

# Measurement of the Azimuthal Correlation between the most Forward Jet and the Scattered Positron in Deep Inelastic Scattering at HERA



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( on behalf of the H1 Collaboration )



- QCD dynamics at low Bjorken-x
- QCD models
- Experimental Method
- Results
- Conclusions

XX International Workshop on  
Deep-Inelastic Scattering and  
Related Subjects



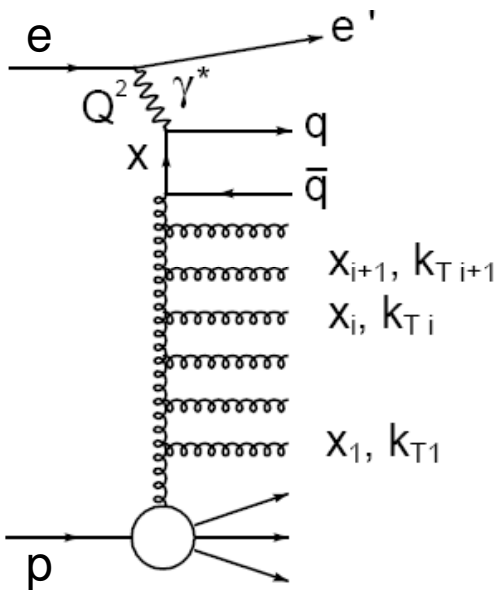
26-30 March 2012, University of Bonn



# QCD dynamics at low Bjorken-x

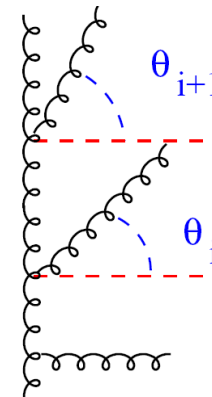
**HERA : DIS at low Bjorken-x down to  $10^{-5}$   $\rightarrow$  large  $\gamma^*p$  centre-of-mass-energy**  
 (  $W_{\gamma^*p} \approx Q^2 / x$  )

- enhanced phase space for gluon cascades exchanged between the proton and the photon
- pQCD – multiparton emissions described only with approximations :



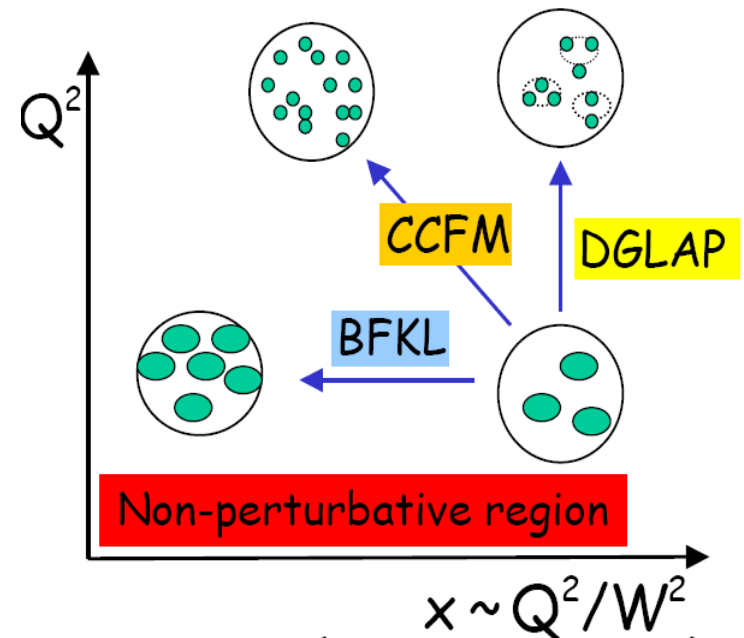
- **DGLAP : Dokshitzer-Gribov-Lipatov-Altarelli-Parisi evolution**  
 applicable at large  $Q^2$   
 Assumes strong ordering of parton  $k_T$   
 Resums terms  $\sim (\alpha_S \ln Q^2)^n$
- **BFKL : Balitsky-Fadin-Kuraev-Lipatov evolution**  
 Transition from DGLAP to BFKL scheme expected at low  $x$   
 No ordering in  $k_T$ , strong ordering in  $x_i$   
 Resums terms  $\sim (\alpha_S \ln(1/x))^n$

- **CCFM : Ciafaloni-Catani-Fiorani-Marchesini equation**  
 applicable at all  $x$  and  $Q^2$   
 Unification of DGLAP and BFKL approaches  
 Emitted partons are ordered in angles



# QCD dynamics at low Bjorken-x

- Search at HERA for effects of parton dynamics beyond the standard DGLAP approach
- Define observables / phase space regions sensitive to low x effects



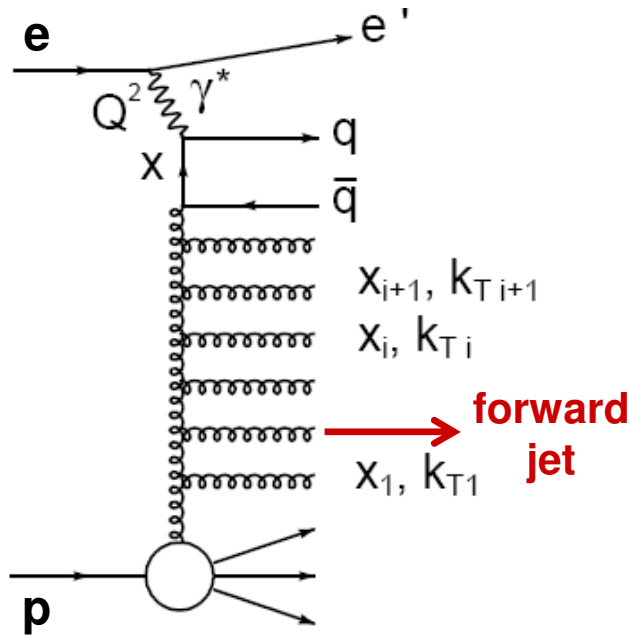
- **Strong rise of the proton structure function  $F_2(x, Q^2)$  with decreasing  $x$** 
  - well described by NLO DGLAP over a large range of  $Q^2$

$F_2$  measurement is too inclusive to discriminate between different QCD evolution schemes

**Hadronic final states – reflect kinematics, structure of gluon emissions**

( forward jets / particles, inclusive jets, multijet production, azimuthal correlation in dijet events, transverse energy flow, pt distribution of hadrons )

# Forward jets in DIS



**Mueller – Navelet jets in DIS (1990) :**

High transverse momentum and high energy jets produced close to the proton remnant direction ( forward region in LAB )

