

Using M_{T2} to Distinguish DM Stabilization Symmetries

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K. Agashe, DK, D. G. Walker, and L. Zhu, , Phys. Rev. D **84** 055020 (2011) arXiv:hep-ph/[1012.4460](https://arxiv.org/abs/1012.4460)

1. Introduction

Motivation

- Evidence for the existence of DM
 - WIMPs (Weakly Interacting Massive Particles): well-motivated DM candidate
 - Annihilation cross section of a pair of DM $\rightarrow M \sim 100$ GeV (Weak scale)
- Many beyond-SM models (e.g., SUSY, UED, and Little Higgs) contain such a DM candidate.
 - direct/indirect measurement, collider experiment
 - (For most of them,) Z_2 /parity as the DM stabilization symmetry
- Z_2 is **NOT** the only choice to stabilize DM!
 - Any discrete or continuous global symmetry can be employed to stabilize DM.
 - Should identify the nature of the symmetry, *experimentally*.
 - Any **DISTINGUISHABLE** features, in particular, between Z_2 and Z_3 in collider signals?
 - (Z_3 as a simple non- Z_2 : e.g., warped GUT: K. Agashe and G. Servant, Phys. Rev. Lett. 93, 231805(2004)
arXiv:[0403143](#), E. Ma, Phys. Lett. B 662, 49 (2008) arXiv:0708.3371, B. Batell, arXiv: 1007.0045)
 - M_{12} distribution as a tool

1. Introduction

Collider signals

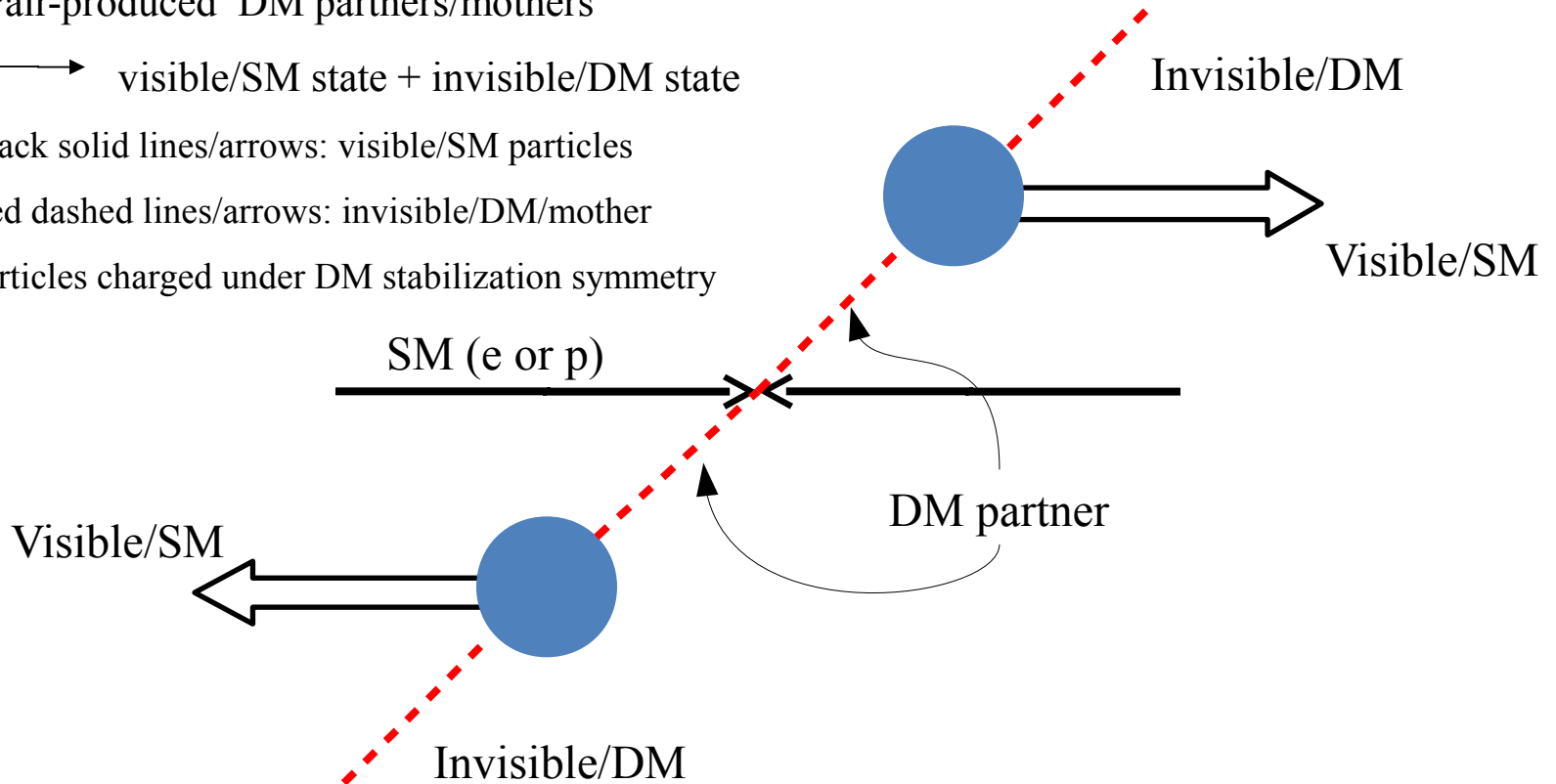
- Pair-produced DM partners/mothers

→ visible/SM state + invisible/DM state

Black solid lines/arrows: visible/SM particles

Red dashed lines/arrows: invisible/DM/mother

particles charged under DM stabilization symmetry



2. Assumptions

Assumptions

- Model-independent argument (for any Z_3 models)
 - Possible to generalize to more complicated symmetries
- Pair-produced same mother particles
- Looking at the decay on **BOTH** decay sides assuming off-shell intermediate states.
 - cf) one decay side using invariant mass variable → see Agashe, DK, Toharia, and Walker Phys. Rev. D **82** 015007 (2010) arXiv: hep-ph/1003.0899
- Mother particles decay into DM **INSIDE** the detector.
 - no meta-stable mother particles (See Walker arXiv:hep-ph/0907.3142)
- Massless visible/SM particles (just for simplicity)

3. Z_3 symmetry

Z_3 primer

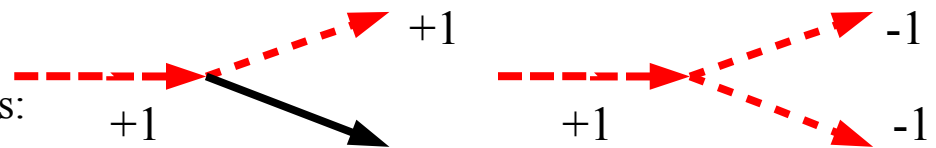
$$\Phi \rightarrow \Phi \exp\left(\frac{2\pi i}{3} q\right) \quad q = 0, +1, -1 (\equiv +2)$$

neutral charged (under Z_3)

