

**PHENO 2012**

# Kinematic edges with flavor oscillation and non-zero widths.

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*work done in collaboration with*

Yuval Grossman *and* Dean J. Robinson.

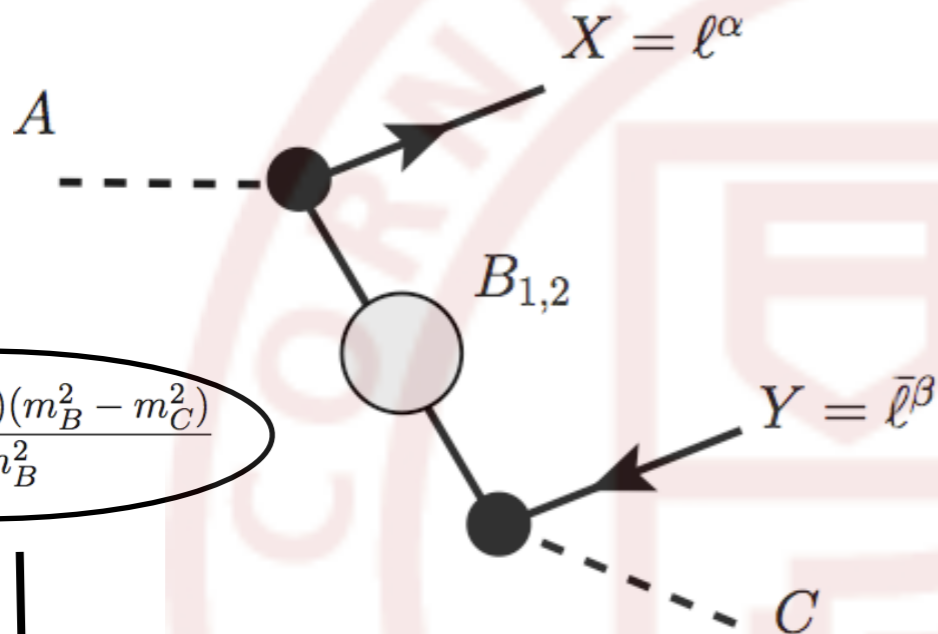
*talk based on*

Yuval Grossman, MM and Dean J. Robinson,  
*JHEP* 1110 (2011) **127**, [hep-ph/1108.5381].

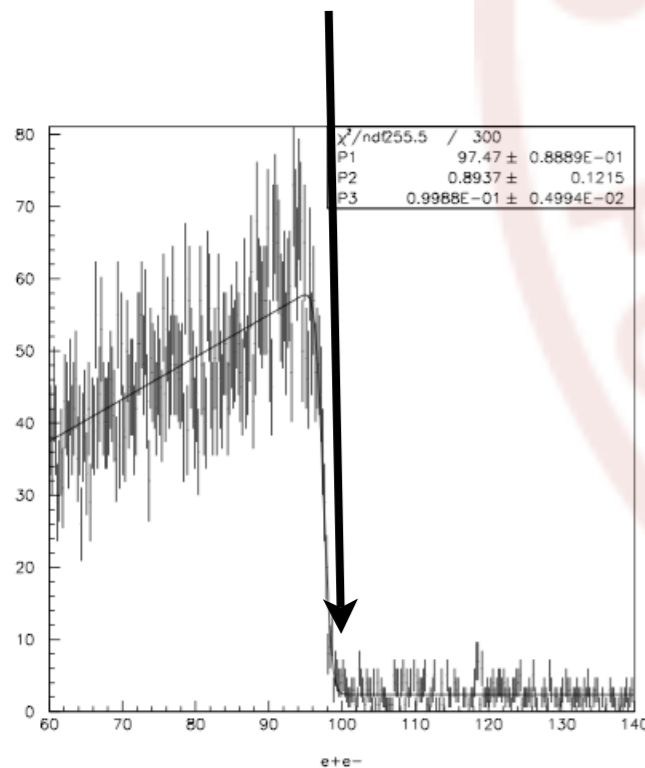
Mario Martone, PHENO 2012, Pittsburgh University 05/07/12

# Kinematic Edges: Generalities

KE or Endpoint method  
 The location of the kinematic edge provides an indirect means to constrain the masses of A, B and C

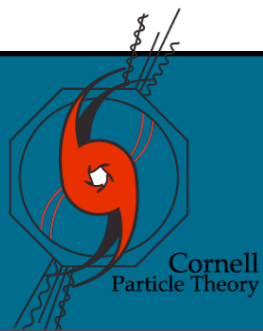


$$s_0 = \frac{(m_A^2 - m_B^2)(m_B^2 - m_C^2)}{m_B^2}$$

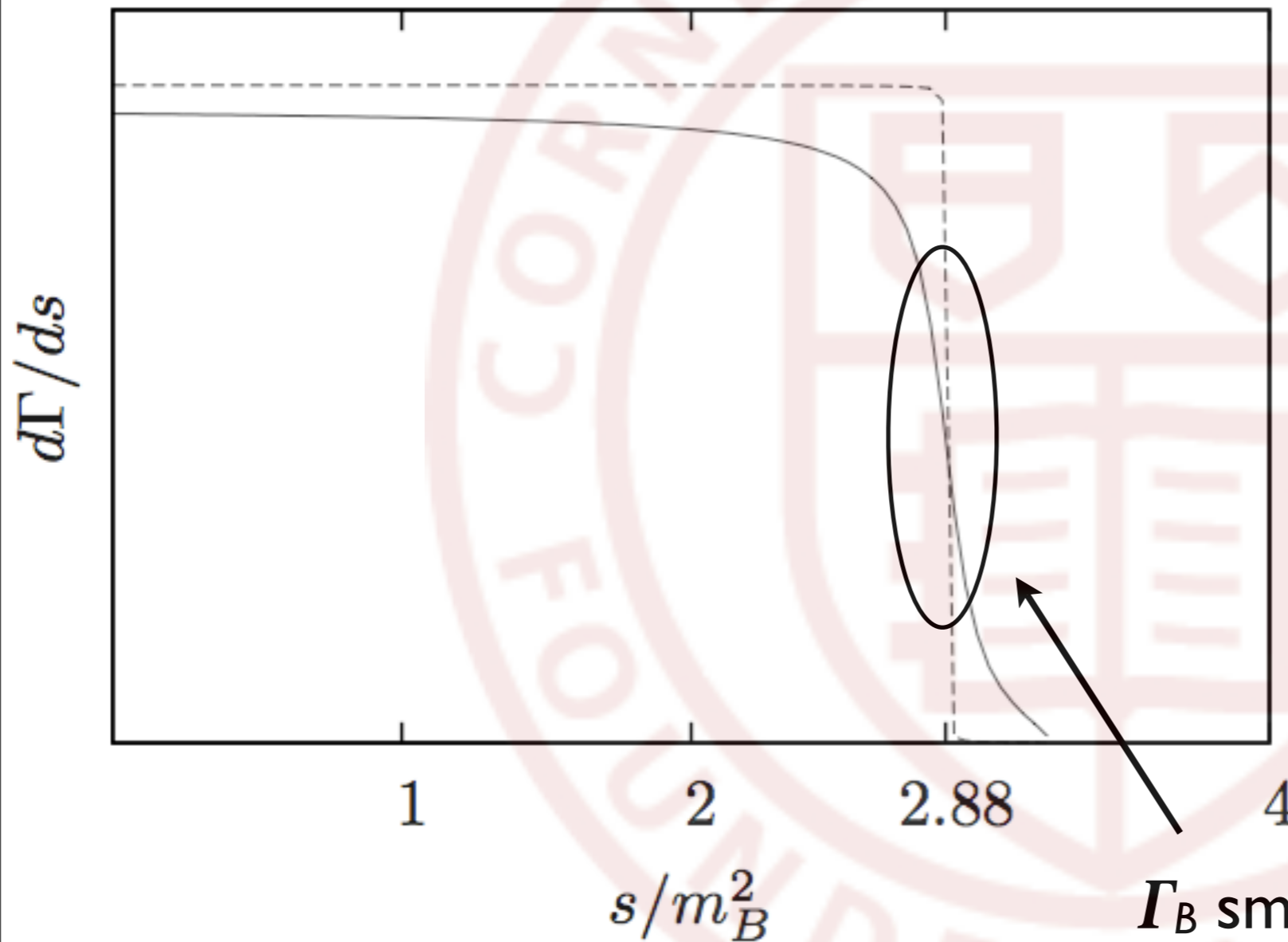


Log likelihood fit to di-electron edge as function of  $m_{ee}$ . The ordinate shows event per bin per  $16 \text{ fb}^{-1}$

- X and Y should be massless.
- The intermediate B should be an on-shell mass eigenstate.
- It neglects that B must have non-zero width  $\Gamma_B$ .
- We expect  $\Gamma_B$  to smear out the kinematic edge.



