^s = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_s^2} \Big|_{\mu_i=0}$$



- ◆ quark number susceptibilities exhibit a **rapid rise** close to T_c
- ◆ at **large T** they reach $\sim 90\%$ of the ideal gas limit

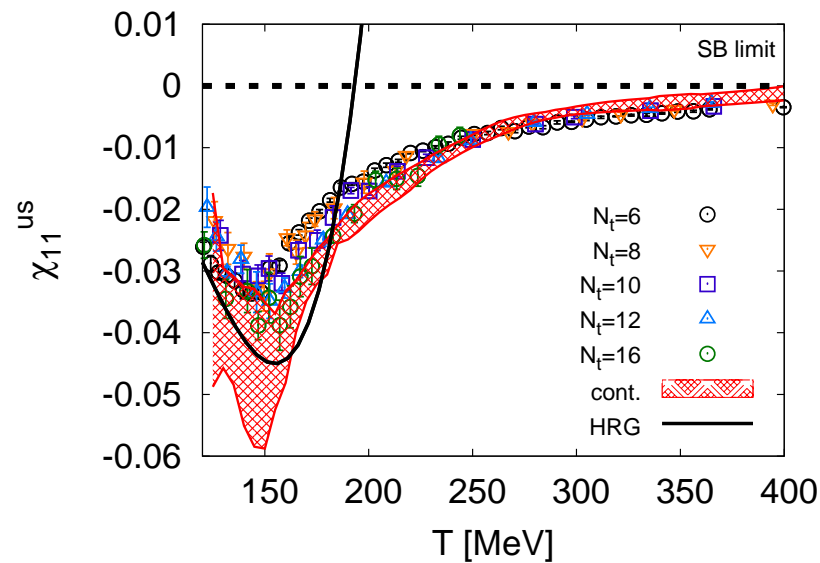
Comparison between light and strange quark susceptibilities



- ❖ strange quark susceptibilities have their rapid rise **at larger temperatures** compared to the light quark ones
- ❖ they **rise more slowly** as a function of T

Results: nondiagonal susceptibilities

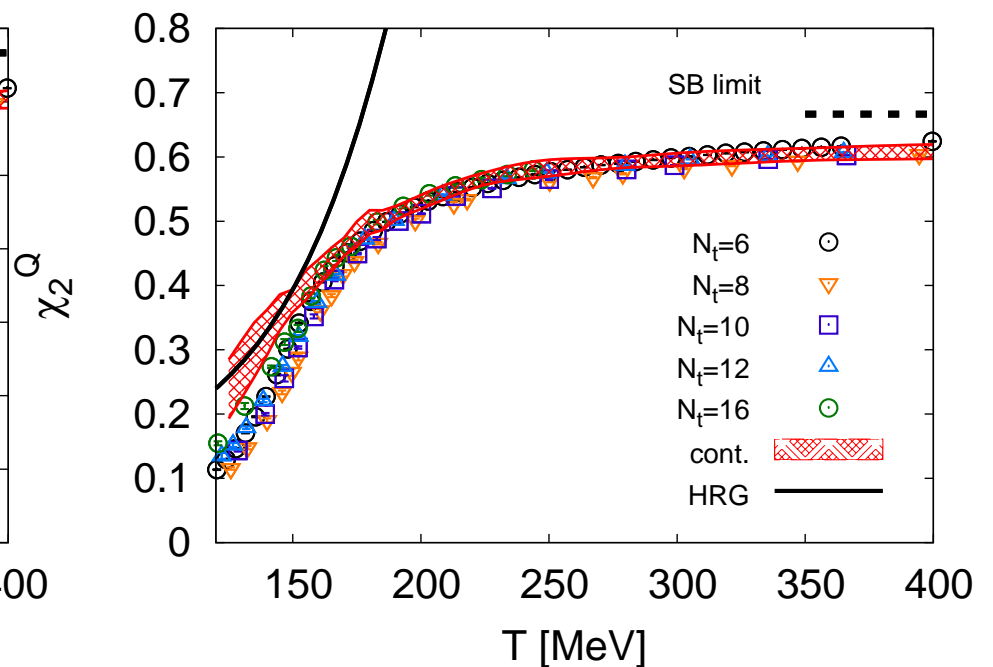
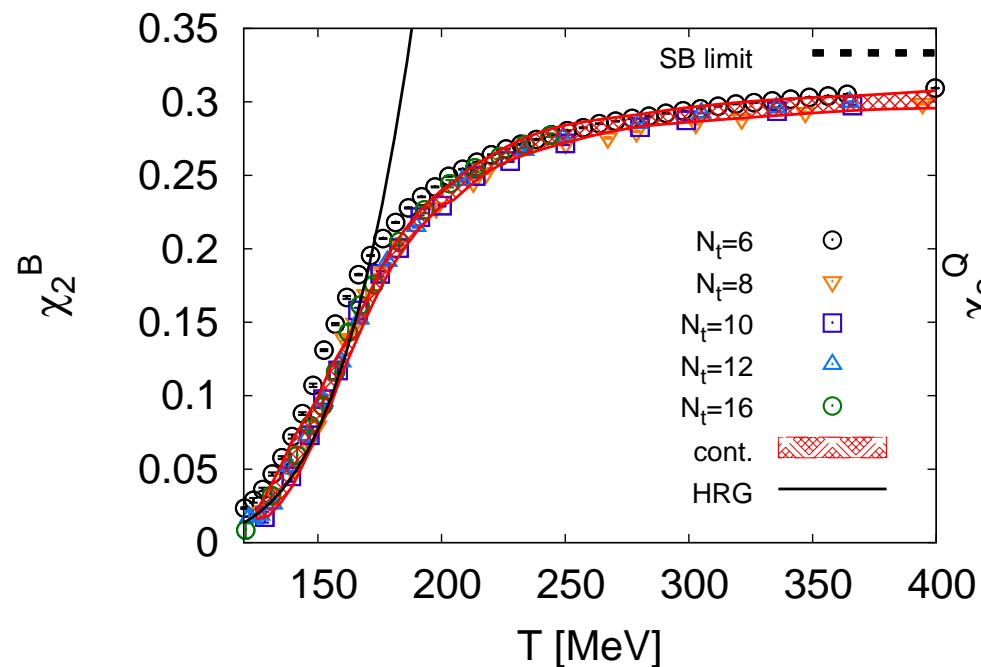
$$\chi_{11}^{us} = \chi_{11}^{ds} = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_u \partial \mu_s} \Big|_{\mu_i=0}$$