- DM is charged +1 \longrightarrow antiparticle -1 (= +2) $DM \neq \overline{DM}$
- (Under Z_2 : DM +1 \longrightarrow antiparticle -1 (= +1) $DM = \overline{DM}$)

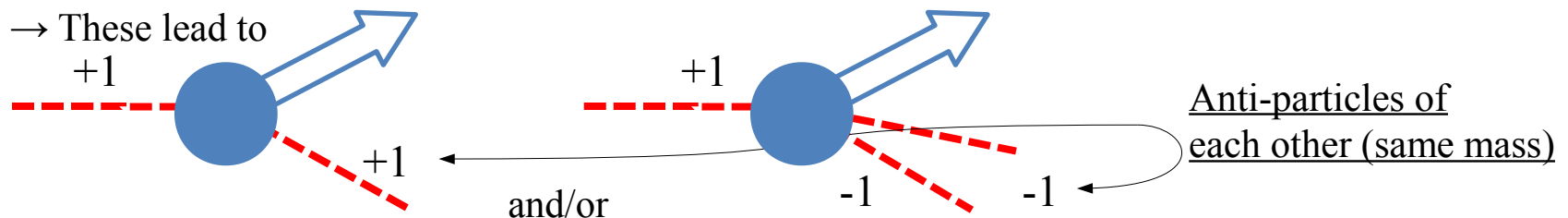
DM is Dirac fermion or complex scalar.

Vertex with 2 Z_3 - or 3 Z_3 -charged particles:



“charged-charged-charged” and “charged-charged-neutral”

\rightarrow These lead to



4.1 Review on M_{T2} variable

● Why M_{T2} ?

- More information available from both decay sides
 - cf) invariant mass variable of visible particles from the same decay side
- Single visible particle in each decay side: invariant mass variable does NOT work
- However, complicated: *invisible* particles in the final state (missing energy/momentum)
 - Missing energy/momentum shared by the two decay chains
 - M_{T2} constructed to comprehend this situation
- **Main strategy**
 - Investigate M_{T2} variable in Z_2 and Z_3 models
 - Find any observables/features different in Z_2 and Z_3 models

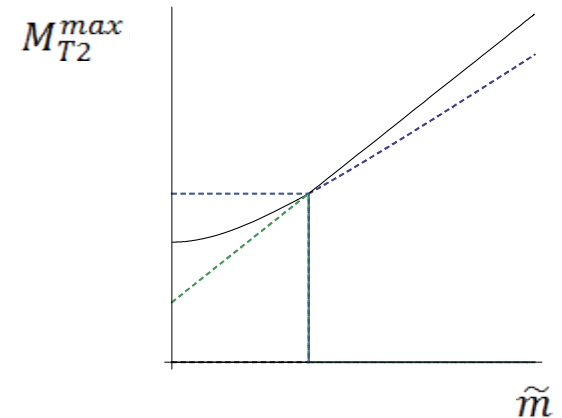
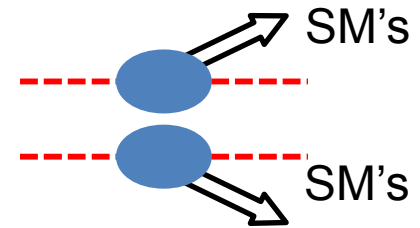
4.1 Review on M_{T2} variable

● $M_{T2}^{(1)}$ primer

- M_{T2} variable: generalization of the transverse mass to the case where pair-produced mother particles decay into SM's & DM per mother

$$M_{T2}(\tilde{m}) = \min_{\substack{\vec{p}_T^{\nu(1)} + \vec{p}_T^{\nu(2)} \\ \vec{p}_T^{\tilde{i}(1)} + \vec{p}_T^{\tilde{i}(2)} = 0}} [\max\{M_T^{(1)}, M_T^{(2)}\}]$$

- $M_{T2}^{max}(\tilde{m} = m_{DM}) = M$ (\tilde{m} : trial DM/LSP mass, M : mother mass)
- **Kink structure**²⁾ (for the case with more than one visible/SM particle in each decay chain) due to two types of solution (balanced/unbalanced)
→ **direct measurement of DM and mother mass**



¹⁾ C.G. Lester, D.J. Summers, Phys. Lett. B**463**, 99 (1999), arXiv:hep-ph/9906349

²⁾ W.S. Cho, K. Choi, Y.G. Kim and C.B. Park, Phys. Rev. Lett. **100**, 171801 (2008), arXiv:0709.0288

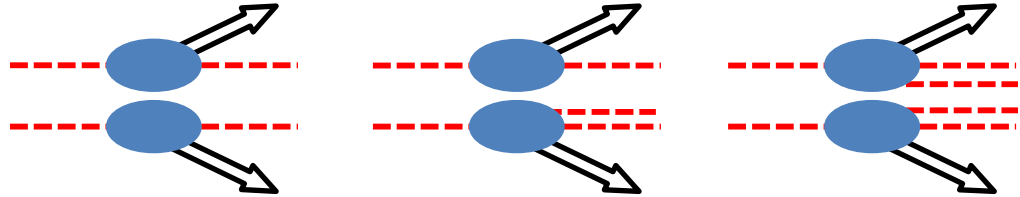
4.2 M_{T2} in Z_3 symmetry

● “Naïve” M_{T2} method

- Each mother emits one or two DM: 2, 3, or 4 DM in the final state

(E_2 , E_3 , and E_4 type events

depending on # of DM)

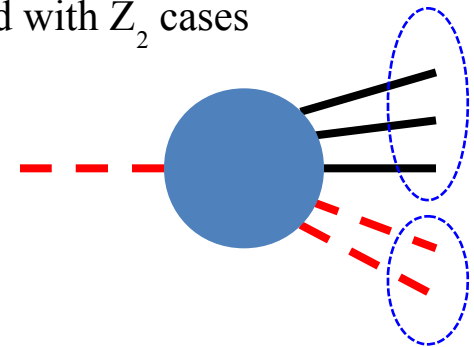


- Still apply M_{T2} variable assuming only 1 DM in each decay chain \rightarrow “Naïve” M_{T2} method
- Will provide different/contradictory and more features compared with Z_2 cases

● Theoretical prediction on the upper edge

- Find the situation to yield the upper edge in M_{T2} distribution
- Consider the “effective” mass of invisible particles

as well as the effective mass of visible particles in the sense of M_{T2} variable