**Suppress standard DGLAP evolution in  $Q^2$  :**

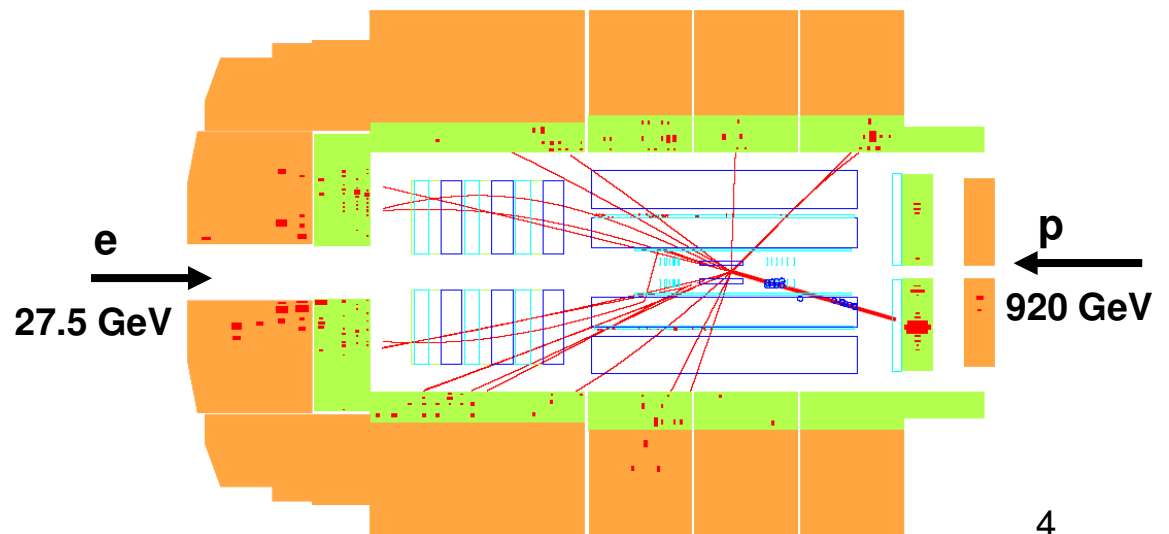
$$p_{T, \text{jet}}^2 \approx Q^2$$

**Enhance BFKL evolution in  $x$  :**

$$x_{\text{fwdjet}} = E_{\text{fwdjet}} / E_p \gg x_{Bj}$$

**BFKL - more hard partons emitted close to the proton**

**Studies of forward jets are an experimental challenge : region of high particle densities close to the proton remnant**

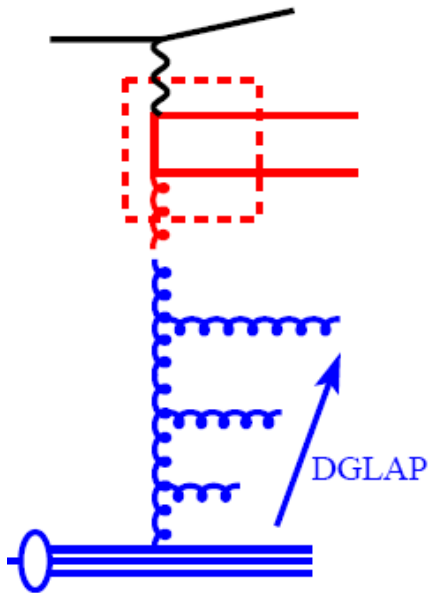


DIS event at low  $Q^2$

# Monte Carlo models with different QCD dynamics

## RAPGAP - DGLAP

LO QCD matrix elements  
+ HO modelled by leading  
log parton showers

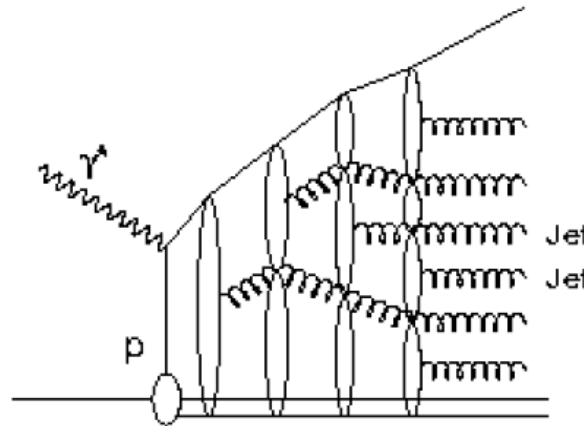


Single DGLAP ladder with  
strong ordering in  $k_T$

## ARIADNE Colour Dipole Model

CDM: QCD radiation from  
the colour dipole formed  
by the struck quark and  
the proton remnant.

Chain of independently  
radiating dipoles formed  
by the emitted gluons.

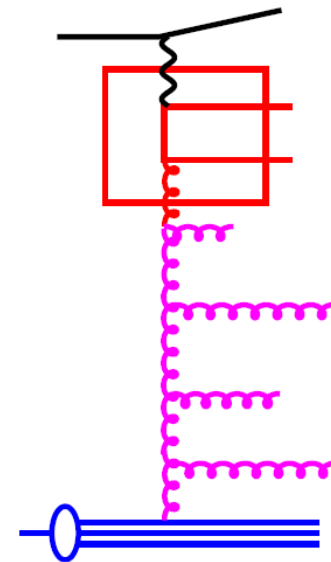


BFKL- like Monte Carlo :  
random walk in  $k_T$

## CASCADE - CCFM

Off-shell QCD ME  
+ parton emissions based  
on the CCFM equation

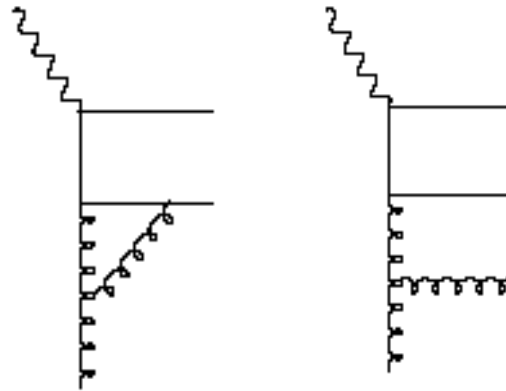
$k_T$  - factorisation



Input : unintegrated gluon  
density function, different  
uPDF sets include singular  
or full terms of the gluon  
splitting function

## Fixed order NLO DGLAP predictions

Forward jet cross sections – comparison with the predictions of pQCD at NLO ( $\alpha_s^2$ ) accuracy



- Forward jet analysis – reconstruction of jets in the Breit frame → at least dijet topology

**NLOJET ++** program ( Nagy & Trocsanyi, 2001 ) :  
dijet production at parton level in DIS at **NLO** ( $\alpha_s^2$ )

- PDF : CTEQ6.6,  $\alpha_s(M_Z) = 0.118$
- parton level cross sections corrected for hadronisation effects using the RAPGAP model

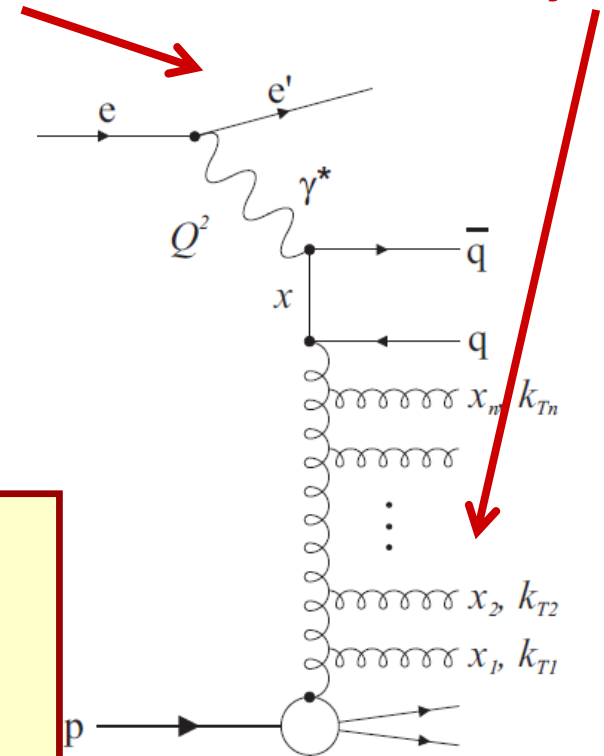
## Azimuthal decorrelation of forward jets in DIS

