

Combination of Electroweak and QCD Effects to Charged Current Drell Yan

Cathy Bernaciak

ITP Universität Heidelberg

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in collaboration with Doreen Wackerath

Importance of Precise M_W Measurement

Charged Current (CC) & Neutral Current (NC) Drell-Yan - valuable physics

- single W, Z production large σ and clear signatures $W \rightarrow \ell + \cancel{E}_T$ or $Z \rightarrow \ell^+ \ell^-$

$\Rightarrow M_W$, PDFS, luminosity monitoring

\Rightarrow improved SM Higgs mass constraint

- uncertainty from radiative corrections:

Tevatron EW Working Group 2012

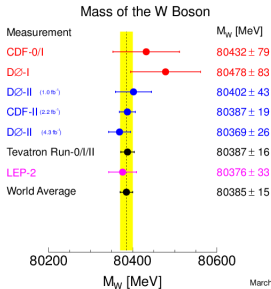
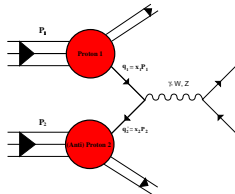
\Rightarrow CDF-II: 4 of 19 MeV

\Rightarrow DØ-II: 7 of 26 MeV

- anticipated LHC measurement of

ΔM_W to within 15 MeV Haywood et al 2000

\Rightarrow precise theoretical handling of higher-order QCD and EW corrections



WGRAD2^{1,2} is a MC code for charged-current (CC) Drell-Yan with full NLO EW corrections

$$d\sigma = \sum_{\text{flavors}} dx_1 dx_2 f_1(x_1) f_2(x_2) \left[d\hat{\sigma}_B + \underbrace{d\hat{\sigma}_{v+s}}_{\sim \delta_s} + \int_{1,2} \frac{dz}{z} \underbrace{d\hat{\sigma}_{\text{HC}}(z)}_{\sim \delta_c} + \int_{\delta_s, \delta_c} d\Phi_{\text{rad}} d\hat{\sigma}_{\text{HC}} \right]$$

- soft, collinear divergences treated with 2-cutoff phase space slicing³ technique
 - ⇒ dependence on δ_s and δ_c must cancel in physical result
- **options/switches:** gauge invariant FS, IS, interference subsets of photon radiation for separate study

¹U.Baur and D.Wackeroth, Phys. Rev. **D70**, 073015 (2004), hep-ph/0405191

²U.Baur, S.Keller and D.Wackeroth, Phys. Rev. **D59**, 013002 (1999), hep-ph/9807417

³B.W. Harris, J.F. Owens, Phys. Rev. **D65**, 094032 (2002), hep-ph/0102128

POWHEG-BOX

POsitive W eight H ardest E vent G enerator^{4,5,6}

- contains NLO QCD corrections matched to Parton Shower (PYTHIA and HERWIG) for several processes (POWHEG-BOX)
- POWHEG method:
 1. generate events with the hardest radiation at NLO
 2. feed events into PYTHIA/HERWIG, all showering is softer than the first, hardest event
- POWHEG master formula:

$$d\sigma = \sum_{\text{flavors}} \bar{B}(\Phi_n) d\Phi_n \left\{ \Delta(\Phi_n, p_T^{\min}) + \sum_{\alpha_r} \frac{[d\Phi_{\text{rad}} \Delta(\Phi_n, k_T > p_T^{\min}) R(\Phi_{n+1})]}{B(\Phi_n)} \right\}$$

- $\bar{B} \Rightarrow$ exact NLO differential cross-section \Rightarrow FKS subtraction
- $\Delta(\Phi_n, k_T) \Rightarrow$ Sudakov form-factor \Rightarrow ensures hardest event

⁴P.Nason, *JHEP* **0411** (2004) 040, hep-ph/0409146

⁵S.Frixione, P.Nason and C. Oleari, *JHEP* **0711** (2007) 070, arXiv:0709.2092

⁶S.Alioli, P.Nason, C. Oleari and E.Re, *JHEP* **1006** (2010) 043, arXiv:1002.2581

⁷S.Alioli, P.Nason, C. Oleari and E.Re, *JHEP* **0807** (2008) 060, arXiv:0805.4802

We incorporate the EW corrections into \bar{B} :

$$\begin{aligned} \bar{B}(\Phi_2) = & B(\Phi_2) + V_{\text{QCD}}(\Phi_2) + V_{\text{EW}}(\Phi_2) + \int_{\oplus} \frac{dz}{z} [G_{\oplus, \text{QCD}}(\Phi_{2, \oplus}) + G_{\oplus, \text{EW}}(\Phi_{2, \oplus})] \\ & + \int_{\ominus} \frac{dz}{z} [G_{\ominus, \text{QCD}}(\Phi_{2, \ominus}) + G_{\ominus, \text{EW}}(\Phi_{2, \ominus})] + \sum_{\alpha_r \in \text{IS}} \int d\Phi_{\text{rad}, \text{IS}} [\hat{R}(\Phi_3) + R_{\text{EW}}(\Phi_3)] \end{aligned}$$