# Non-zero widths

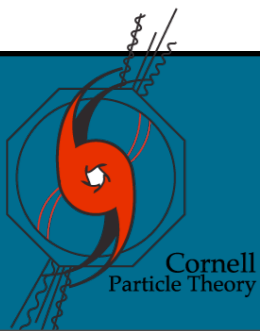


- To study flavor oscillations we need to include non-zero width effects.

- We neglect  $\Gamma_A$  and compute the decay amplitude using a Breit-Wigner:

$$i\mathcal{M} = \frac{ig_X g_Y}{p_B^2 - m_B^2 + im_B \Gamma_B}$$

$\Gamma_B$  smears out the kinematic edge!



Most studies of kinematic edges assume universal slepton masses but we expect that RG-running down to the TeV scale produces a mass splitting. For the *smuon* and the *selectron* we expect  $\Delta m_{\tilde{\ell}} \sim \text{few GeV}$

- kinematic edges could then be used to probe a non-trivial flavor structure.

### **No-mixing**

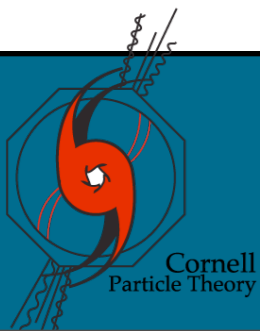
B.C.Allanach, J. P. Conlon and C. G. Lester, Phys. Rev. D **77** (2008) 076006, [hep-ph/0801.3666].

### **No-oscillation**

Iftah Galon and Yael Shadmi, Phys. Rev. D **85** (2012) 015010 [hep-ph/1108.2220].

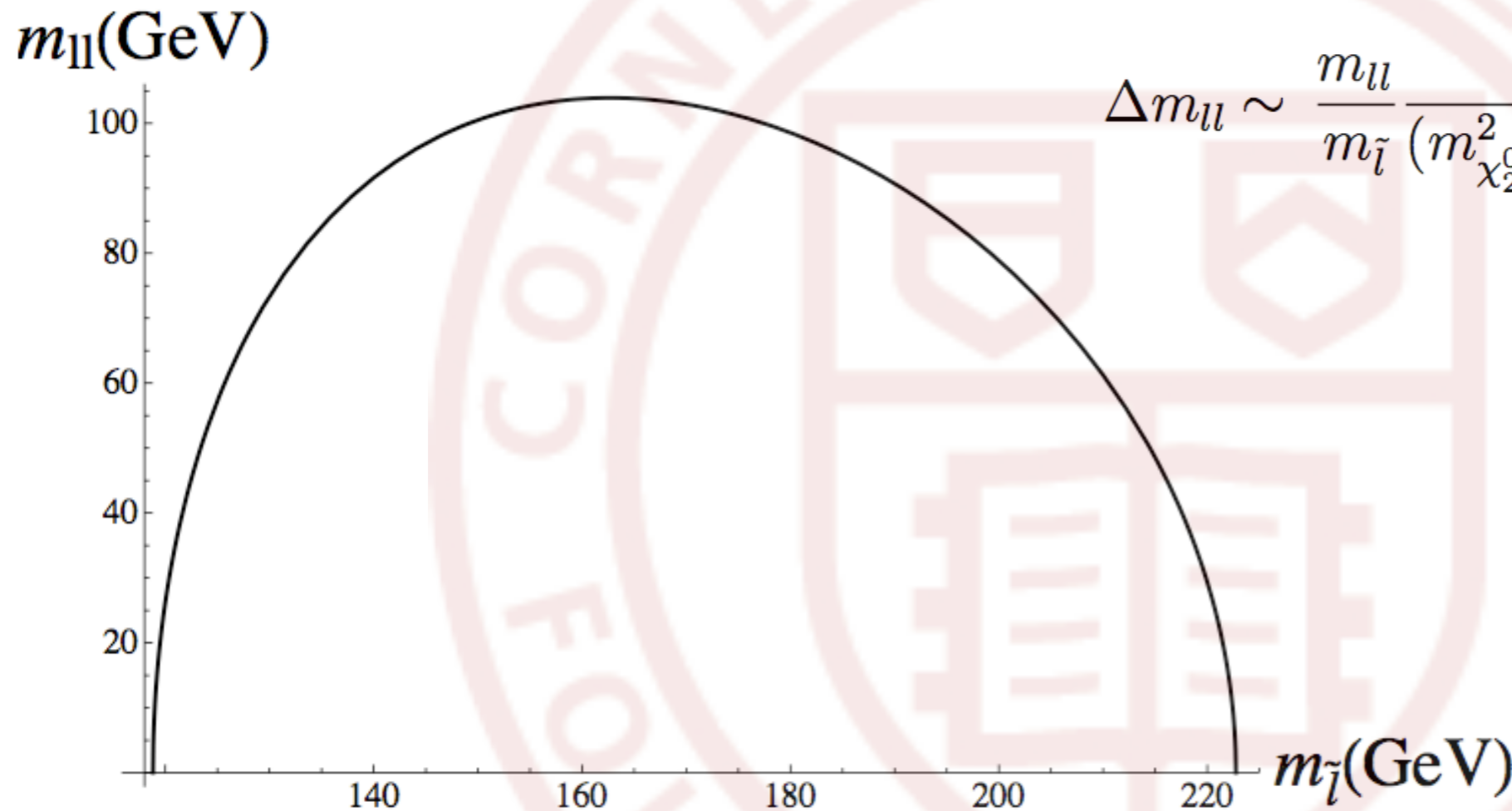
### **General case**

Yuval Grossman, MM and Dean J. Robinson, JHEP **1110** (2011) **127**, [hep-ph/1108.5381].





# kinematic edge splitting

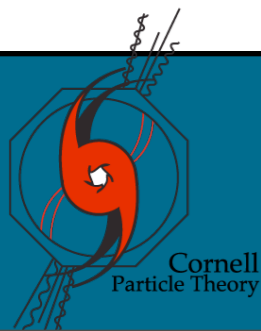


$$\Delta m_{II} \sim \frac{m_{II}}{m_{\tilde{l}}} \frac{m_{\chi_2^0}^2 m_{\chi_1^0}^2 - m_{\tilde{l}}^4}{(m_{\chi_2^0}^2 - m_{\tilde{l}}^2)(m_{\tilde{l}}^2 - m_{\chi_1^0}^2)} \Delta m_{\tilde{l}}$$

## soft leptons

If one of the two slepton is too close to either neutralinos one of the emitted lepton is too soft and therefore hard to detect.

Endpoint location as a function of the slepton mass, with the neutralino masses at values  $m_{\chi_2^0} = 222$  GeV and  $m_{\chi_1^0} = 118$  GeV (SU3 values).



