

Differential and total cross sections for top pair and single top production

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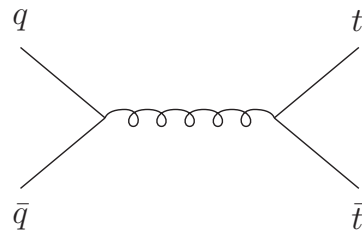
- $t\bar{t}$ and single top production channels
- Higher-order two-loop corrections
- $t\bar{t}$ cross section at LHC and Tevatron
- Top p_T and rapidity distributions
- t -channel production
- s -channel production
- Associated production of a top with a W^- or H^-

Partonic processes at LO

Top-antitop pair production

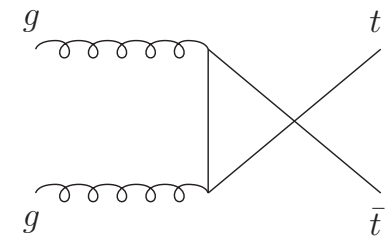
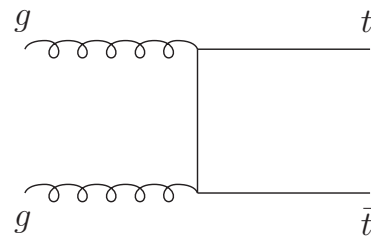
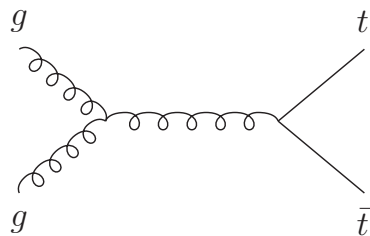
- $q\bar{q} \rightarrow t\bar{t}$

dominant at Tevatron



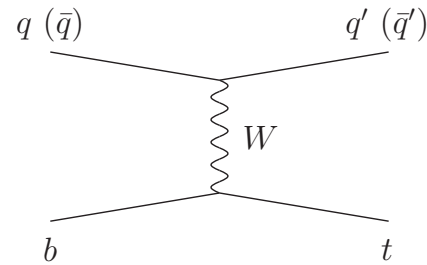
- $gg \rightarrow t\bar{t}$

dominant at LHC

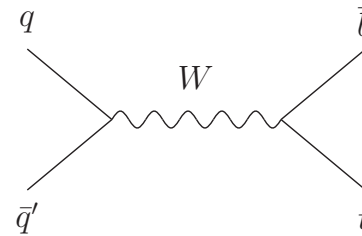


Single top quark production

- **t channel:** $qb \rightarrow q't$ and $\bar{q}b \rightarrow \bar{q}'t$
dominant at Tevatron and LHC

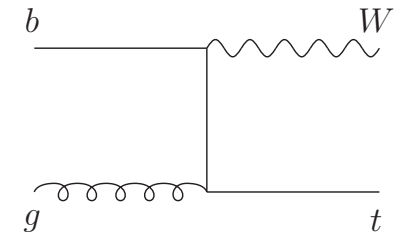
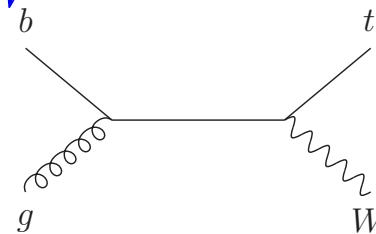


- **s channel:** $q\bar{q}' \rightarrow \bar{b}t$
small at Tevatron and LHC



- **associated tW production:** $bg \rightarrow tW^-$
very small at Tevatron, significant at LHC

Related process: $bg \rightarrow tH^-$



Higher-order corrections

QCD corrections significant for top pair and single top quark production

Soft-gluon corrections from emission of soft (low-energy) gluons

Soft corrections: $\left[\frac{\ln^k(s_4/m^2)}{s_4} \right]_+$ with $k \leq 2n - 1$, s_4 distance from threshold

Soft-gluon corrections are dominant near threshold

Resum these soft corrections - factorization and RGE

Complete results at NNLL–two-loop soft anomalous dimension

NK, PRD 82, 114030 (2010); PRD 84, 011504 (2011) ($t\bar{t}$)

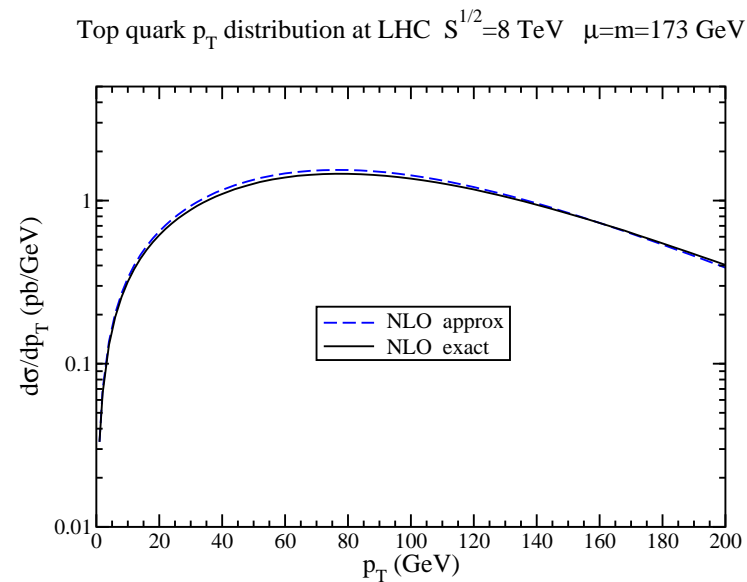
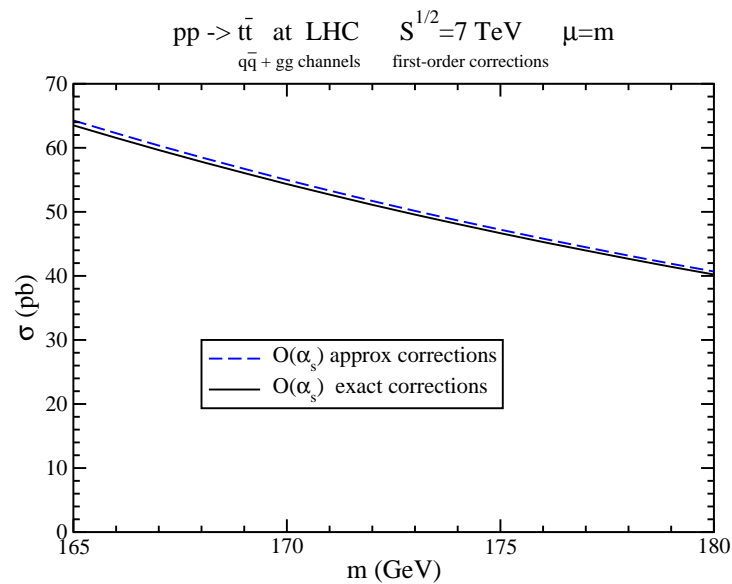
NK, PRD81, 054028 (2010); PRD 82, 054018 (2010); PRD 83,091503 (2011) (single top)

Approximate NNLO cross section from expansion of resummed cross section

This is the only calculation at the differential cross section level using the standard moment-space resummation in pQCD

