

Numerical tools to quantify field quality in high-field magnets

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Contents

- 1. Introduction to T-A formulation**
- 2. Effect of screening currents on magnetic field**
- 3. What constitutive law for superconductors?**

Contents

1. Introduction to T-A formulation

2. Effect of screening currents on magnetic field

3. What constitutive law for superconductors?

T-A formulation

- ❑ Proposed in Zhang et al. 2017 *Supercond Sci. Technol.* **30** 024005
- ❑ Particularly efficient to simulate coated conductors in 2D
- ❑ Superconducting layer assumed infinitely thin
 - Width: 4-12 mm
 - Thickness: a few micrometers
 - Very large width-to-thickness ratio

T-A formulation

- ❑ Magnetic vector potential \mathbf{A} to calculate magnetic field everywhere
- ❑ Current vector potential \mathbf{T} to calculate current in the superconductor
- ❑ In COMSOL Multiphysics

- Magnetic field module (mf) for A -part
- PDE (reduced dimensions) for T -part

$$\nabla \times (\nabla \times \mathbf{A}) = \mu \mathbf{J}$$

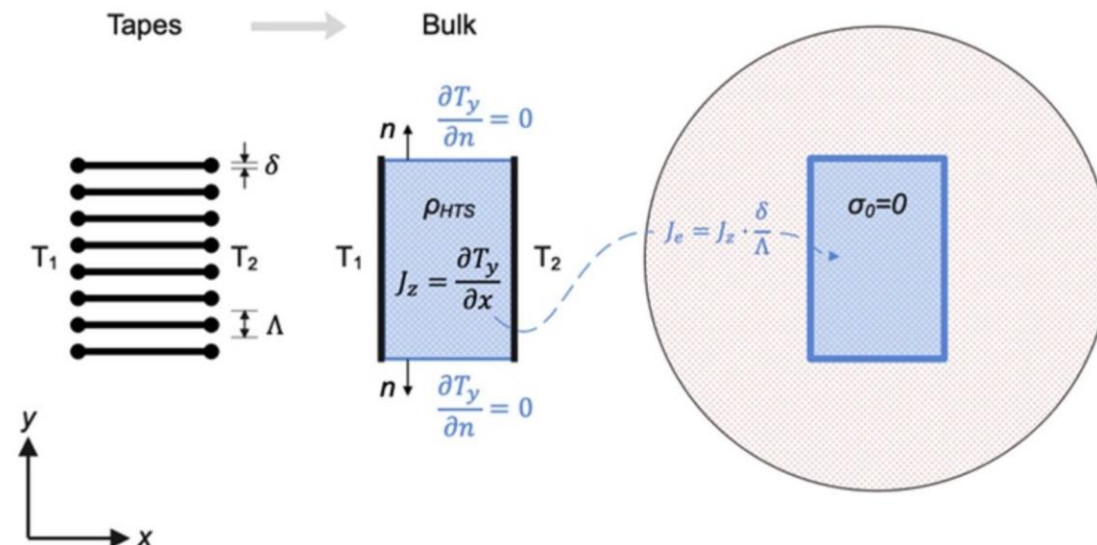
$$\nabla \times (\rho \nabla \times \mathbf{T}) = -\frac{\partial \mathbf{B}}{\partial t}$$

- ❑ Superconductor's resistivity

$$\rho(J) = \frac{E_c}{J_c(\mathbf{B})} \left| \frac{J}{J_c(\mathbf{B})} \right|^{n(\mathbf{B})-1}$$

Homogenization

- ❑ Individual turns homogenized as a bulk conductor (reduction of DOFs)
- ❑ Same current per tape condition maintained
- ❑ Still only one component of \mathbf{T}



