

# Inelastic Dark Matter and Small Neutrino Mass

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H. An, BD, Y. Cai and R. N. Mohapatra, *Phys. Rev. Lett.* **108**, 081806 (2012) [1110.1366]

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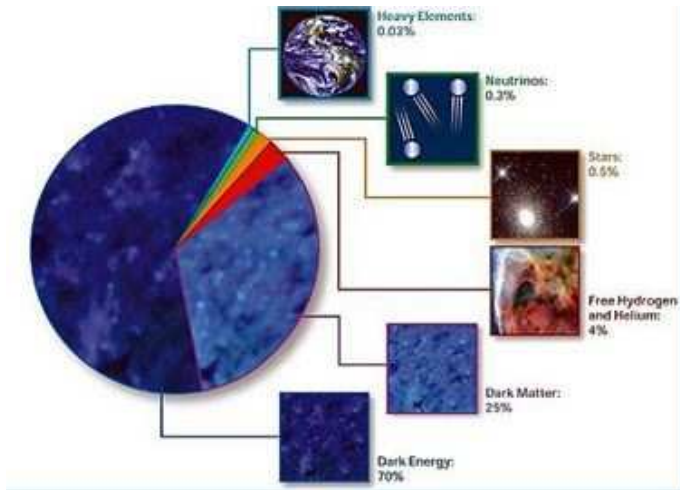
May 08, 2012



# Outline

- Introduction
- Inverse Seesaw for Neutrino Mass
- Inelastic Dark Matter
- Collider Phenomenology
- Conclusion

# Our Universe is mostly Dark!

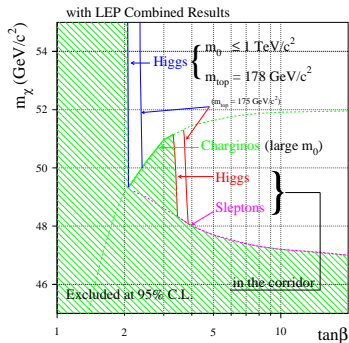


# Dark Matter in MSSM

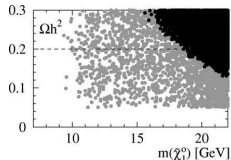
- Neutral LSP is a *natural* DM candidate in SUSY models with  $R$ -parity.
- Two CDM candidates in MSSM:
  - **Left Sneutrino**  $\tilde{\nu}_L$ : Ruled out (invisible  $Z$ -width + relic density + direct detection constraints).
  - **Lightest Neutralino**  $\tilde{\chi}_1^0$  ( $\tilde{B}^0$ ,  $\tilde{W}_{3L}^0$ ,  $\tilde{h}_u^0$ ,  $\tilde{h}_d^0$ ): Only DM candidate.

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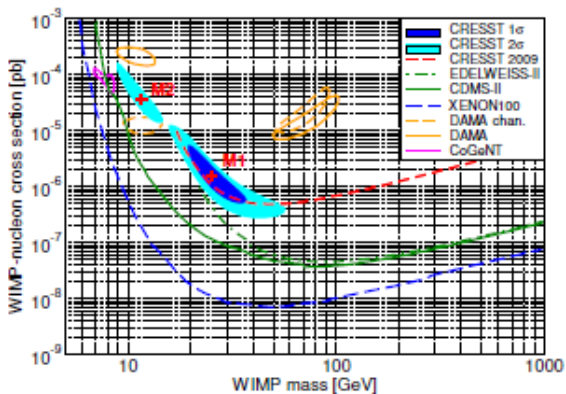


- LEP lower limit:  $M_{\tilde{\chi}_1^0} > 47$  GeV (with gaugino unification). [PDG '10]
- Slightly tighter ( $> 50$  GeV) for cMSSM.
- More generic bound from cosmology:  $> 18$  GeV. [Hooper, Plehn '02]



# Light Dark Matter?

[Angloher *et al.* '11]



If confirmed, might need to look beyond MSSM.

