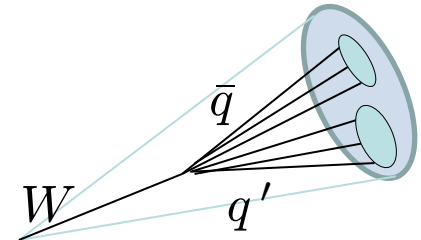
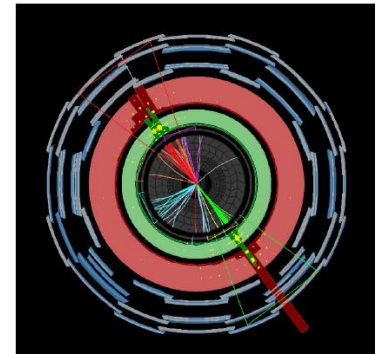
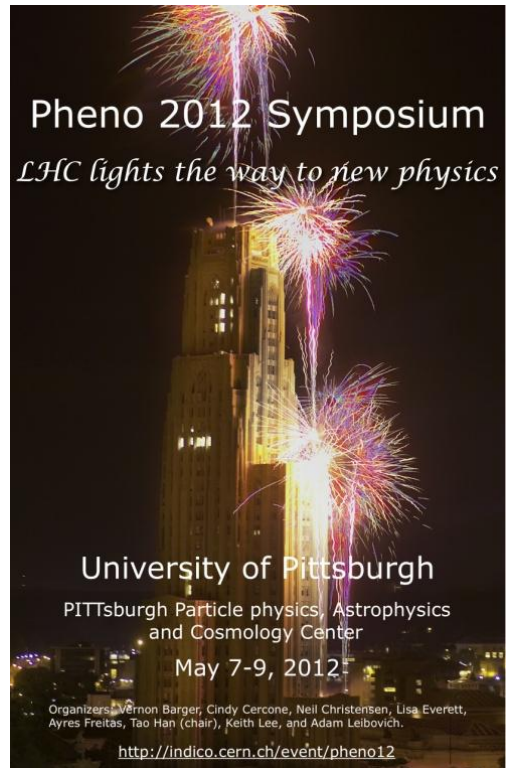
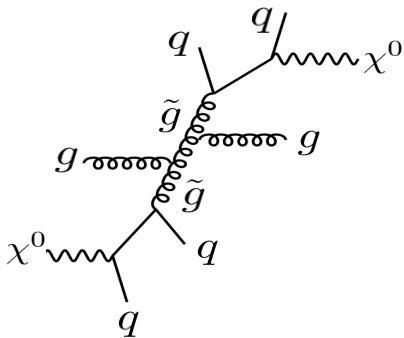
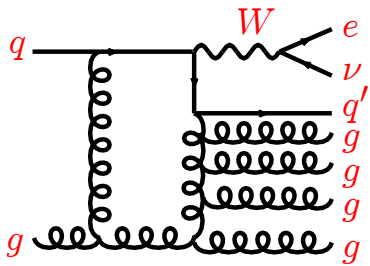


Perturbative QCD at the LHC

Pheno 2012 Symposium
Pittsburgh, May 7, 2012
Zvi Bern, UCLA



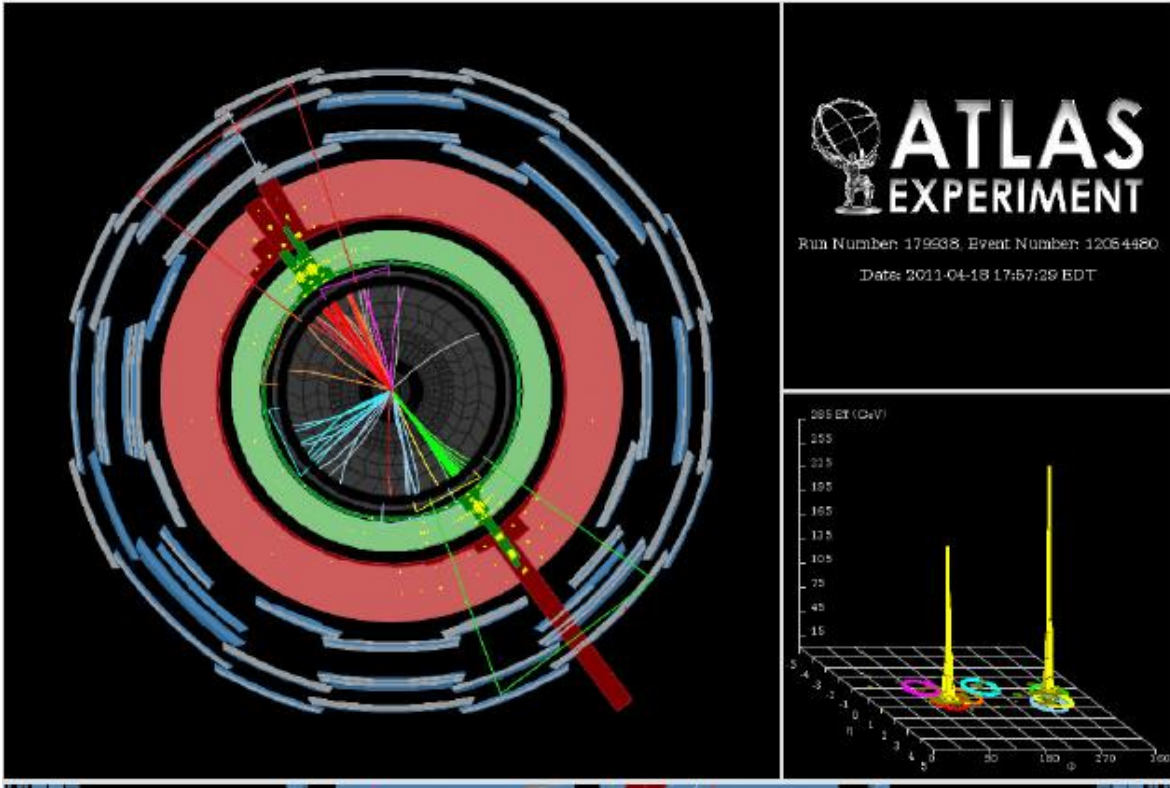
Outline

- **Some new developments in QCD for understanding LHC physics.**
- **Examples of QCD in results such as susy exclusions and Higgs boson.**

Vast field. Impossible to cover everything in a half an hour, so I will just show a few examples of recent progress.

Apologies to the many who's important work I will gloss over or skip.

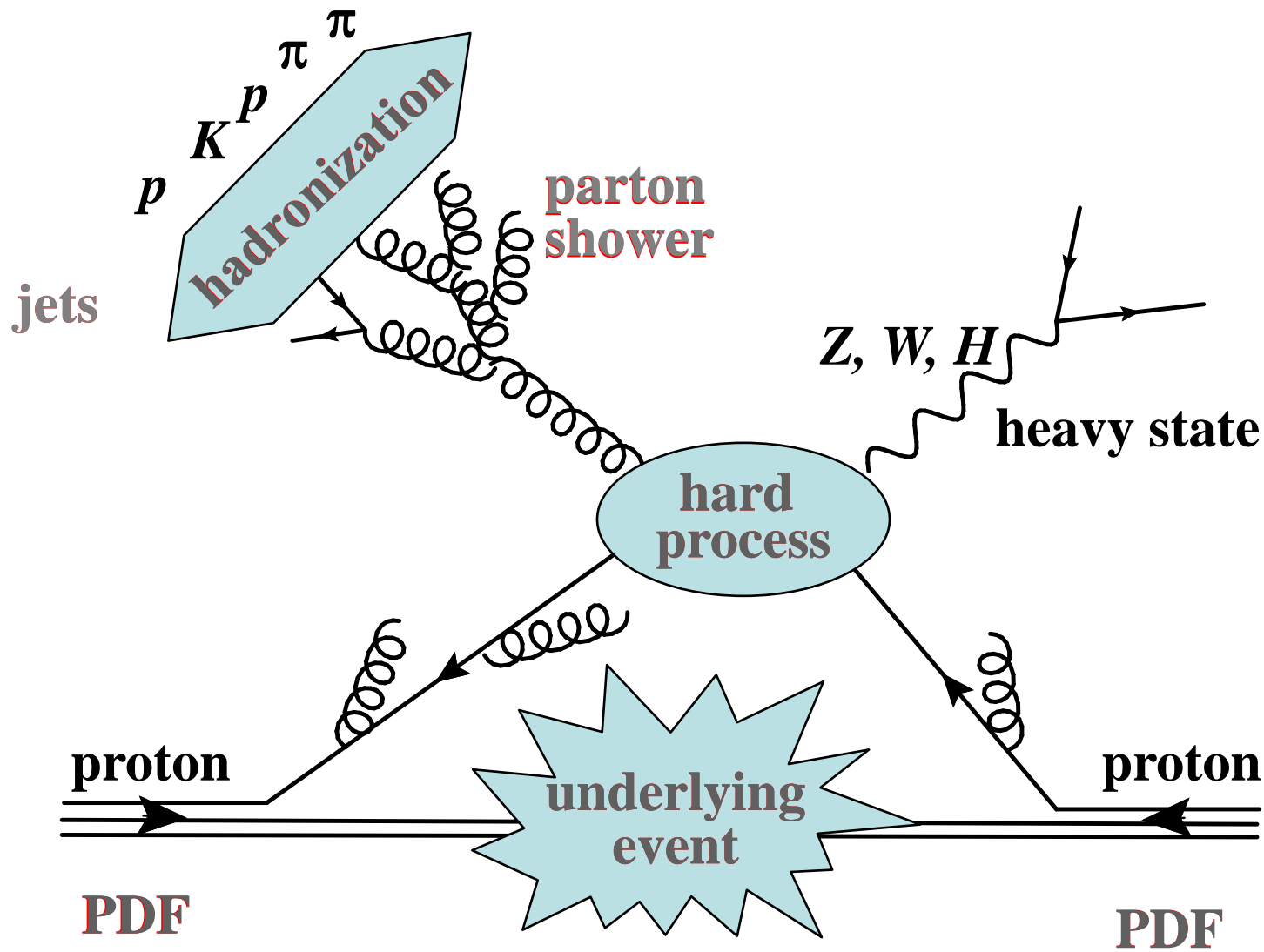
Experimenter's View of LHC Collision



Note jets

To properly interpret we need QCD

Theorist's View of LHC Collision



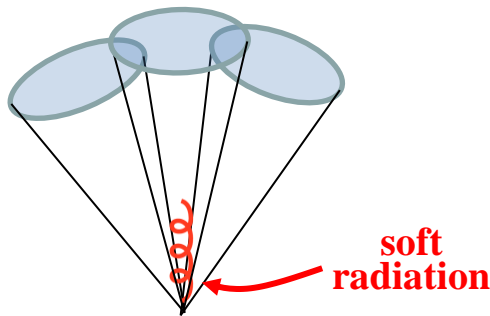
Complicated environment: many aspects of QCD must be understood

Standard QCD Tools for Experimenters

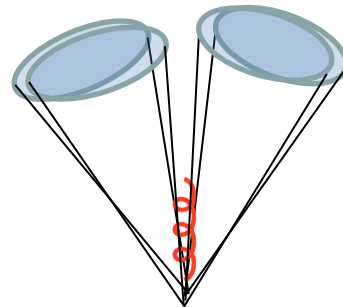
Many important theoretical tools used by experimenters: Pythia, Herwig, Alpgen, Madgraph, Sherpa, Alpgen, MC@NLO, POWHEG, etc. Many important improvements in recent years.

In this talk I will focus on recent examples of *precision QCD calculations* for hadron colliders, especially examples aiding the search for new physics.