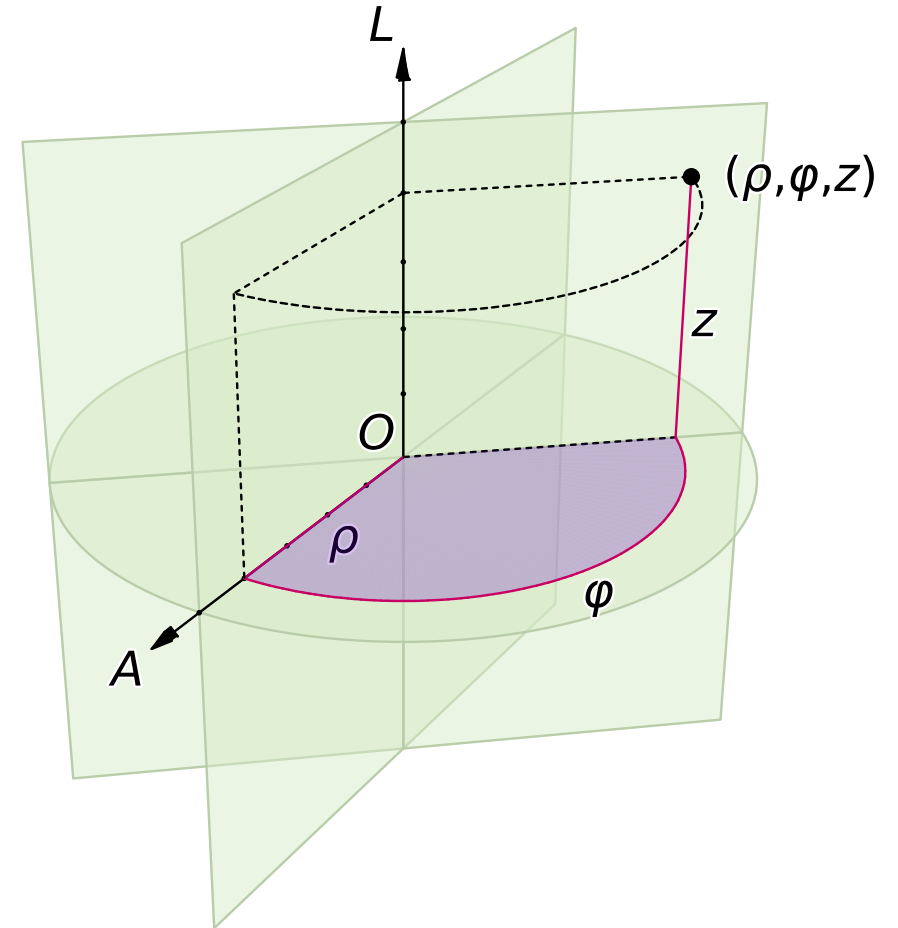
Equations in cylindrical coordinates

$$\nabla \times (\nabla \times \mathbf{A}) = \mu \mathbf{J}$$

$$\nabla^2 A_\varphi = -\mu J_\varphi$$

$$\nabla \times (\rho \nabla \times \mathbf{T}) = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\frac{\partial}{\partial z} \left(\rho_{\text{HTS}} \frac{\partial T_r}{\partial z} \right) = \frac{\partial B_r}{\partial t}$$



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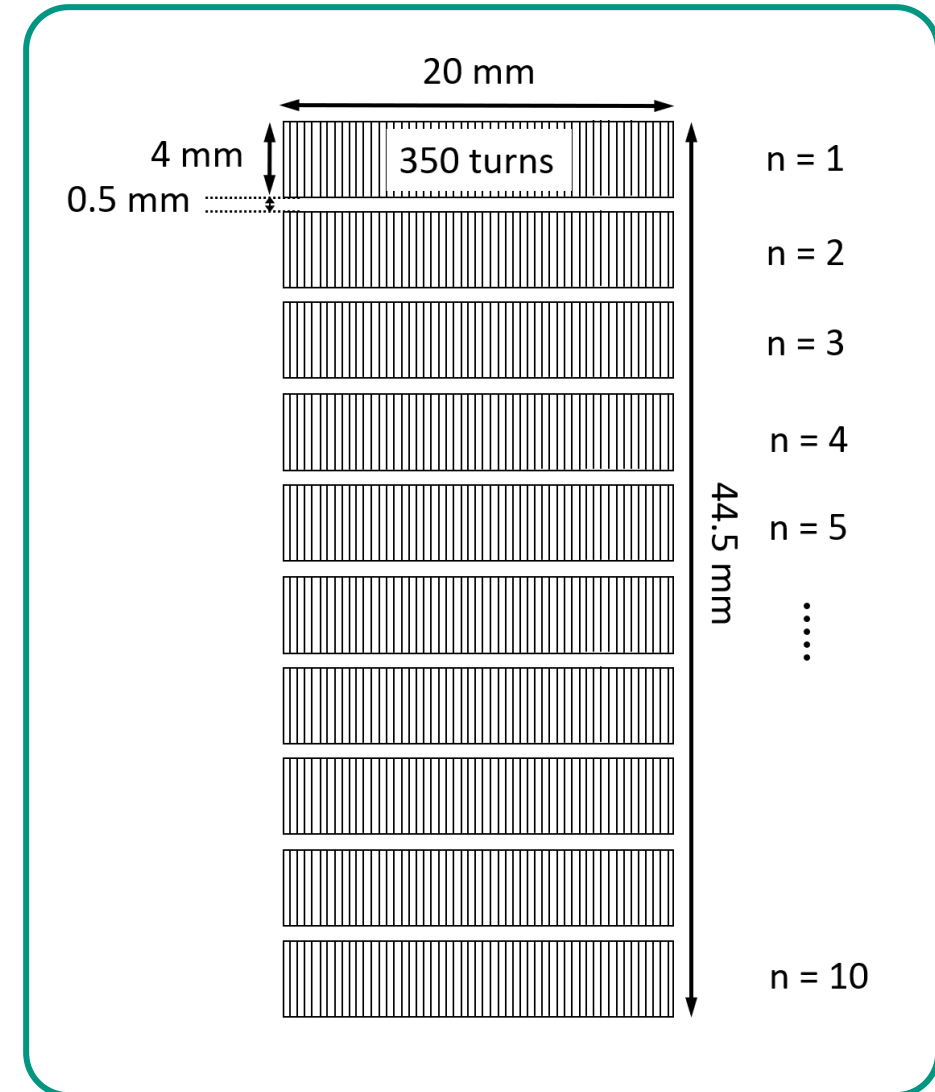
Simulations parameters