4.2 M_{T2} in Z_3 symmetry

One visible/SM particle in each decay chain

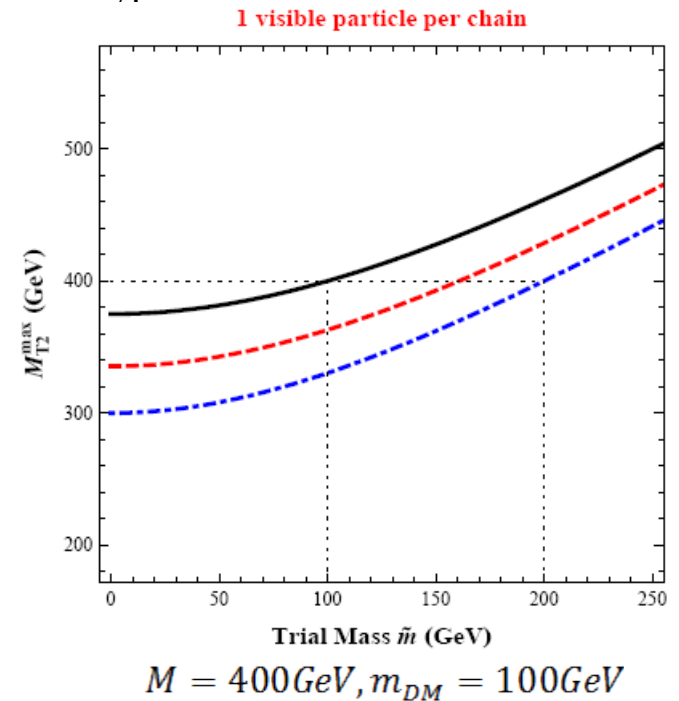
- No kink structure as expected
- Three different upper edges corresponding to three different types of events

$M_{T2,E_2}^{max} > M_{T2,E_3}^{max} > M_{T2,E_4}^{max}$ for all trial DM mass

$$M_{T2,E_2}^{max} = \sqrt{\frac{(M^2 - m_{DM}^2)^2}{4M^2}} + \sqrt{\frac{(M^2 - m_{DM}^2)^2}{4M^2} + \tilde{m}^2}$$

$$M_{T2,E_3}^{max} = \sqrt{\frac{(M^2 - m_{DM}^2)(M^2 - 4m_{DM}^2)}{4M^2}} + \sqrt{\frac{(M^2 - m_{DM}^2)(M^2 - 4m_{DM}^2)}{4M^2} + \tilde{m}^2}$$

$$M_{T2,E_4}^{max} = \sqrt{\frac{(M^2 - 4m_{DM}^2)^2}{4M^2}} + \sqrt{\frac{(M^2 - 4m_{DM}^2)^2}{4M^2} + \tilde{m}^2}$$



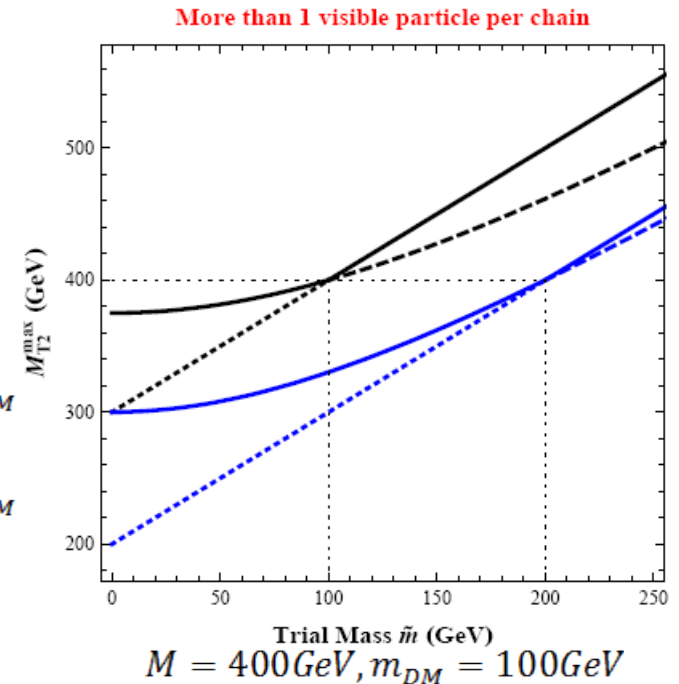
4.2 M_{T2} in Z_3 symmetry

More than one visible/SM particle in each decay chain

- Kink appears as expected, but not always for E_3
- Determine mother and DM masses by kink from E_2 type events, and cross check by the kink from E_4 type events

$$M_{T2,E_2}^{max} = \begin{cases} M - m_{DM} + \tilde{m} & , \quad \tilde{m} \geq m_{DM} \\ \sqrt{\frac{(M^2 - m_{DM}^2)^2}{4M^2} + \sqrt{\frac{(M^2 - m_{DM}^2)^2}{4M^2} + \tilde{m}^2}} & , \quad \tilde{m} \leq m_{DM} \end{cases}$$

$$M_{T2,E_4}^{max} = \begin{cases} M - 2m_{DM} + \tilde{m} & , \quad \tilde{m} \geq 2m_{DM} \\ \sqrt{\frac{(M^2 - 4m_{DM}^2)^2}{4M^2} + \sqrt{\frac{(M^2 - 4m_{DM}^2)^2}{4M^2} + \tilde{m}^2}} & , \quad \tilde{m} \leq 2m_{DM} \end{cases}$$



4.2 M_{T2} in Z_3 symmetry

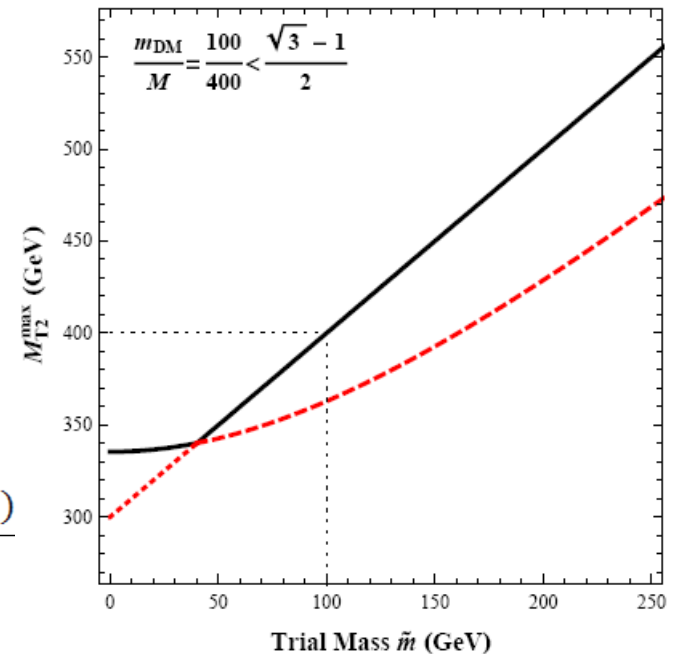
E_3 type events under M_{T2}

- Asymmetric in the final states of both decay sides
- Kink appears depending on the mass hierarchy between mother and DM masses

$$M_{T2,E_3}^{max} = M - m_{DM} + \tilde{m} \quad \text{for all } \tilde{m}$$

$$M_{T2,E_3}^{max} = \begin{cases} M - m_{DM} + \tilde{m}, & \tilde{m} \geq m' \\ \sqrt{\frac{(M^2 - m_{DM}^2)(M^2 - 4m_{DM}^2)}{4M^2}} + \sqrt{\frac{(M^2 - m_{DM}^2)(M^2 - 4m_{DM}^2)}{4M^2}} + \tilde{m}^2, & \tilde{m} \leq m' \end{cases}$$