- ❖ non-diagonal susceptibilities look at the linkage between **different flavors**
- ❖ they exhibit a strong dip in the vicinity of T_c
- ❖ they vanish **in the QGP phase** at large temperatures

Results: susceptibilities of baryon number and electric charge

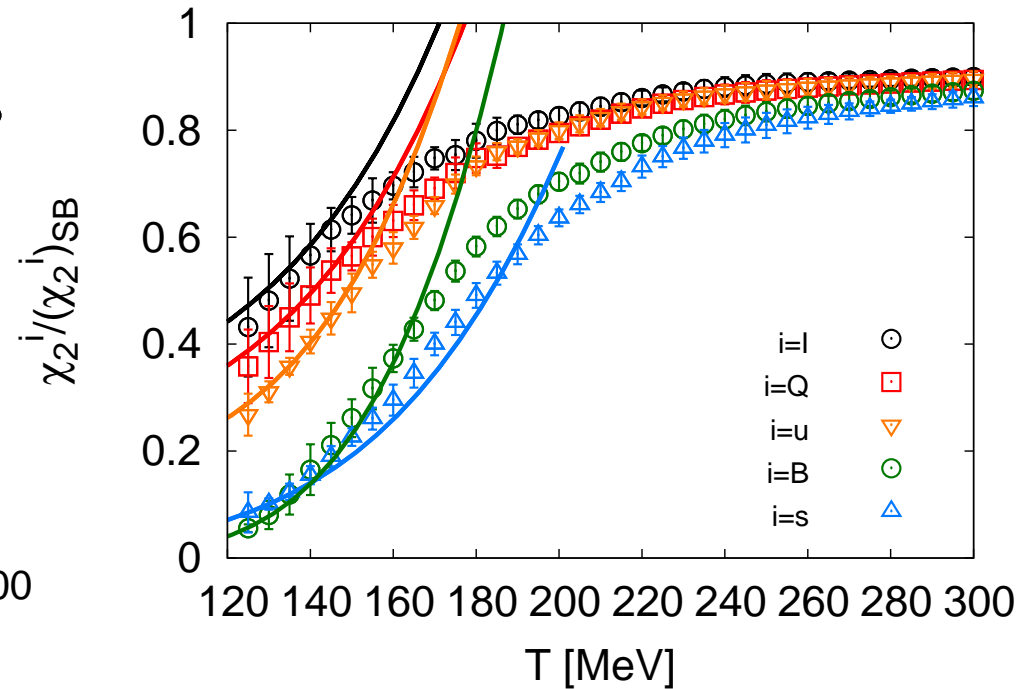
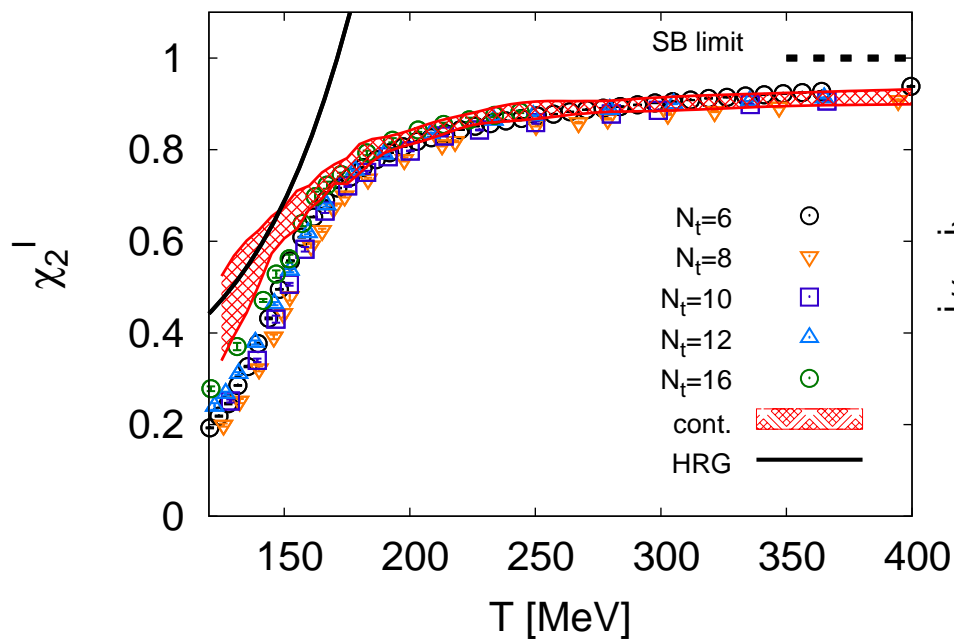
$$\chi_2^B = \frac{1}{9} (2\chi_2^u + \chi_2^s + 2\chi_{11}^{ud} + 4\chi_{11}^{us}); \quad \chi_2^Q = \frac{1}{9} (5\chi_2^u + \chi_2^s - 4\chi_{11}^{ud} - 2\chi_{11}^{us})$$