2G-HTS Parameters

Parameter	Value
Tape Width	0.004 m
Tape Thickness	5.7143×10^{-5} m
HTS Layer Thickness	1 μ m
Jc0 (20K)	5.49×10^{11} A/m ²
Power-law Index (n)	25

Pancake Coil Geometry

Parameter	Value
Inner Radius	0.02 m
Outer Radius	0.04 m
Num. Tapes	350
Num. Pancakes	10



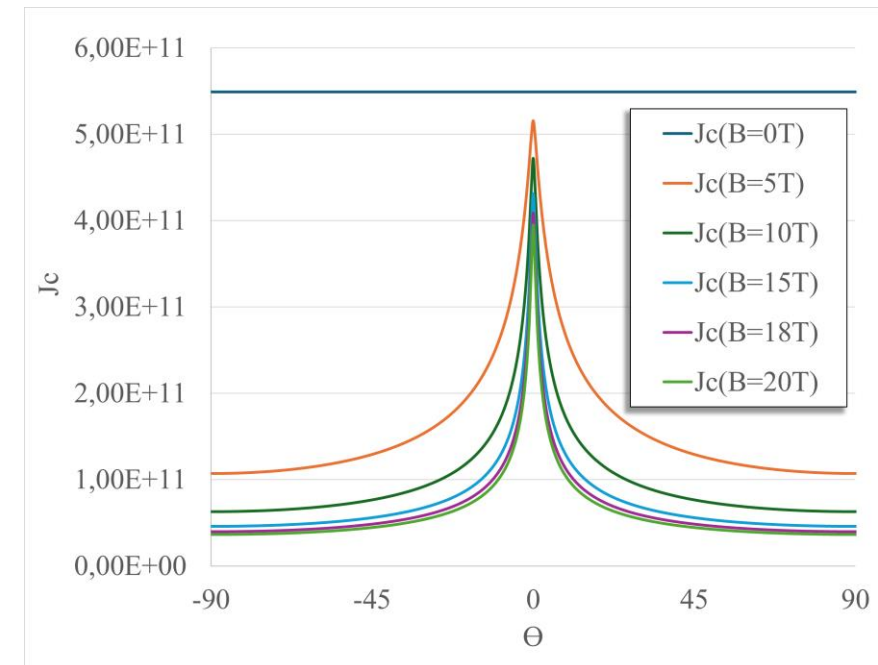
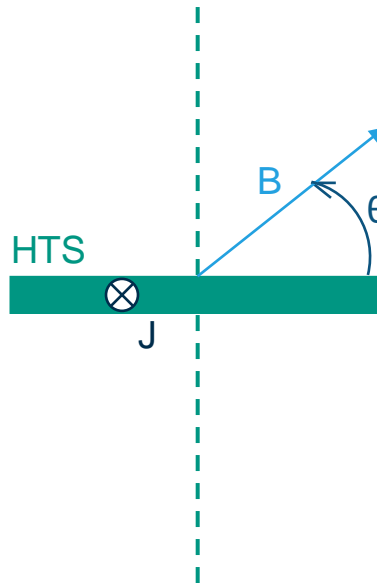
Dependence of critical current on magnetic field