An important ingredient underlying precision physics with jets at the LHC are *infrared safe* jet algorithms used by both CMS and ATLAS. Without these, problematic to compare to QCD.



not infrared safe



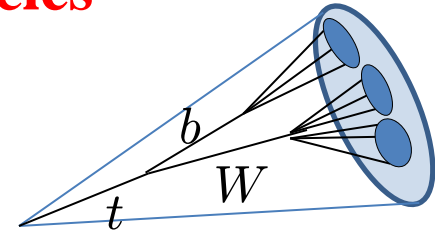
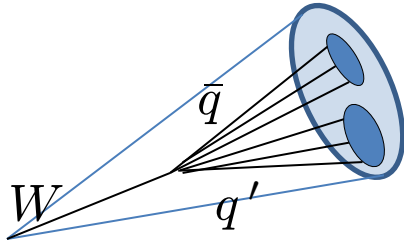
infrared safe

**FastJet package
supplies IR safe
algorithms**

Cacciari, Salam, Soyez

Boosted Objects and Jet Substructure

Use jet substructure to identify heavy particles



Clean up jets to expose heavy particles in jet substructure:

- **Filtering:** undo last recombinations and keep main subjects.

Butterworth, Davison, Rubin, Salam (arXiv:0802.2470)

- **Trimming:** remove regions in a jet with too little energy.

Krohn, Thaler and Wang (arXiv:0912.1342)

- **Pruning:** take a jet and recluster it removing asymmetric wide angle recombinations

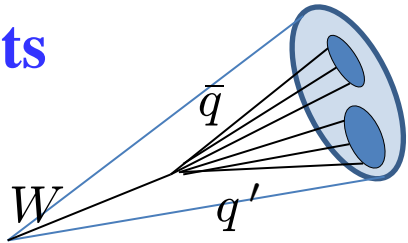
Ellis, Vermilion, Walsh (arXiv:0903.5081, arXiv:0912.0033)

Improves resolution by removing soft, large-angle particles from jet

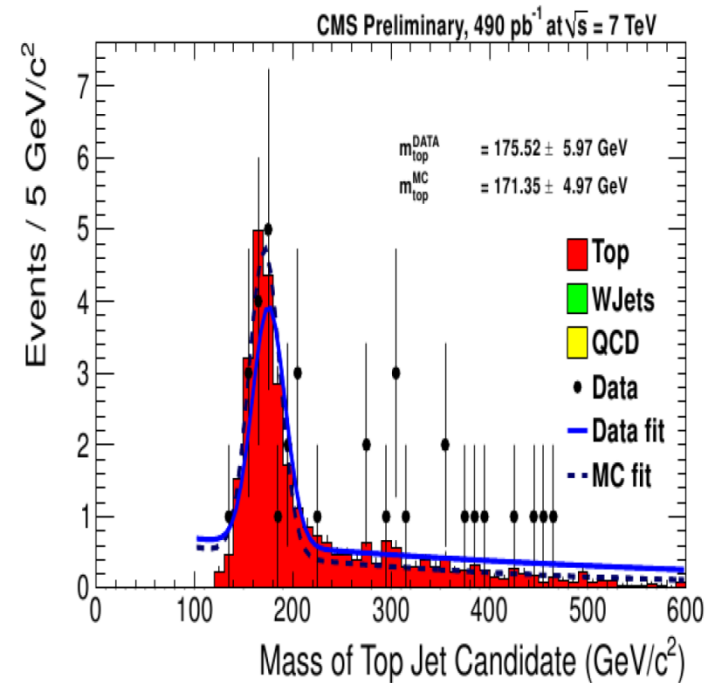
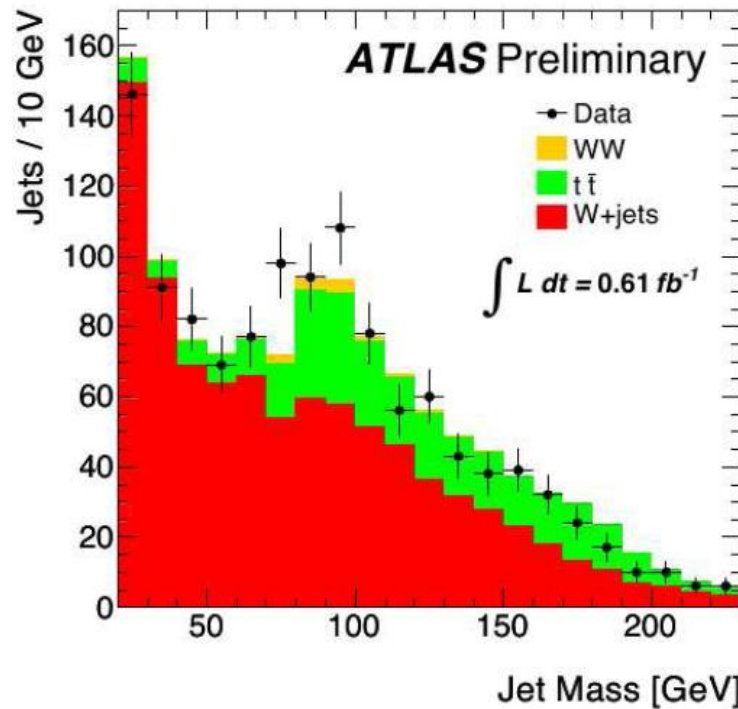
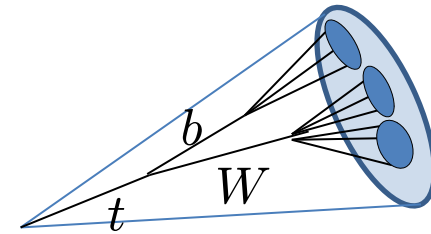
Many others have contributed: Almeida, Cacciari, Chen, Erdogan, Falkowski, Han, Hook, Jankowiak, Juknevich, Katz, Kim, Kribs, Larkoski, Lee, Martin, Nojiri, Perez, Plehn, Raklev, Rehermann, Roy, Rojo, Shelton, Sreethawong, Son, Soyez, Sung, Tweedie, Schwartz, Seymour, Soper, Spannowsky, Sterman, van Tilburg, Virzi, Wacker, Wang, Zhu, etc.

Experimental Progress on Boosted Objects and Jet Substructure

W jets



top jets

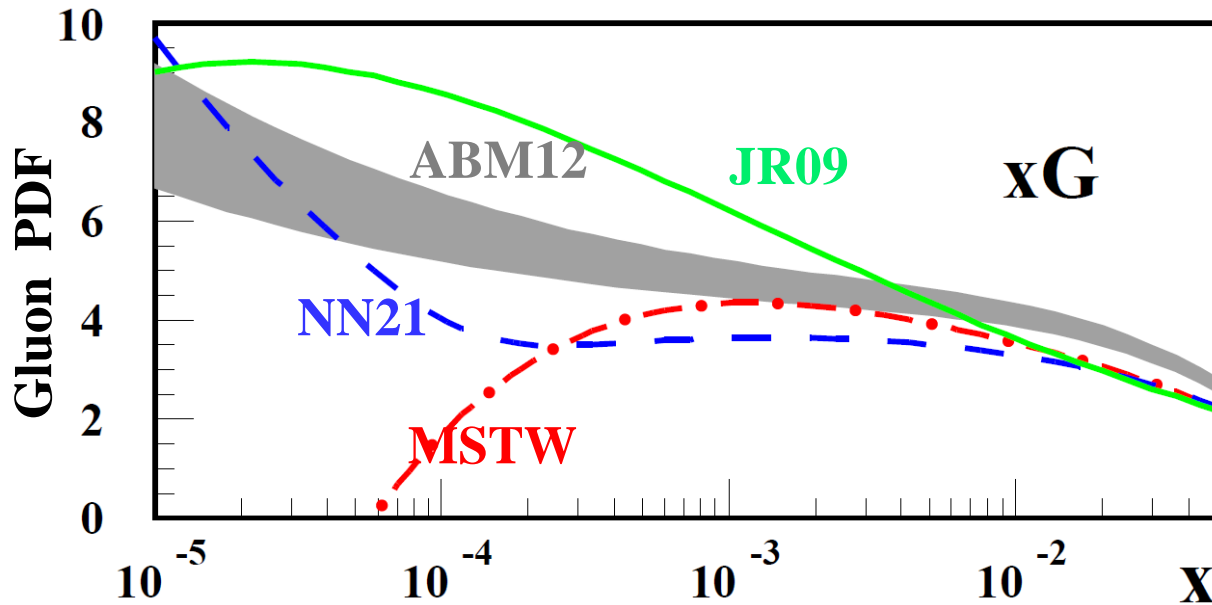


Offers a new window to search for new heavy mass states decaying into jets, previously thought to be inaccessible due to QCD background.

PDF Issues and Higgs

What's up with the gluons?

Alekhin, Blumlein, Moch (arXiv:1202.2281)



disagreement
outside quoted
errors

The discrepancy due to use of different data sets
and treatment of power corrections. α_s low for ABM

m_H	ABM11	ABKM09	JR09	MSTW	NN21
125	16.99 ^{+1.69 +0.37} _{-1.63 -0.37}	16.87 ^{+1.68 +0.47} _{-1.63 -0.47}	16.53 ^{+1.54 +0.53} _{-1.44 -0.53}	18.36 ^{+1.92 +0.21} _{-1.82 -0.28}	19.30 ^{+2.09 +0.26} _{-1.89 -0.26}

Up to 15% effect on the Higgs cross section at 8 TeV

Illustrates the crucial importance of getting the PDF's right.

Why We Do Higher-Order QCD Calculations

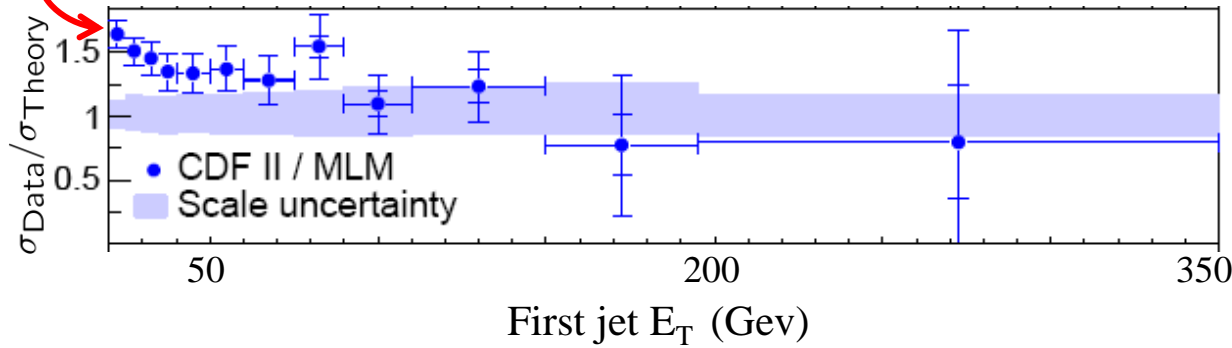
Classic example of the use of higher order QCD

note
disagreement

W + 2 jets at the Tevatron

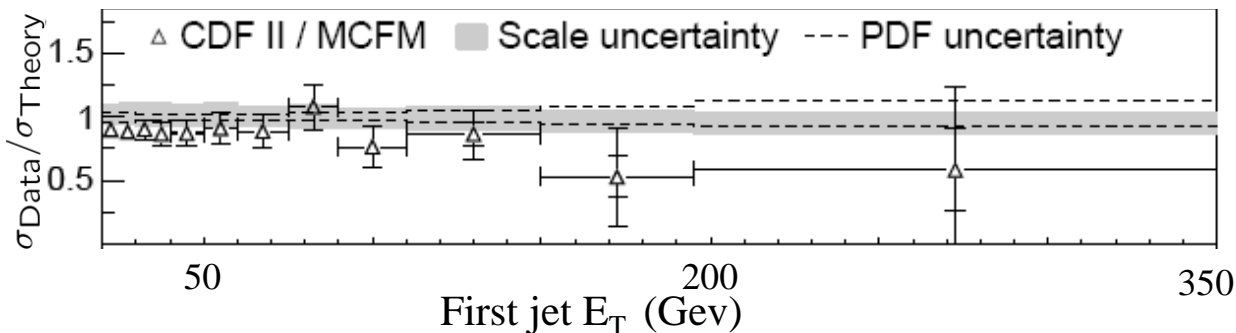
CDF collaboration
arXiv: 0711.4044

LO



leading order +
parton showering

NLO
QCD



NLO does better,
smallest theoretical
uncertainty

Higher order QCD can resolve discrepancies between theory and experiment.