- ◆ rapid rise around T_c
- ◆ It reaches $\sim 90\%$ of ideal gas value at large temperatures

Results: isospin susceptibility

$$\chi_2^I = \frac{1}{2} (\chi_2^u - \chi_{11}^{ud})$$



- ◆ rapid rise around T_c
- ◆ It reaches $\sim 90\%$ of ideal gas value at large temperatures

Testing the presence of bound states in the QGP

We define the following object

$$C_{BS} = -3 \frac{\langle BS \rangle}{\langle S^2 \rangle}$$

V. Koch, A. Majumder, J. Randrup, PRL95 (2005).

In a QGP phase:

$$\blacklozenge -3\langle BS \rangle = \langle (n_{\bar{s}} - n_s)^2 \rangle$$

$$\langle S^2 \rangle = \langle (n_{\bar{s}} - n_s)^2 \rangle$$

at **all** T and μ

$$C_{BS} = 1$$

In hadron gas phase:

$$\blacklozenge -3\langle BS \rangle = 3[\Lambda + \bar{\Lambda} + \Sigma + \bar{\Sigma} + \dots] + 6[\Xi + \bar{\Xi} + \dots] + 9[\Omega + \bar{\Omega} + \dots]$$

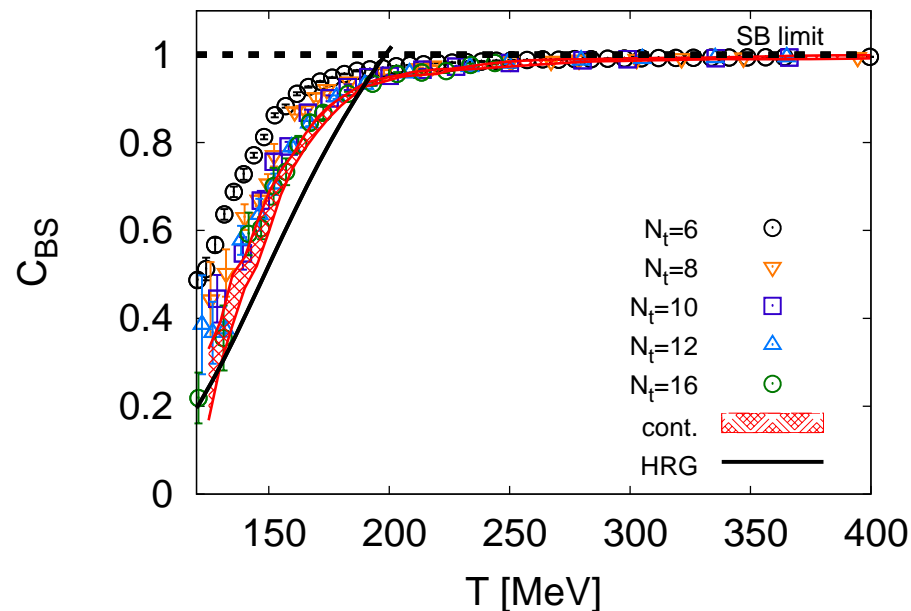
$$\langle S^2 \rangle = K^+ + K^- + K^0 + \Lambda + \bar{\Lambda} + \dots$$

at $T \simeq T_c$ and $\mu = 0$

$$C_{BS} = 0.66$$

Results: baryon-strangeness correlator

$$C_{BS} = 1 + \frac{\chi_{11}^{us} + \chi_{11}^{ds}}{\chi_2^s}$$



- ❖ C_{BS} indicates the possibility of **bound states** in a certain window above T_c
- ❖ there is a window of about **100 MeV above the transition** where $C_{BS} < 1$

