

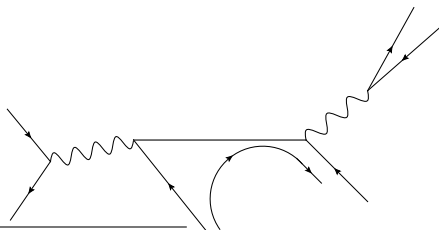
# Lepton Number Violation and $W'$ Chiral Couplings at the LHC<sup>1</sup>

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# The Standard Model (SM) of Particle Physics

- **SM**: A fantastically successful theory that describes the microscopic interactions of matter.
- Consists of 6 objects:  $\ell, q; \bar{u}, \bar{d}, \bar{e}; \Phi$ , with huge multiplicity.
- Impose local invariance, break with  $\langle \Phi_0 \rangle = v$ , and voilà!  
We have a universe!

- ▶ Quarks ( $g, \gamma, W, Z$ )
- ▶ Neutral leptons (neutrinos) ( $W, Z$ )
- ▶ Charged leptons ( $\gamma, W, Z$ )
- ▶ Gluon mediates  $SU(3)_{Color}$
- ▶ Photon mediates  $U(1)_{EM}$
- ▶  $W^\pm/Z^0$  mediate  $SU(2)_{Left}$
- ▶  $h$  dynamically generates masses
  - Only missing piece!

1978: SLAC <b>u</b> up quark	1971: Brookhaven & SLAC <b>c</b> charm quark	1995: Fermilab <b>t</b> top quark	1974: DESY <b>g</b> gluon
1978: SLAC <b>d</b> down quark	1971: Manchester University <b>s</b> strange quark	1977: Fermilab <b>b</b> bottom quark	1993: Washington University $\gamma$ photon
1928: Savannah River Plant $\nu_e$ electron neutrino	1976: Brookhaven $\nu_\mu$ muon neutrino	2000: Fermilab $\nu_\tau$ tau neutrino	1983: CERN <b>W</b> W boson
1933: Cavendish Laboratory <b>e</b> electron	1937: Caltech and Harvard $\mu$ muon	1976: SLAC $\tau$ tau	1973: CERN <b>Z</b> Z boson

# Even with SM Higgs, Questions Remain: Motivation for New Physics

- ▶ What is the origin of **neutrino masses**?
  - ▶ Dirac mass terms require  $N_R$
  - ▶  $N_R$  are SM singlets and may have Majorana mass terms, too.
- ▶ What is the origin of **Parity Asymmetry** in SM
  - ▶ Is there a  $V + A$  structure,  $SU(2)_R$ , too? Is it from  $SU(5)$ ?
  - ▶ Lots of different phenomenology.
- ▶ Are these even independent questions?

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- ▶ What is the origin of **Parity Asymmetry** in SM
  - ▶ Is there a  $V + A$  structure,  $SU(2)_R$ , too? Is it from  $SU(5)$ ?
  - ▶ Lots of different phenomenology.
- ▶ Are these even independent questions?
- ▶ Left-Right Symmetric theories, **GUTS**, **SUSY GUTS**,  
Extra Dim w/  $KK$ , Little Higgs w/ **new gauge sectors**
  - ▶ **Commonality 1**:  $N_R$  (SM singlet) + heavy mass states
  - ▶ **Commonality 2**: Some charged vector boson  $W'^{\pm}$ .

### 3. Model Discrimination with $W'$ and $N$

**Issue:** These are phenomenologically similar models.

- Measuring chiral couplings to  $W'$  is imperative.

### 3. Model Discrimination with $W'$ and $N$

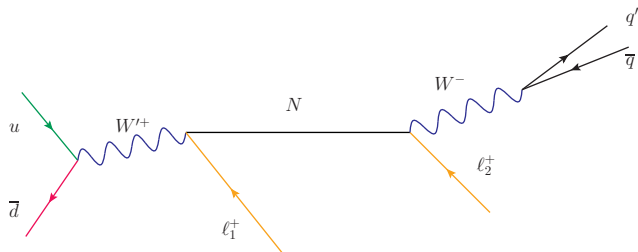
**Issue:** These are phenomenologically similar models.

