

Heavy Quark Production in the ACOT Scheme at NNLO and N3LO

Fred Olness

SMU

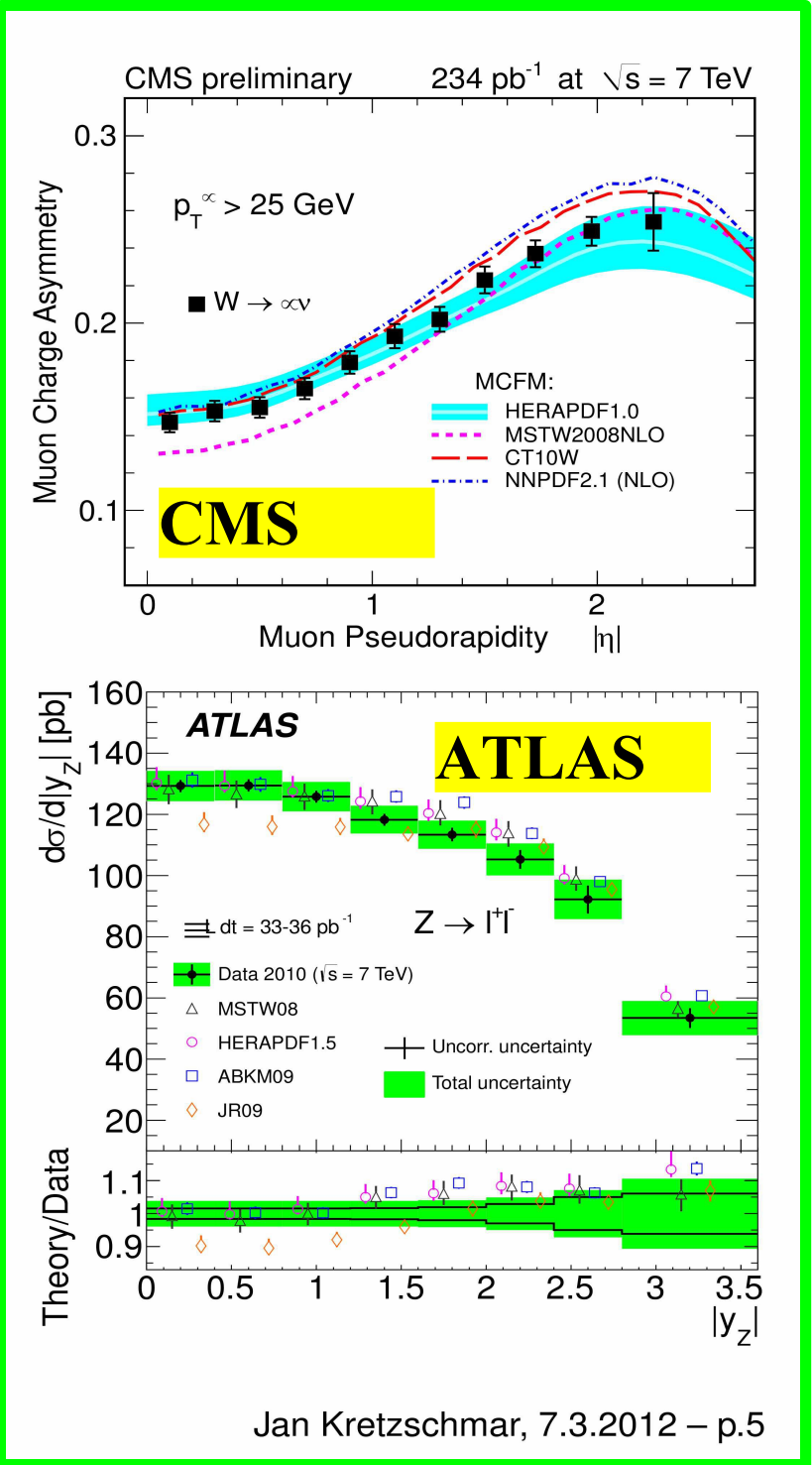
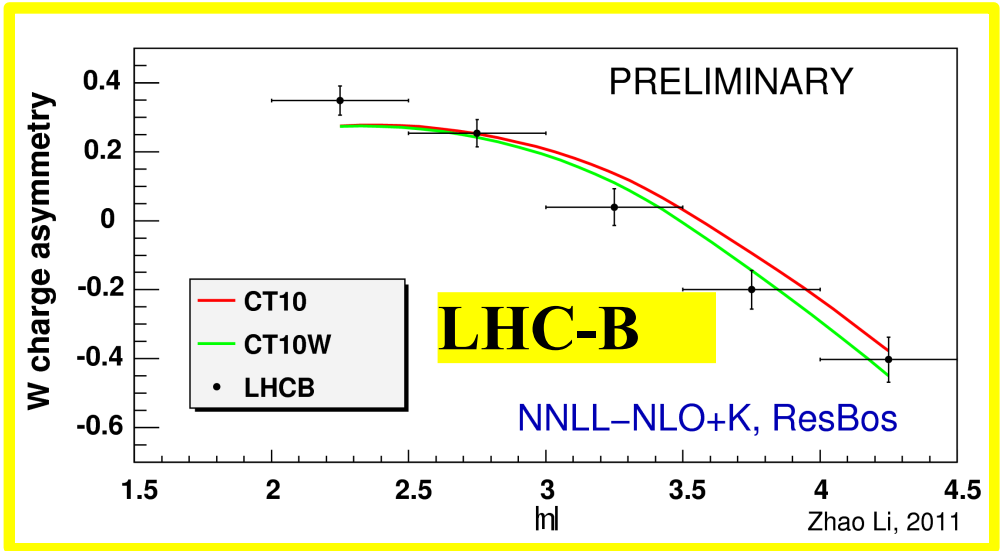
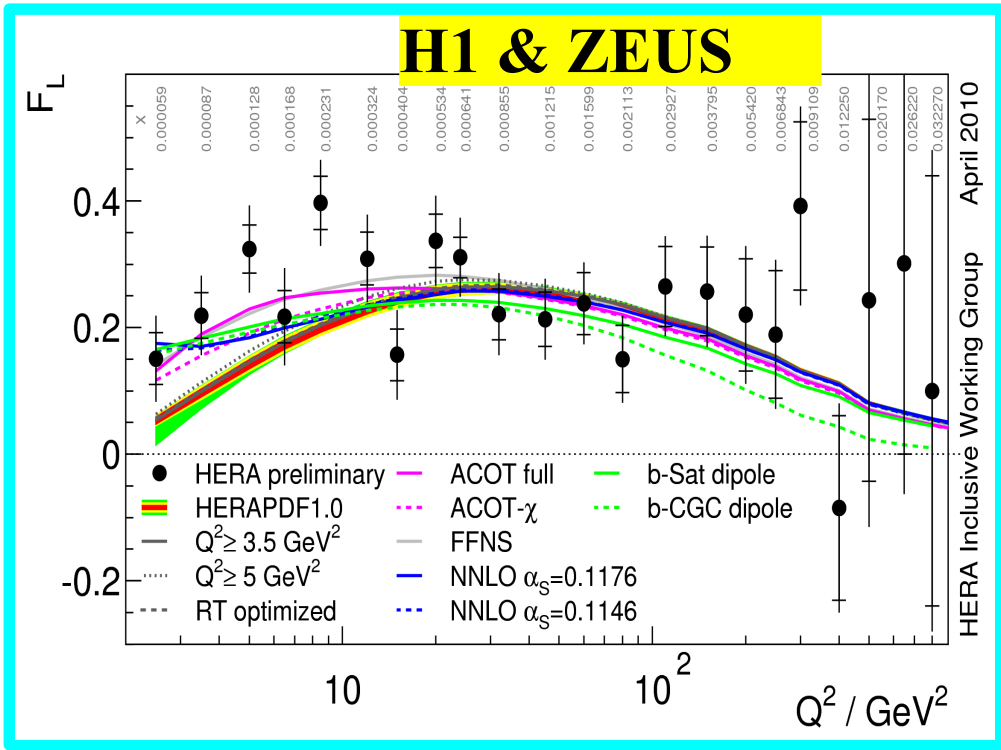
Conspirators:

**K. Kovarik, I Schienbein, J. Yu, J. Morfin, P. Nadolsky,
T.P. Stavreva, A. Kusina, M. Guzzi, J. Gao, Z. Liang
J. Owens, C. Keppel, D. Soper ...**

DIS 2012, Bonn
28 March 2012

Motivation

Recent Measurements: Requires Theoretical Improvements



ACOT

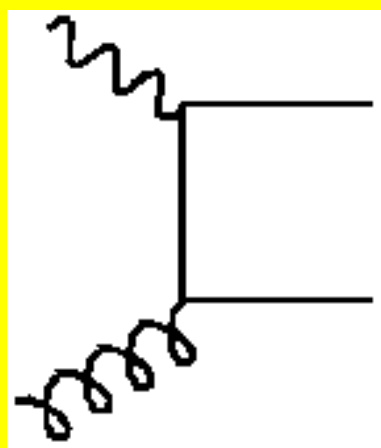
@ NNLO + N³LO

Stavreva, Olness, Schienbein, Jezo, Kusina, Kovarik, Yu
arXiv:1203.0282

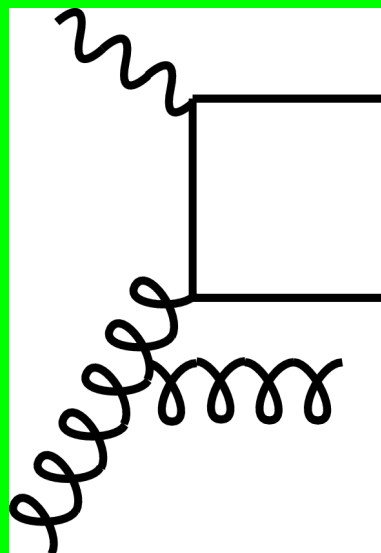
LO



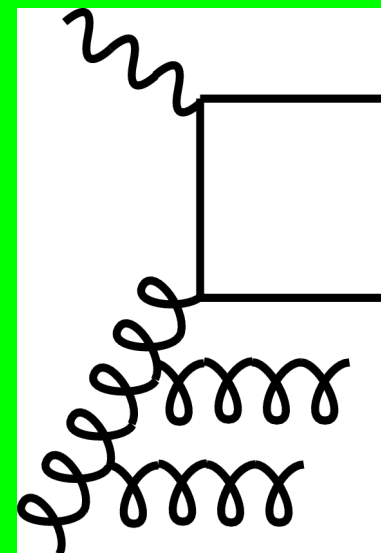
NLO



N2LO



N3LO



Full ACOT

Based on the Collins-Wilczek-Zee (CWZ) Renormalization Scheme

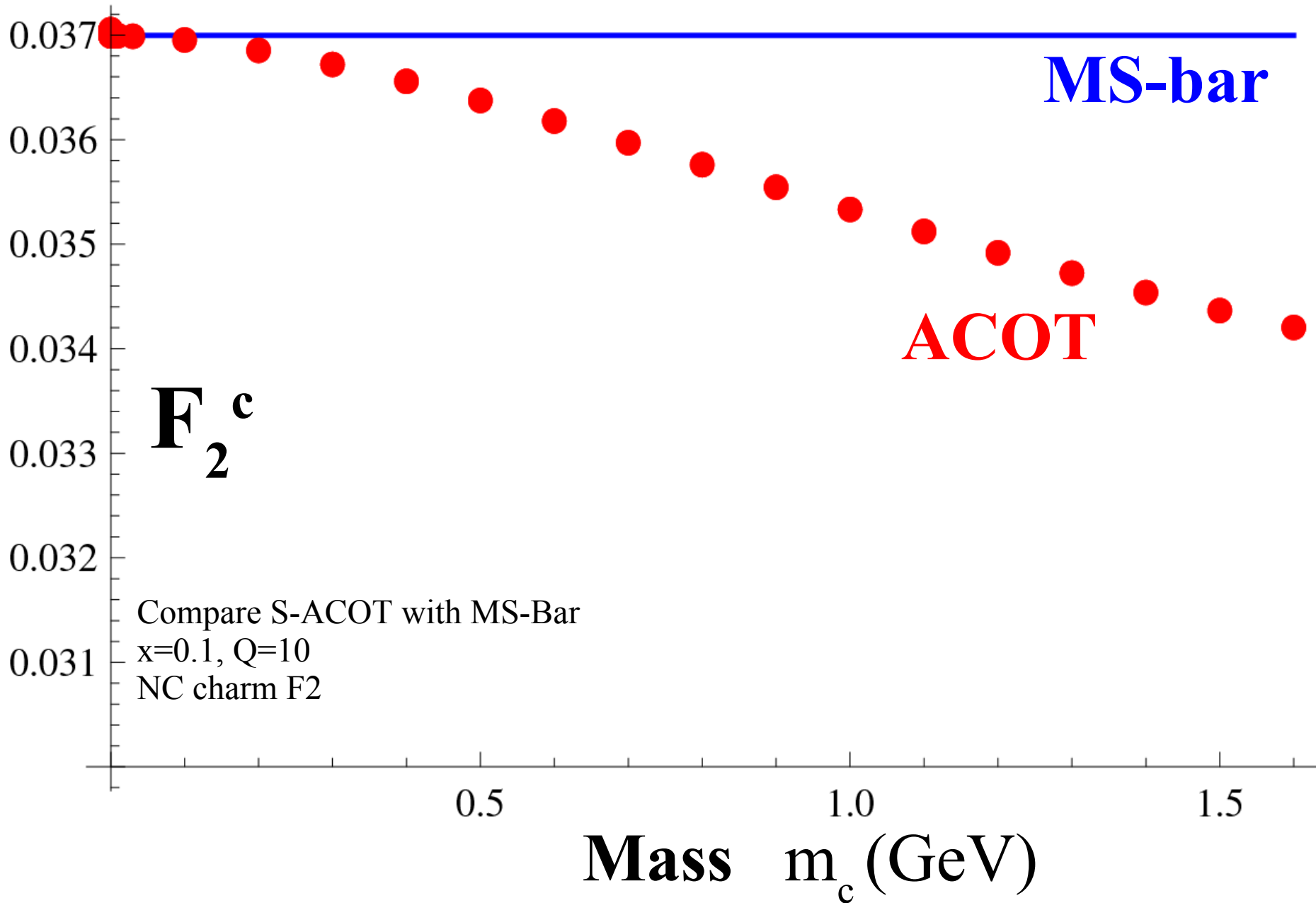
... hence, extensible to all orders

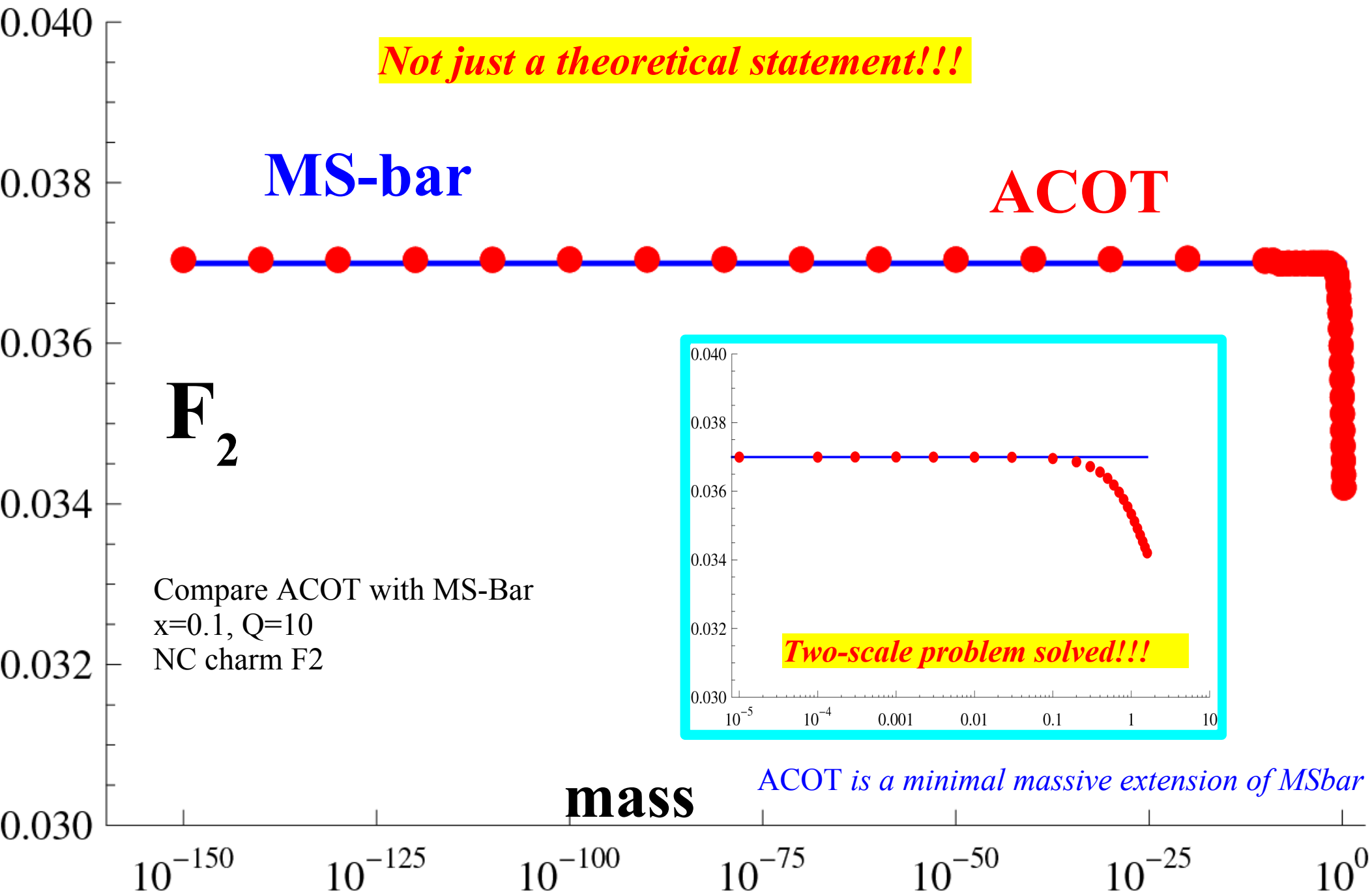
DGLAP kernels & PDF evolution are pure \overline{MS} -Bar