Azimuthal angle difference  $\Delta\Phi$  between the **scattered positron** and the **forward jet** may offer a signature of BFKL dynamics

- **Quark Parton Model  $e + q \rightarrow e + q$**   
simple two-body kinematics  $\Delta\phi = \phi_{el} - \phi_{fwdjet} = \pi$
- **Inclusion of higher order processes  $O(\alpha_S^n)$**   
decorrelates the jet from the positron

As the rapidity distance approximated by  $Y = \ln(x_{fwdjet}/x_{Bj})$  between the scattered positron and the forward jet grows the probability of multi-gluon emissions is increased

- **J. Bartels et al., Phys. Lett. B384(1996)300**  
calculated  $\Delta\phi$  in LO BFKL, resumming the dominant terms  $\sim (\alpha_S Y)^n$
- **S. Vera & F. Schwennsen, Phys. Rev. D77(2008)014001**  
calculated  $\Delta\phi$  in NLO BFKL, resumming the dominant terms  $\sim \alpha_S (\alpha_S Y)^n$



# Data selection

H1 experiment, HERA data (2000) with  $38.2 \text{ pb}^{-1}$

## DIS selection

$$0.1 < y < 0.7$$

$$5 < Q^2 < 85 \text{ GeV}^2$$

$$0.0001 < x < 0.004$$

## Forward jets ( inclusive $k_T$ algorithm )

Jets reconstructed in the Breit frame  
from combined track-calorimeter cluster objects  
and then boosted to LAB, all cuts in LAB

$$p_{T, \text{fwdjet}} > 6 \text{ GeV}$$

$$1.73 < \eta_{\text{fwdjet}} < 2.79$$

$$x_{\text{fwdjet}} = E_{\text{fwdjet}} / E_p > 0.035$$

$$0.5 < p_{T, \text{fwdjet}}^2 / Q^2 < 6.0$$

- suppress  $k_T$  ordered evolution by cut on  $p_T^2 / Q^2$
- enhance phase space for BFKL evolution without  $k_T$  ordering by cut on  $x_{\text{fwdjet}}$

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~ 14000 DIS events with at least one forward jet

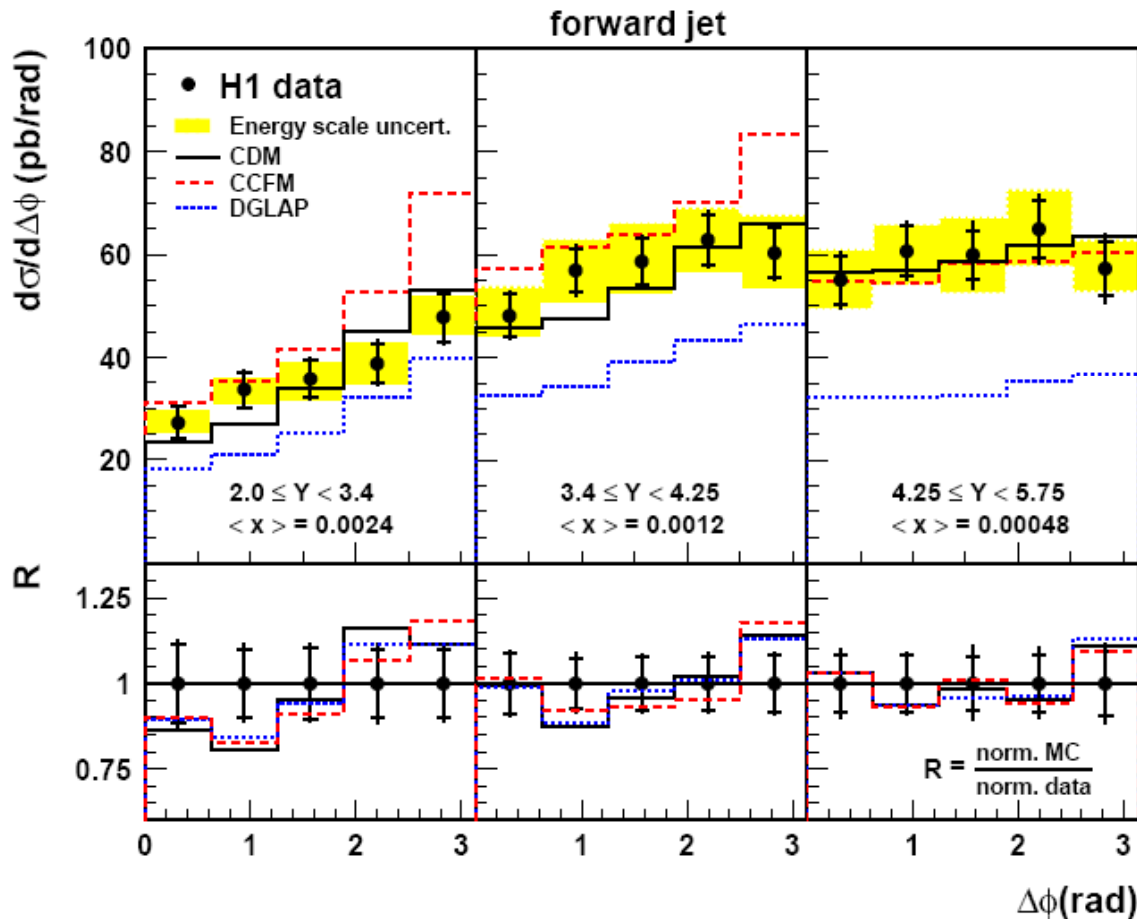
if more than one forward jet is found, the jet with the largest  $\eta_{\text{fwdjet}}$  is chosen  
 $\eta = -\ln(\tan \theta/2)$ ,  $\theta$  defined with respect to the initial proton direction



# Forward jet azimuthal correlations

At higher Y corresponding to lower x the forward jet is more decorrelated from the scattered electron

Positron – fwd jet rapidity distance  $Y = \ln(x_{\text{fwdjet}} / x)$



## Cross sections :

- well described by BFKL-like model CDM
- DGLAP predictions below the data
- CCFM (set A0) as good description as CDM at large Y