Threshold approximation

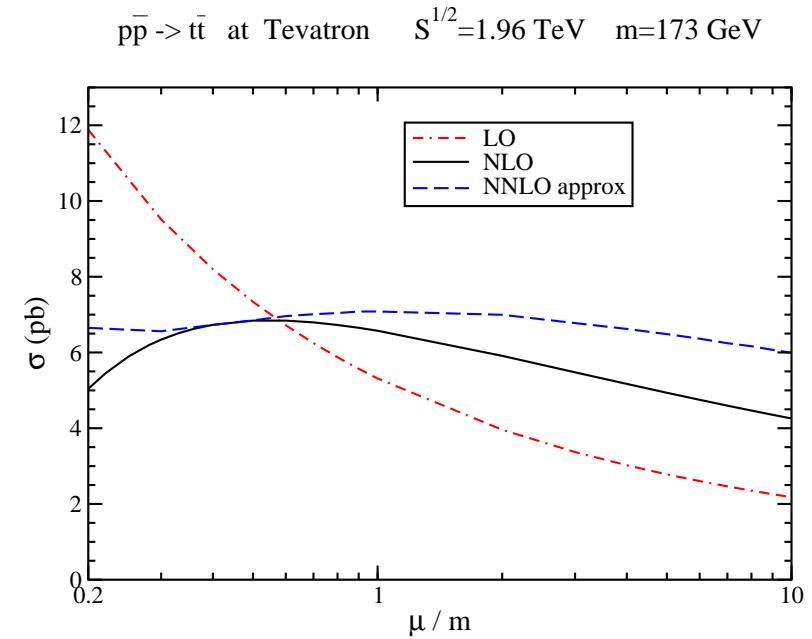
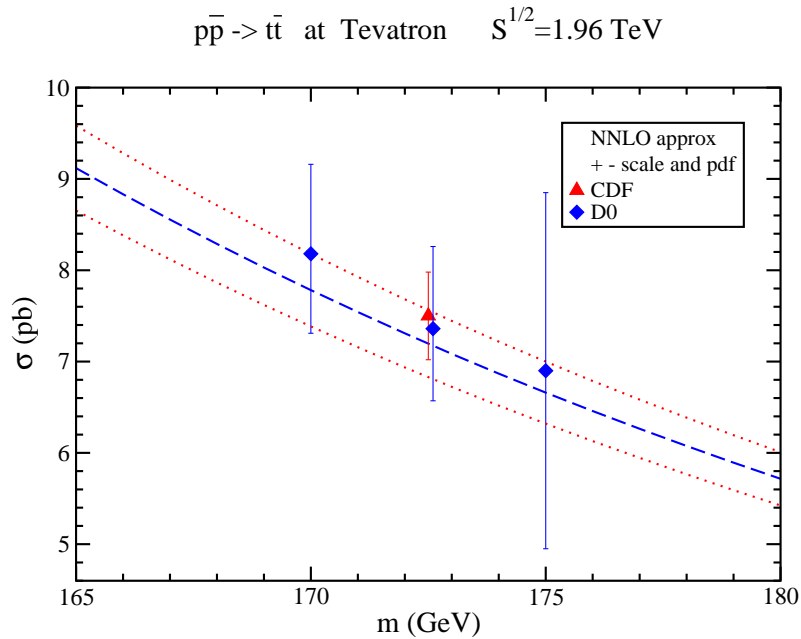
Approximation works very well not only for Tevatron but also for LHC energies because partonic threshold is still important



only 1% difference between first-order approximate and exact corrections
 \rightarrow less than 1% difference between NLO approximate and exact cross sections
Also true for differential distributions

For best prediction add NNLO approximate corrections to exact NLO cross section

$t\bar{t}$ cross section at the Tevatron



$$\sigma_{t\bar{t}}^{\text{NNLOapprox}}(m_t = 173 \text{ GeV}, 1.96 \text{ TeV}) = 7.08^{+0.00+0.36}_{-0.24-0.27} \text{ pb}$$