# No mixing

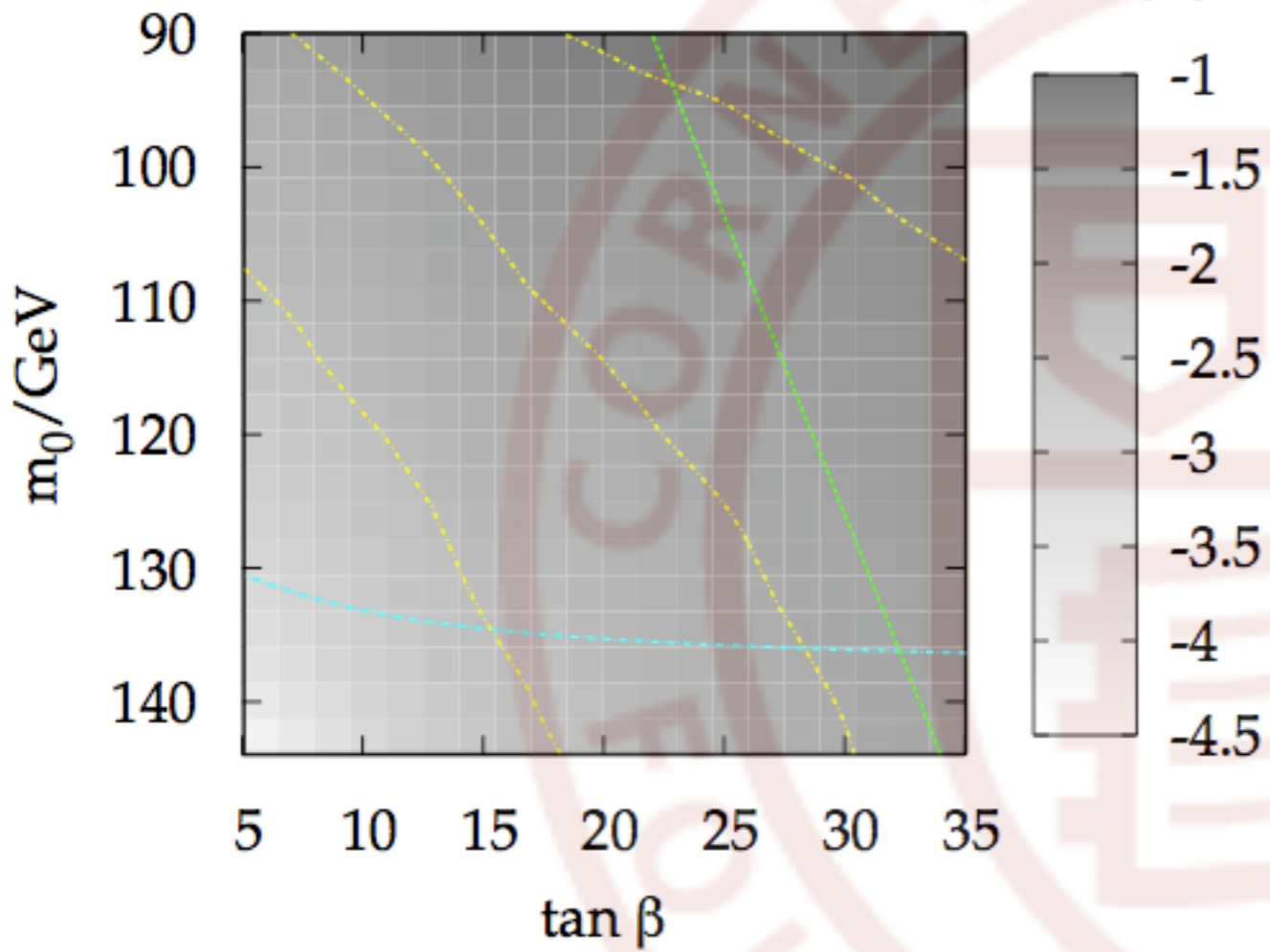
$$E \equiv \frac{\Delta m_{\tilde{l}}}{m_{\tilde{l}}}$$

$\log_{10} E$

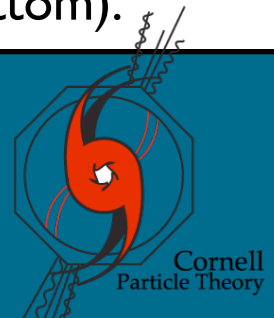
B.C.Allanach, J. P. Conlon and C. G. Lester, Phys. Rev. D **77** (2008) 076006, [hep-ph/0801.3666].

In absence of mixing, using kinematic edge splitting in same-flavor-di-lepton distributions, we therefore could have sensitivity up to

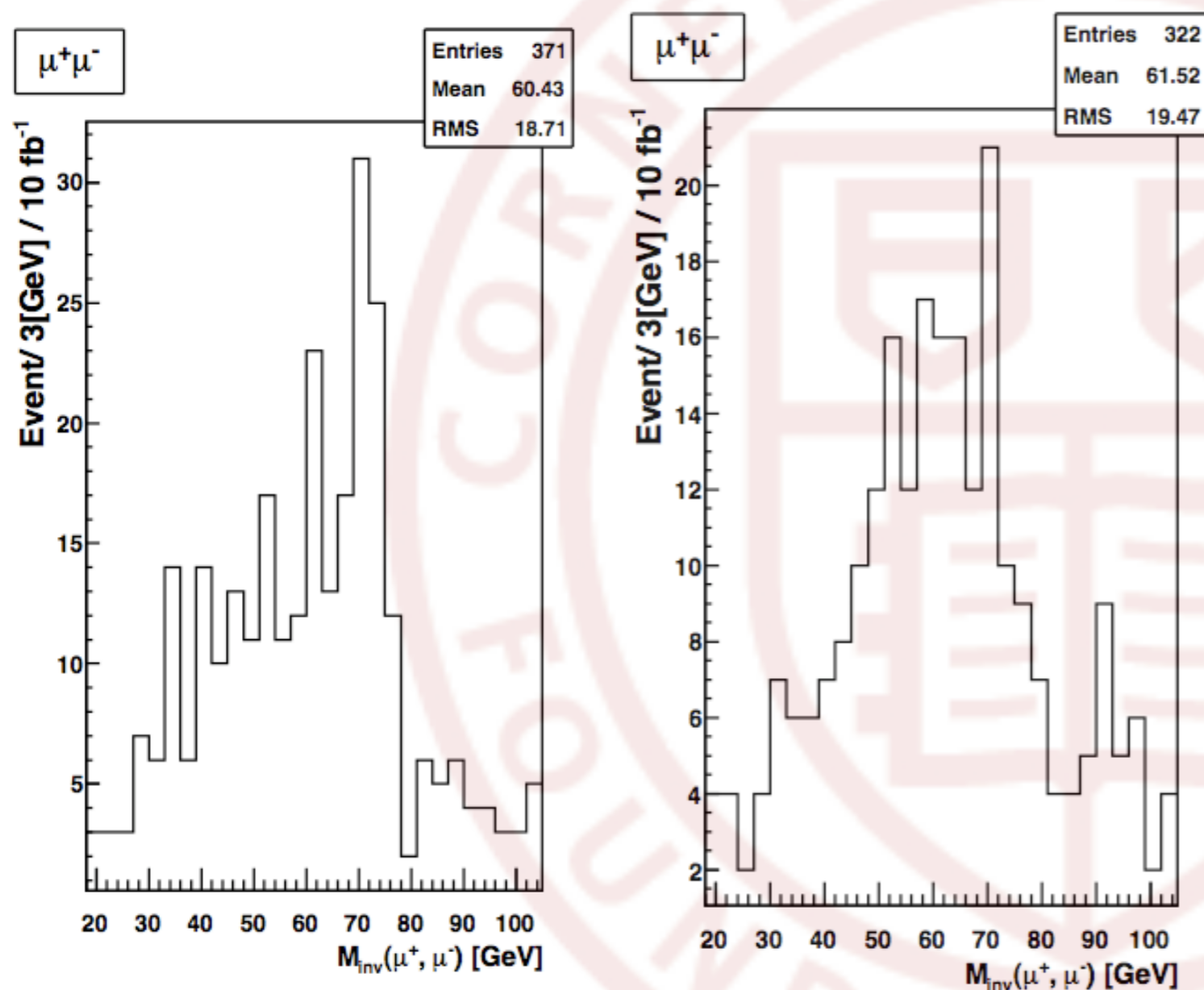
$$\frac{\Delta m_{\tilde{l}}}{m_{\tilde{l}}} \sim 10^{-4}$$