- $\Rightarrow V_{\text{EW}}(\Phi_2)$ virtual + soft finite EW corrections
 - \Rightarrow switch for resonant/non-resonant (box diagrams) effects
- $\Rightarrow G_{\text{EW}}(\Phi_2, z)$ IS and FS collinear EW pieces
- $\Rightarrow R_{\text{EW}}(\Phi_3)$ finite real piece - IS and FS together
 - \Rightarrow switch for IS, FS, interference QED radiation

Resulting public code available within POWHEG-BOX as subprocess W_{ew}-BW

Crosschecks and Validation

First, can we get WGRAD2 results from POWHEG-W_BW by turning off NLO QCD? **Yes.**

	Tevatron, W^+	LHC, W^+	LHC, W^-
WGRAD2	362.55(2) pb	1059.6(1) pb	759.26(3) pb
POWHEG-W_BW	362.4(2) pb	1059.0(5) pb	758.7(8) pb

Second, are they stable wrt unphysical δ_s and δ_c ? **Yes.**

(δ_s, δ_c)	Tevatron, W^+	LHC, W^+	LHC, W^-
0.01, 0.005	362.4(2) pb	1059.0(5) pb	758.7(8) pb
0.01, 0.001	362.4(2) pb	1059.1(7) pb	759.2(5) pb
0.001, 0.0005	362.3(2) pb	1059.4(9) pb	759.4(5) pb
0.001, 0.0001	362.3(2) pb	1059.2(8) pb	759.3(5) pb

Process: $W^\pm \rightarrow \mu^\pm \nu_\mu$ **Bare Cuts:** $p_T(\mu^\pm), p_T(\nu_\mu) > 25\text{GeV}, |\eta_\mu| < 1$

$M_T(W)$ Distributions - Tevatron

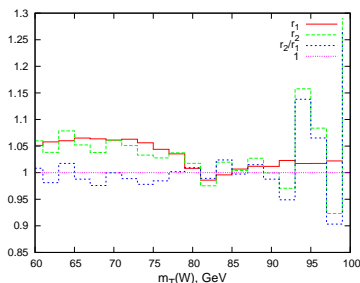
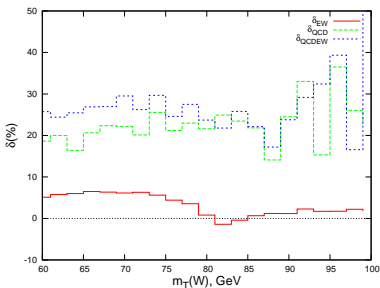
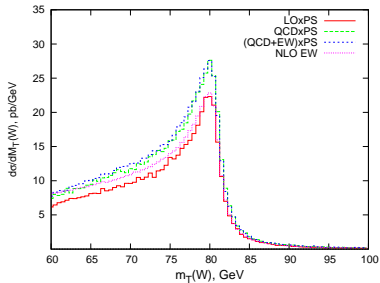
$p\bar{p} \rightarrow W^+ \rightarrow \mu^+\nu_\mu$, $\sqrt{S} = 1.96$ TeV, Pythia showering

$$M_T(W) = \sqrt{2p_T(\ell)p_T(\nu)(1 - \cos(\Delta(\phi_{\ell\nu})))}$$

- fits of $d\sigma/dM_T(W)$ used to measure M_W
 - \Rightarrow lineshape sensitive to FS QED effects around Jacobian peak due to collinear logs $\sim \alpha \log(m_l^2/\hat{s})$

$$\delta_a = \left[\left(\frac{d\sigma_a}{d\mathcal{O}} - \frac{d\sigma_{LO}}{d\mathcal{O}} \right) / \frac{d\sigma_{LO}}{d\mathcal{O}} \right] \times 100$$

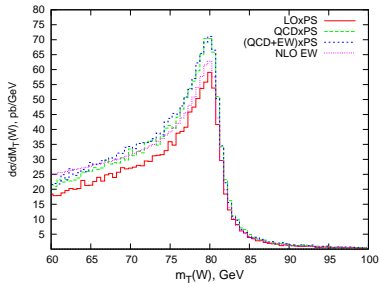
$$r_1 = \frac{d\sigma_{EW}}{d\mathcal{O}} / \frac{d\sigma_{LO}}{d\mathcal{O}}, \quad r_2 = \frac{d\sigma_{(QCD+EW) \times PS}}{d\mathcal{O}} / \frac{d\sigma_{QCD \times PS}}{d\mathcal{O}}$$