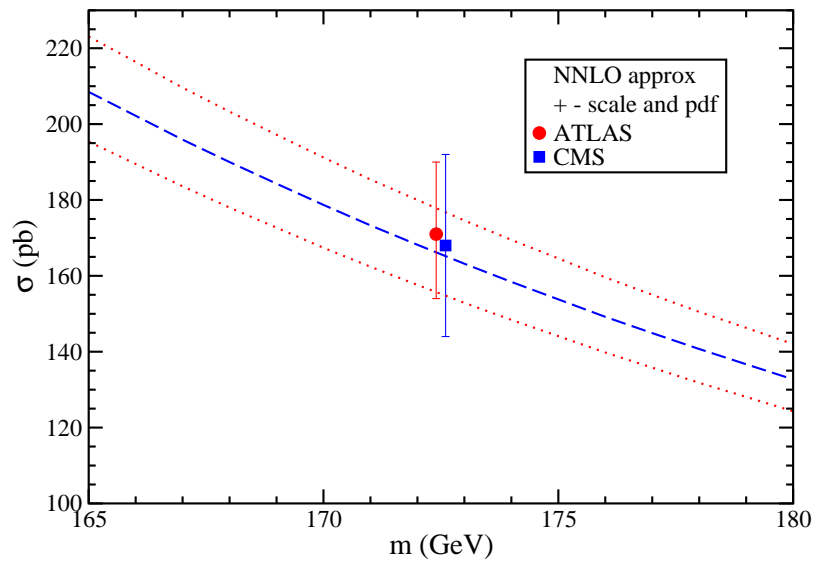
scale pdf

NNLO approx: 7.8% enhancement over NLO
scale dependence greatly reduced

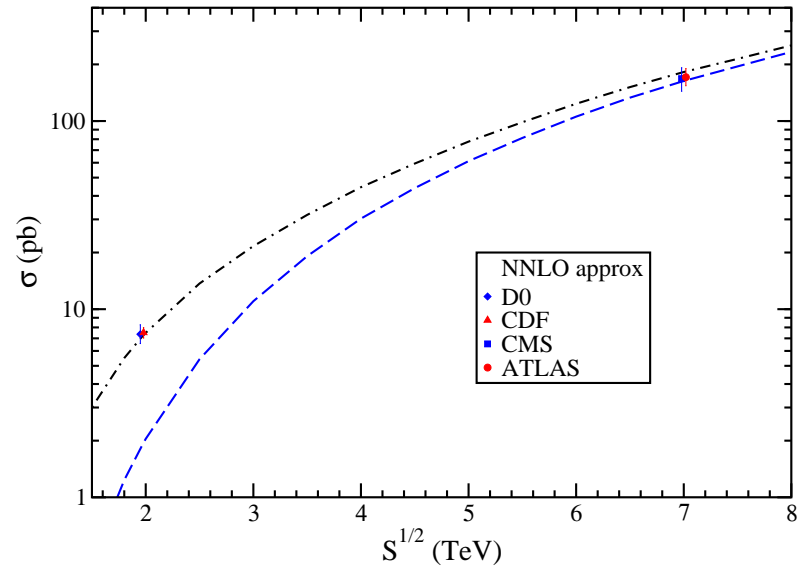
used MSTW 2008 NNLO pdf

$t\bar{t}$ cross section at the LHC

$pp \rightarrow t\bar{t}$ at LHC $S^{1/2} = 7$ TeV



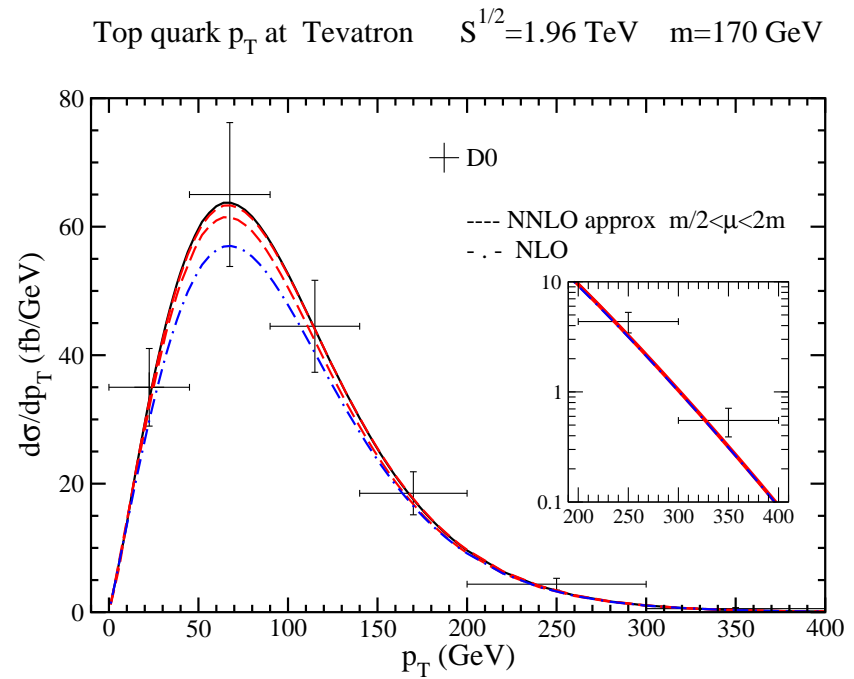
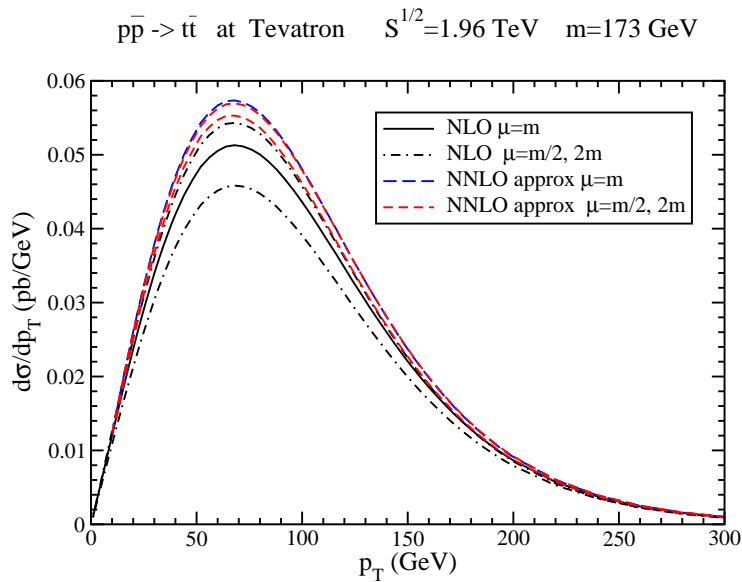
$t\bar{t}$ cross section at $p\bar{p}$ and pp colliders



$$\begin{aligned} \sigma_{t\bar{t}}^{\text{NNLOapprox}}(m_t = 173 \text{ GeV}, 7 \text{ TeV}) &= 163_{-5}^{+7} \pm 9 \text{ pb} \\ \sigma_{t\bar{t}}^{\text{NNLOapprox}}(m_t = 173 \text{ GeV}, 8 \text{ TeV}) &= 234_{-7}^{+10} \pm 12 \text{ pb} \\ \sigma_{t\bar{t}}^{\text{NNLOapprox}}(m_t = 173 \text{ GeV}, 14 \text{ TeV}) &= 920_{-39}^{+50} {}_{-35}^{+33} \text{ pb} \end{aligned}$$

**NNLO approx: enhancement over NLO (same pdf) is 7.6% at 7 TeV;
7.8% at 8 TeV; 8.0% at 14 TeV**

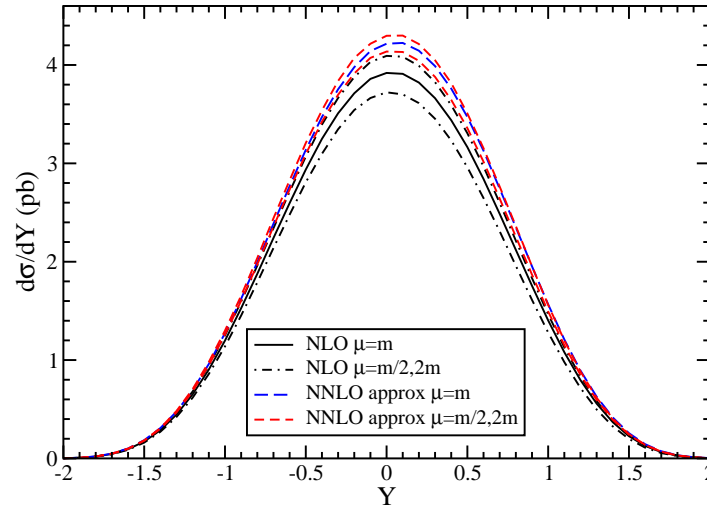
Top quark p_T distribution at Tevatron



Excellent agreement of NNLO approx results with D0 data

Top quark rapidity distribution at Tevatron

Top quark rapidity at Tevatron $S^{1/2}=1.96$ TeV $m=173$ GeV



Top Forward-backward asymmetry

$$A_{\text{FB}} = \frac{\sigma(Y > 0) - \sigma(Y < 0)}{\sigma(Y > 0) + \sigma(Y < 0)}$$

