SOFT PHOTONS & $B_s^0 \rightarrow \mu^+ \mu^-$

KRISTOPHER J. HEALEY ALEXEY A. PETROV Y.G. ADITYA

WAYNE STATE UNIVERSITY

PHENOMENOLOGY SYMPOSIUM 2012 UNIVERSITY OF PITTSBURGH

THE DECAY $B_s^0 \to \mu^+ \mu^-$

- Helicity Suppressed
 - Pseudoscalar Lepton pair spin flip
 - Standard Model amplitude is small

$$\mathcal{A}(B_s^0 \to \mu^+ \mu^-) \propto \left(\frac{m_\ell}{m_{B_s^0}}\right)$$

THE DECAY $B_s^0 \to \mu^+ \mu^-$

- Helicity Suppressed
 - Pseudoscalar Lepton pair spin flip
 - Standard Model amplitude is small
- The SM prediction is very clean

Br(
$$B_s^0 \to \mu^+ \mu^-)_{SM} = (3.2 \pm 0.2) \times 10^{-9}$$

• A. J. Buras, Phys. Lett. B566(2003) 115

Br(
$$B_s^0 \to \mu^+ \mu^-)_{SM} = (3.33 \pm 0.21) \times 10^{-9}$$

• Golowich, Hewett, Pakvasa, Petrov, Yeghiyan, Phys.Rev.D83(2011):114017

$$\mathcal{A}(B_s^0 \to \mu^+ \mu^-) \propto \left(\frac{m_\ell}{m_{B_s^0}}\right)$$

THE DECAY $B_s^0 \rightarrow \mu^+ \mu^-$

- Helicity Suppressed
 - Pseudoscalar Lepton pair spin flip
 - Standard Model amplitude is small
- The SM prediction is very clean

Br(
$$B_s^0 \to \mu^+ \mu^-)_{SM} = (3.2 \pm 0.2) \times 10^{-9}$$

• A. J. Buras, Phys. Lett. B566(2003) 115

Br(
$$B_s^0 \to \mu^+ \mu^-)_{SM} = (3.33 \pm 0.21) \times 10^{-9}$$

- Golowich, Hewett, Pakvasa, Petrov, Yeghiyan, Phys.Rev.D83(2011):114017
- Current Experimental Upper Limits (95%C.L.)

$$\mathcal{A}(B_s^0 \to \mu^+ \mu^-) \propto \left(\frac{m_\ell}{m_{B_s^0}}\right)$$

THE DECAY $B_s^0 \to \mu^+ \mu^-$

- Suppressed SM = Excellent probe of New Physics
 - Additional final state particle lifts the suppression.
 - Can carry away angular momentum
- SM contributions from soft photons may be a large source of systematic uncertainty

$$Br(B_s^0 \to \mu^+ \mu^-)_{exp} = Br(B_s^0 \to \mu^+ \mu^-)_{SM} (1 + R_{\gamma_s})$$

THE DECAY $B_s^0 \rightarrow \mu^+ \mu^-$

- Suppressed SM = Excellent probe of New Physics
 - Additional final state particle lifts the suppression.
 - Can carry away angular momentum
- SM contributions from soft photons may be a large source of systematic uncertainty

$$Br(B_s^0 \to \mu^+ \mu^-)_{exp} = Br(B_s^0 \to \mu^+ \mu^-)_{SM} (1 + R_{\gamma_s})$$

- Previous work on $B_s^0 \to \mu^+ \mu^- \gamma$
 - Model dependent form factors
 - Photon Energy Cuts
 - Near our region of interest
- Our calculation:
 - Focus on soft region
 - Model independent (where we can)
 - Expand in powers of 1/M + Chiral