$M_T(W)$ Distributions - LHC

$pp \rightarrow W^+ \rightarrow \mu^+ \nu_\mu$, $\sqrt{S} = 7$ TeV, Pythia showering

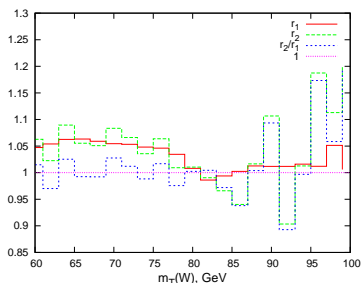
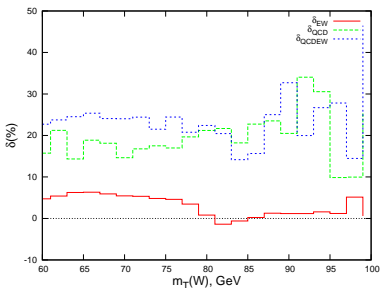
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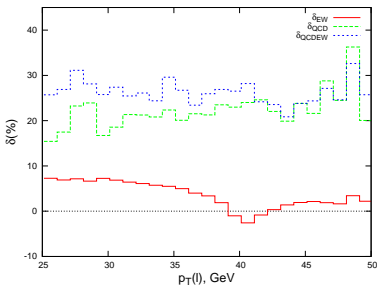
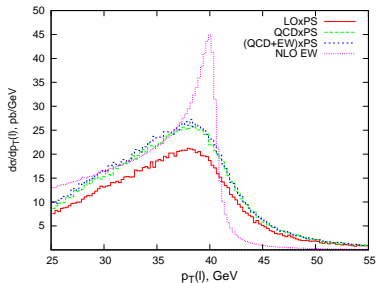
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$p_T(l)$ Distributions - Tevatron

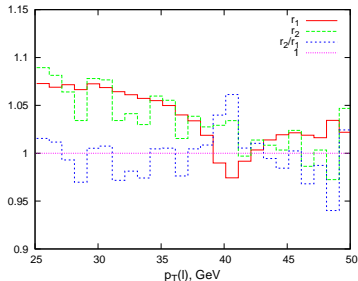
$p\bar{p} \rightarrow W^+ \rightarrow \mu^+\nu_\mu$, $\sqrt{S} = 1.96$ TeV, Pythia showering



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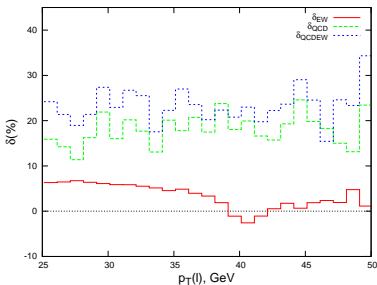
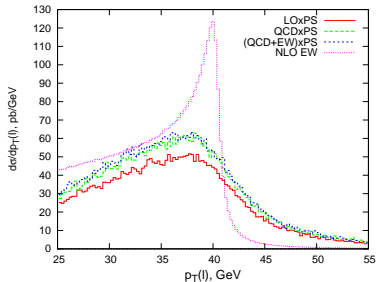
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$p_T(l)$ Distributions - LHC

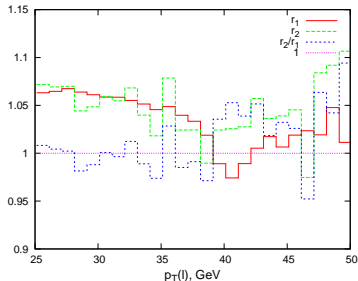
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Summary: QCD + EW Effects on Distributions

What can we conclude about effects of *combined* EW and QCD corrections on $\frac{d\sigma}{dM_T(W)}$ and $\frac{d\sigma}{dp_T(l)}$?

$$r_2 = \underbrace{\frac{d\sigma_{(QCD+EW)\times PS}}{d\mathcal{O}} / \frac{d\sigma_{QCD\times PS}}{d\mathcal{O}}}_{\text{effect of EW corrections on } \frac{d\sigma}{dp_T(\mu)} \text{ in presence of QCD}}$$

effect of EW corrections on $\frac{d\sigma}{dp_T(\mu)}$ in presence of QCD

not the same as $r_1 = \underbrace{\frac{d\sigma_{EW}}{d\mathcal{O}} / \frac{d\sigma_{LO}}{d\mathcal{O}}}_{\text{effect of EW corrections only}}$

effect of EW corrections only

if it was, $\frac{r_2}{r_1} \simeq 1$

- $\mathcal{R} = \frac{r_2}{r_1}$ deviation from unity implies non-additive (interference) EW, QCD effects $\Rightarrow p_T(l)$
- understanding of interplay of QCD and EW corrections to Drell-Yan useful to reduce QED uncertainty in M_W measurement.

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effect of EW corrections on $\frac{d\sigma}{dp_T(\mu)}$ in presence of QCD

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Thank You!

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