

Searches with non-LFV channels



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- Rare decays in charm
- Charm mixing and correlations
- B_s rare decays and mixing

1. Rare leptonic decays of charm

- These decays only proceed at one loop in the SM; GIM is very effective
 - SM rates are expected to be small

★ Rare decays $D \rightarrow M e^+ e^- / \mu^+ \mu^-$ and $D \rightarrow e^+ e^- / \mu^+ \mu^-$ are mediated by $c \rightarrow u$ II

$$\mathcal{L}_{\text{eff}}^{\text{SD}} = \frac{G_F}{\sqrt{2}} V_{cb}^* V_{ub} \sum_{i=7,9,10} C_i Q_i$$

$$Q_9 = \frac{e^2}{16\pi^2} \bar{u}_L \gamma_\mu c_L \bar{\ell} \gamma^\mu \ell, \quad Q_{10} = \frac{e^2}{16\pi^2} \bar{u}_L \gamma_\mu c_L \bar{\ell} \gamma^\mu \gamma_5 \ell,$$

- SM contribution is dominated by LD effects
- could be used to study NP effects

Burdman, Golowich, Hewett, Pakvasa;
Fajfer, Prelovsek, Singer

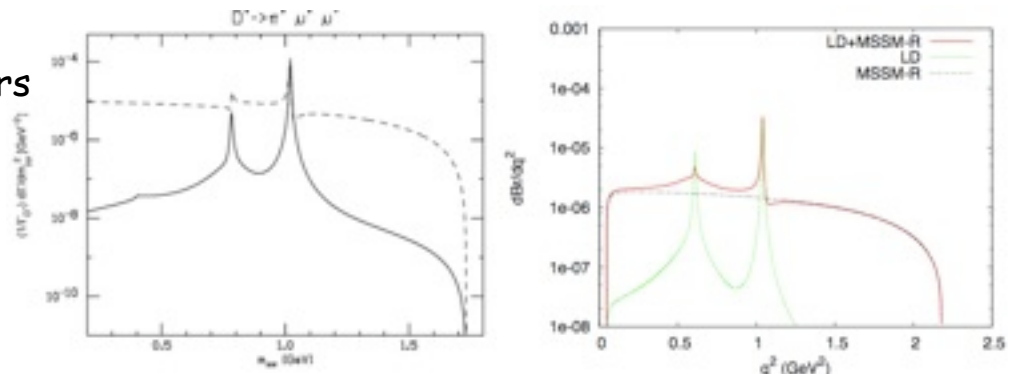
Mode	LD	Extra heavy q	LD + extra heavy q
$D^+ \rightarrow \pi^+ e^+ e^-$	2.0×10^{-6}	1.3×10^{-9}	2.0×10^{-6}
$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	2.0×10^{-6}	1.6×10^{-9}	2.0×10^{-6}
Mode	MSSM \cancel{R}	LD + MSSM \cancel{R}	
$D^+ \rightarrow \pi^+ e^+ e^-$	2.1×10^{-7}	2.3×10^{-6}	
$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	6.5×10^{-6}	8.8×10^{-6}	

★ Example: R-parity-violating SUSY

- operators with the same parameters contribute to D-mixing
- feed results into rare decays

★ Easiest: $D \rightarrow e^+ e^- / \mu^+ \mu^-$

Fajfer, Kosnik, Prelovsek



Standard Model contribution to $D \rightarrow \mu^+ \mu^-$

★ Short distance analysis

$$Q_{10} = \frac{e^2}{16\pi^2} \bar{u}_L \gamma_\mu c_L \bar{\ell} \gamma^\mu \gamma_5 \ell,$$

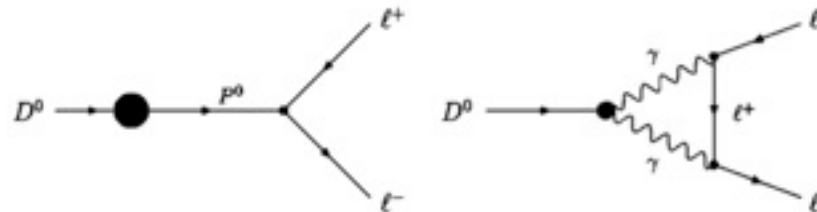
$$B_{D^0 \ell^+ \ell^-}^{(s.d.)} \simeq \frac{G_F^2 M_W^2 f_D m_\ell}{\pi^2} F,$$

$$F = \sum_{i=d,s,b} V_{ui} V_{ci}^* \left[\frac{x_i}{2} + \frac{\alpha_s}{4\pi} x_i \cdot \left(\ln^2 x_i + \frac{4 + \pi^2}{3} \right) \right]$$

- only Q_{10} contribute, SD effects amount to $\text{Br} \sim 10^{-18}$
- single non-perturbative parameter (decay constant)

UKQCD, HPQCD; Jamin, Lange;
Penin, Steinhauser; Khodjamirian

★ Long distance analysis



Burdman, Golowich, Hewett, Pakvasa;
Fajfer, Prelovsek, Singer

$$B_{D^0 \ell^+ \ell^-}^{(\text{mix})} = \sum_{P_n} \langle P_n | \mathcal{H}_{wk}^{(p.c.)} | D^0 \rangle \frac{1}{M_D^2 - M_{P_n}^2} B_{P_n \ell^+ \ell^-}$$

$$\text{Im } \mathcal{M}_{D^0 \rightarrow \ell^+ \ell^-} = \frac{1}{2!} \sum_{\lambda_1, \lambda_2} \int \frac{d^3 q_1}{2\omega_1 (2\pi)^3} \frac{d^3 q_2}{2\omega_2 (2\pi)^3} \times \mathcal{M}_{D \rightarrow \gamma\gamma} \mathcal{M}_{\gamma\gamma \rightarrow \ell^+ \ell^-}^* (2\pi)^4 \delta^{(4)}(p - q_1 - q_2)$$