Final Di-Muon Signal Windows

 $\begin{array}{l} {\rm D0:} \ (5.0 ({\rm GeV}) < m_{\mu\mu} < 5.8 ({\rm GeV})) \rightarrow E_{\gamma_{cut}} \approx 350 \ ({\rm MeV}) \\ {\rm ATLAS:} \ (5.1 ({\rm GeV}) < m_{\mu\mu} < 5.7 ({\rm GeV})) \rightarrow E_{\gamma_{cut}} \approx 300 \ ({\rm MeV}) \\ {\rm CDF:} \ (5.3 ({\rm GeV}) < m_{\mu\mu} < 5.4 ({\rm GeV})) \rightarrow E_{\gamma_{cut}} \approx 60 \ ({\rm MeV}) \\ {\rm CMS:} \ (5.3 ({\rm GeV}) < m_{\mu\mu} < 5.4 ({\rm GeV})) \rightarrow E_{\gamma_{cut}} \approx 60 \ ({\rm MeV}) \\ {\rm LHCb:} \ (5.3 ({\rm GeV}) < m_{\mu\mu} < 5.4 ({\rm GeV})) \rightarrow E_{\gamma_{cut}} \approx 60 \ ({\rm MeV}) \\ \end{array}$







EFFECTIVE WEAK B-S TRANSITION

The (bs) FCNC is at 1-loop in SM (penguin + box)

• Weak transition can be expanded in terms of effective operators:



$$\mathcal{H}_{eff} = \sqrt{2} \operatorname{vist}_{ls} \Sigma \operatorname{vit}_{ls} \Sigma \operatorname{vit}_{lr} \operatorname{vit}_{lr} \operatorname{vit}_{lr}$$

$$\mathcal{H}_{b \to s\bar{\ell}\ell} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e}{8\pi^2} m_b C_{7\gamma}(\mu^2) \cdot \bar{s} \sigma^{\mu\nu} (1+\gamma_5) b \cdot F_{\mu\nu}$$

$$\mathcal{H}_{b \to s\bar{\ell}\ell} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{8\pi^2} \Big[\bar{s} \gamma^{\mu} (1-\gamma_5) b \cdot \bar{\ell} \Big[C_{9V}^{eff}(\mu, q^2) \gamma_{\mu} + C_{10A}(\mu^2) \gamma_{\mu} \gamma_5 \Big] \ell$$

$$- 2im_b \frac{C_{7\gamma}(\mu^2)}{q^2} q_{\nu} \cdot \bar{s} \sigma^{\mu\nu} (1+\gamma_5) b \cdot \bar{\ell} \gamma_{\mu} \ell \Big]$$

 $\mathcal{H}_{i}^{b \to s} = \frac{G_F}{E} V_{tb} V_{i}^* \sum C_i(\mu) O_i(\mu)$

EFFECTIVE WEAK B-S TRANSITION

The (bs) FCNC is at 1-loop in SM (penguin + box)

• Weak transition can be expanded in terms of effective operators:



$$\mathcal{H}_{eff}^{\sigma} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum C_i(\mu) O_i(\mu)$$
$$\mathcal{H}_{b \to s\bar{\ell}\ell} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e}{8\pi^2} m_b C_{7\gamma}(\mu^2) \cdot \bar{s} \sigma^{\mu\nu} (1+\gamma_5) b \cdot F_{\mu\nu}$$
$$\mathcal{H}_{b \to s\bar{\ell}\ell} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{8\pi^2} \Big[\bar{s} \gamma^{\mu} (1-\gamma_5) b \cdot \bar{\ell} \Big[C_{9V}^{eff}(\mu, q^2) \gamma_{\mu} + C_{10A}(\mu^2) \gamma_{\mu} \gamma_5 \Big] \ell \Big]$$
$$-2im_b \frac{C_{7\gamma}(\mu^2)}{q^2} q_\nu \cdot \bar{s} \sigma^{\mu\nu} (1+\gamma_5) b \cdot \bar{\ell} \gamma_{\mu} \ell \Big]$$

 $a \mapsto s$

Heavy Meson Chiral Perturbation Theory to parameterize the (bs) quark bilinears:

 $\langle 0|(\bar{s}_L\gamma^{\mu}b_L)|B_s^*\rangle = \frac{i}{2}M_{B_s}f_{B_s}\eta^{\mu}$ $\langle 0|(\bar{s}\sigma^{\mu\nu}(1+\gamma_5)b)|B_s^*\rangle = M_Bf_{B_s}[i\epsilon^{\mu\nu\alpha\beta}v_{\alpha}\eta_{\beta} + v^{\mu}\eta^{\nu} - v^{\nu}\eta^{\mu}]$

