

# CEBAF 22 GeV with Fixed Field Alternating (FFA) Gradient Design

Developing a pre-conceptual design for  
an FFA racetrack in the existing CEBAF  
tunnel to reach ~22 GeV

September 2025

**Donish Khan** on behalf of the FFA@CEBAF Collaboration

 **Jefferson Lab**



U.S. DEPARTMENT  
of **ENERGY**



# The FFA@CEBAF Collaboration



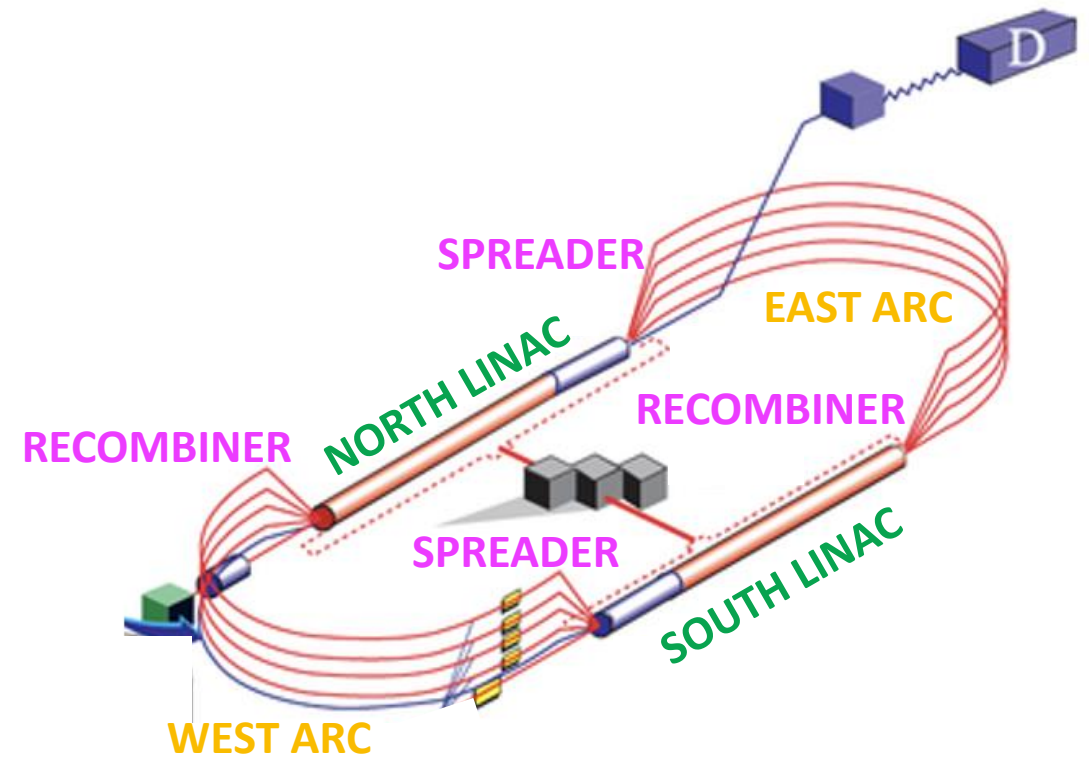
R. M. Bodenstern, S.A. Bogacz, K.E. Deitrick, B.R. Gamage, R. Kazimi, D. Khan, E.A. Nissen,  
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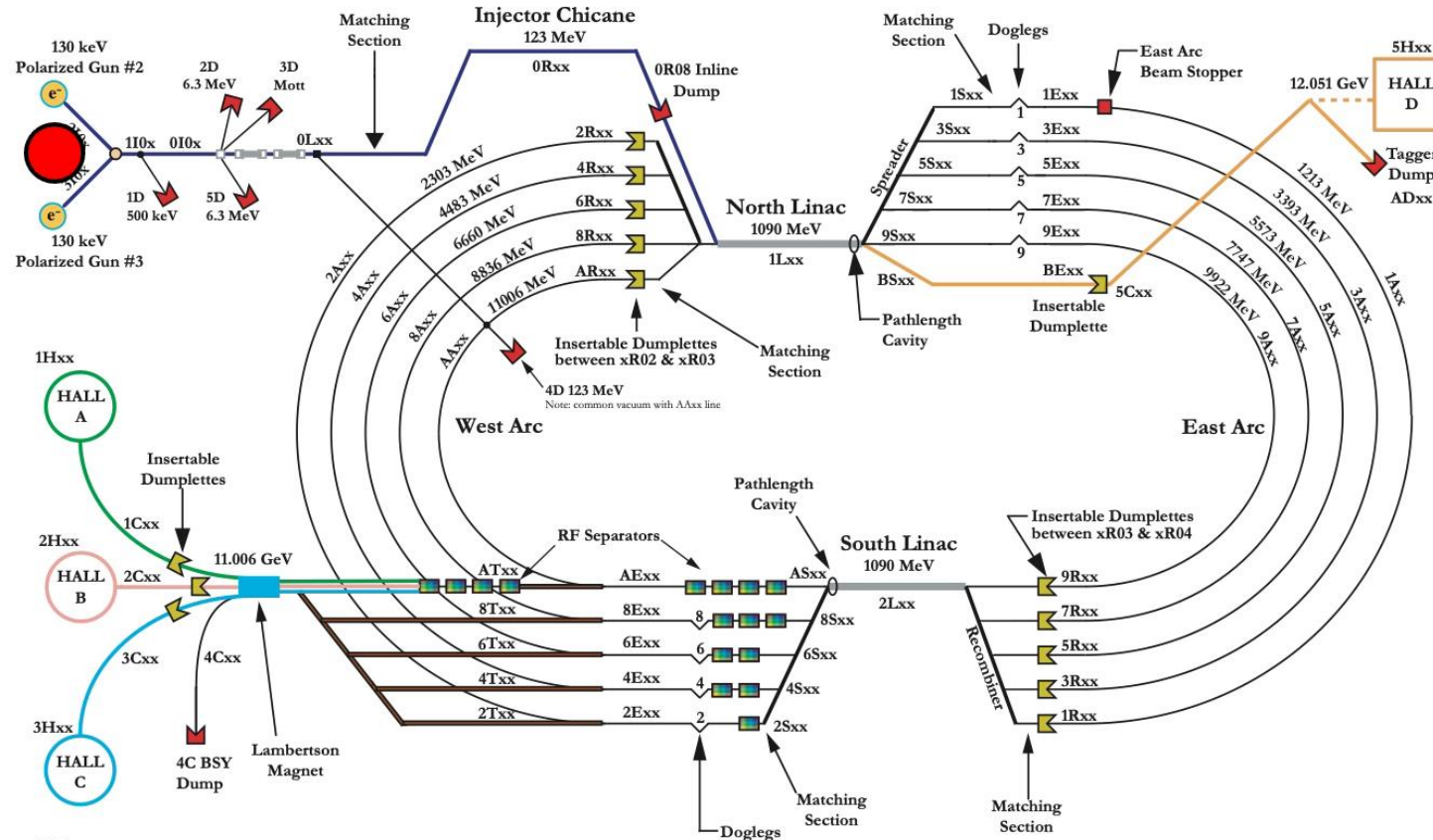
# Introduction: CEBAF @ Jefferson Lab

- The Continuous Electron Beamline Accelerator Facility (CEBAF) is a racetrack accelerator consisting of:
  1. Injection from Low Energy Recirculating Facility (LERF) with 135 MeV electron beam.
  2. Two (North and South) anti-parallel superconducting linacs ( $\Delta E_0 \sim 1.1 \text{ GeV}$ ).
  3. Two (East and West)  $180^\circ$  multi-level recirculating arcs.
  4. Beams separated via electromagnetic vertical bend systems Spreader/Recombiners.
- These components in act together to get the beam to a final energy of 12 GeV.



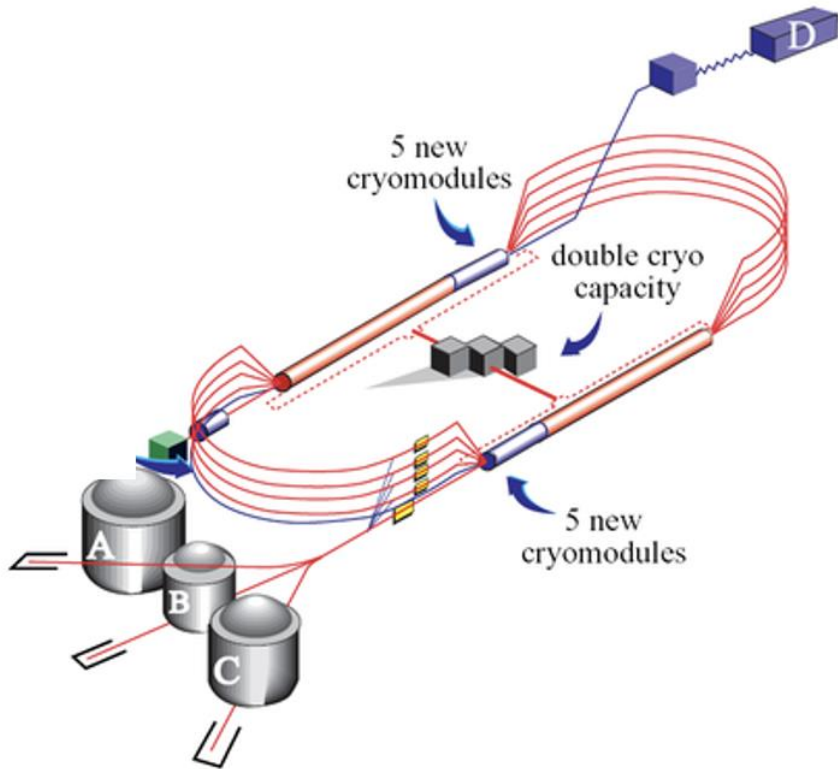
# Introduction: CEBAF @ Jefferson Lab

## JEFFERSON LAB 12 GeV BEAMLINe



E. Forman  
11 November 2013  
File: 12-GeV\_mainmachine\_beamline\_Dwg.ai

# CEBAF's Energy Upgrade

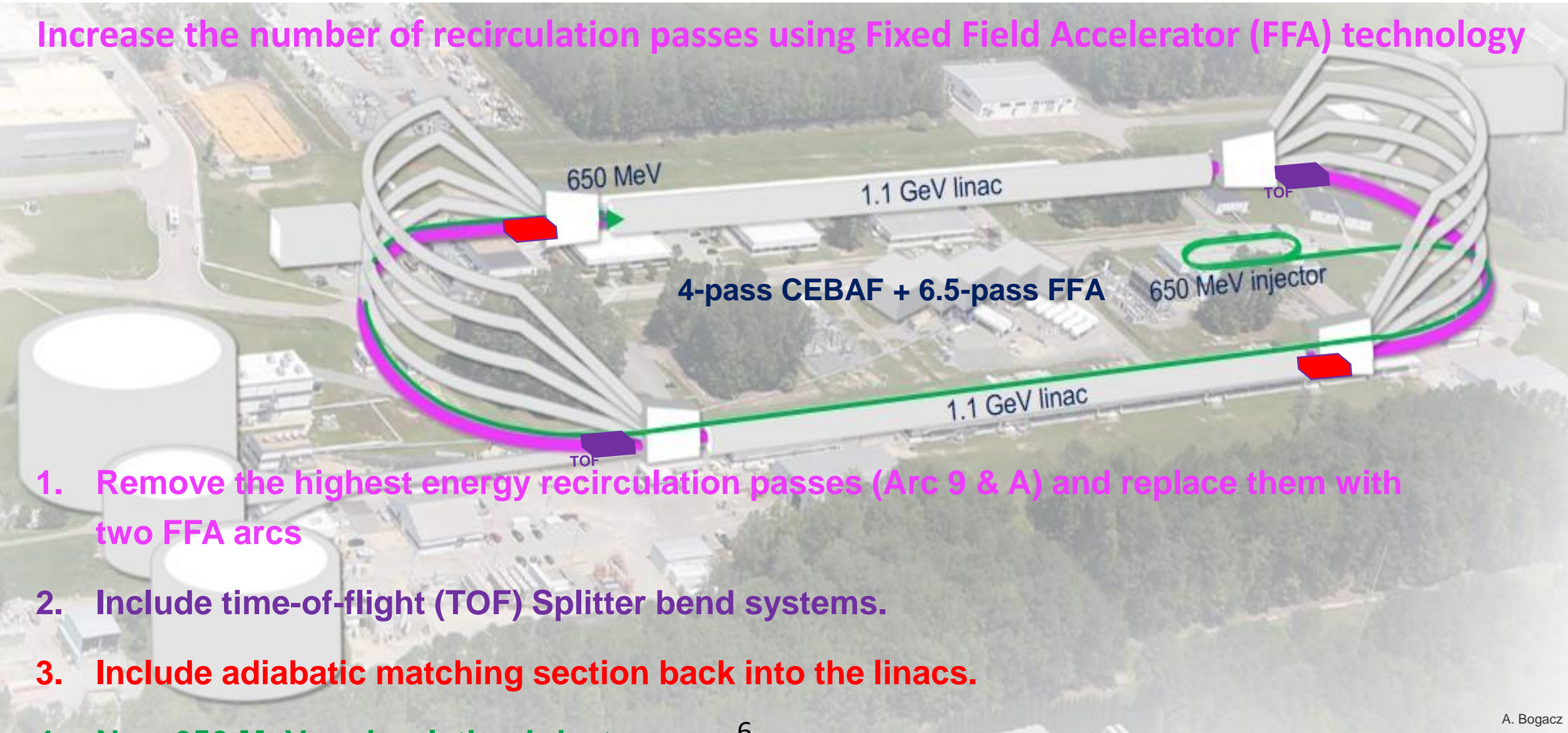


DOI: <https://doi.org/10.22323/1.172.0001>

- The last energy upgrade (6 GeV to 12 GeV) in ~2015 was achieved by adding additional RF cryomodules in linacs free space:
  - 5 Cryomodules per linac
  - Cryomodule energy change: 100 MV
- Next Energy upgrade (12 GeV to 22 GeV):
  - Existing footprint preserved.
  - No room for additional cavities.
  - Need to be clever; leverage advancement of magnet/accelerator technology.