Subtractions are \overline{MS} -Bar

ACOT: $m \rightarrow 0$ limit yields \overline{MS} -Bar

with no finite renormalization





ACOT m→ 0 limit cross check with QCDNUM at NLO

PATCH FOR TESTING: HMASS=0= 0.938000023

IHADRON: SET TO HADRON= 1

GZ and ZZ are for testing

			F_2	F_L
print x,q, ratios:	0.00319999992	12.2474487	1.00092636	1.0012981
print x,q, ratios:	0.00499999989	12.2474487	1.00098575	1.00126809
print x,q, ratios:	0.00800000038	12.2474487	1.00106943	1.00153596
print x,q, ratios:	0.00319999992	14.1421356	1.00092542	1.00125357
print x,q, ratios:	0.00499999989	14.1421356	1.00097202	1.00121532
print x,q, ratios:	0.00800000038	14.1421356	1.00104411	1.00146055
print x,q, ratios:	0.0130000003	14.1421356	1.00107382	1.0013549
print x,q, ratios:	0.0199999996	14.1421356	1.00114663	1.0014694
print x,q, ratios:	0.0320000015	14.1421356	1.00119237	1.00152525
print x,q, ratios:	0.0500000007	14.1421356	1.00117963	1.00131561
print x,q, ratios:	0.0799999982	14.1421356	1.00098036	1.00123239
print x,q, ratios:	0.00499999989	15.8113883	1.00095999	1.00117694
print x,q, ratios:	0.00800000038	15.8113883	1.0010229	1.00140587
print x,q, ratios:	0.0130000003	15.8113883	1.00104124	1.00130353
print x,q, ratios:	0.0199999996	15.8113883	1.00110599	1.00140934
print x,q, ratios:	0.0320000015	15.8113883	1.00114419	1.00146259
print x,q, ratios:	0.0500000007	15.8113883	1.00113621	1.00125726
print x,q, ratios:	0.0799999982	15.8113883	1.00095108	1.0011996
print x,q, ratios:	0.129999995	15.8113883	1.00055001	1.00103563
print x,q, ratios:	0.25	15.8113883	0.99929117	1.0000816
print x,q, ratios:	0.400000006	15.8113883	0.997267345	0.998376607
print x,q, ratios:	0.00499999989	17.3205081	1.00094852	1.00114569
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print x,q, ratios:	0.0130000003	17.3205081	1.00101481	1.00118502
print x,q, ratios:	0.0199999996	17.3205081	1.00107357	1.00136459
print x,q, ratios:	0.0320000015	17.3205081	1.00110601	1.00140262

NLO Check with
QCDNUM

~1E-3

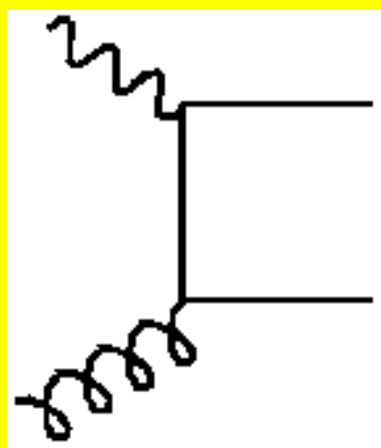
ACOT

Phase Space & Dynamic Mass

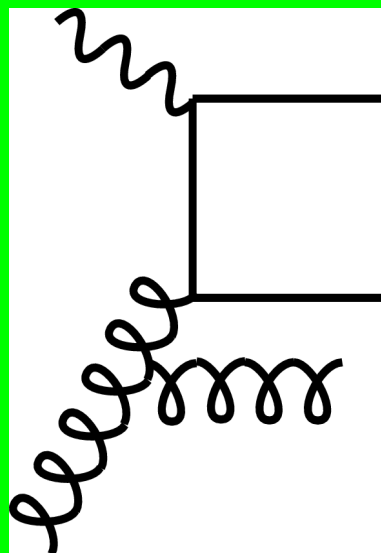
LO



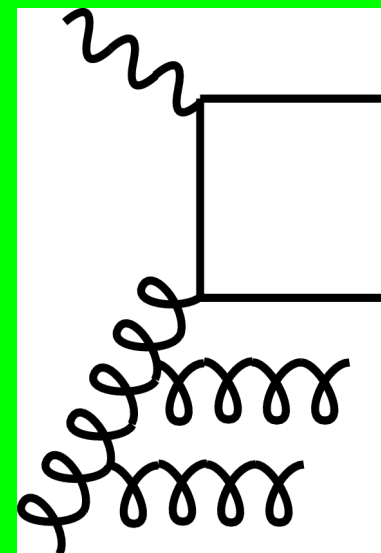
NLO



N2LO



N3LO



Full ACOT

Extensible to any order

$$\sigma = f(\xi(x, m_{ps}), Q) \otimes \hat{\sigma}(m_{dyn})$$

$$\xi(x, m_{ps}) = x \left(1 + \left[\frac{n m_{ps}}{Q} \right]^2 \right)$$

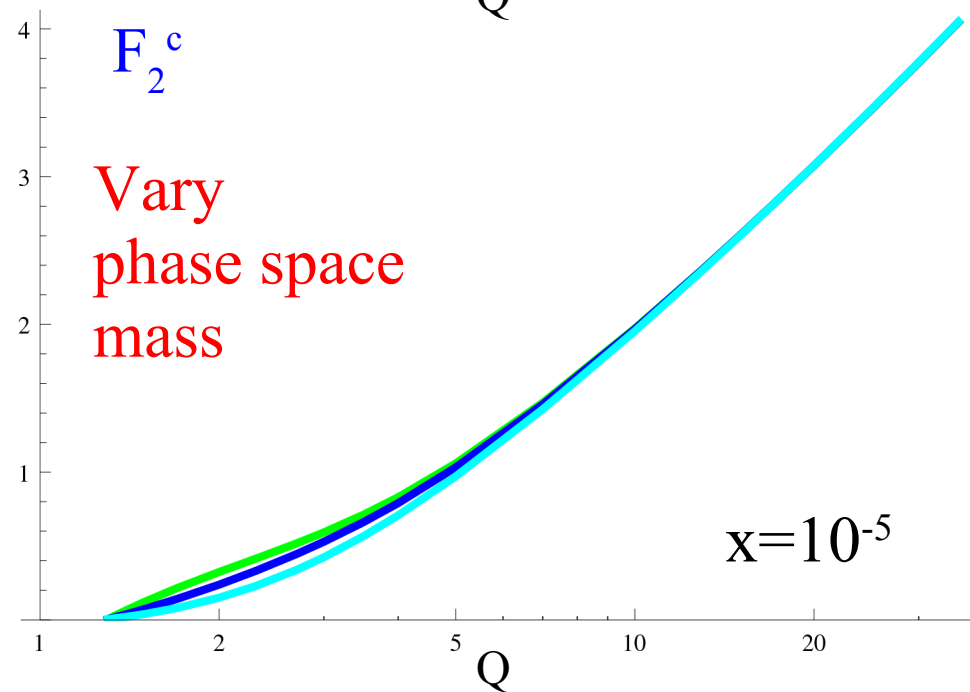
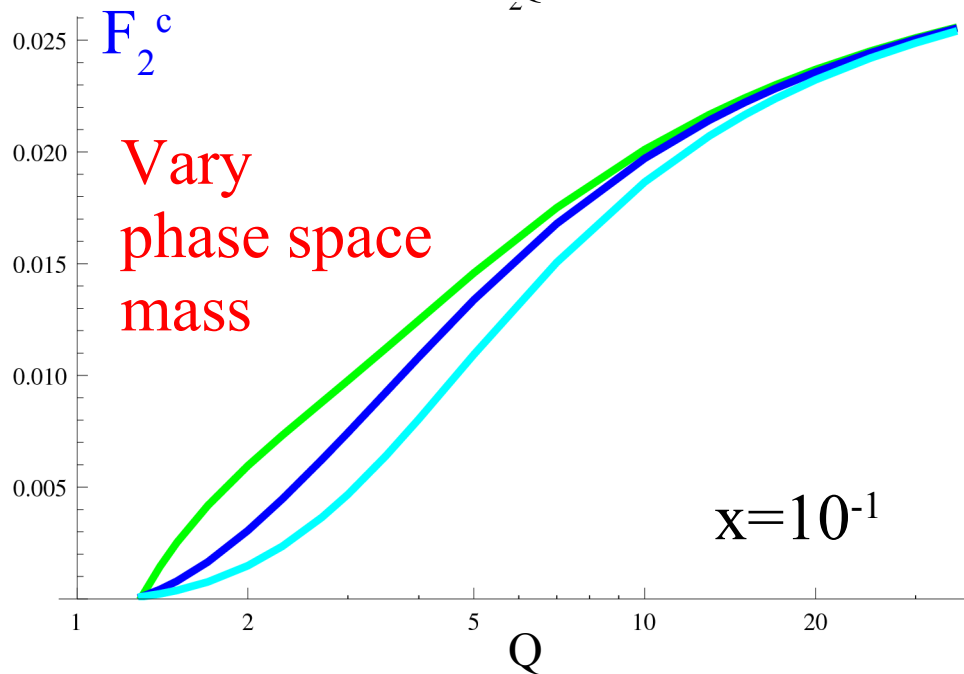
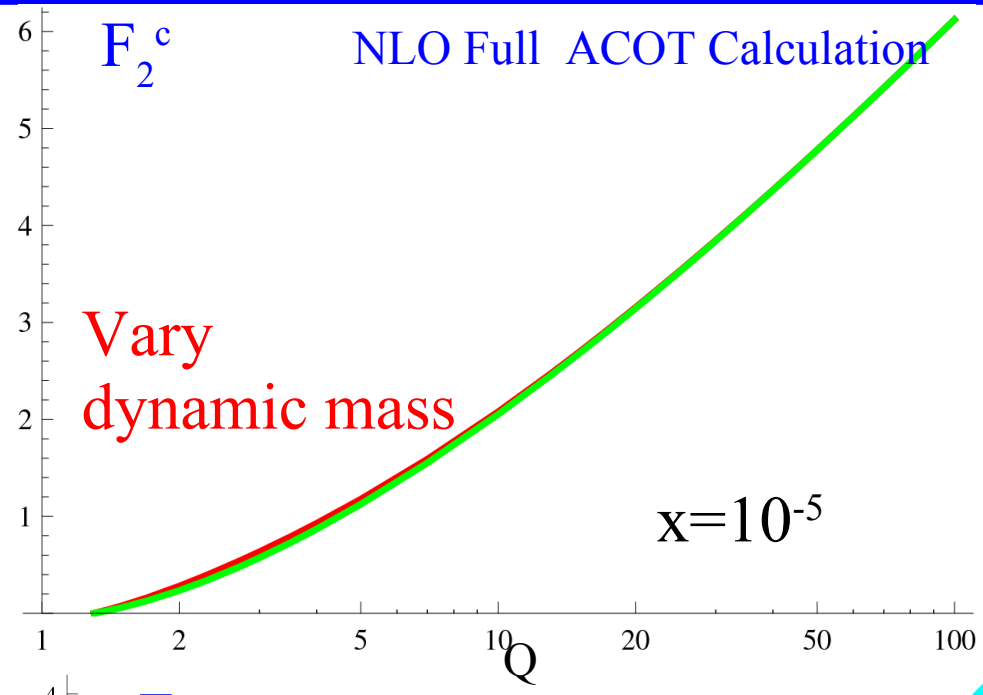
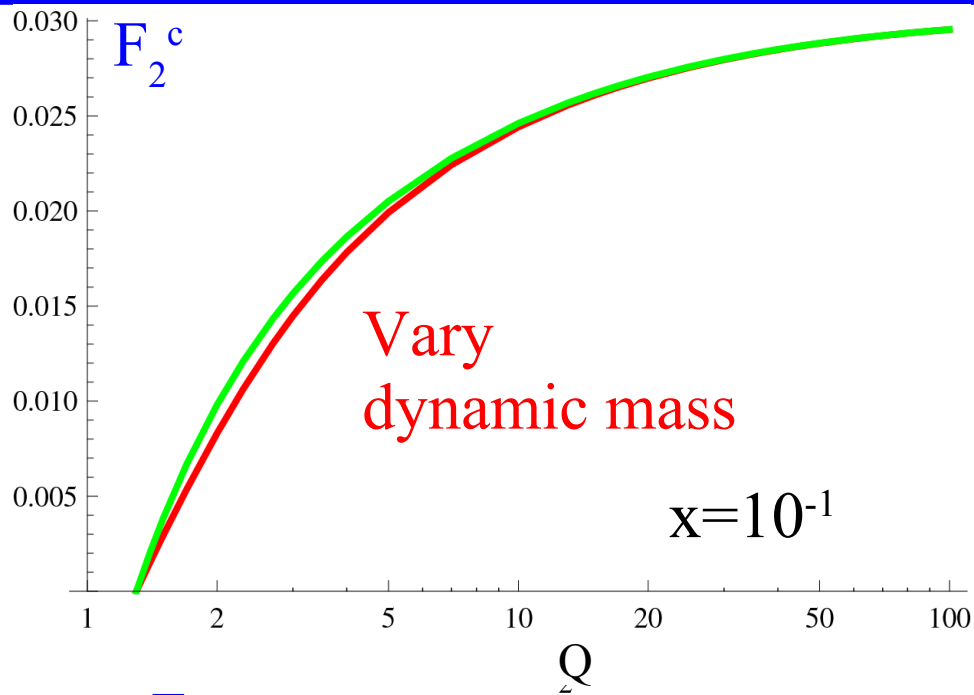
$$n = \{0, 1, 2\}$$