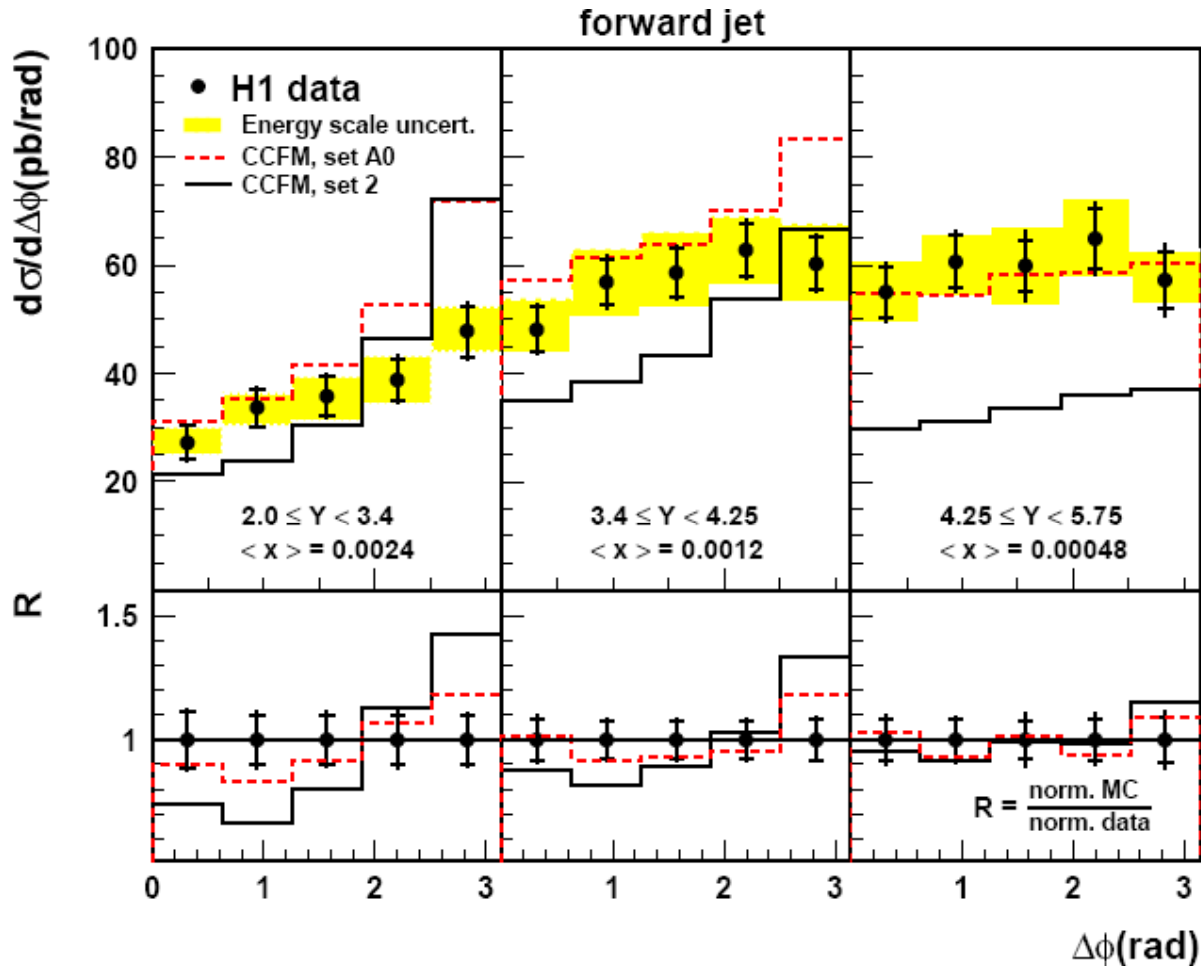
Ratio R of MC to data for normalised cross-section

$$R = \left( \frac{1}{\sigma^{\text{MC}}} \frac{d\sigma^{\text{MC}}}{d\Delta\phi} \right) / \left( \frac{1}{\sigma^{\text{data}}} \frac{d\sigma^{\text{data}}}{d\Delta\phi} \right)$$

The shape of  $\Delta\phi$  distributions is well described by all MC models

# Forward jet azimuthal correlations

Predictions of the CCFM model depend on the choice of uPDF



- **Cross sections**  
strongly depend on uPDF
- **Shape of  $\Delta\phi$  distributions**
  - at low Y shows sensitivity to uPDF
  - well described by the set A0

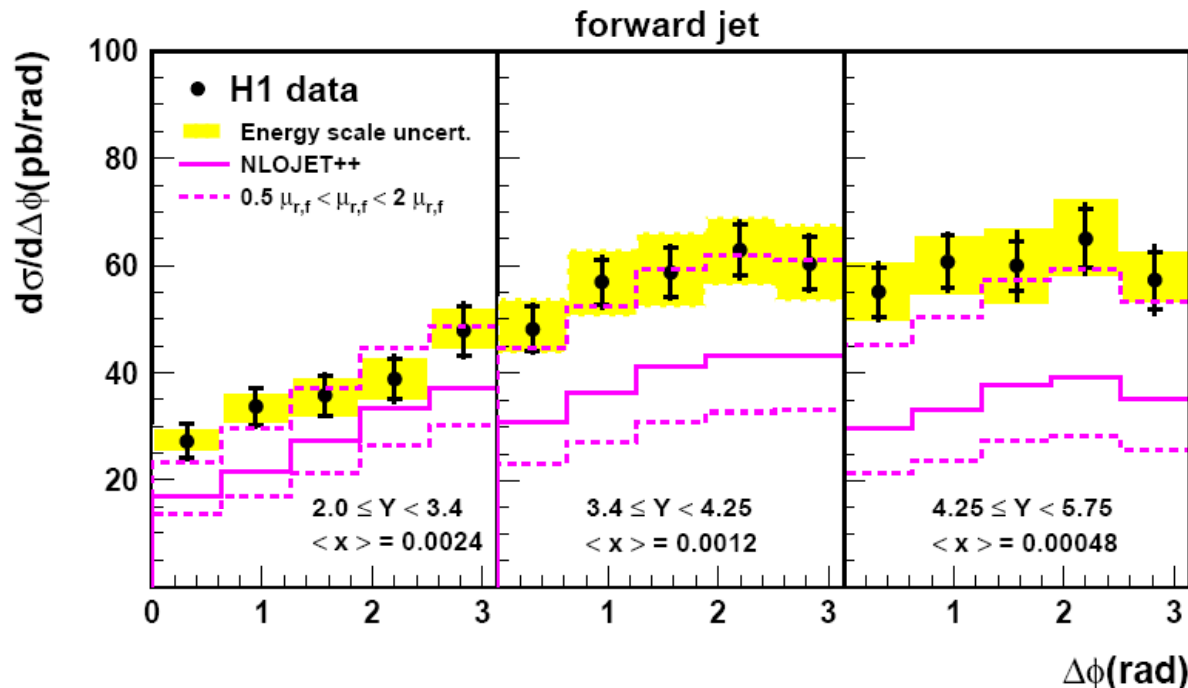
Different splitting functions used in uPDF :

set A0 – only singular terms of the gluon splitting function

set 2 – includes also non-singular terms

# Forward jet azimuthal correlations

## Comparison to NLO ( $O(\alpha_s^2)$ ) predictions



### NLO predictions

- shape of  $\Delta\phi$  distributions described, but central value too low
- large scale uncertainty (of up to 50%) indicates importance of higher orders

### NLOJET++

PDF : CTEQ6.6,  $\alpha_s(M_Z)=0.118$

renormalisation and factorisation scales :

$$\mu_r^2 = \mu_f^2 = (p_{T, \text{fwdjet}}^2 + Q^2) / 2$$

theoretical uncertainty : factor 2 or  $1/2$  applied to  $\mu_r$  and  $\mu_f$  scales simultaneously

