

# Meson spectroscopy: too much excitement and too few excitations

*George Rupp*

CFIF, Instituto Superior Técnico, Lisbon

Collaborator: Eef van Beveren      PhD Student: Susana Coito

I. Introduction

II. Status of mainstream meson spectroscopy

III. Resonance-Spectrum Expansion

IV. Selected Results

V. Conclusions

# I. Introduction

⇒ Myth to be busted in meson spectroscopy: *“there are too many resonances to be accounted for by normal  $q\bar{q}$  states.”* Reasons:

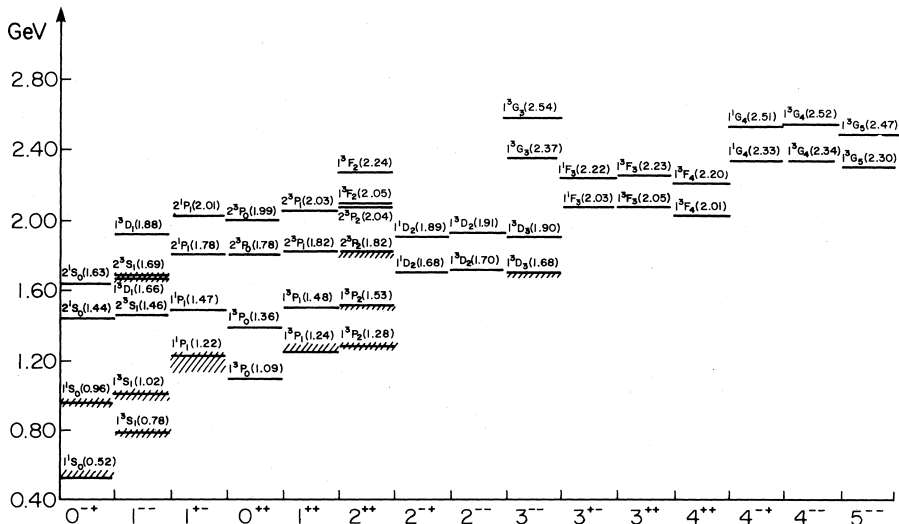
- Quenched quark-model predictions with standard Coulomb-plus-linear confinement are taken for granted, despite serious failures.
- Often biased PDG interpretation and selection of experimental results are usually mistaken for the true status of meson resonances.
- Statistically significant bumps in the data are almost invariably interpreted as resonances, without even considering possible threshold effects or inelasticity phenomena due to competing channels.
- When a new “resonance” does not seem to fit in mainstream spectroscopy, it becomes right away an exotic candidate, ignoring possible mass shifts due to meson loops (“unquenching”).
- When meson loops are included, their effect is in general strongly underestimated by ignoring the Coulombic part of the potential.
- Dynamical  $q\bar{q}$  resonances from unquenching are not considered.

## II. Status of mainstream meson spectroscopy

⇒ Reference (quenched) quark model (1716 citations in *INSPIRE*):  
Stephen Godfrey and Nathan Isgur, Phys. Rev. D **32** (1985) 189:

- Typical Coulomb-plus-linear (“funnel”) confining potential, with a phenomenological running strong coupling  $\alpha_s(r)$ .
- One-gluon exchange gives rise the Coulombic part, as well as the usual spin-spin and spin-orbit interactions.
- The model uses relativistic kinematics, fixed constituent quark masses, and phenomenological smearing functions as regulators.
- The model was applied to a very large variety of light, heavy-light, and heavy  $q\bar{q}$  states, thus almost covering the whole PDG meson spectrum.
- Most other constituent quark model predict masses that are generally in reasonable agreement with those of the Godfrey-Isgur (GI) model, but no other model has been applied so widely.
- Despite the enormous merits of the GI model, several shortcomings have become evident over the years.

# GI model, light-quark isoscalar mesons:



## Principal problems:

- $0^{++}/^3P_0$ : Lowest GI scalar  $\sim 500$  MeV heavier than  $f_0(600)$ .
- $0^{++}/^3P_0$ : GI  $s\bar{s}$  scalar almost 400 MeV heavier than  $f_0(980)$ .
- $2^{++}/^3P_2\text{-}^3F_2$ : PDG listings report 6 likely  $n\bar{n}$  ( $n = u, d$ ) states up to  $\approx 2.15$  GeV, viz.  $f_2(1270)$ ,  $f_2(1565)$ ,  $f_2(1640)$ ,  $f_2(1810)$ ,  $f_2(1910)$ ,  $f_2(2150)$ , whereas GI only predict 3.

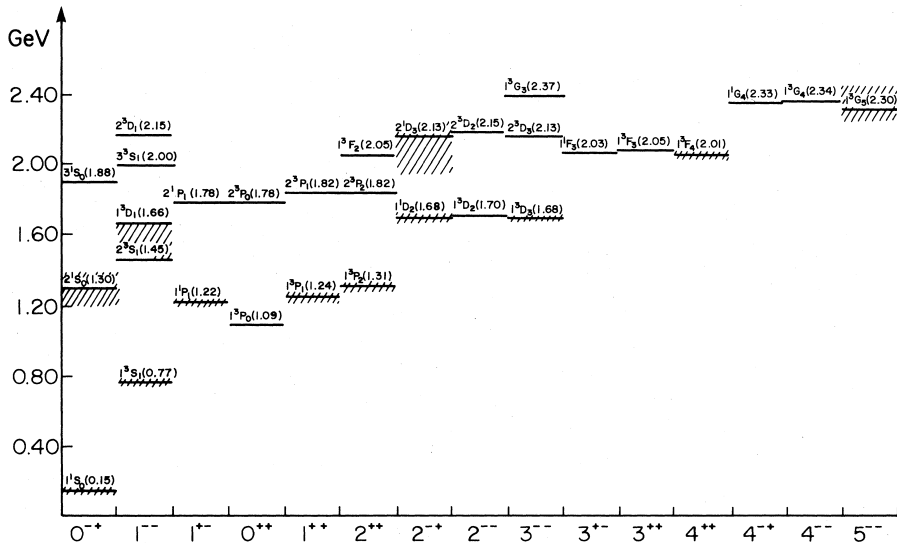
In probably dominant  $s\bar{s}$  sector, PDG also lists 6 states up to  $\approx 2.35$  GeV:  $f_2(1430)$ ,  $f_2'(1525)$ ,  $f_2(1950)$ ,  $f_2(2010)$ ,  $f_2(2300)$ ,  $f_2(2340)$ , and GI again only predicts 3.