Expected  $30 \text{ fb}^{-1}$  1-sigma sensitivity,  $E$ , to selectron-smuon mass splitting in perturbed mSUGRA around SPS1a. The region to the right of the almost vertical side has  $m_{\tilde{\tau}_1} < m_{\tilde{\chi}_1^0}$ . The region underneath the mostly horizontal line has  $m_{\tilde{\chi}_2^0} - m_{\tilde{l}} < 10 \text{ GeV}$ . The lighter lines show contours of  $\log_{10} E = -2, -2.5, -3$  (top to bottom).



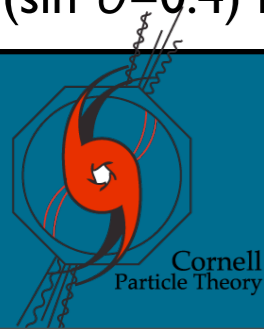
# Mixing without oscillation



Iftah Galon and Yael Shadmi, Phys. Rev. D85 (2012) 015010 [hep-ph/1108.2220].

For large mixing the edges in the same-flavor distributions is harder to measure but the  $e\mu$  distribution should exhibit some edge structure which would indicate flavor mixing.

Opposite-sign-di-muon invariant mass distributions with slepton masses  $m_{\tilde{l}_1}=131$  GeV and  $m_{\tilde{l}_2}=133.8$  GeV. Left the small mixing case ( $\sin^2\theta=0.4$ ) right the large mixing one ( $\sin^2\theta=0.9$ ).





# Regimes

$$x \equiv \frac{\Delta m}{\bar{\Gamma}}$$

$$x \ll 1$$

Oscillations length scale is too long, oscillation effects unimportant.

$$x \sim 1$$

Oscillation effects are significant.

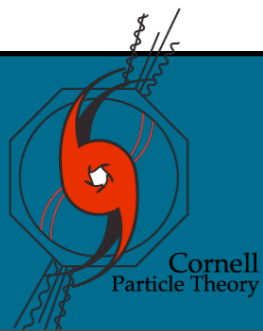
$$x \gg 1$$

Oscillations are too fast and average out, oscillation effects unimportant.

**Sleptons are almost degenerate.**

**No-oscillation**

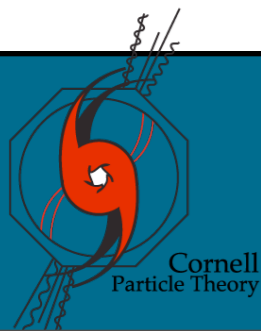
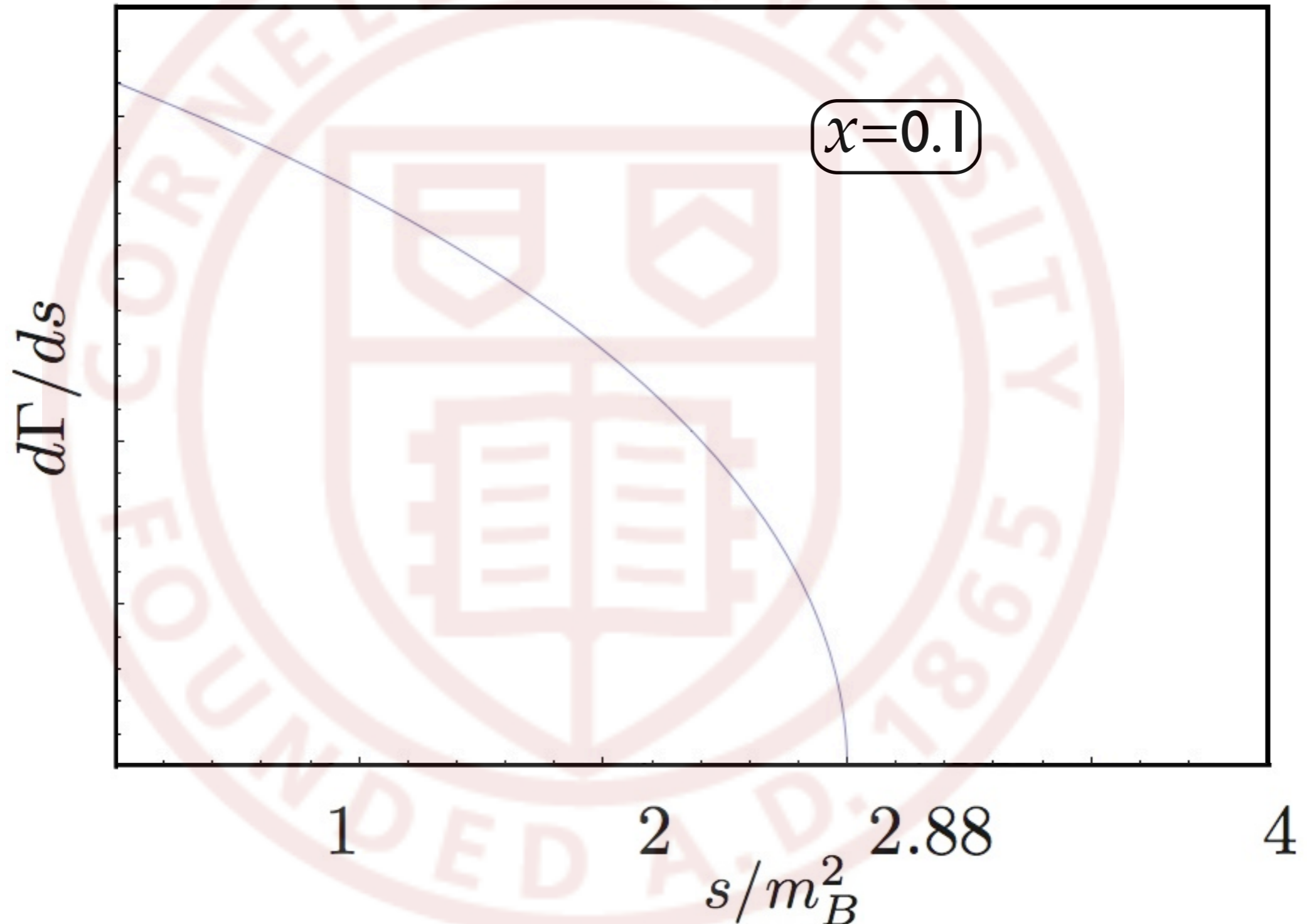
Iftah Galon and Yael Shadmi, Phys. Rev. D **85** (2012) 015010 [hep-ph/1108.2220].