Distinguish:
 “phase space” mass
 “dynamic” mass

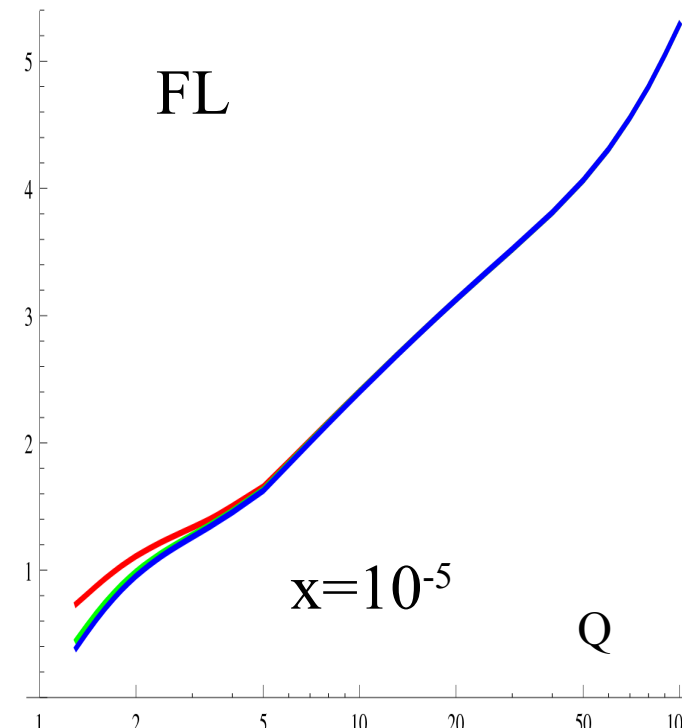
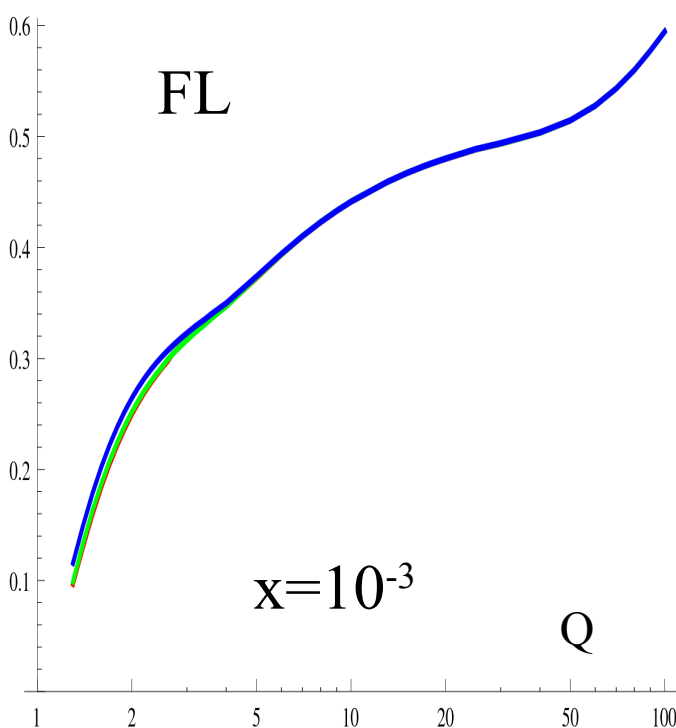
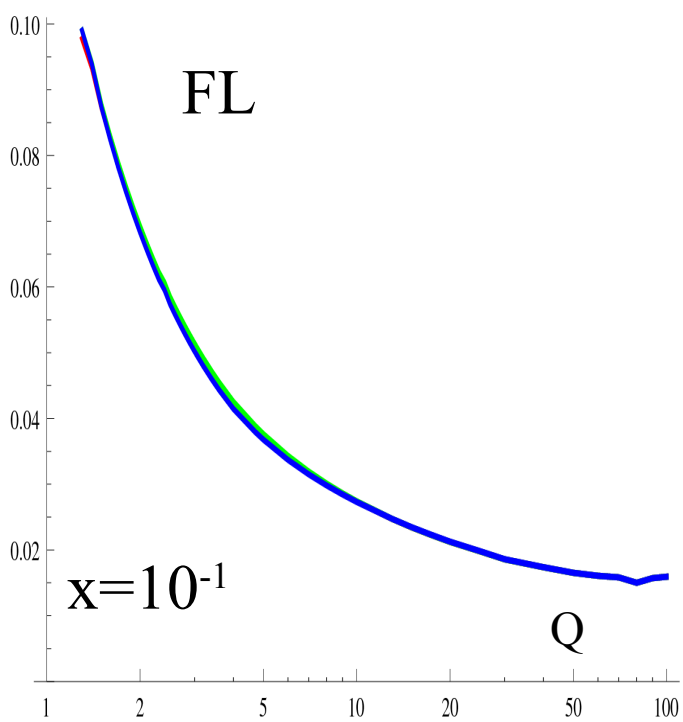
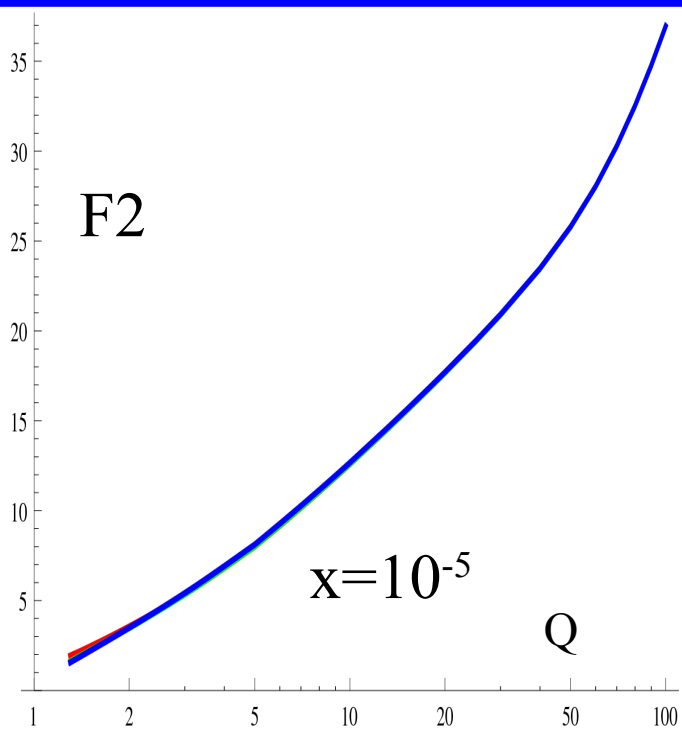
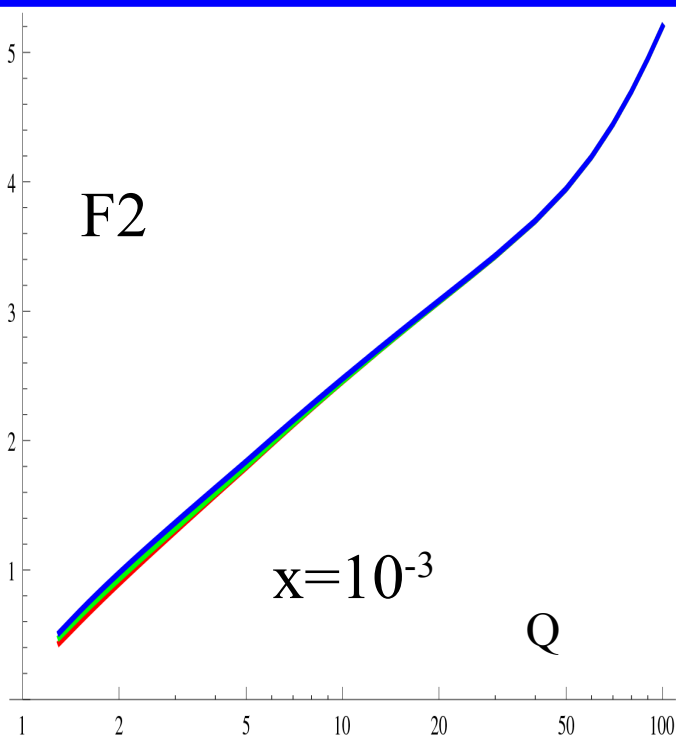
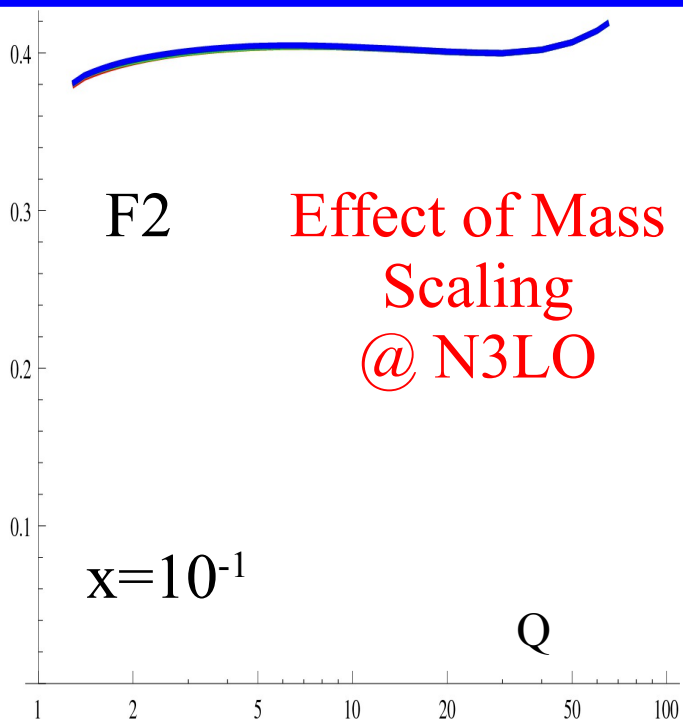
Demonstrate:

- 1) PS mass dominates
- 2) Estimated Error small

Identify Two Types of Mass Dependence: “dynamic” & “phase space” 11



“phase space” mass yields larger variation. Not a proof, but



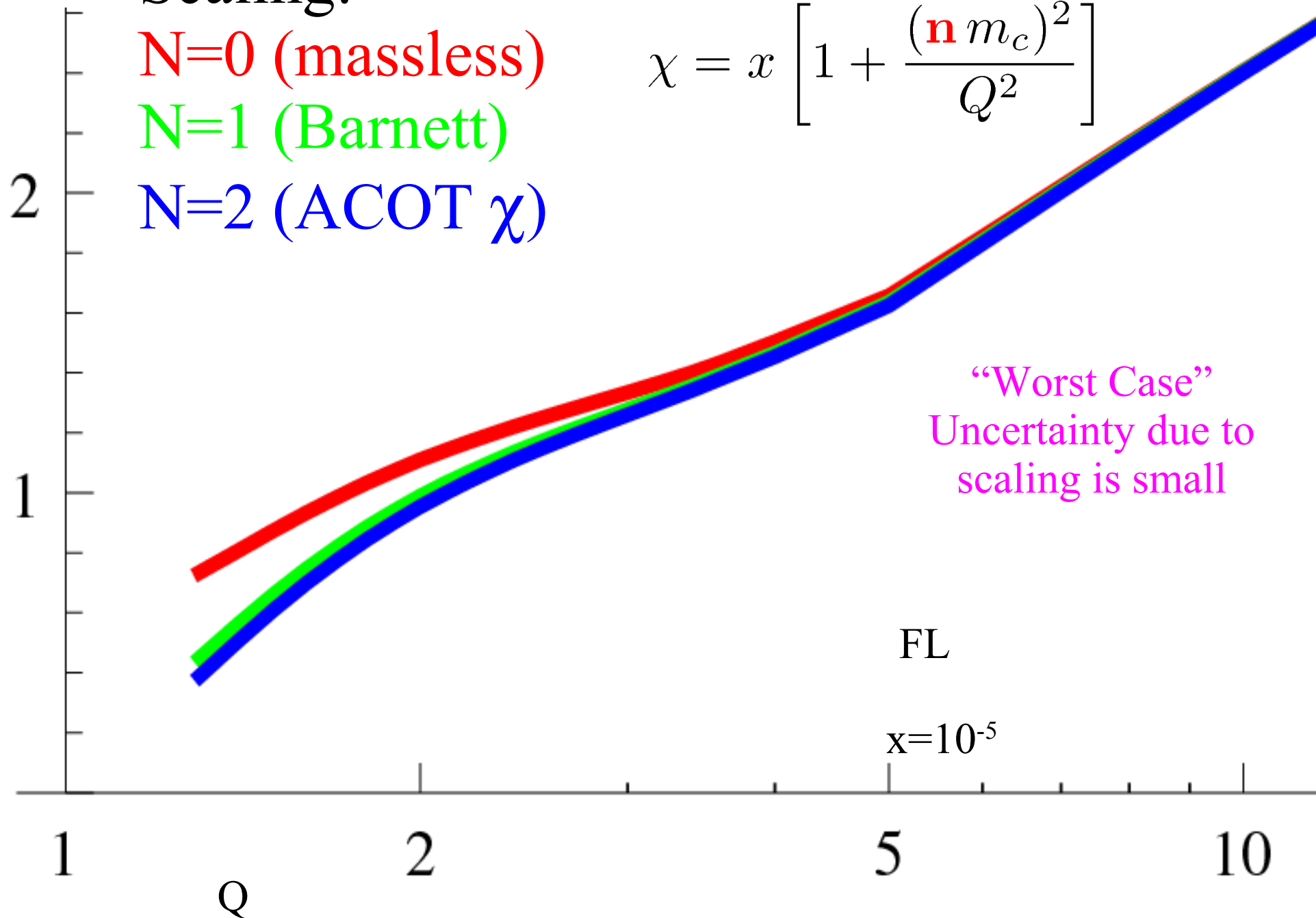
Scaling:

N=0 (massless)

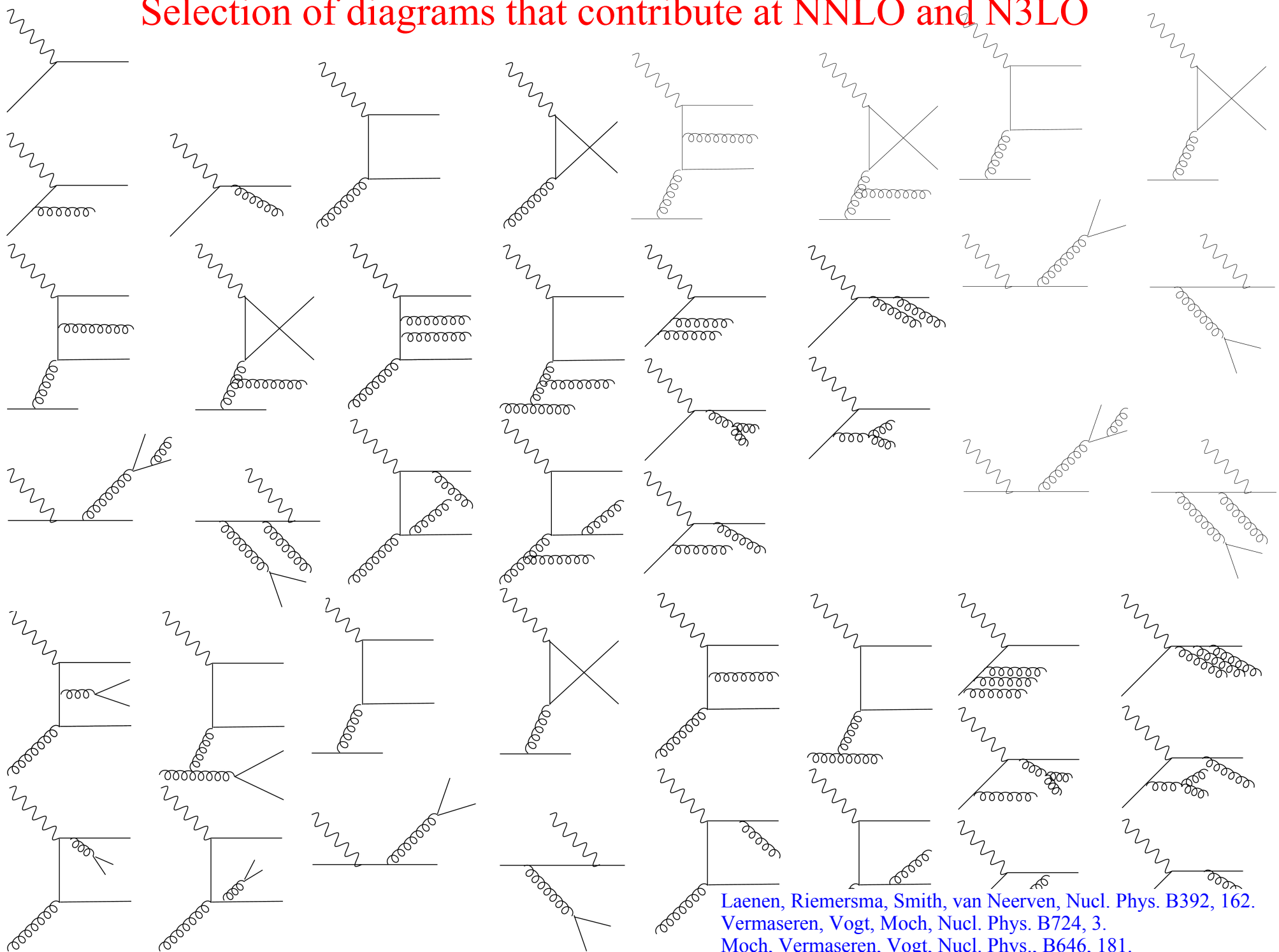
N=1 (Barnett)

N=2 (ACOT χ)

$$\chi = x \left[1 + \frac{(\mathbf{n} m_c)^2}{Q^2} \right]$$



Selection of diagrams that contribute at NNLO and N3LO



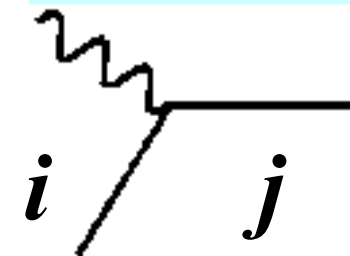
[Laenen, Riemersma, Smith, van Neerven, Nucl. Phys. B392, 162.](#)
[Vermaseren, Vogt, Moch, Nucl. Phys. B724, 3.](#)
[Moch, Vermaseren, Vogt, Nucl. Phys., B646, 181.](#)
[Moch, Vermaseren, Vogt, Phys. Lett., B606, 123.](#)
[Blumlein, Hasselhuhn, Kovacikova, Moch, Phys.Lett. B700, \(2011\) 294.](#)

Master formula for decomposing the flavor components

T.P. Stavreva, I Schienbein

$$F = \sum_{i,j}^6 F^{ij}$$

**The Goal: Convert from
{s, ns, ps} to {q,g, ...}**



$$x^{-1} F_a^{ij} = q_i^+ \otimes \left\{ e_i^2 \left[C_{a,q}^{\text{ns}}(n_f = 0) \delta_{ij} \right. \right.$$

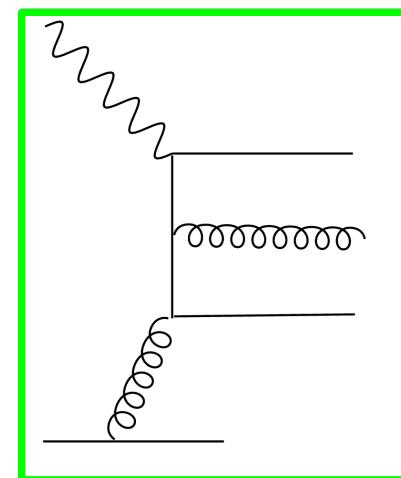
$$\left. + C_{a,q}^{\text{ns}}(j) - C_{a,q}^{\text{ns}}(j-1) \right]$$

$$\left. - \langle e^2 \rangle^{(j)} C_{a,q}^{\text{ps}}(j) - \langle e^2 \rangle^{(j-1)} C_{a,q}^{\text{ps}}(j-1) \right\}$$