- LD effects amount to $\text{Br} \sim 10^{-13}$
- could be used to study NP effects in correlation with D-mixing

Standard Model contribution to $D \rightarrow \mu^+ \mu^-$

★ Short distance analysis

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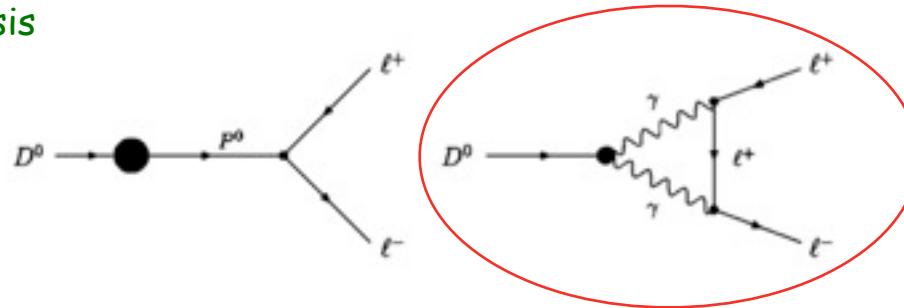
$$B_{D^0 \ell^+ \ell^-}^{(s.d.)} \simeq \frac{G_F^2 M_W^2 f_D m_\ell}{\pi^2} F,$$

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$$\text{Im } \mathcal{M}_{D^0 \rightarrow \ell^+ \ell^-} = \frac{1}{2!} \sum_{\lambda_1, \lambda_2} \int \frac{d^3 q_1}{2\omega_1 (2\pi)^3} \frac{d^3 q_2}{2\omega_2 (2\pi)^3} \times \mathcal{M}_{D \rightarrow \gamma\gamma} \mathcal{M}_{\gamma\gamma \rightarrow \ell^+ \ell^-}^* (2\pi)^4 \delta^{(4)}(p - q_1 - q_2)$$

- LD effects amount to $\text{Br} \sim 10^{-13}$
- could be used to study **NP effects in correlation with D-mixing**

What about D-mixing?

E.Golowich, J. Hewett, S. Pakvasa and A.A.P.
Phys. Rev. D76:095009, 2007

★ Let's write the most general $\Delta C=2$ Hamiltonian

$$\mathcal{H}_{NP}^{\Delta C=2} = \frac{1}{\Lambda_{NP}^2} \sum_{i=1}^8 C_i(\mu) Q_i$$

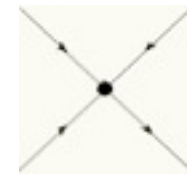
... with the following set of 8 independent operators...

$$Q_1 = (\bar{u}_L \gamma_\mu c_L) (\bar{u}_L \gamma^\mu c_L), \quad Q_5 = (\bar{u}_R \sigma_{\mu\nu} c_L) (\bar{u}_R \sigma^{\mu\nu} c_L),$$

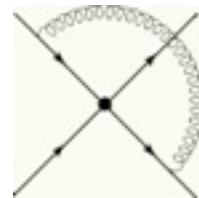
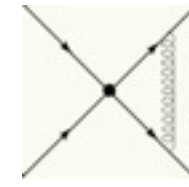
$$Q_2 = (\bar{u}_L \gamma_\mu c_L) (\bar{u}_R \gamma^\mu c_R), \quad Q_6 = (\bar{u}_R \gamma_\mu c_R) (\bar{u}_R \gamma^\mu c_R),$$

$$Q_3 = (\bar{u}_L c_R) (\bar{u}_R c_L), \quad Q_7 = (\bar{u}_L c_R) (\bar{u}_L c_R),$$

$$Q_4 = (\bar{u}_R c_L) (\bar{u}_R c_L), \quad Q_8 = (\bar{u}_L \sigma_{\mu\nu} c_R) (\bar{u}_L \sigma^{\mu\nu} c_R).$$



$\mu \leq 1 \text{ TeV}$



$\mu : 1 \text{ GeV}$

RG-running relate $C_i(m)$ at NP scale to the scale of $m \sim 1 \text{ GeV}$, where ME are computed (on the lattice)

$$\frac{d}{d \log \mu} \vec{C}(\mu) = \hat{\gamma}^T(\mu) \vec{C}(\mu)$$

Each model of New Physics
provides unique matching
condition for $C_i(\Lambda_{NP})$

Generic restrictions on NP

★ Comparing to experimental value of x , obtain constraints on NP models

- assume x is dominated by the New Physics model
- assume no accidental strong cancellations b/w SM and NP

$$\mathcal{H}_{NP}^{\Delta C=2} = \frac{1}{\Lambda_{NP}^2} \sum_{i=1}^8 z_i(\mu) Q'_i$$

$$\begin{aligned} Q_1^{cu} &= \bar{u}_L^\alpha \gamma_\mu c_L^\alpha \bar{u}_L^\beta \gamma^\mu c_L^\beta, \\ Q_2^{cu} &= \bar{u}_R^\alpha c_L^\alpha \bar{u}_R^\beta c_L^\beta, \\ Q_3^{cu} &= \bar{u}_R^\alpha c_L^\beta \bar{u}_R^\beta c_L^\alpha, \end{aligned} + \left\{ \begin{array}{c} L \\ \updownarrow \\ R \end{array} \right\} + \begin{aligned} Q_4^{cu} &= \bar{u}_R^\alpha c_L^\alpha \bar{u}_L^\beta c_R^\beta, \\ Q_5^{cu} &= \bar{u}_R^\alpha c_L^\beta \bar{u}_L^\beta c_R^\alpha, \end{aligned}$$