# $\Delta\phi$ decorrelation: no discrimination between different evolution schemes

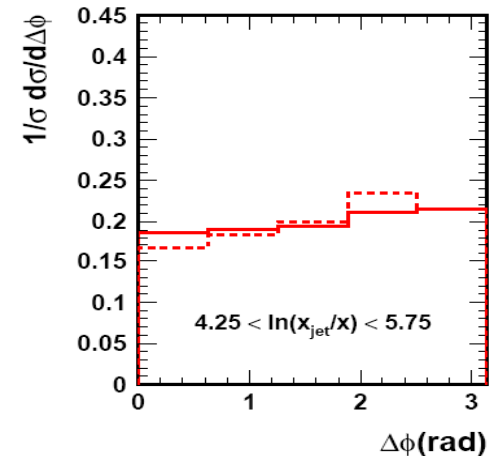
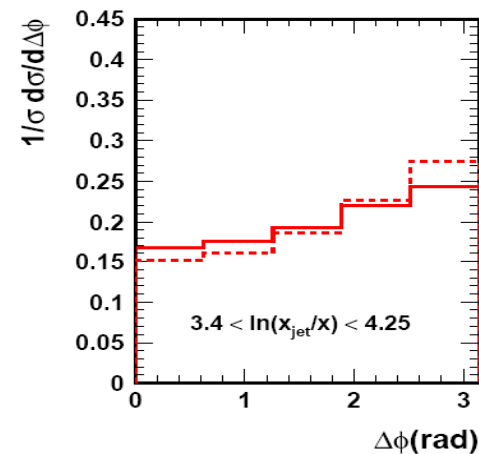
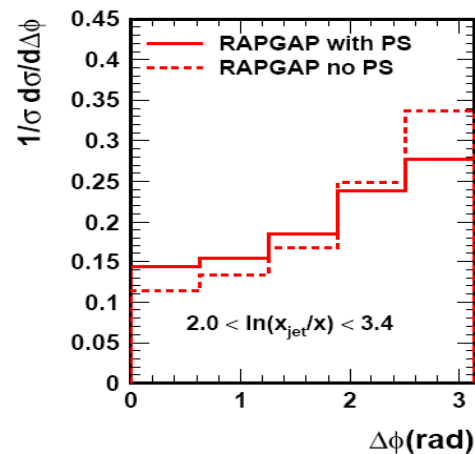
- Does forward jet originate from the hard matrix elements ? No !

Studies of parton to hadron correlation with the DGLAP-based RAPGAP model

→ ~ 80% of forward jets produced by parton showers

- Why no dependence of  $\Delta\phi$  shape on parton shower ?

RAPGAP  
parton showers  
switched on / off

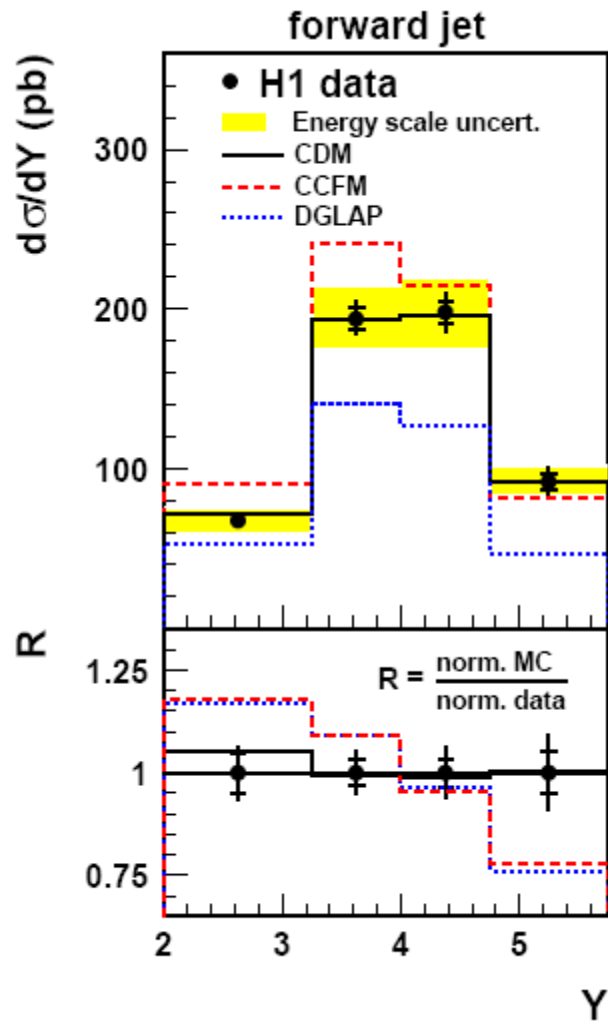


- The shape of  $\Delta\phi$  only slightly changed when the initial state parton shower is switched off

Decorrelation in  $\Delta\phi$  is governed by the phase space requirements  
( mainly by rapidity separation Y )

Normalisation of the cross sections depends on the evolution scheme

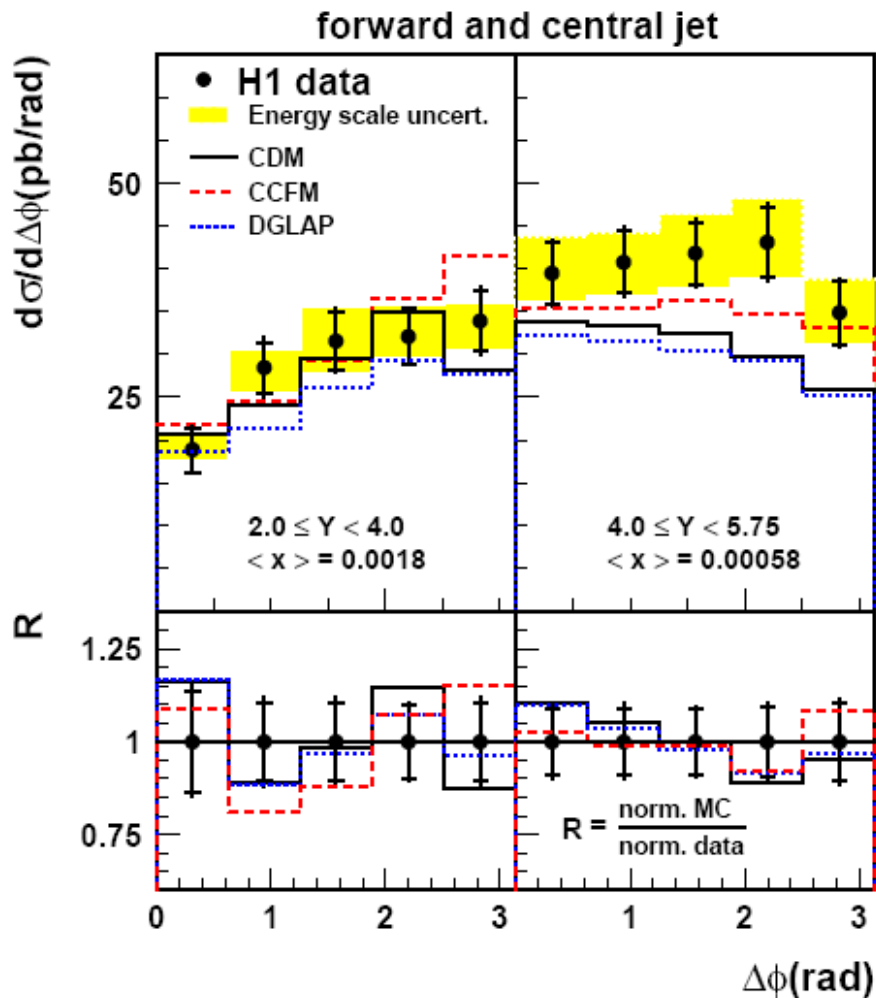
# Forward jet cross section $d\sigma / dY$