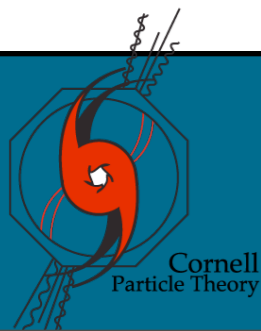
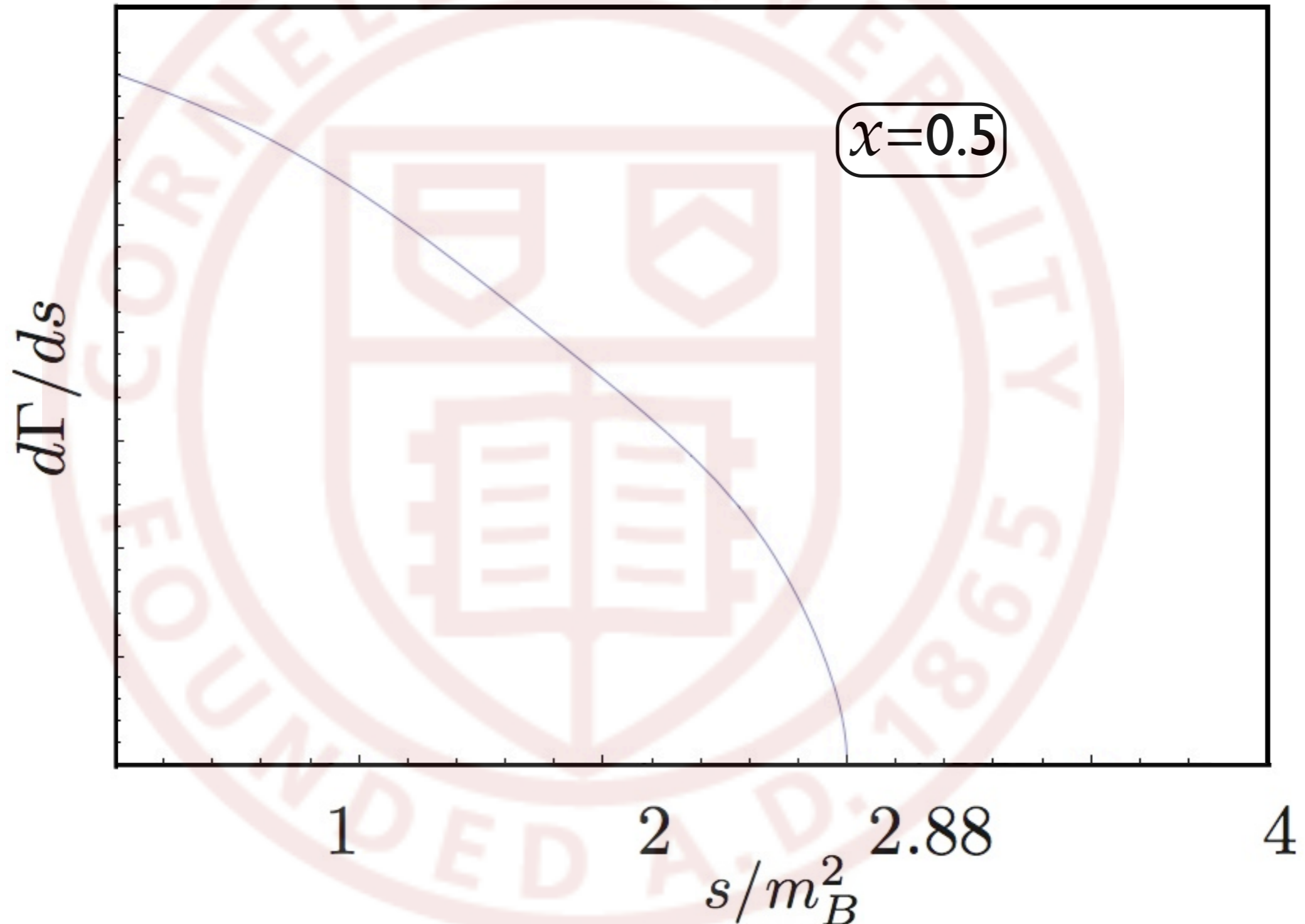
## KE with Flavor oscillations

Differential decay rate with parameter choice  $m_A/m_B=2$ ,  $m_C/m_B=0.2$  and  $\Gamma_B/m_B=10^{-1}$  (solid) or  $\Gamma_B/m_B=10^{-3}$  (dashed).