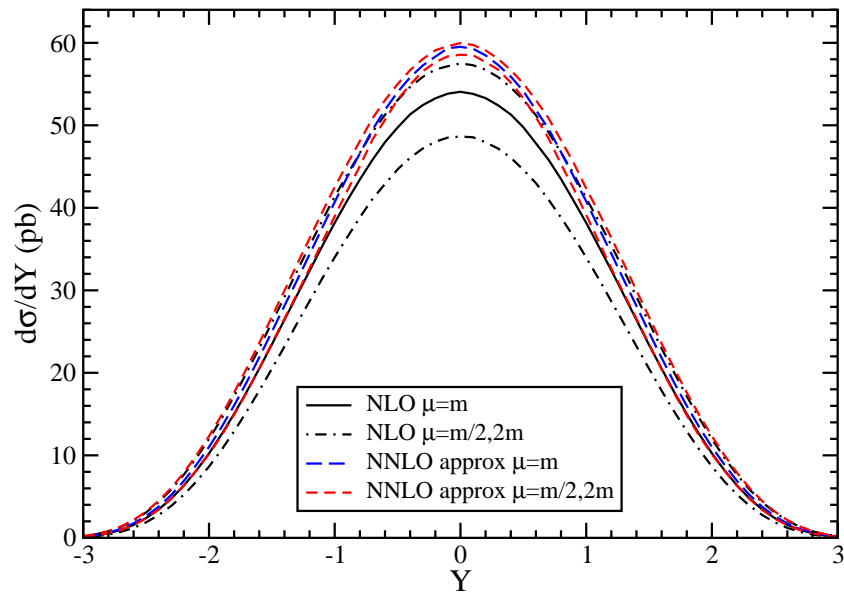
Asymmetry significant at the Tevatron

Theoretical result at Tevatron: $A_{\text{FB}} = 0.052^{+0.000}_{-0.006}$

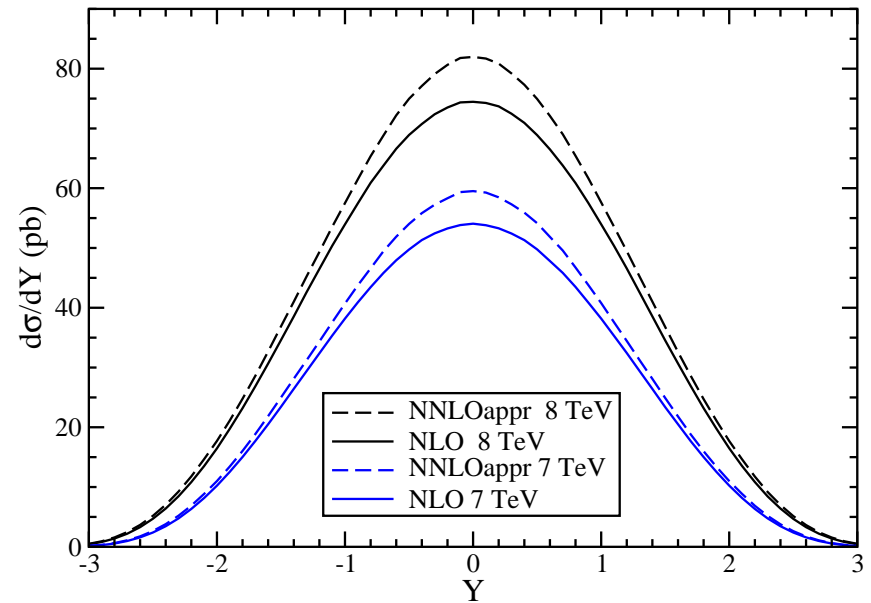
smaller than observed values

Top quark rapidity distribution at LHC

Top quark rapidity at LHC $S^{1/2}=7$ TeV $m=173$ GeV

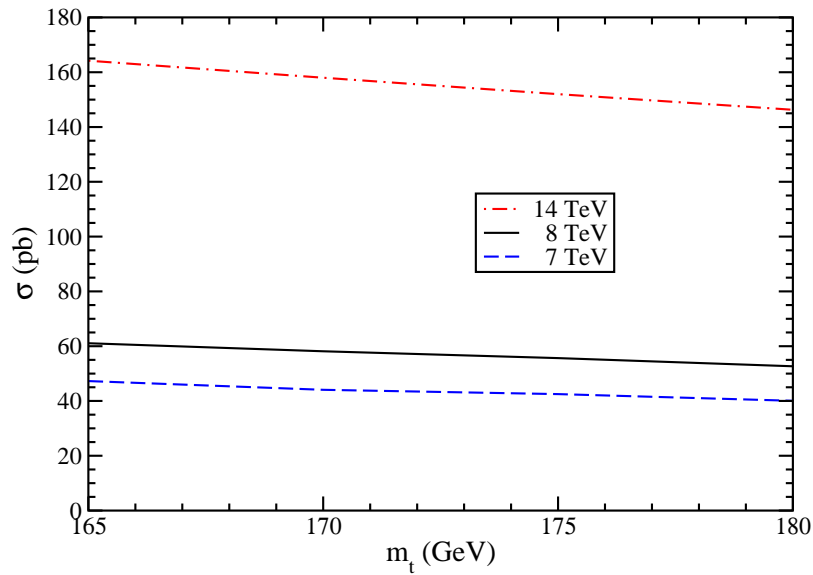


Top quark rapidity distribution at LHC $\mu=m=173$ GeV

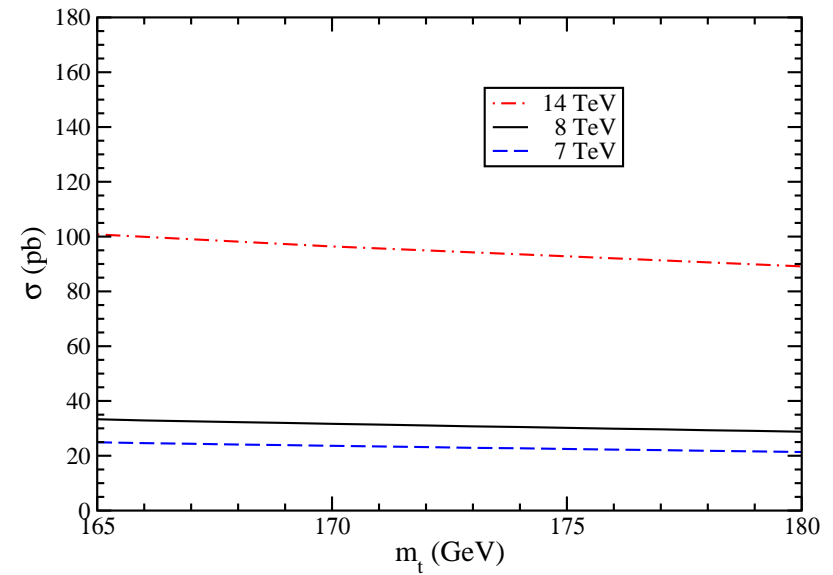


t -channel cross sections at LHC

Single top LHC t -channel NNLO approx (NNLL) $\mu = m_t$



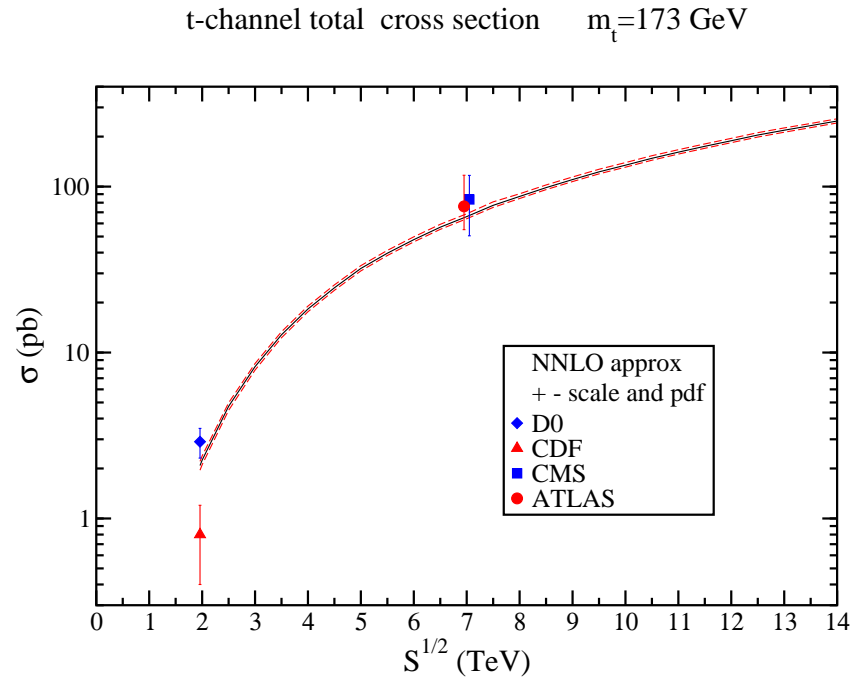
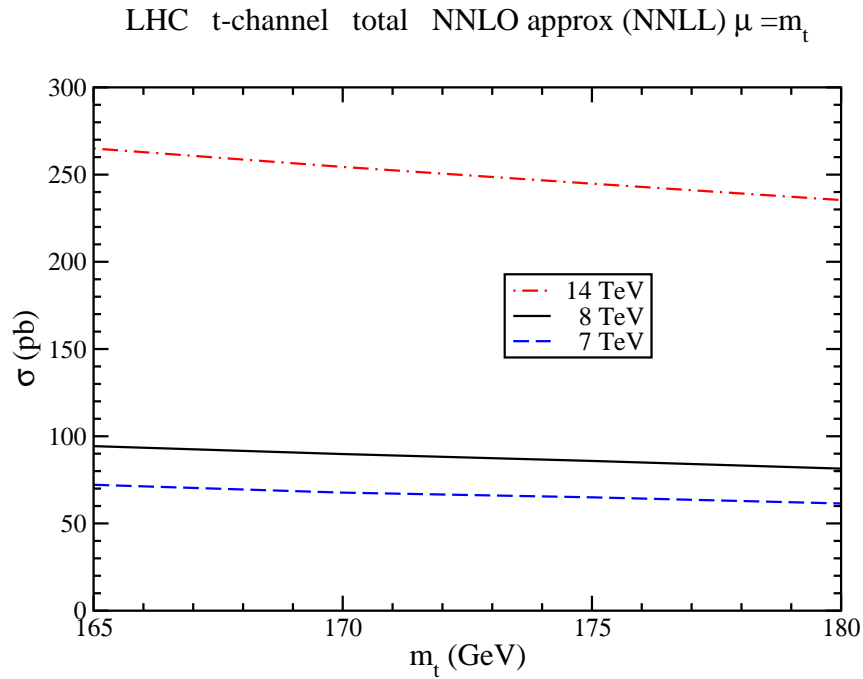
Single antitop LHC t -channel NNLO approx (NNLL) $\mu = m_t$



For $m_t = 173$ GeV

LHC	t	\bar{t}
7 TeV	$43.0^{+1.6}_{-0.2} \pm 0.8$	$22.9 \pm 0.5^{+0.7}_{-0.9}$