★ ... which are

$$\begin{aligned} |z_1| &\lesssim 5.7 \times 10^{-7} \left(\frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_2| &\lesssim 1.6 \times 10^{-7} \left(\frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_3| &\lesssim 5.8 \times 10^{-7} \left(\frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_4| &\lesssim 5.6 \times 10^{-8} \left(\frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_5| &\lesssim 1.6 \times 10^{-7} \left(\frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2. \end{aligned}$$

New Physics is either at a very high scales

tree level: $\Lambda_{NP} \geq (4 - 10) \times 10^3 \text{ TeV}$

loop level: $\Lambda_{NP} \geq (1 - 3) \times 10^2 \text{ TeV}$

or have highly suppressed couplings to charm!

★ Constraints on particular NP models available

Gedalia, Grossman, Nir, Perez
arXiv:0906.1879 [hep-ph]

E. Golowich, J. Hewett, S. Pakvasa and A.A.P.
Phys. Rev. D76:095009, 2007

Example of a model of New Physics

★ Consider an example: FCNC Z^0 -boson

appears in models with
extra vector-like quarks
little Higgs models

1. Integrate out Z : for $\mu < M_Z$ get

$$\mathcal{H}_{2/3} = \frac{g^2}{8 \cos^2 \theta_w M_Z^2} (\lambda_{uc})^2 \bar{u}_L \gamma_\mu c_L \bar{u}_L \gamma^\mu c_L$$

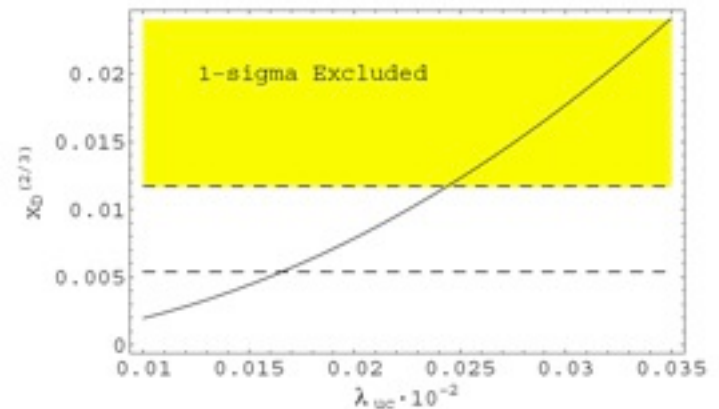
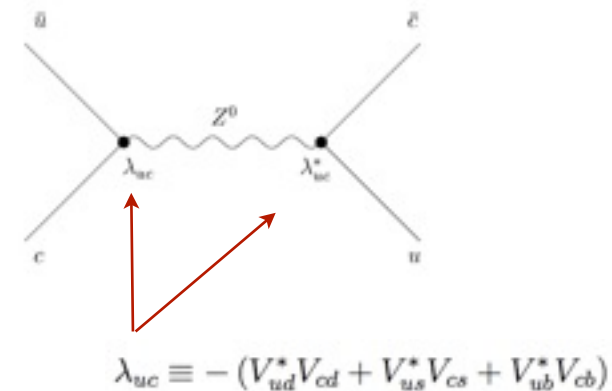
2. Perform RG running to $\mu \sim m_c$ (in general: operator mixing)

$$\mathcal{H}_{2/3} = \frac{g^2}{8 \cos^2 \theta_w M_Z^2} (\lambda_{uc})^2 r_1(m_c, M_Z) Q_1$$

3. Compute relevant matrix elements and x_D

$$x_D^{(2/3)} = \frac{2G_F f_D^2 M_D}{3\sqrt{2}\Gamma_D} B_D (\lambda_{uc})^2 r_1(m_c, M_Z)$$

4. Assume no SM - get an upper bound on NP model parameters/correlate with rare decays!



Generic NP contribution to $D \rightarrow \mu^+ \mu^-$

★ Most general effective Hamiltonian:

$$\begin{aligned} \langle f | \mathcal{H}_{NP} | i \rangle &= G \sum_{i=1}^{\infty} \tilde{C}_i(\mu) \langle f | Q_i | i \rangle(\mu) \\ \tilde{Q}_1 &= (\bar{\ell}_L \gamma_\mu \ell_L) (\bar{u}_L \gamma^\mu c_L), & \tilde{Q}_4 &= (\bar{\ell}_R \ell_L) (\bar{u}_R c_L), \\ \tilde{Q}_2 &= (\bar{\ell}_L \gamma_\mu \ell_L) (\bar{u}_R \gamma^\mu c_R), & \tilde{Q}_5 &= (\bar{\ell}_R \sigma_{\mu\nu} \ell_L) (\bar{u}_R \sigma^{\mu\nu} c_L), \\ \tilde{Q}_3 &= (\bar{\ell}_L \ell_R) (\bar{u}_R c_L), & & \text{plus } L \leftrightarrow R \end{aligned}$$

★ ... thus, the amplitude for $D \rightarrow e^+ e^- / \mu^+ \mu^-$ decay is

$$\begin{aligned} \mathcal{B}_{D^0 \rightarrow \ell^+ \ell^-} &= \frac{M_D}{8\pi\Gamma_D} \sqrt{1 - \frac{4m_\ell^2}{M_D^2}} \left[\left(1 - \frac{4m_\ell^2}{M_D^2}\right) |A|^2 + |B|^2 \right], \\ \mathcal{B}_{D^0 \rightarrow \mu^+ e^-} &= \frac{M_D}{8\pi\Gamma_D} \left(1 - \frac{m_\mu^2}{M_D^2}\right)^2 [|A|^2 + |B|^2], \\ |A| &= G \frac{f_D M_D^2}{4m_c} [\tilde{C}_{3-8} + \tilde{C}_{4-9}], \\ |B| &= G \frac{f_D}{4} \left[2m_\ell (\tilde{C}_{1-2} + \tilde{C}_{6-7}) + \frac{M_D^2}{m_c} (\tilde{C}_{4-3} + \tilde{C}_{9-8}) \right], \quad \tilde{C}_{i-k} \equiv \tilde{C}_i - \tilde{C}_k \end{aligned}$$