- BFKL-like model CDM describes the data best
- DGLAP too low, especially at large Y
- CCFM (set A0) predictions too high at low x, but describe the data at large Y

$Y = \ln(x_{\text{jet}} / x)$  rapidity separation between the most forward jet and the scattered positron

# Forward and central jet cross sections $d\sigma / d\Delta\phi$



- Subsample of events with **forward jet + additional central jet** (~8900 events)

$$p_{T,\text{cenjet}} > 4 \text{ GeV}$$

$$-1 < \eta_{\text{cenjet}} < 1$$

$$\Delta\eta = \eta_{\text{fwdjet}} - \eta_{\text{cenjet}} > 2$$

(enhance radiation between the forward and central jet)

- $\Delta\phi$  still between the forward jet and the scattered positron

- at low Y all models describe the data reasonably well

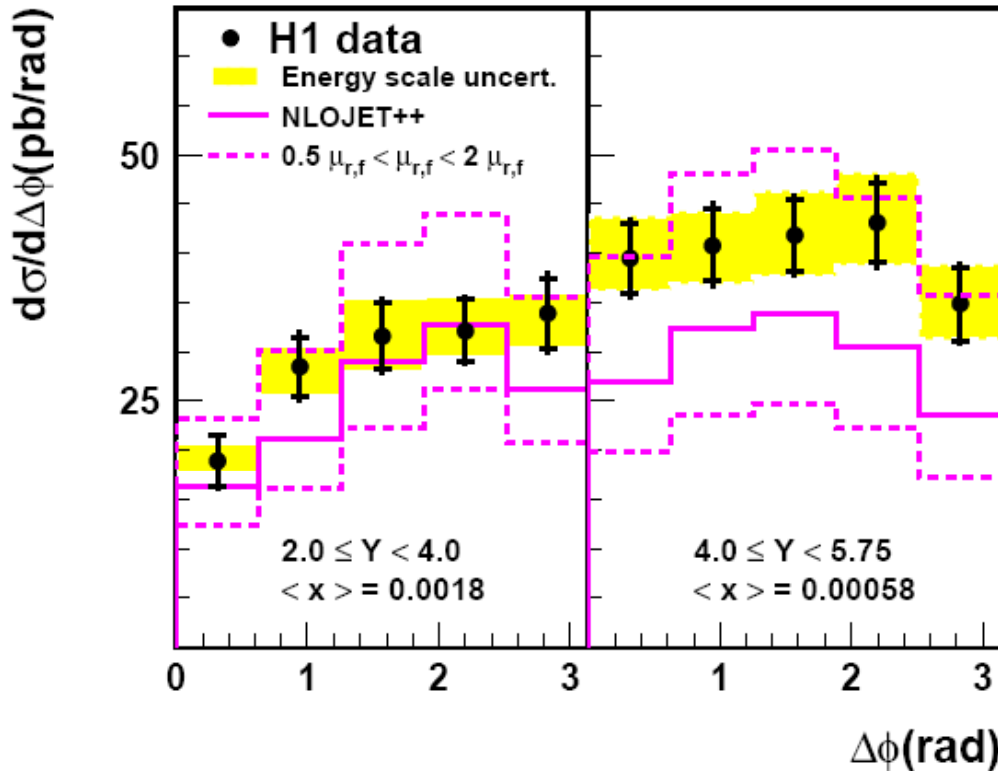
- at high Y all models are below the measurements

► with CCFM (set A0) closest to the data

# Forward and central jet cross sections $d\sigma / d\Delta\phi$

## Comparison to NLO ( $\mathcal{O}(\alpha_s^2)$ ) predictions

forward and central jet



### NLO predictions

- at low Y reasonable description of the data
- at high Y, central value too small but the data still within theory uncertainty
- large scale uncertainty ( of up to 40% ) indicates importance of higher order contributions

### NLOJET++

PDF : CTEQ6.6,  $\alpha_s(M_Z)=0.118$

$$\mu_r^2 = \mu_f^2 = (0.5 (\mathbf{p}_{T, \text{fwdjet}} + \mathbf{p}_{T, \text{cenjet}})^2 + Q^2) / 2$$

## Conclusions

- Differential cross sections & normalised distributions have been measured as a function of  $\Delta\phi$  and the rapidity separation  $Y$ , between the forward jet and the scattered positron
- Cross sections are best described by the BFKL-like model CDM
- DGLAP-based RAPGAP model is substantially below the data
- The CCFM model gives a reasonable description of the data but shows sizeable sensitivity to uPDF
- The shape of  $\Delta\phi$  distributions is well described by MC models based on different QCD evolution schemes
- NLO DGLAP predictions are in general below the data, but still in agreement with the large theoretical uncertainties

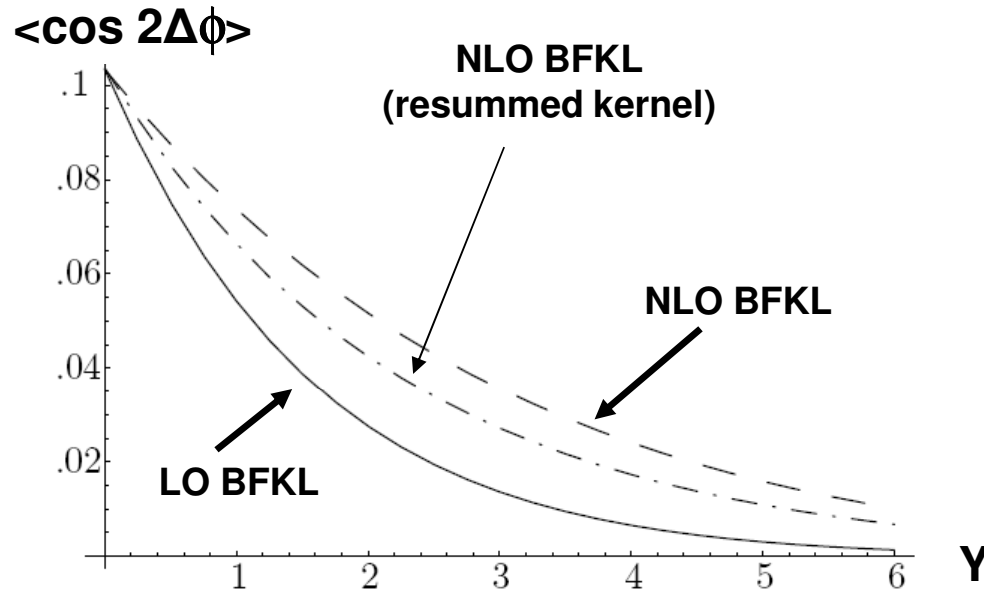


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# Forward jet production at NLO BFKL