- Measuring chiral couplings to  $W'$  is imperative.

**Solution:** Use model-independent parameterization.

- Parameters can then be measured with the spectacular

$L$ -Violating process<sup>2</sup>:  $u\bar{d} \rightarrow W'^+ \rightarrow N\ell^+ \rightarrow \ell^+\ell^+q'\bar{q}$



<sup>2</sup>Keung & Senjanovic [[PRL 50 \(1983\)](#)]

### 3. Why $u\bar{d} \rightarrow W'^+ \rightarrow N\ell^+ \rightarrow \ell^+\ell^+q'\bar{q}$ ?

1.  $W'$  is heavy<sup>3</sup>. At the LHC, an  $s$ -channel  $u\bar{d} \rightarrow W'^+$  annihilation provides the best opportunity to produce it.
2.  $N$  must also be heavy<sup>4</sup>. The  $W'^+ \rightarrow N\ell^+$  sub-process is the least constrained by phase space (v.s.  $t$ -channel  $N$  exchange).
3.  $W^- \rightarrow q'\bar{q}(jj)$  allows for full reconstruction of kinematics;  $W$ -tagging is also a powerful background reducer.
4.  $pp \rightarrow \ell^+\ell^+jj$  is a lepton number-violating process and a “smoking-gun” indication of Majorana behavior<sup>5</sup>.

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<sup>3</sup>CMS Collaboration [[arXiv:1204.4764](#)]

<sup>4</sup>ATLAS Collaboration [[arXiv:1203.5420](#)]

<sup>5</sup>T. Han, et. al. [[arXiv:hep-ph/0505260](#)]

# Outline

Synopsis: *We have investigated the production of a heavy Majorana  $N$  in association with a heavy  $W'$ , and have determined an efficient way to measure the couplings associated with a model-independent parameterization of  $W'$  at the LHC.*

1. The Standard Model
2. Motivation
  - ▶ For New Physics
  - ▶ For Lepton No. Violation in association with Chiral Couplings
3. Model Discrimination with  $W'$  and  $N$ 
  - ▶ Utility of the  $pp \rightarrow \ell^+ \ell^+ jj$  collider signature
4. Model-Independent Parameterization
5. Analytic Results
6. Numerical Results
7. Summary & Conclusion



## 4. Model-Independent Parameterization (1/1.5)

- ▶  $W'$  coupling to quarks:

$$\mathcal{L} = -\frac{1}{\sqrt{2}} W'_\mu{}^+ \bar{u}_i V_{ij}^{CKM'} \gamma^\mu [g_R^q P_R + g_L^q P_L] d_j + h.c.$$

- ▶  $W'$  coupling to leptons.

$$\begin{aligned} \mathcal{L} = & -\frac{g_R^\ell}{\sqrt{2}} W'_\mu{}^+ \left[ \sum_{m=1}^3 \bar{\nu}_m^c C_{m\ell}^R + \bar{N} D_{N\ell}^R \right] \gamma^\mu P_R \ell^- \\ & -\frac{g_L^\ell}{\sqrt{2}} W'_\mu{}^+ \left[ \sum_{m=1}^3 \bar{\nu}_m^c C_{m\ell}^{L*} + \bar{N}^c D_{N\ell}^{L*} \right] \gamma^\mu P_L \ell^- + h.c. \end{aligned}$$

- ▶ E.g., Left-Right Symmetric  $W'_R$

- ▶ Light mass mixing is small and heavy mass mixing is large:

$$g_L \equiv 0, \quad |C_{m\ell}^R| \sim \mathcal{O}\left(\frac{m_m}{m_N}\right) \text{ for } m \leq 3, \quad \text{and} \quad |D_{N\ell}^R| \sim \mathcal{O}(1)$$

## 4. Model-Independent Parameterization (1.5/1.5)

- ▶ SM  $W$  coupling to leptons:

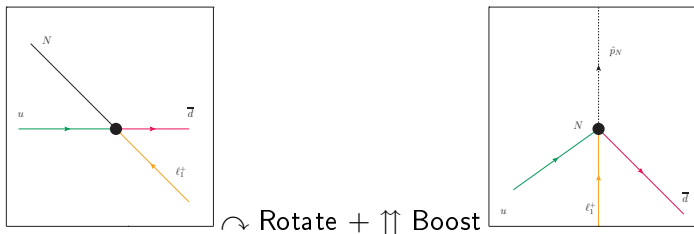
$$\mathcal{L} = -\frac{g}{\sqrt{2}} W_{\mu}^{\prime+} \left[ \sum_{m=1}^3 \bar{\nu}_m U_{m\ell}^* + \bar{N}^c V_{N\ell}^* \right] \gamma^{\mu} P_L \ell^{-} + h.c.$$

- ▶ Light mass mixing is large and heavy mass mixing is small:

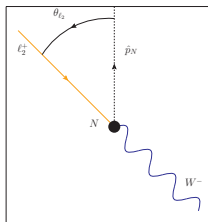
$$|U_{m\ell}| \sim \mathcal{O}(1), \quad \text{and} \quad |V_{m\ell}| \sim \mathcal{O}\left(\frac{m_m}{m_N}\right) \quad \text{for } m \leq 3$$

## 5. Pre-Results: Definition of Observables $\theta_{l_2}$ and $\Phi$

**Production Plane:** Take initial  $2 \rightarrow 2$  process in CM frame, then rotate and boost into  $N$ 's rest frame



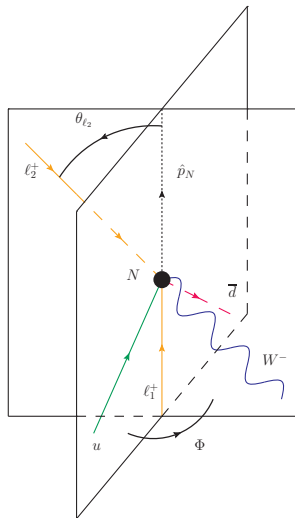
**Decay Plane:**  $N$ 's products relative to  $\hat{p}_N$  (Direction of  $N$  in CM)



## 5. Pre-Results: Definition of Observables $\theta_{\ell_2}$ and $\Phi$

**Production Plane** and **Decay Plane** share same axis, so angle between two can be defined

- Algebraically: dot products of cross products of 3-momenta



## 5. Analytical Result I: Coupling to Final-State Leptons

- Analytical calculation of angular distributions leads to fascinating results!

$$\frac{d\hat{\sigma}}{d\cos\theta_{\ell_2}} = \frac{\hat{\sigma}_0}{2} \left[ 1 + \mathcal{A} \cdot \left( \frac{g_R^{\ell 2} - g_L^{\ell 2}}{g_R^{\ell 2} + g_L^{\ell 2}} \right) \cdot \cos\theta_{\ell_2} \right],$$

where  $\mathcal{A}$  contains a few mass ratios, etc., and

$$\hat{\sigma}_0 = \hat{\sigma}_{Tot.}(u\bar{d} \rightarrow \ell^+\ell^+W^-) \times BR(W \rightarrow q\bar{q}').$$

- ▶ This is a measurement of  $W'$  coupling to leptons.
- ▶ Slope of angular distribution is sensitive to handedness of  $W'$ .
- ▶  $\mathcal{A} \rightarrow -\mathcal{A}$  for Dirac neutrino case ( $\ell^+\ell^-jj$ ).