Many NP models give contributions to both D-mixing and $D \rightarrow e^+ e^- / \mu^+ \mu^-$ decay: **correlate!!!**

Mixing vs rare decays: a particular model

★ Recent experimental constraints

$$\mathcal{B}_{D^0 \rightarrow \mu^+ \mu^-} \leq 1.3 \times 10^{-6}, \quad \mathcal{B}_{D^0 \rightarrow e^+ e^-} \leq 1.2 \times 10^{-6},$$

$$\mathcal{B}_{D^0 \rightarrow \mu^\pm e^\mp} \leq 8.1 \times 10^{-7},$$

E. Golowich, J. Hewett, S. Pakvasa and A.A.P.
PRD79, 114030 (2009)

★ Relating mixing and rare decay

- consider an example: heavy vector-like quark ($Q=+2/3$)
- appears in little Higgs models, etc.

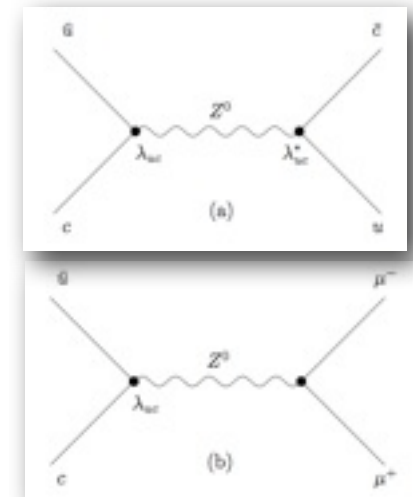
Mixing:

$$\mathcal{H}_{2/3} = \frac{g^2}{8 \cos^2 \theta_w M_Z^2} \lambda_{uc}^2 Q_1 = \frac{G_F \lambda_{uc}^2}{\sqrt{2}} Q_1$$

$$x_D^{(+2/3)} = \frac{2 G_F \lambda_{uc}^2 f_D^2 M_D B_D r(m_c, M_Z)}{3 \sqrt{2} \Gamma_D}$$

Rare decay:

$$A_{D^0 \rightarrow \ell^+ \ell^-} = 0 \quad B_{D^0 \rightarrow \ell^+ \ell^-} = \lambda_{uc} \frac{G_F f_D m_\mu}{2}$$



$$\mathcal{B}_{D^0 \rightarrow \mu^+ \mu^-} = \frac{3\sqrt{2}}{64\pi} \frac{G_F m_\mu^2 x_D}{B_D r(m_c, M_Z)} \left[1 - \frac{4m_\mu^2}{M_D} \right]^{1/2}$$

$$\simeq 4.3 \times 10^{-9} x_D \leq 4.3 \times 10^{-11}.$$



Note: a NP parameter-free relation!

Mixing vs rare decays

★ Correlation between mixing/rare decays

- possible for tree-level NP amplitudes

E. Golowich, J. Hewett, S. Pakvasa and A.A.P.
PRD79, 114030 (2009)

Spin-1 intermediate boson: $\mathcal{H}_V = \mathcal{H}_V^{\text{FCNC}} + \mathcal{H}_V^L$

$$\mathcal{H}_V^{\text{FCNC}} = g_{V1} \bar{u}_L \gamma_\mu c_L V^\mu + g_{V2} \bar{u}_R \gamma_\mu c_R V^\mu + g_{V3} \bar{u}_L \sigma_{\mu\nu} c_R V^{\mu\nu} + g_{V4} \bar{u}_R \sigma_{\mu\nu} c_L V^{\mu\nu} \quad \left| \quad \mathcal{H}_V^L = g'_{V1} \bar{\ell}_L \gamma_\mu \ell_L V^\mu + g'_{V2} \bar{\ell}_R \gamma_\mu \ell_R V^\mu + g'_{V3} \bar{\ell}_L \sigma_{\mu\nu} \ell_R V^{\mu\nu} + g'_{V4} \bar{\ell}_R \sigma_{\mu\nu} \ell_L V^{\mu\nu} \right.$$

Mixing: $x_D^{(V)} = \frac{f_D^2 M_D B_D}{2M_V^2 \Gamma_D} \left[\frac{2}{3} (C_1(m_c) + C_6(m_c)) - \left[\frac{1}{2} + \frac{\eta}{3} \right] C_2(m_c) + \left[\frac{1}{12} + \frac{\eta}{2} \right] C_3(m_c) \right],$

$$C_1(m_c) = r(m_c, M_V) g_{V1}^2,$$

$$C_2(m_c) = 2r(m_c, M_V)^{1/2} g_{V1} g_{V2},$$

$$C_3(m_c) = \frac{4}{3} [r(m_c, M_V)^{1/2} - r(m_c, M_V)^{-4}] g_{V1} g_{V2},$$

$$C_6(m_c) = r(m_c, M_V) g_{V2}^2.$$

Rare decay: $\mathcal{B}_{D^0 \rightarrow \ell^+ \ell^-}^{(V)} = \frac{f_D^2 m_\ell^2 M_D}{32 \pi M_V^4 \Gamma_D} \sqrt{1 - \frac{4m_\ell^2}{M_D^2}} \times (g_{V1} - g_{V2})^2 (g'_{V1} - g'_{V2})^2.$