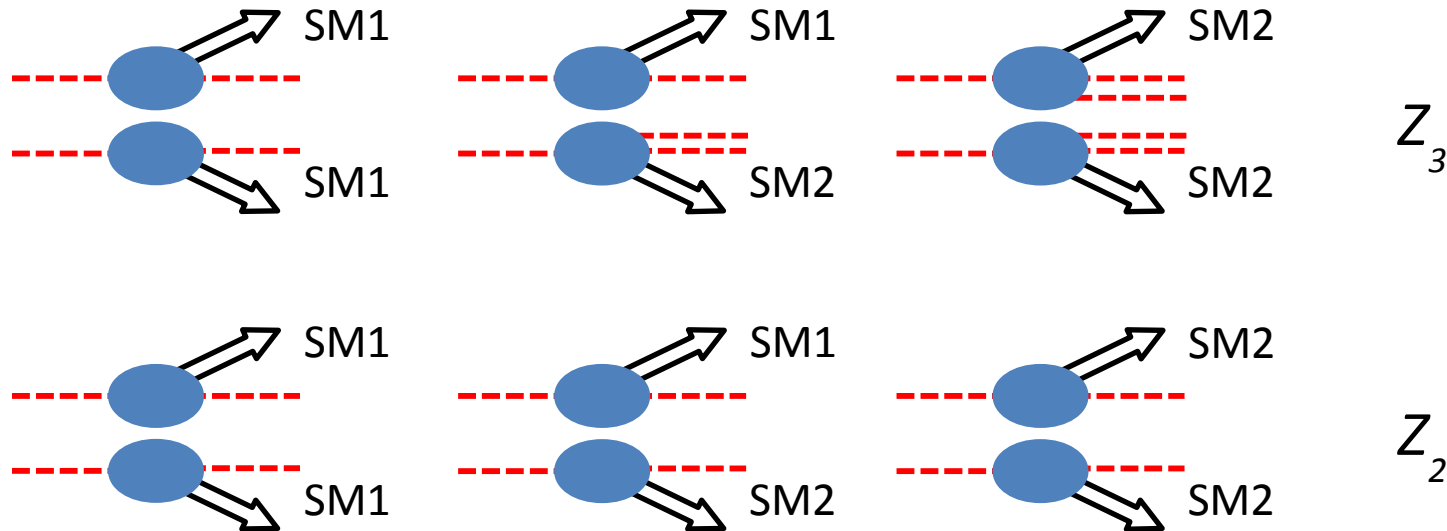
$$m' = \frac{(M - m_{DM})(\sqrt{(M^2 - m_{DM}^2)(M^2 - 4m_{DM}^2)} - M(M - m_{DM}))}{2M(M - m_{DM}) - \sqrt{(M^2 - m_{DM}^2)(M^2 - 4m_{DM}^2)}}$$



4.3 Non-identical visible particle(s) in 2 decay chains

3 decay topologies

- SM state with 1 DM is different from SM state with 2DM



- Main idea: **Three different types of event/richer structures** in the sense of M_{T2} variable

4.3 Non-identical visible particle(s) in 2 decay chains

● One visible/SM particle in each decay chain

- Z_2 case: Only one common upper edge (1DM + 1DM only)
- Z_3 case: Three different upper edges in M_{T2} distribution (1DM + 1DM, 1DM + 2DM, 2DM + 2DM) → Two of them for separate measurement of mother and DM masses, remaining one for cross-check in spite of a kink

● More than 1 visible/SM particle in each decay chain

- Z_2 case: Only one upper edge, and a kink structure at $(\text{trial } m_{DM}) = (\text{real } m_{DM})$
- Z_3 case: 2 edges for $(\text{trial } m_{DM}) \geq (\text{real } m_{DM})$, 3 edges for $(\text{trial } m_{DM}) < (\text{real } m_{DM})$, and also kink structure in each type of events → Measurement of mother and DM masses from (1DM + 1DM) give predictions on upper edges & kink location for the other two types of events

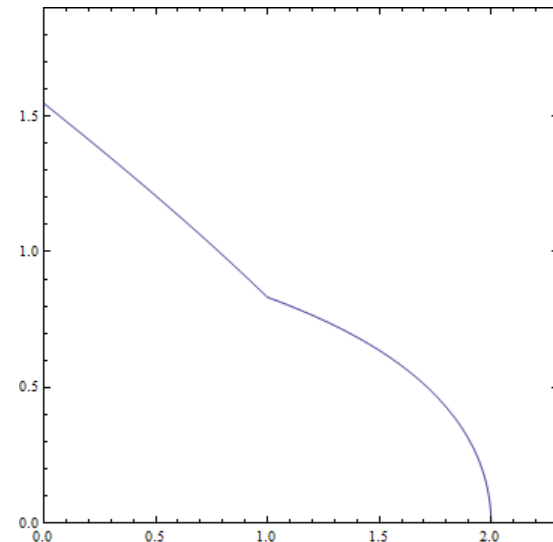
4.4 Identical visible particle(s) in 2 decay chains

Possible trials

- No way to separate E_2 , E_3 , and E_4 simply by particle identities → Only combined distribution
- 1 visible particle in each decay chain: Kinks in M_{T2} distribution at the upper edges for E_3 , E_4 ?
 - Not clear due to longer tails
 - Smearing effect/Statistical fluctuations
- More than 1 visible particle in each decay chain:
 - Still hard to see this kink

⇒ Introduction of a new method

- Separate E_3 events from combined events
(using imbalance of E_3 type events in both decay sides)
- Do the same analysis for the separated events



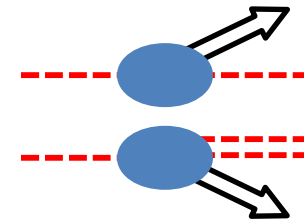
4.4 Identical visible particle(s) in 2 decay chains

● Pt/Ht ratio cut

- Employ the fact that E_3 type events are asymmetric in the final state while E_2 are symmetric:
2DM side carries less momentum/energy than 1DM side, on average

- Define P_t/H_t ratio

$$R_{Pt} = \frac{P_t^{max}}{P_t^{min}} \quad R_{Ht} = \frac{H_t^{max}}{H_t^{min}}$$