Modified Kim model

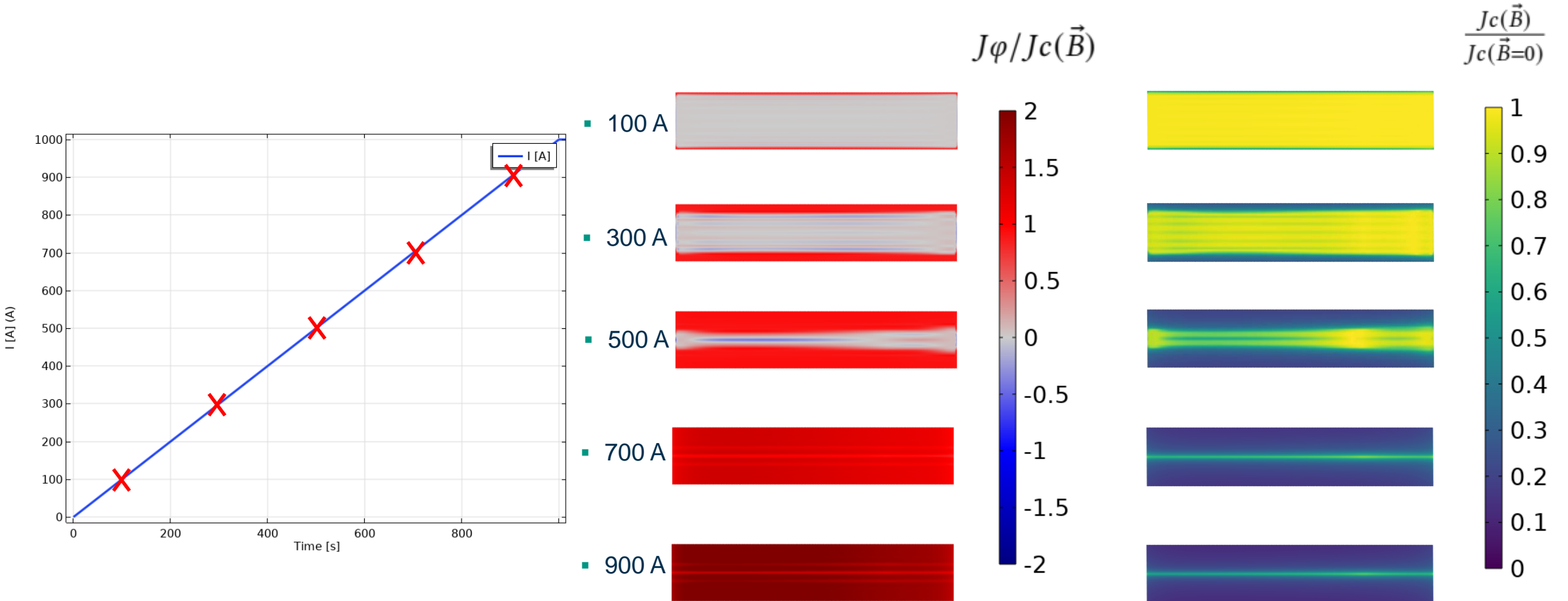
$$J_c(B, \theta) = J_{c0} \left(1 + \epsilon_\theta \left(\frac{B}{B_0} \right)^\alpha \right)^{-\beta}$$