Note: some PDG  $f_2$  states may not be resonances (see D. V. Bugg, Phys. Rept. **397** (2004) 257), but  $f_2(1565)$  looks reliable. Then, PDG:  $m(2^3P_2) - m(1^3P_2) \approx 300$  MeV; GI:  $m(2^3P_2) - m(1^3P_2) = 540$  MeV.

For unknown reasons, PDG omits  $f_2(1565)$  from Summary Table.

- $1^{+-}/^1P_1$ : PDG  $n\bar{n}$  states:  $h_1(1170)$ ,  $h_1(1595)$ .  
GI predicts:  $h_1(1220)$  ( $1^1P_1$ ),  $h_1(1780)$  ( $2^1P_1$ ).

# GI model, light-quark isovector mesons:



## Principal problems:

- $0^{++}/^3P_0$ : PDG:  $a_0(980)$ ,  $a_0(1450)$ .  
GI:  $a_0(1090)$  ( $1^3P_0$ ),  $a_0(1780)$  ( $2^3P_0$ ).
- $1^{++}/^3P_1$ : PDG:  $a_1(1260)$ ,  $a_1(1640)$ .  
GI:  $a_1(1240)$  ( $1^3P_1$ ),  $a_1(1820)$  ( $2^3P_1$ ).
- $2^{++}/^3P_2$ : PDG:  $a_2(1320)$ ,  $a_2(1700)$ .  
GI:  $a_2(1310)$  ( $1^3P_2$ ),  $a_2(1820)$  ( $2^3P_2$ ).
- $1^{--}/^3S_1$ - $^3D_1$ : PDG:  $\rho(1450)$ ,  $\rho(1570)$ ,  $\rho(1700)$ ,  $\rho(1900)$ .  
GI:  $\rho(1450)$  ( $2^3S_1$ ),  $\rho(1660)$  ( $1^3D_1$ ),  $\rho(2000)$  ( $3^3S_1$ ),  $\rho(2150)$  ( $2^3D_1$ ).  
Note: a recent analytic S-matrix analysis by S. Surovtsev and P. Bydzovsky, Nucl. Phys. A **807** (2008) 145, arrived at assignments quite different from both PDG and GI (see Table):  $\rho(1250)$ ,  $\rho(1470)$ ,  $\rho(1600)$ ,  $\rho(1900)$ . Also, they conclude that only  $\rho(1250)$  and  $\rho(1600)$  are crucial to describe the phase shifts, whereas  $\rho(1900)$  and, to a lesser extent,  $\rho(1470)$  improve the inelasticity (see plot). PDG hides  $\rho(1250)$  under the  $\rho(1450)$  entry!!

Table 1

Pole clusters distributed on sheets II, III, and IV for the  $\rho$ -like resonances.  $\sqrt{s_r}$  in MeV is given

Three resonances			
	II	III	IV
$\rho(770)$	$767.3 \pm 0.6 - i(73.3 \pm 0.5)$	$782 \pm 10.9 - i(65.6 \pm 4.7)$	
$\rho(1250)$		$1249.9 \pm 19.9 - i(152 \pm 14.3)$	$1249 \pm 16.9 - i(146.2 \pm 14.4)$
$\rho(1600)$		$1585 \pm 15.3 - i(130.5 \pm 22.5)$	$1578 \pm 8.8 - i(72.2 \pm 12.5)$
Four resonances			
	II	III	IV
$\rho(770)$	$766.5 \pm 0.6 - i(73.2 \pm 0.5)$	$783.1 \pm 10.6 - i(66.2 \pm 4.9)$	
$\rho(1250)$		$1251.4 \pm 18.8 - i(152.1 \pm 14.2)$	$1249 \pm 16.3 - i(144.3 \pm 13.9)$
$\rho(1600)$		$1585.2 \pm 18.2 - i(141.8 \pm 22.3)$	$1579.6 \pm 8.1 - i(73.6 \pm 10.3)$
$\rho(1900)$		$1871.5 \pm 30.5 - i(97.2 \pm 30.1)$	$1894 \pm 33.6 - i(95.3 \pm 32)$
Five resonances			
	II	III	IV
$\rho(770)$	$765.8 \pm 0.6 - i(73.3 \pm 0.4)$	$778.2 \pm 9.1 - i(68.9 \pm 3.9)$	
$\rho(1250)$		$1251.4 \pm 11.3 - i(130.9 \pm 9.1)$	$1251 \pm 11.1 - i(130.5 \pm 9.2)$
$\rho(1470)$		$1469.4 \pm 10.6 - i(91 \pm 12.9)$	$1465.4 \pm 12.1 - i(99.8 \pm 15.6)$
$\rho(1600)$		$1634 \pm 20.1 - i(144.7 \pm 23.8)$	$1592.9 \pm 7.9 - i(73.7 \pm 11.7)$
$\rho(1900)$		$1882.8 \pm 24.8 - i(112.4 \pm 25.2)$	$1893 \pm 21.9 - i(93.4 \pm 19.9)$