8 TeV	$56.4^{+2.1}_{-0.3} \pm 1.1$	$30.7 \pm 0.7^{+0.9}_{-1.1}$
14 TeV	$154^{+4}_{-1} \pm 3$	94^{+2+2}_{-1-3}

t-channel total cross section at LHC



$$\sigma_{t\text{-channel}}^{\text{NNLOapprox, total}}(m_t = 173 \text{ GeV}, 7 \text{ TeV}) = 65.9_{-0.7-1.7}^{+2.1+1.5} \text{ pb}$$

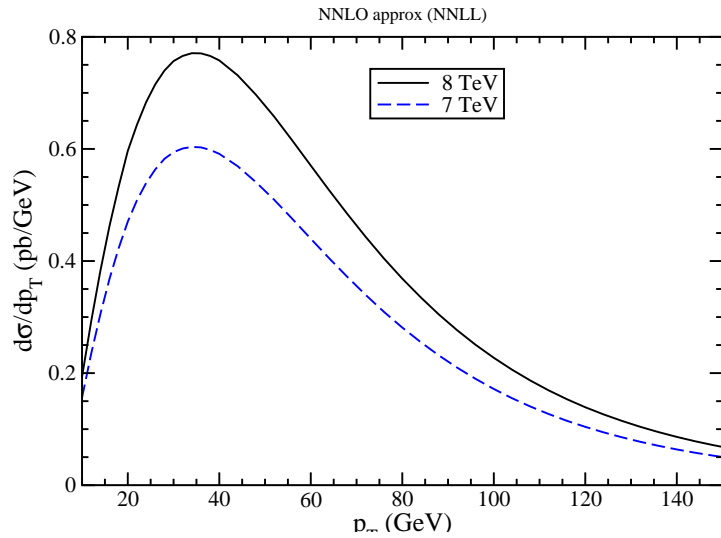
$$\sigma_{t\text{-channel}}^{\text{NNLOapprox, total}}(m_t = 173 \text{ GeV}, 8 \text{ TeV}) = 87.2_{-1.0-2.2}^{+2.8+2.0} \text{ pb}$$

$$\sigma_{t\text{-channel}}^{\text{NNLOapprox, total}}(m_t = 173 \text{ GeV}, 14 \text{ TeV}) = 248_{-2-6}^{+6+5} \text{ pb}$$

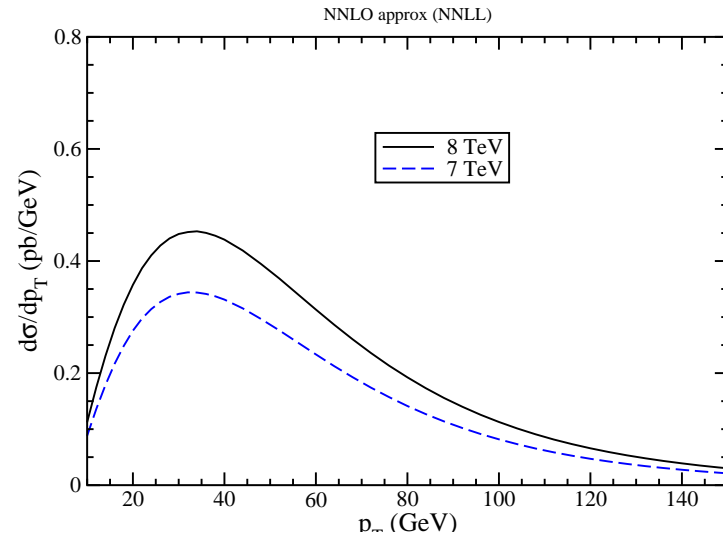
Small $\mathcal{O}(1\%)$ corrections over NLO

t -channel top and antitop p_T distributions at LHC

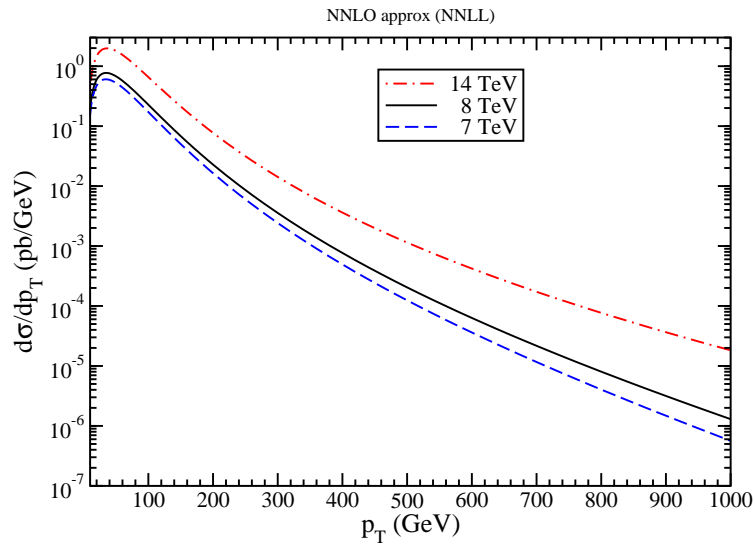
t-channel top quark p_T distribution at LHC $\mu=m_t=173$ GeV