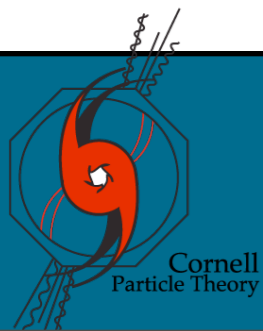
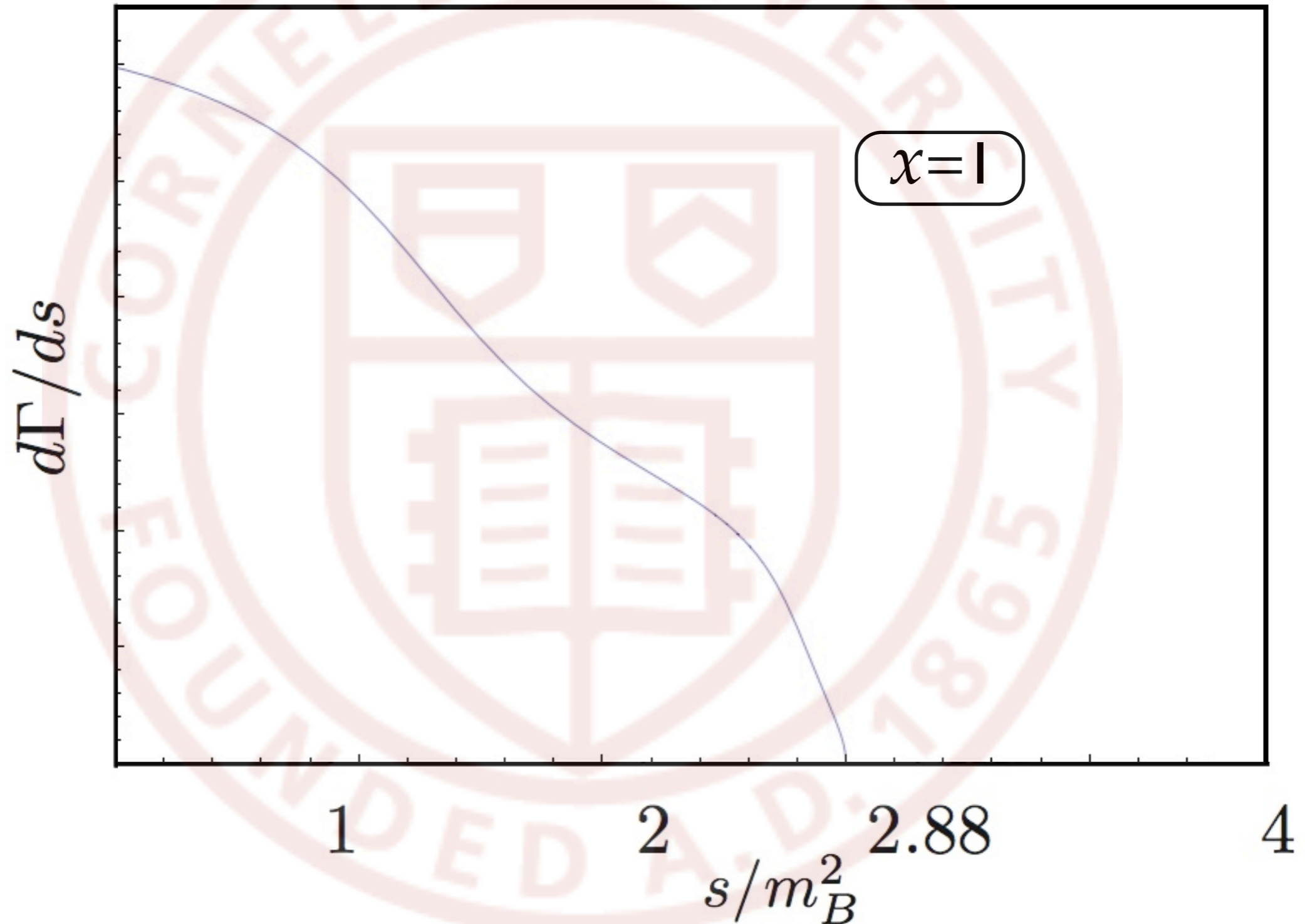
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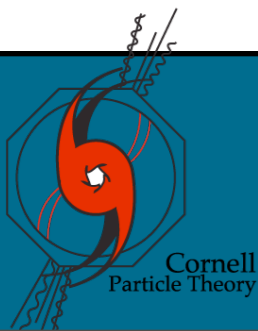
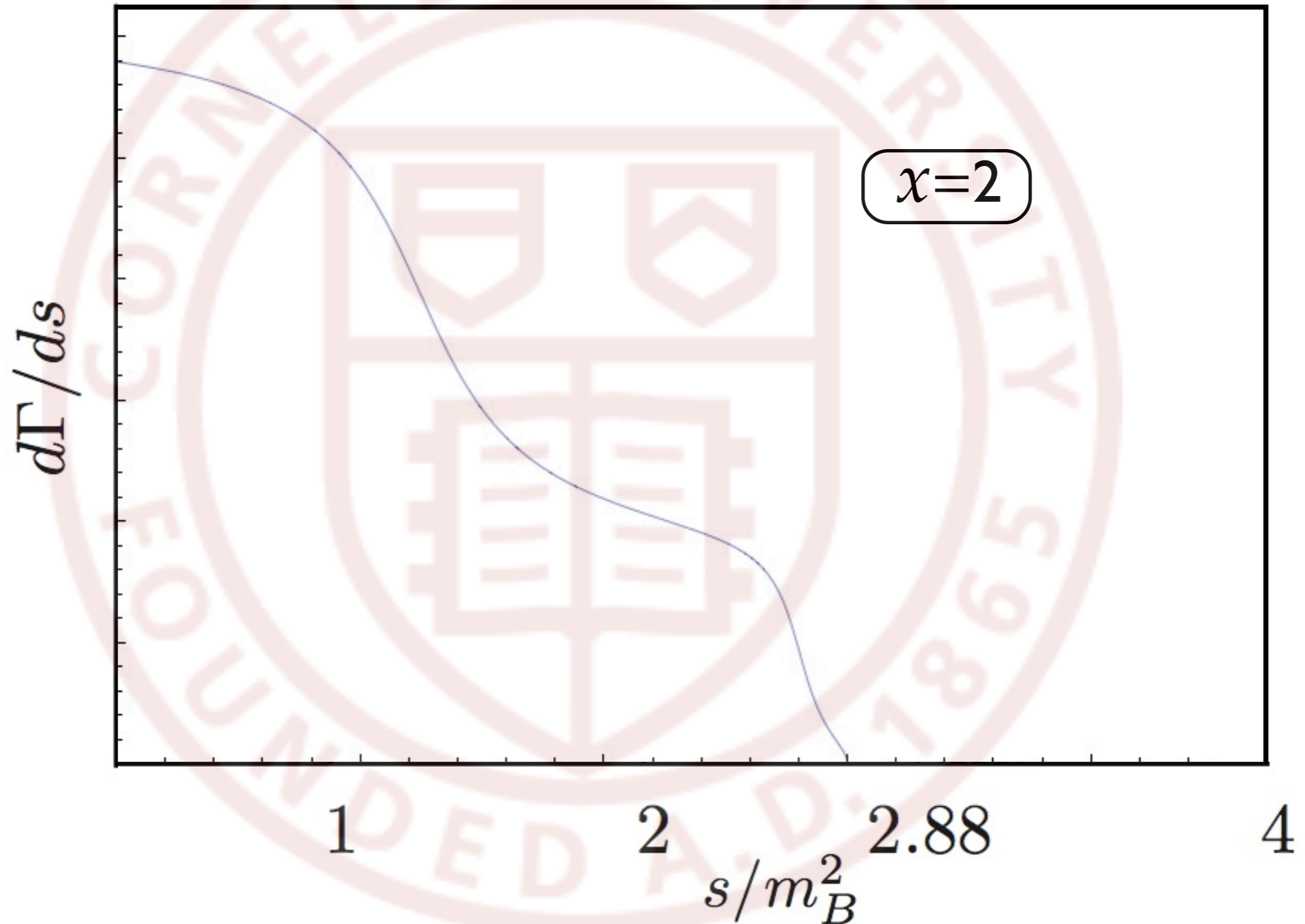
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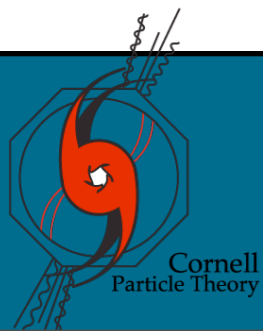
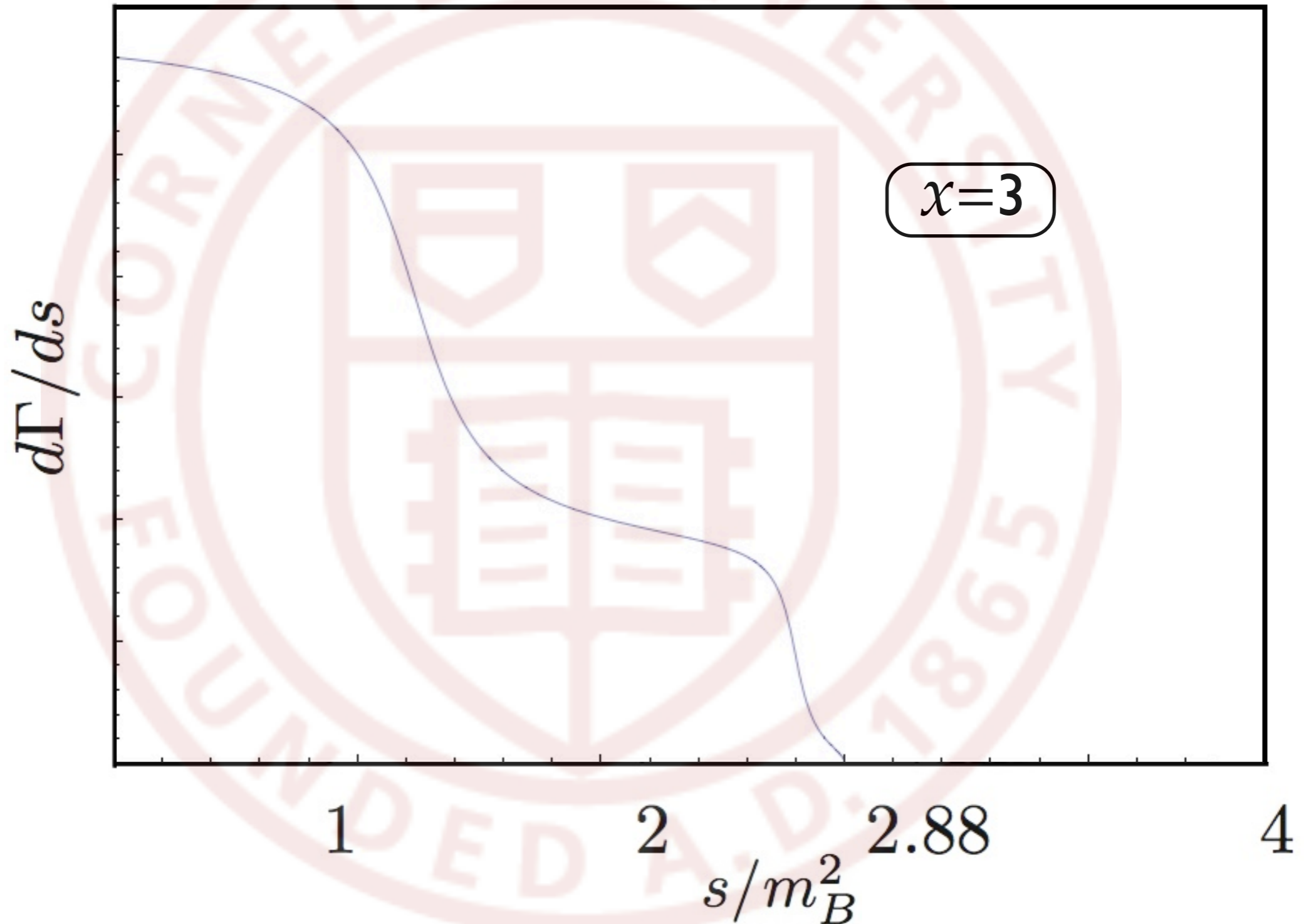
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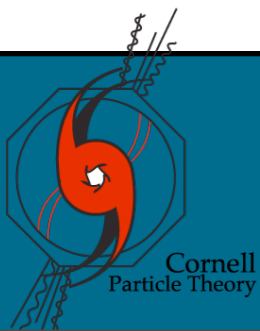