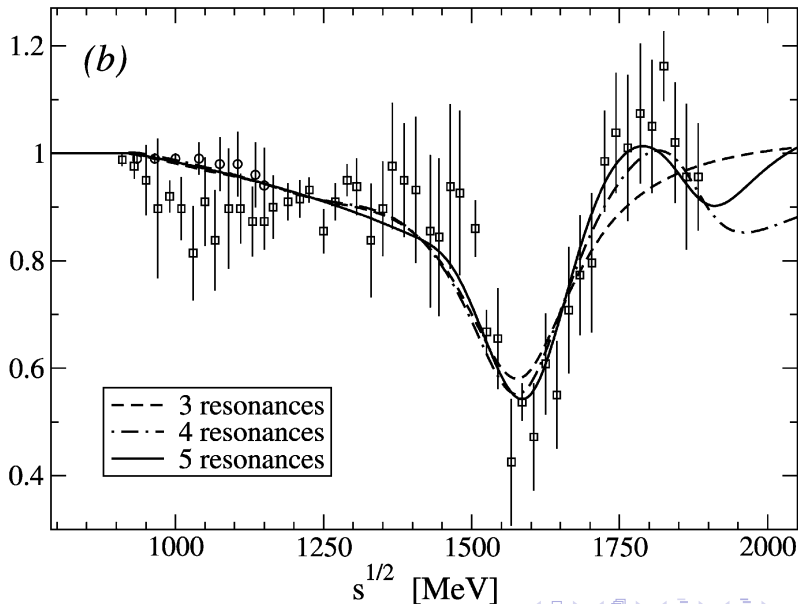
Table 2

Calculated masses and total widths of the  $\rho$ -states (all in MeV)

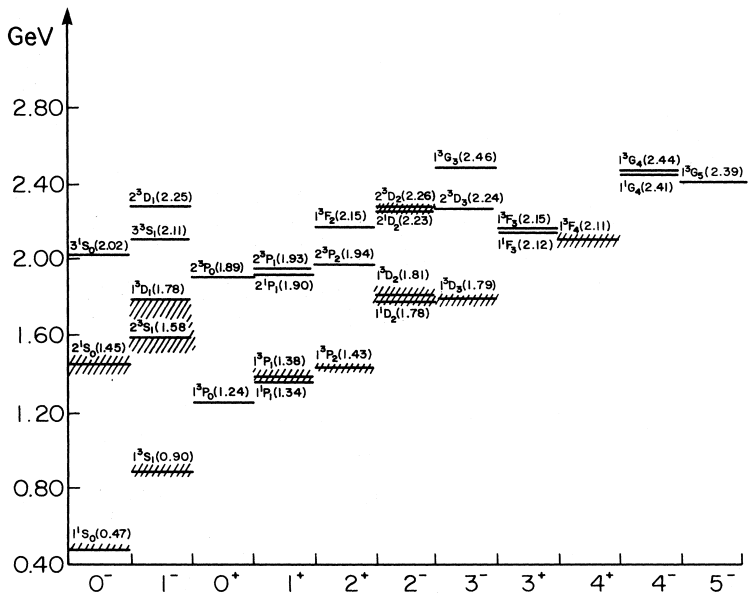
	$m_{\text{res}}$	$\Gamma_{\text{tot}}$
$\rho(770)$	$769.3 \pm 0.6$	$146.6 \pm 0.9$
$\rho(1250)$	$1257.8 \pm 11.1$	$261 \pm 18.3$
$\rho(1470)$	$1468.8 \pm 12.1$	$199.6 \pm 31.2$
$\rho(1600)$	$1594.6 \pm 8$	$147.4 \pm 23.4$
$\rho(1900)$	$1895.3 \pm 21.9$	$186.8 \pm 39.8$



$\pi\pi\text{-}\omega\pi$  inelasticity  $\eta$ :



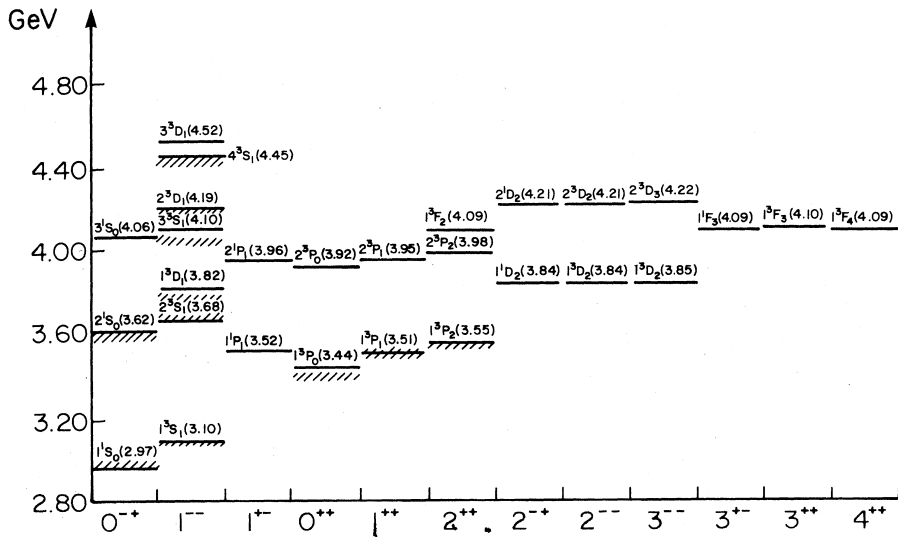
# GI model, strange mesons:



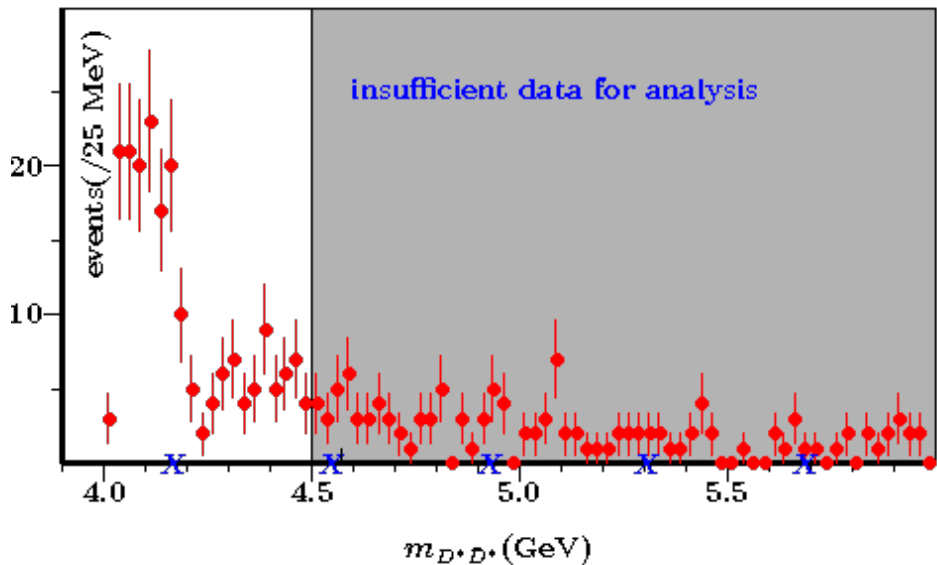
## Principal problems:

- $0^- / {}^1S_0$ : PDG:  $K(1460)$ ,  $K(1830)$ .  
GI:  $K(1450)$  ( $2^1S_0$ ),  $K(2020)$  ( $3^1S_0$ ).
- $0^+ / {}^3P_0$ : PDG:  $K_0^*(800)$ ,  $K_0^*(1430)$ ,  $K_0^*(1950)$ .  
GI:  $K_0^*(1240)$  ( $1^3P_1$ ),  $K_0^*(1890)$  ( $2^3P_1$ )
- $1^- / {}^3S_1$ - ${}^3D_1$ : PDG:  $K^*(1410)$ ,  $K^*(1680)$ .  
GI:  $K^*(1580)$  ( $2^3S_1$ ),  $K^*(1780)$  ( $1^3D_1$ ).
- $1^+ / {}^3P_1$ - ${}^1P_1$ : PDG:  $K_1(1270)$ ,  $K_1(1400)$ ,  $K_1(1650)$ .  
GI:  $K_1(1340)$  ( $1^1P_1$ ),  $K_1(1380)$  ( $1^3P_1$ ),  $K_1(1900)$  ( $2^1P_1$ ),  
 $K_1(1930)$  ( $2^3P_1$ ).
- $2^- / {}^1D_2$ - ${}^3D_2$ : PDG:  $K_2(1580)$ ,  $K_2(1770)$ ,  $K_2(1820)$ ,  $K_2(2250)$ .  
GI:  $K_2(1780)$  ( $1^1D_2$ ),  $K_2(1810)$  ( $1^3D_2$ ),  $K_2(2230)$  ( $2^1D_2$ ),  
 $K_2(2260)$  ( $2^3D_2$ ).

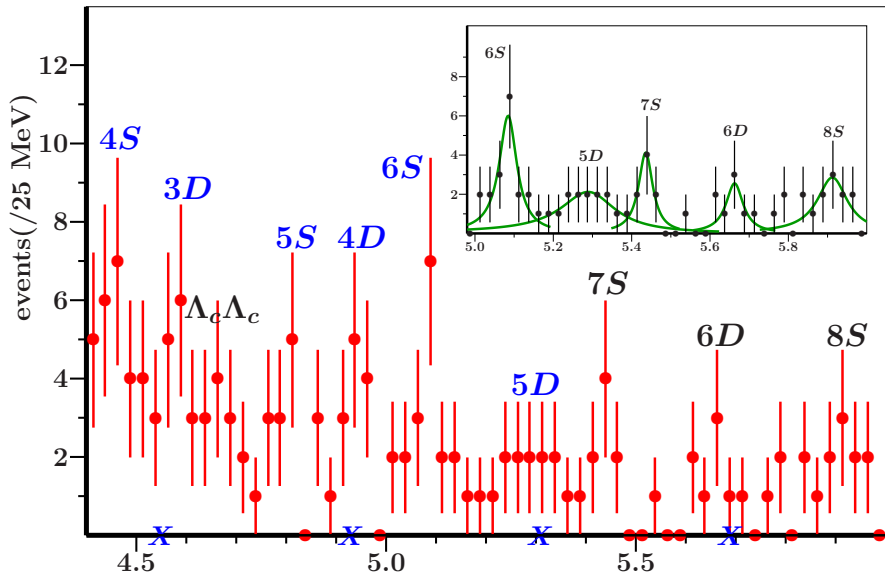
# GI model, charmonia:



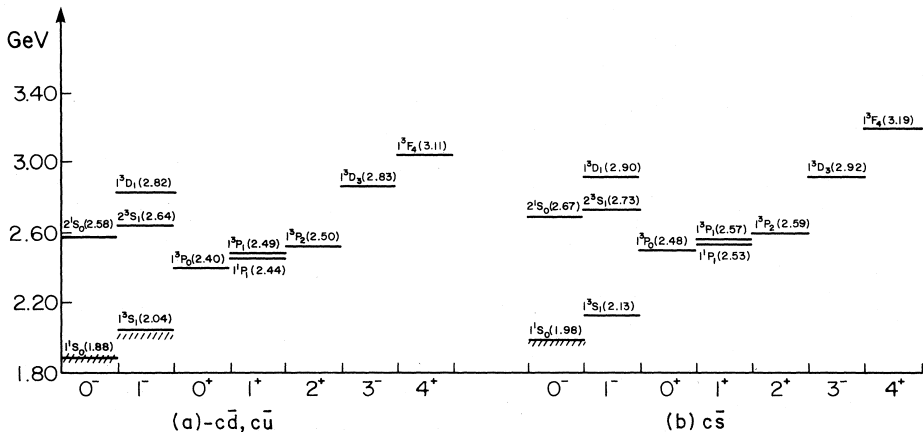
2009  $D^*\bar{D}^*$  BABAR data on vector charmonium:



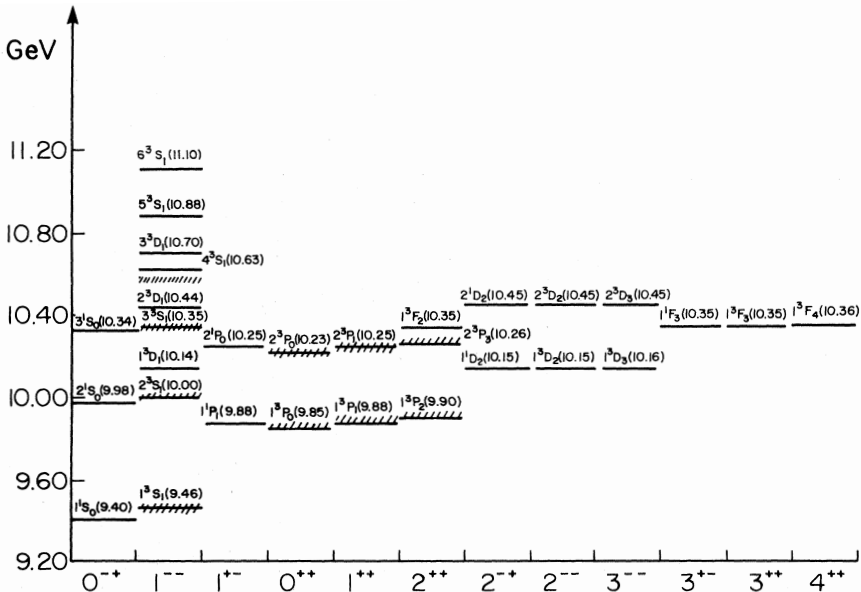
Our interpretation (EvB & GR, Chin. Phys. C **35** (2011) 1):



# GI model, charmed mesons:



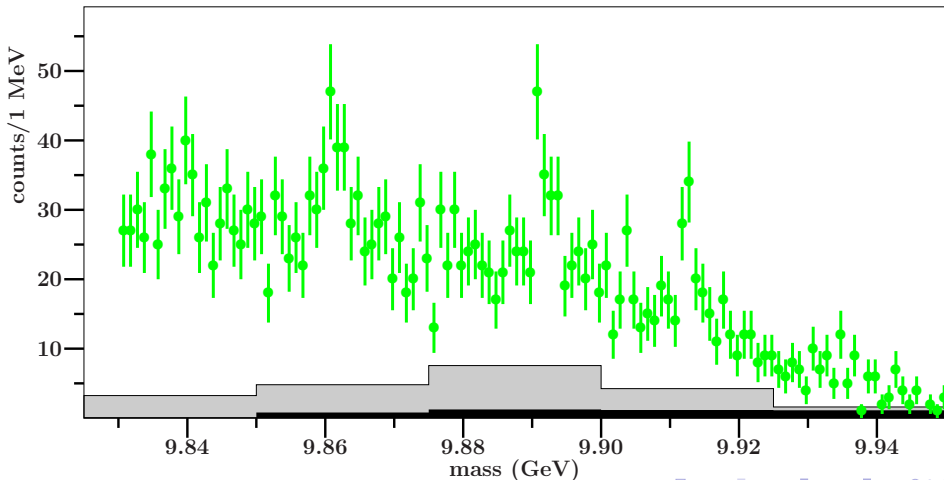
# GI model, bottomonia:





“Progress” in  $b\bar{b}$  spectroscopy (see [EvB](#), [GR](#), [arXiv:1204.1984 \[hep-ph\]](#)):

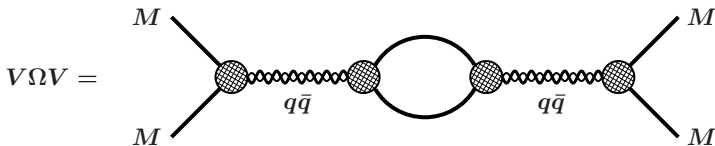
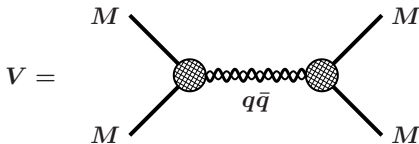
- Green points and error bars: ARGUS data on  $\chi_B(1P)$  states (Phys. Lett. B **160** (1985) 331);
- Grey areas: corresponding ATLAS/LHC data (Phys. Rev. Lett. **108** (2012) 152001).



### III. Resonance-Spectrum Expansion

(EvB & GR, Annals Phys. **324** (2009) 1620)

⇒ Building blocks of (non-exotic) RSE are:



- $V$  is the effective two-meson potential;
- $\Omega$  is the two-meson loop function;
- the blobs are the  $^3P_0$  vertex functions, modelled by a spherical  $\delta$  shell in  $r$  space, i.e., a spherical Bessel function in  $p$  space;
- the wiggly lines stand for  $s$ -channel exchanges of infinite towers of  $q\bar{q}$  states, i.e., a kind of Regge propagators.

⇒ For  $N$  meson-meson channels and several  $q\bar{q}$  channels:

$$V_{ij}^{(L_i, L_j)}(p_i, p'_j; E) = \lambda^2 r_0 j_{L_i}^i(p_i r_0) j_{L_j}^j(p'_j r_0) \sum_{\alpha=1}^{N_{q\bar{q}}} \sum_{n=0}^{\infty} \frac{g_i^{(\alpha)}(n) g_j^{(\alpha)}(n)}{E - E_n^{(\alpha)}} \\ \equiv \mathcal{R}_{ij}(E) j_{L_i}^i(p_i r_0) j_{L_j}^j(p'_j r_0) .$$