# FFA@CEBAF

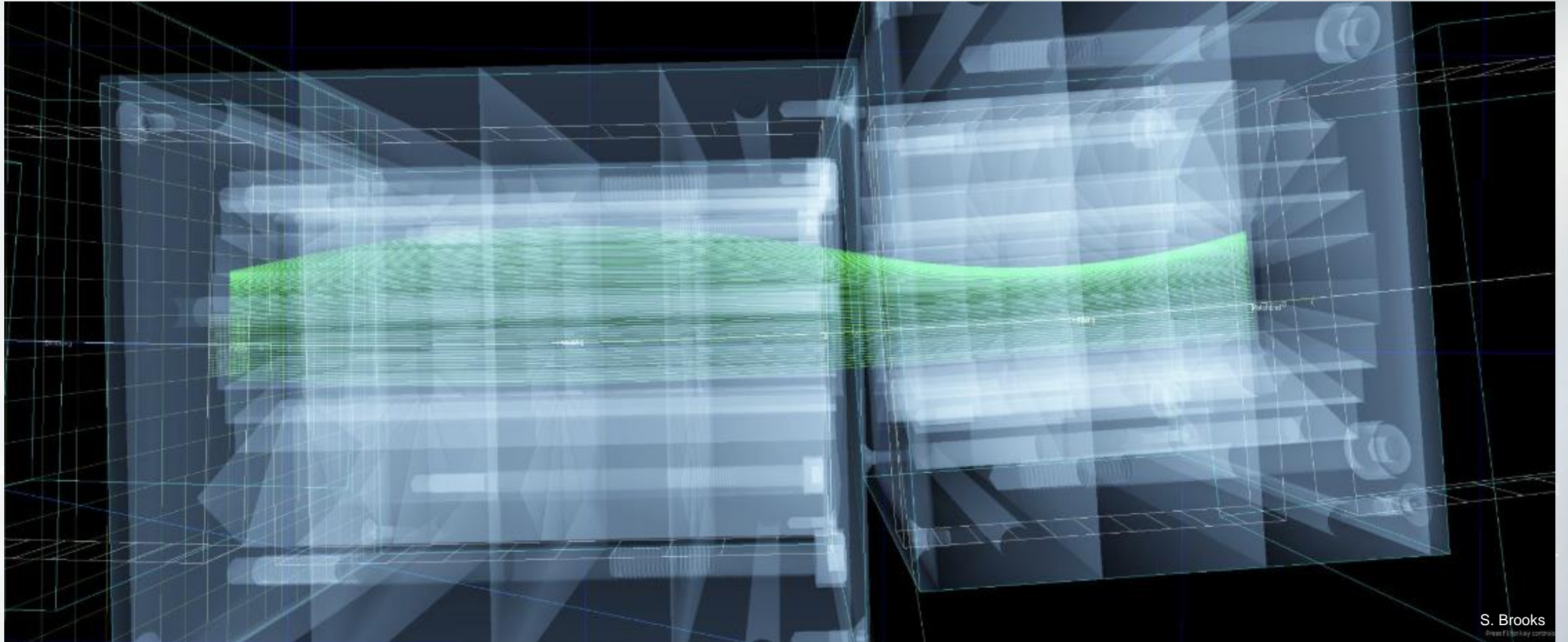
Increase the number of recirculation passes using Fixed Field Accelerator (FFA) technology



1. Remove the highest energy recirculation passes (Arc 9 & A) and replace them with two FFA arcs
2. Include time-of-flight (TOF) Splitter bend systems.
3. Include adiabatic matching section back into the linacs.
4. New 650 MeV recirculating injector

- For the current 22 GeV baseline (650 MeV inj + 4-pass CEBAF + 6.5-pass FFA) we have the following modifications:
  1. FFA arc(s) in highest-energy recirculating arc location(s)
  2. 135 MeV → 650 MeV injector upgrade
  3. New multi-pass linac optics
  4. Design of modified CEBAF EM arcs and switchyard(s):
    - a) Arcs 1-8
    - b) TOF correction 'Splitters'
    - c) Arc-To-Linac Transition Section

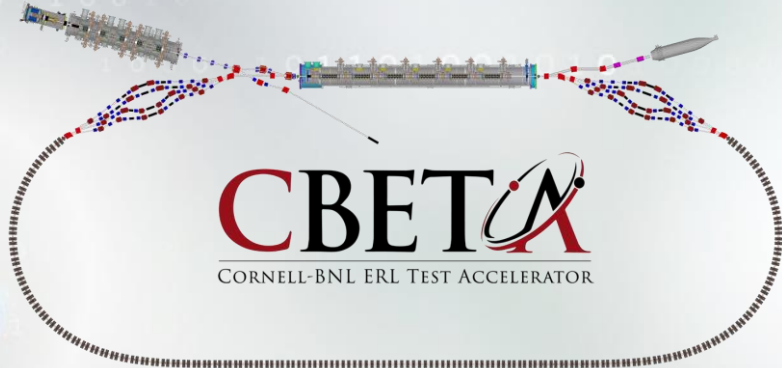
# FFA Arc - FODO Cell



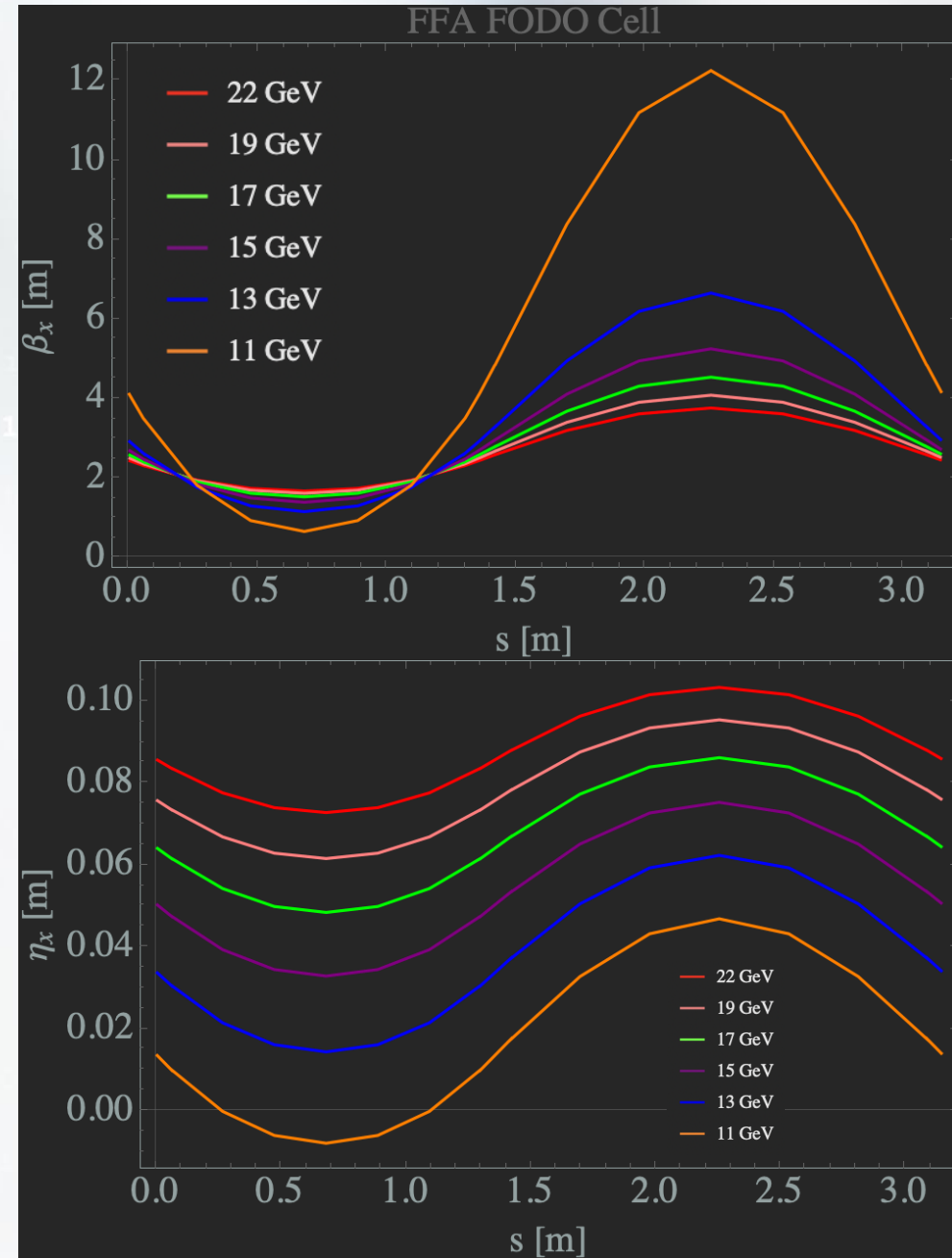
S. Brooks  
FFA Arc - FODO Cell

# FFA Arc – Compact FODO Cell

Inspiration taken from Cornell-BNL ERL Test Accelerator (CBETA, 40 - 150 MeV):



- Large momentum acceptance; transport 6 beams with energies spanning a factor of two (11 - 22 GeV)
  - Compact cells:  $L_{\text{cell}} = 3.15 \text{ m}$
  - Small betas (sub 10 m)
  - Low dispersions (a few cm)
- Closely spaced orbits for all six beams ( $\sim 4 \text{ cm}$ )



= 0.4 ns

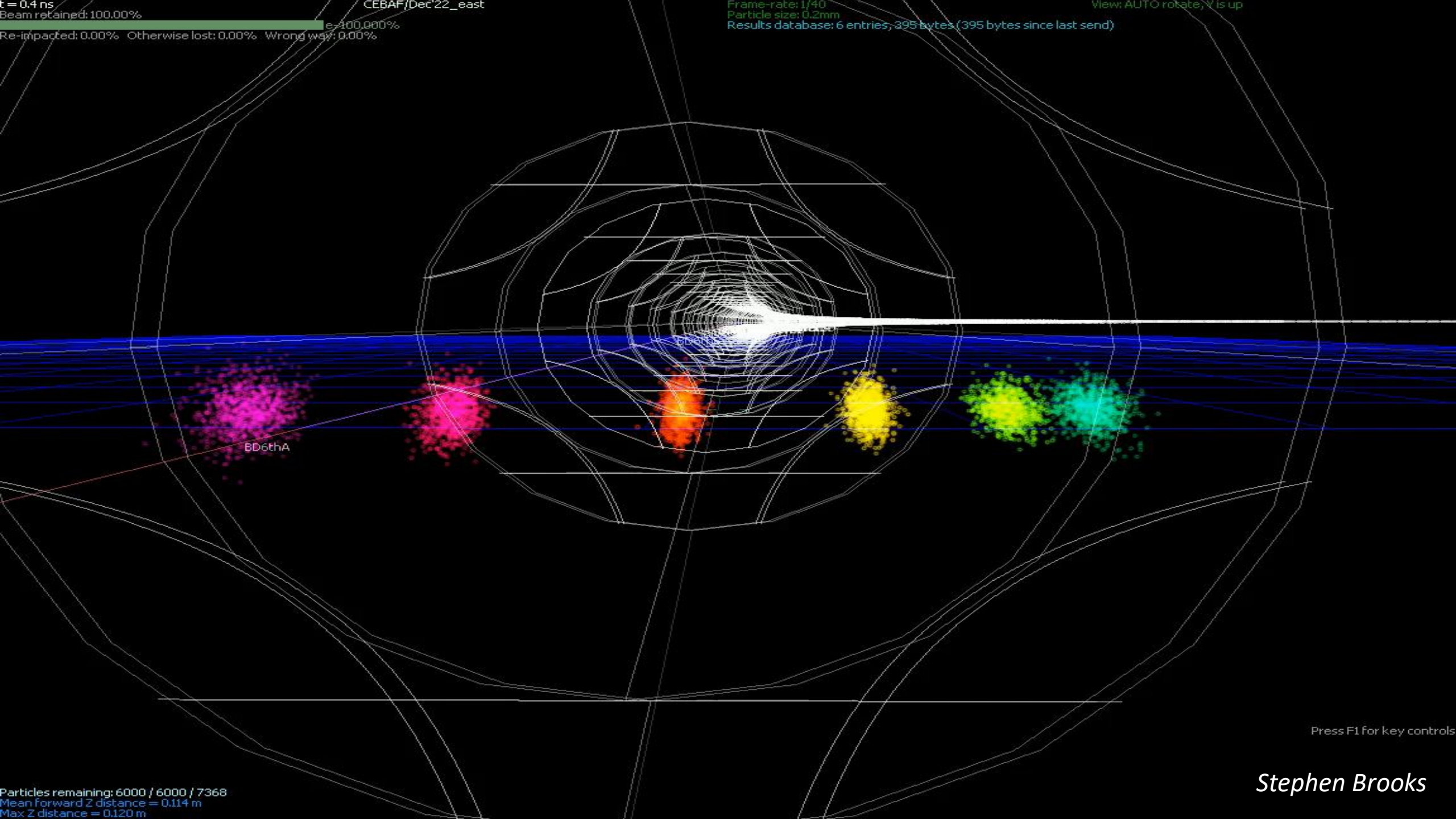
Beam retained: 100.00%  
e- 100.000%

CEBAF/Dec 22\_east

Frame-rate: 1/40  
Particle size: 0.2mm  
Results database: 6 entries, 395 bytes (395 bytes since last send)