# Neutrino Mass and Seesaw

- Another reason to go beyond MSSM.
- A simple way is to introduce SM singlets and break  $(B - L)$ -symmetry at tree-level  $\implies$  **Seesaw mechanism**
- Observed baryon asymmetry can be explained by **leptogenesis**.
- In SUSY seesaw: Superpartner of the singlet neutrino(s) with a small admixture of left sneutrino can be a DM candidate.

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- Observed baryon asymmetry can be explained by **leptogenesis**.
- In SUSY seesaw: Superpartner of the singlet neutrino(s) with a small admixture of left sneutrino can be a DM candidate.
- Could be directly probed at colliders if the seesaw scale is  $\mathcal{O}(\text{TeV})$ .
- **Is a TeV-scale SUSY seesaw consistent with neutrino mass, leptogenesis, (light) DM and coupling unification?**



# Canonical Seesaw

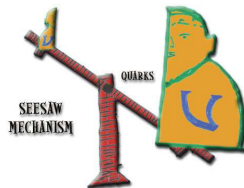
Add one set of SM singlet Majorana neutrinos. [ Minkowski '77; Yanagida '79; Glashow '79; Gell-Mann, Ramond, Slansky '80; Mohapatra, Senjanović '80]

$$W \supset y_{\nu ij} L_i H_u N_j^c + M_{N_i} N_i^c N_i^c,$$

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix}$$

$$m_\nu^{\text{light}} = -M_D M_N^{-1} M_D^T$$

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Sub-eV  $m_\nu$  for heavy  $M_N$ .

- TeV scale  $M_N$  possible for tiny  $M_D \lesssim m_e$  (unless fine-tuned)  $\implies$  Hard to test MSSM+seesaw at colliders.
- SO(10)-GUT embedding  $\implies$  relates  $M_D$  to charged fermion sector.
- Predicts the seesaw scale  $M_N \sim 10^{10-14}$  GeV.

# Inverse Seesaw

Add two sets of SM singlets: One Dirac ( $N$ ) and one Majorana ( $S$ ) fermion. [Mohapatra '86; Mohapatra, Valle '86]

$$W \supset y_{\nu ij} L_i H_u N_j^c + M_{Nij} N_i^c S_j + \mu_{Sij} S_i S_j,$$

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & M_D & 0 \\ M_D^T & 0 & M_N \\ 0 & M_N^T & \mu_S \end{pmatrix}$$

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$$\left( \frac{m_\nu}{0.1 \text{ eV}} \right) \simeq \left( \frac{M_D}{100 \text{ GeV}} \right)^2 \left( \frac{\mu_S}{1 \text{ keV}} \right) \left( \frac{M_N}{10 \text{ TeV}} \right)^{-2}$$

- TeV scale  $M_N$  possible even with large  $M_D \sim m_t$ .
- Smallness of  $\mu_S$  is “technically natural”.

# SUSY Inverse Seesaw

- Inverse seesaw within MSSM gauge group  $SU(2)_L \times U(1)_Y$  – Needs to omit terms like  $LH_U S$  and  $NN$  allowed by gauge symmetry.
- Could extend the gauge symmetry to  $SU(2)_L \times U(1)_Y \times U(1)_{B-L}$  [Khalil, Okada, Toma '11].