NO contribution from vectors
(vector current conservation)

Mixing vs rare decays

★ Correlation between mixing/rare decays

- possible for tree-level NP amplitudes

E. Golowich, J. Hewett, S. Pakvasa and A.A.P.
PRD79, 114030 (2009)

Spin-0 intermediate boson: $\mathcal{H}_S = \mathcal{H}_S^{\text{FCNC}} + \mathcal{H}_S^L$,

$$\mathcal{H}_S^{\text{FCNC}} = g_{S1} \bar{u}_L c_R S + g_{S2} \bar{u}_R c_L S + g_{S3} \bar{u}_L \gamma_\mu c_L \partial^\mu S + g_{S4} \bar{u}_R \gamma_\mu c_R \partial^\mu S$$

$$\mathcal{H}_S^L = g'_{S1} \bar{\ell}_L \ell_R S + g'_{S2} \bar{\ell}_R \ell_L S + g'_{S3} \bar{\ell}_L \gamma_\mu \ell_L \partial^\mu S + g'_{S4} \bar{\ell}_R \gamma_\mu \ell_R \partial^\mu S.$$

Mixing:

$$x_D^{(S)} = -\frac{f_D^2 M_D B_D}{2\Gamma_D M_S^2} \left[\left[\frac{1}{12} + \frac{\eta}{2} \right] C_3(m_c) - \frac{5\eta}{12} (C_4(m_c) + C_7(m_c)) + \eta (C_5(m_c) + C_8(m_c)) \right],$$

Rare decay:

$$\mathcal{B}_{D^0 \rightarrow \ell^+ \ell^-}^{(S)} = \frac{f_D^2 M_D^5}{128 \pi m_c^2 M_S^4 \Gamma_D} \sqrt{1 - \frac{4m_\ell^2}{M_D^2}} (g_{S1} - g_{S2})^2 \times \left[(g'_{S1} + g'_{S2})^2 \left(1 - \frac{4m_\ell^2}{M_D^2} \right) + (g'_{S1} - g'_{S2})^2 \right].$$

NO contribution from scalars

Mixing vs rare decays

★ Correlation between mixing/rare decays

- possible for tree-level NP amplitudes
- some relations possible for loop-dominated transitions

E.Golowich, J. Hewett, S. Pakvasa and A.A.P.
PRD79, 114030 (2009)

★ Consider several popular models

Model	$\mathcal{B}_{D^0 \rightarrow \mu^+ \mu^-}$
Standard Model (SD)	$\sim 10^{-18}$
Standard Model (LD)	$\sim \text{several} \times 10^{-13}$
$Q = +2/3$ Vectorlike Singlet	4.3×10^{-11}
$Q = -1/3$ Vectorlike Singlet	$1 \times 10^{-11} (m_S/500 \text{ GeV})^2$
$Q = -1/3$ Fourth Family	$1 \times 10^{-11} (m_S/500 \text{ GeV})^2$
Z' Standard Model (LD)	$2.4 \times 10^{-12} / (M_{Z'}(\text{TeV}))^2$
Family Symmetry	$0.7 \times 10^{-18} \text{ (Case A)}$
RPV-SUSY	$1.7 \times 10^{-9} (500 \text{ GeV} / m_{\tilde{d}_k})^2$

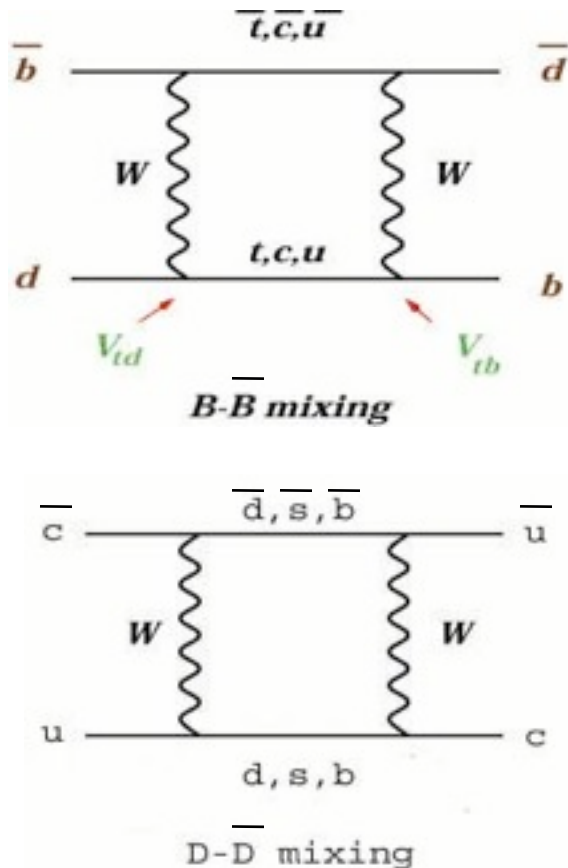
Obtained upper limits on rare decay branching ratios.

Can we apply the same idea where better data exists?

Same idea can be employed to relate D-mixing to K-mixing

Blum, Grossman, Nir, Perez
arXiv:0903.2118 [hep-ph]

2. D^0 -mixing vs B_s -mixing



$\overline{D^0} - D^0$ mixing	$\overline{B^0} - B^0$ mixing
<ul style="list-style-type: none"> intermediate down-type quarks SM: b-quark contribution is negligible due to $V_{cd}V_{ub}^*$ $rate \propto f(m_s) - f(m_d)$ (zero in the SU(3) limit) <p>Falk, Grossman, Ligeti, and A.A.P. Phys.Rev. D65, 054034, 2002 2nd order effect!!!</p>	<ul style="list-style-type: none"> intermediate up-type quarks SM: t-quark contribution is dominant $rate \propto m_t^2$ (expected to be large)
<ol style="list-style-type: none"> Sensitive to long distance QCD Small in the SM: New Physics! (must know SM x and y) 	<ol style="list-style-type: none"> Computable in QCD (*) Large in the SM: CKM!