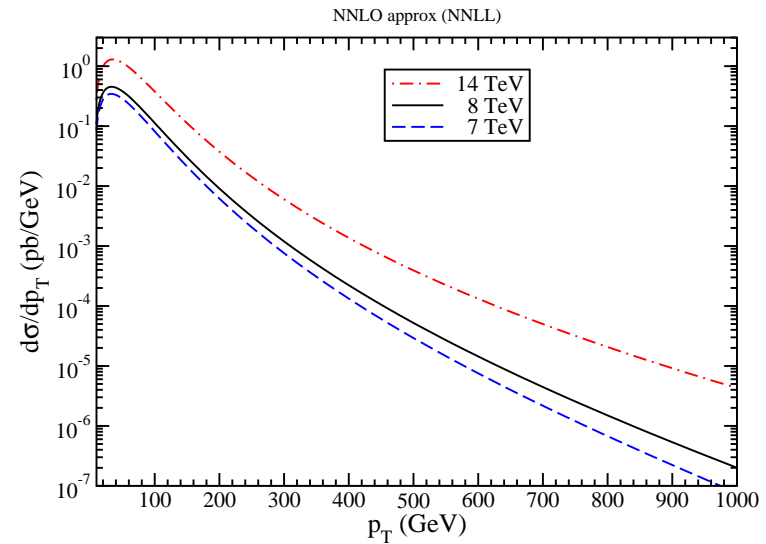
t-channel antitop quark p_T distribution at LHC $\mu=m_t=173$ GeV



t-channel top quark p_T distribution at LHC $\mu=m_t=173$ GeV

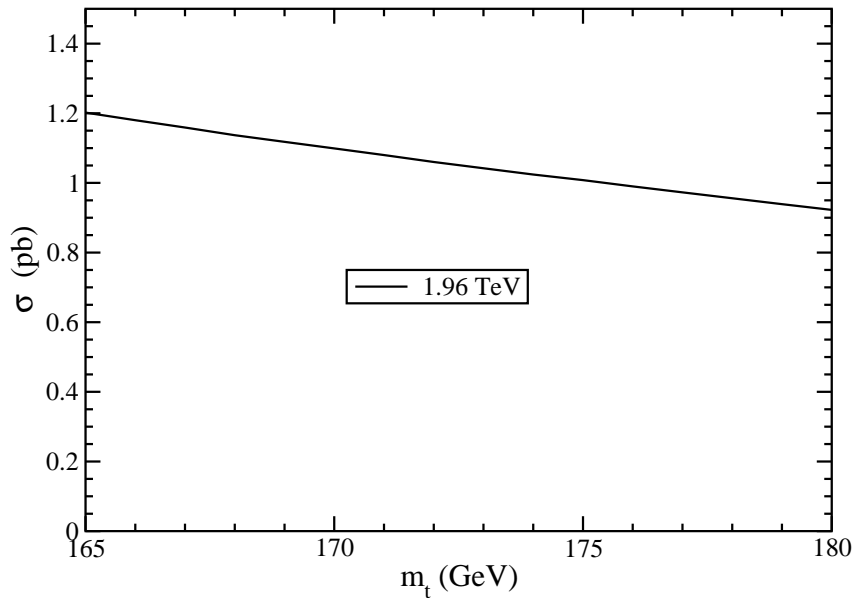


t-channel antitop quark p_T distribution at LHC $\mu=m_t=173$ GeV

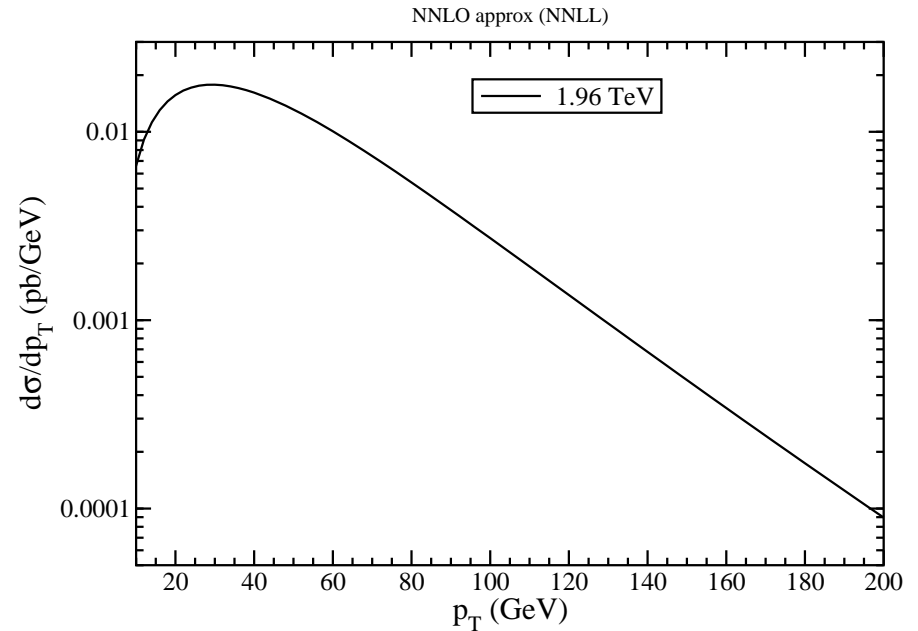


t-channel top quark production at Tevatron

Single top Tevatron t-channel NNLO approx (NNLL) $\mu=m_t$



t-channel top quark p_T distribution at Tevatron $\mu=m_t=173$ GeV

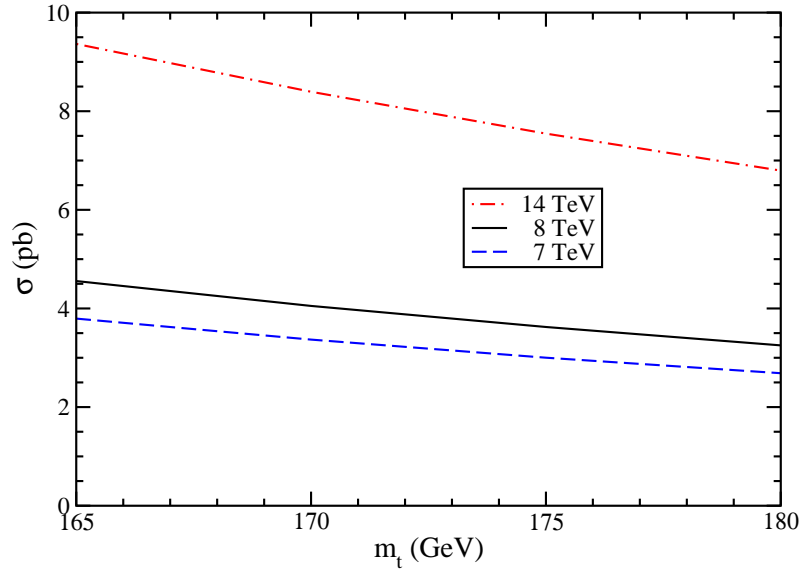


$$\sigma_{t\text{-channel}}^{\text{NNLOapprox, top}}(m_t = 173 \text{ GeV}, 1.96 \text{ TeV}) = 1.04_{-0.02}^{+0.00} \pm 0.06 \text{ pb}$$