$$\epsilon_\theta = \sqrt{\gamma^{-1} \cos^2(\theta) + \sin^2(\theta)}$$

Parameter	Value
I_{c0} (T=20K)	2196 A
B_0	0.6736 T
γ	18490
α	1.368
β	0.5829

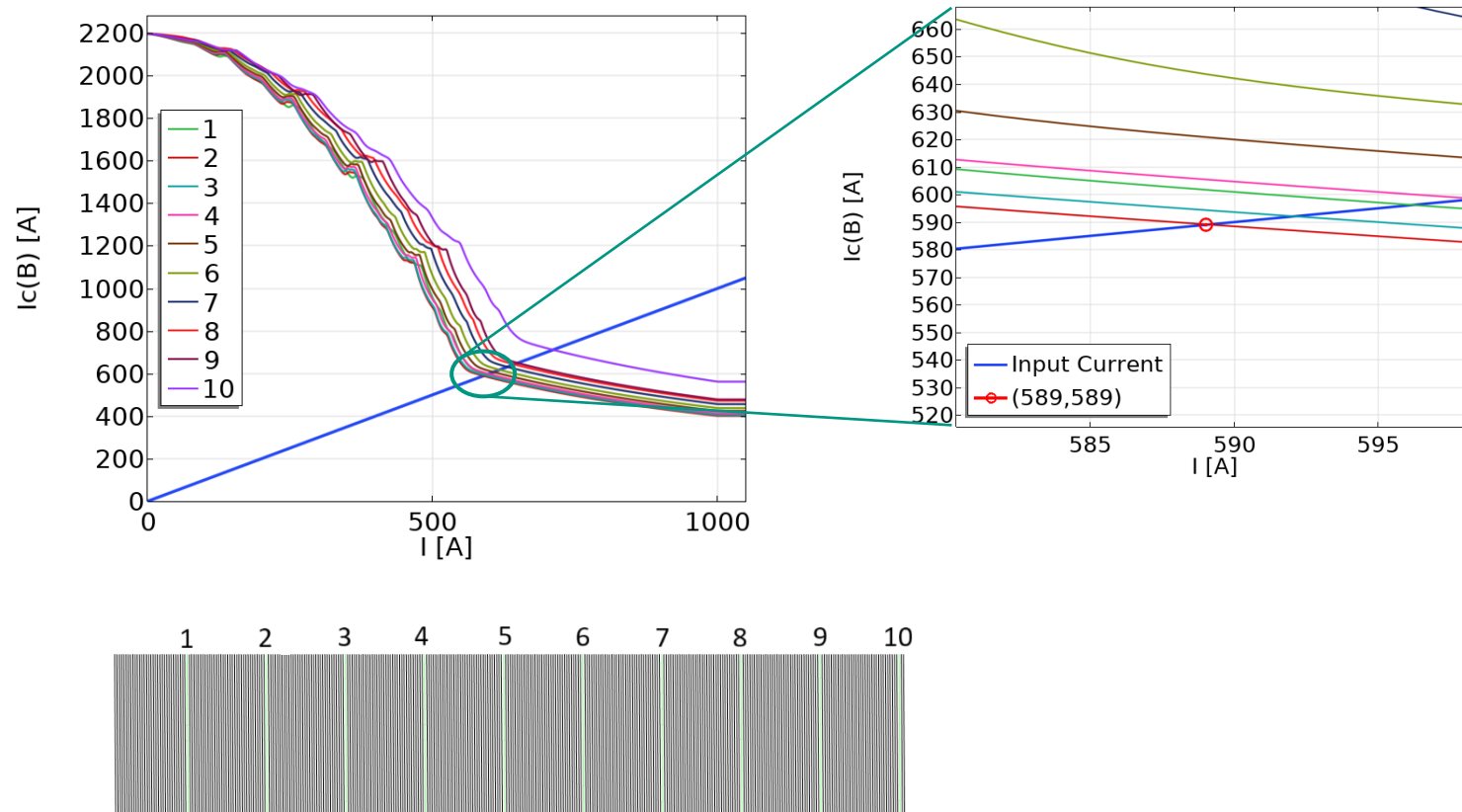


Current density distribution in a single pancake coil