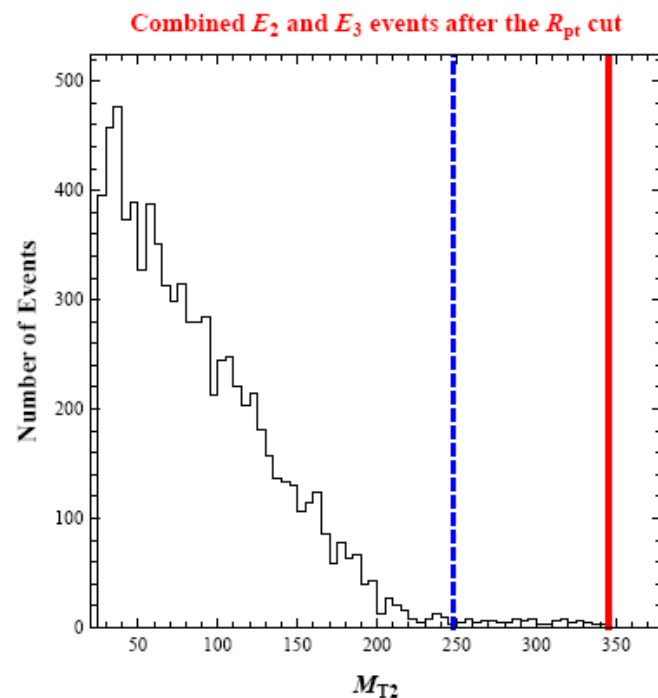
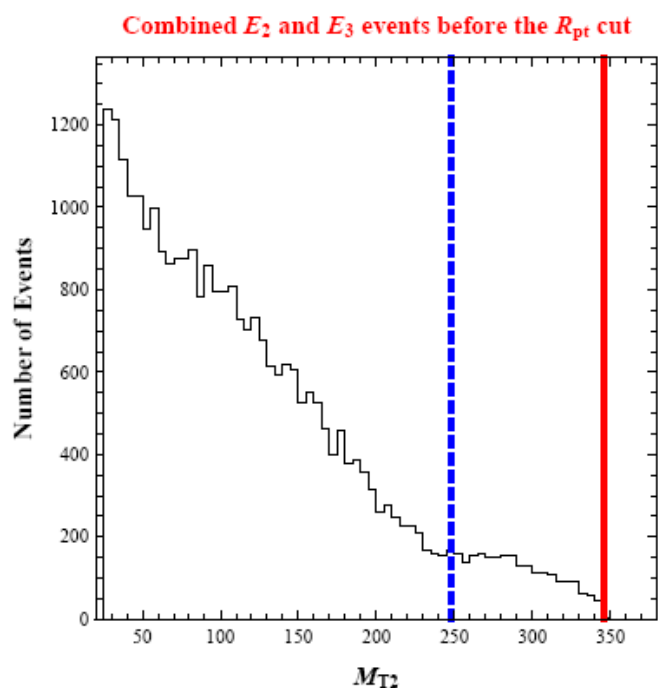


- Expect many E_2 type events give 1 vs. many E_3 type events give >1
- Remove/keep decay events by imposing ratio cuts
- Compare survival rates among different types of events
- Re-do M_{T2} analysis after cuts as further confirmation: for Z_3 upper edge will shift down
(especially, to distinguish Z_3 from $Z_2 + \text{neutrino}$)

4.4 Identical visible particle(s) in 2 decay chains

One visible/SM particle in each decay chain

- Solid red – theoretical E_2 edge, dotted blue – theoretical E_3 edge
 $M = 400\text{GeV}, m_{DM} = 150\text{GeV}, \tilde{m} = 25\text{GeV}$ R_{pt} cut = 5 $E_2 : E_3 = 1:2$

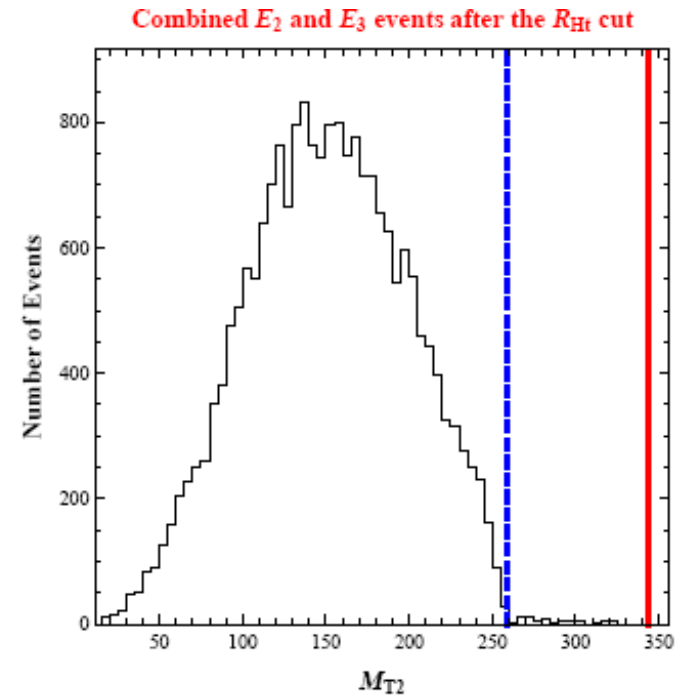
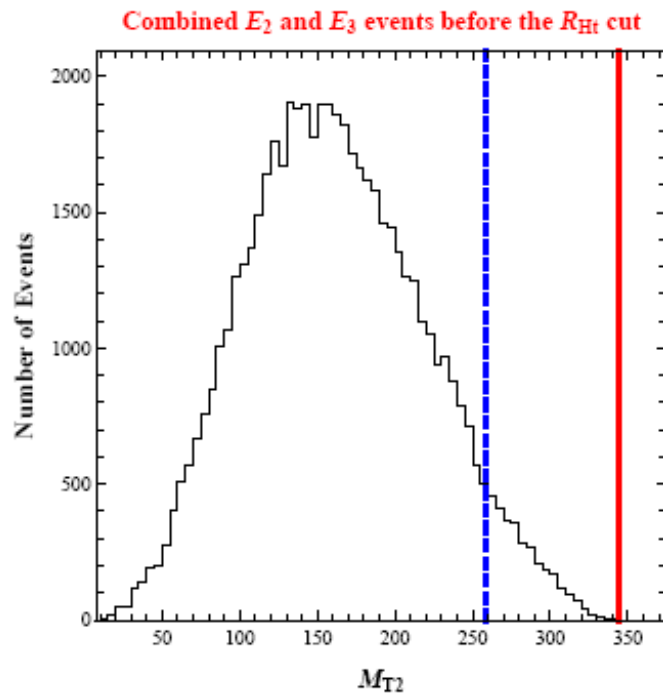


4.4 Identical visible particle(s) in 2 decay chains

More than one visible/SM particle in each decay chain

- Solid red – theoretical E_2 edge, dotted blue – theoretical E_3 edge

$$M = 400\text{GeV}, m_{DM} = 150\text{GeV}, \tilde{m} = 25\text{GeV} \quad R_{Ht} \text{ cut} = 5 \quad E_2 : E_3 = 1:2$$



5. Summary

● We have learned that...