## 5. Analytical Result II: Coupling to Initial-State Quarks

- We see some surprising results, too!

$$\frac{d\hat{\sigma}}{d\Phi} = \frac{\hat{\sigma}_0}{2\pi} \left[ 1 + \mathcal{B} \cdot \left( \frac{g_R^{q^2} - g_L^{q^2}}{g_R^{q^2} + g_L^{q^2}} \right) \cdot \cos \Phi \right],$$

where  $\mathcal{B}$  contains a few mass ratios, etc., and

$$\hat{\sigma}_0 = \hat{\sigma}_{Tot.}(u\bar{d} \rightarrow \ell^+ \ell^+ W^-) \times \mathcal{BR}(W \rightarrow q\bar{q}').$$

- ▶ This is a measurement of  $W'$  couplings to quarks.
- ▶ Slope of angular distribution is sensitive to handedness of  $W'$ .
- ▶  $\mathcal{B} \rightarrow -\mathcal{B}$  for Dirac neutrino case ( $\ell^+ \ell^- jj$ ).
  - ▶ Majorana nature of  $N$  can be verified with angular distributions!

## 6. Running the Numbers: Monte Carlo Input

To demonstrate usefulness of the  $W'^+ \rightarrow \ell^+ \ell^+ jj$  signal for measuring model parameters, we assume the following input:

- ▶  $pp \rightarrow W'^+ \rightarrow \mu^+ \mu^+ \bar{q} q'$ 
  - ▶  $\sqrt{s} = 14$  TeV  $pp$  Collisions
- ▶  $W'^+$ :
  - ▶  $M_{W'} = 2.5$  TeV
  - ▶  $g_R^{\ell,q} = 1$ ,  $g_L^{\ell,q} = 0$ , i.e., pure gauge state  $W'_R$ .
  - ▶  $g_R^{\ell,q} = 0$ ,  $g_L^{\ell,q} = 1$ , i.e., pure gauge state  $W'_L$ .
  - ▶  $|V_{u\bar{d}}^{CKM'}|^2 = 1$  for the  $u\bar{d}W'^+$  vertex.
- ▶  $N$ :
  - ▶  $m_N = 500$  GeV (only one heavy mass state)
  - ▶  $|V_{\mu N}|^2 = 5.0 \times 10^{-4}$  for the  $N \rightarrow W^- \mu^+$  vertex<sup>6</sup>
  - ▶  $|D_{\mu N}^L|^2 = |D_{\mu N}^R|^2 = 1$  for the  $W'^+ \rightarrow N \mu^+$  vertex

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<sup>6</sup>*G. Belanger, et. al.*, [[hep - ph/9508317](#)]; *D. London*, [[hep - ph/9907419](#)]; *delAguila, et. al* [[arXiv : 0803.4008](#)].

## 6. Numerical Results I: Cross Section

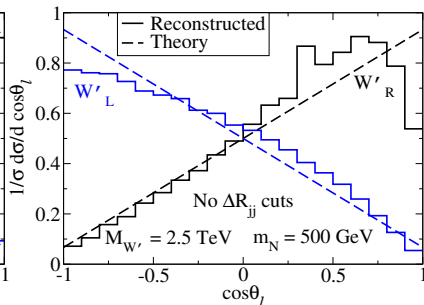
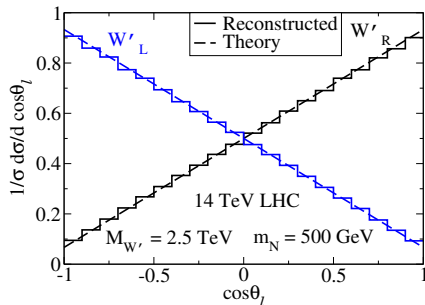
- ▶ Cross section (fb) for  $pp \rightarrow W'^+ \rightarrow \mu^+ \mu^+ \bar{q} q'$
- ▶ Reconstruction/selection details in “Backup Slides”
- ▶ Irreducible background  $< 0.1$  fb