Data Driven Background Estimation

CMS uses photons to estimate Z background to susy searches.

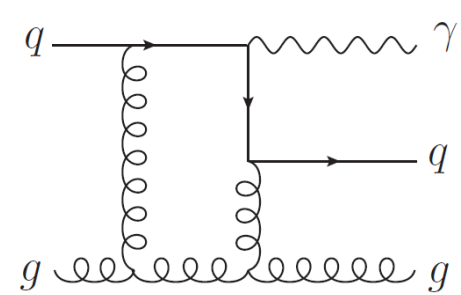
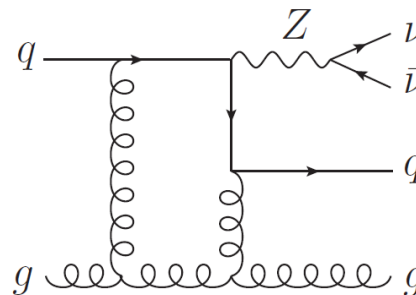
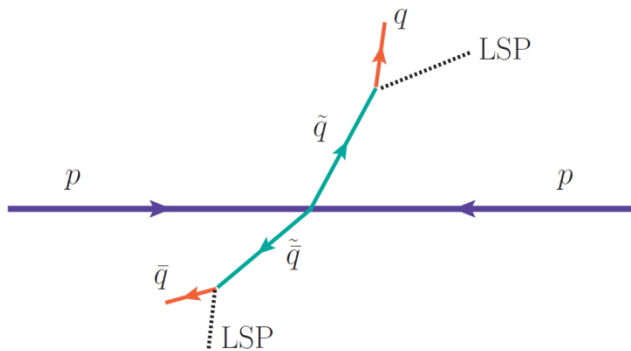
CMS PAS SUS-08-002; CMS PAS SUS-10-005; arXiv:1106.4503

$$\sigma(pp \rightarrow Z(\rightarrow \nu\bar{\nu}) + \text{jets}) = \sigma(pp \rightarrow \gamma + \text{jets}) \times R_{Z/\gamma}$$

irreducible background

measure this

ratio is theory input



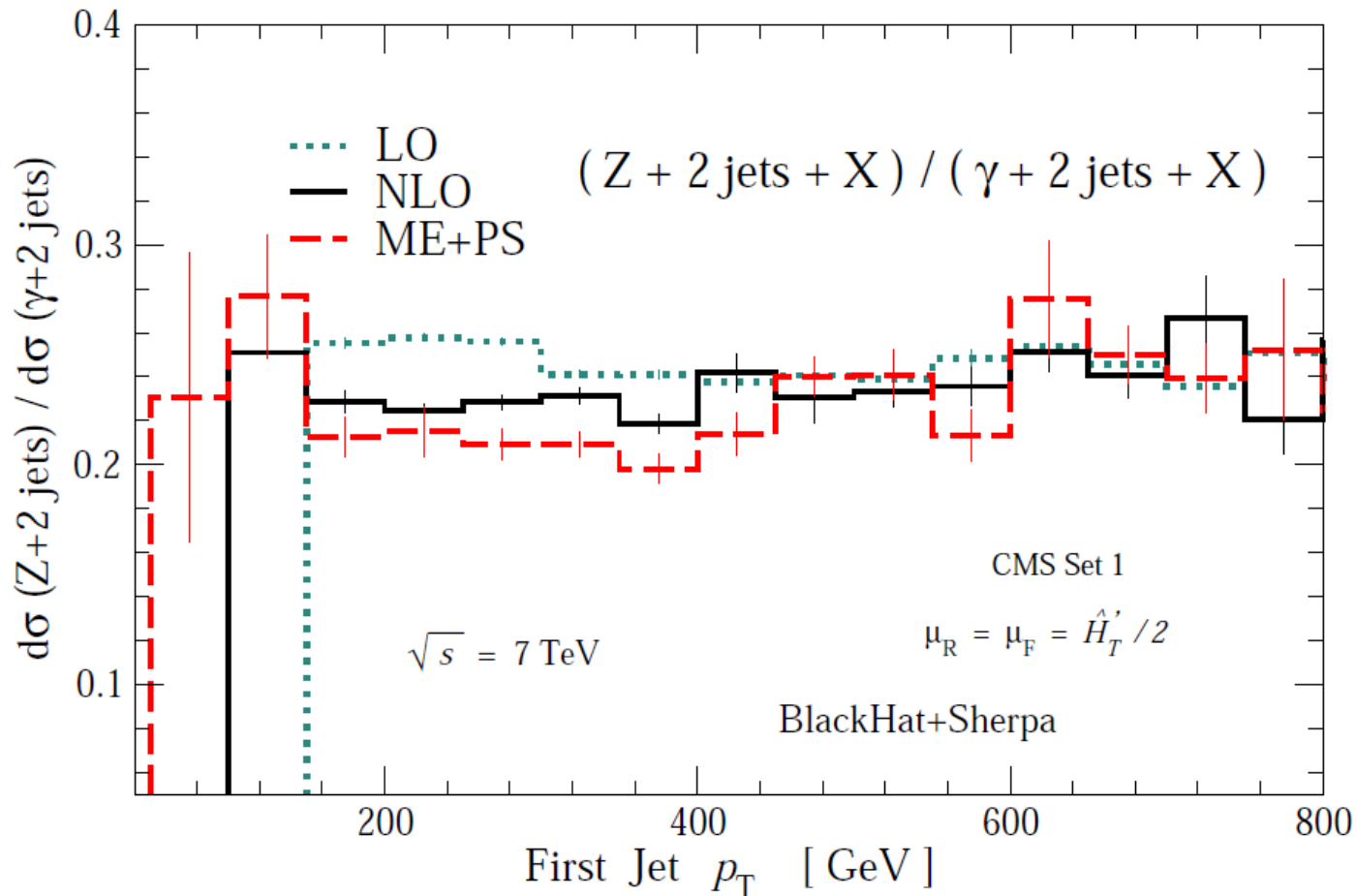
Photons have better statistics than $Z \rightarrow \mu\bar{\mu}$

Task of theorist was to theoretically understand conversion and give *theoretical uncertainty* to CMS.

ZB, Diana, Dixon, Febres Cordero, Hoche, Ita, D.A. Kosower, D. Maitre, Ozeren (arXiv:1106.1423)
Ask, Parker, Sandoval, Shea, Stirling (arXiv:1107.2803)

Z/ γ ratio

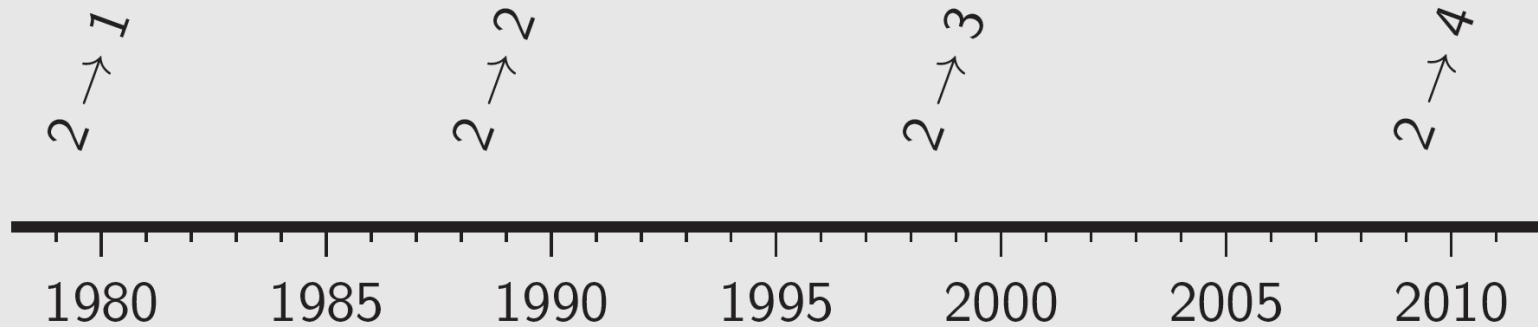
BlackHat Collaboration



Different theoretical predictions track each other.
This conversion directly used by CMS in their estimate of theory uncertainty in susy search.

The NLO revolution

G. Salam, ICHEP 2010



2009: NLO $W+3j$ [Rocket: Ellis, Melnikov & Zanderighi]

[unitarity]

2009: NLO $W+3j$ [BlackHat: Berger et al]

[unitarity]

2009: NLO $t\bar{t}b\bar{b}$ [Bredenstein et al]

[traditional]

2009: NLO $t\bar{t}b\bar{b}$ [HELAC-NLO: Bevilacqua et al]

[unitarity]

2009: NLO $q\bar{q} \rightarrow b\bar{b}b\bar{b}$ [Golem: Binoth et al]

[traditional]

2010: NLO $t\bar{t}jj$ [HELAC-NLO: Bevilacqua et al]

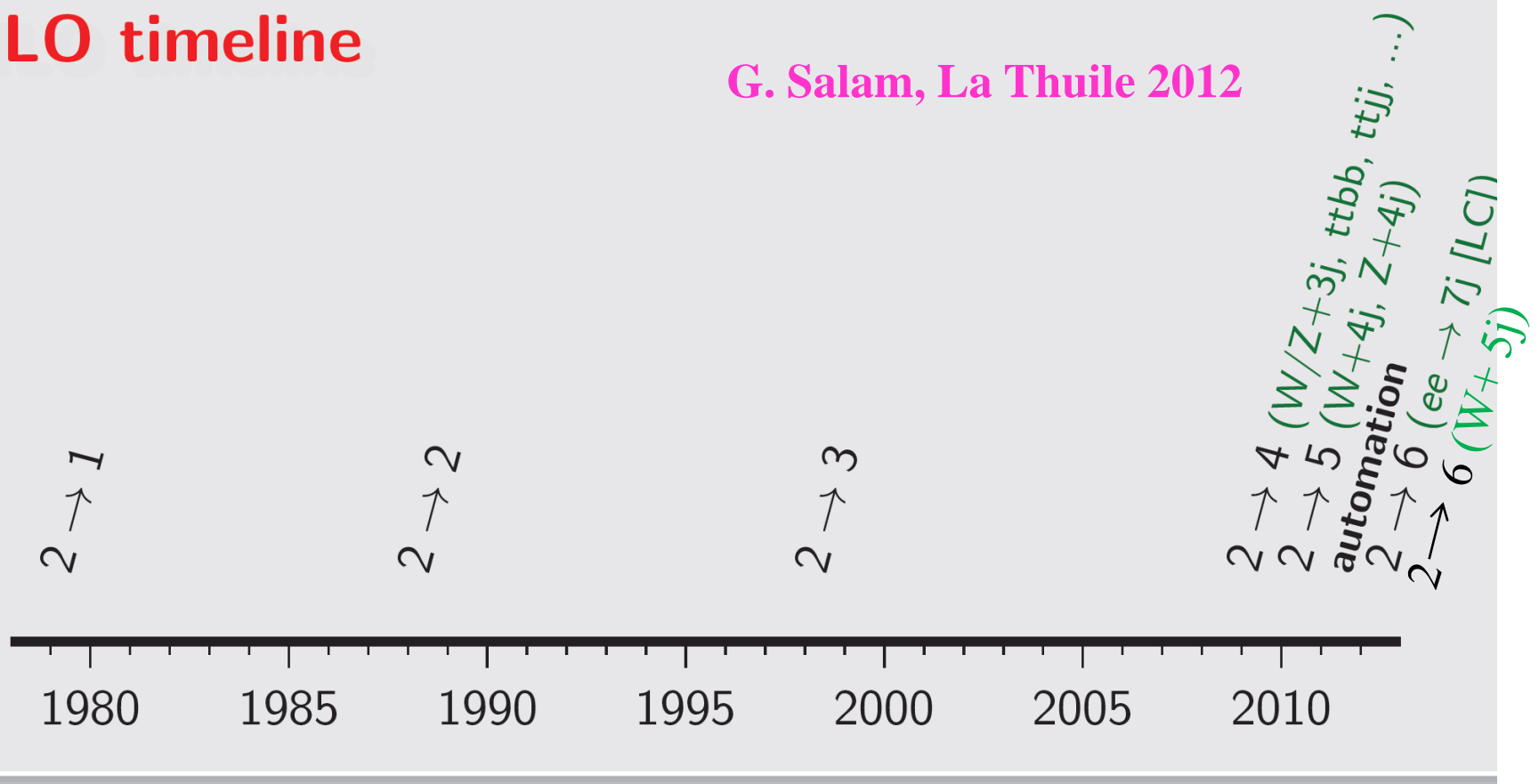
[unitarity]