(*) up to matrix elements of 4-quark operators

Available experimental data for B_s

➤ LHCb will probe $B_s \rightarrow \mu^+\mu^-$ at the SM level within a year

★ B_s mixing data:

$$\Delta M_{B_s}^{(\text{expt})} = (117.0 \pm 0.8) \times 10^{-13} \text{ GeV},$$

PDG

E. Golowich, J. Hewett, S. Pakvasa, A.A.P. and G. Yeghian PRD83, 114017 (2011)

$$\Delta M_{B_s}^{(\text{SM})} = \frac{(G_F M_W |V_{ts}^* V_{tb}|)^2}{6\pi^2} M_{B_s} f_{B_s}^2 \hat{B}_{B_s} \eta_{B_s} S_0(\bar{x}_t) = (125.2_{-12.7}^{+13.8}) \times 10^{-13} \text{ GeV}$$

Nierste,
Lenz;
Buras

$\alpha_s(M_Z) = 0.1184 \pm 0.0007$ [6]	$ V_{ts} = 0.0403_{-0.0007}^{+0.0011}$ [7]
$\Delta M_{B_s} = (117.0 \pm 0.8) \times 10^{-13} \text{ GeV}$ [7]	$\Delta\Gamma_{B_s}/\Gamma_{B_s} = 0.092_{-0.054}^{+0.051}$ [7]
$\bar{m}_t(\bar{m}_t) = (163.4 \pm 1.2) \text{ GeV}$ [8]	$f_{B_s} \sqrt{\hat{B}_{B_s}} = 275 \pm 13 \text{ MeV}$ [9]
$\hat{B}_{B_s} = 1.33 \pm 0.06$ [9]	$f_{B_s} = 0.2388 \pm 0.0095 \text{ GeV}$ [9]

★ Rare decays

$$\begin{aligned} Br_{B_s \rightarrow \mu^+\mu^-}^{(\text{PDG})} &< 47 \times 10^{-9} \quad (\text{CL} = 90\%); & Br_{B_s \rightarrow \mu^+\mu^-}^{(\text{CDF})} &= (18_{-9}^{+11}) \times 10^{-9} \\ Br_{B_s \rightarrow \mu^+\mu^-}^{(\text{LHC})} &< 9 \times 10^{-9} \quad (\text{CL} = 90\%); & Br_{B_s \rightarrow \mu^+\mu^-}^{(\text{LHC})} &< 11 \times 10^{-9} \quad (\text{CL} = 95\%) \end{aligned}$$

$$Br_{B_s \rightarrow \mu^+\mu^-}^{(\text{SM})} = \frac{1}{8\pi^5} \cdot \frac{M_{B_s}}{\Gamma_{B_s}} \cdot (G_F^2 M_W^2 m_\mu f_{B_s} |V_{ts}^* V_{tb}| \eta_Y Y(\bar{x}_t))^2 \left[1 - 4 \frac{m_\mu^2}{M_{B_s}^2} \right]^{1/2}$$

$$Br_{B_s \rightarrow \mu^+\mu^-}^{(\text{SM})} = \frac{3}{4\pi^3} \cdot \frac{\Delta M_{B_s}^{(\text{Expt})}}{\Gamma_{B_s}} \cdot \frac{(G_F M_W m_\mu \eta_Y Y)^2}{\hat{\eta} \hat{B}_{B_s} S_0(\bar{x}_t)} \left[1 - 4 \frac{m_\mu^2}{M_{B_s}^2} \right]^{1/2} = (3.3 \pm 0.2) \times 10^{-9}$$

Buras, Carlucci,
Gori, Isidori

New Physics in B_s -mixing

➤ Relate NP contributions in B_s mixing and rare decays

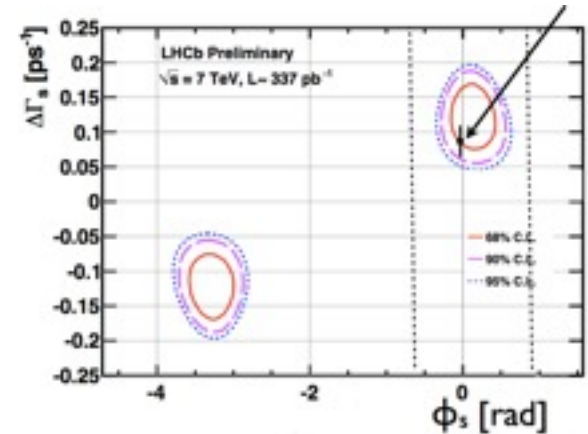
★ B_s mixing data:

$$\Delta M_{B_s} = \Delta M_{B_s}^{(\text{SM})} + \Delta M_{B_s}^{(\text{NP})} \cos \phi.$$

$$\Delta M_{B_s}^{(\text{Expt})} = \Delta M_{B_s}^{(\text{SM})} + \Delta M_{B_s}^{(\text{NP})}$$

$$\Delta M_{B_s}^{(\text{NP})} = (-20.9 \rightarrow +5.6) \times 10^{-13} \text{ GeV}$$

$$|\Delta M_{B_s}^{(\text{NP})}| \leq 20.9 \times 10^{-13} \text{ GeV}$$



SM

NP

This characterizes the size of NP "window" still possible in B_s -mixing.
This is what should be related to rare decays (same formulas...)