$\sigma(\text{fb})$	7 TeV	7 TeV	14 TeV	14 TeV
Cuts	$W'_L$	$W'_R$	$W'_L$	$W'_R$
Event Reco.	0.095	0.12	2.7	3.6
Smear + Kinematics	0.083	0.088	2.4	2.6
+ Isolation	0.049	0.071	1.2	2.0
+ $M_{W'}^{\text{Cand}} + m_N^{\text{Cand}}$ Cuts	0.026	0.048	0.95	1.8
+ $\cancel{E}_T + m_{jj}$ Cut	0.022	0.042	0.77	1.5
$\mathcal{A} = \sigma_{\text{AllCuts}}/\sigma_{\text{Reco}}$	23%	35%	29%	42%



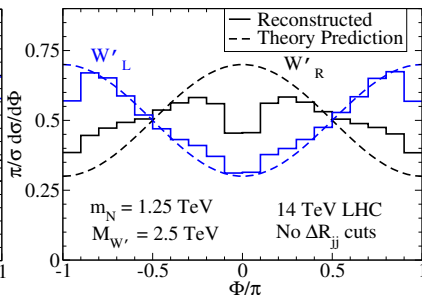
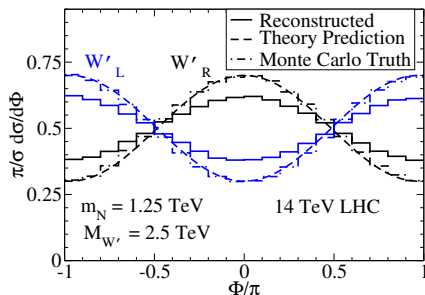
## 6. Numerical Results II: Polar Distribution ( $g^\ell$ )

- ▶ (L) No smearing or cuts; (R) smearing and full selection cuts
- ▶ Great Agreement!
  - ▶ Jet-isolation cut not applied (Jets are very collinear).



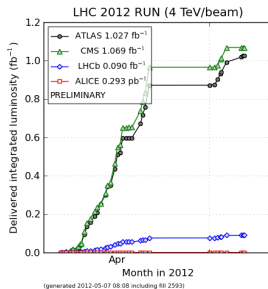
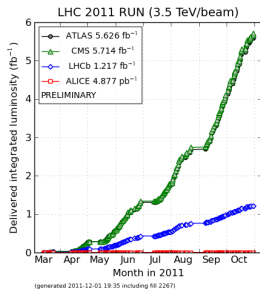
## 6. Numerical Results III: Azimuthal Distribution ( $g^q$ )

- ▶ Dependent on  $(m_N/M_{W'})^2$ , so set  $m_N = 1.25$  TeV for clarity.
- ▶ (L) No smearing or cuts; (R) smearing and full selection cuts
- ▶ Great Agreement!
  - ▶ Jet-isolation cut not applied (Jets are very collinear).

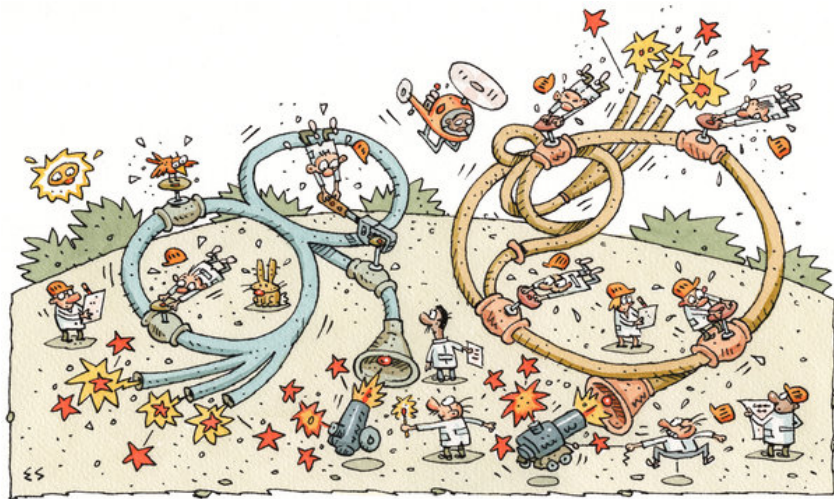


# Summary & Conclusion

- ▶ If new physics appears in the form of  $W'$  &  $N$ , we are ready to exploit it for whatever it is worth.
  - ▶ Chiral couplings to leptons
  - ▶ Chiral couplings to quarks
  - ▶ Discriminating power between Dirac and Majorana behavior
- ▶ The LHC Experiments' Mantra: Be ready for new physics.
  - ▶ With so much data, we better be!