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- Could extend the gauge symmetry to  $SU(2)_L \times U(1)_Y \times U(1)_{B-L}$  [Khalil, Okada, Toma '11].
- However, this scenario does not arise from GUT.
- To realize inverse seesaw at TeV scale within a GUT framework, we must use the SUSYLR gauge group  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ . [BD, Mohapatra '09]
- Minimal inverse seesaw structure arises *naturally* as the  $SU(2)_R$  gauge symmetry forbids other terms in the superpotential:

$$\mathcal{W} = \mathcal{W}_{\text{MSSM}} + h_\nu L \Phi L^c + h_S S \phi_R L^c + S \mu_S S$$

# Sneutrino LSP in Inverse Seesaw

$$\mathcal{M}_{\tilde{\nu}} = \begin{pmatrix} m_{\tilde{\nu}^\dagger \tilde{\nu}}^2 & m_{\tilde{\nu}^\dagger \tilde{\nu}^{c\dagger}}^2 & m_{\tilde{\nu}^\dagger \tilde{S}}^2 \\ (m_{\tilde{\nu}^\dagger \tilde{\nu}^{c\dagger}}^2)^\dagger & m_{\tilde{\nu}^c \tilde{\nu}^{c\dagger}}^2 & m_{\tilde{\nu}^c \tilde{S}}^2 \\ (m_{\tilde{\nu}^\dagger \tilde{S}}^2)^\dagger & (m_{\tilde{\nu}^c \tilde{S}}^2)^\dagger & m_{\tilde{S}^\dagger \tilde{S}}^2 \end{pmatrix}$$

- In the limit  $\mu_S \rightarrow 0$ , the **complex scalar** eigenstate for sneutrino LSP:

$$\tilde{\chi}_1 = \sum_{i=1}^3 \left[ (U^\dagger)_{1\nu_i} \tilde{\nu}_i + (U^\dagger)_{1\nu_i^c} \tilde{\nu}_i^{c\dagger} + (U^\dagger)_{1S_i} \tilde{S}_i \right]$$

$c_{(0,1,2)} \equiv \sum_{i=1}^3 |U_{1(\nu_i, \nu_i^c, S_i)}|^2$  determines the fraction of each component.

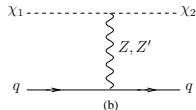
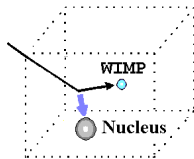
- The  $\not{L}$  term  $S\mu_S\tilde{S}$  induces the splitting terms  $\sum_{m,n=1}^9 A_{mn} \tilde{\chi}_m^\dagger \tilde{\chi}_n$  through the  $F$ -term:

$$\left| \frac{\partial \mathcal{W}}{\partial \tilde{S}} \right|_{\tilde{S}=\tilde{S}}^2 = \left| \mu_S \tilde{S} + h_S \nu_{Rd} \tilde{\nu}^c \right|^2$$

- Leads to two **real scalar** fields ( $\chi_{1,2}$ ) for the LSP with mass splitting

$$\delta M_\chi = \frac{|A_{11}|}{M_\chi} \quad (A_{11} \sim \mu_S \nu_R)$$

# A Natural Inelastic DM Candidate



- Gauge bosons *necessarily* connect  $\chi_1$  to  $\chi_2$  through  $iZ^\mu(\chi_1\partial_\mu\chi_2 - \chi_2\partial_\mu\chi_1)$
- Naturally leads to **inelastic DM** for direct detection.
- The elastic channel through Higgs is typically small due to Yukawa suppression.
- Typical splitting  $\delta M_\chi \sim$  a few keV is comparable to recoil energy of the nucleus  $\implies$  Observable effects in direct detection.
- **Inelasticity of the DM intimately linked to the small Majorana mass of the neutrino.** [An, BD, Cai, Mohapatra '11]



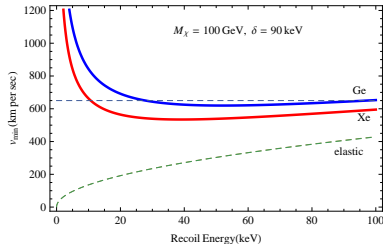
# iDM Scattering

[Tucker-Smith, Weiner '01]