2010: NLO $Z+3j$ [BlackHat: Berger et al]

[unitarity]

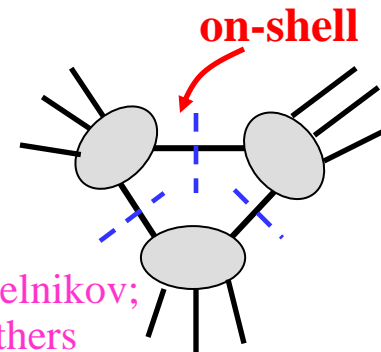
NLO timeline

G. Salam, La Thuile 2012



- 2010: NLO $W+4j$ [BlackHat+Sherpa: Berger et al] [unitarity]
- 2011: NLO $WWjj$ [Rocket: Melia et al] [unitarity]
- 2011: NLO $Z+4j$ [BlackHat+Sherpa: Ita et al] [unitarity]
- 2011: NLO $4j$ [BlackHat+Sherpa: Bern et al] [unitarity]
- 2011: first automation [MadNLO: Hirschi et al] [unitarity + feyn.diags]
- 2011: first automation [Helac NLO: Bevilacqua et al] [unitarity]
- 2011: first automation [GoSam: Cullen et al] [feyn.diags(+unitarity)]
- 2011: $e^+e^- \rightarrow 7j$ [Becker et al, leading colour] [numerical loops]
- 2012: NLO $W+5j$ [BlackHat, preliminary] [unitarity]

Some Advances



- **On-Shell Revolution. A different way to do QFT.**

ZB, Dixon, Dunbar, Kosower ; ZB, Morgan; ZB, Dixon, Kosower;
Britto, Cachazo and Feng; Anastasiou, Britto, Feng, Kunszt, Mastroliia;
Giele, Kunszt, Melnikov; Badger; Ossola, Papadopoulos, Pittau; Giele, Kunszt, Melnikov;
Forde; Berger, ZB, Kosower, Forde, Gleisberg, Hoeche, Ita, Maitre, Ozeren; & others

- **Improved efficiency in Feynman diagram methods.**

Bredenstein, Denner, Dittmaier, Pozzorini; Cascioli , Maierhofer, and Pozzorini.

- **New purely numerical approach.**

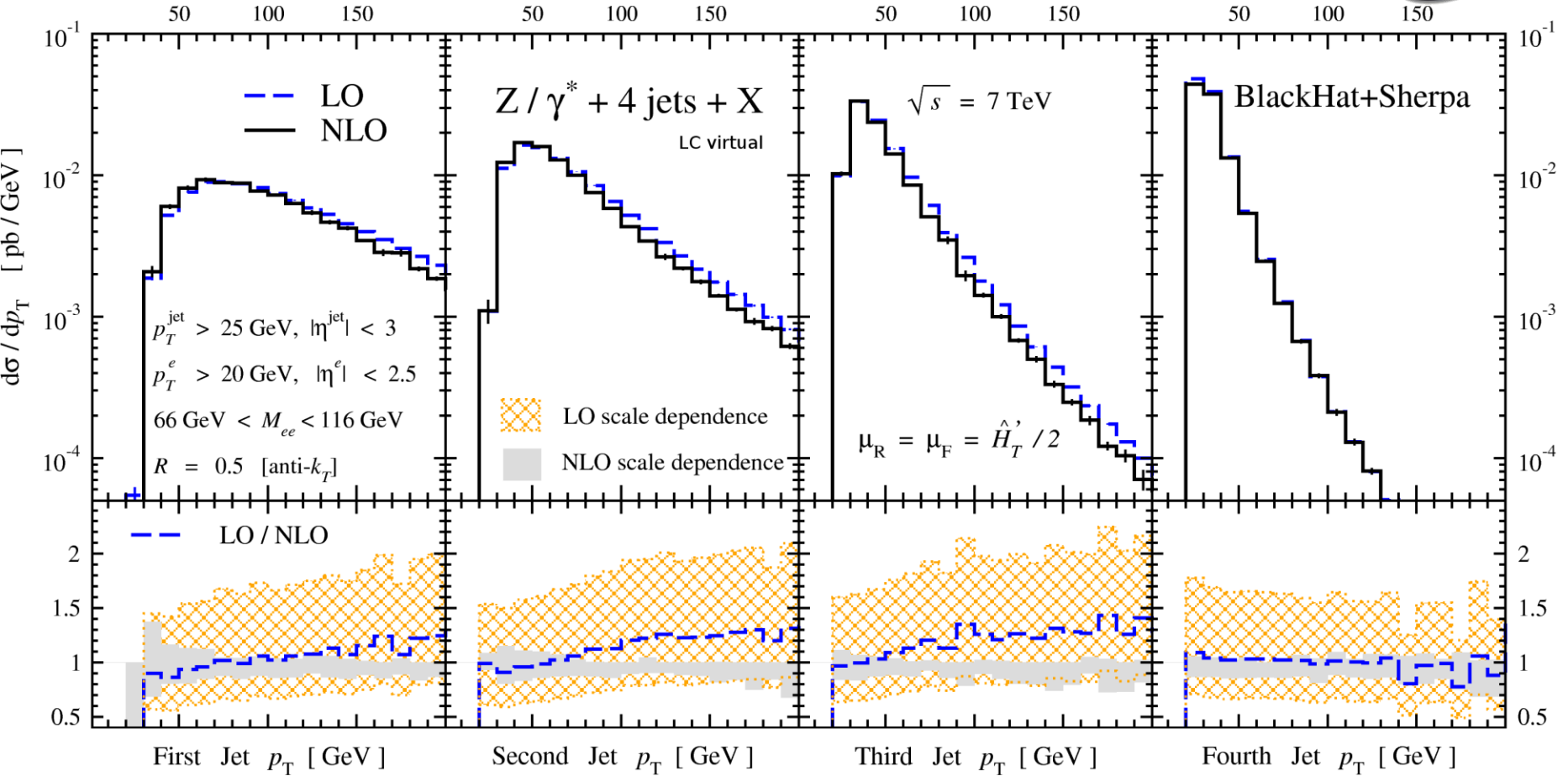
Becker, Goetz, Reuschle, Schwan, Weinzierl

Some of the new packages using modern ideas:

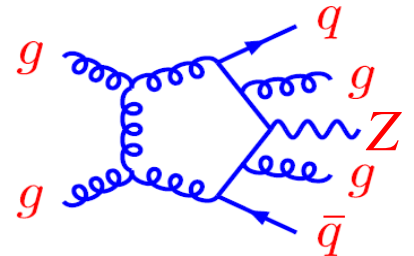
- **Helac-NLO** Bevilacqua, Czakon, Garzelli, van Hameren, Kardos, Ossola, Papadopoulos, Pittau, Worek
- **CutTools** Ossola, Papadopoulos, Pittau
- **BlackHat** ZB, Dixon, Febres Cordero, Hoeche, Ita, Kosower, Maitre, Ozeren
- **Rocket** Ellis, Giele, Kunszt, Melnikov, Zanderighi
- **SAMURAI** Mastroliia, Ossola, Reiter, Tramontano
- **MadLoop** Hirchi, Maltoni, Frixione, Frederix, Garzelli, Pittau
- **GoSam** Cullen, Greiner, Heinrich, Luisoni, Mastroliia, Ossola, Reiter, Tramontano
- **Ngluon** Badger, Biedermann, Uwer

Z+4 Jets at NLO

[BlackHat] Ita, ZB, Febres Cordero, Dixon, Kosower, Maitre (2011)

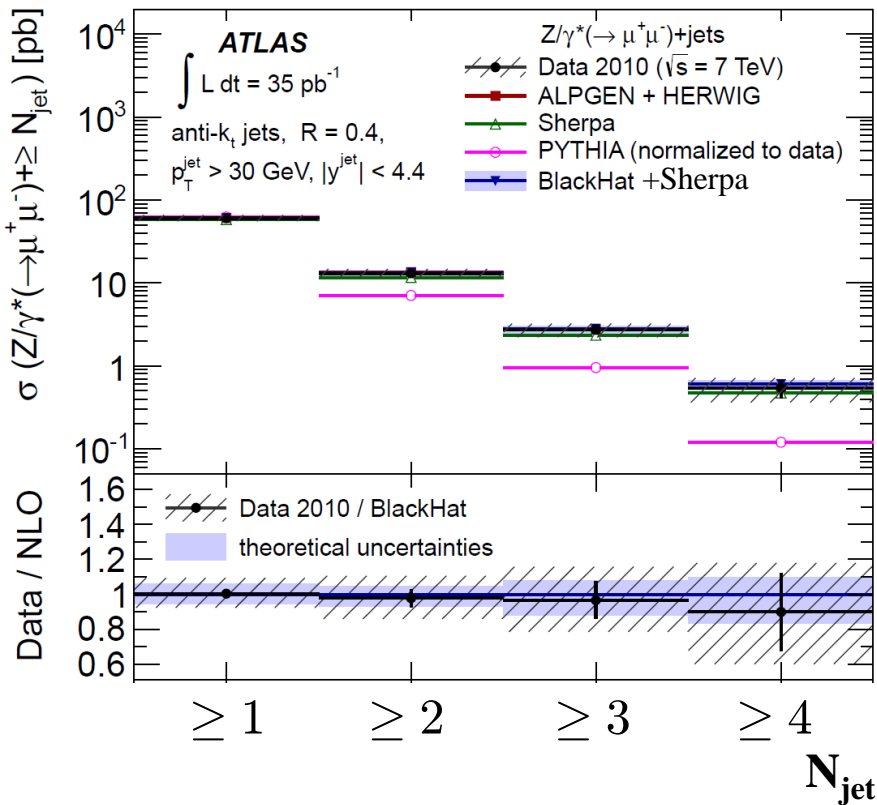


- Big improvement in scale stability.
- Best available theoretical predictions.



ATLAS Comparison Against NLO QCD

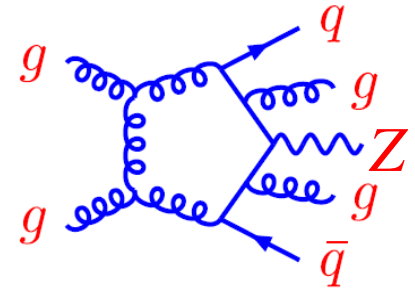
Z + 1, 2, 3, 4 jets inclusive



Powerful experimental confirmation of NLO approach. With these experimental cuts no new physics is expected.