charm quark susceptibilities

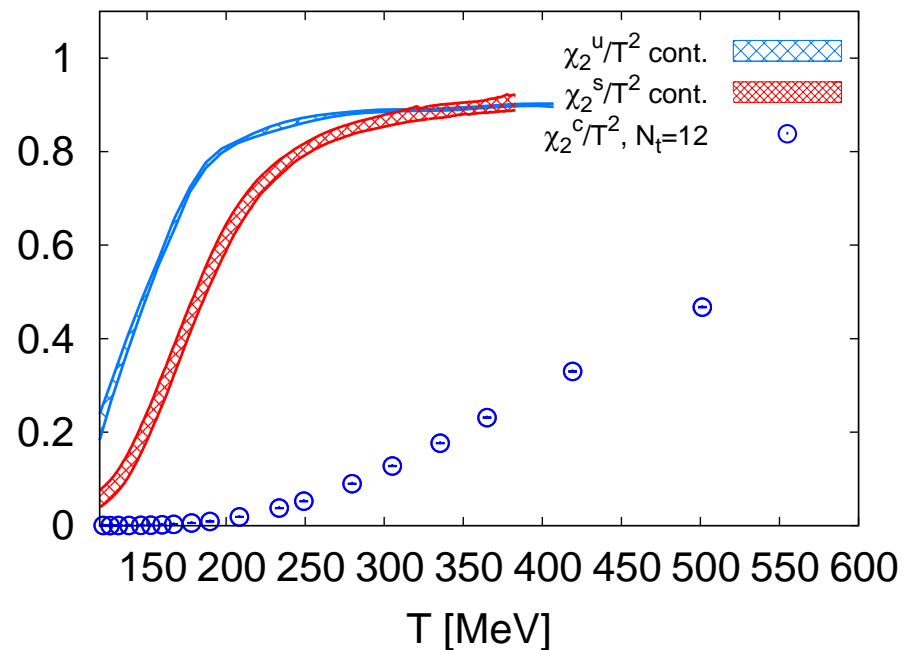
$$N_f = 2 + 1 + 1$$

with partial quenched charm

$$m_c/m_s = 11.85$$

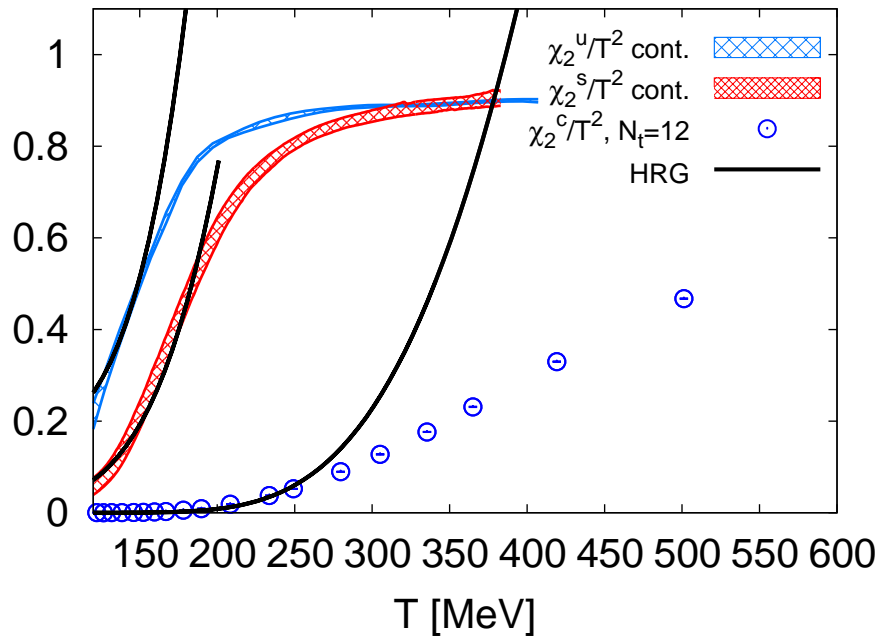
Charm quark number susceptibilities

$$\chi_2^c = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_c \partial \mu_c} \Big|_{\mu_i=0}$$



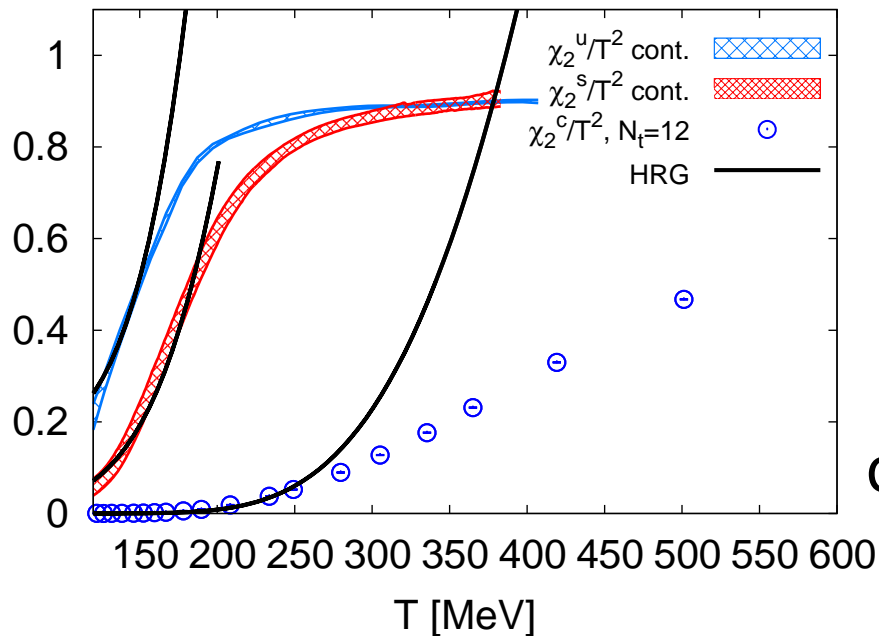
- ❖ charm susceptibilities rise at **much larger temperatures** compared to the light quark ones
- ❖ their rise with temperature is much slower