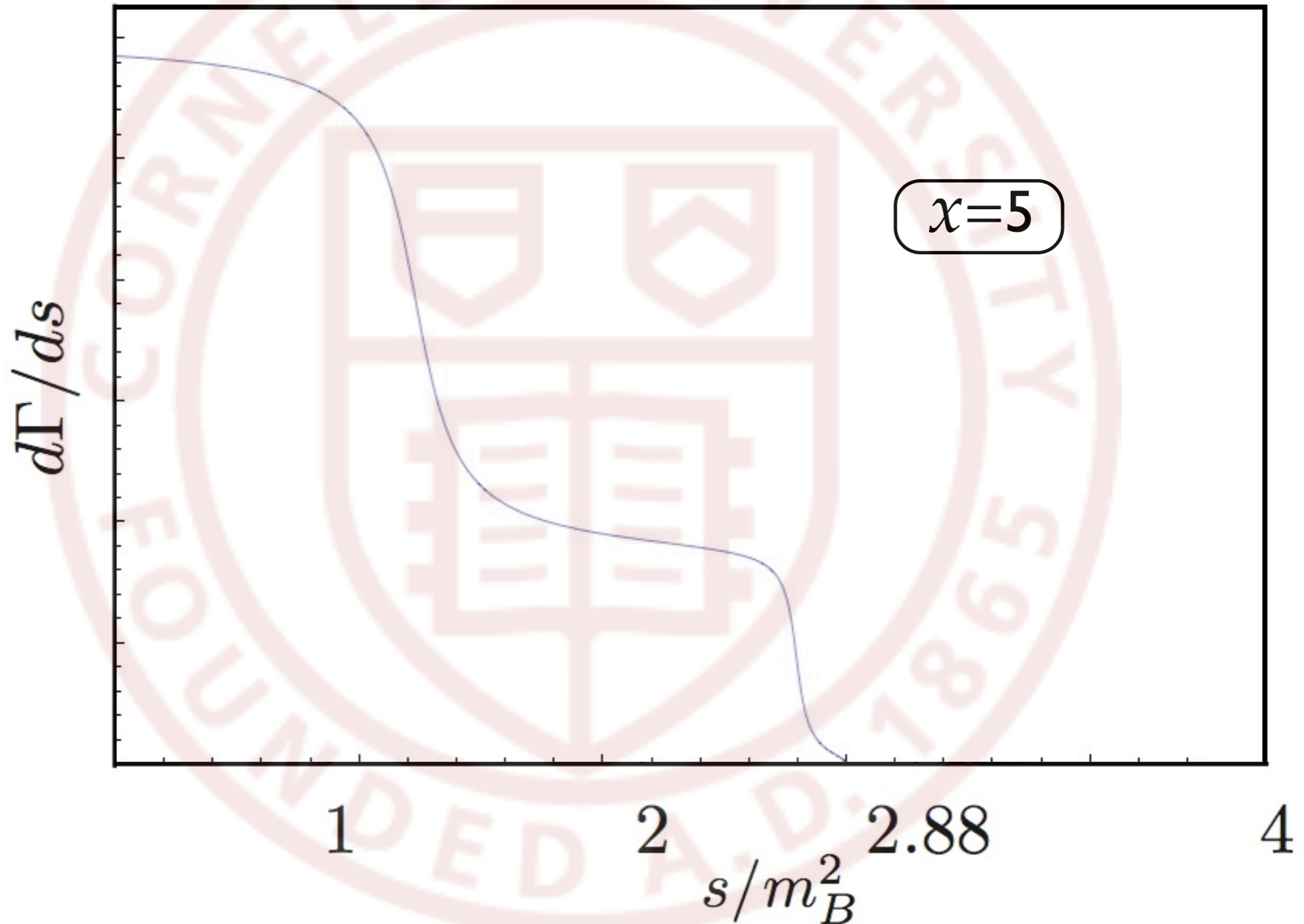
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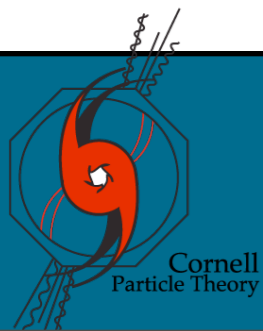
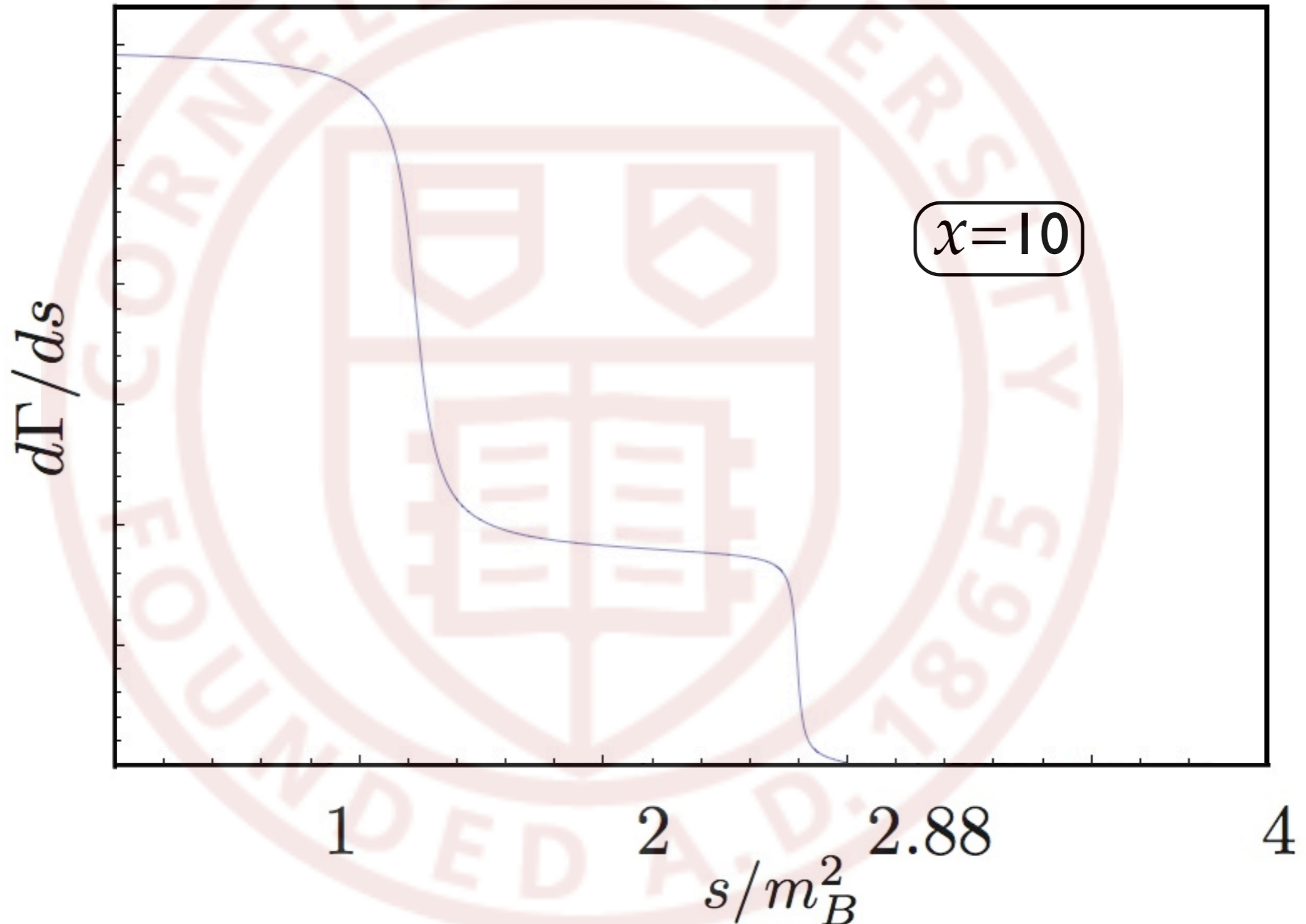
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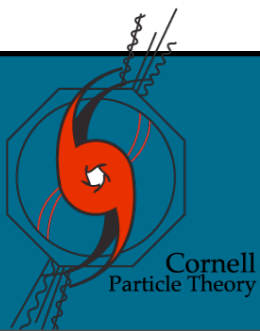
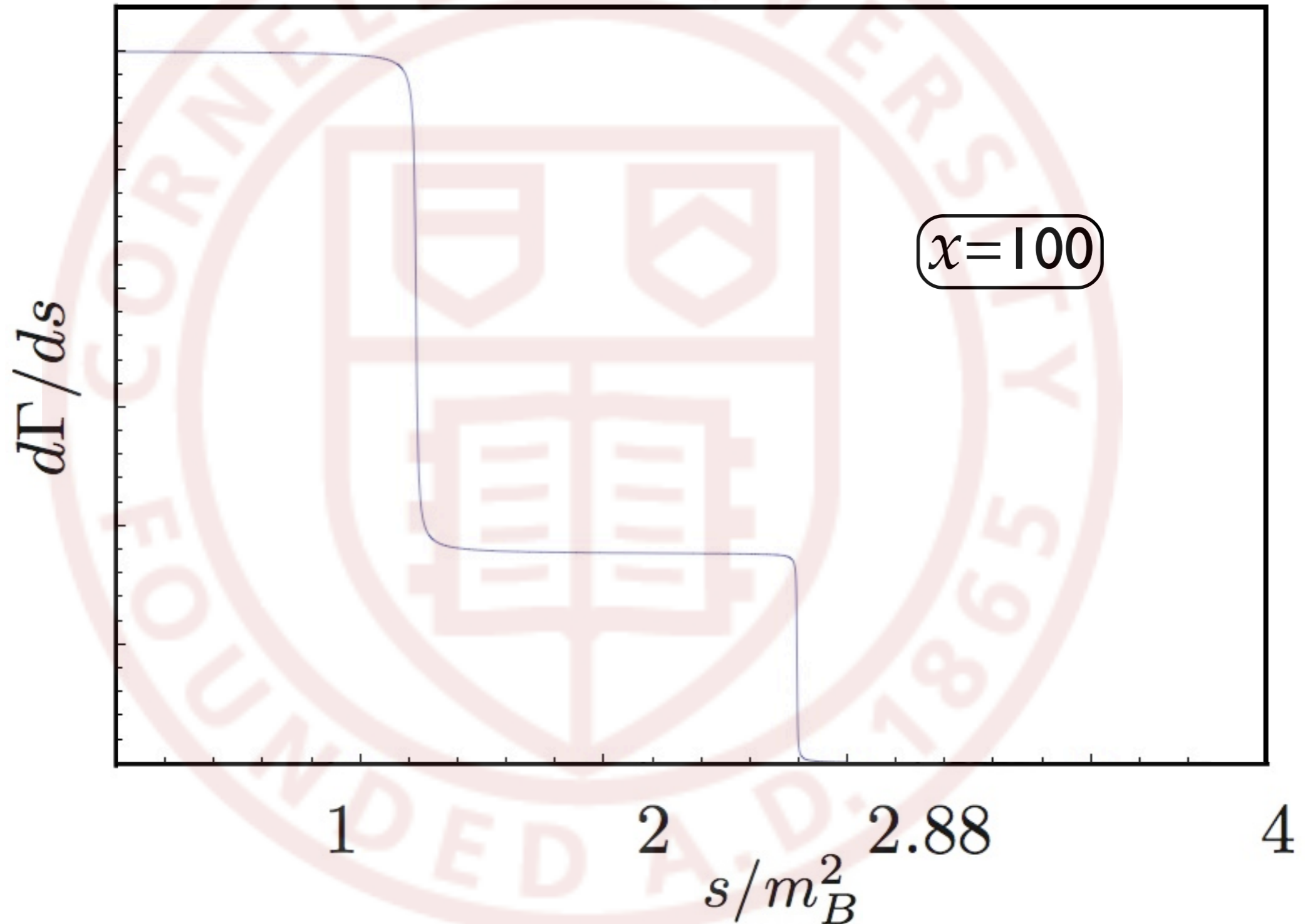
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## edge width