Thank You! Questions?



[Credit: NYTimes [nyti.ms/oPvA0a](https://www.nytimes.com/2010/04/04/science/04robot.html)]

# Backup

## 6. Event Reconstruction (1/2)

- ▶ In order to make our events more realistic, we apply a **Gaussian smearing** to the reconstructed  $\mu$  and  $j$  energies:

$$\frac{\sigma(E)}{E} = \frac{a}{\sqrt{E}} \oplus b,$$

with  $a(a) = 5(100)\%$  and  $b(b) = 0.55(5)\%$ ;

- ▶ Followed by basic **fiducial + kinematic** cuts:

$$p_T^j \geq 30 \text{ GeV}, p_T^\ell \geq 20 \text{ GeV}, |\eta_j| \leq 3.0 \quad |\eta_\ell| \leq 2.5;$$

- ▶ For particles  $i$  and  $j$ , we define the **isolation** parameter  $\Delta R_{ij} = \sqrt{(\Delta\phi_{ij})^2 + (\Delta\eta_{ij})^2}$ , and **require**

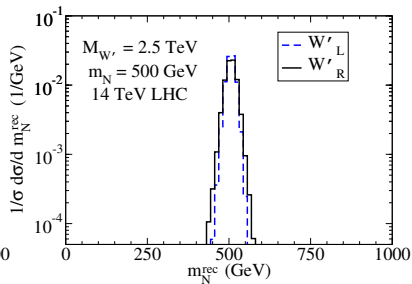
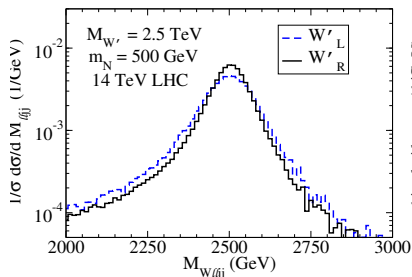
$$\Delta R_{jj} \geq 0.3, \Delta R_{\ell j}^{\min} \geq 0.4,$$

where  $\Delta R_{\ell j}^{\min}$  represents the smallest  $\Delta R_{\ell j}$  amongst  $\mu_1^+$  &  $\mu_2^+$

## 6. Event Reconstruction (2/2)

The invariant mass distributions from reconstructed pseudo-experiment events:

$$\blacktriangleright m_{W'}^{Reco.} = m_{\ell\ell jj} \text{ and } m_N^{Reco.} = \min_{\ell=\mu_1, \mu_2} [m_N - m_{\ell jj}]$$



## 6. LHC Monte Carlo: Event Selection (1/1)

- ▶ Apply standard **smearing**, **kinematic** cuts, and **isolation** cuts.
- ▶ Impose cuts on the **reconstructed candidate mass**  $m_N^{Reco}$  and  $m_{W'}^{Reco}$ :

$$\frac{|m_N^{Reco.} - m_N|}{m_N} \leq 0.1, \& \quad \frac{|\sqrt{\hat{s}} - M_{W'}^{Reco.}|}{M_{W'}} \leq 0.1;$$

- ▶ To reduce background from  $\bar{t}t \rightarrow W^- b \bar{c} \ell^+ \ell^+ \nu_\ell \bar{\nu}_\ell$  decays, we add  $\cancel{E}_T$  &  $m_{W'}^{Reco.}$  cuts:

$$\cancel{E}_T < 30 \text{ GeV}, \quad 60 \text{ GeV} < M_{W'}^{Reco} < 100 \text{ GeV}.$$

- ▶ The **irreducible background** comprises rare SM processes, e.g.,  $pp \rightarrow W^\pm W^\pm W^\mp$ , and contribute at most 0.085 fb.