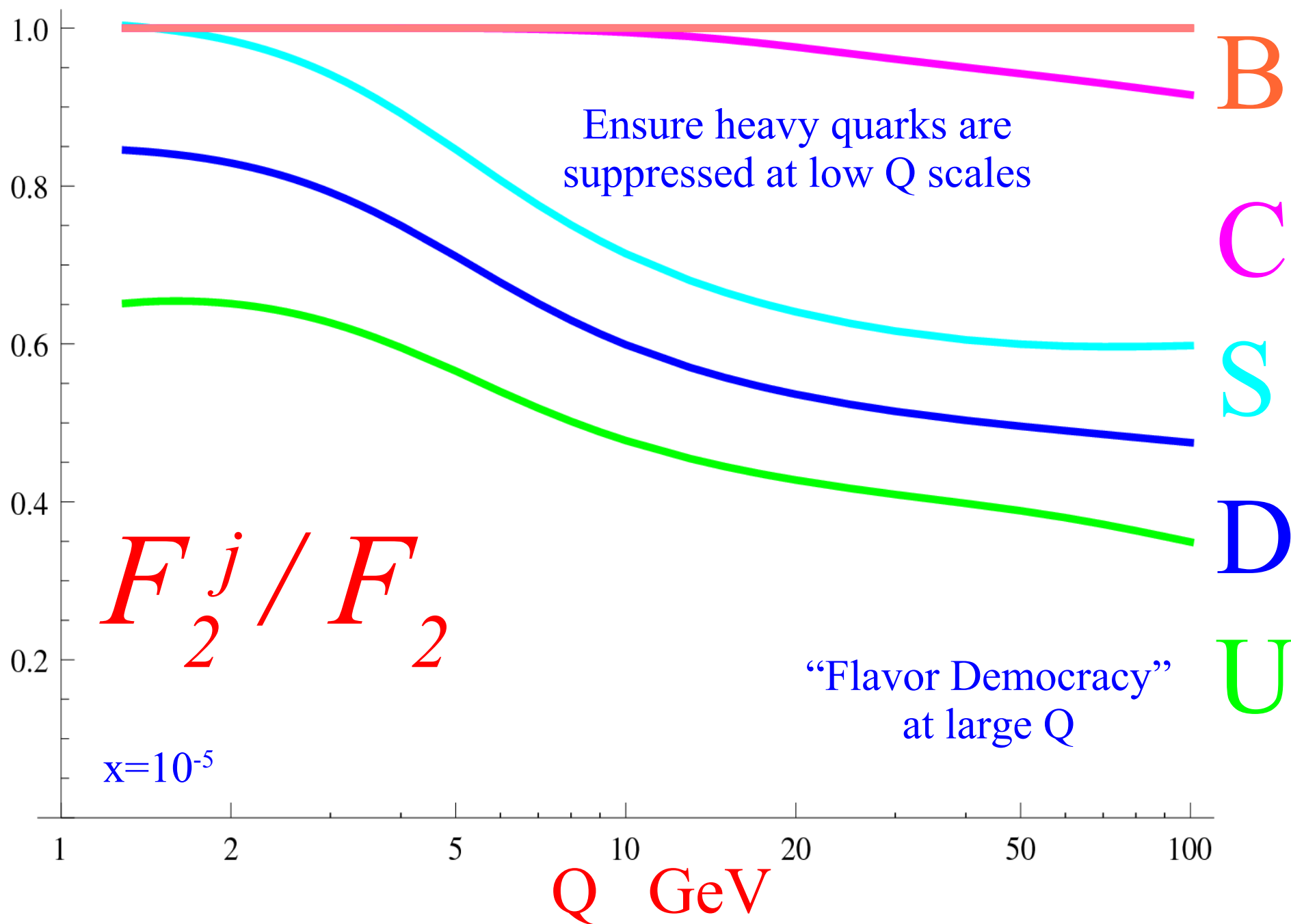
Issues: Flavor separation:

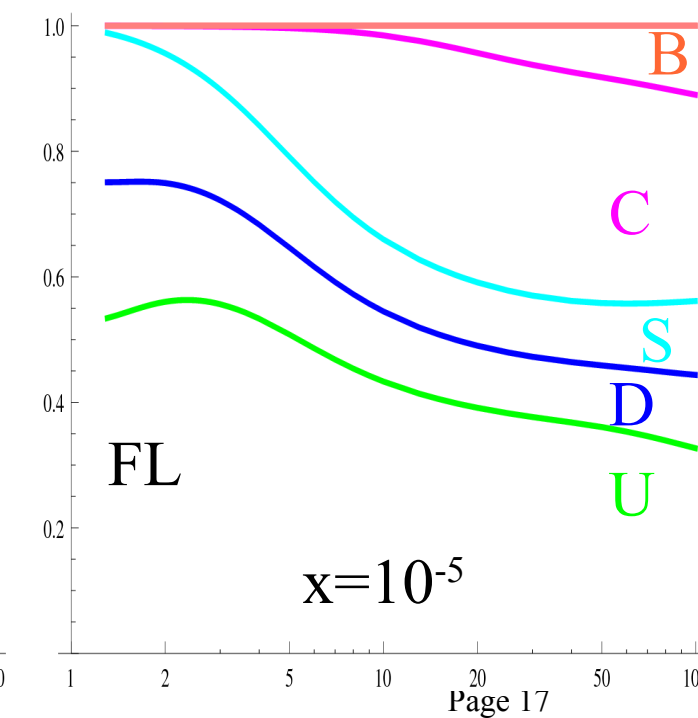
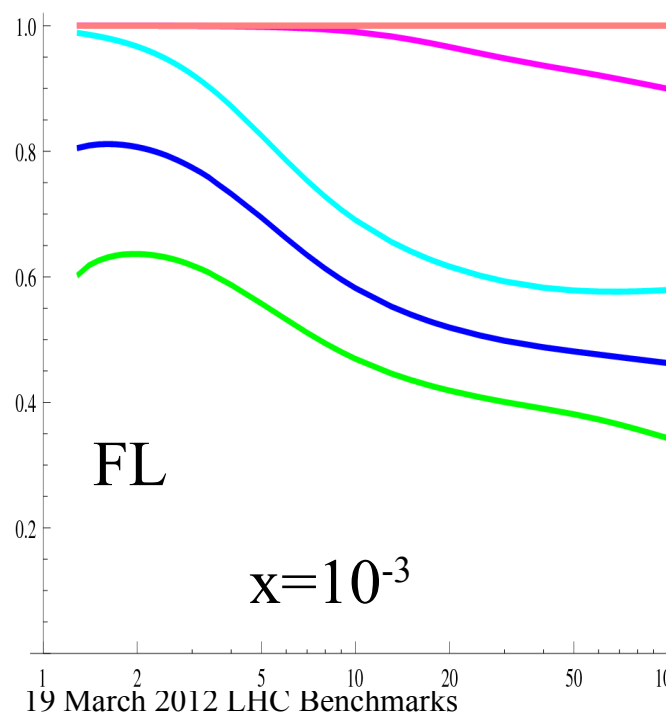
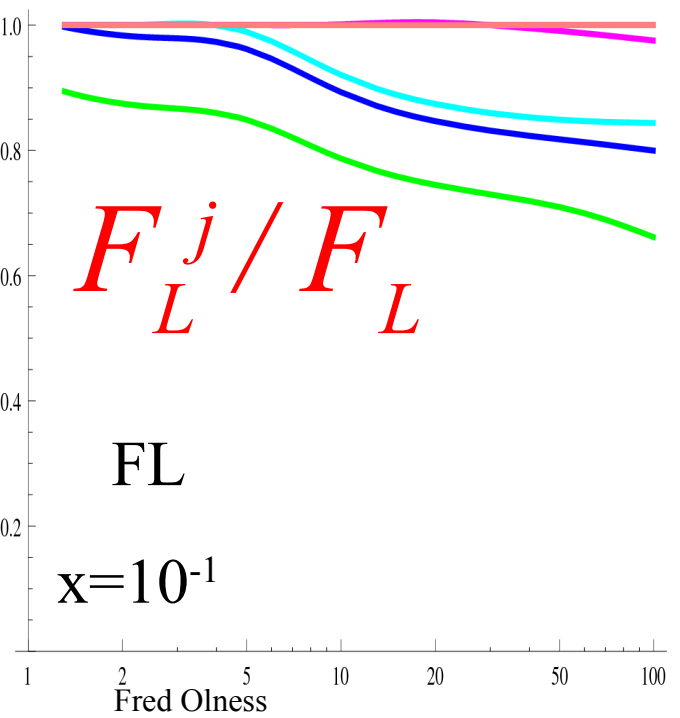
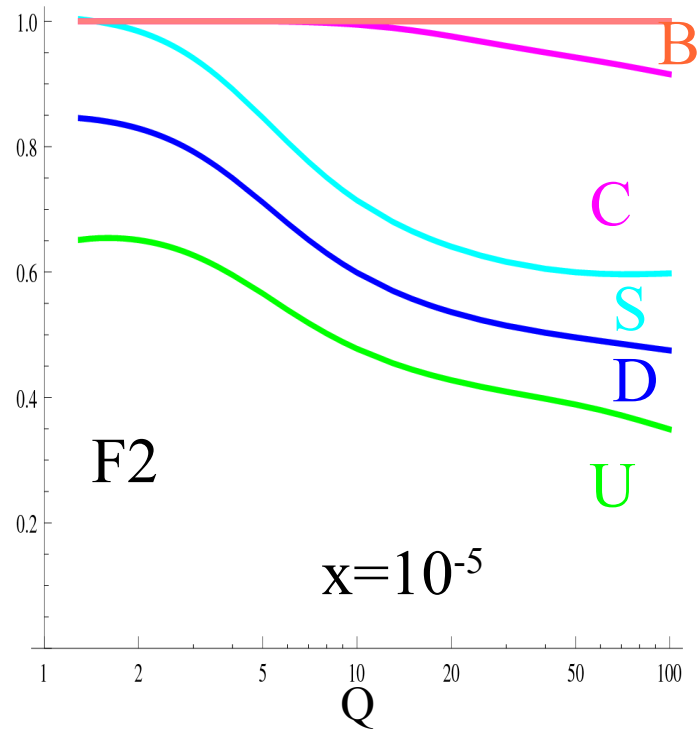
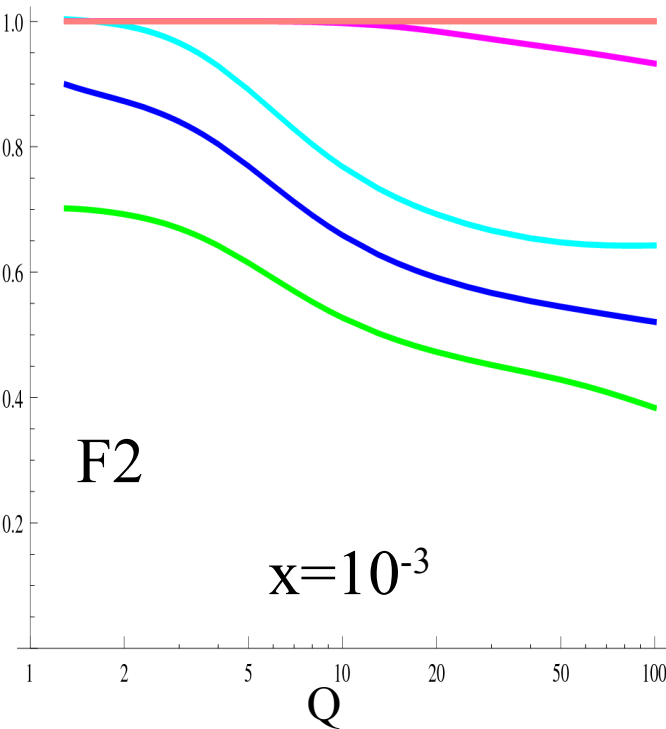
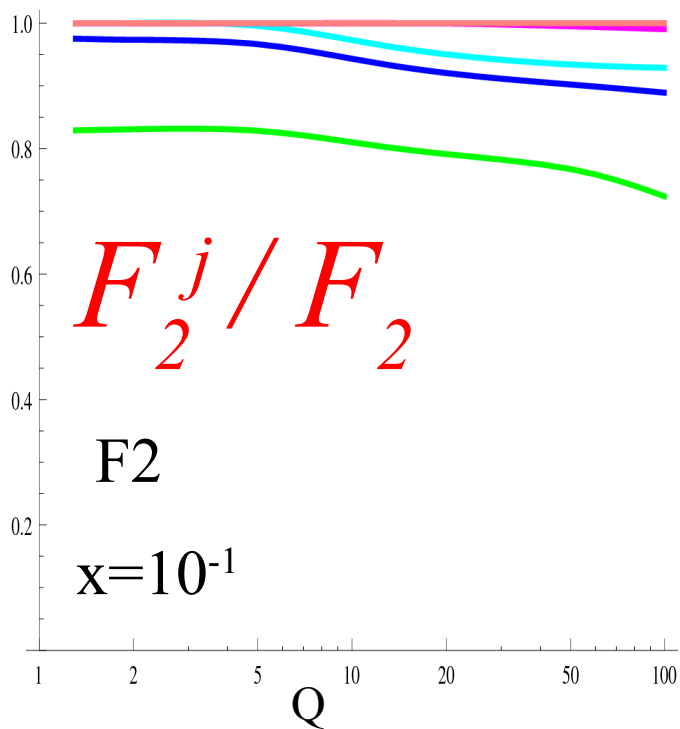
New diagrams at this order