- DM stabilization symmetry does **NOT** have to be Z_2



- Mother particle decays in Z_3 → More structure → Can be distinguished from Z_2



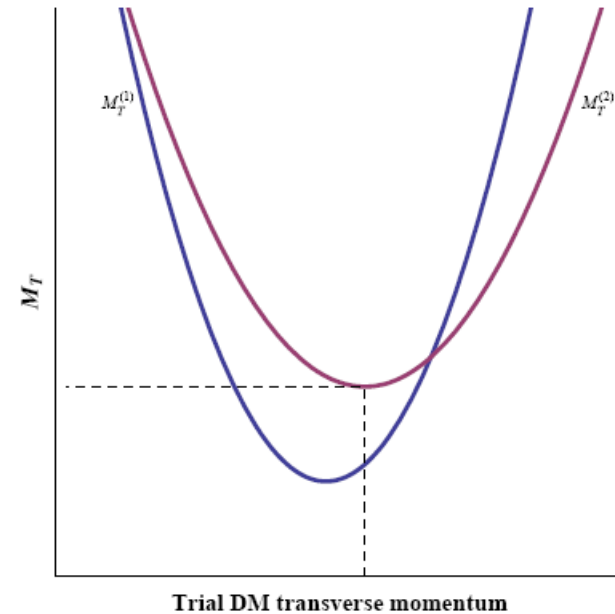
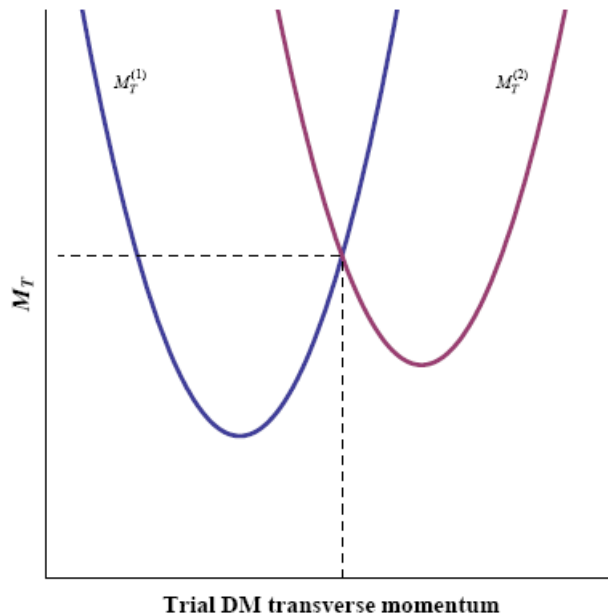
- 2,3, and 4 DM in the final state for Z_3 while 2 DM for Z_2
- Non-identical visible particle(s) : **NUMBER of UPPER EDGES in M_{12}** from multiple decay topologies/ M_{12} distributions in Z_3
- Identical visible particle(s): event separation by **Pt/Ht RATIO CUT** → number of upper edges
- A follow-up paper will come out soon. Stay tuned!**

Thank You

Backup

● M_{T2} primer: balanced and unbalanced solutions

- Balanced solution: intersection between two M_T 's = M_{T2}
- Unbalanced solution: intersection between two M_T 's $> M_{T2}$

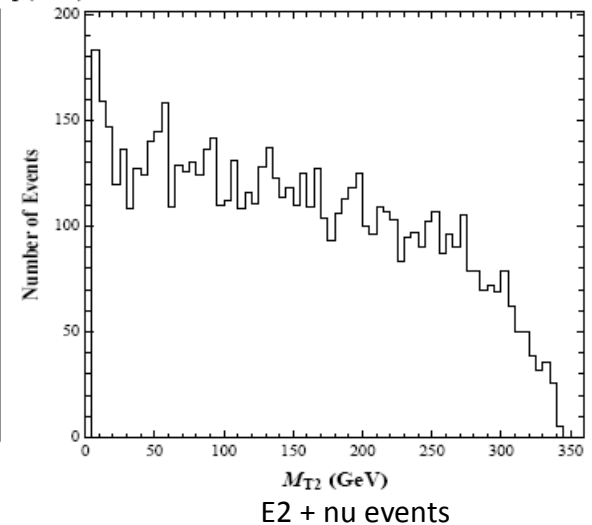
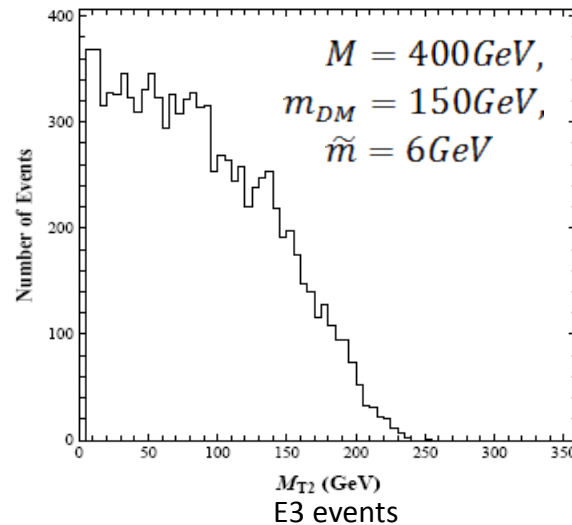
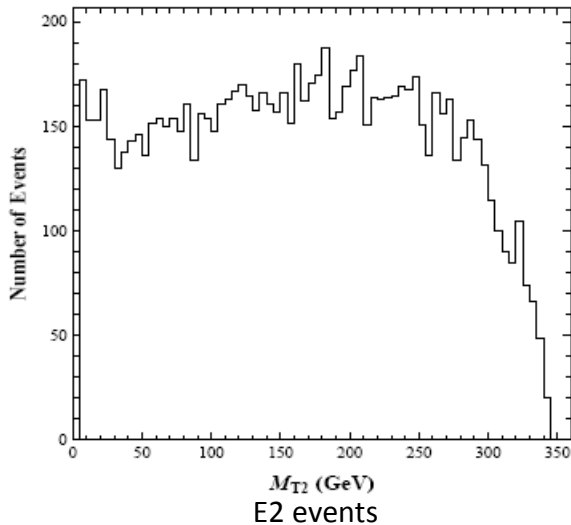