 $G_{EU} = U + \sum O() O()$

EFFECTIVE WEAK B-S TRANSITION

The (bs) FCNC is at 1-loop in SM (penguin + box)

Weak transition can be expanded in terms of effective operators:



$$\mathcal{H}_{eff} = \sqrt{2} \mathbf{v}_{tb} \mathbf{v}_{ts} \underline{\mathcal{L}} \mathbf{C}_{i}(\mu) \mathbf{C}_{i}(\mu)$$
$$\mathcal{H}_{b \to s\gamma} = \frac{G_{F}}{\sqrt{2}} V_{tb} V_{ts}^{*} \frac{e}{8\pi^{2}} m_{b} C_{7\gamma}(\mu^{2}) \cdot \bar{s} \sigma^{\mu\nu} (1 + \gamma_{5}) b \cdot F_{\mu\nu}$$
$$\mathcal{H}_{b \to s\bar{\ell}\ell} = \frac{G_{F}}{\sqrt{2}} V_{tb} V_{ts}^{*} \frac{e^{2}}{8\pi^{2}} \left[\bar{s} \gamma^{\mu} (1 - \gamma_{5}) b \cdot \bar{\ell} \left[C_{9V}^{eff}(\mu, q^{2}) \gamma_{\mu} + C_{10A}(\mu^{2}) \gamma_{\mu} \gamma_{5} \right] \ell$$
$$- 2im_{b} \frac{C_{7\gamma}(\mu^{2})}{q^{2}} q_{\nu} \cdot \bar{s} \sigma^{\mu\nu} (1 + \gamma_{5}) b \cdot \bar{\ell} \gamma_{\mu} \ell \right]$$

Heavy Meson Chiral Perturbation Theory to parameterize the (bs) quark bilinears:

$$\langle 0|(\bar{s}_L\gamma^{\mu}b_L)|B_s^*\rangle = \frac{i}{2}M_{B_s}f_{B_s}\eta^{\mu} \langle 0|(\bar{s}\sigma^{\mu\nu}(1+\gamma_5)b)|B_s^*\rangle = M_Bf_{B_s}[i\epsilon^{\mu\nu\alpha\beta}v_{\alpha}\eta_{\beta} + v^{\mu}\eta^{\nu} - v^{\nu}\eta^{\mu}]$$

 $\mathcal{U}^{b \to s} = \frac{G_F}{V} V^* \sum C(u) O(u)$



Expansion (Leading Order):

$$- \left[\begin{array}{c} \left(\frac{1}{M_{B_s^0}} \right)^0 \\ \frac{p_\pi}{\Lambda_\chi} \end{array} \right]$$



Expansion (Leading Order):

$$- \left[\begin{array}{c} \left(\frac{1}{M_{B_s^0}} \right)^0 \\ \frac{p_\pi}{\Lambda_\chi} \end{array} \right]$$



$$= \mathcal{M}_{B_s \to B_s^* \gamma} \left(\frac{-ig^{\mu \alpha}}{2(v \cdot k + \Delta)} \right) \mathcal{M}_{B_s^* \to \mu^+ \mu^-}$$

 $\mathcal{M}_{B_s \to B_s^* \gamma} = -ie\mu \eta_\alpha^* v_\beta k_\mu \epsilon_\nu^* \epsilon^{\mu\nu\alpha\beta}$

Matrix Element : Transition Magnetic Moment

Expansion (Leading Order):

$$\begin{bmatrix} \left(\frac{1}{M_{B_s^0}}\right)^0\\ \frac{p_\pi}{\Lambda_\chi} \end{bmatrix}$$

$$\underbrace{\overset{B_s^{0*}}{\underset{\mu^+}{\overset{\mu^-}}}}_{\overset{\mu^+}{\underset{\mu^+}{\overset{\mu^-}}}} = \mathcal{M}_{B_s \to B_s^* \gamma} \left(\frac{-ig^{\mu\alpha}}{2(v \cdot k + \Delta)} \right) \mathcal{M}_{B_s^* \to \mu^+ \mu^-} -$$

$$\mathcal{M}_{B_s \to B_s^* \gamma} = -ie\mu \eta_\alpha^* v_\beta k_\mu \epsilon_\nu^* \epsilon^{\mu\nu\alpha\beta}$$