View: AUTO rotate, Y is up

Re-impacted: 0.00% Otherwise lost: 0.00% Wrong way: 0.00%



BD6thA

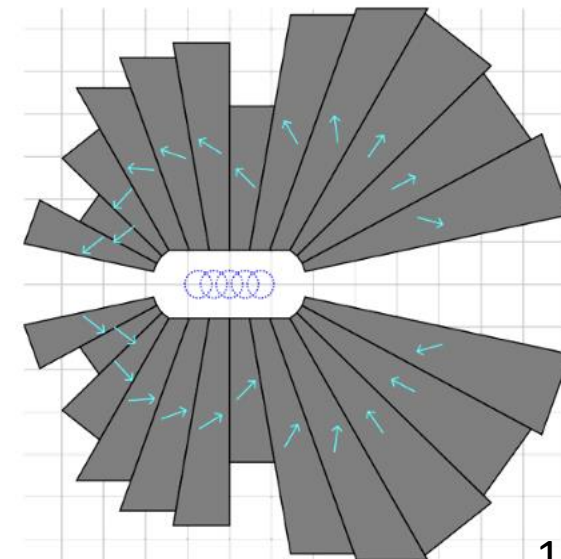
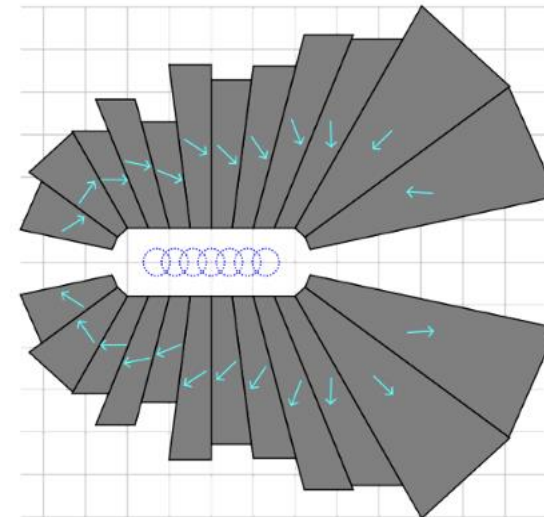
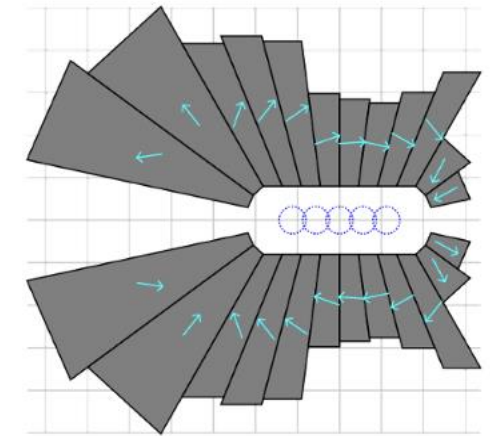
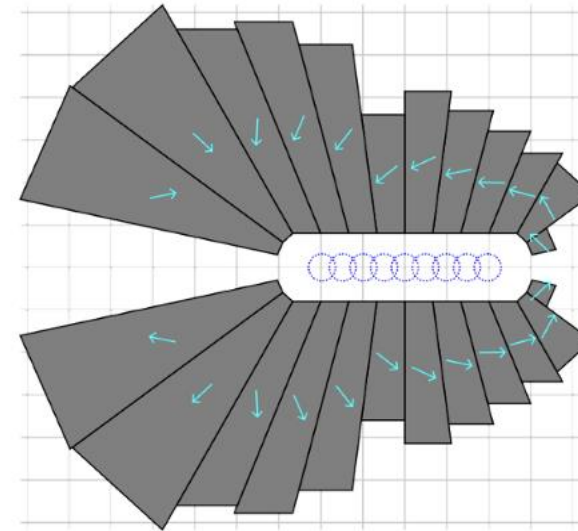
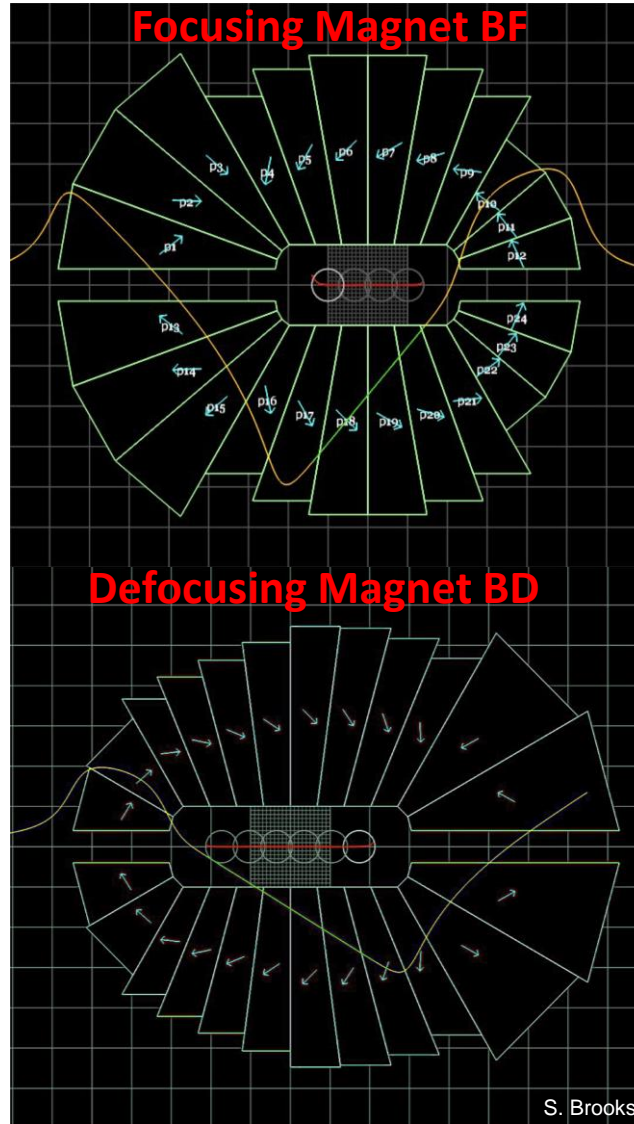
Press F1 for key controls

Particles remaining: 6000 / 6000 / 7368  
Mean forward Z distance = 0.114 m  
Max Z distance = 0.120 m

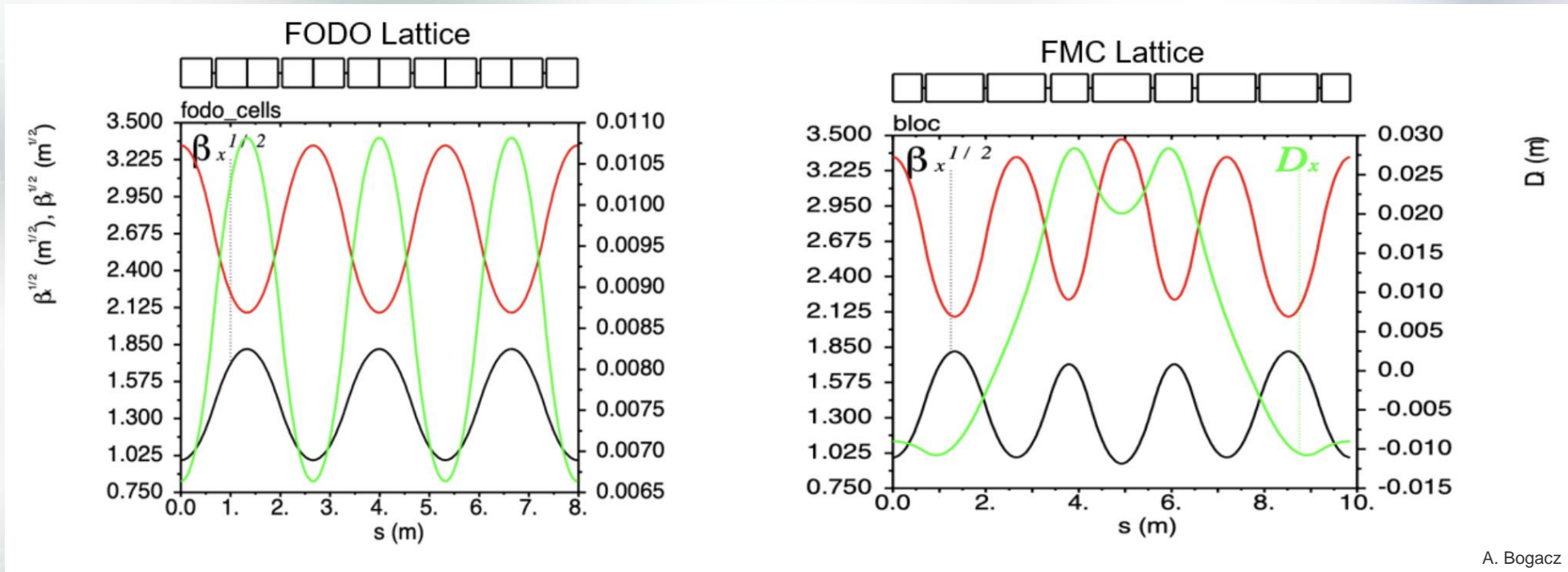
Stephen Brooks

# Halbach Permanent Magnet Design

- **Compact** compared to conventional electromagnets.
- Allows for accommodating 6 additional passes in CEBAF tunnel.
- Provides power and cost savings.
- Open mid-plane geometry
- Concept successfully tested at **CBETA**.



# Exploring Different FFA Optics

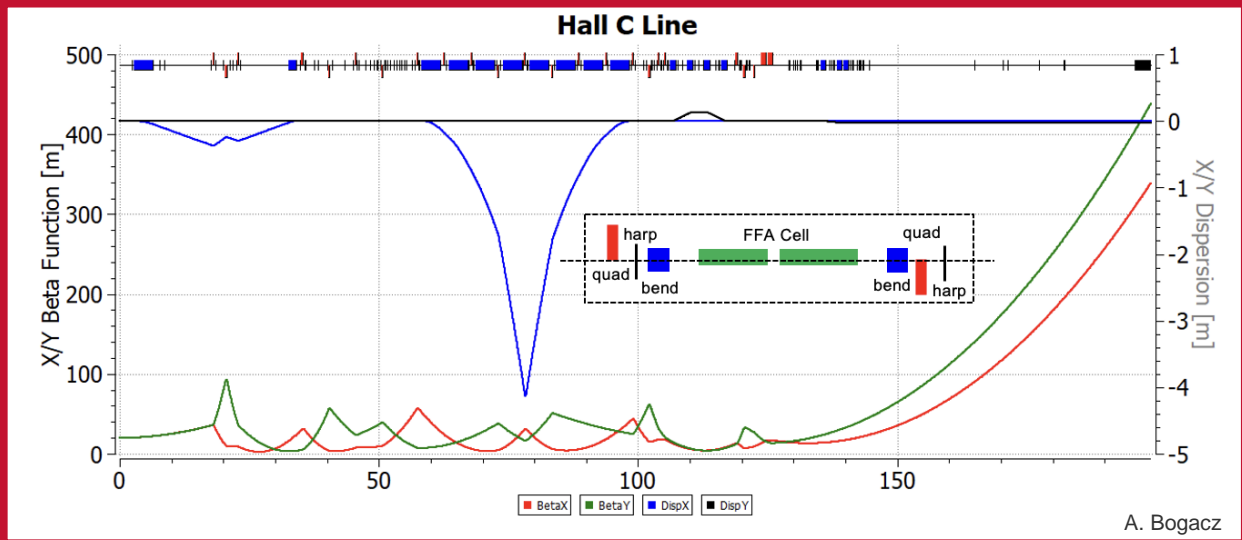
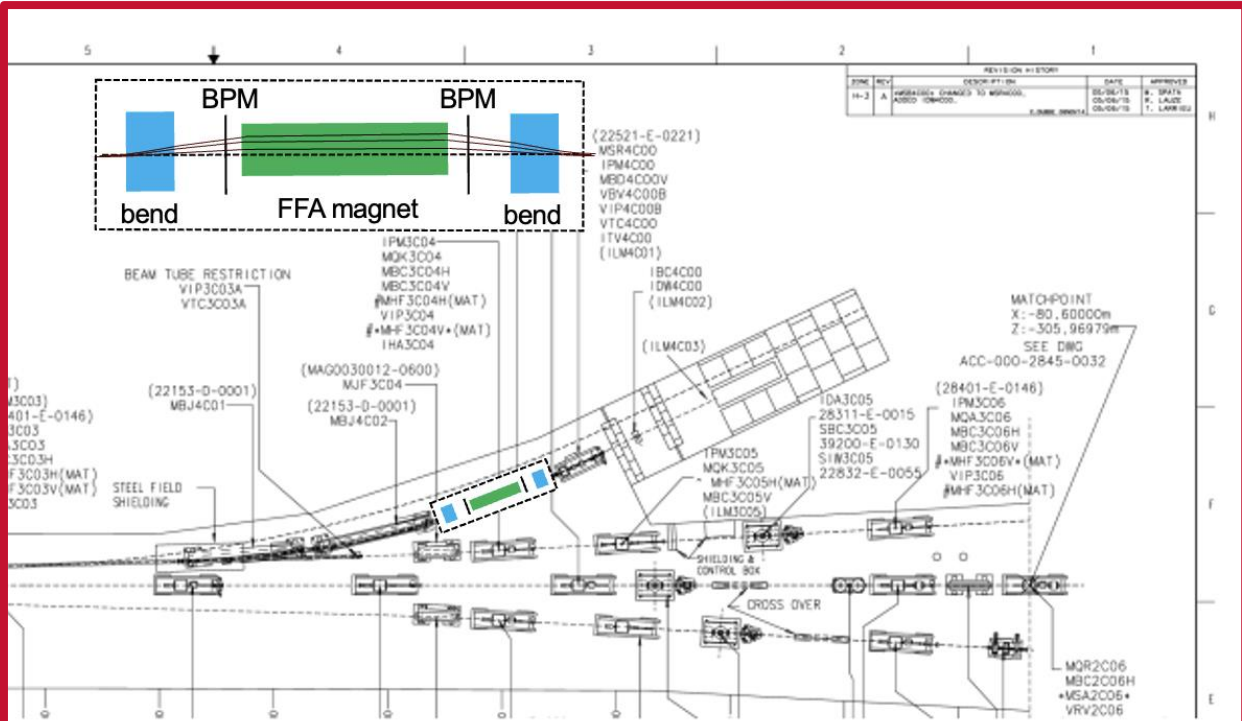