Backup

Shapes of M_{T2} distribution

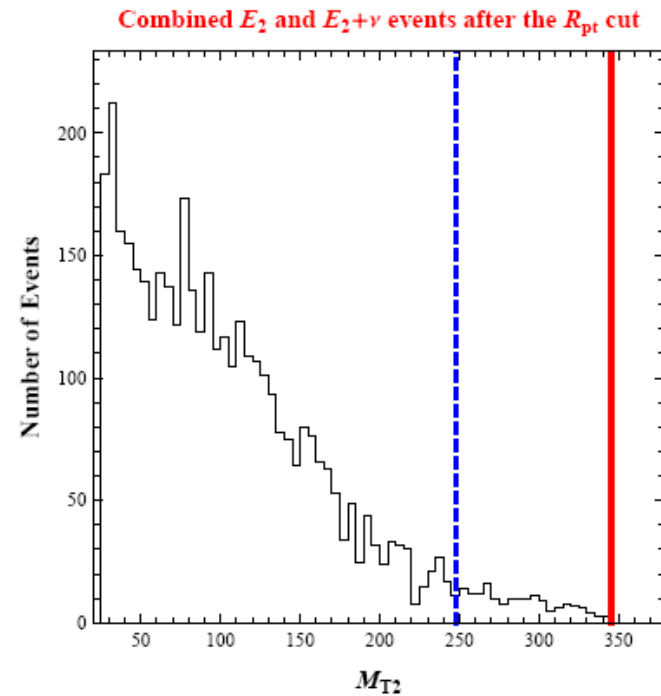
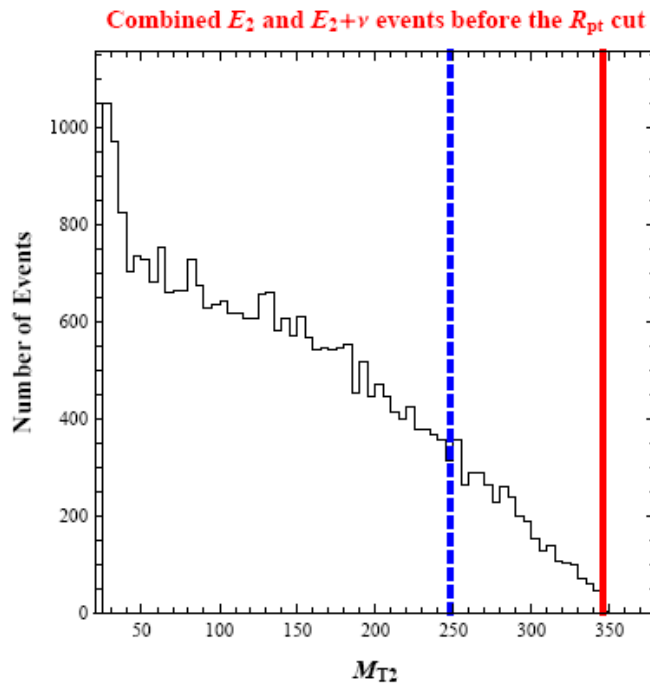
- (Relatively) longer tail for E_3 and E_4 type events: more physical constraints (e.g. rapidity) between decay products should be satisfied
- Adding neutrino \rightarrow relatively longer tail than pure E_2 , but still distinguishable!

\rightarrow E_2 and $E_2 + \nu$ with same edges in Z_2 vs. E_2 , E_3 , and E_4 with different edges in Z_3



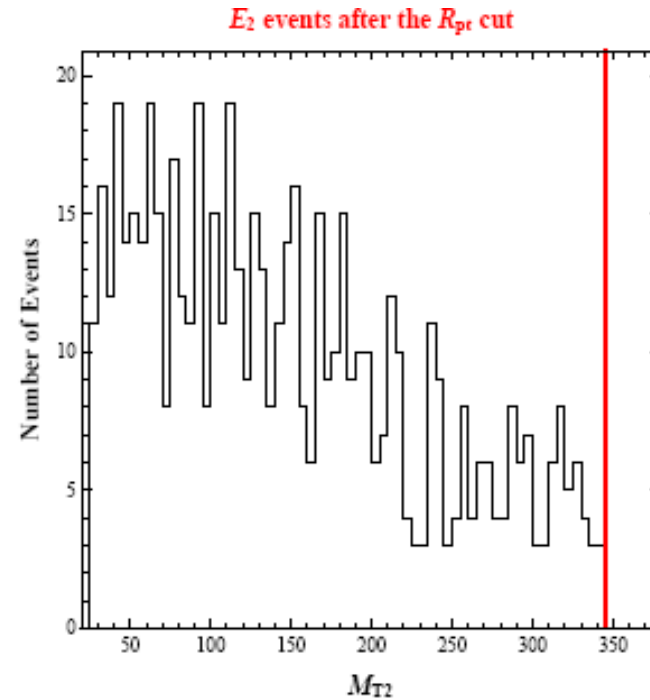
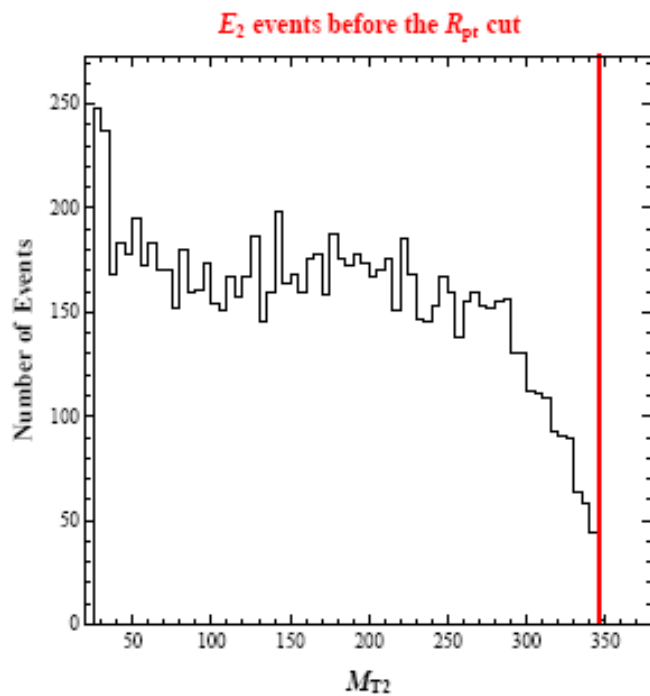
Backup

- One visible/SM particle in each decay chain ($E_2 + \nu$)



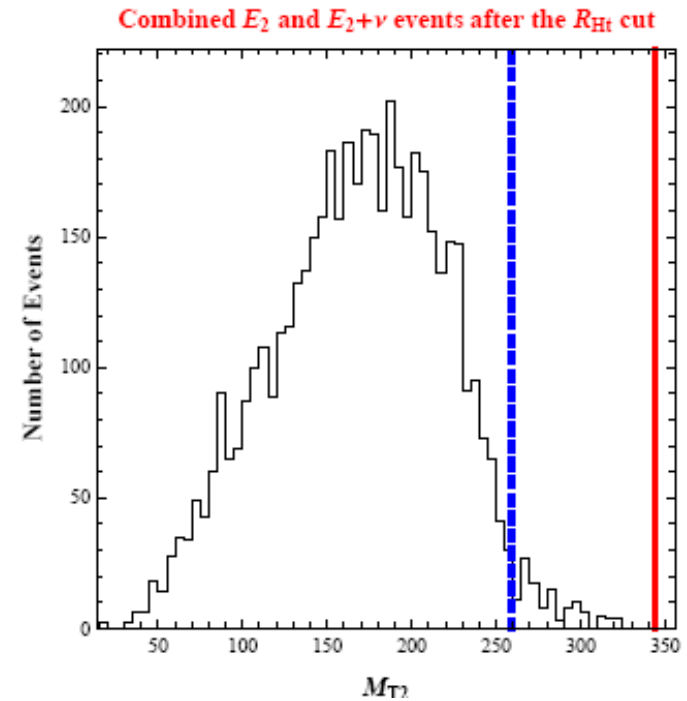
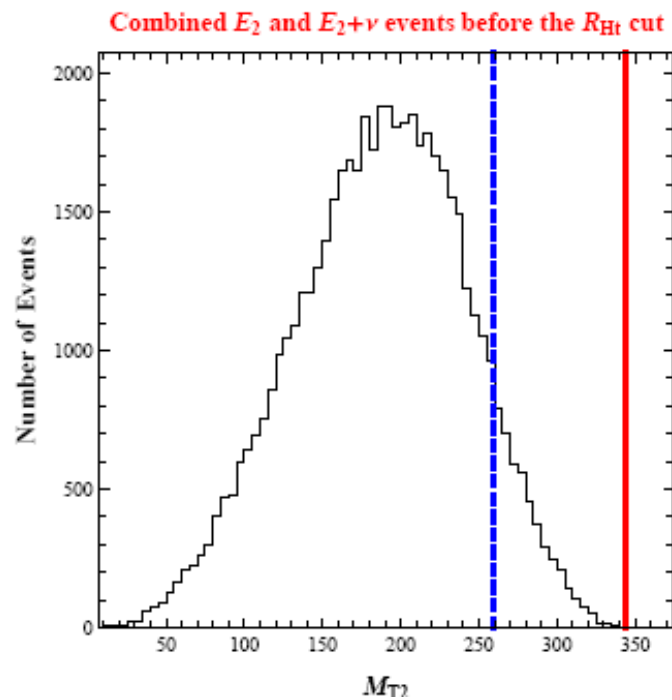
Backup