We look forward to higher precision data.

very good agreement

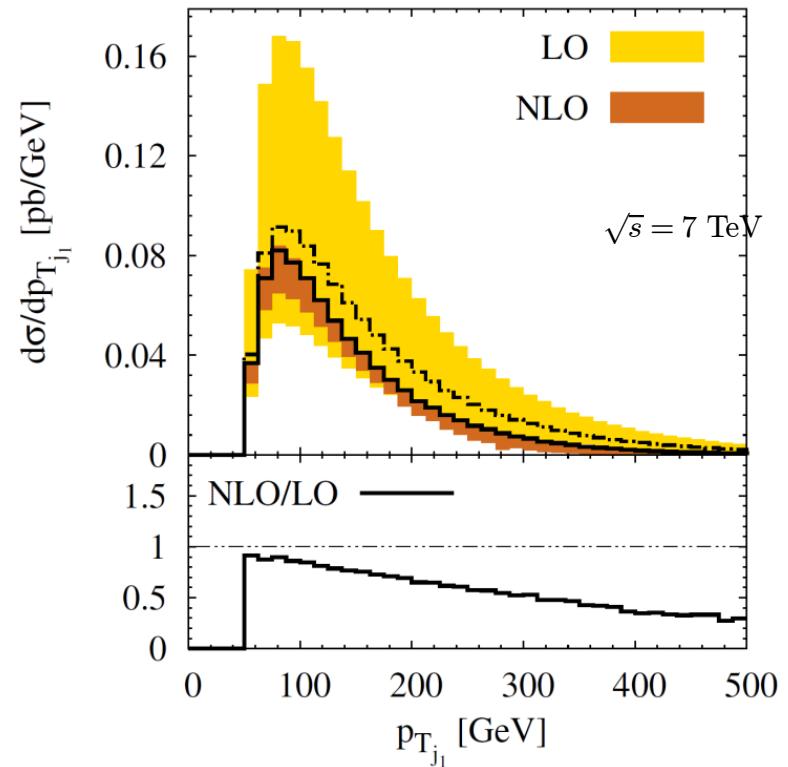
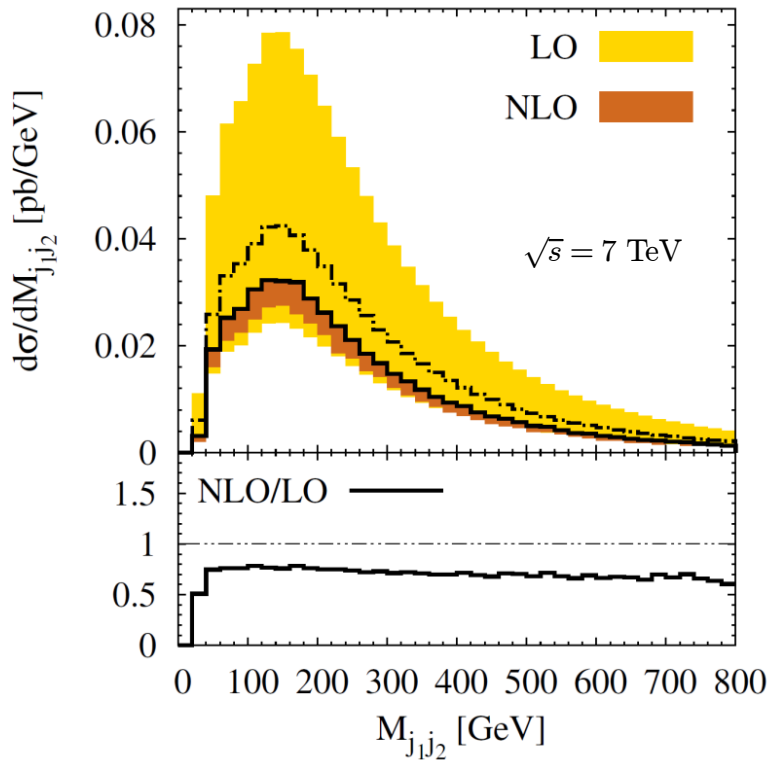


- **Even $W+5$ jets at NLO nearly complete.** see **K. Ozeren's talk at LoopFest**
- **Serious advance in our ability to do NLO calculations.**

Recent Advances in NLO

Bevilacqua, Czakon, Papadopoulos, Worek (arXiv: 1108.2851)

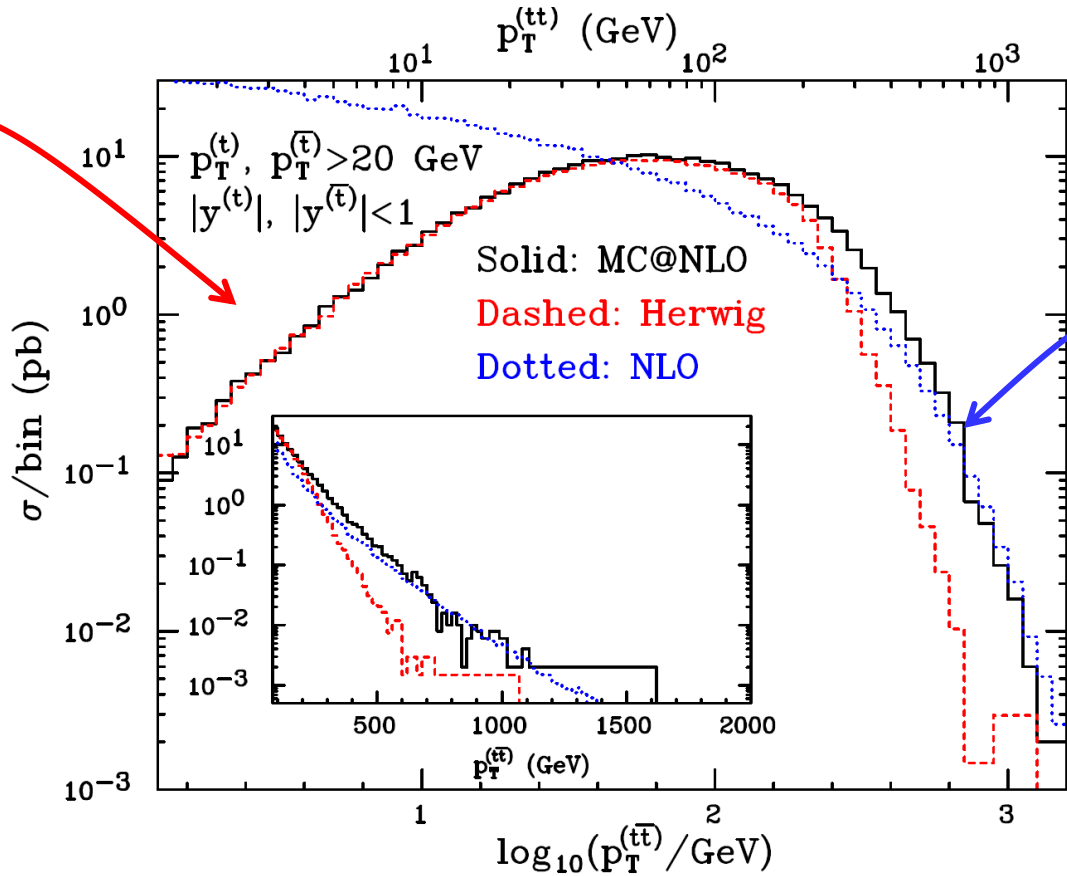
A very nice example from HELAC-NLO: $tt + 2$ jet production



Besides the enormous reduction in scale uncertainty, large changes in shape between LO and NLO are evident for some distributions.

Merging NLO with Parton Showers

Frixione, Nason and Webber (hep-ph/0305252)



matches shower at low p_T

matches NLO at high p_T

MC@NLO uses Herwig

Classic example of utility of NLO + parton showers

By Merging NLO with Parton showers we get advantages of both

Merging NLO with Parton Showers

- Want to simultaneously have advantages of both NLO and parton showers.
- Nontrivial technical issues, e.g must remove double counting.

Impressive new progress from many groups

- MC@NLO

Frixione, Webber, et al

- POWHEG

Frixione, Nason, Oleari, Alioli, Re. Melia, Nason, Rontsch, Zanderighi

- SHERPA

Hoeche, Krauss, Schoenherr, Siegert

- VINCIA

Giele, Kosower, and Skands, et al.

- GENeVa

Bauer, Tackman, Thaler, et al.,

- aMC@NLO

Frederix, Frixione, Hirschi, Maltoni, Pittau, Torrielli

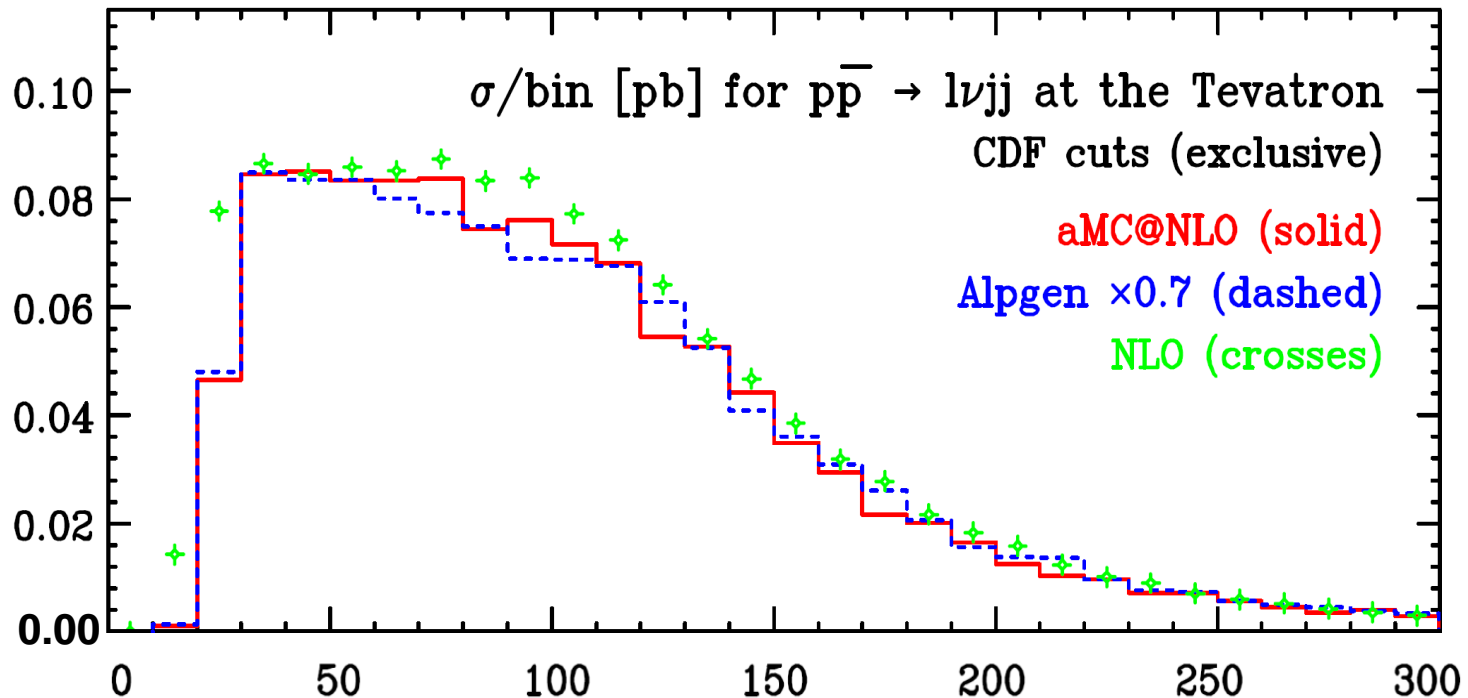
- KRKMC

Skrzypek, Jadach, Kusina, Placzek, Slawinska, Gituliar

Merging NLO with Parton Showers

Frederix, Frixione, Hirschi, Maltoni, Pittau, Torrielli (arXiv:1110.5502)

A key application of NLO + parton showers has been to look at CDF dijet anomaly. See talk from Frederix