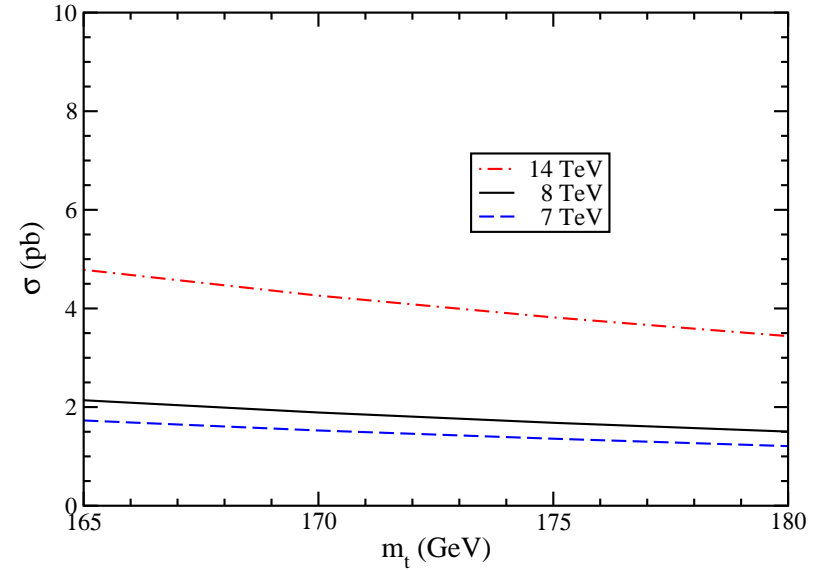
Cross section for antitop t-channel production at Tevatron is identical

s-channel cross sections

Single top LHC s-channel NNLO approx (NNLL) $\mu = m_t$



Single antitop LHC s-channel NNLO approx (NNLL) $\mu = m_t$

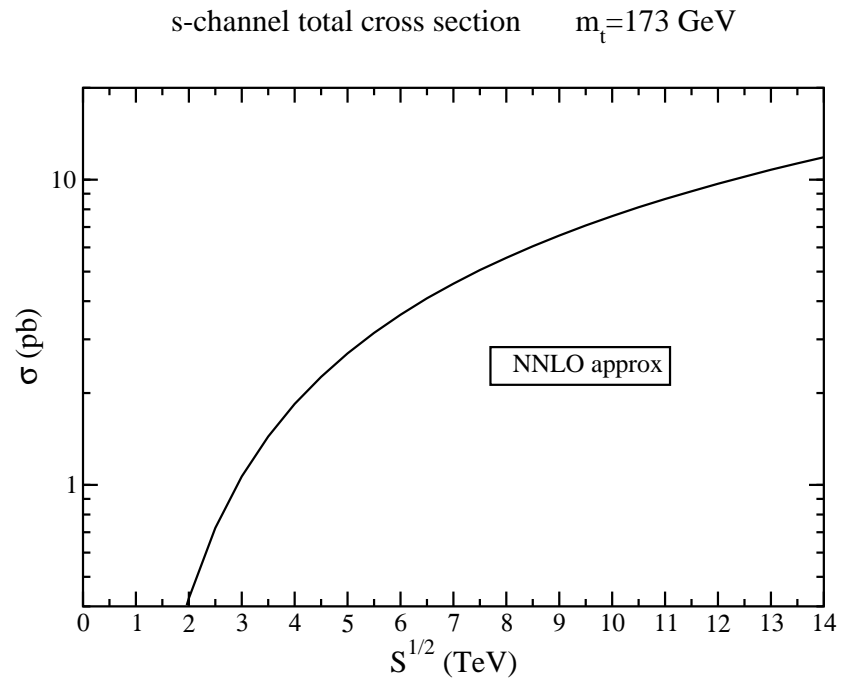
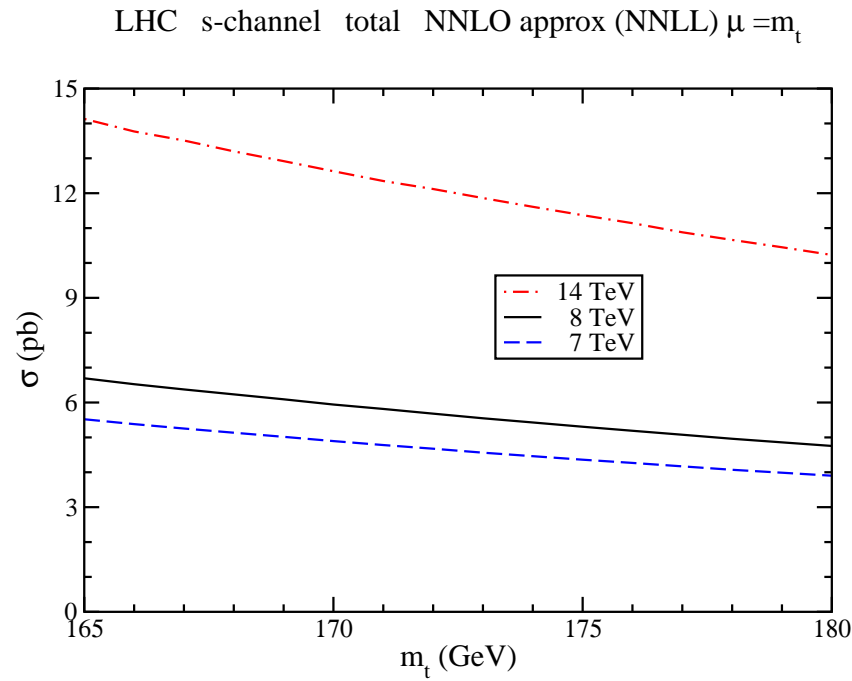


For $m_t = 173 \text{ GeV}$

LHC	t	\bar{t}
7 TeV	$3.14 \pm 0.06^{+0.12}_{-0.10}$	$1.42 \pm 0.01^{+0.06}_{-0.07}$
8 TeV	$3.79 \pm 0.07 \pm 0.13$	$1.76 \pm 0.01 \pm 0.08$
14 TeV	$7.87 \pm 0.14^{+0.31}_{-0.28}$	$3.99 \pm 0.05^{+0.14}_{-0.21}$