A. Bogacz

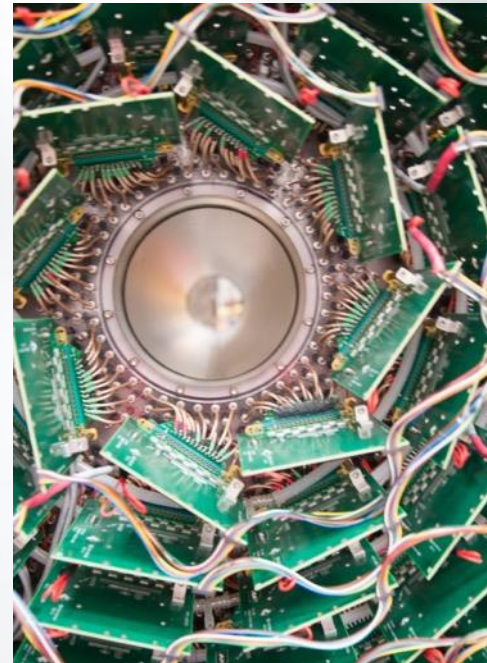
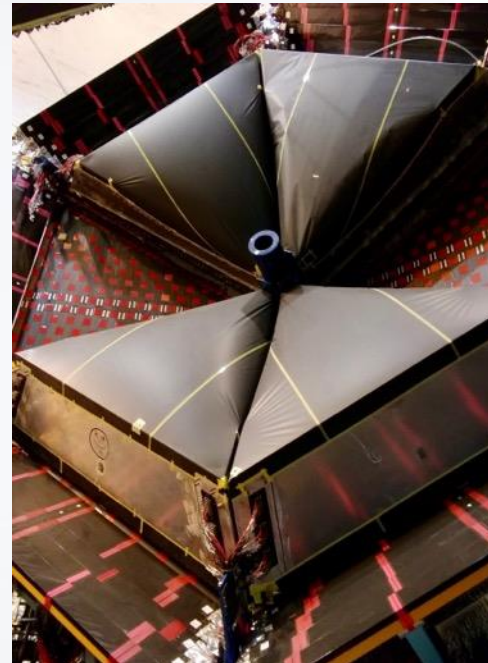
- FFA arc optics are flexible enough to have several options.
- Exploring a Flexible Momentum Compaction (FMC) lattice.
  - Similar betatron function amplitudes.
  - Larger dispersion amplitude but quasi-isochronous ( $R_{56} \sim 0$ ) across all 6 passes.
  - Relax stringent constraints (e.g.  $R_{56}$ , time of flight, dispersion, derivative of dispersion, and Twiss parameters) on the upstream systems, such as: the 'Splitter' and the FFA arc-to-linac 'Transition'.

# FFA Beam Transport Test at CEBAF

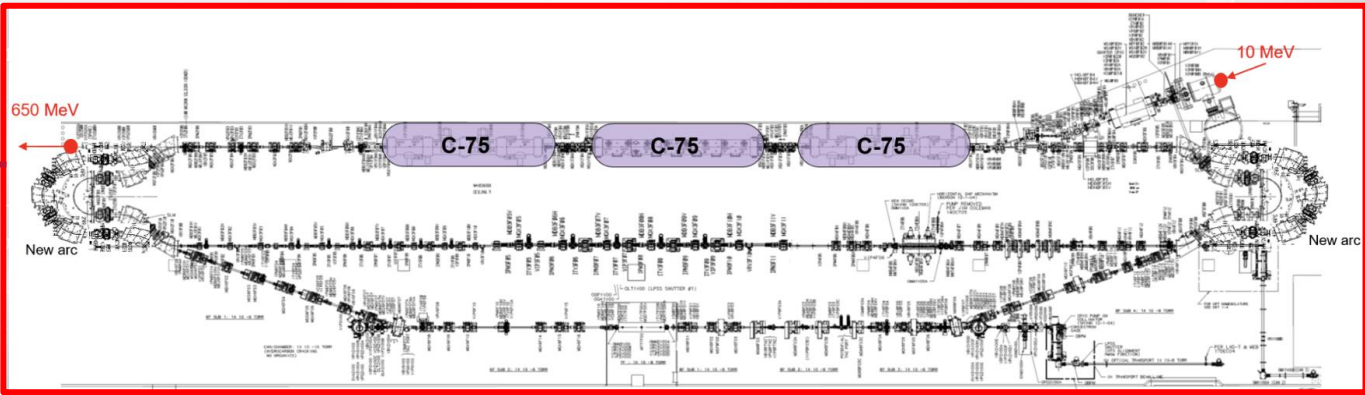
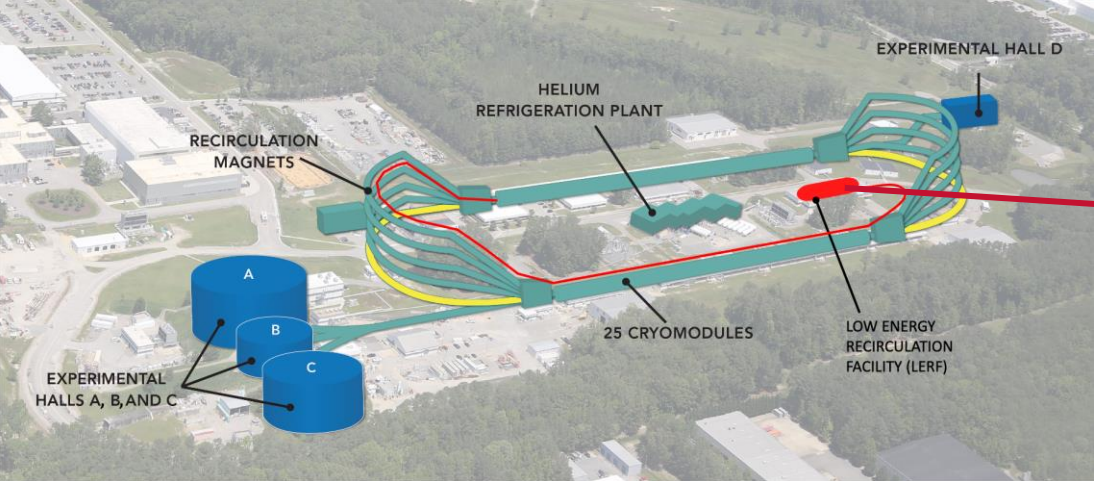
- Expand on the low-energy demonstration at **CBETA**.
  - Transport beams of multiple/higher energies spanning a factor of  $\sim 2.5$ :
    - 4.5, 6.7, 8.9 & 11 GeV
  - Orbit/Optics validation for FFA Cell
  - Technology demonstration
- Two potential (dispersive) sites:
  - BSY Dump
  - Hall C
- Actual study is pending funding via Jefferson Lab's LDRD program.



# Injector Upgrade

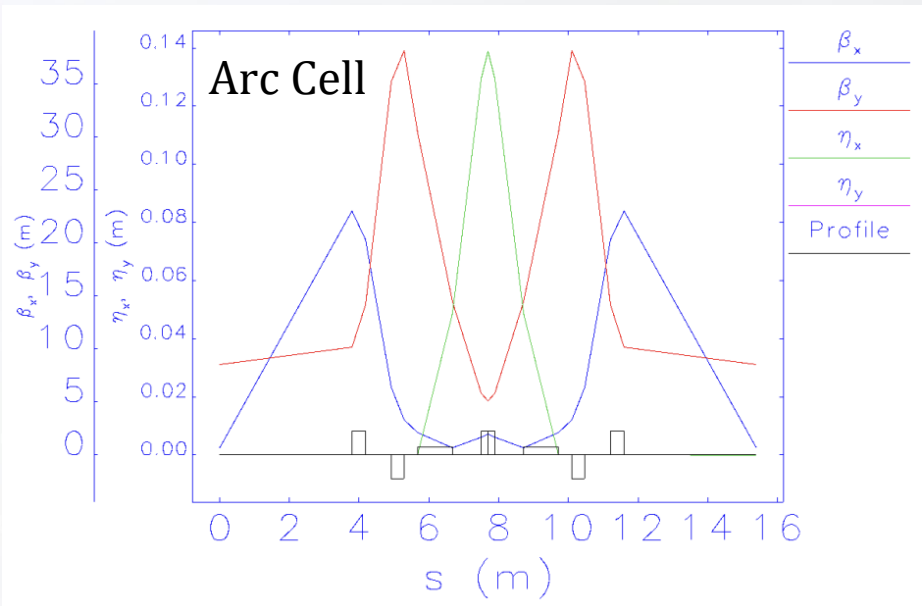
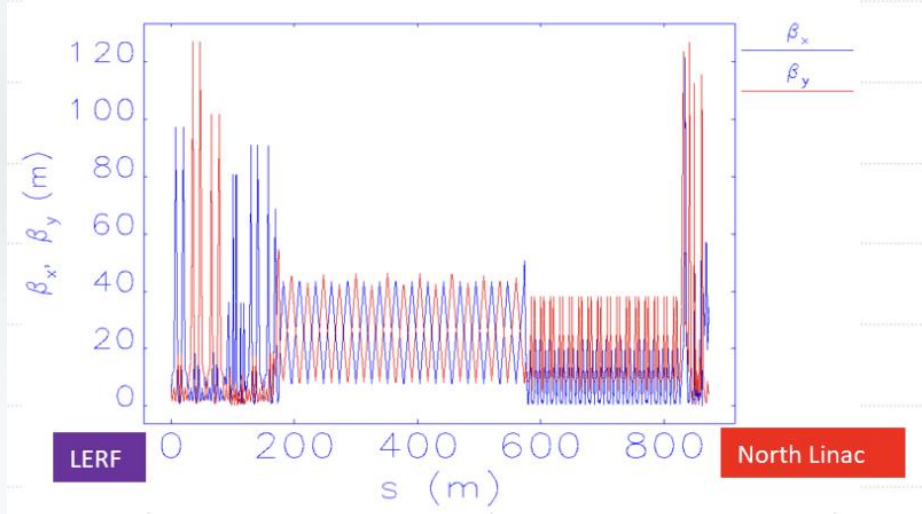
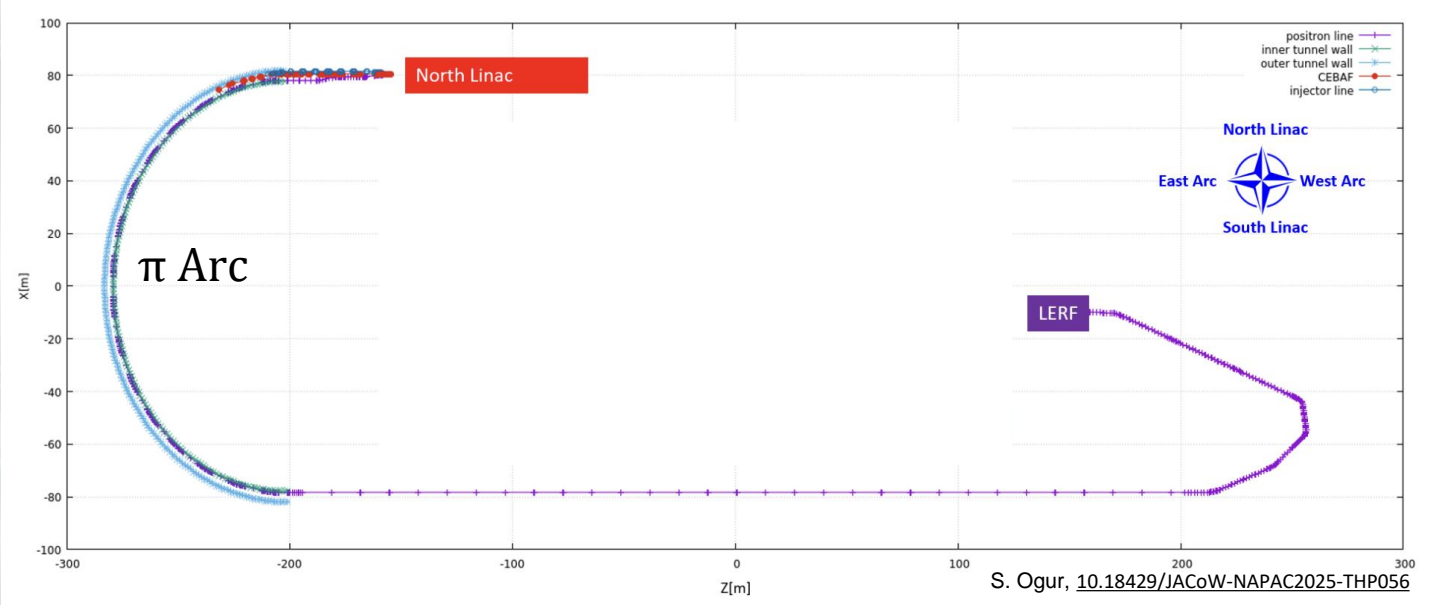


# Injector Upgrade – 650 MeV Recirculating Injector



- With the present 135 MeV injector, the difference in the first and final pass energies in the North Linac is too large (1:175) to effectively control the beam.
- 650 MeV recirculating injector (3-pass) based on Low Energy Recirculator Facility (LERF) will allow a manageable difference in energies (1:33)

# Injector (LERF) Transfer Line Optics



- LERF to North Linac transfer line has been designed.
- Composed of several beamlines:
  1. LERF Transfer Line (LTL)
  2. South Transfer Line (STL)
  3. West transfer Line (WTL)
  4. Merger Transfer Line (MTL)