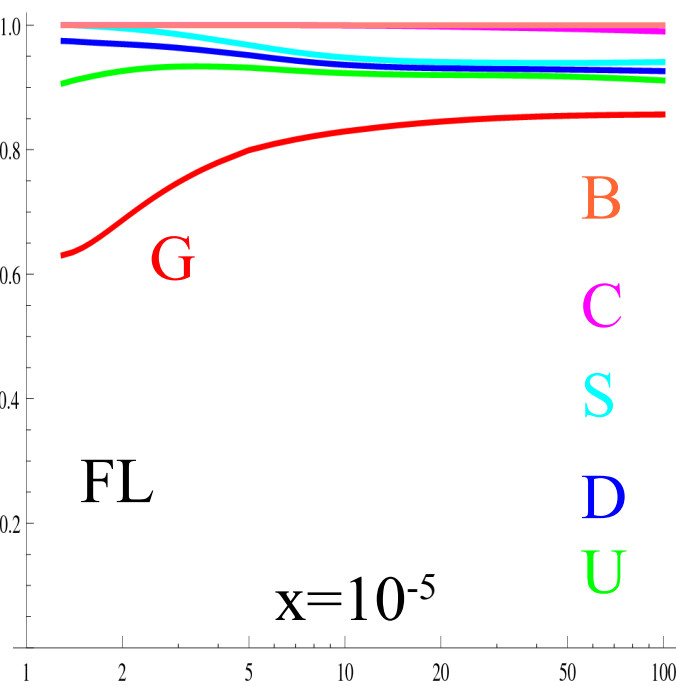
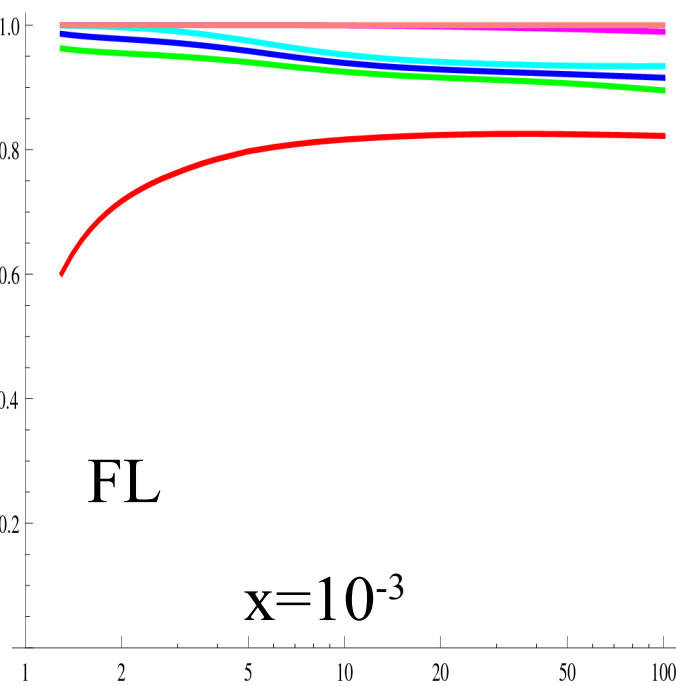
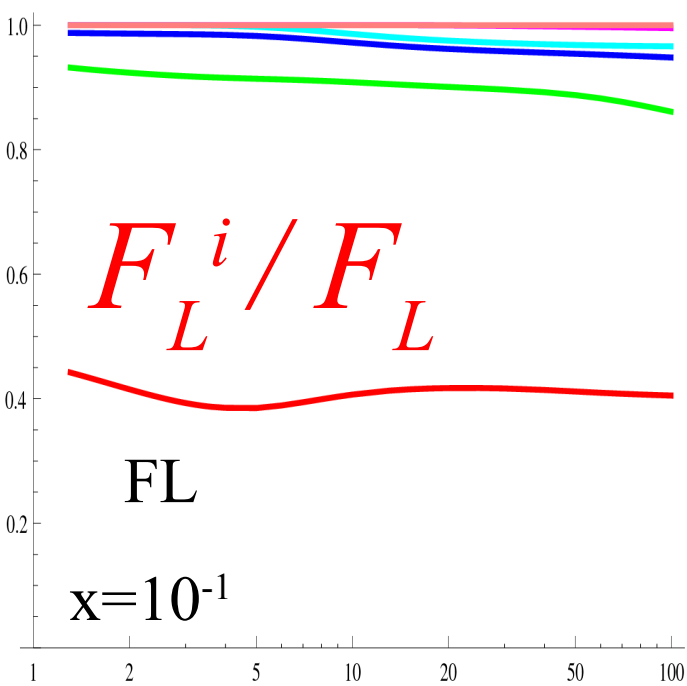
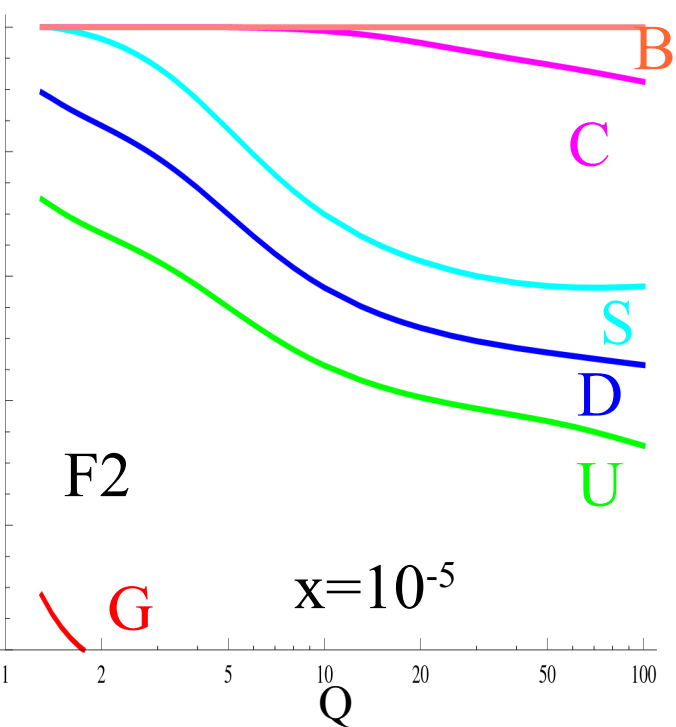
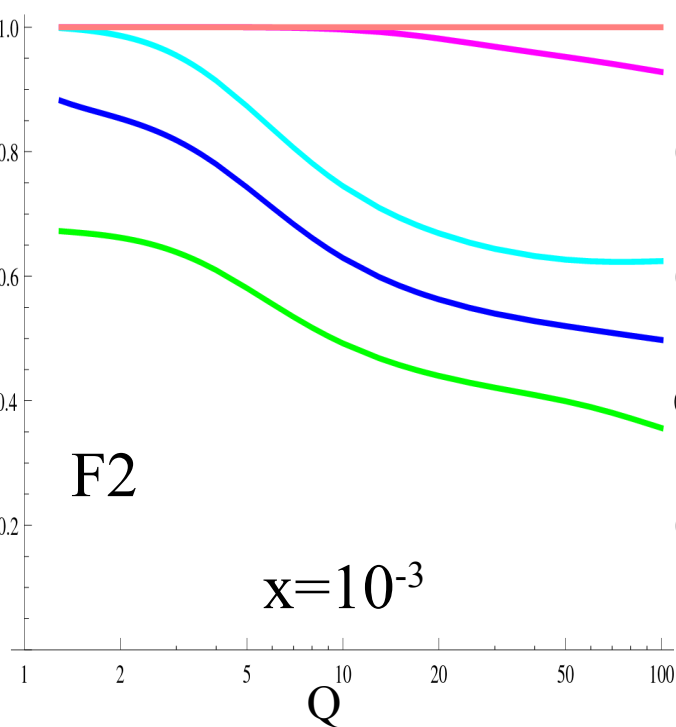
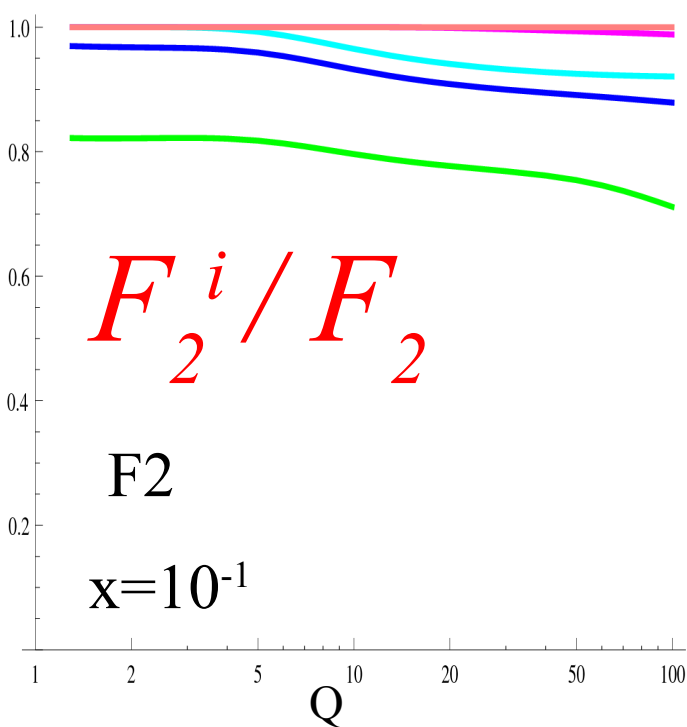
- c,b, goes down beam pipe
- both c & b in final state



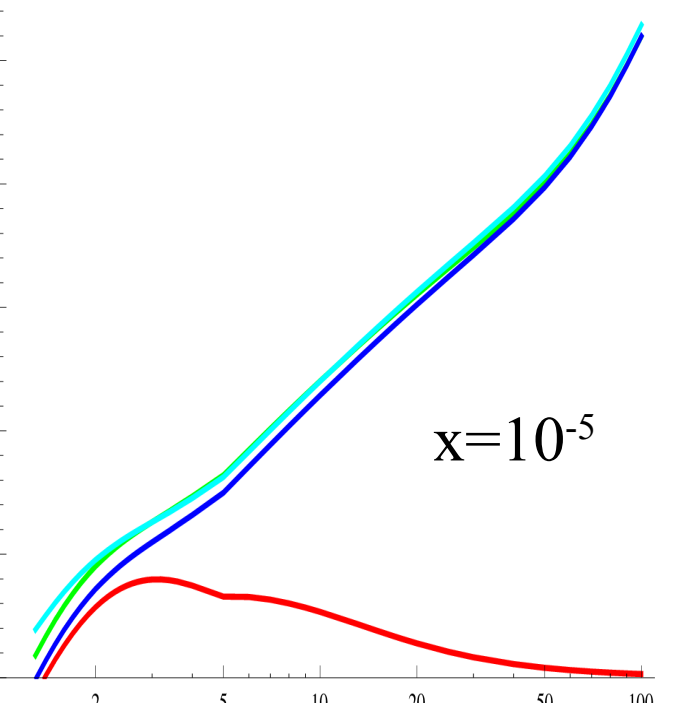
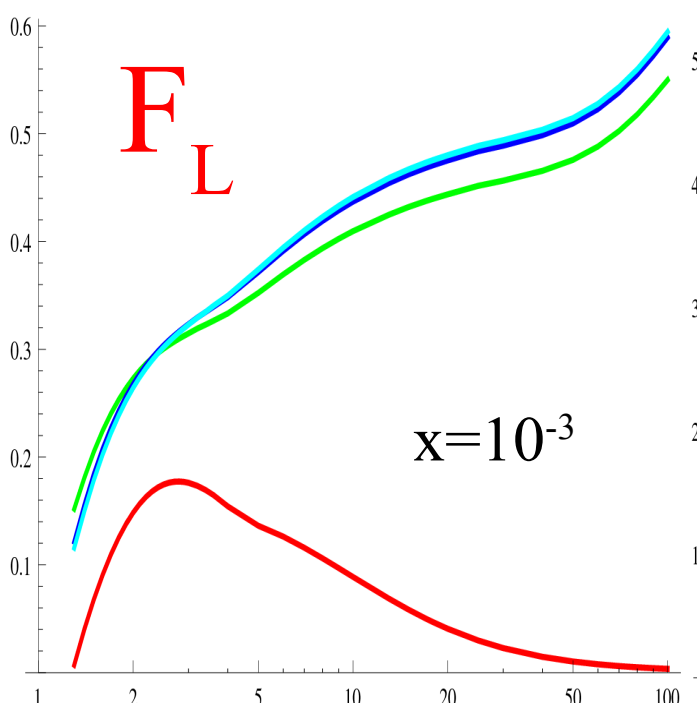
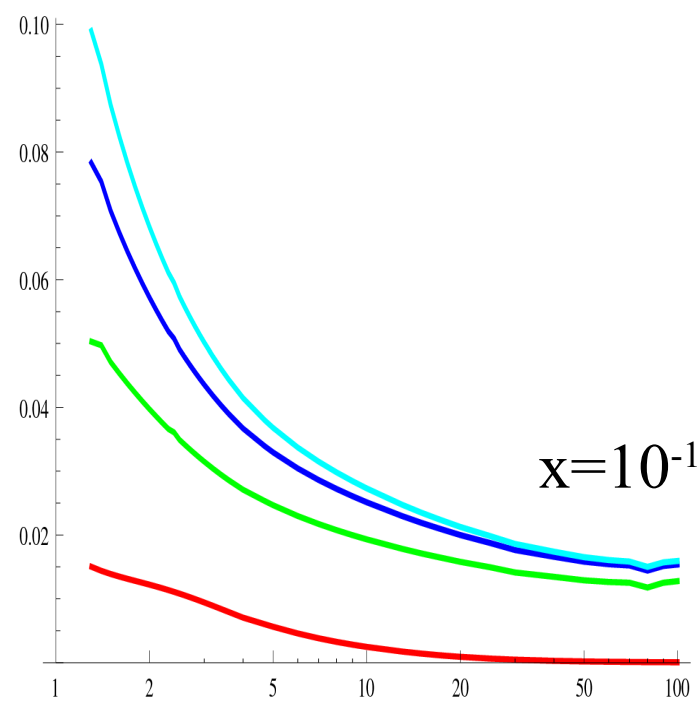
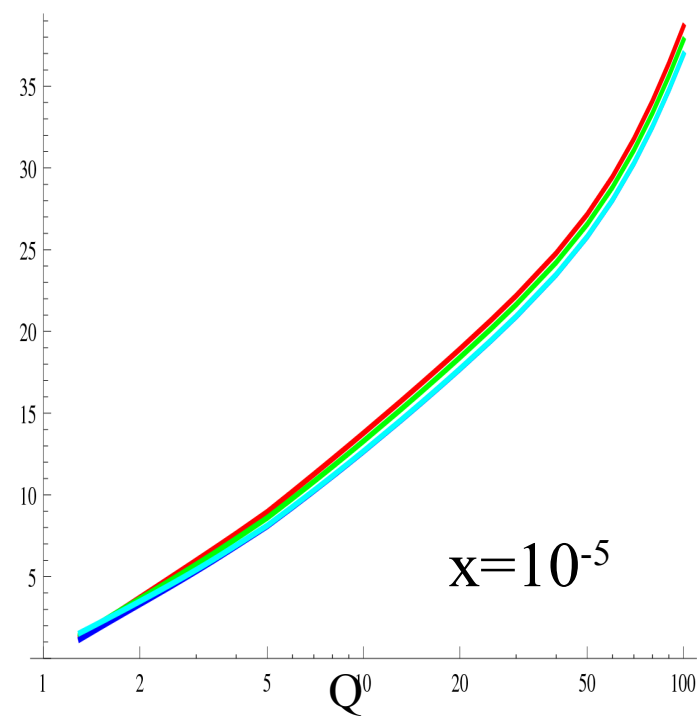
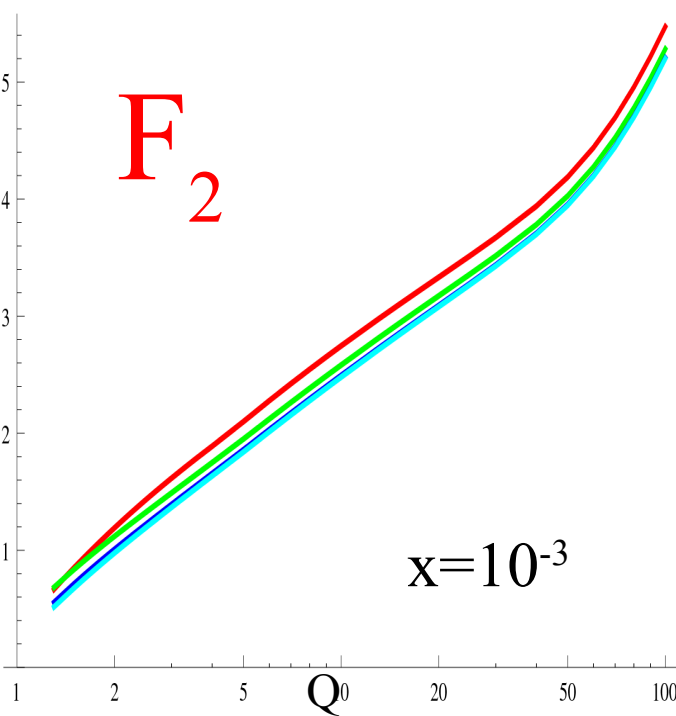
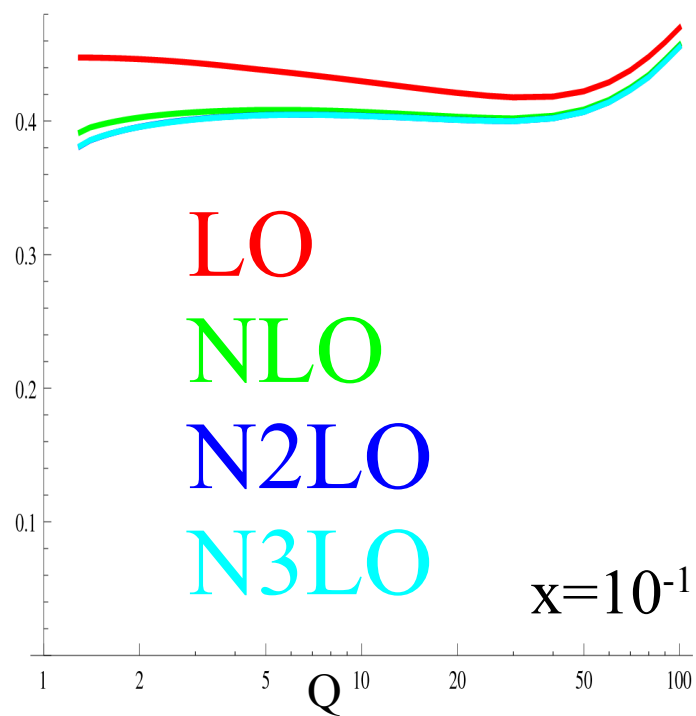
FLAVOR DECOMPOSITION







