## CM31: Step V. 0

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## Life after Step IV...



STEP V

No Coupling Coil...?


STEP V. 0

## Step V. 0 Operating Modes

- FCs share the same power supply (| $\mathrm{J}_{\mathrm{FC}} \mid$ )
- Can flip sign
$\rightarrow$ different running modes for Step V.O?
- Match Coils also tuneable (M1,2)


Flip Mode


## Other possibilities:





## Matching Step V. 0

- Want operating currents for FC \& M1,2
- Evolve Beta Fn. through MICE with:

$$
2 \beta \beta^{\prime \prime}-\left(\beta^{\prime}\right)^{2}+4 \beta^{2} \kappa^{2}-4=0
$$

- Minimize: $\quad F=\frac{1}{2}\left(\beta_{0} \gamma-2 \alpha_{0} \alpha+\beta \gamma_{0}\right)$

1. Match beam between FCs $\rightarrow$ Find $\beta_{0}, J_{F C}$
2. Match beam from solenoid $\rightarrow$ Find $J_{M 1}, J_{M 2}$

- Tune MICE optics for all modes.
- Ignore current limits for now.
$1^{\text {st }}$ FC centre
$2^{\text {nd }}$ FC centre




## Flip Mode

- Use Minuit to search parameter space
- Minima in two distinct regions.



## Solutions

| Mode | $J_{\text {FC }}$ | $\mathrm{J}_{\mathrm{M} 2}$ | $\mathrm{J}_{\text {M1 }}$ | $\beta_{0}[\mathrm{~cm}]$ | $\mathrm{p}_{\mathrm{z}}[\mathrm{MeV} / \mathrm{c}]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Flip | 241.90 | 168.64 | 229.32 | 10.41 | 200 |
| +-- + | 124.00 | 233.99 | 211.80 | 76.00 | 200 |
| Battery | 270.99 | 62.84 | 241.04 | 7.03 | 200 |
| + - + | 116.00 | 254.18 | 231.11 | 82.00 | 200 |
| Solenoid ++++ Seesaw | no fit |  |  |  |  |

( $J$ in units of $A / \mathrm{mm}^{2}$ )

- Battery Mode not discussed any further
$\rightarrow$ Flip Mode better.


## Flip Mode - 4T

- High \& low $\beta$ sols.




## Scaled Solutions

- However: $\left|\mathrm{J}_{\mathrm{FC}}\right|<140$ \& $\left|\mathrm{J}_{\mathrm{M} 1,2}\right|<160$
- Options:

1) Scale down all coil currents
-3 T in SS, reduce $\mathrm{p}_{\mathrm{z}} \rightarrow \beta_{\text {in }}=33.3 \mathrm{~cm}$
Matching Condition

2) Scale down FC \& M1, M2.

- Run at 4T in SS, reduce $p_{z} \rightarrow \beta_{\text {in }}$ reduced.

| $\beta_{0}[\mathrm{~cm}]$ | $\mathrm{J}_{\mathrm{FC}}$ | $\mathrm{J}_{\mathrm{M} 2}$ | $\mathrm{~J}_{\mathrm{M} 1}$ | $\mathrm{p}_{\mathrm{Z}}[\mathrm{MeV} / \mathrm{c}]$ |
| :---: | :---: | :---: | :---: | :---: |
| 10 | 137 | 96 | 130 | 113 |
| 76 | 85 | 160 | 144 | 136 |

## 1) Scale down all coil currents



Flip 3T
$\beta_{0}=76 \mathrm{~cm}$ solution

$p_{z}=136 \mathrm{MeV} / \mathrm{c}$ no material



## 2) Scale down only FC \& M1,2

 $p_{z}=123 \mathrm{MeV} / \mathrm{c}$ no material

$$
\begin{aligned}
& \beta_{0} \sim 76 \mathrm{~cm} \\
& \mathrm{~J}_{\mathrm{FC}}=76.284 \\
& \mathrm{~J}_{\mathrm{M} 1}=125.66 \\
& \mathrm{~J}_{\mathrm{M} 2}=149.80
\end{aligned}
$$



## Step V.O: Modes (scaled)

| Mode | JFC |  | J4 (M2) |  | J5 (M1) |  | $\beta_{0}$ | $\mathrm{p}_{2}[\mathrm{MeV} / \mathrm{c}]$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Flip | 241.90 | 137.00 | 168.64 | 95.51 | 229.32 | 129.87 | 10.41 | 200 | 113.27 |
| + - + | 124.00 | 84.79 | 233.99 | 160 | 211.80 | 144.82 | 76.00 | 200 | 136.76 |
| Battery | 270.99 | 137.00 | 62.84 | 31.77 | 241.04 | 121.86 | 7.03 | 200 | 101.11 |
| + - + - | 116.00 | 73.02 | 254.18 | 160 | 231.11 | 145.48 | 82.00 | 200 | 125.90 |
| Solenoid   <br> ++++ nofit  <br> Seesaw   <br> ++--   |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  | Max. J $\mathrm{JCC}^{\text {c }}$ | 137 |  |  |  |  |  |
|  |  |  | Max. J ${ }_{\text {MC }}$ | 160 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

Limiting parameter underlined

## Step V. 0 in G4MICE

Flip $3 T$
$\beta_{0}=76 \mathrm{~cm} \mathrm{sol}$.

## emittance $[m m]$



Z [m]
$\beta_{\text {[cm] }}$

$p_{z}=136 \mathrm{MeV} / \mathrm{c}$
no material

## Step V. 0 in G4MICE

Flip 4T
$\beta_{0}=10 \mathrm{~cm}$ sol.
emittance $[m m]$
$\beta$ [cm]
$\varepsilon=3 \mathrm{~mm}$
$\sigma_{\mathrm{pz}}=1 \mathrm{MeV} / \mathrm{c}$


$p_{z}=113 \mathrm{MeV} / \mathrm{c}$
no material

## Step V. 0 in G4MICE

Flip 4T
$\beta_{0}=76 \mathrm{~cm} \mathrm{sol}$.
emittance $[m m]$
$\beta_{\text {[cm }]}$

$p_{z}=136 \mathrm{MeV} / \mathrm{c}$
no material

## Summary

- Step V. 0 - RF without the Coupling Coil.
- Matched solutions found for Step V. 0 in Flip Mode.
- Evolve beam envelope eqns (on axis beams)
- Require $p_{z}<140 \mathrm{MeV} / \mathrm{c}$
- Too low?
- Not matched with "real" beams in G4MICE
- Non-linear effects wreck matching
- Alternative matching techniques?
> Step V. 0 a non-starter at present