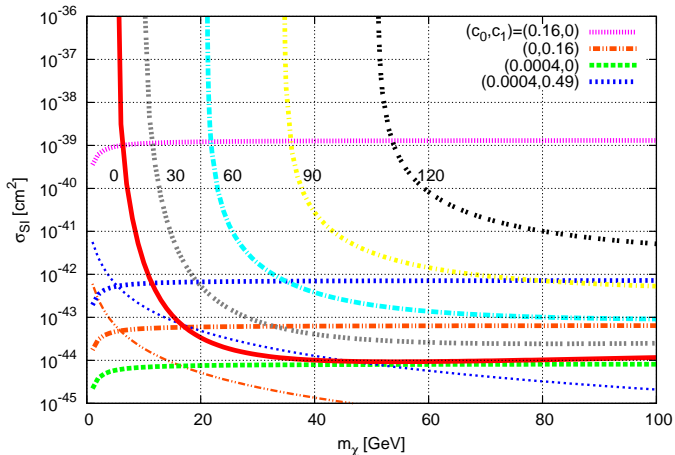
$$\frac{dR}{dE_r} = \frac{\rho_{\chi_1}}{M_{\chi}} \int_{|\mathbf{v}| > v_{\min}} d^3\mathbf{v} \frac{f(\mathbf{v})}{|\mathbf{v}|} \frac{A_{\text{eff}}^2 \bar{\sigma}_N}{2\mu_{\chi N}} F^2(|\mathbf{q}|)$$

$$v_{\min} = \frac{1}{\sqrt{2M_A E_r}} \left( \frac{M_A E_r}{\mu_{\chi A}} + \delta \right)$$

- Sampling only high-velocity tail of Maxwellian velocity distribution.
- Favors target nuclei with heavier mass.
- Threshold velocity for iDM scattering to occur:  $v_{\text{threshold}} = \sqrt{2\delta/\mu_{\chi A}}$ .
- No events at low recoil energies.
- A peak in the scattering rate.
- Enhanced annual modulation.



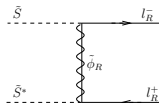
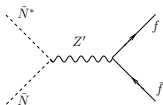
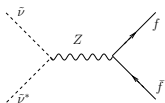
# Direct Detection Cross Section



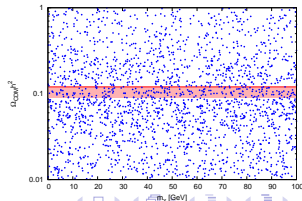
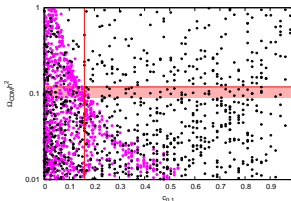
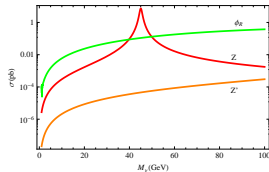
XENON100 constraints restrict the sneutrino DM to be light. [An, BD, Cai, Mohapatra '11]

# Annihilation of Sneutrino DM in SUSYLR

Recall  $\tilde{\chi}_1 \equiv (\tilde{\nu}, \tilde{N}^\dagger, \tilde{S})$ . Dominant channels:



- Both s- and t-channel are p-wave scattering.
- Need LH component < 40% to satisfy relic density and invisible Z-decay width constraints.
- Relic Density: Very light sneutrino DM allowed. [An, BD, Cai, Mohapatra '11]



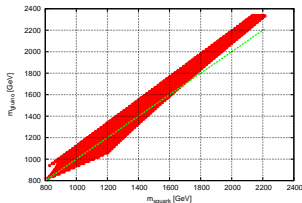
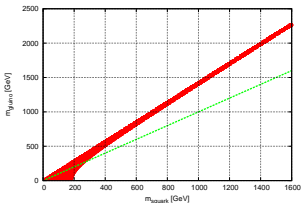
# Sneutrino vs Neutralino DM at Collider