- One visible/SM particle in each decay chain (E_2)



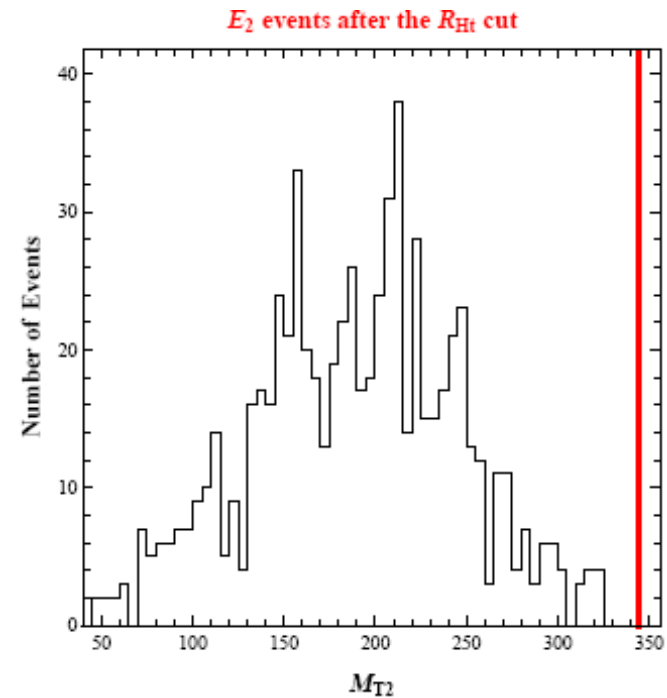
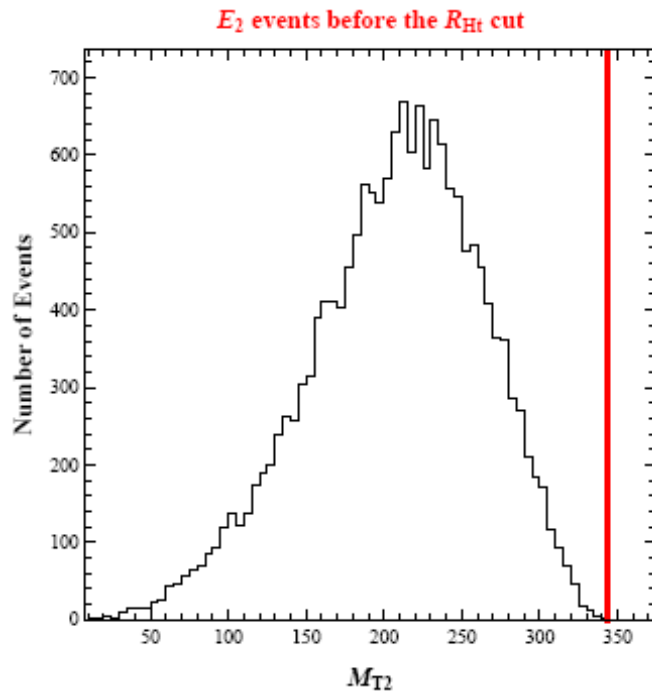
Backup

- More than one visible/SM particle in each decay chain ($E_2 + \nu$)



Backup

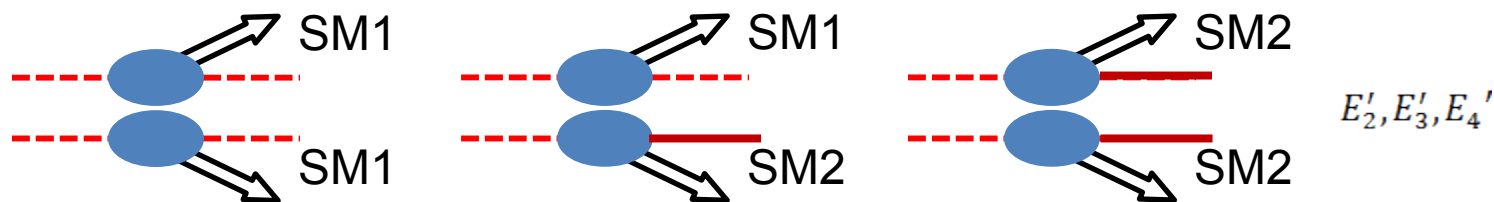
- More than one visible/SM particle in each decay chain (E_2)



Backup

Signal fakes

- (Effective) second invisible particle (e.g. another DM, collider-stable invisible, on-shell intermediate particle whose decay products are all invisible)



- Three upper edges in M_{T2} distribution **NOT because of # of DM BUT because of another DM-like particle** → Can be resolved!
 - One SM/visible in each decay chain: **SHAPE** (3 clear sharp upper edges vs. 1 sharp edge + 2 (relatively) longer tailed edges)
 - More than 1 SM/visible in each decay chain: 1) mother and DM masses from kink in M_{T2}^{\max} vs. trial m_{DM} 2) Predictions on upper edges of E_3, E_4 3) Good matches only for Z_3

Backup

● Signal fakes

- E_2' , E_3' , and E_4' type events are combined
- One visible particle in each decay chain
 - Two sharp kinks in the middle of the distribution: E_3' and E_4' have only 1 DM in each decay chain
- More than 1 SM/visible in each decay chain
 - 1) mother and DM masses from kink in M_{T2}^{\max} vs. trial m_{DM} 2) Predictions on upper edges for the other types of events 3) Event separation by Pt/Ht ratio cut 4) Good matches only for Z_3