$F_{2,L}$ @ N3LO



A Complementary Approach

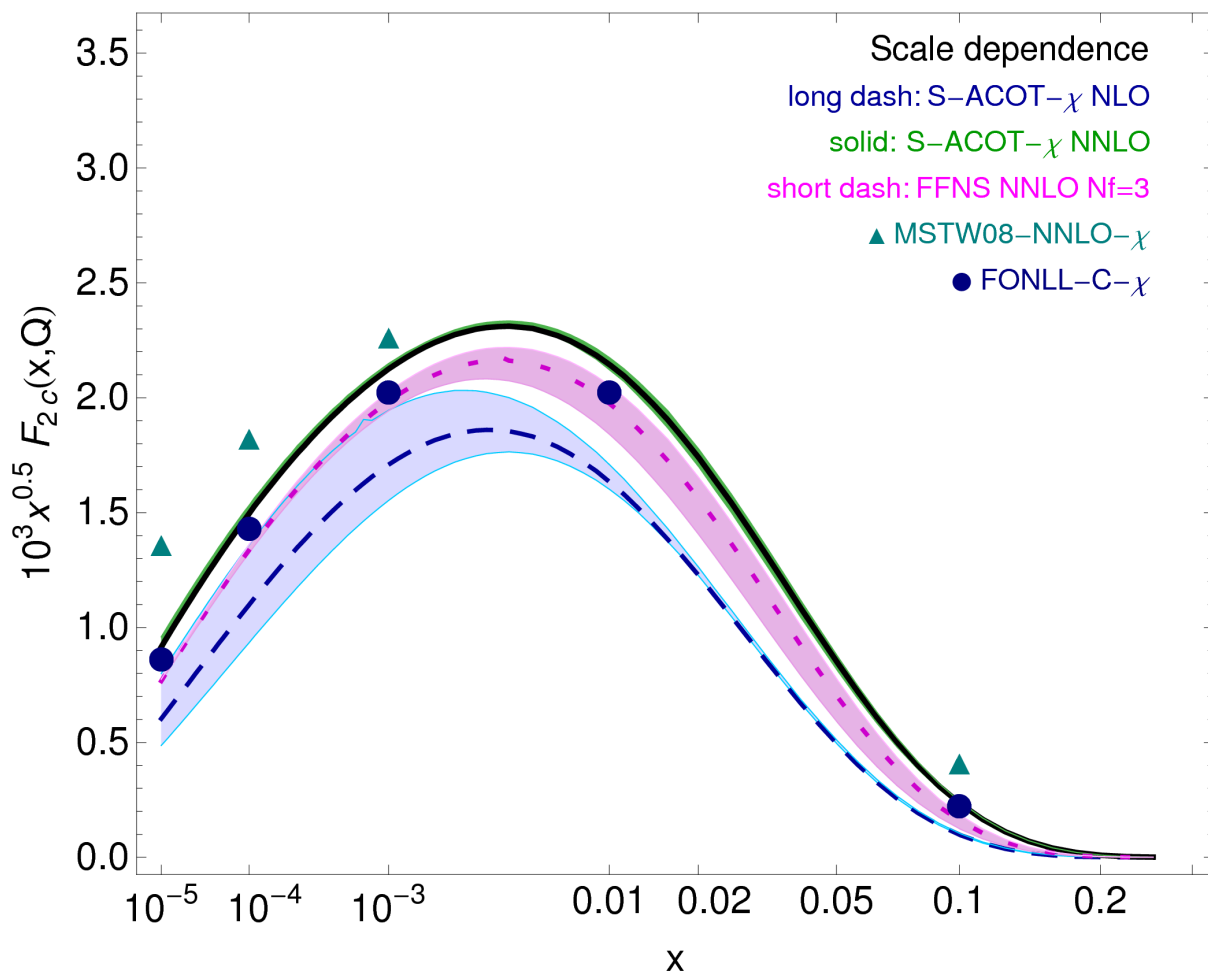
S-ACOT χ

at NNLO

led by Marco Guzzi and Pavel Nadolsky

Drastic μ_F -scale reduction in $F_2^c(x, Q^2)$ at NNLO

LH PDFs $Q=2$ GeV, $m_c=1.41$ GeV

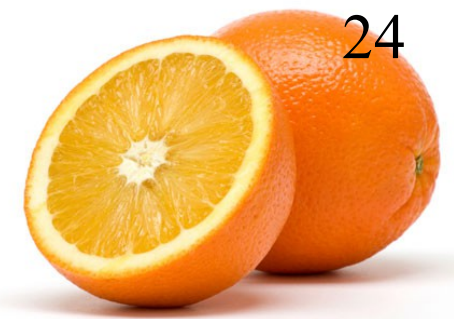


S-ACOT χ
for Neutral Currents
based on Smith vanNeerven

key step for NNLO PDFs
(see Pavel's talk)

By using S-ACOT- χ we obtain a drastic reduction of the theoretical errors compared to the NLO computation.

Comparison



Les Houches Comparative Studies

Excellent progress in addressing how to compute heavy quarks

The Cast:

ACOT & S-ACOT Codes
Used in CTEQ4HQ, 5HQ, 6HQ

Aivazis, Collins, Olness, Tung,
Phys.Rev.D50:3102-3118,1994.

S-ACOT
CTEQ 6.5 & 6.6

Tung, Lai, Belyaev, Pumplin, Stump, Yuan,
JHEP 0702:053,2007.
Nadolsky, Tung, Phys.Rev.D79:113014,2009.

Thorne-Roberts (TR')
MSTW Fits

Thorne, Phys.Rev.D73:054019,2006.

FONLL:
Used in NNPDF Fits

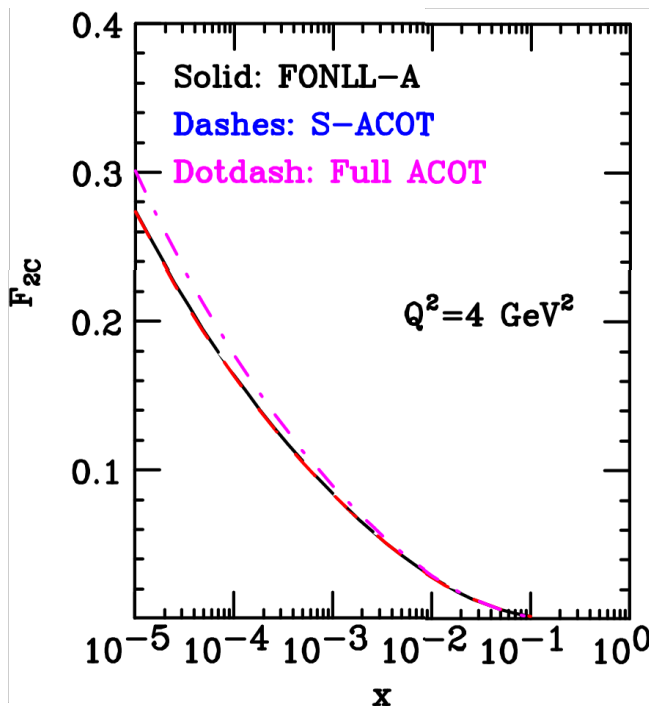
Forte, Laenen, Nason, Rojo,
Nucl.Phys.B834:116-162,2010.

ABKM:

Blumlein, Klein, Moch
Phys.Rev.D81:014032,2010

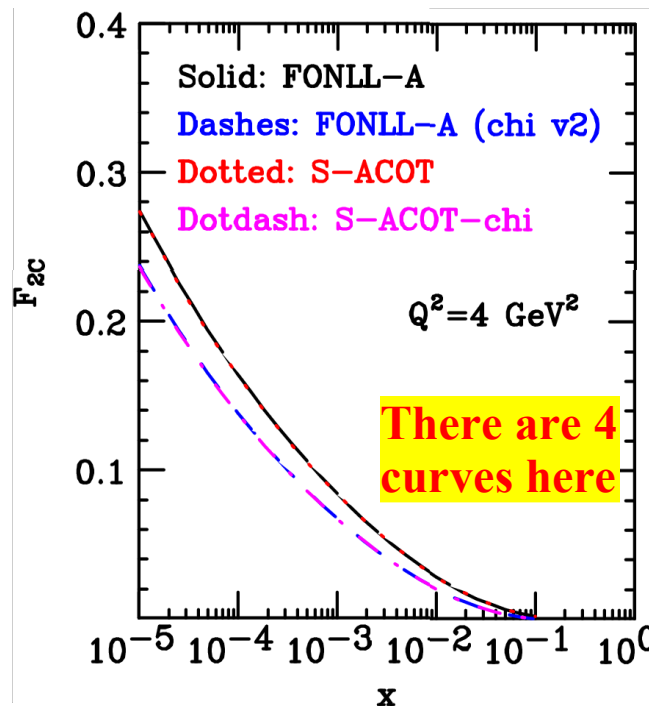
Work is continuing

**Many of the above incorporated
in HERA-Fitter**



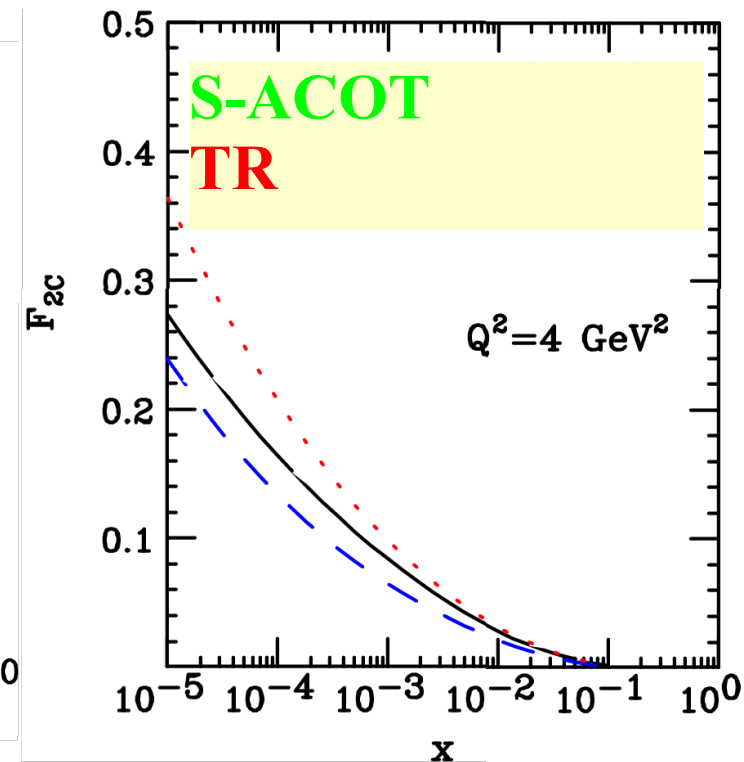
ACOT & S-ACOT
essentially identical

... scheme
differences are
higher order



FONNL & S-ACOT

Numerically similar



MSTW09

We can quantify
theoretical scheme
differences

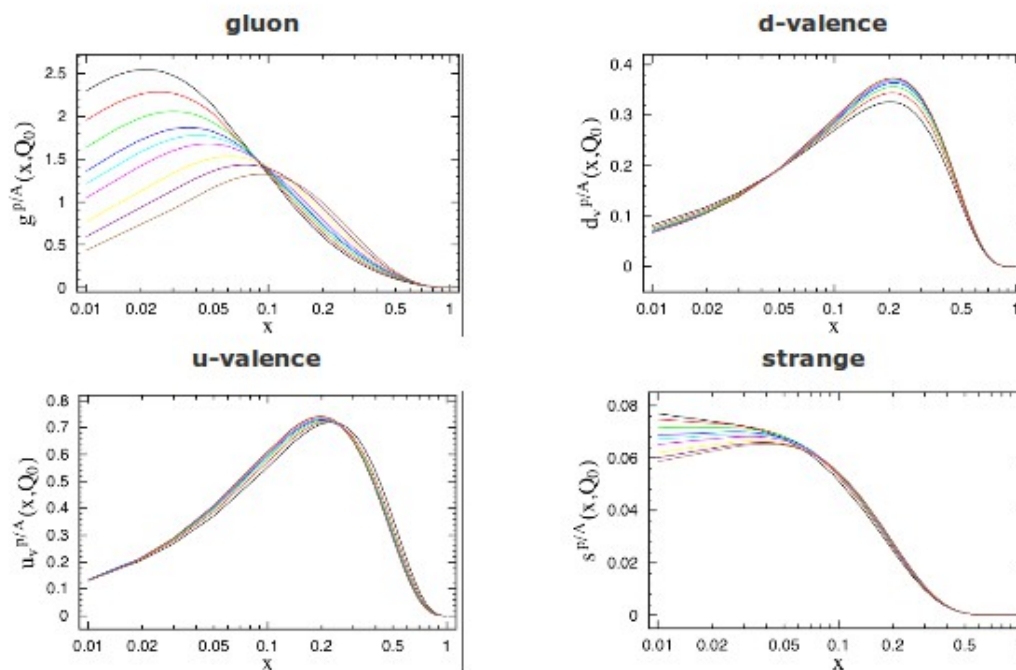
nCTEQ

nuclear parton distribution functions

- Home
- PDF grids & code
- Papers & Talks
- Subversion
- Tracker
- Wiki

nCTEQ project is an extension of the CTEQ collaborative effort to determine parton distribution functions inside of a free proton. It generalizes the free-proton PDF framework to determine densities of partons in bound protons (hence nCTEQ which stands for nuclear CTEQ). More details on the framework and the first results can be found in [arXiv:09072357 \[hep-ph\]](https://arxiv.org/abs/09072357).

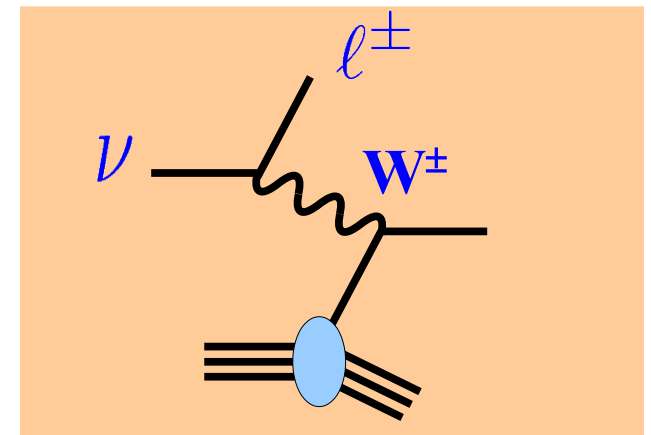
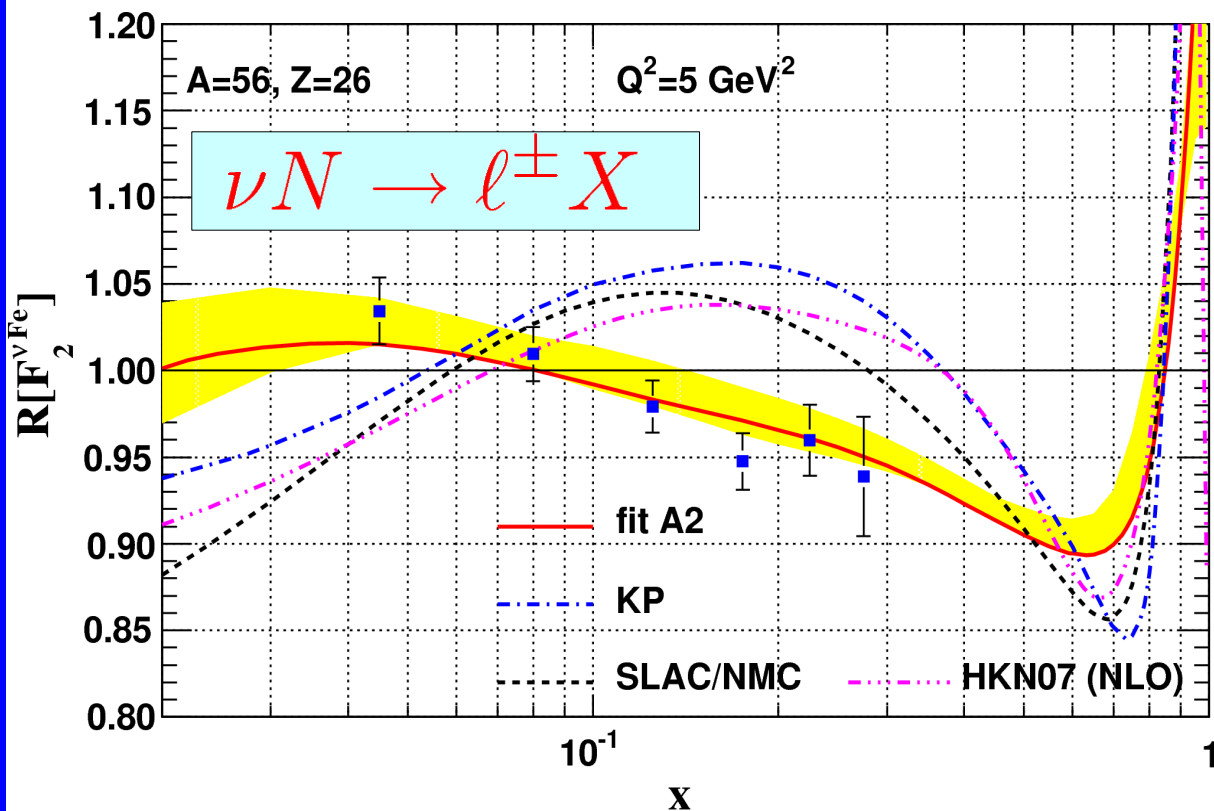
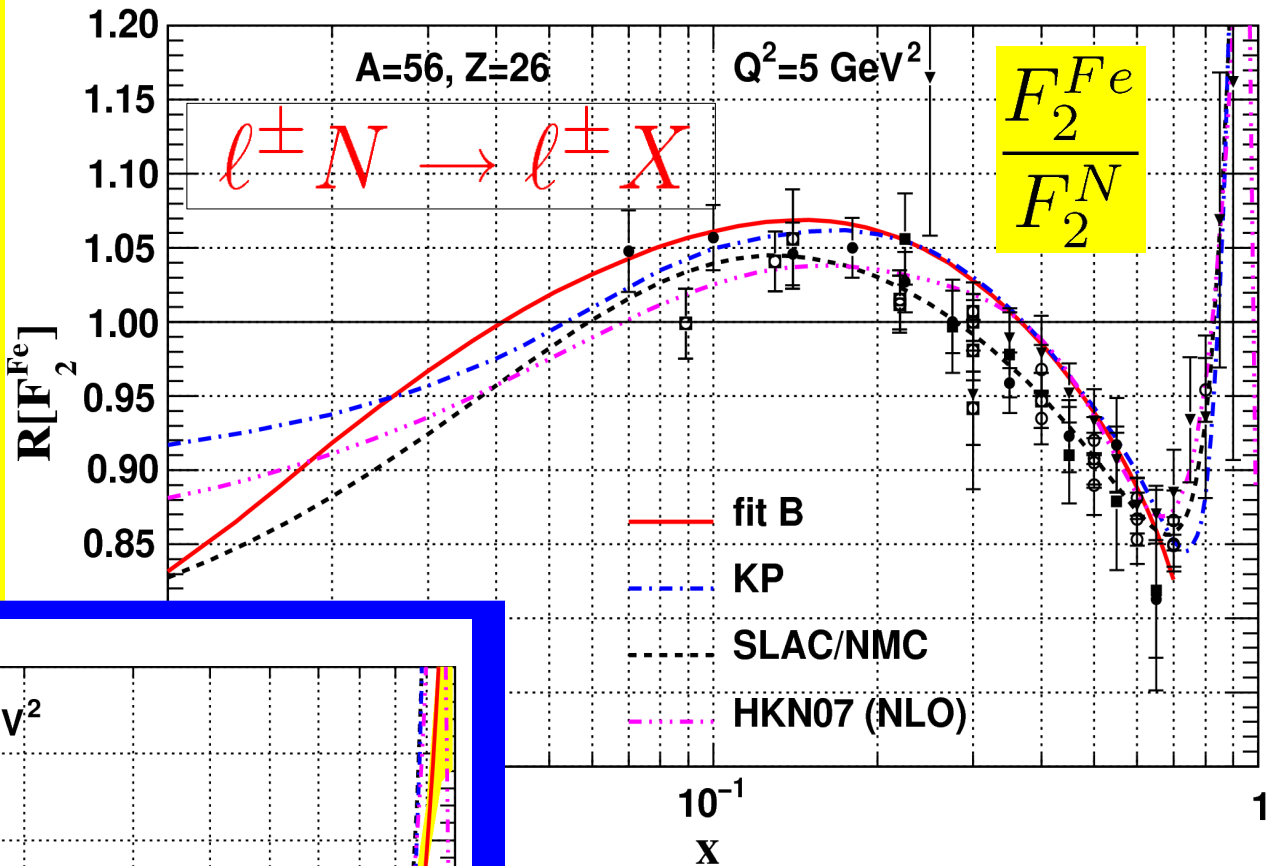
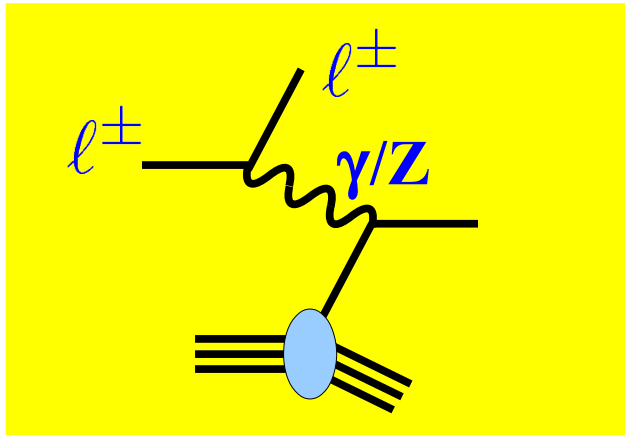
The effects of the nuclear environment on the parton densities can be shown as modified parton densities