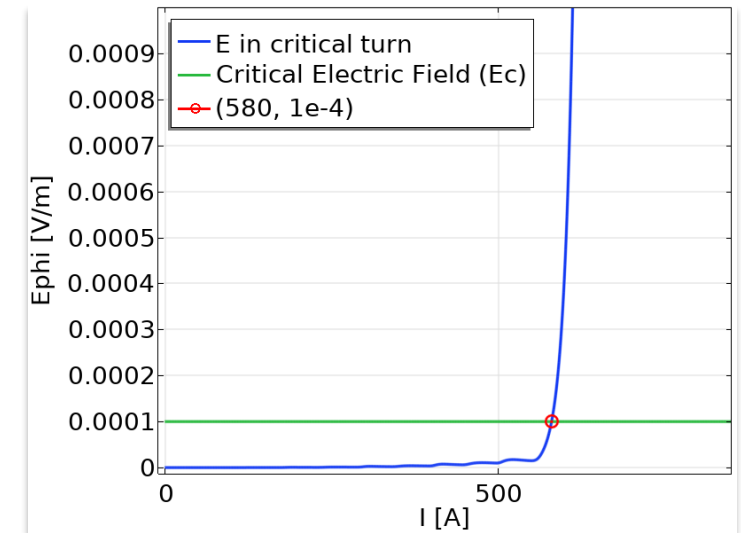


Maximum input current for a single pancake coil

Load line method



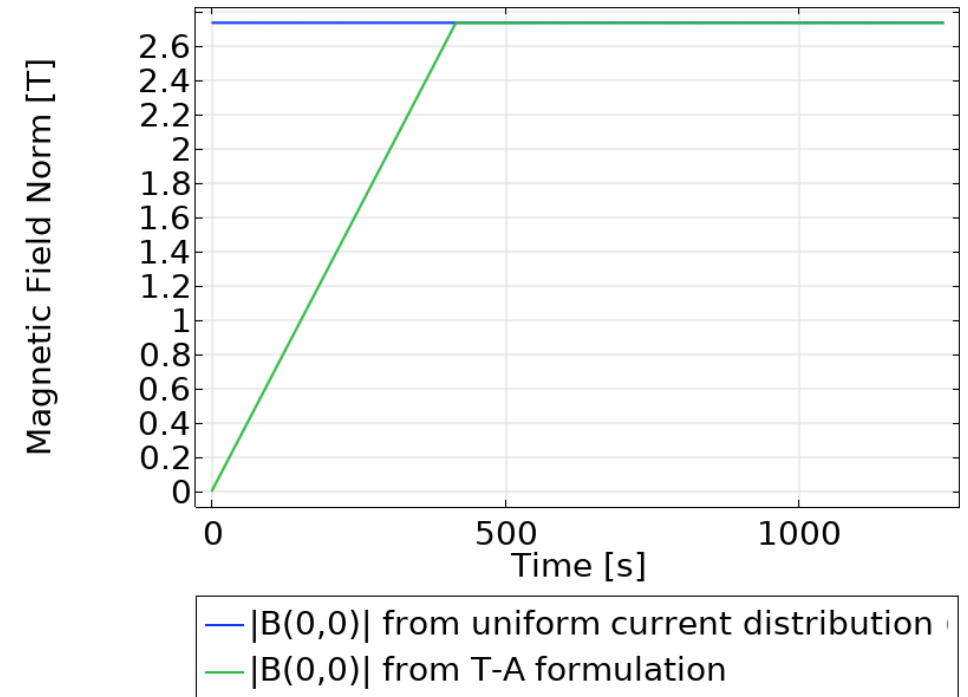
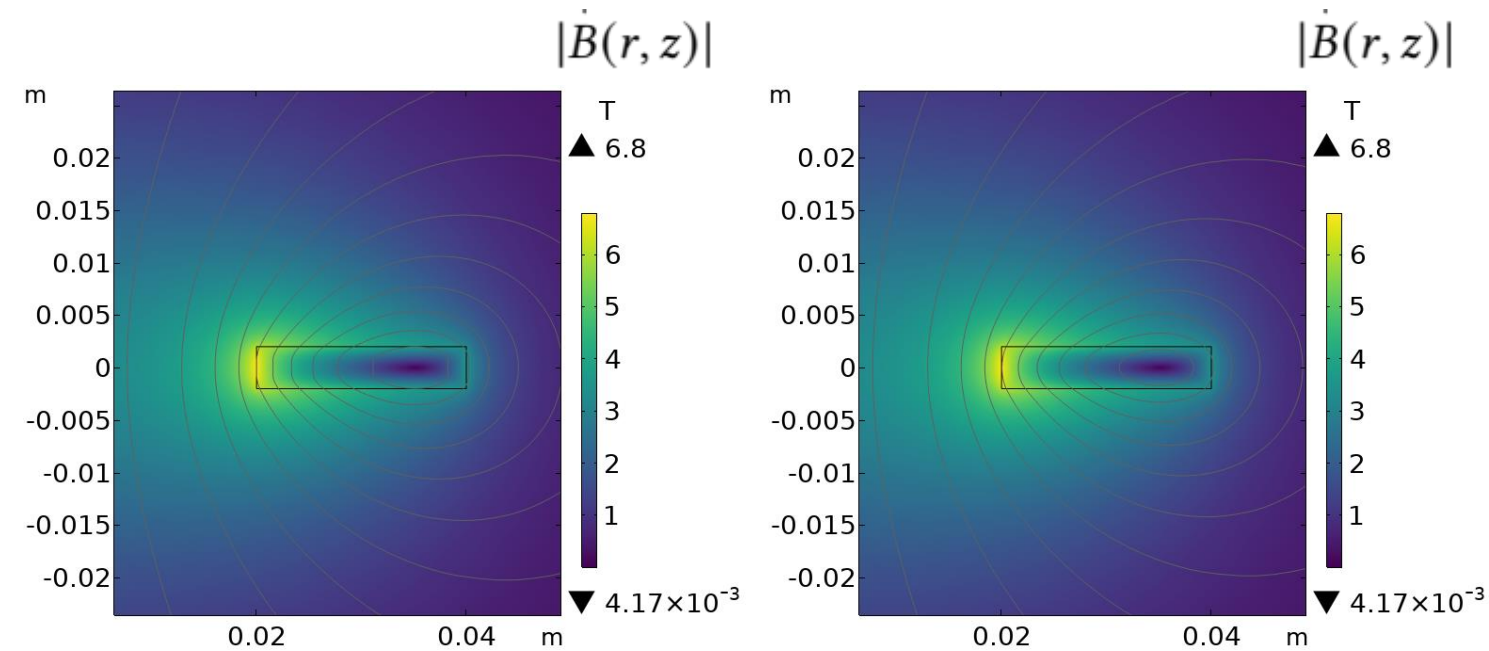
Voltage-current characteristic