Gradient of the differential decay rate near the kinematic edge

$$d^2\Gamma/ds^2 = \frac{f(s_0)}{(s-s_0)^2 + \sigma^2}$$

We can therefore identify  $\sigma$  as the edge width:

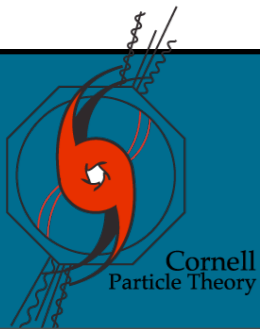
$$\sigma \simeq \frac{4m^2 z}{x} \left( 1 - \frac{m_{\chi_1}^2 m_{\chi_2}^2}{m^4} \right)$$

### EDGE RESOLUTION CRITERION

The two edges can be resolved if

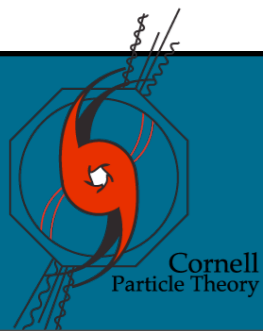
$$|s_0^1 - s_0^2| > \frac{\sigma_1 + \sigma_2}{2}$$

In the case in exam this criterion reduces to a simple restriction on  $x$

$$x > 1$$


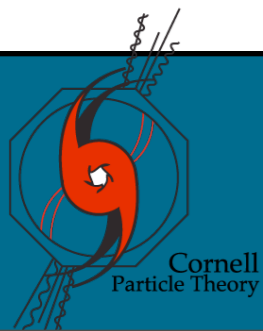
## **Future Directions**

- This is a first step towards studying the most general non-universal flavor scenario, including slepton oscillation. For  $x \sim 1$  it is hard to clearly resolve the two edges.
- We plan in carrying out a more detailed analysis in specific and concrete SUSY scenarios, like the ones presented in the case oscillations are absent.



## Conclusions

- kinematic edges provide one of the many tools to extract superpartner masses which are particularly useful if the final state cannot be fully reconstructed.
- KE could turn useful to identify a non-universal flavor structure since for certain value of slepton masses, the edge splitting is bigger than the mass splitting itself (not always true + soft leptons).



Thanks!