S. Vera and F. Schwennsen, Phys. Rev. D77 (2008) 014001

**BFKL kernel at NLO accuracy**, jet vertex & photon impact factor using LO approximation



**Results**  
for forward jets with ZEUS cuts

$$20 < Q^2 < 100 \text{ GeV}^2$$

$$0.05 < y < 0.7$$

$$4 \cdot 10^{-4} < x_{Bj} < 5 \cdot 10^{-3}$$

$$0.5 < p_t^2 / Q^2 < 2.0$$

$$\Delta\phi = \phi_{el} - \phi_{fwdjet}$$

$$Y = \ln(x_{jet} / x_{BJ}) - \text{evolution length in BFKL formalism}$$

- The forward jet is more decorrelated from the scattered lepton for larger rapidity difference  $Y$  (center of mass energy)
- The azimuthal angle correlations increase when HO corrections are included for a fixed value of  $Y$

## Systematic uncertainties

	$\frac{d\sigma}{d\Delta\phi}$ $f_j$	$\frac{d\sigma}{d\Delta\phi}$ $f_j + c_j$	$d\sigma/dY$
Model dependence (CDM,Rapgap)		2 – 6%	
LAr hadronic en. scale ( $\pm 4\%$ )		7 – 12%	
Spacal em en. scale ( $\pm 1\%$ )		below 3%	
Angle of scattered electron ( $\pm 1$ mrad)		negligible effect	
Trigger		2 – 4%	
Luminosity		1.5%	
Total		11 – 12%	

## $\Delta\phi$ decorrelation :

### no discrimination between different evolution schemes

- **forward jet originates from the hard matrix elements ?**  
( similar in used MC models)

Studies of parton to hadron correlation with the DGLAP-based RAPGAP model :

- ▶ define "distance measure"  $\Delta R$  between parton jet and hadron jet

$$\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\Phi)^2}$$

$\Delta R < 0.5$  hadron jet is correlated to parton from ME / from parton shower

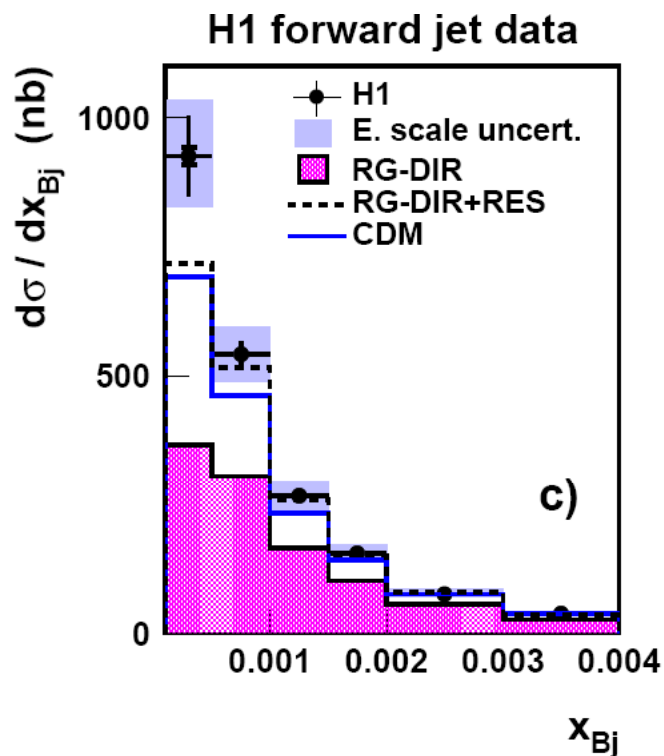
- ▶ **Y bin**

### forward jet originated from PS

bin no. 1 ( $2 < Y < 3.4$ )	51.9%
bin no. 2 ( $3.4 < Y < 4.25$ )	67.5%
bin no. 3 ( $4.25 < Y < 5.75$ )	79.0%

# Forward jet cross section $d\sigma/dx$

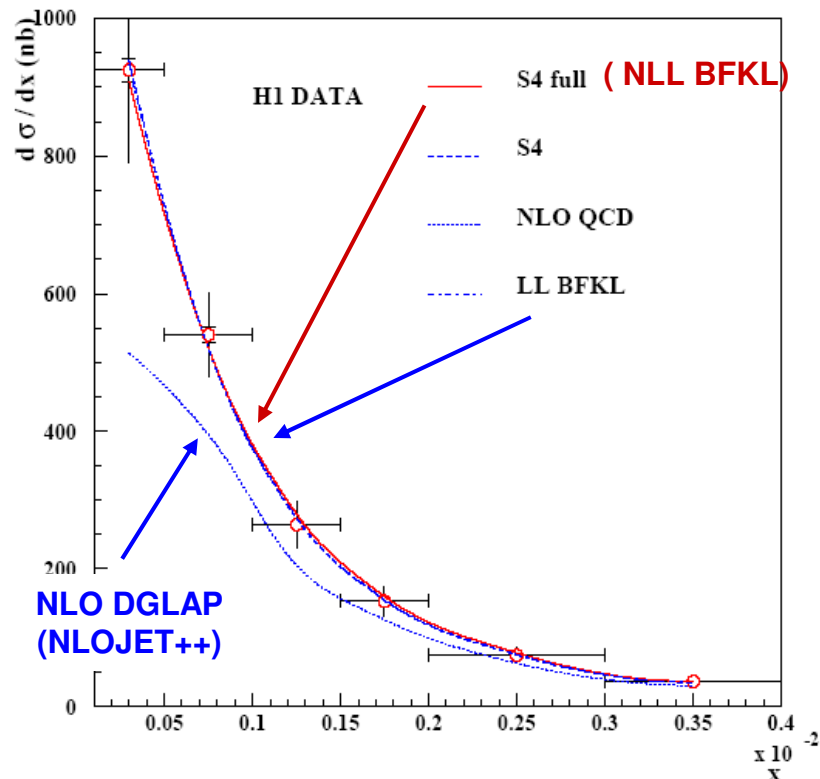
H1 data : Eur. Phys. J. C46 (2006)27



LO DGLAP (RG-DIR) below the data

CDM model and DGLAP resolved photon model (RG-DIR+RES) closest to the data, however the data are still below predictions at low  $x$

BFKL calculations  
Kepka, Royon, Marquet & Peschanski  
Phys. Lett. B665 (2007) 236



NLO DGLAP below the data at low  $x$

Difference between LL-BFKL and NLL-BFKL ( NLL BFKL kernel + free normalisation parameter ) is very small