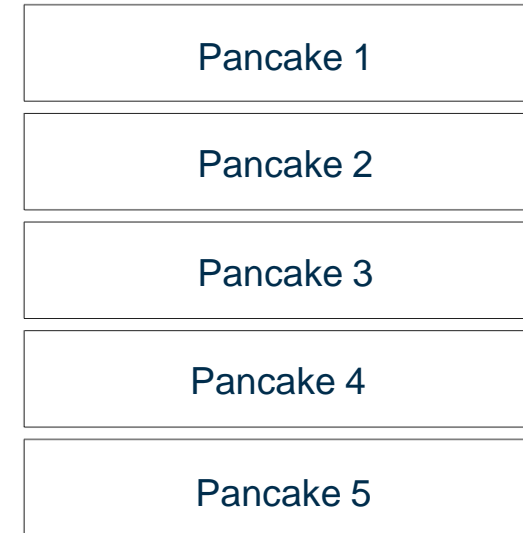
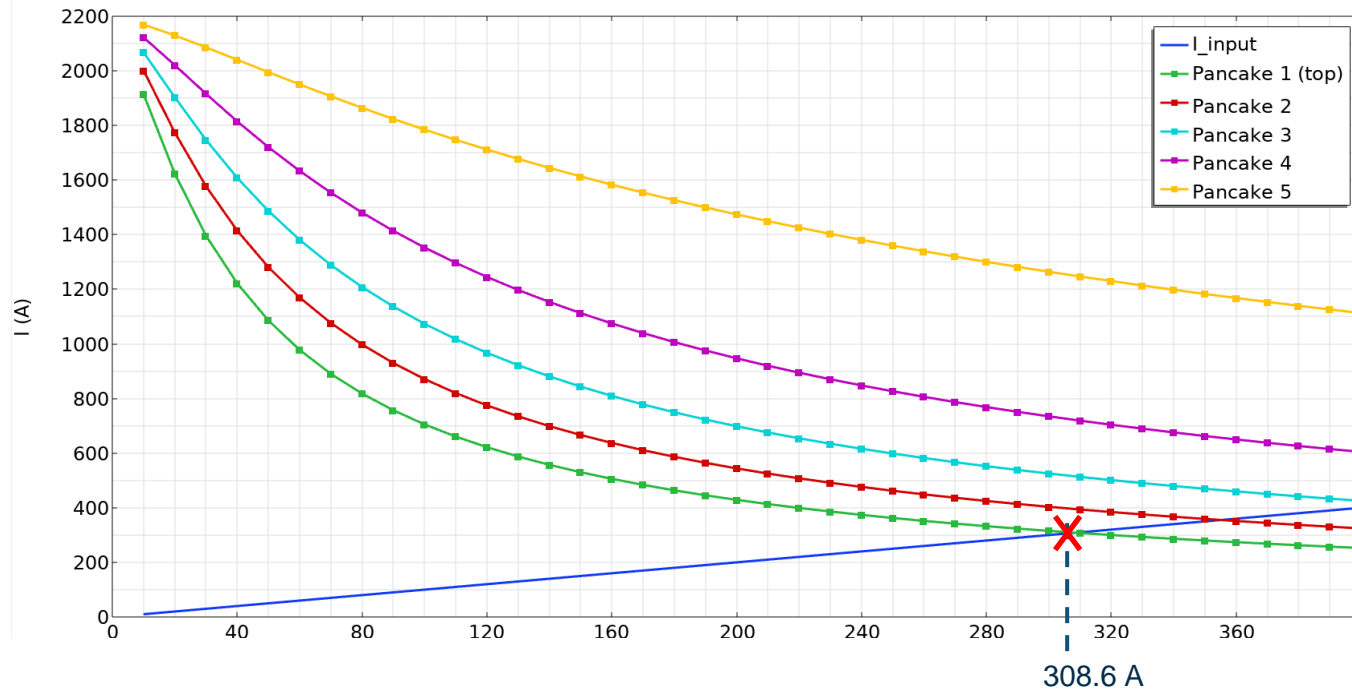
Magnetic field distribution in/around a single pancake coil

T-A formulation

Uniform current distr.