- Cascade decay of squarks and gluinos through charginos and neutralinos, which further go to sneutrino LSP with large  $\cancel{E}_T$ :

$$\tilde{\chi}_1^0 \rightarrow \nu\tilde{\nu}_1, \quad \tilde{\chi}_1^\pm \rightarrow \ell^\pm\tilde{\nu}_1,$$

whereas for neutralino LSP,  $\tilde{\chi}_1^\pm \rightarrow W^\pm\tilde{\chi}_1^0, \tilde{f}\tilde{f}\tilde{\chi}_1^0$

- For detailed analysis, need the sparticle spectrum.
  - (SN1)  $m_{\tilde{g}} < m_{\tilde{q}}$ : 4 jets +  $\cancel{E}_T$  + (0,1,2) leptons.
  - (SN2)  $m_{\tilde{g}} \simeq m_{\tilde{q}}$ : 2-3 jets +  $\cancel{E}_T$  + (0,1,2) leptons.
  - (SN3)  $m_{\tilde{g}} > m_{\tilde{q}}$ , two hard jets +  $\cancel{E}_T$  + 1-2 leptons.
- For SUSY inverse seesaw (in mSUGRA):

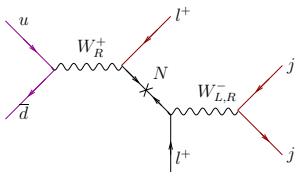


[BD (preliminary)]

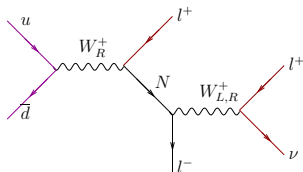
# Type I vs. Inverse seesaw at Collider

- TeV scale heavy RH neutrinos  $\implies$  may be produced on shell at LHC.
- **Pseudo-Dirac fermions** (with small Majorana component), unlike in type I case (purely Majorana).
- The “smoking gun” LHC signature for type-I,  $pp \rightarrow l_{\alpha}^{\pm} l_{\beta}^{\pm} + \text{jets}$ , will be suppressed for inverse seesaw.
- The dominant signal will be the triplepton event  $pp \rightarrow l_{\alpha}^{\pm} l_{\beta}^{\pm} l_{\gamma}^{\mp} \nu(\bar{\nu}) + \text{jets}$ .
- Can be used to distinguish a heavy Dirac neutrino from a Majorana. [del

Aguila, Aguilar-Saavedra, de Blas '09; Chen, BD '11]



(a) Majorana  $N$



(b) Dirac  $N$

# Summary and Outlook

- SUSY inverse seesaw naturally leads to iDM with inelasticity linked to the small Majorana mass.
- Light sneutrino dark matter ( $\lesssim 20$  GeV) allowed by relic density, unlike in typical MSSM scenario.
- Could be important if the DM mass is in the few GeV range.
- Distinct collider signatures for sneutrino LSP could be searched for.
- Inverse seesaw can be identified at LHC in multi-lepton channel.

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- Other observable low-energy effects in leptonic sector.
- A natural realization of resonant leptogenesis, with quasi-degeneracy explained by smallness of Majorana neutrino mass.
- Can be realized as a low-energy theory of a SUSY  $SO(10)$ -GUT, proton decay rates being consistent with current bounds for TeV-scale squark masses.

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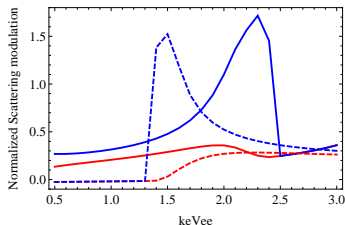
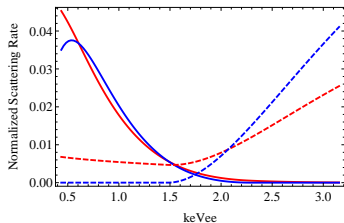
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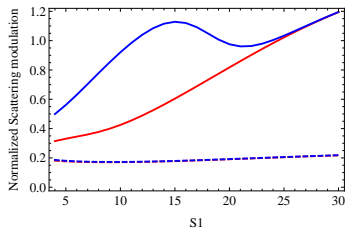
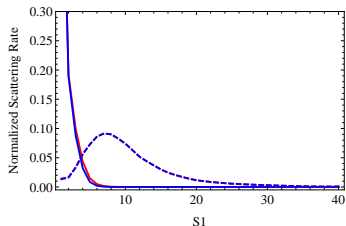