Possible interpretations

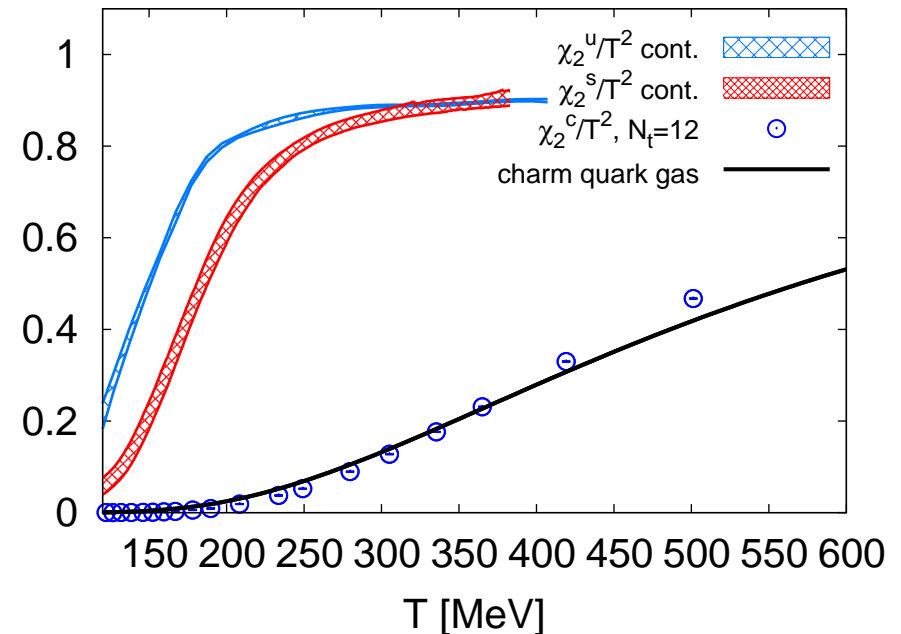


- ◆ survival of open charm hadrons up to $T \simeq 2T_c$?
- ◆ HRG results agree with the lattice up to the inflection point in the data

Possible interpretations



Or



- ❖ survival of open charm hadrons up to $T \simeq 2T_c$?
- ❖ HRG results agree with the lattice up to the inflection point in the data

- ❖ thermal excitation of charm quarks takes place at larger temperatures
- ❖ **ideal gas of charm quarks** agrees with lattice

need for **non-diagonal** quark number susceptibilities

Conclusions

- ❖ study of **diagonal** and **non-diagonal** quark number susceptibilities for $N_f = 2 + 1$ dynamical flavors
- ❖ diagonal **quark number susceptibilities**: signals of QCD phase transition
 - ➡ rapid rise close to T_c
 - ➡ susceptibilities of different flavors show their rise at different T
- ❖ correlations between different flavors are large immediately above T_c
 - ➡ possibility of bound states survival in the QGP
- ❖ diagonal charm quark susceptibilities rise at **much larger temperatures**
- ❖ they don't allow to distinguish between HRG and free charm gas
 - ➡ need for non-diagonal correlators

Backup slides

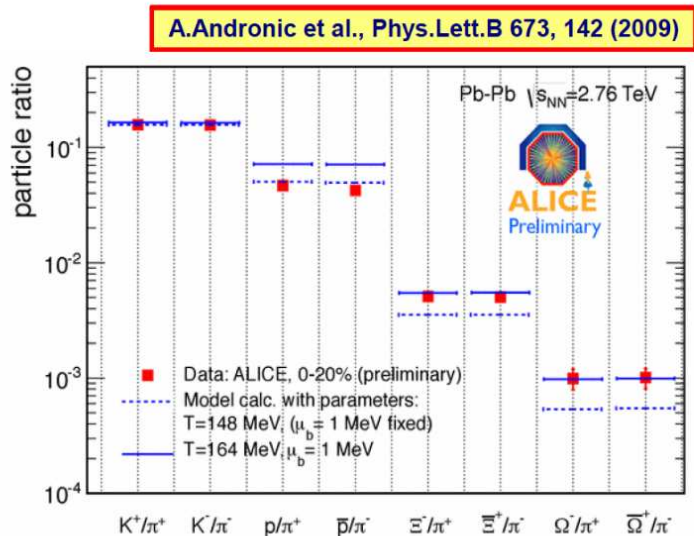
There are evidences for deviations from statistical model predictions at the LHC