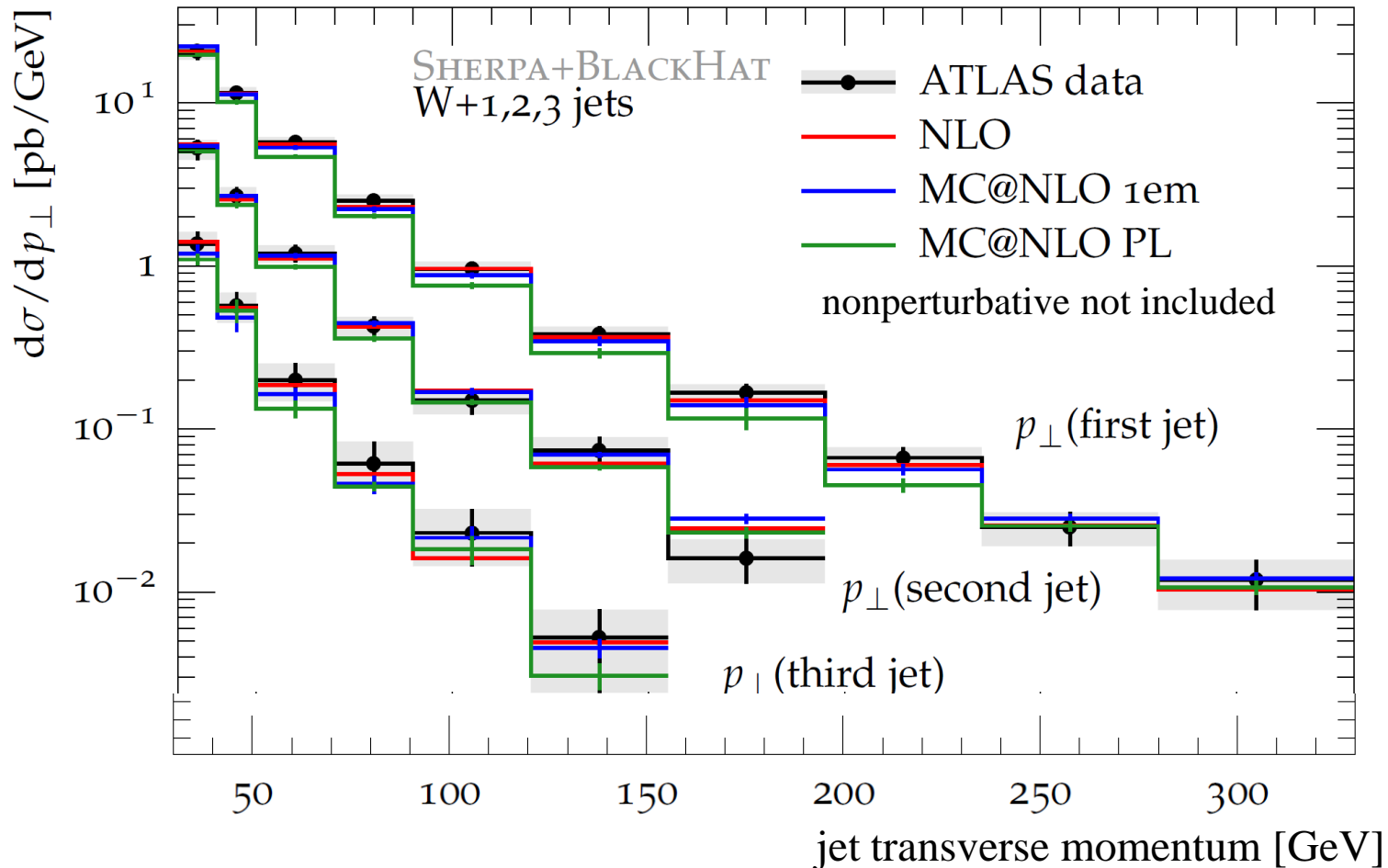
- CMS used Alpgen (scaled). NLO has a slightly different shape.
- aMC@NLO is close to Alpgen, so it looks that QCD is under good control.

Merging NLO with Parton Showers

Recent state-of-the-art example

Hoeche, Krauss, Schoenherr, Siegert

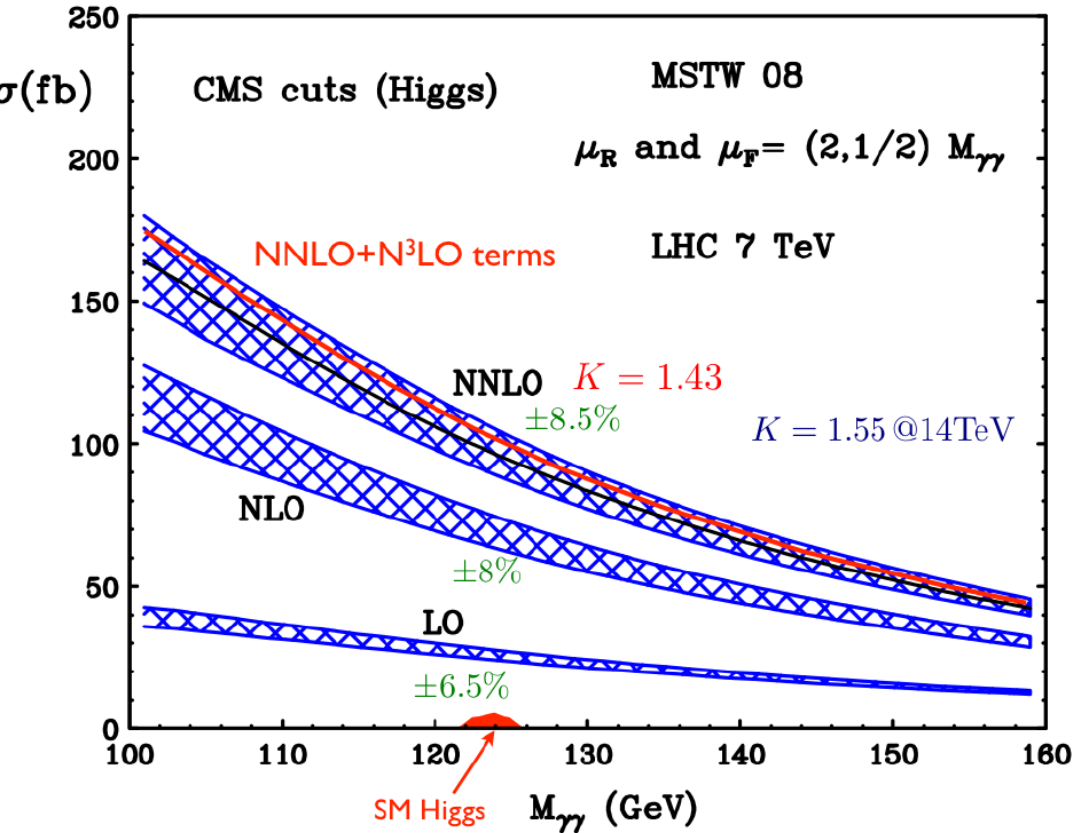
Jet transverse momenta



Nontrivial example of $W+3$ jets based on MC@NLO framework

NNLO QCD: $\gamma\gamma$ Background to Higgs

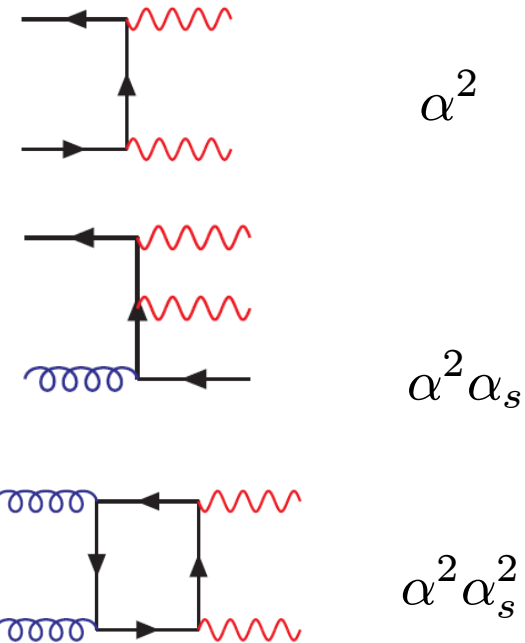
Catani, Cieri, de Florian, Ferrera, Grazzini



- Example where NNLO is really required.
- By NNLO all channels open.
- Known N^3LO terms don't cause large shift.

ZB, Dixon, Schmidt

When new large luminosity channels open at high orders, low order predictions will be unreliable.

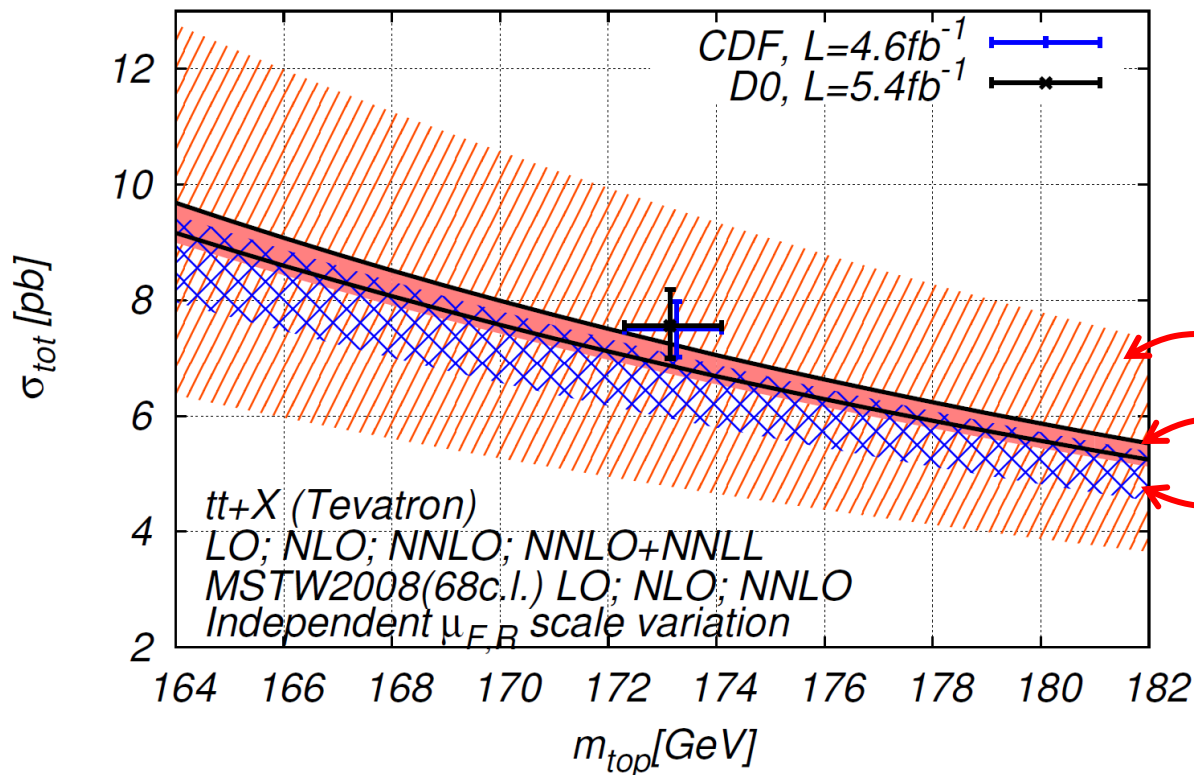


LHC is glue factory so box contribution is same order as born

Top Production at Tevatron

Recent paper demonstrates the remarkable power of NNLO (here combined with NNLL resummation).

Barnreuther, Czakon and Mitov (arXiv:1204.5201)



$$\bar{q}q \rightarrow \bar{t}t + X$$

contributions at NNLO
Sufficient for Tevatron

First complete NNLO calculation with four colored partons

LO

NNLO

NLO

Will be useful for understanding A_{FB}

Theoretical uncertainties smaller than experimental ones.