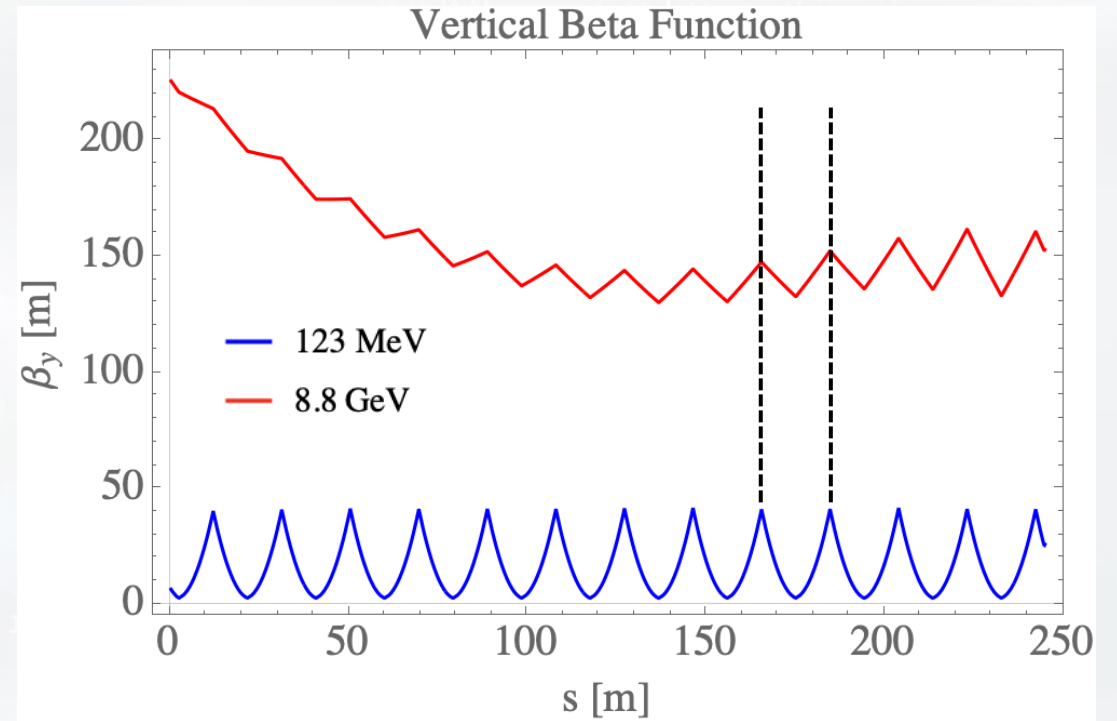
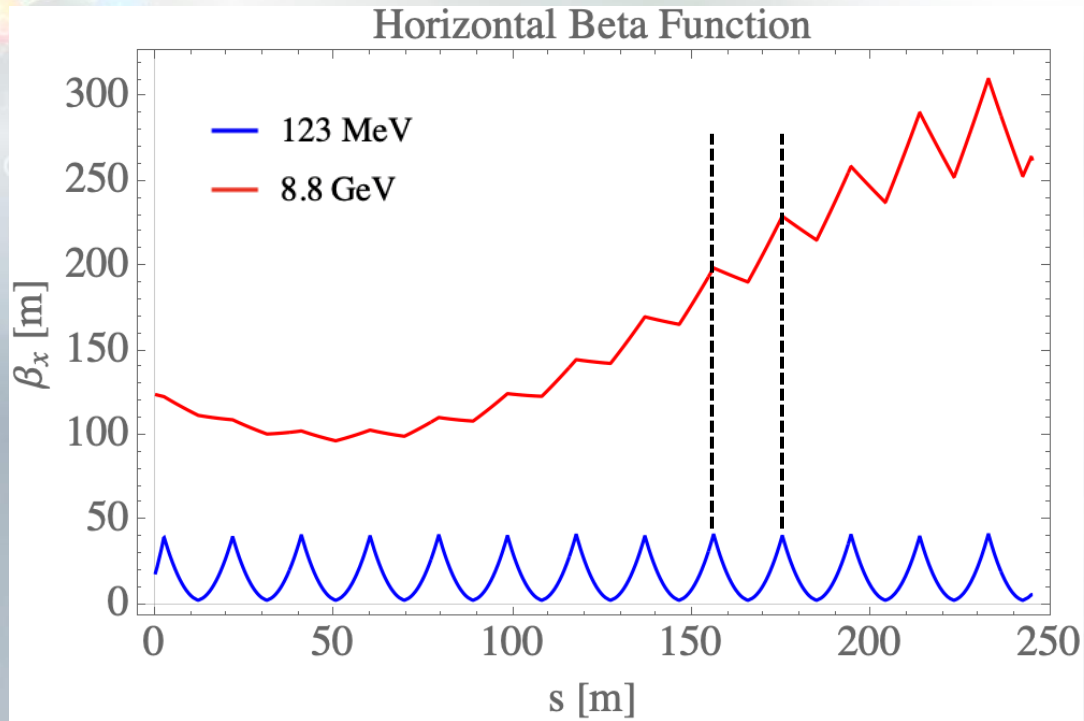
3 simulation cross validation: elegant, Bmad, OptiM

# Linac Optics Upgrade



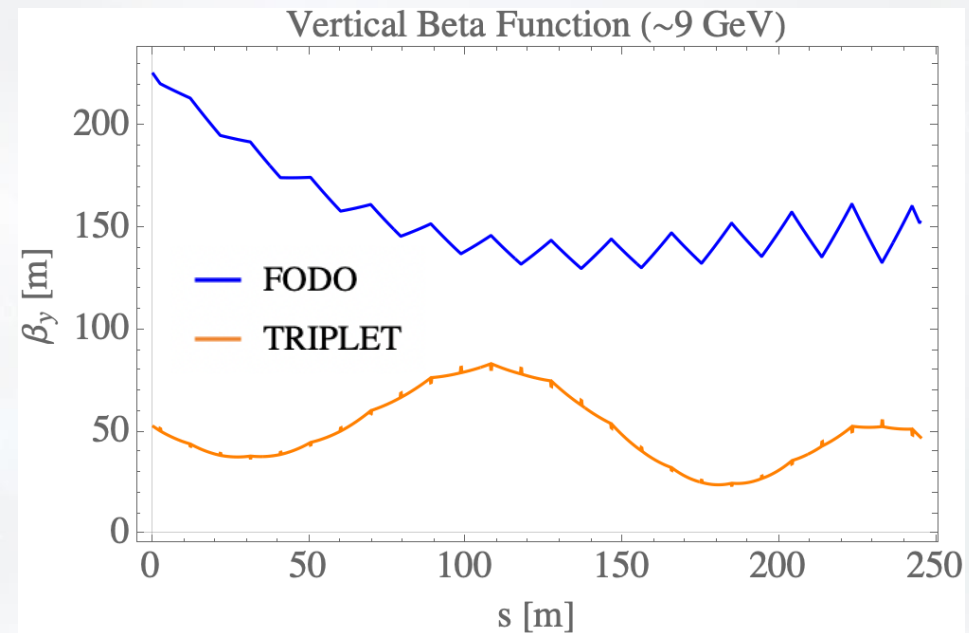
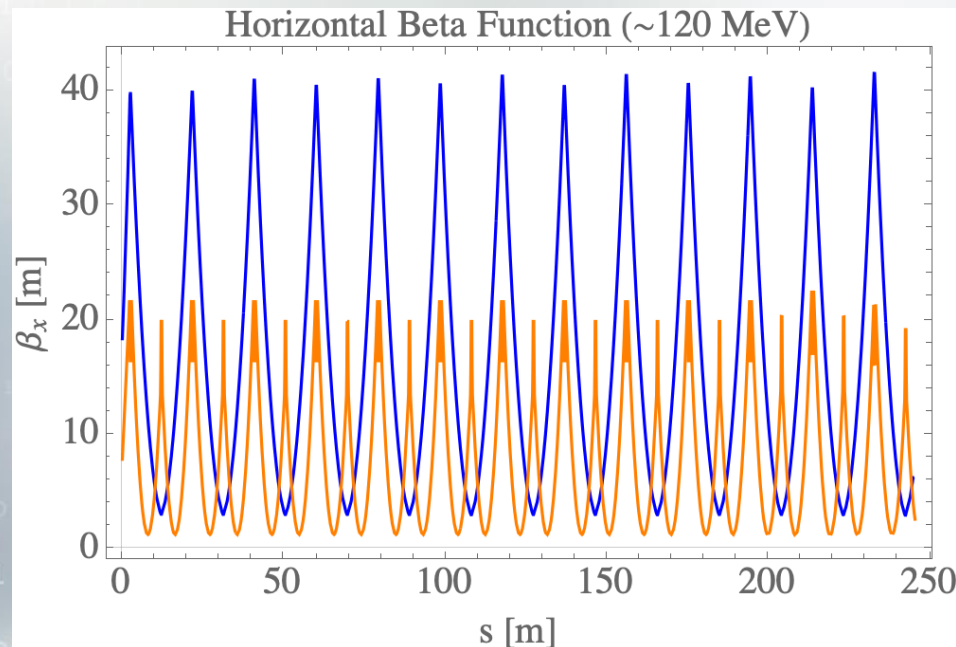
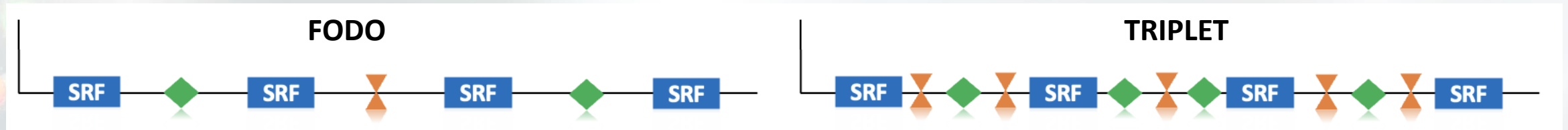
# 12 GeV CEBAF Linac Optics

- Current CEBAF linac is composed of FODO cells.
- There is no electromagnet “ramping” implemented.
- From ~0.1 GeV injection to 12 GeV final energy the focusing structure is static.
- Energy increases with each pass and via higher beam rigidity nullifies the focusing.
- Error in the focusing creates beta-beating.

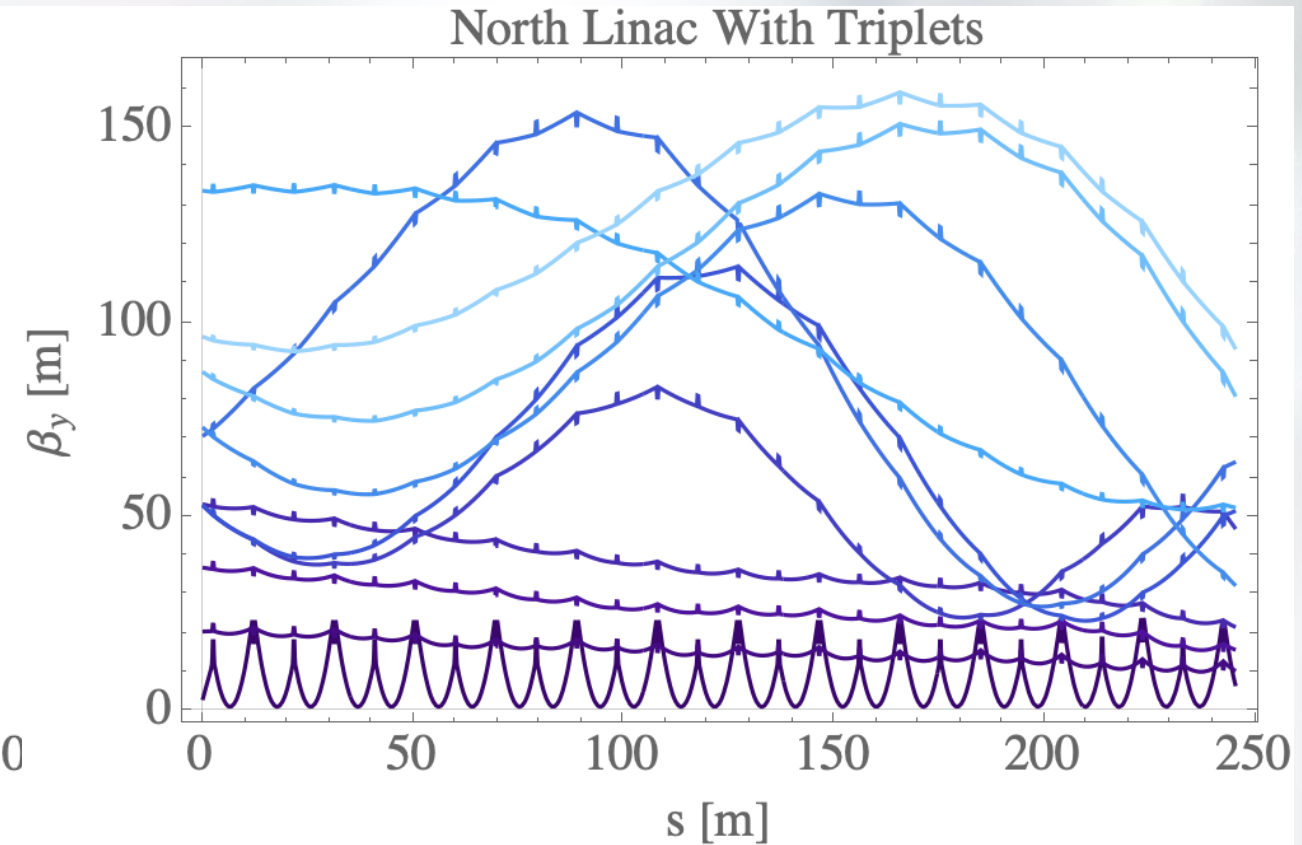
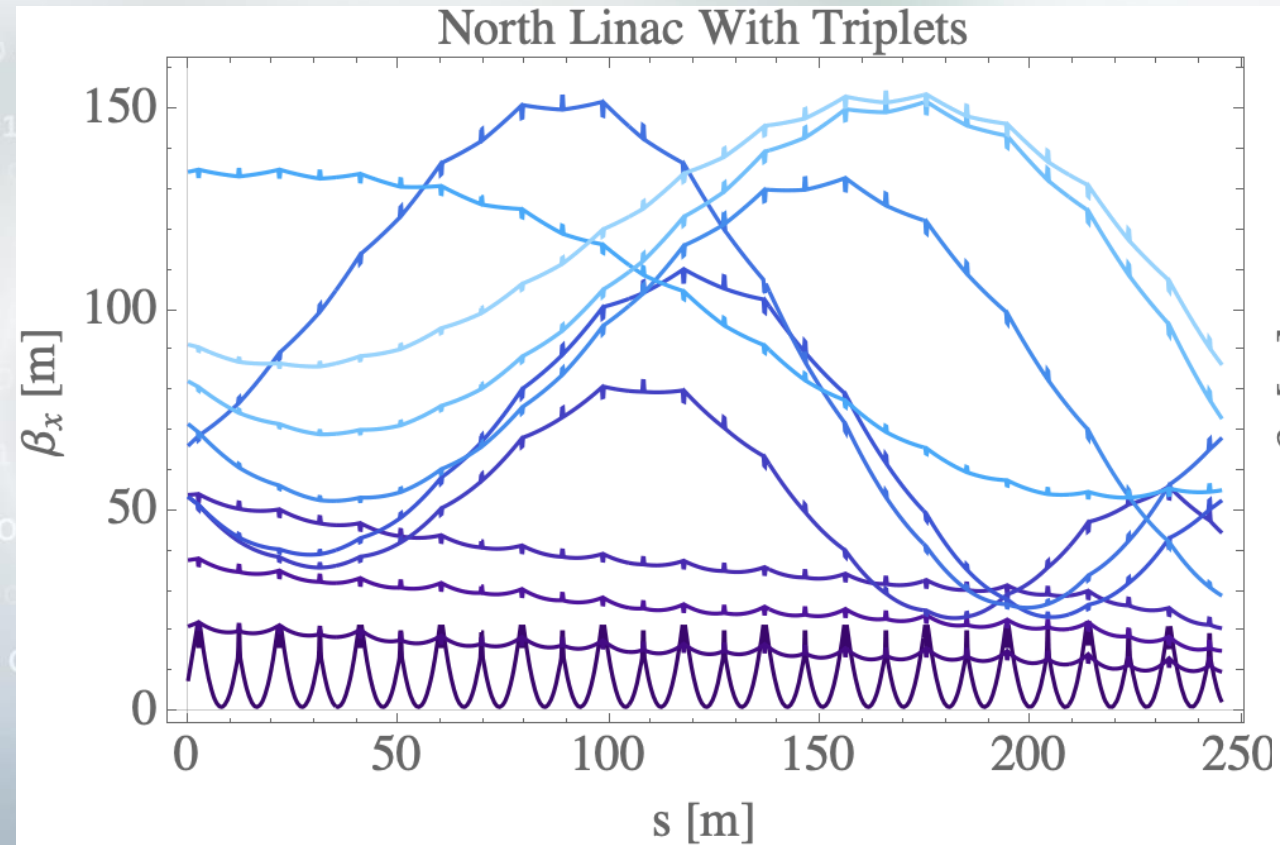