- baryon production -

R. Preghenella, ALICE Collaboration, SQM 2011:

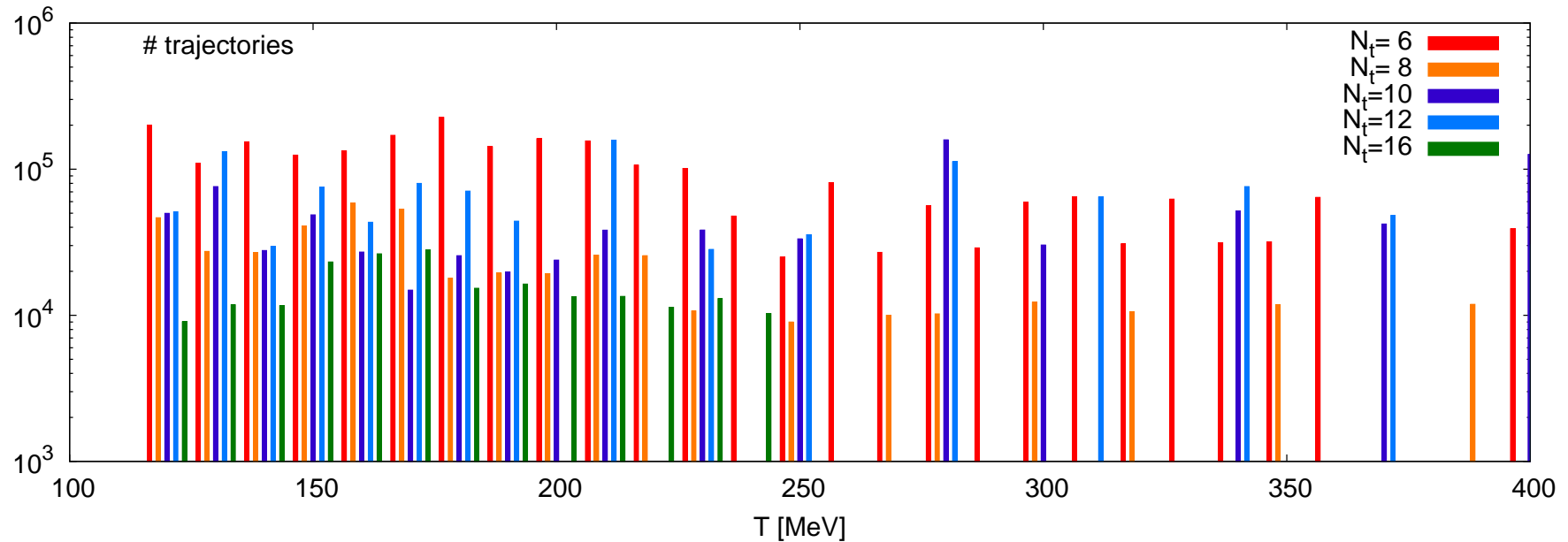
	ALICE data Pb-Pb $\sqrt{s_{NN}} = 2.6$ TeV <i>these results</i>	LHC prediction* $T_{ch} = 164$ MeV, $\mu_B = 1$ MeV <i>A.Andronic et al, Phys.Lett.B 673, 142 (2009)</i>	LHC prediction* $T_{ch} = (170 \pm 5)$ MeV, $\mu_B = (1 \pm 4)$ MeV <i>J.Cleymans et al, PRC 74, 034903 (2006)</i>
K^+/π^+	0.156 ± 0.012	0.164	0.180 ± 0.001
K^-/π^-	0.154 ± 0.012	0.163	0.179 ± 0.001
p/π^+	0.0454 ± 0.0036	0.072	0.091 ± 0.009
p/π^-	0.0458 ± 0.0036	0.071	0.091 ± 0.009

* prediction for central Pb-Pb collisions at $\sqrt{s_{NN}} = 5.5$ TeV



Conclusion:
possibly no common freeze-out surface for all particle species ?

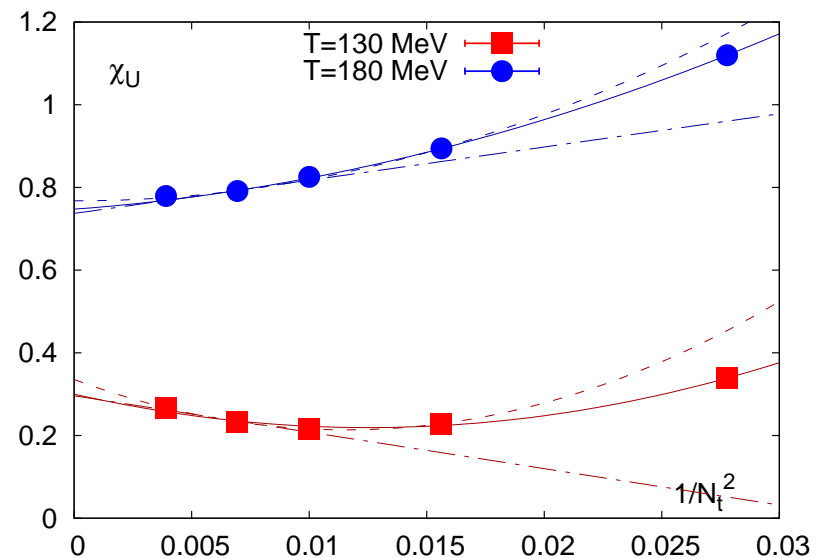
Statistics and continuum extrapolation



❖ all observables are **continuum extrapolated**

→ obtained by measuring them at several $a \sim 1/N_t$ and taking the limit $a \rightarrow 0$

❖ parabolic fit is performed

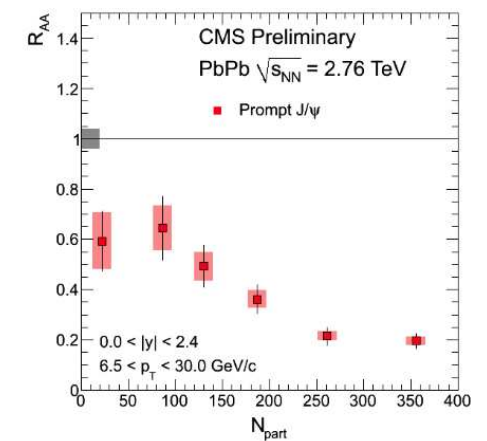
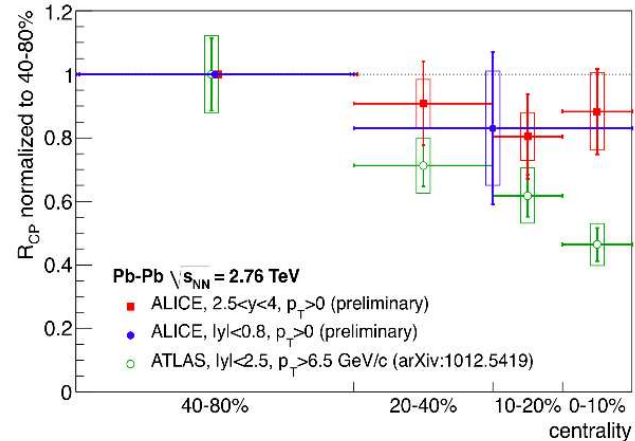
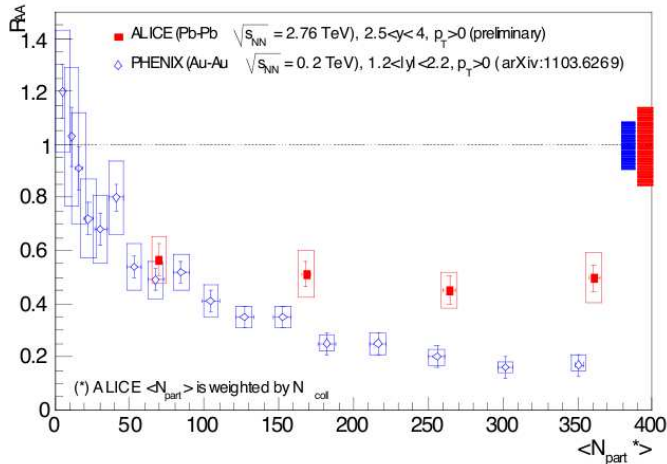