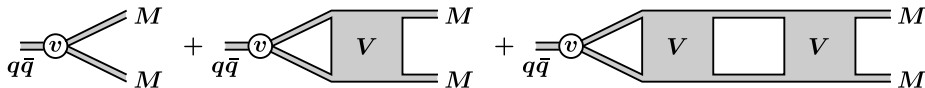
⇒ The closed-form off-energy-shell  $T$ -matrix then reads

$$T_{ij}^{(L_i, L_j)}(p_i, p'_j; E) = \\ -2\lambda^2 r_0 \sqrt{\mu_i p_i \mu'_j p'_j} j_{L_i}^i(p_i r_0) \sum_{m=1}^N \mathcal{R}_{im}(E) \{[\mathbb{1} - \Omega \mathcal{R}]^{-1}\}_{mj} j_{L_j}^j(p'_j r_0) , \\ \Omega = -2i\lambda^2 r_0 \text{diag} \left( j_{L_n}^n(k_n r_0) h_{L_n}^{(1)n}(k_n r_0) \right) .$$

⇒ The corresponding unitary and symmetric  $S$ -matrix is given by

$$S_{ij}^{(L_i, L_j)}(k_i, k'_j; E) = \delta_{ij} + 2iT_{ij}^{(L_i, L_j)}(k_i, k'_j; E) .$$

Production amplitudes (EvB & GR, Annals Phys. **323** (2008) 1215):



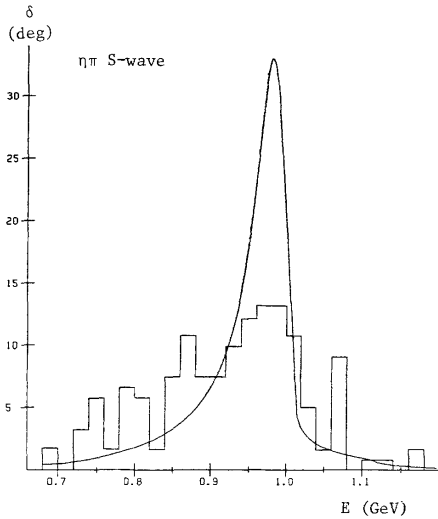
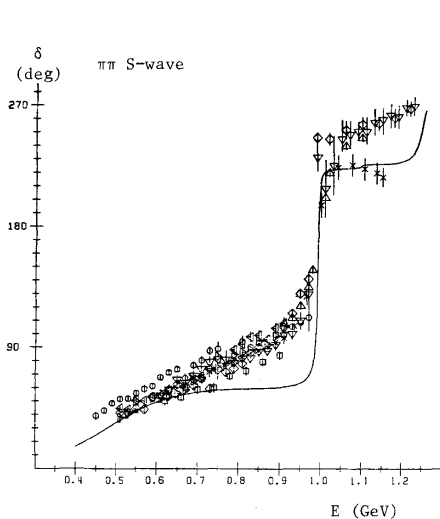
$$a(\alpha \rightarrow i) = \frac{\hat{\lambda}}{\sqrt{\pi}} \sum_{\ell, m} (-i)^\ell j_\ell(p_i r_0) Y_m^{(\ell)}(\hat{p}_i) Q_{\ell q\bar{q}}^{(\alpha)}(E) \\ \times \left\{ \frac{g_{\alpha i}}{\mathcal{D}^{(\ell)}} + i \sum_{v \neq i} \mu_v p_v h_\ell^{(1)}(p_v r_0) \left[ g_{\alpha i} \frac{t_\ell(v \rightarrow v)}{j_\ell(p_v r_0)} - g_{\alpha v} \frac{t_\ell(i \rightarrow v)}{j_\ell(p_i r_0)} \right] \right\}$$

$$\mathcal{D}^{(\ell)}(E) = 1 + 2i\hat{\lambda}^2 \sum_v g_v^2 \left\{ \sum_{n=0}^{\infty} \frac{|F_{c\bar{c}}^{(n)}(r_0)|^2}{E - E_n} \right\} \mu_v p_v j_\ell(p_v r_0) h_\ell^{(1)}(p_v r_0)$$

## IV. Selected Results

1) Light scalar mesons (EvB, GR, *et al.*, Z. Phys. C **30** (1986) 615)

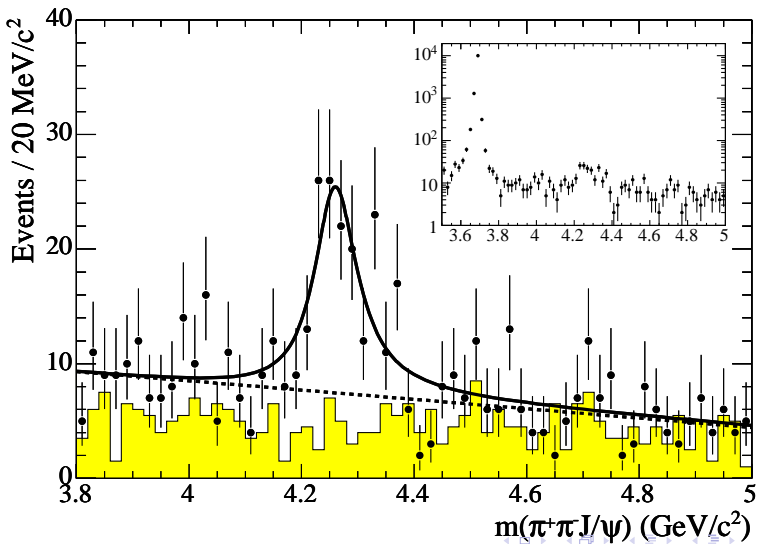
$f_0(470 - i208)$ ,  $K_0^*(727 - i263)$ ,  $a_0(968 - i28)$ ,  $f_0(994 - i20)$



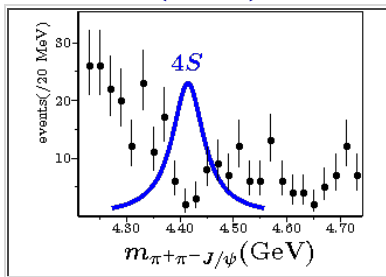


3)  $X(4260)$ , EvB & GR, Phys. Rev. Lett. **105** (2010) 102001

⇒ BaBar Collaboration, Phys. Rev. Lett. 95 (2005) 142001



## X(4260)

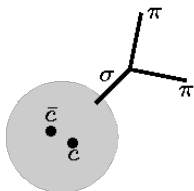


**No signal in  $\pi\pi J/\psi$  where the  $\psi(4S)$  is expected,  
Because  $\psi(4S) \rightarrow D_s^* \bar{D}_s^*$  depletes the  $\pi\pi J/\psi$  signal.**