~ 3% perturbative uncertainty

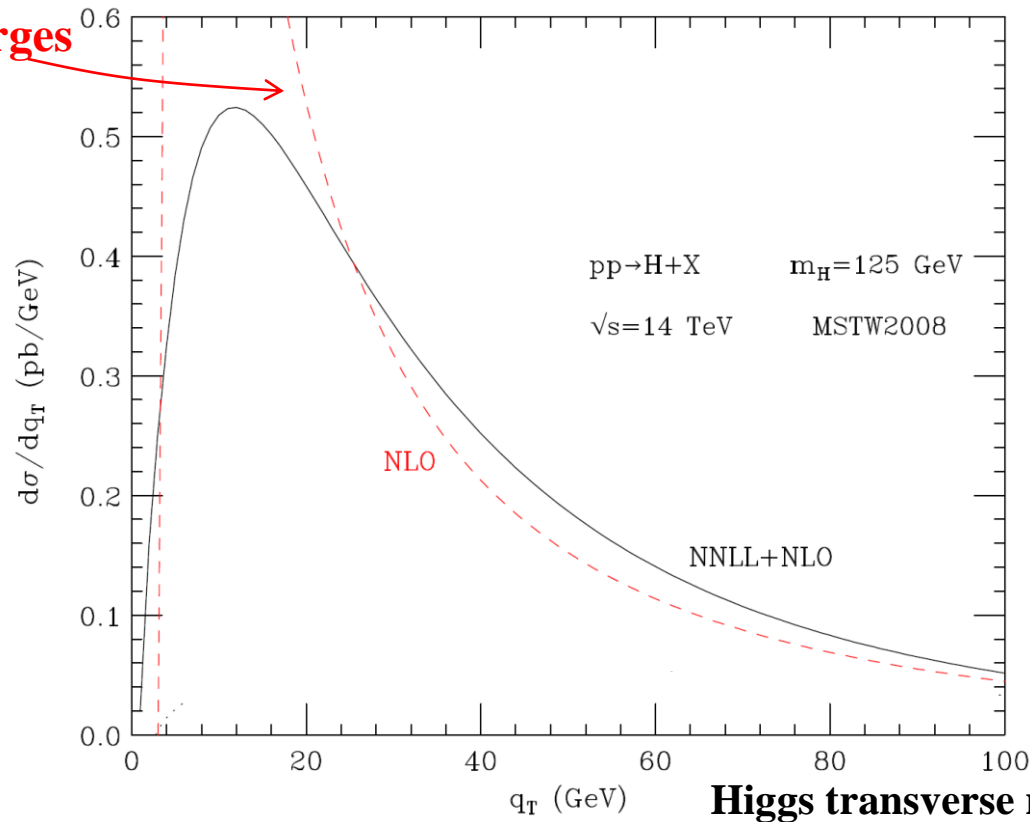
Resummation Application to Higgs

Large logs for small transverse momentum, q_T , of Higgs: $\text{Log}(q_T^2/M_H^2)$

Either use parton shower program or carry out resummation of logs.

de Florian, Ferrera, Grazzini, Tommasini (arXiv: 1109.2109)

fixed order diverges



Recent example of NNLL resummation matched to NLO QCD

See also Ahrens, Becher, Neubert and Yang (arXiv:1008.3162) with N³LL

Generalized Resummations

- Other large logs can lurk in perturbative expansion, e.g. large rapidities.
- Need to resum large logs whenever they occur.
- One approach called soft collinear effective theory (SCET) provides a systematic formalism.

SCET: Bauer, Fleming, Pirjol, Luke, Stewart, etc

Nice example of jet physics work being done here in Pittsburgh

Recent example: jet broadening at LEP.

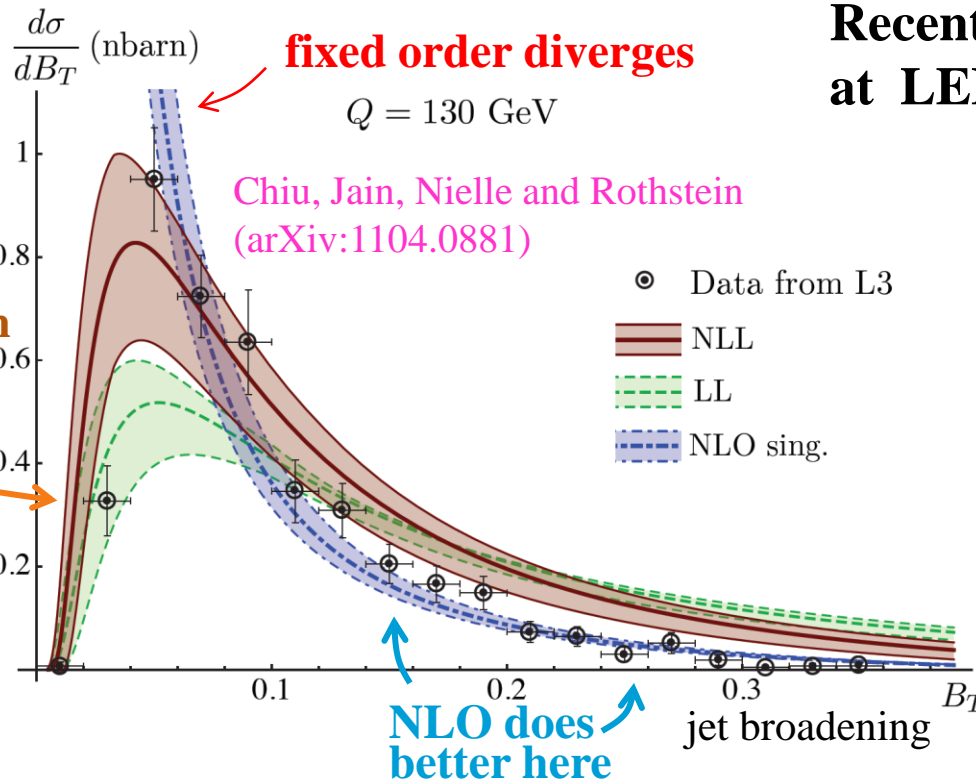
$$B_T = \frac{1}{2} \sum_i \left| \frac{\vec{p}_{i\perp}}{\sqrt{s}} \right|$$

NLO gives naked log

$$\frac{d\sigma}{dB_T} = \sigma_0 \frac{\alpha_s(\mu) C_F}{\pi B_T} (-3 - 4 \log B_T)$$

Resummation fixes it

$$\frac{d\sigma}{dB_T} = \frac{\sigma_0}{B_T} \frac{U_H(Q^2, \mu_Q, \mu)}{\Gamma(2\omega_s) e^{2\gamma_E \omega_s}} \left(\frac{QB_T}{\mu} \right)^{2\omega_s}$$



Resummation ideas can be applied broadly when large logs encountered

Summary

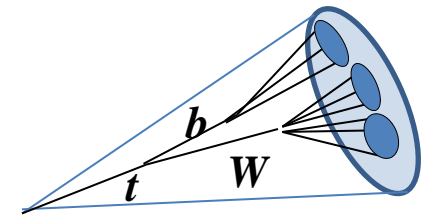
- **QCD is providing crucial input to collider experiments in the hunt for new physics.**
- **New ideas for using information from inside jets to study heavy particles.**
- **Enormous progress in higher multiplicities and/or loops.**
- **Merging of different techniques and approaches.**

Reviewed examples with vector bosons, Higgs, top, susy searches and generic heavy particles.

The tools and advances described here are essential for getting the most out of the LHC and for making an exciting future.

Extra Slides

New Search Strategies



• **N -subjettiness** Thaler and van Tilburg (arXiv:1011.2268,1108.2701), Kim (arXiv:1011.1493)

$$\tau_N = \frac{\sum_k p_{T,k} (\min \{ \Delta R_{1,k}, \Delta R_{2,k}, \dots, \Delta R_{N,k} \})^\beta}{\sum_k p_{T,k} (R_0)^\beta}$$

$$0 \leq \tau_N \leq 1$$

$\beta = 1$ good choice

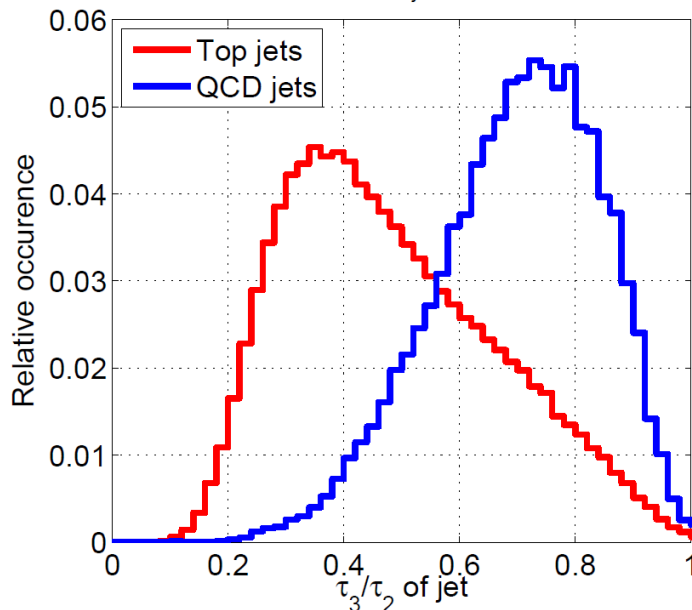
$$\Delta R^2 = \Delta\phi^2 + \Delta\eta^2$$

R_0 jet radius

τ_N/τ_{N-1} provides strong discriminating power for N -pronged objects

Thaler and van Tilburg

$145 \text{ GeV} < m_j < 205 \text{ GeV}$



Many other ideas, e.g.:

• **Dipolarity color flow observable**

Hook, Jankowiak, Wacker

• **Substructure via angular correlations**

Jankowiak and Larkoski

• **Template overlap method**

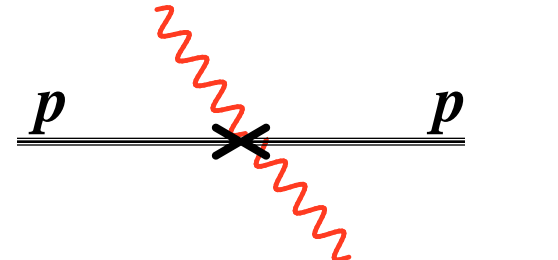
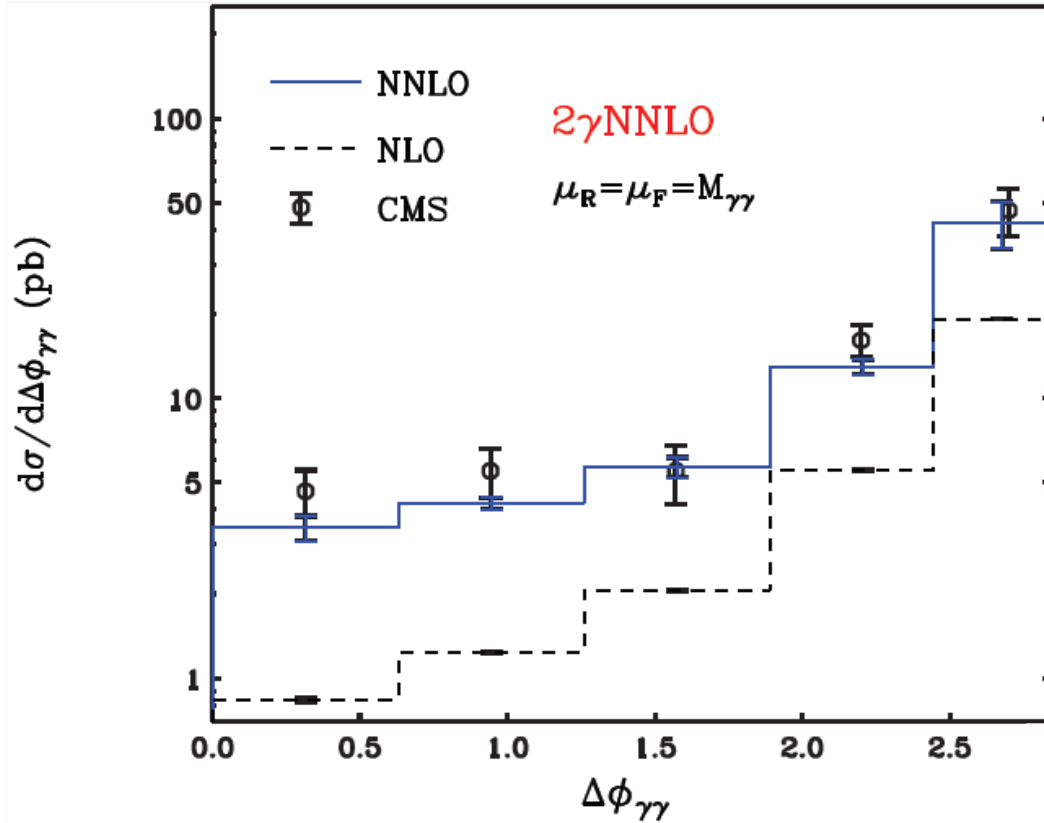
Almeida, Erdogan, Juknevich, Lee, Perez, Sterman