# Linac FODO to Triplet

- Present FODO linac offers periodic optics generates large beta beating for higher passes (beta  $\sim 1000$  m), which is not compatible with the acceptance of the SRF linac or the small betas ( $\sim 5$  m) in the potential FFA arcs.
- Replacing FODO with alternating triplets – more uniform beam envelope (beating still exists).

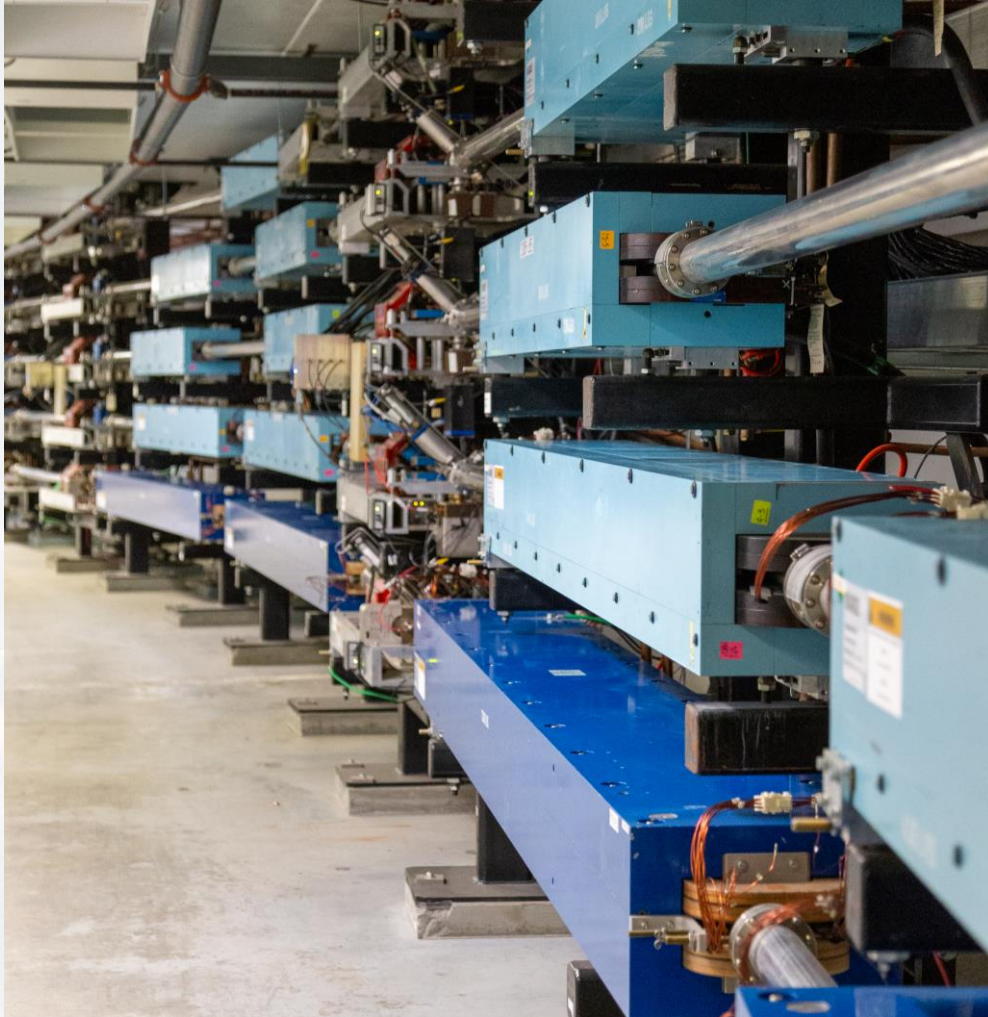


# 'Beta Beat' Linac Optics for FFA Passes (passes 5-10)



- Deviate from optics periodicity  $\Rightarrow$  Induce and optimize  $\beta$  beat in linacs  $\Rightarrow$  Reasonably small  $\beta$ 's at both ends of each linac at the expense of increase in maximum  $\beta$  inside the linacs,  $\alpha$ 's adjusted to nearly zero as favored by FFA matching  $\Rightarrow$  Greatly relaxed matching requirements

# Modified Arcs/Switchyard to FFA



# Electromagnetic (Non-FFA) Arcs

- The recirculation arcs are composed of bend magnets that are rated for limited B-field limit.
- The new beam energy would require certain arcs to exceed their B-field limit.
- Low-cost solution (Jay B.) upgrade arcs by moving them vertically by one slot, discarding ARC1 (too weak).
- Rematch new incoming/outgoing optics from Linacs to periodic optics of Arc.



Current electromagnetic recirculation arcs in CEBAF

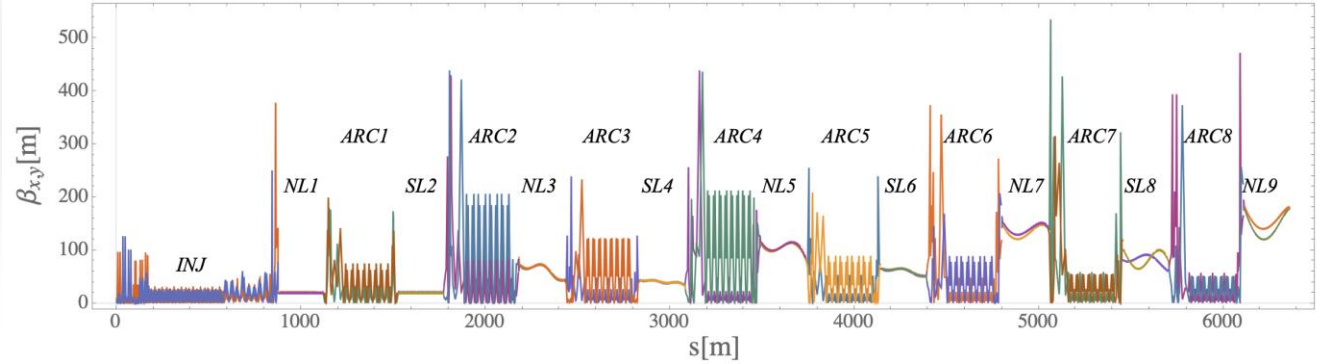
# Electromagnetic Arcs Optics

- Recirculation arcs are responsible for matching the beam:

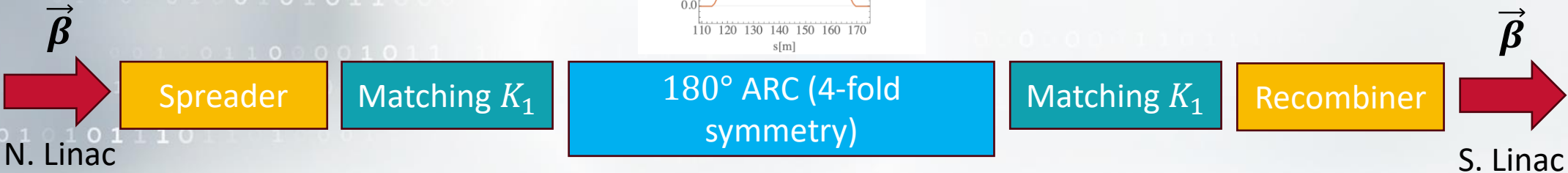
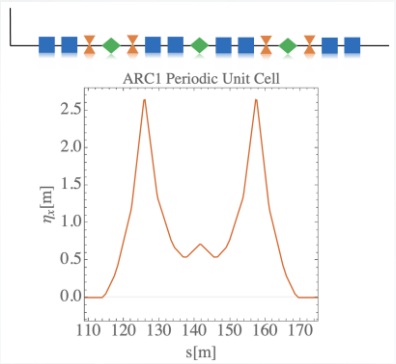
- From Linac to Arc periodic optics.
- From Arc periodic optics to Linac.

- Constraints:

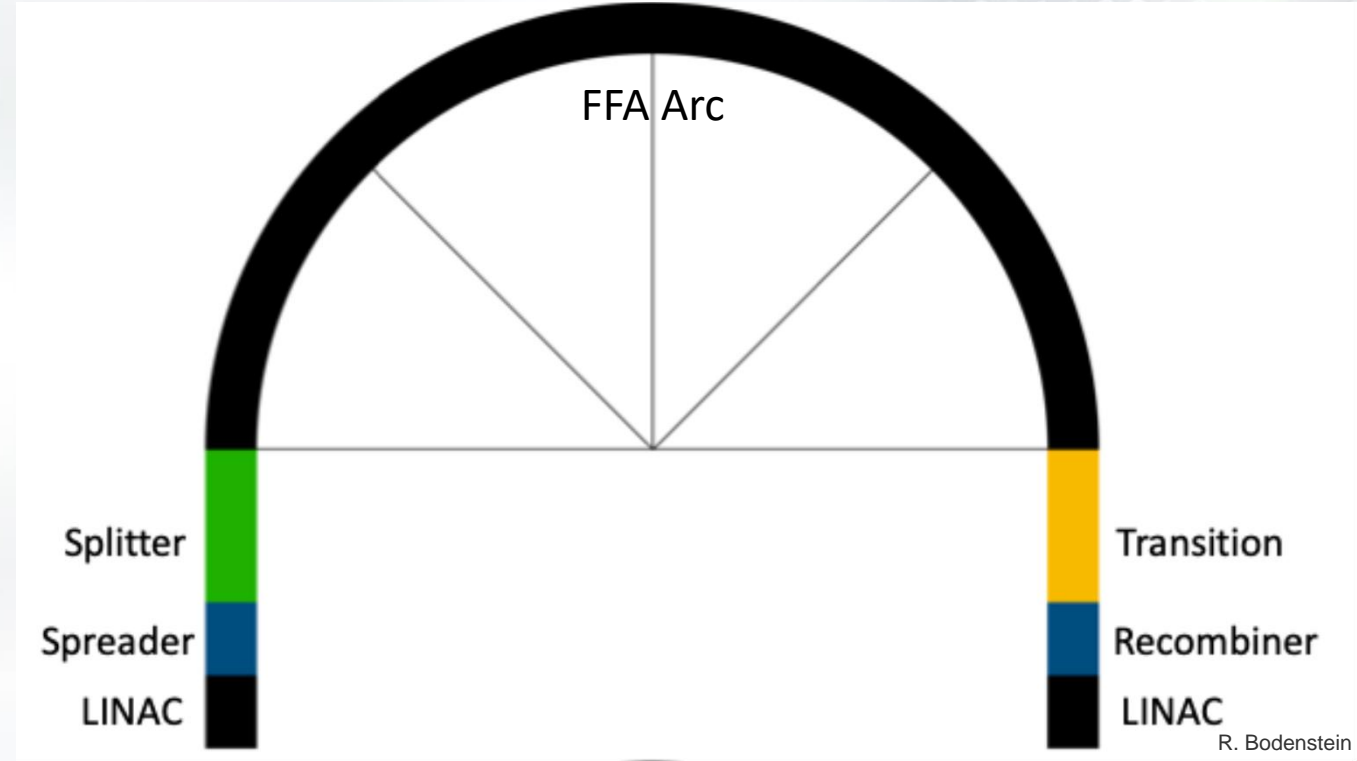
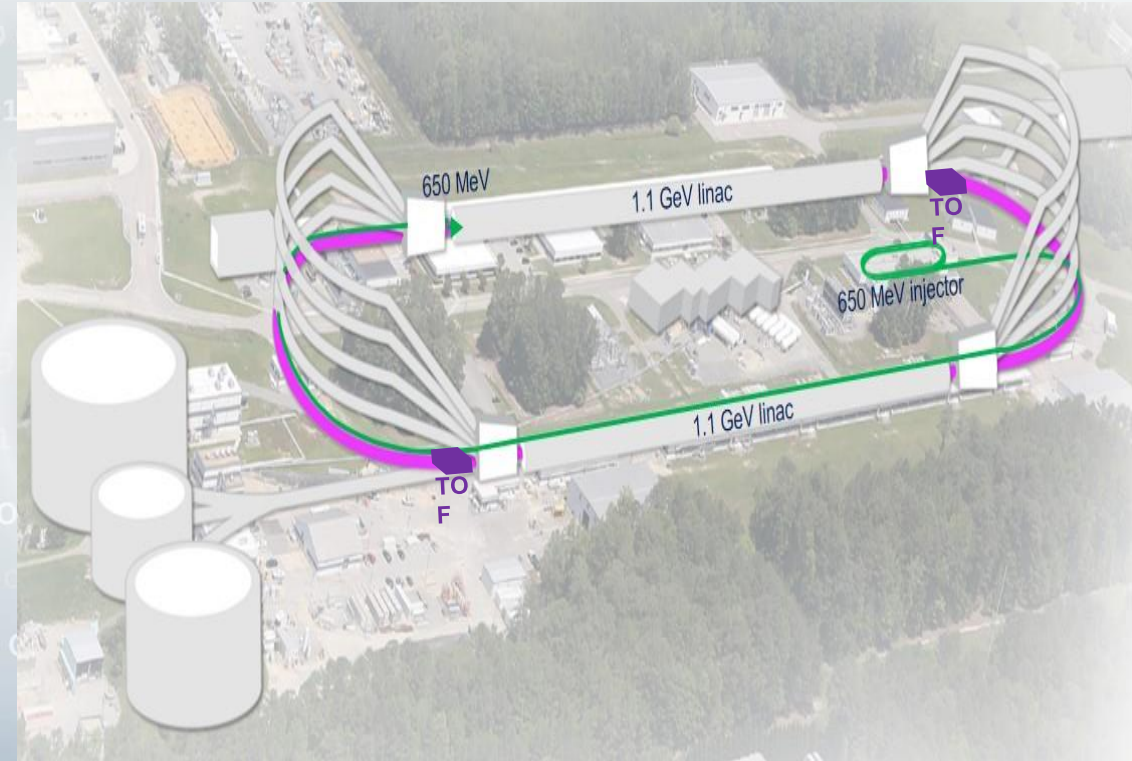
- Use existing footprint of arc.
- Spreader ( $R_{56} < 0$ ) + Recombiner ( $R_{56} < 0$ ) + Arcs beamline is isochronous ( $R_{56} = 0$ ).
- Arcs are composed of cells with 4-fold symmetry.