At Tevatron $\sqrt{S} = 1.96 \text{ TeV}$: $0.523^{+0.001+0.030}_{-0.005-0.028} \text{ pb}$ for top; same for antitop

s-channel total cross section at LHC

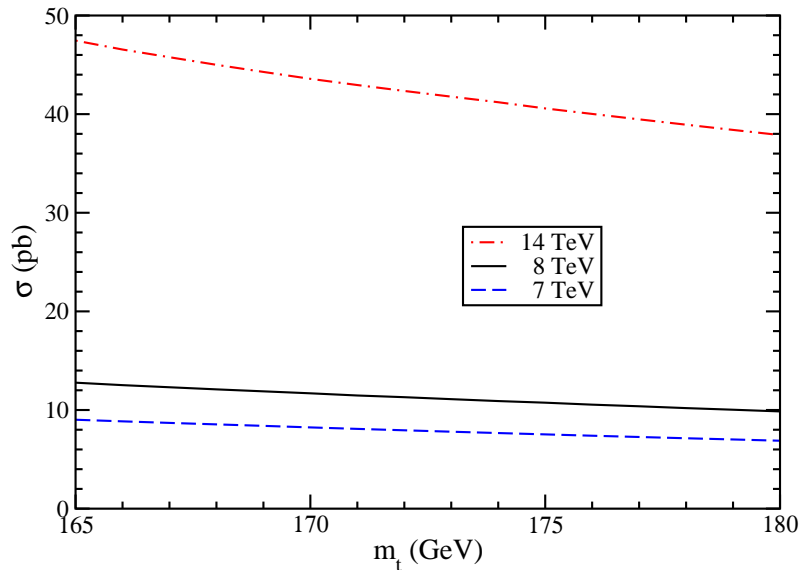


$$\begin{aligned} \sigma_{s\text{-channel}}^{\text{NNLOapprox, total}}(m_t = 173 \text{ GeV}, 7 \text{ TeV}) &= 4.56 \pm 0.07^{+0.18}_{-0.17} \text{ pb} \\ \sigma_{s\text{-channel}}^{\text{NNLOapprox, total}}(m_t = 173 \text{ GeV}, 8 \text{ TeV}) &= 5.55 \pm 0.08 \pm 0.21 \text{ pb} \\ \sigma_{s\text{-channel}}^{\text{NNLOapprox, total}}(m_t = 173 \text{ GeV}, 14 \text{ TeV}) &= 11.86 \pm 0.19^{+0.45}_{-0.49} \text{ pb} \end{aligned}$$

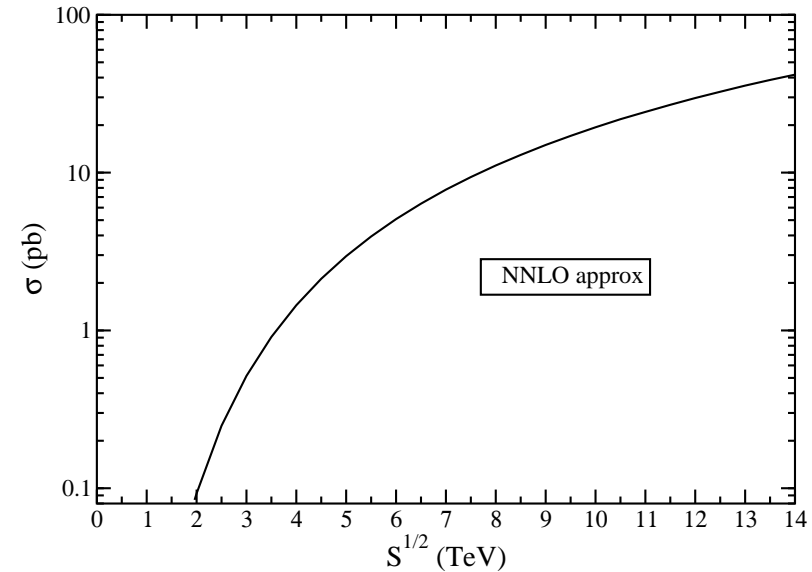
NNLO approx: enhancement over NLO is $\sim 10\%$

Associated tW^- production at the LHC

tW production at LHC NNLO approx (NNLL) $\mu = m_t$



tW cross section $m_t = 173$ GeV

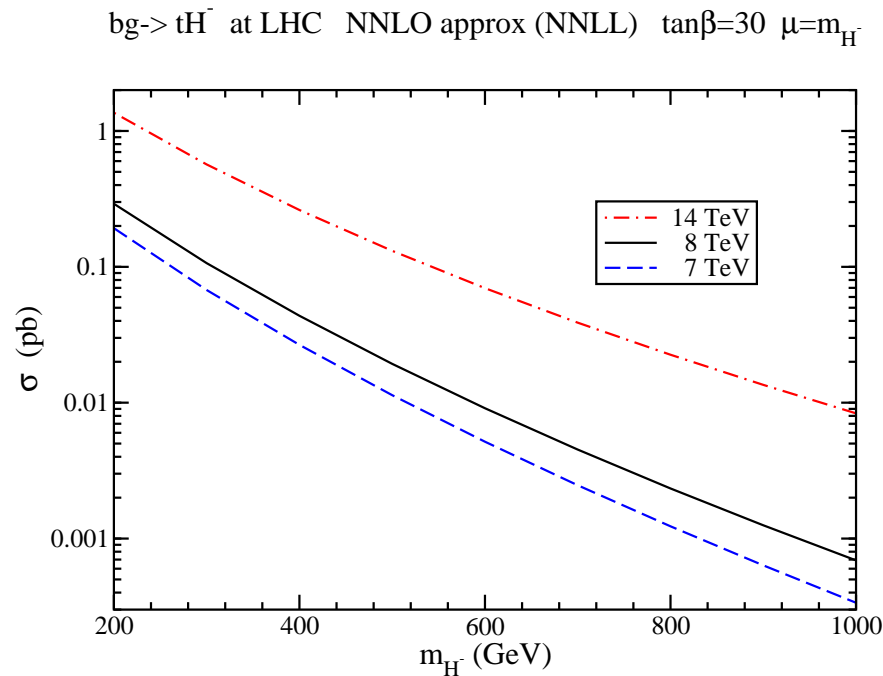


$$\begin{aligned} \sigma_{tW}^{\text{NNLOapprox}}(m_t = 173 \text{ GeV}, 7 \text{ TeV}) &= 7.8 \pm 0.2_{-0.6}^{+0.5} \text{ pb} \\ \sigma_{tW}^{\text{NNLOapprox}}(m_t = 173 \text{ GeV}, 8 \text{ TeV}) &= 11.1 \pm 0.3 \pm 0.7 \text{ pb} \\ \sigma_{tW}^{\text{NNLOapprox}}(m_t = 173 \text{ GeV}, 14 \text{ TeV}) &= 41.8 \pm 1.0_{-2.4}^{+1.5} \text{ pb} \end{aligned}$$

NNLO approx corrections increase NLO cross section by $\sim 8\%$

Cross section for $\bar{t}W^+$ production is identical

Associated production of a top quark with a charged Higgs



NNLO approx corrections increase NLO cross section by ~ 15 to $\sim 20\%$

Summary

- NNLL resummation for top quark pair and single top production
- $t\bar{t}$ production cross section
- top quark p_T and rapidity distributions
- single top cross sections and p_T distributions
- NNLO approx corrections for top pair and single top production are significant at Tevatron and LHC
- good agreement with LHC and Tevatron data