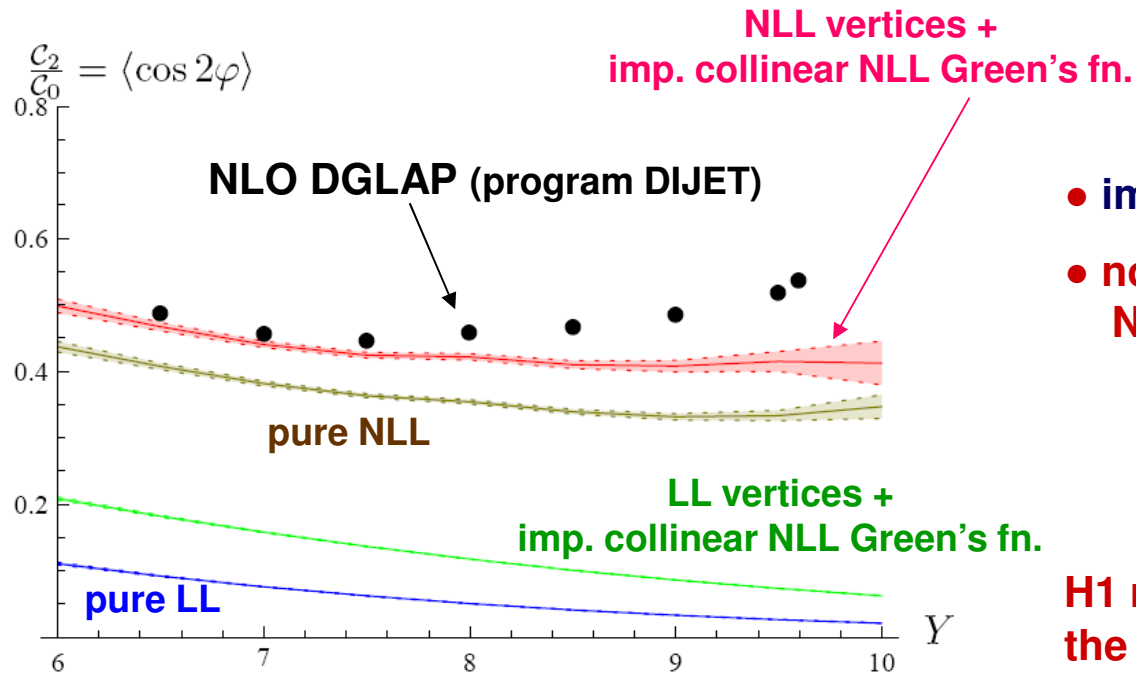
# Mueller- Navelet jets at LHC – complete NLL BFKL calculations

Colferai, Schwennsen, Szymanowski & Wallon,  
**JHEP 12(2010)026**

next-to-leading corrections to the Green's function and to the Mueller-Navelet vertices

LHC  $\sqrt{S} = 14$  TeV,  $p_{T, \text{jet1}} = 35$  GeV,  $p_{T, \text{jet2}} = 50$  GeV

Azimuthal correlation  $\langle \cos 2\phi \rangle = \langle \cos(2 \cdot (\phi_{\text{jet1}} - \phi_{\text{jet2}} - \pi)) \rangle$



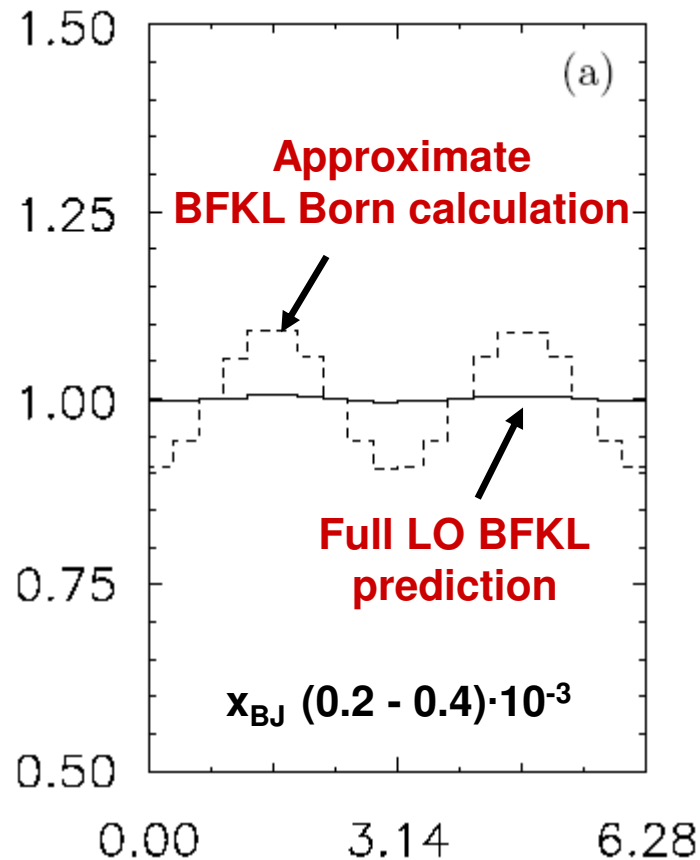
- importance of NLL vertex corrections
- no significant difference between NLL BFKL and NLO DGLAP

H1 measurements  $\rightarrow$   
 the electron-forward jet decorrelation in DIS does not discriminate between different evolution schemes

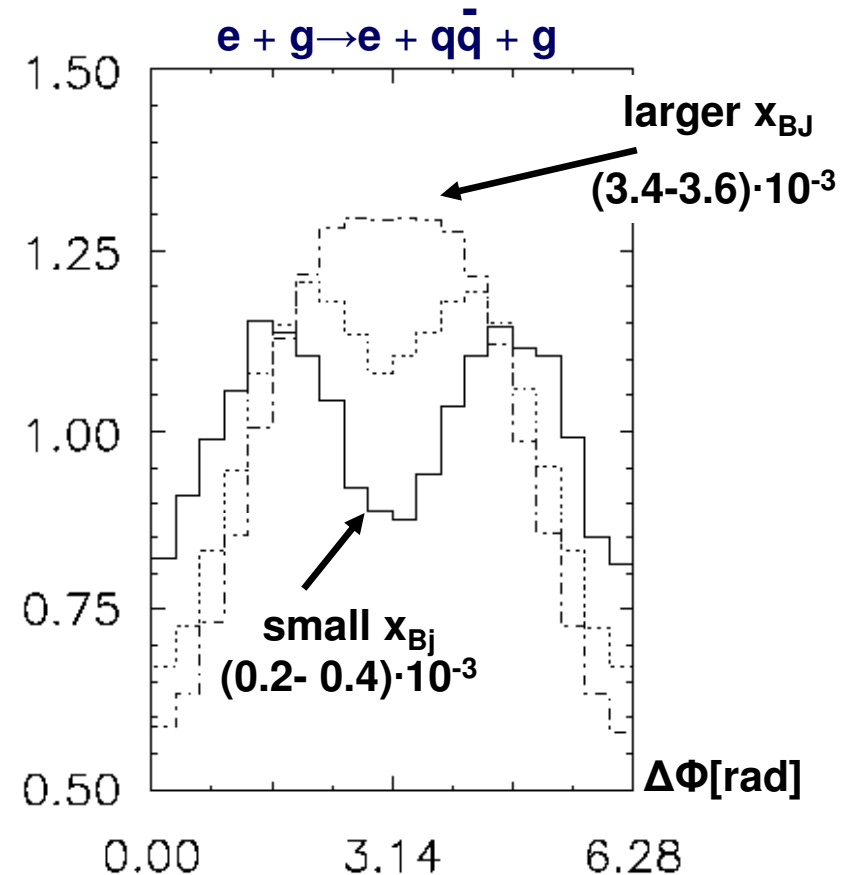
Forward jets in DIS, Bartels et al., 1996,  $\Delta\Phi = \Phi_{el} - \Phi_{jet}$  in the LAB frame

normalised  
cross section

**LO BFKL**



**Fixed order  $O(\alpha_s^2)$  predictions**



BFKL Born - clear maximum at  $\Delta\Phi = \pi/2$   
Full LO BFKL - no  $\Phi$  dependence

small  $x_{BJ}$  - fixed order  $O(\alpha_s^2)$  and BFKL Born predictions are similar  
(max. at  $\Delta\Phi \sim \pi/2$ )