- data from BaBar, Phys. Rev. Lett. 95, 142001 (2005)
- EvB, GR, Chin. Phys. C 35 (2011) 319
- EvB, GR, Phys. Rev. Lett. 105 (2010) 102001

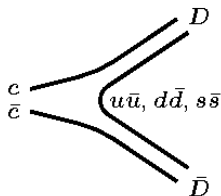


## Depletion



**Radiation of a system with vacuum quantum numbers ( $\sigma$ ).**

**The  $c\bar{c}$  system jumps to a lower lying stable state:  $\psi(1,2S)$ .**



**Open-charm decay via the creation of a light quark-antiquark pair.**

**Left: Slow radiation process.**

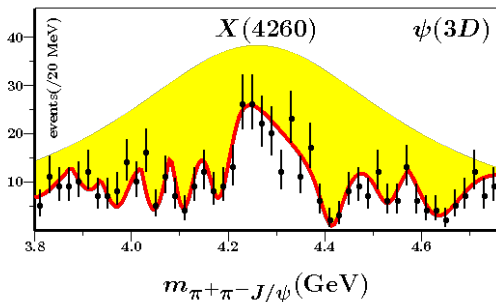
**Right: Fast open-charm decay.**

**The latter process dominates at resonances and threshold enhancements.**

- EvB, GR, arXiv:0904.4351

- EvB, GR, J. Segovia, Phys. Rev. Lett. 105 (2010) 102001

**Depletion by open-charm decays  
of the X(4260) signal  
in  $\pi^+\pi^- J/\psi$**



**By threshold enhancements:**

**DD, DD\*, D<sub>s</sub>D<sub>s</sub>, D\*D\*, D<sub>s</sub>D<sub>s</sub>\*, D<sub>s</sub>\*D<sub>s</sub>\*,  $\Lambda_c\Lambda_c$ .**

**By cc resonances:  $\psi(3S)$ ,  $\psi(2D)$ ,  $\psi(4S)$ ,  $\psi(3D)$ .**

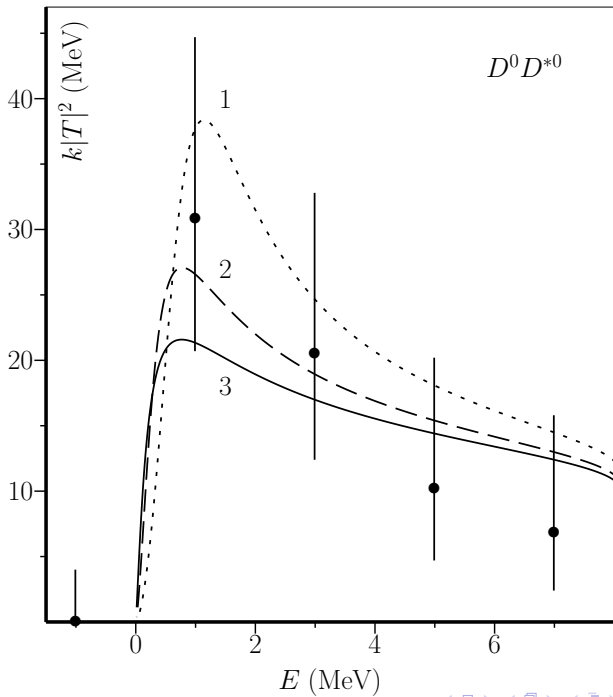
- data from BaBar, Phys. Rev. Lett. 95, 142001 (2005)

- figure from Evt, GR, JS, Phys. Rev. Lett. 105, 102001 (2010)

#### 4) $X(3872)$ as a unitarised $1^{++} c\bar{c}$ state

⇒ SC, GR, EvB, Eur. Phys. J. C **71** (2011) 1762

- In RSE, bare  $2^3P_1 c\bar{c}$  state lies at 3979 MeV;
- Couple it to  $D^0 D^{*0}$  and other OZI-allowed channels, as well as to  $\omega J/\psi$  and  $\rho^0 J/\psi$ ;
- $\omega J/\psi$  and  $\rho^0 J/\psi$  channels are smeared out so as to account for the  $\omega$  and  $\rho$  widths, by taking complex  $\omega$  and  $\rho$  masses and reunitarising the  $S$ -matrix (see paper in EPJC);
- $D^0 D^{*0}$  and  $\rho^0 J/\psi$  data are easily described (see plot on next slide), as well as the  $\omega J/\psi / \rho^0 J/\psi$  branching ratio;
- Corresponding  $X(3872)$  pole settles at or slightly below the  $D^0 D^{*0}$  threshold, with an imaginary part of about 0.1–0.7 MeV;
- Peak in  $\rho^0 J/\psi$  at  $\approx 3872$  MeV and cusp-like structure in  $D^0 D^{*0}$  at  $\approx 3874$  MeV appear naturally, with no need for an additional state.