# Scattering Rate and Annual Modulation

CoGeNT



XENON

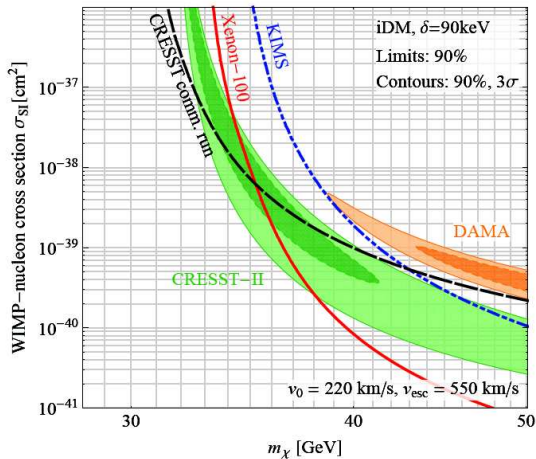


$$(c_0, c_1) = \begin{cases} (0.001, 0.1) \\ (0.1, 0.001) \end{cases}, \quad (M_\chi, \delta) = \begin{cases} (10 \text{ GeV}, 20 \text{ keV}) \\ (50 \text{ GeV}, 60 \text{ keV}) \end{cases} \begin{matrix} \text{(solid)} \\ \text{(dashed)} \end{matrix}$$

▶ [\[An, BD, Cai, Mohapatra '11\]](#)

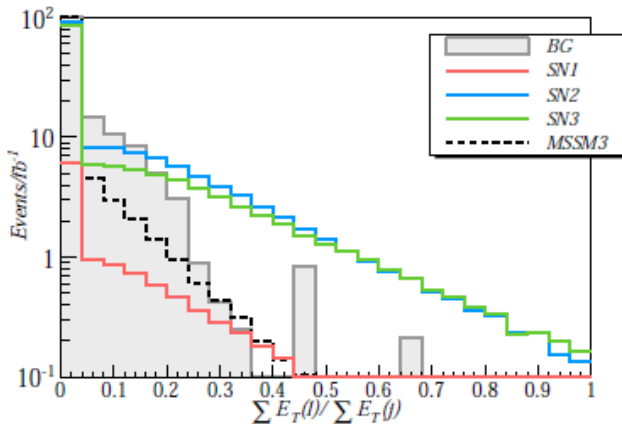


## Fitting CRESST, DAMA, ...



[Kopp, Schwetz, Zupan '11]

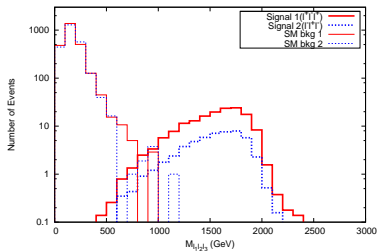
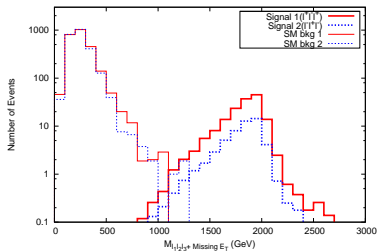
# Signal Distribution for LHC7



$$E_T > 300 \text{ GeV}, n(j) > 2, p_T(j_1) > 100 \text{ GeV}, p_T(j) > 50 \text{ GeV}$$

# Trilepton Signal for Inverse Seesaw

[Chen, BD '11]



Can also be used to discover the heavy gauge boson  $W_R$ .