There are evidences for deviations from statistical model predictions at the LHC

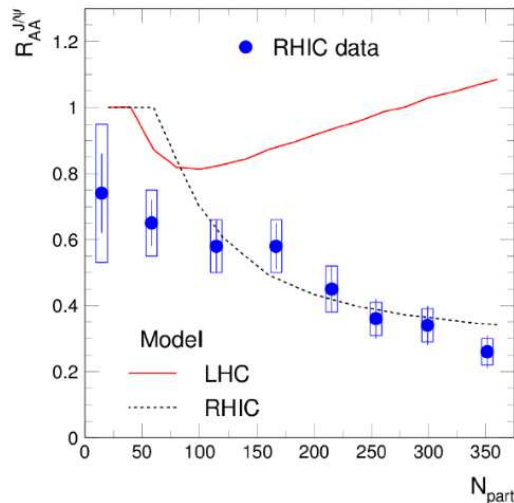
- J/ψ production -

Data: ALICE/ PHENIX (forward rapidity) - QM 2011

Data: ALICE / ATLAS / CMS (mid rapidity) - QM 2011



Prediction: Braun-Munzinger, Stachel arXiv:0901.2500

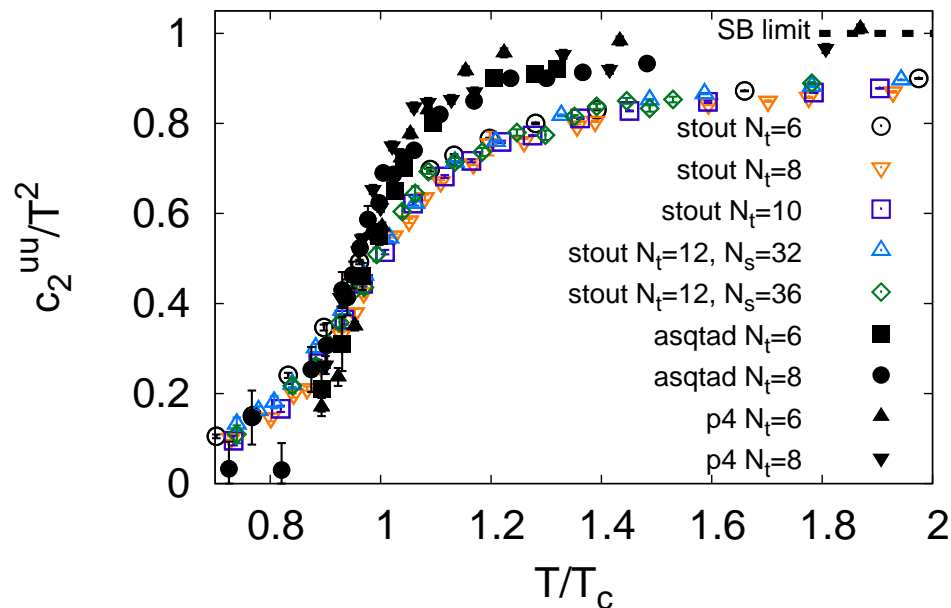


Conclusion:

All datasets (forward and mid-rapidity, low and high p_T) show significant J/ψ suppression in central collisions in contradiction to statistical model predictions: possibly no common freeze-out surface or no strong partonic recombination ?

Comparison with previous lattice data

$$c_2^{uu} = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_u \partial \mu_u} \Big|_{\mu_i=0}$$

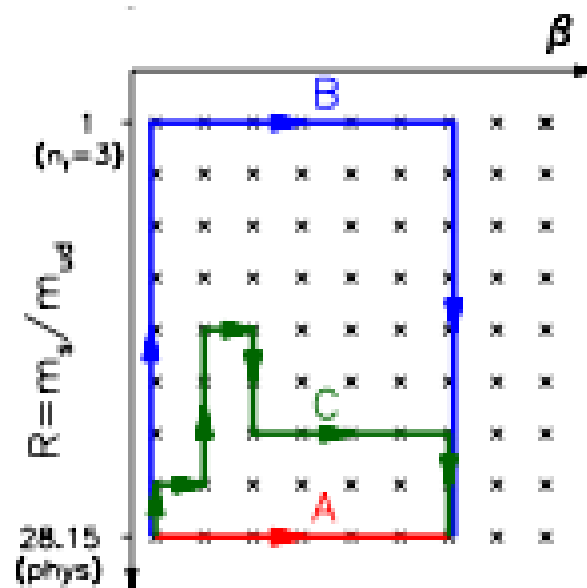


- ❖ physical quark masses $m_s/m_{u,d} = 28.15$
- ❖ finer lattice spacings approaching the continuum
- ❖ the phase transition turns out to be **much smoother**