Linear optics matched from injector to start of FFA



# FFA Switchyard Components

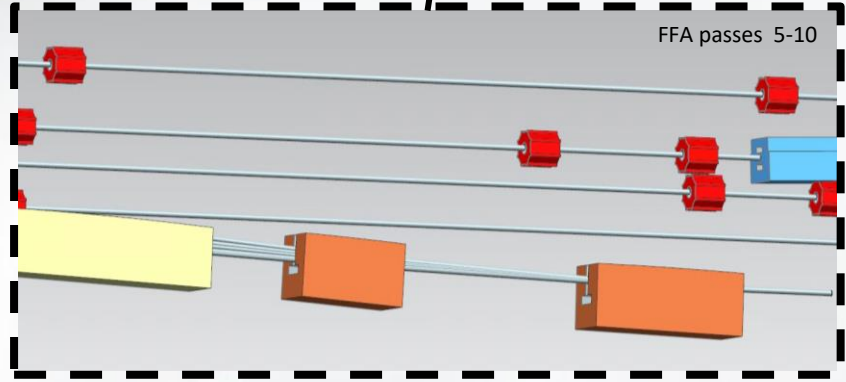
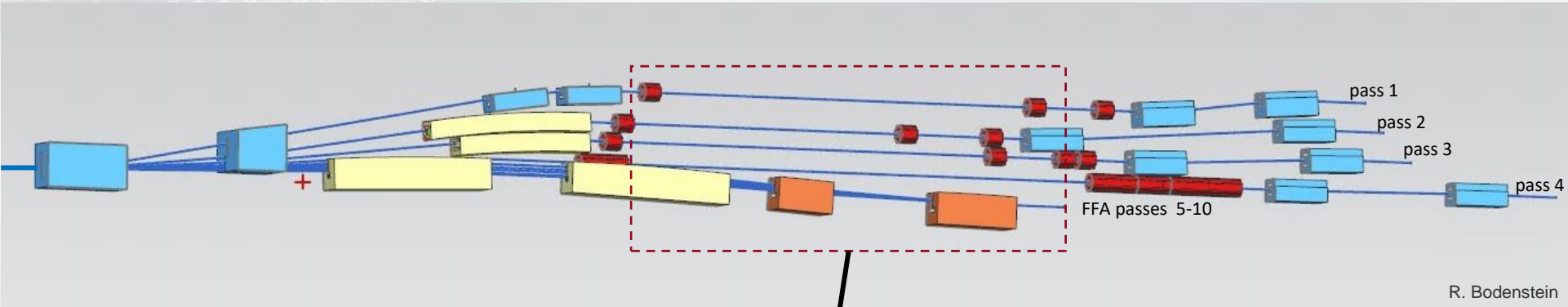


R. Bodenstein

1. **Spreader/Recombiner:** Vertical bend system transporting beam to FFA arc.
2. **Splitter:** Comprehensive matching section into FFA arc.
3. **Transition:** Matching section from FFA arc to linac.

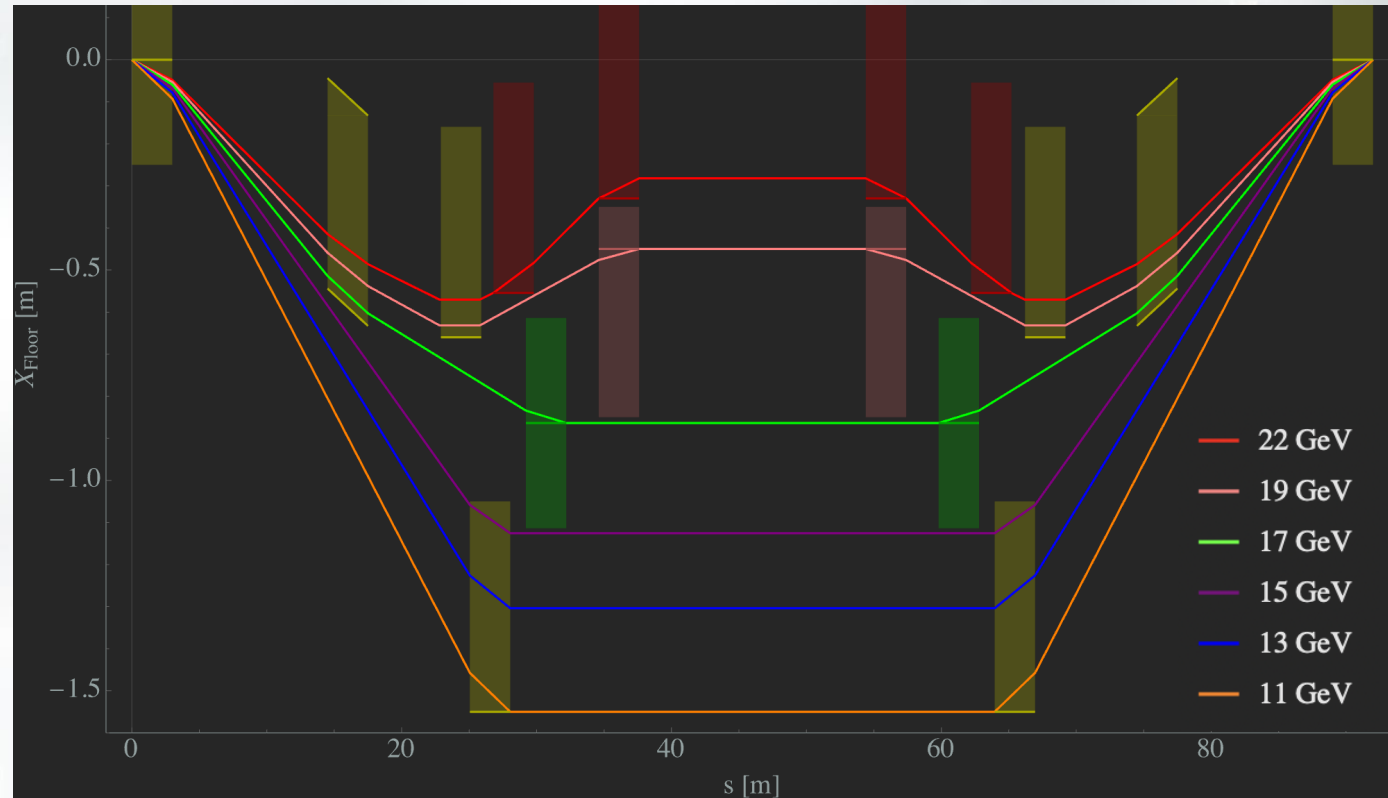
# 1. FFA Pass Spreader/Recombiner

- The vertical bend system (Spreader/Recombiner) that transports the beam to the FFA arc will need to be modified.
- The higher energy of the FFA passes will require larger/stronger dipole magnets to transport from linac-to-FFA.



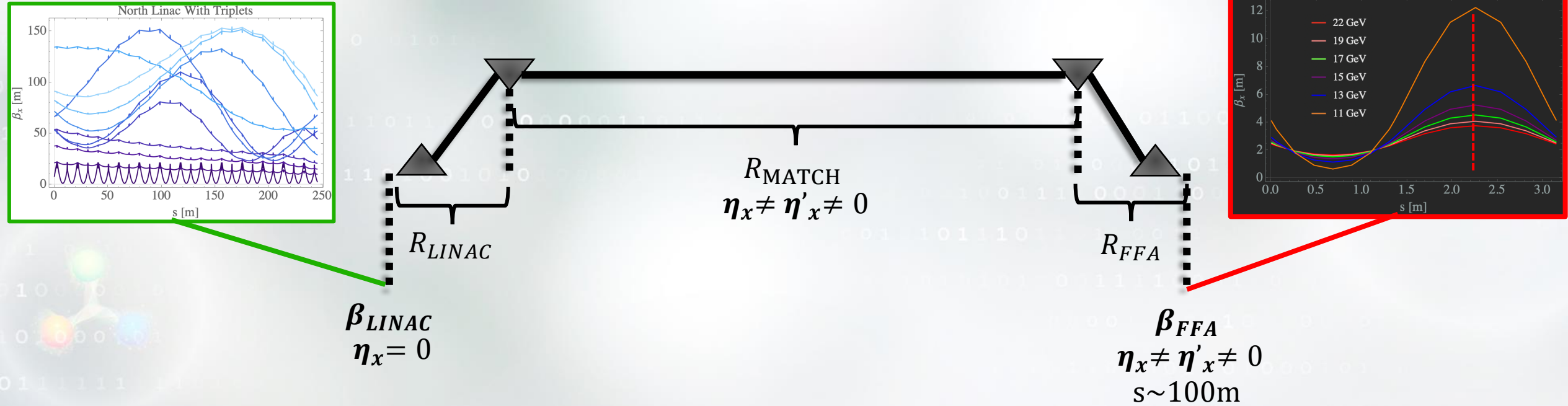
## 2. Splitter Section

- Required to match from the linac to the FFA for all 6 passes
- Heavy payload for matching:
  - Twiss parameters:  $\beta_{x,y}$ ,  $\alpha_{x,y}$
  - Dispersion:  $\eta_x, \eta'_x$
  - Momentum compaction:  $R_{56}$
  - Time of flight tuning for machine variability
- Current baseline “Symmetric” design
  - Matches all parameters
  - Working on optimizing betatron amplitudes; large linac optics to small FFA optics is a challenge
  - Global optimization of optics to control emittance dilution (i.e.  $\langle \mathcal{H} \rangle$ )



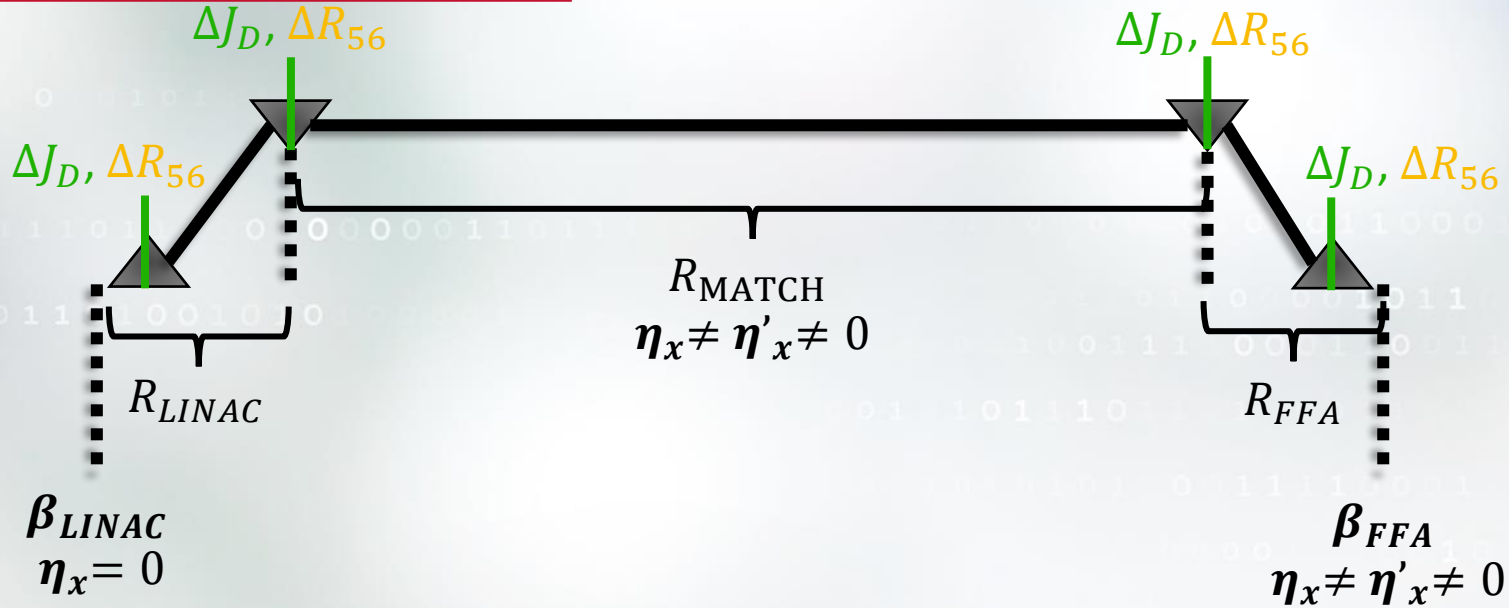
**Symmetric Splitter Design (quadrupoles not pictured)**

# 2. Splitter Design



- $R_{LINAC}$  and  $R_{FFA}$  roughly static (no space for the tuning quadrupoles) magnetic responsible for beam separation.
  - Optics on linac side ( $R_{LINAC}$ ) are nicely behaved.
  - Optics on FFA side ( $R_{FFA}$ ) resemble final focus optics behavior due to the small FFA matching optics.
- $R_{MATCH}$  will contain space to facilitate matching linac to FFA optics; space between different beamlines/passes require some interleaving of magnets.
- Difficulty lies in matching Twiss optics while tuning  $R_{56}$ .