where all black curves stand for free proton PDF and red, green, blue, cyan, pink, yellow, magenta and brown curves show PDF in protons bound in nuclei - from deuterium (red) to lead (brown).

K Kovarik,
I. Schienbein,
J.Y. Yu,
T. Stavreva,
T Jezo,
C. Keppel,
J.G. Morfin,
F. Olness,
J.F. Owens.

Charged Lepton DIS \Rightarrow



\Leftarrow Neutrino DIS

Conclusion

This technique provides an NNLO & N3LO extension of ACOT

“Phase space” mass is included via rescaling
Dominant effect for LO & NLO

F2: Stable.
LO and NLO have full m -dependence
N2LO and N3LO very similar

FL: More complex as NLO corrections are large (Callan-Gross)
N2LO and N3LO terms converge

Heavy quark terms vanish for low Q ;
this moderates mass effects

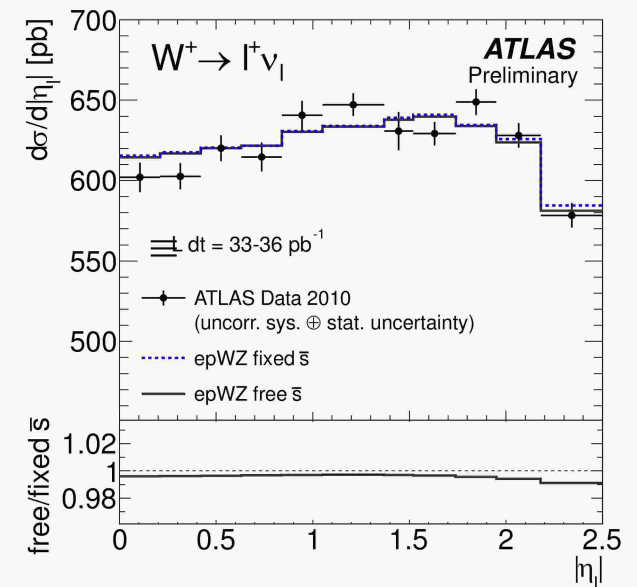
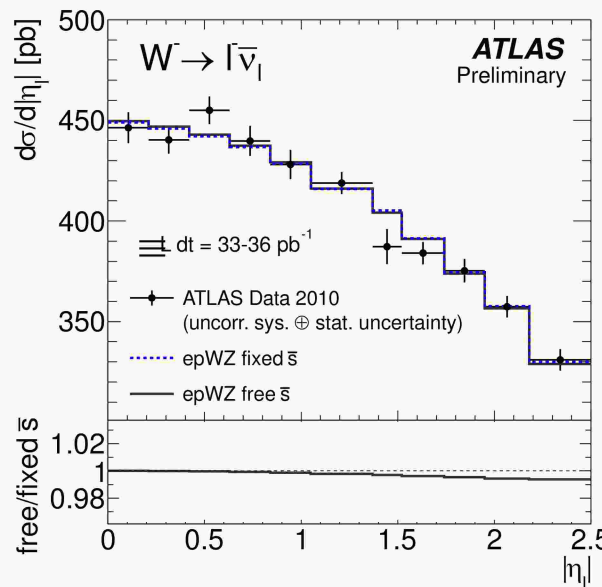
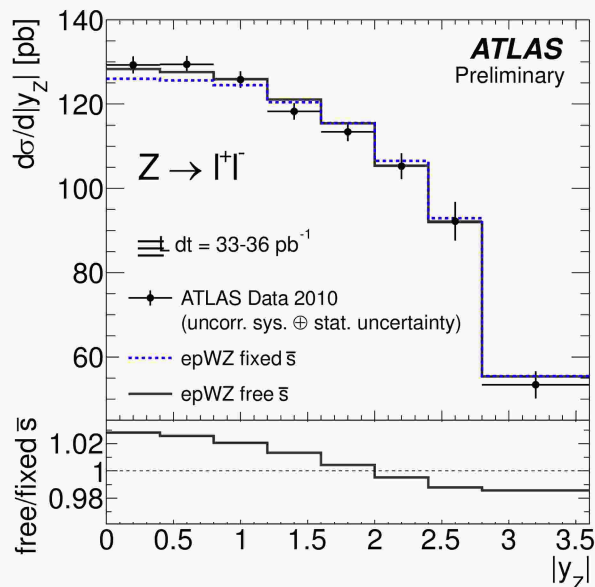
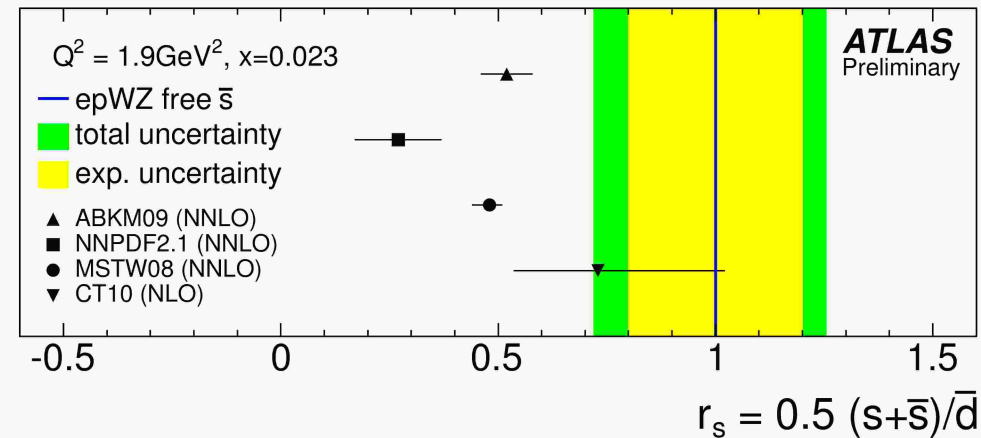
Thanks to: K. Kovarik, A. Kusina, T.P. Stavreva I Schienbein, J.-Y. Yu,
P. Nadolsky, M. Guzzi, J. Owens, J. Morfin, C. Keppel, D. Soper ...

& the HERA-PDF Working Group

W, Z data sensitivity to strange sea

- ATLAS performed NNLO QCD fit to Z, W^+, W^- + HERA ep DIS cross sections: significant tension for Z observed when suppressing strange by 50% at low scale 1.9 GeV^2
- Fit with free strange sea gives no suppression

$$r_s = 1.00 \pm 0.20_{\text{exp}} \begin{matrix} +0.16 \\ -0.20 \text{ sys} \end{matrix}$$



nCTEQ Nuclear PDF's

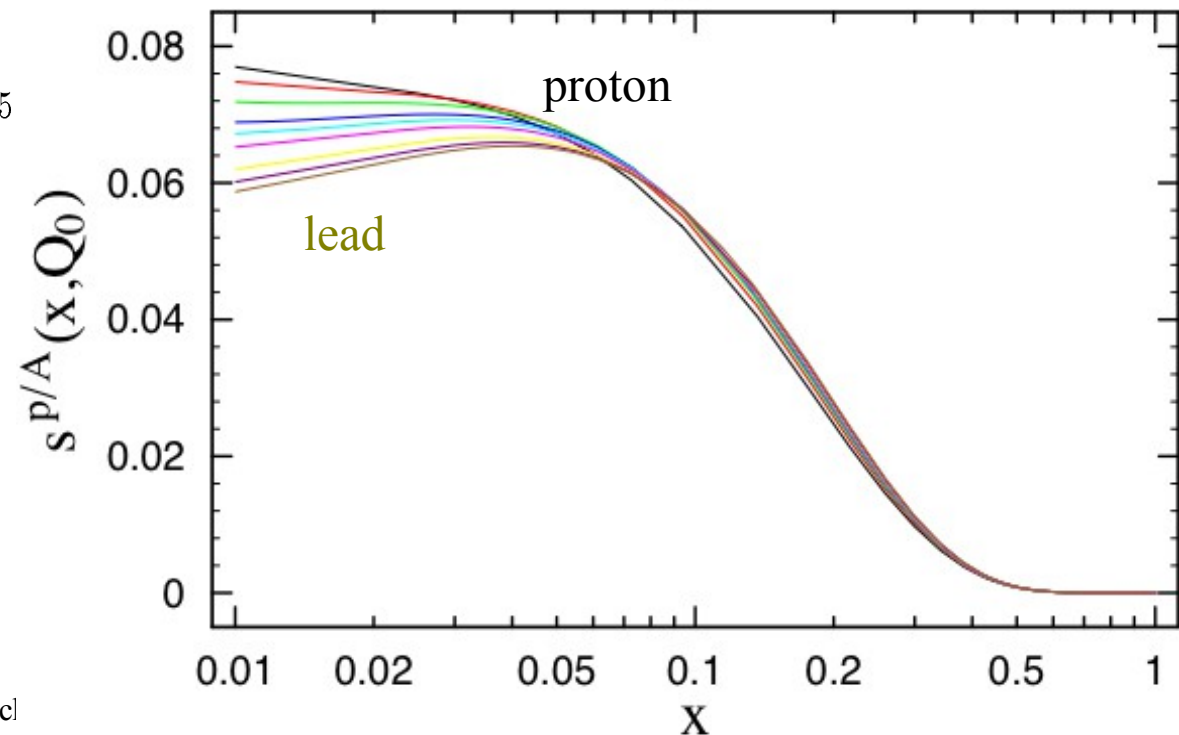
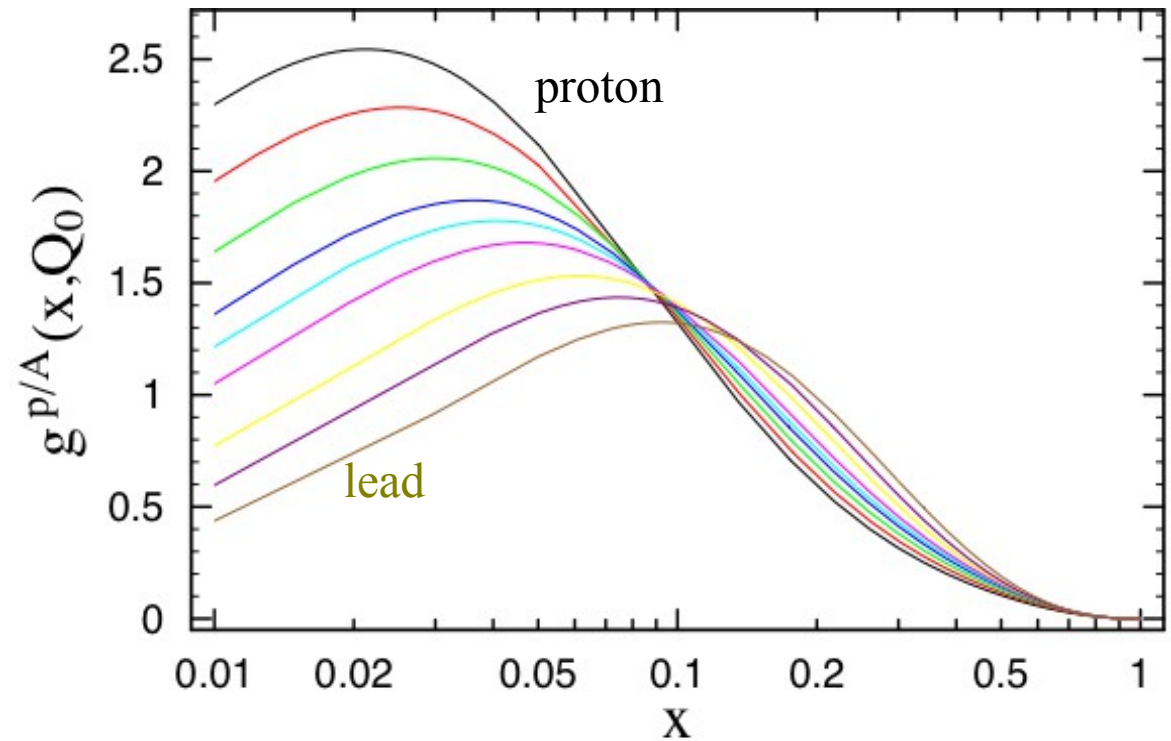
- ✓ CTEQ style global fit extended
handle various nuclear targets
- ✓ CTEQ Data + nuclear DIS & DY
[~19 targets; ~2000+ data]
- ✓ A-dependence modeled;
NLO fits work well