E. Golowich, J. Hewett, S. Pakvasa, A.A.P.,
and G. Yeghiyan PRD83, 114017 (2011)

Mixing vs rare decays: some models

➤ Consider RPV SUSY: $\mathcal{W}_R = \frac{1}{2}\lambda_{ijk}L_iL_jE_k^c + \lambda'_{ijk}L_iQ_jD_k^c + \frac{1}{2}\lambda''_{ijk}U_i^cD_j^cD_k^c$

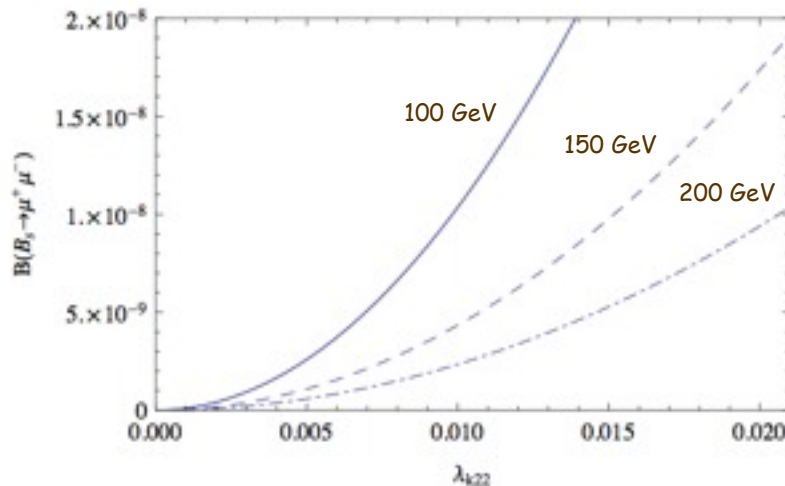
Mixing: $\mathcal{L}_R = -\lambda'_{i23}\tilde{\nu}_{iL}\bar{b}_R s_L - \lambda'_{i32}\tilde{\nu}_{iL}\bar{s}_R b_L + \text{H.c.},$

$$\Delta M_{B_s}^{(\mathcal{R})} = \frac{5}{24}f_{B_s}^2 M_{B_s} F(C_3, B_3) \sum_i \frac{\lambda'_{i23}\lambda_{i32}^*}{M_{\tilde{\nu}_i}^2},$$

Rare decay: $\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(\mathcal{R})} = \frac{f_{B_s}^2 M_{B_s}^3}{64\pi\Gamma_{B_s}} \left(\frac{M_{B_s}}{m_b}\right)^2 \left(1 - \frac{2m_\mu^2}{M_{B_s}^2}\right) \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} \times \left(\left| \sum_i \frac{\lambda_{i22}^* \lambda'_{i32}}{M_{\tilde{\nu}_i}^2} \right|^2 + \left| \sum_i \frac{\lambda_{i22} \lambda_{i32}^*}{M_{\tilde{\nu}_i}^2} \right|^2 \right)$

$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(\mathcal{R})} = k \frac{f_{B_s}^2 M_{B_s}^3}{64\pi\Gamma_{B_s}} \left(\frac{\lambda_{i22}\lambda'_{i32}}{M_{\tilde{\nu}_i}^2}\right)^2 \left(\frac{M_{B_s}}{m_b}\right)^2 \left(1 - \frac{2m_\mu^2}{M_{B_s}^2}\right) \times \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}},$

...assume that a single sneutrino dominates, neglect possible CP-violation...



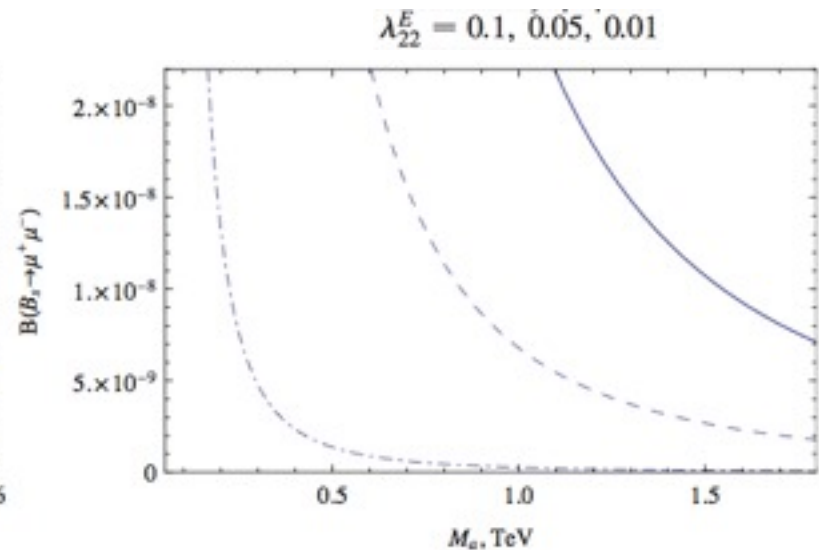
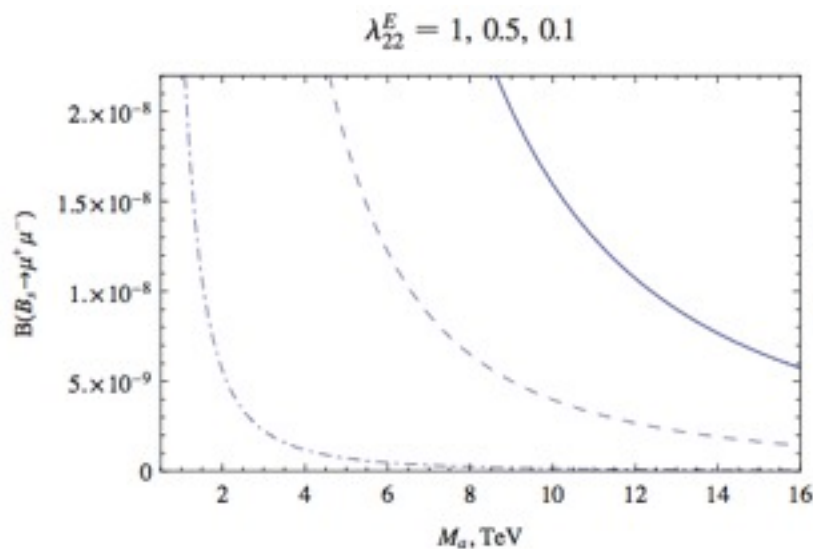
$$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(\mathcal{R})} = \frac{3}{20\pi} \frac{M_{B_s}^2}{F(C_3, B_3)} \left(\frac{M_{B_s}}{m_b}\right)^2 \left(1 - \frac{2m_\mu^2}{M_{B_s}^2}\right) \times \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} x_{B_s}^{(\mathcal{R})} \frac{\lambda_{k22}^2}{M_{\tilde{\nu}_i}^2}.$$