• **Shower deconstruction**

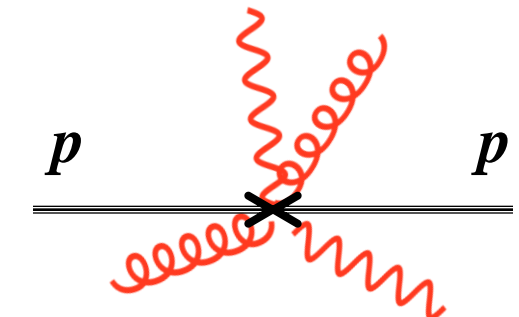
Soper and Spanowsky 29

NNLO QCD: $\gamma\gamma$ Background to Higgs

Catani, Cieri, de Florian, Ferrera, Grazzini (arXiv: 1110.2375)



In LO QCD $\Delta\phi_{\gamma\gamma} = \pi$



In NLO and NNLO QCD
 $\Delta\phi_{\gamma\gamma} \leq \pi$

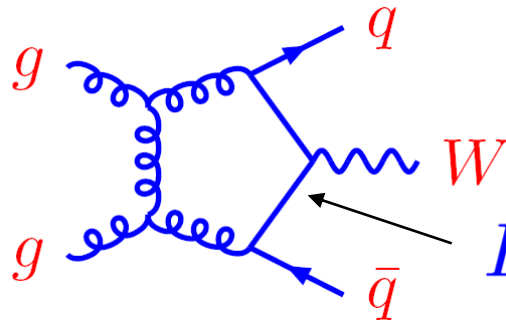
- With NNLO QCD excellent agreement with experiment.
- No surprise here. Perturbative QCD is working exactly as expected.

Why are Feynman diagrams difficult for high-loop or high-multiplicity processes?

- Vertices and propagators involve unphysical gauge-dependent off-shell states. An important origin of the complexity.



$$\int \frac{d^3\vec{p} dE}{(2\pi)^4}$$



Individual Feynman diagrams unphysical

$$E^2 - \vec{p}^2 \neq m^2$$

Einstein's relation between momentum and energy violated in the loops. **Unphysical states! Not gauge invariant.**

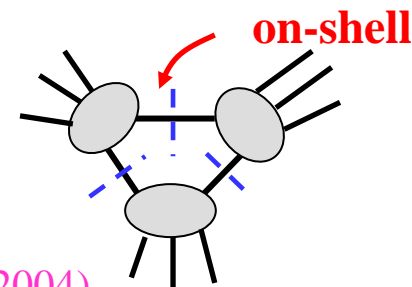
- **All steps should be in terms of gauge invariant on-shell physical states. On-shell formalism. Need to rewrite quantum field theory!**

Some Theoretical Developments

- **Unitarity method.** ZB, Dixon, Dunbar, Kosower (1994,1998).

- **Complex momenta in generalized cuts.**

Britto, Cachazo, Feng (2004).



- **D dimensional unitarity to capture rational pieces of loops.**

ZB, Morgan (1995); ZB, Dixon, Dunbar, Kosower (1996), ZB, Dixon, Kosower (2000); Anastasiou, Britto, Feng, Kunszt, Mastroliia (2006); Giele, Kunszt, Melnikov (2008); Badger (2009)

- **Efficient on-shell reduction of integrals compatible with on-shell**

Ossola, Papadopoulos, Pittau (OPP) (2006); Giele, Kunszt, Melnikov (2008); Forde (2007); Berger et al [BlackHat] (2008)

- **Improved efficiency in Feynman diagram methods.**

Bredenstein, Denner, Dittmaier, Pozzorini (2008)

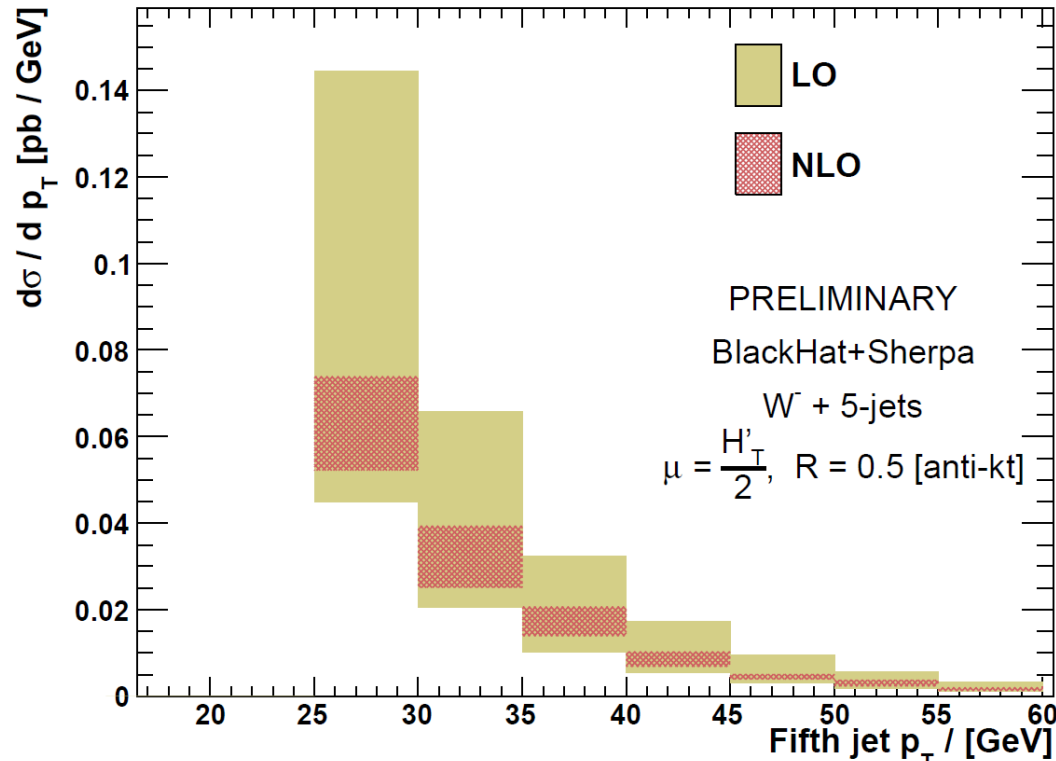
- **New efficient purely numerical approach.**

Becker, Goetz, Reuschle, Schwan, Weinzierl (2011)

Preliminary $W + 5$ Jets in NLO QCD

ZB, Dixon, Febres Cordero, Hoeche, Ita, Kosower, Maitre, Ozeren [BlackHat collaboration]

P_T spectrum of 5th jet



Vary renormalization
and factorization scales
by a factor of 2

- A new level for “state of the art”.
 - First NLO QCD 2 + 6 process for the LHC!
 - People at ATLAS promises to immediately compare to data when complete. Particularly important background to *top* production
- As expected, enormous scale dependence reduced by NLO

Advances in NLO Automation

There has been a lot of recent work on automating recent NLO advances.

2 \rightarrow 2,3 and some 2 \rightarrow 4 processes automated

- **Helac-NLO:** Bevilacqua, Czakon, Ossola, Papadopoulos, Pittau, Worek
- **MadLoop:** Hirchi, Maltoni, Frixione, Frederix, Garzelli, Pittau
- **GoSam:** Cullen, Greiner, Heinrich, Luisoni, Mastrolia, Ossola, Reiter, Tramontano

Example from MadLoop arXiv:1103.0621

Process	μ	n_{lf}	Cross section (pb)	
			LO	NLO
a.1 $pp \rightarrow t\bar{t}$	m_{top}	5	123.76 ± 0.05	162.08 ± 0.12
a.2 $pp \rightarrow tj$	m_{top}	5	34.78 ± 0.03	41.03 ± 0.07
a.3 $pp \rightarrow tj j$	m_{top}	5	11.851 ± 0.006	13.71 ± 0.02
a.4 $pp \rightarrow t\bar{b}j$	$m_{top}/4$	4	25.62 ± 0.01	30.96 ± 0.06
a.5 $pp \rightarrow t\bar{b}j j$	$m_{top}/4$	4	8.195 ± 0.002	8.91 ± 0.01
b.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e$	m_W	5	5072.5 ± 2.9	6146.2 ± 9.8
b.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e j$	m_W	5	828.4 ± 0.8	1065.3 ± 1.8
b.3 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e j j$	m_W	5	298.8 ± 0.4	300.3 ± 0.6
b.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^-$	m_Z	5	1007.0 ± 0.1	1170.0 ± 2.4
b.5 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- j$	m_Z	5	156.11 ± 0.03	203.0 ± 0.2
b.6 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- j j$	m_Z	5	54.24 ± 0.02	56.69 ± 0.07
c.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e b\bar{b}$	$m_W + 2m_b$	4	11.557 ± 0.005	22.95 ± 0.07
c.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e t\bar{t}$	$m_W + 2m_{top}$	5	0.009415 ± 0.000003	0.01159 ± 0.00001
c.3 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- b\bar{b}$	$m_Z + 2m_b$	4	9.459 ± 0.004	15.31 ± 0.03
c.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- t\bar{t}$	$m_Z + 2m_{top}$	5	0.0035131 ± 0.0000004	0.004876 ± 0.000002
c.5 $pp \rightarrow \gamma t\bar{t}$	$2m_{top}$	5	0.2906 ± 0.0001	0.4169 ± 0.0003
d.1 $pp \rightarrow W^+ W^-$	$2m_W$	4	29.976 ± 0.004	43.92 ± 0.03
d.2 $pp \rightarrow W^+ W^- j$	$2m_W$	4	11.613 ± 0.002	15.174 ± 0.008
d.3 $pp \rightarrow W^+ W^+ j j$	$2m_W$	4	0.07048 ± 0.00004	0.1377 ± 0.0005
e.1 $pp \rightarrow HW^+$	$m_W + m_H$	5	0.3428 ± 0.0003	0.4455 ± 0.0003
e.2 $pp \rightarrow HW^+ j$	$m_W + m_H$	5	0.1223 ± 0.0001	0.1501 ± 0.0002
e.3 $pp \rightarrow HZ$	$m_Z + m_H$	5	0.2781 ± 0.0001	0.3659 ± 0.0002
e.4 $pp \rightarrow HZ j$	$m_Z + m_H$	5	0.0988 ± 0.0001	0.1237 ± 0.0001
e.5 $pp \rightarrow Ht\bar{t}$	$m_{top} + m_H$	5	0.08896 ± 0.00001	0.09869 ± 0.00003
e.6 $pp \rightarrow Hb\bar{b}$	$m_b + m_H$	4	0.16510 ± 0.00009	0.2099 ± 0.0006
e.7 $pp \rightarrow H j j$	m_H	5	1.104 ± 0.002	1.036 ± 0.002