Matrix Element : Transition Magnetic Moment

Described by the effective b-s Weak Transition:

 $\mathcal{H}_{eff}^{b \to s} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum C_i(\mu) O_i(\mu)$

$$\mathcal{M}_{B_s^* \to \mu^+ \mu^-} = i \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{8\pi^2} f_{B_s} m_{B_s} [\eta_\mu^* \bar{u}(p_{\mu^+}) [C_9 \gamma^\mu + C_{10} \gamma^\mu \gamma_5] v(p_{\mu^-}) - 2m_b \frac{C_7}{q^2} (\bar{u}(p_{\mu^+}) \gamma_\mu v(p_{\mu^-})) q_\nu (i \epsilon^{\mu\nu\alpha\beta} v_\alpha \eta_\beta + v^\mu \eta^\nu - v^\nu \eta^\mu)]$$

Parameterized in terms of the decay constant

Expansion (Leading Order): $\int \left(\frac{1}{M_{B_s^0}}\right)^{\circ} \frac{p_{\pi}}{\Lambda}$











 $\begin{bmatrix} \left(\frac{1}{M_{B_s^0}}\right)^0 \\ \frac{p_{\pi}}{\Lambda} \end{bmatrix}$

$$\mathcal{L}_h = \frac{Q_Q}{2m_Q} \bar{h}_v \sigma_{\mu\nu} h_v F^{\mu\nu},$$

Light DOF Contribution :



 $\int \left(\frac{1}{M_{B_s^0}}\right)^0 \frac{p_{\pi}}{\Delta}$



HMxPT coupling constants:

$$\mu_{eff} = -\frac{1}{3m_b} - \frac{1}{3}\beta + g^2 \frac{m_K}{4\pi f_K^2}$$

• Use experimental D decays.

$$\Gamma(D_q^* \to D_q \gamma) = \frac{\alpha}{3} \frac{M_{D_q^*}}{M_{D_q}} |\mu_{eff}|^2 |\vec{k}|^3 \qquad - \begin{bmatrix} \mu_{eff} [D^{\pm *} \to D^{\pm} \gamma] = \frac{2}{3\Lambda_c} - \frac{1}{3}\beta + g^2 \frac{m_{\pi}}{4\pi f_{\pi}^2} \\ \mu_{eff} [D^{0*} \to D^0 \gamma] = \frac{2}{3\Lambda_c} + \frac{2}{3}\beta - g^2 \frac{m_K}{4\pi f_K^2} - g^2 \frac{m_{\pi}}{4\pi f_{\pi}^2} \end{bmatrix}$$

$$\Gamma(D^{*+} \to D^0 \pi^+) = \frac{g^2}{6\pi f_\pi^2} |p_\pi|^3$$
$$\Gamma(D^{*0} \to D^0 \pi^0) = \frac{g^2}{12\pi f_\pi^2} |p_\pi|^3$$

$$\begin{array}{l} 0.52 < g < 0.66 \\ 2.0 \, GeV^{-1} < \beta < 4.1 \, GeV^{-1} \\ \end{array}$$

$$\begin{array}{l} 0.19 \, GeV^{-1} < \mu_{eff}(B_s^* \rightarrow B_s \gamma) < 0.53 \, GeV^{-1} \end{array}$$

LIGHT VECTOR RESONANCE

Light Vector Resonance Pole Diagrams : φ(1020)



$$\mathcal{A}(B^0_s \to \mu \bar{\mu} \phi \to \mu \bar{\mu} \gamma_s) = \mathcal{A}(B^0_s \to \mu \bar{\mu} \phi) \times \frac{g_{\mu\nu}}{m_{\phi}^2} \times \mathcal{A}(\phi \to \gamma_s)$$

Leading Contribution

Subleading Contribution (1/M)

LIGHT VECTOR RESONANCE

Light Vector Resonance Pole Diagrams : φ(1020)



Leading Contribution



Subleading Contribution (1/M)

 $\mathcal{A}^{\mu}(\phi \to \gamma_s) = \frac{1}{3} e f_{\phi} m_{\phi} \epsilon^*_{\mu}$