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Mixing vs rare decays: some models

➤ FCNC pseudoscalars:

$$\mathcal{B}_{B_s^0 \rightarrow \ell^+ \ell^-}^{(a)} = \frac{3}{10\pi} \cdot \frac{M_{B_s}^4 x_s^{(a)}}{m_b^2 f_a(\bar{C}_i, m_b)} \left(1 - \frac{4m_\ell^2}{M_{B_s}^2}\right)^{1/2} \left(\frac{\lambda_{22}^E}{M_a}\right)^2,$$



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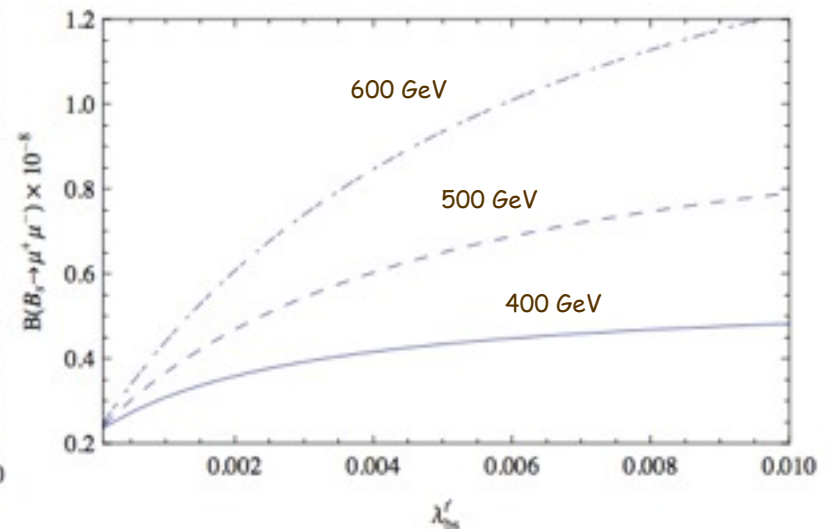
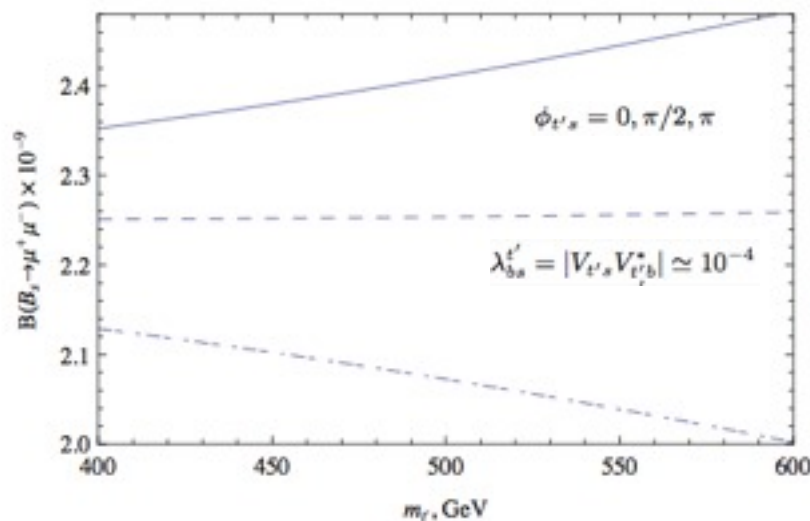
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➤ Sequential 4th generation of quarks:

$$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-} = \frac{3\alpha^2 m_\mu^2 x_{B_s}}{8\pi \hat{B}_{B_s} M_W^2} \sqrt{1 - \frac{4m_\mu^2}{m_{B_s}^2} \frac{|C_{10}^{tot}|^2}{|\Delta'|}},$$

$$\Delta' = \eta_t S_0(x_t) + \eta_{t'} R_{t't}^2 S_0(x_{t'}) + 2\eta_{t'} R_{t't} S_0(x_t, x_{t'})$$

Soni et al



Things to take home

- Indirect effects of New Physics at flavor factories help to distinguish among models possibly observed at the LHC in the future
 - a combination of bottom/charm sector studies
- Charm provides great opportunities for New Physics studies
 - unique access to up-type quark sector
 - large available statistics/in many cases small SM background
 - contributions from New Physics are still possible
- Can correlate mixing and rare decays with New Physics models
 - signals in D-mixing vs rare decays help differentiate among models
 - similar correlations in B_s studies restrict parameter space of several popular models