All path approach

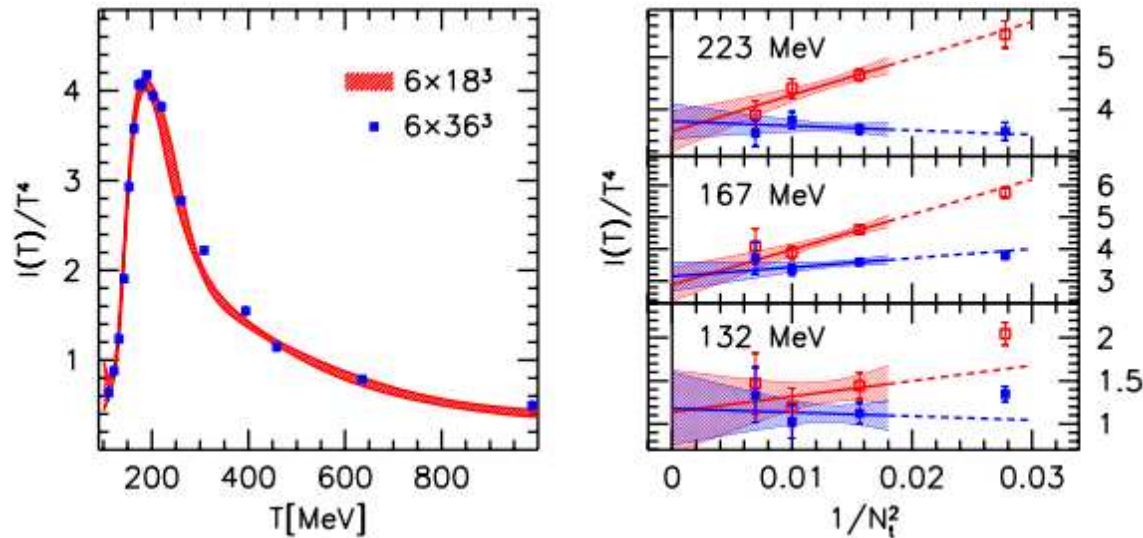
❖ Our goal:

- ➡ determine the equation of state for several pion masses
- ➡ reduce the uncertainty related to the choice of β^0



- ❖ conventional path: A, though B, C or any other paths are possible
- ❖ generalize: take all paths into account

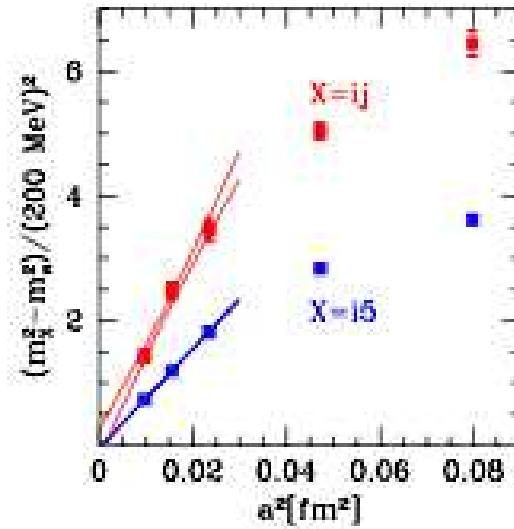
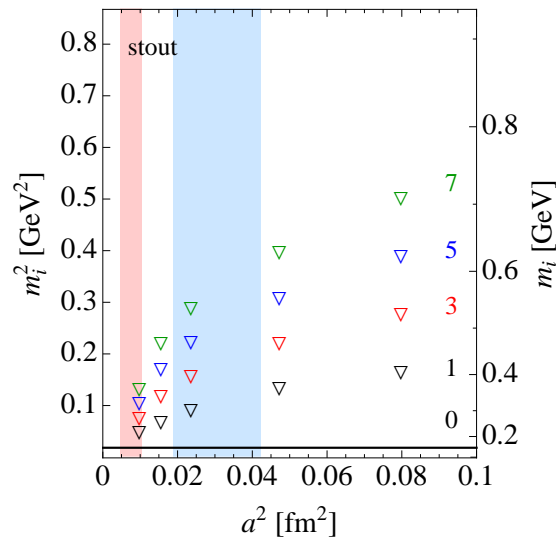
Finite volume and discretization effects



- ❖ finite V : $N_s/N_t = 3$ and 6 (8 times larger volume): **no sizable difference**
- ❖ finite a : improvement program of lattice QCD (action observables)
 - ➡ tree-level improvement for p (thermodynamic relations fix the others)
 - ➡ trace anomaly for three T -s: high T , transition T , low T
 - ➡ continuum limit $N_t = 6, 8, 10, 12$: same with or without improvement
- ❖ improvement strongly reduces cutoff effects: slope $\simeq 0$ ($1 - 2\sigma$ level)

Pseudo-scalar mesons in staggered formulation

- ❖ Staggered formulation: **four degenerate quark flavors** ('tastes') in the continuum limit
- ❖ **Rooting procedure**: replace fermion determinant in the partition function by its **fourth root**
- ❖ At **finite lattice spacing** the four tastes are not degenerate
 - ➡ **each pion** is split into **16**
 - ➡ the sixteen pseudo-scalar mesons have **unequal masses**
 - ➡ **only one** of them has vanishing mass in the chiral limit



- ❖ Scaling starts for $N_t \geq 8$.