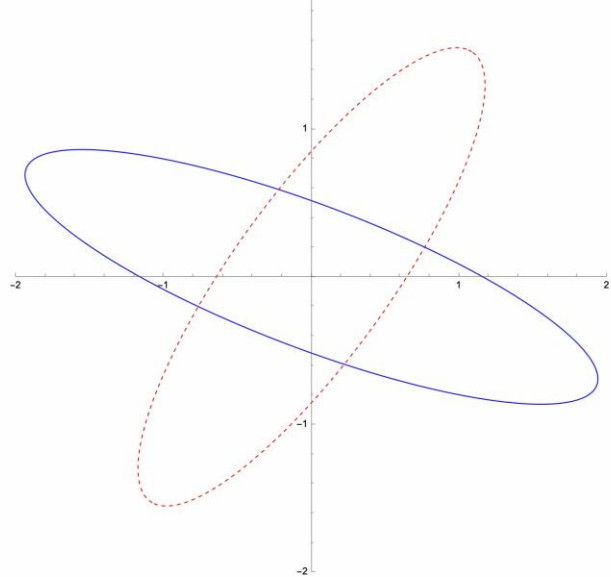
# 2. Splitter Design



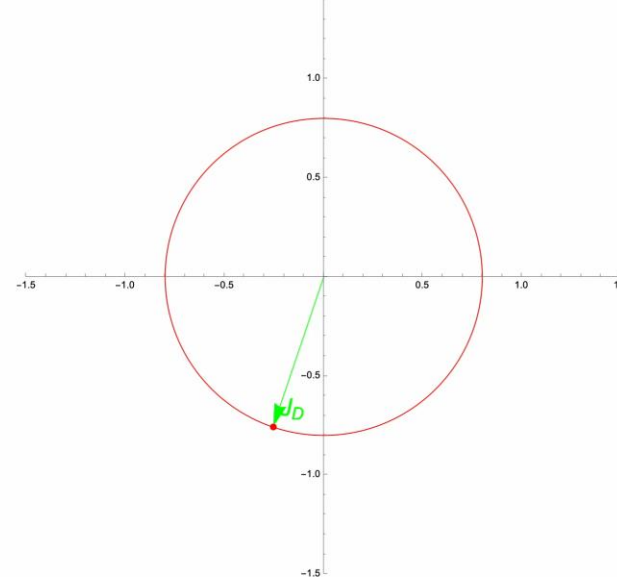
Beta/alpha matching

$$x'' + Kx = 0 \rightarrow \frac{\partial \epsilon}{\partial s} = 0$$

Transverse Phase Space



Normalized Dispersion Phase Space



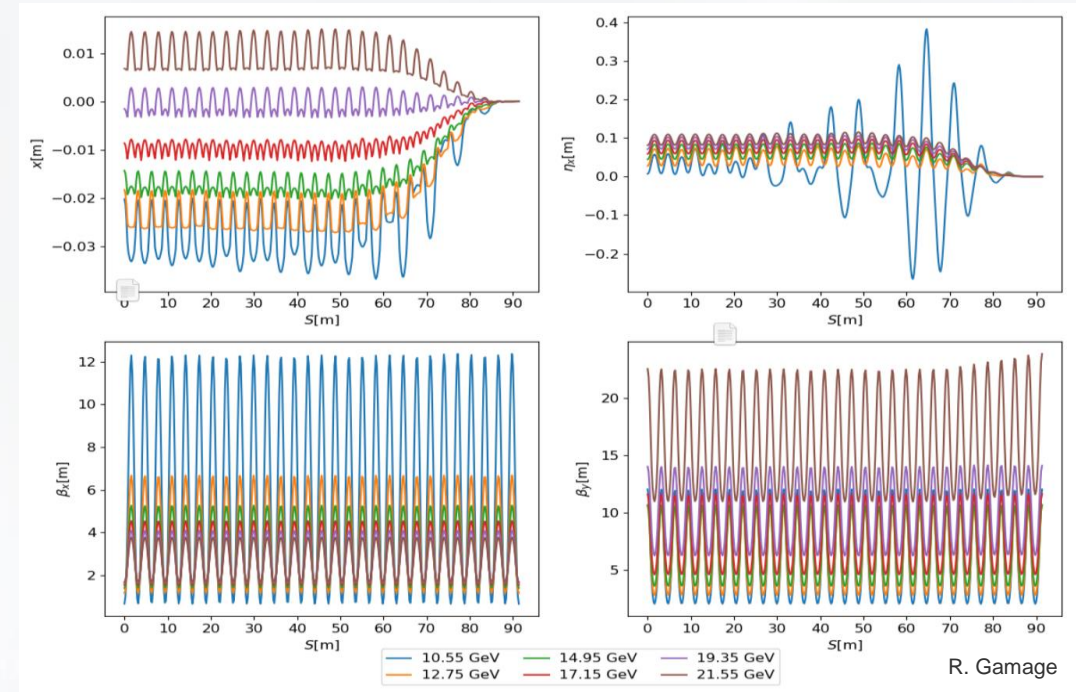
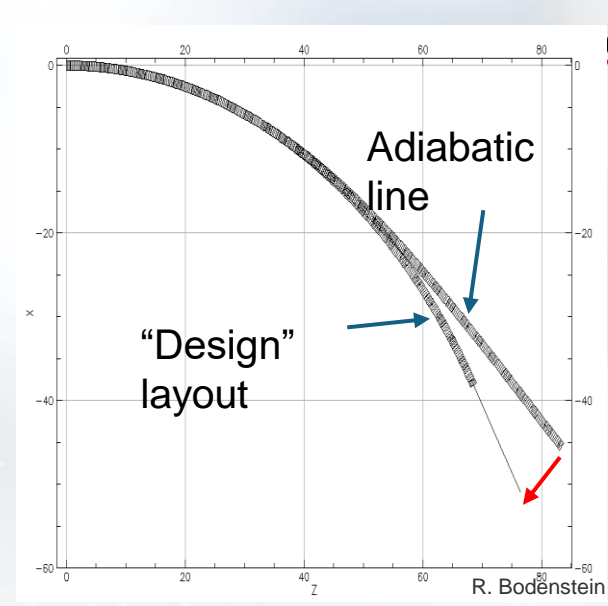
Dispersion/R56 matching

$$\eta'' + K\eta = \frac{1}{\rho} \rightarrow \frac{\partial J_D}{\partial s} \neq 0$$

$$R_{56} = \frac{\partial z}{\partial \delta} = \int \frac{\eta}{\rho} ds$$

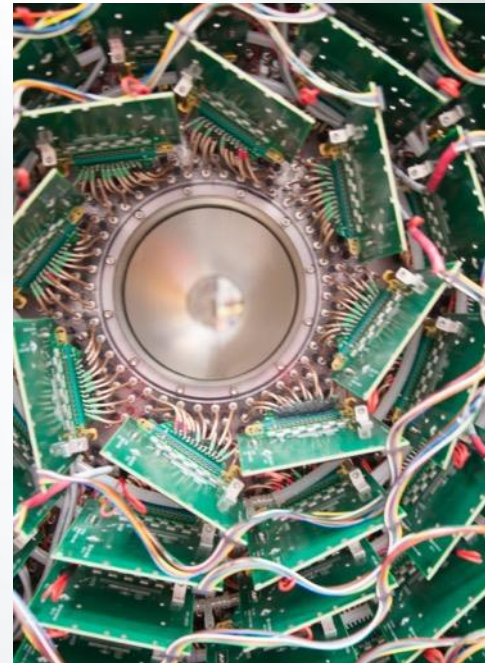
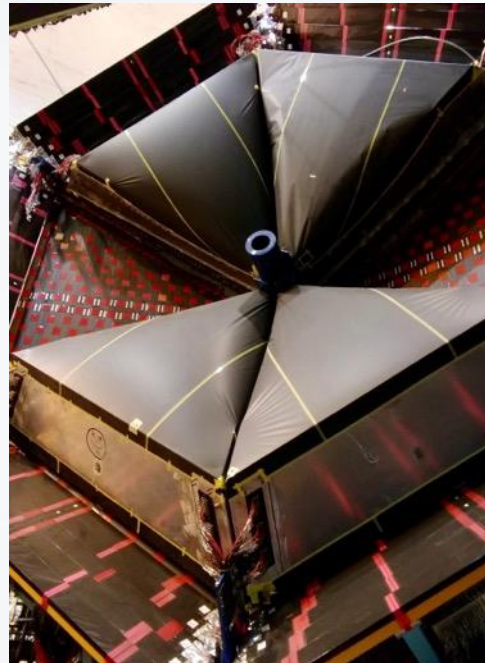
# 3. Transition Section

- In FFA transition, the different-energy passes must be matched simultaneously  $\Rightarrow$  Change in a single magnet parameter affects all passes  $\Rightarrow$  Challenging to find a solution
- Resonance-based systematic matching approach
  - Individual passes differ in their phase advance per cell
  - Make use of the phase advance difference to selectively control particular passes
  - Use resonance to selectively excite  $\beta$  functions of a particular pass
  - Focusing quadrupole kicks applied at twice the frequency of natural betatron oscillations



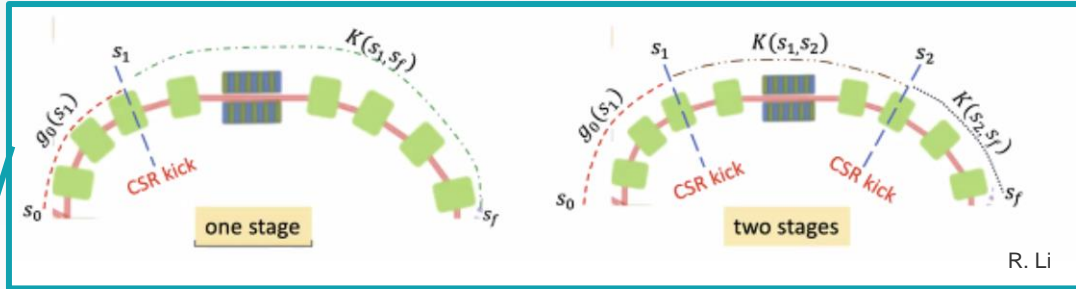
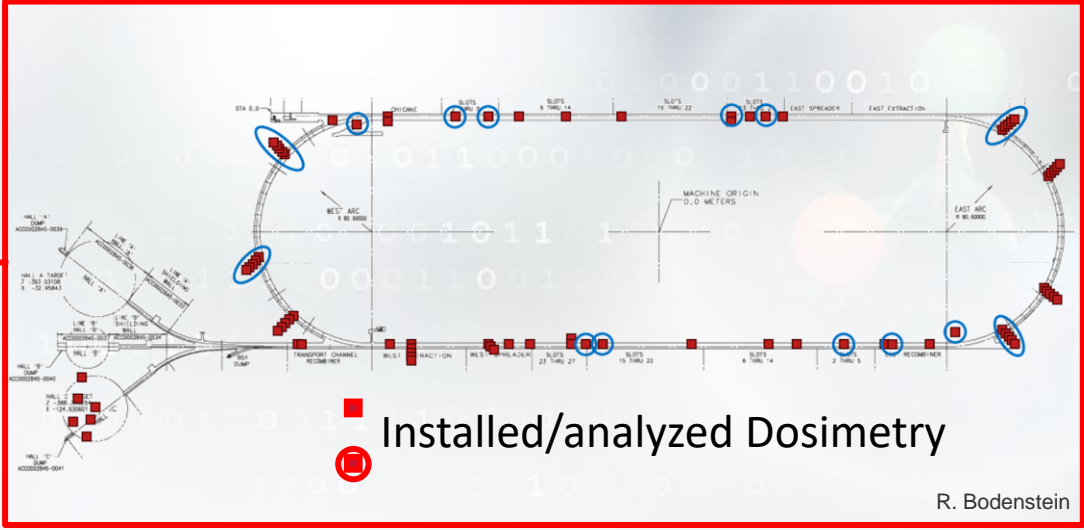
Arc-To-Linac transition section optics.

# Next Steps



# Future Work

- Study the effects of radiation on permanent magnets (JLAB funded LDRD)
  - Test the radiation resiliency of permanent magnets in this high energy environment
  - Test performed at JLAB could provide permanent magnet research to a wide range of applications: complex bend in light sources/rings etc.
- Integration of all beamline sections S2E simulation
  - Allows us to further validate the preconceptual design
  - Iterate and improve design strategies
  - Evaluate beam quality
- Optimization of current preliminary design and study of various effects:
  - Integrate new extraction paradigm
  - Beam break up (BBU)
  - Coherent synchrotron radiation induced emittance dilution in FFA arcs



Thank you