A-Dependent PDFs

$$xf(x) = x^{a_1}(1-x)^{a_2}e^{a_3x}(1+e^{a_4x})^{a_5}$$

$$a_i \rightarrow a_i(A)$$

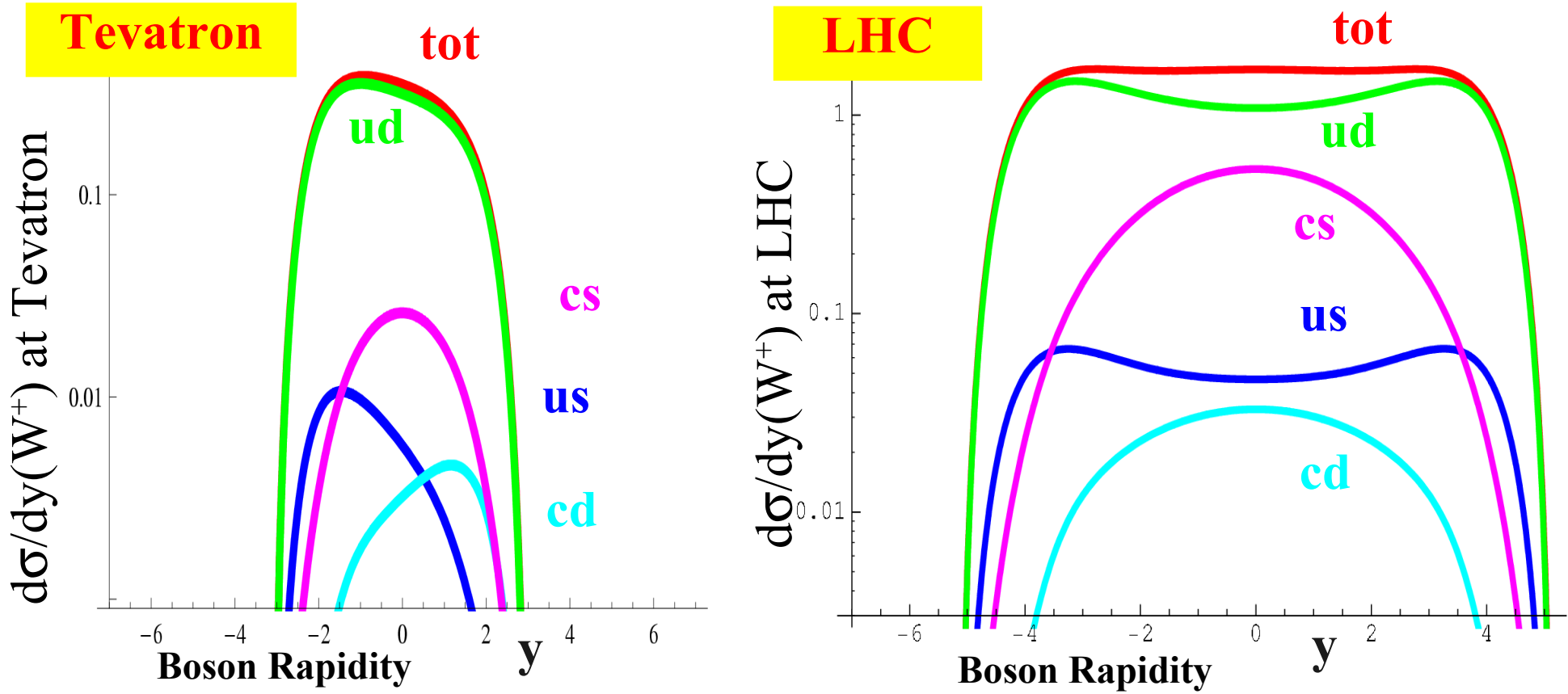
$$a_k = a_{k,0} + a_{k,1}(1 - A^{-a_{k,2}})$$



Kovarik, et al., PRD

I. Schienbein, J.Y. Yu, C. Keppel, J.G. Morfin,

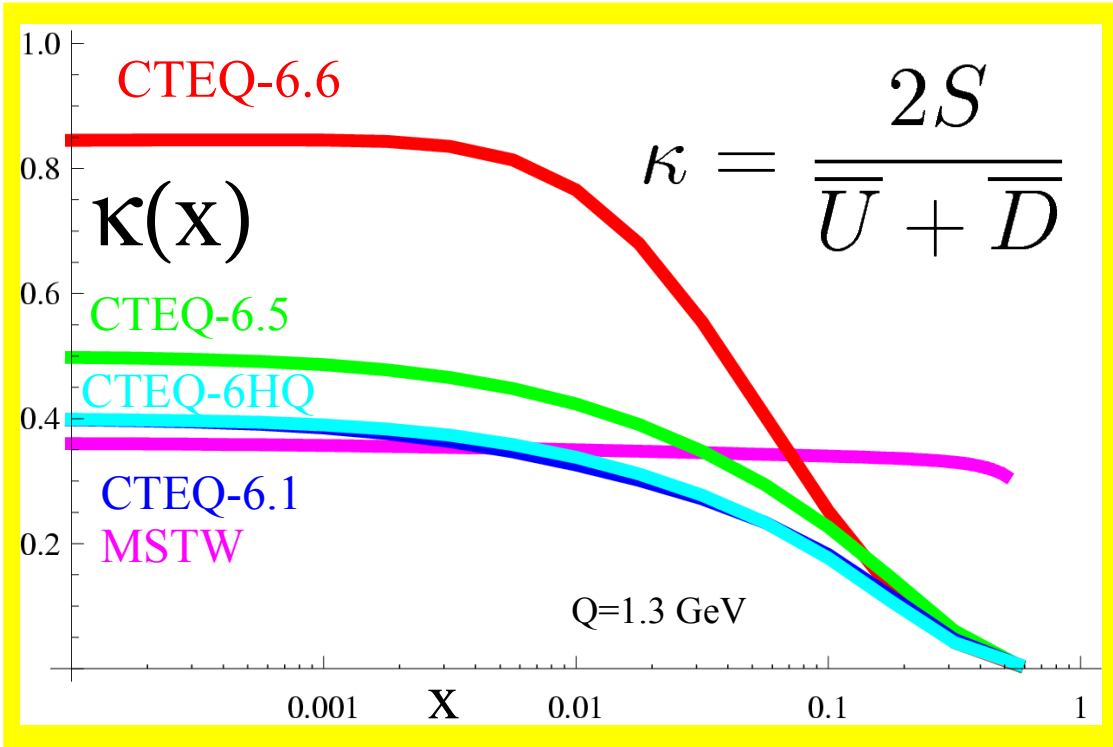
F. Olness, J.F. Owens. Phys.Rev.D77:054013,2008.



- Larger Energy \Rightarrow probes PDFs to small momentum fraction x
- Larger Rapidity (y) \Rightarrow probes PDFs to *really* small x
- Larger fraction of heavy quarks

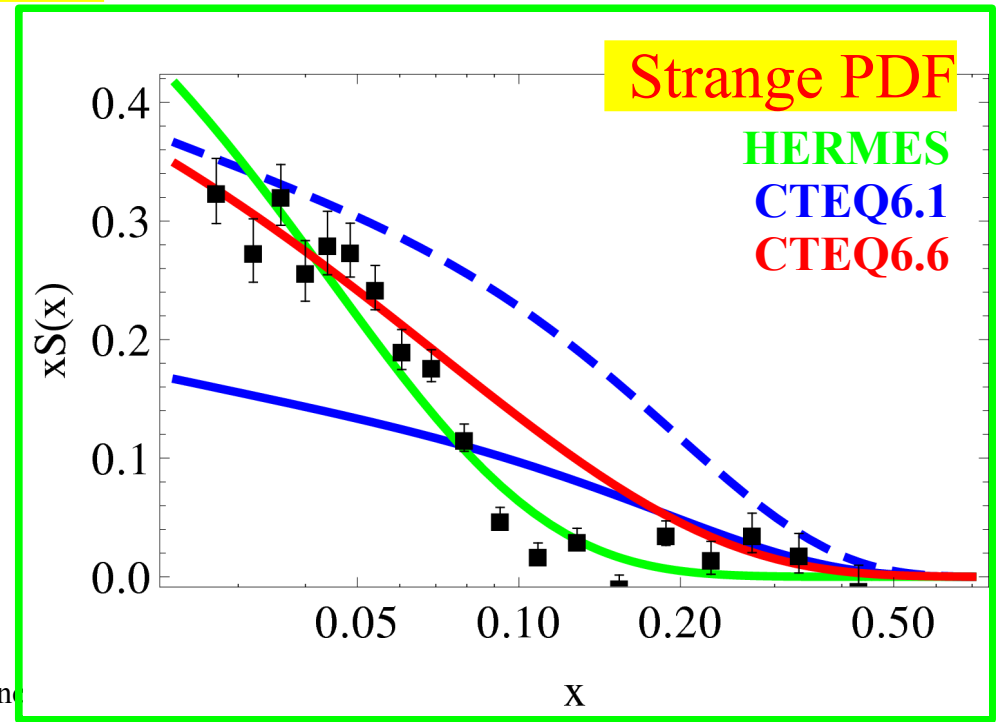
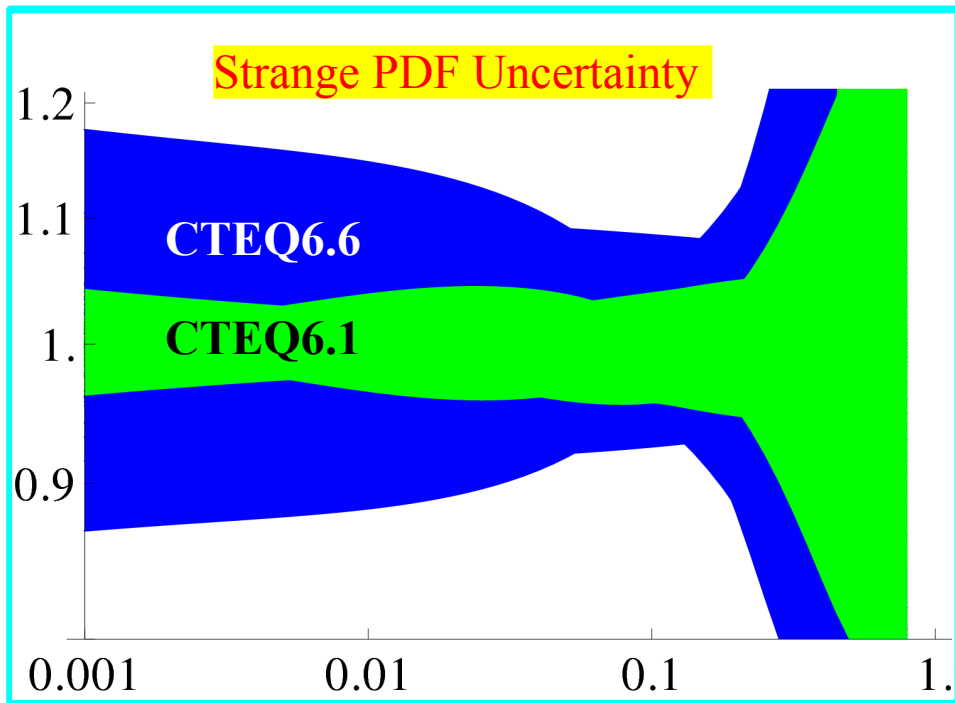
Heavy Quark components play an increasingly important role at the LHC

How well do we know the Strange PDF???

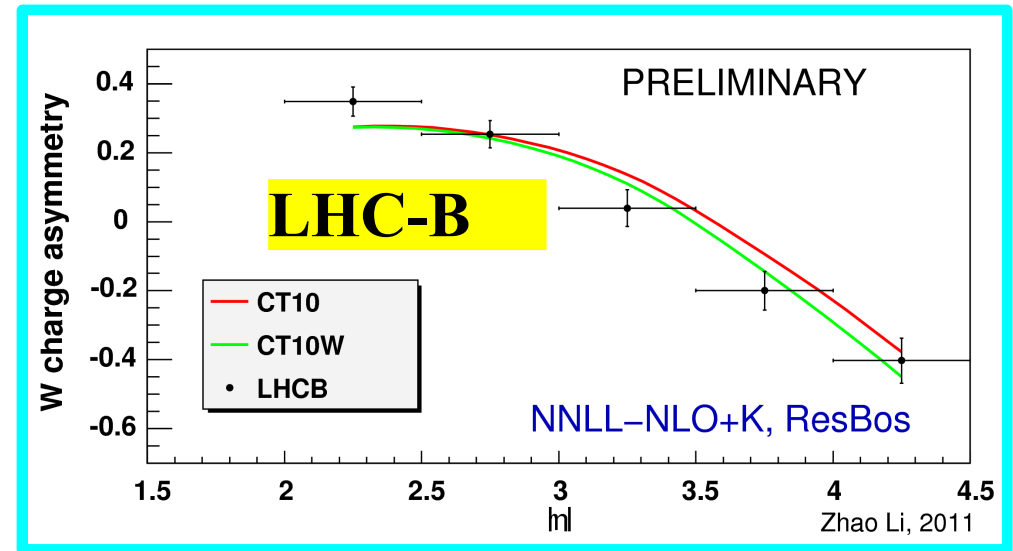
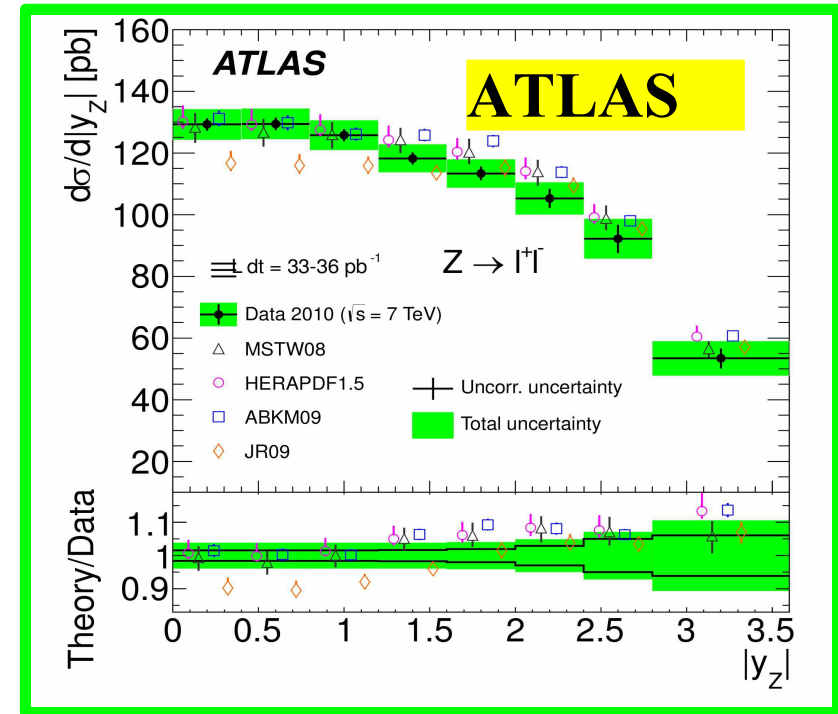
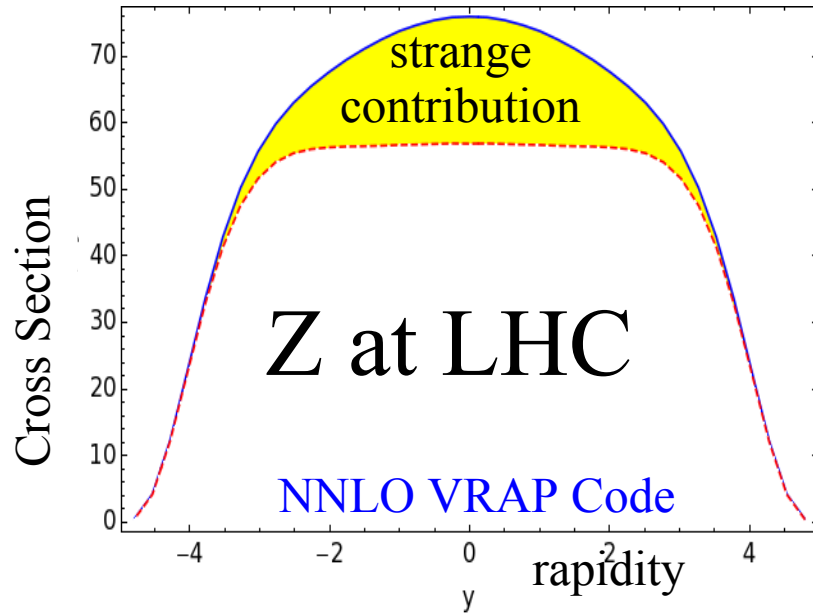
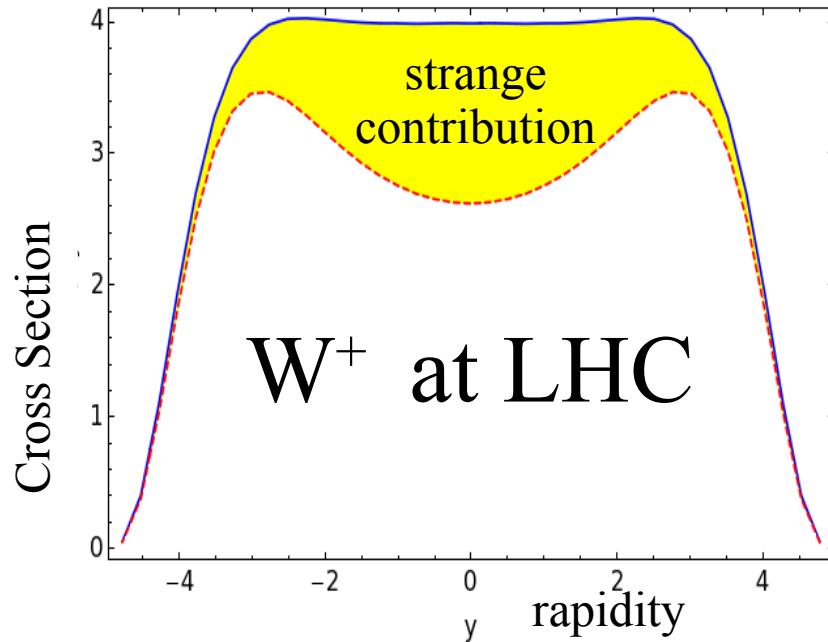


Not so well

... even after 20 years of PDFs
... extra complication:
nuclear corrections



PDF Uncertainties \Rightarrow $S(x)$ PDF \Leftrightarrow W/Z at LHC



NNLO VRAP Code
Anastasiou, Dixon, Melnikov, Petriello,
Phys.Rev.D69:094008,2004.

Kusina, Stavreva, Berge, Olness,
Schienbein, Kovarik, Jezo, Yu, Park
arXiv:1203:1290

**y distribution shape
can constrain $s(x)$ PDF**