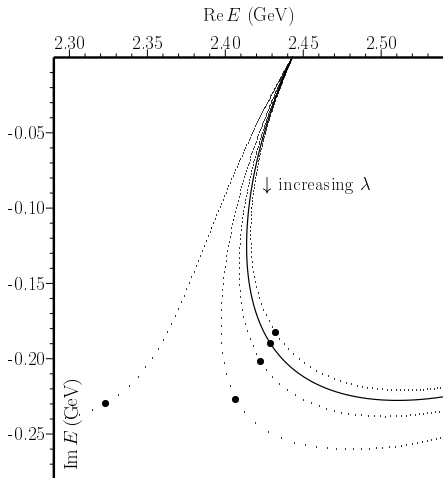


5)  $D_1(2420)$ ,  $D_1(2430)$ ,  $D_{s1}(2536)$ ,  $D_{s1}(2460)$

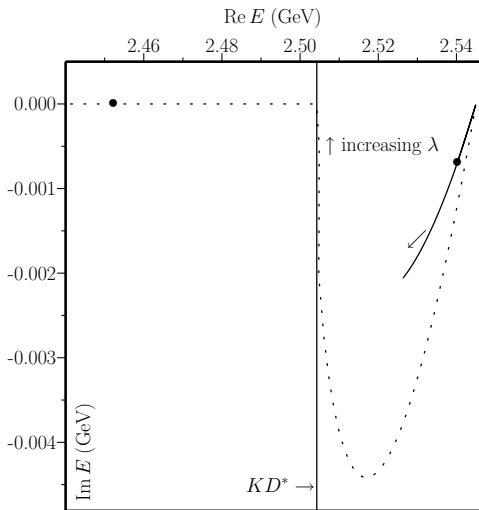
⇒ SC, GR, EvB, Phys. Rev. D **84** (2011) 094020

- $D_1(2420)$  and  $D_1(2430)$  are almost degenerate in mass, whereas  $D_{s1}(2536)$  and  $D_{s1}(2460)$  are 76 MeV apart;
- $D_{s1}(2536)$  and  $D_{s1}(2460)$  are very narrow ( $< 2.3$  resp.  $< 3.5$  MeV),  $D_1(2420)$  is narrow (20–25 MeV), and  $D_1(2430)$  is very broad ( $\sim 384$  MeV);
- No simple quark model, with spin-orbit splitting, can reproduce this pattern of masses and widths;
- Also chiral Lagrangians for heavy-light systems, with chiral loop corrections, fail dramatically, with the loops even worsening the discrepancies.
- **Our work:** couple bare  $^3P_1$  and  $^1P_1$   $c\bar{q}$  and  $c\bar{s}$  systems to the most important OZI-allowed meson-meson channels, in RSE approach;
- Dynamics of equations generates 2 quasi-bound states in the continuum ( $D_1(2420)$  and  $D_{s1}(2536)$ ), as well as 2 strongly shifted states ( $D_1(2430)$  and  $D_{s1}(2460)$ ); see next slide;
- 8 observables are quite well reproduced with 2 parameters.

Left:  $D_1(2430)$  pole trajectories.



Right:  $D_{s1}(2460)$  and  $D_{s1}(2536)$ .



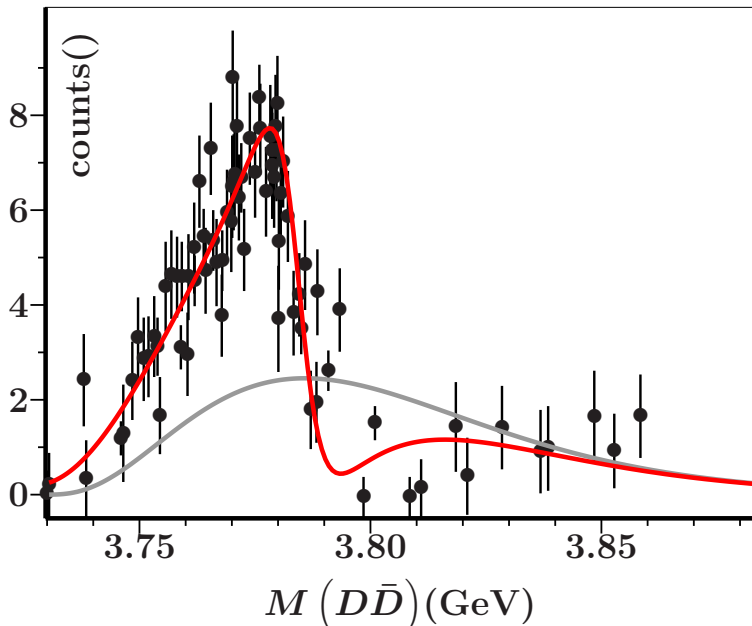
## 6) $\psi(3770)$

BES reported an “anomalous line shape” of the  $\psi(3770)$  resonance in arXiv:0807.0494 [hep-ex]:

*“The anomalous line-shape may be explained by two possible enhancements of the inclusive hadron production near the center-of-mass energies of 3.764 GeV and 3.779 GeV, indicating that either there is likely a new structure in addition to the  $\psi(3770)$  resonance around 3.773 GeV, or there are some physics effects reflecting the  $DD$  production dynamics.”*

Our explanation in [EvB, GR, Phys. Rev. D \*\*80\*\* \(2009\) 074001](#):

- Opening of  $D\bar{D}$  threshold in  $e^+e^-$  produces a broad bump in the production cross section (Bessel function).
- On top of the structure there is a Breit-Wigner resonance, with  $M = 3781$  MeV and  $\Gamma = 17$  MeV, i.e., narrower and a little bit heavier than in the PDG tables.
- See figure on next slide.





## V. Conclusions

⇒ Meson spectroscopy is in a globally bad shape:

- Many  $q\bar{q}$  states predicted by the quark model are missing, especially in the charmed, bottom,  $c\bar{c}$ , and  $b\bar{b}$  sectors.
- In the light-quark sector, there are very serious discrepancies between several excited states and the Godfrey-Isgur model.
- Other funnel-type models will hardly do much better there.
- As the vast majority of meson resonances are inelastic, there is little hope that lattice QCD will come to rescue soon. Where Lüscher's method fails, maybe Oset's new approach is a way out.
- Dedicated spectroscopy experiments are needed in all flavour sectors, with reliable partial-wave analyses, and no PDG bias.
- Threshold and inelasticity effects should be included in experimental analyses of meson-production data. This is still in its infancy.
- Spectroscopists must unquench their models in a realistic way, before getting too excited about "exotic" discoveries.
- Modern meson spectroscopy is about poles in  $S$ -matrix and production amplitudes, and not bound states in confining potentials.