 $\mathcal{A}(B^0_s \to \mu \bar{\mu} \phi \to \mu \bar{\mu} \gamma_s) = \mathcal{A}(B^0_s \to \mu \bar{\mu} \phi) \times \frac{g_{\mu\nu}}{m_{\phi}^2} \times \mathcal{A}(\phi \to \gamma_s)$

LIGHT VECTOR RESONANCE

Light Vector Resonance Pole Diagrams : φ(1020)



Leading Contribution



Subleading Contribution (1/M)

$$\mathcal{A}(B^0_s \to \mu \bar{\mu} \phi \to \mu \bar{\mu} \gamma_s) = \mathcal{A}(B^0_s \to \mu \bar{\mu} \phi) \times \frac{g_{\mu\nu}}{m_{\phi}^2} \times \mathcal{A}(\phi \to \gamma_s)$$

Couple HMxPT to Light Vector Resonances

$$\rho_{\mu} \equiv i \frac{g_{V}}{\sqrt{2}} \begin{pmatrix} \frac{\rho^{0}}{\sqrt{2}} + \frac{\omega}{\sqrt{2}} & \rho^{+} & K^{*+} \\ \rho^{-} & -\frac{\rho^{0}}{\sqrt{2}} + \frac{\omega}{\sqrt{2}} K^{*0} \\ K^{*-} & \bar{K}^{*0} & \phi \end{pmatrix}$$

$$\begin{split} L_{1a}^{\mu\nu} &= i\alpha_1 \left\{ g^{\mu\alpha} g^{\nu\beta} - \frac{i}{2} \epsilon^{\mu\nu\alpha\beta} \right\} \langle \gamma_5 H_b \left[\gamma_\alpha (\rho_\beta - \mathcal{V}_\beta)_{bc} - \gamma_\beta (\rho_\alpha - \mathcal{V}_\alpha)_{bc} \right] \xi_{ca}^{\dagger} \rangle \\ \\ L_{1a}^{\mu} &= \alpha_1 \langle \gamma_5 H_b (\rho^\mu - \mathcal{V}^\mu)_{bc} \xi_{ca}^{\dagger} \rangle \end{split}$$
 First order in 1/M and derivitaves.

Next Step : Bremsstrahlung

BREMSSTRAHLUNG

Bremsstrahlung

- Photon is emitted from final state leptons
 - Creates an IR divergence
 - Interferes with our region of interest



• IR divergence cancelled by 1-Loop QED Corrections to $B^0_s \to \mu^+ \mu^-$

BREMSSTRAHLUNG

Bremsstrahlung

- Photon is emitted from final state leptons
 - Creates an IR divergence
 - Interferes with our region of interest



• IR divergence cancelled by 1-Loop QED Corrections to $B^0_s \to \mu^+\mu^-$



BREMSSTRAHLUNG

Bremsstrahlung

- Photon is emitted from final state leptons
 - Creates an IR divergence
 - Interferes with our region of interest



• IR divergence cancelled by 1-Loop QED Corrections to $B^0_s \to \mu^+ \mu^-$



RESULTS

Preliminary Results (Without 1-Loop QED Corrections)

Use Lower Energy cut of 10 MeV

$$Br(B_s^0 \to \mu^+ \mu^-)_{exp} = Br(B_s^0 \to \mu^+ \mu^-)_{SM} (1 + R_{\gamma_s})$$



RESULTS

Preliminary Results (Without 1-Loop QED Corrections)

• Use Lower Energy cut of 10 MeV

 $Br(B_s^0 \to \mu^+ \mu^-)_{exp} = Br(B_s^0 \to \mu^+ \mu^-)_{SM} (1 + R_{\gamma_s})$



CONCLUSIONS

$$Br(B_s^0 \to \mu^+ \mu^-)_{exp} = Br(B_s^0 \to \mu^+ \mu^-)_{SM} (1 + R_{\gamma_s})$$

- Soft photons that are not discernable by detectors can amplify SM contributions to the $B_s^0 \to \mu^+ \mu^-$ decay width
 - Depending on experimental photon cuts the contribution R_{γ_s} can be large.
 - CDFII, CMS, LHCb ~ 8%
 - ATLAS, D0 > 15%

Thank You.