Maximum input current for multiple pancake coils

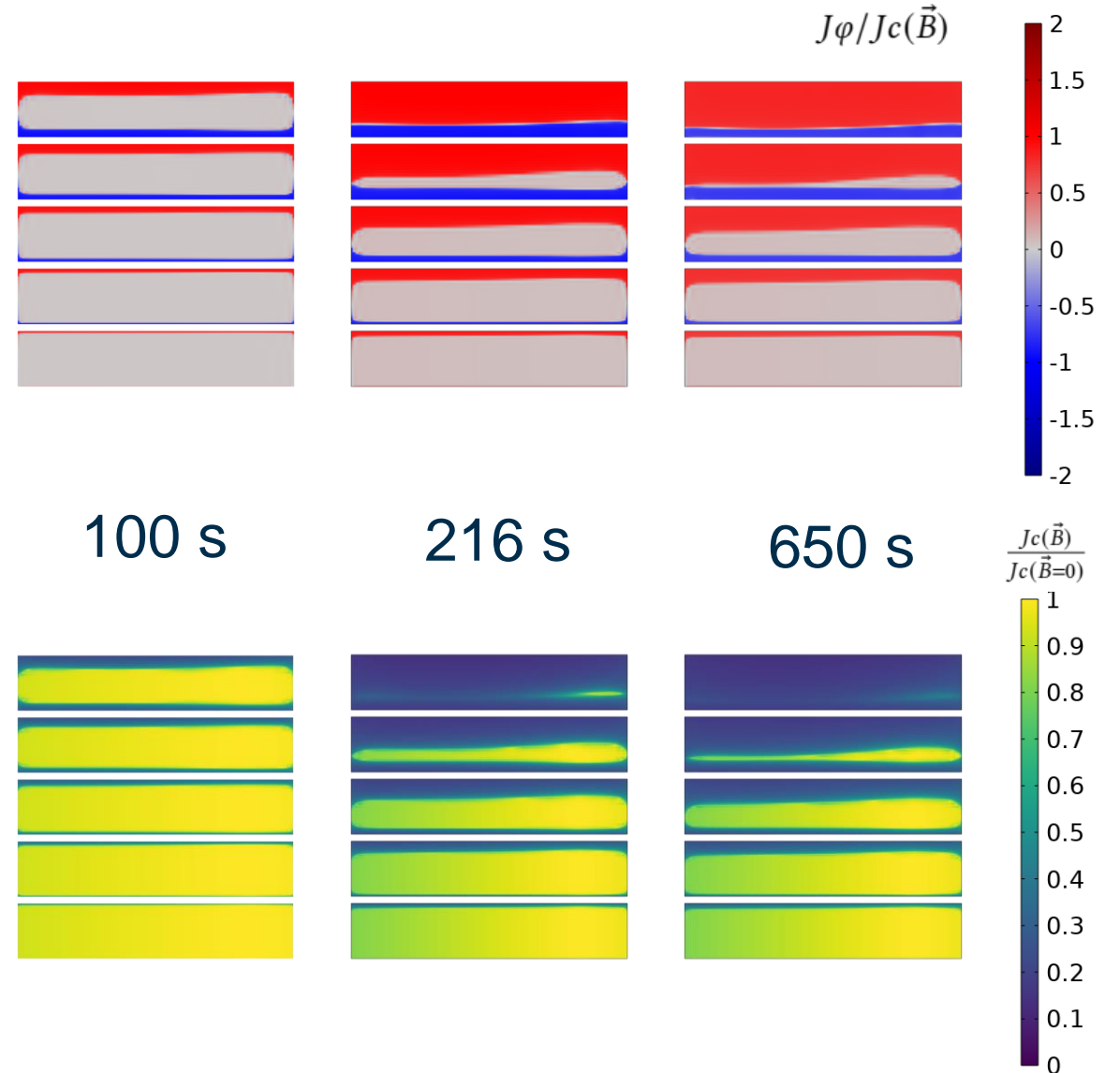
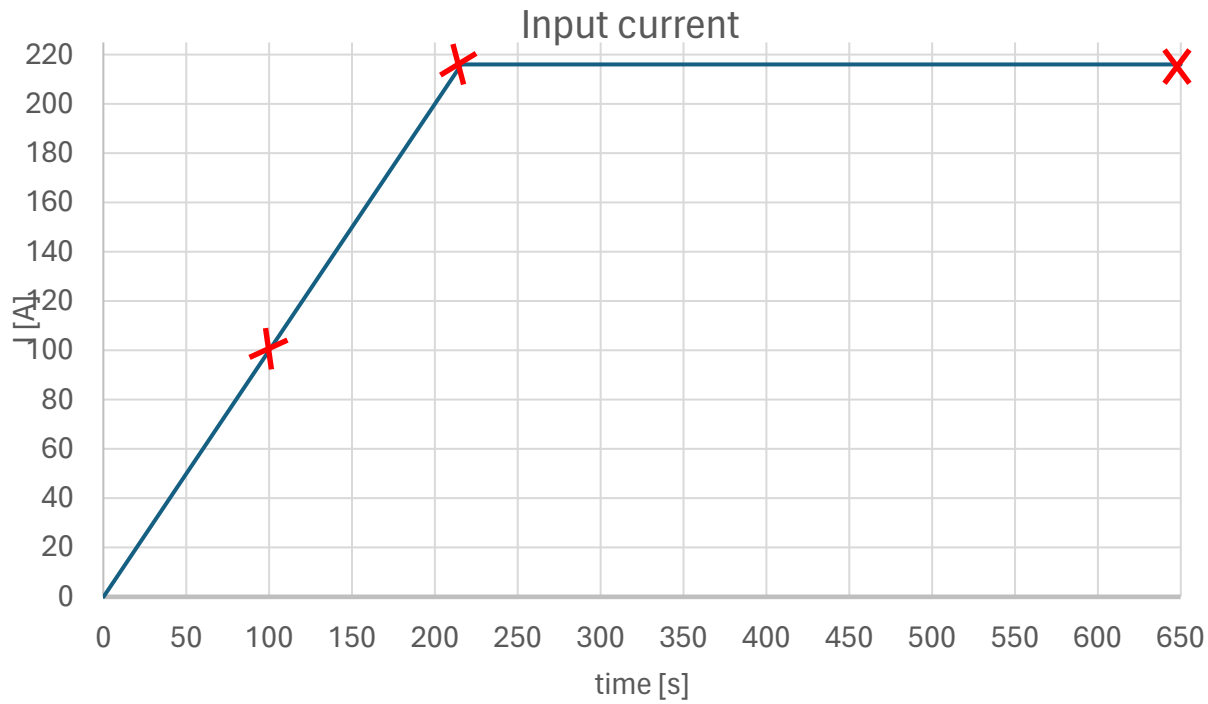


The minimum value at which the critical current curves intersect the applied current curve is 308.6 A

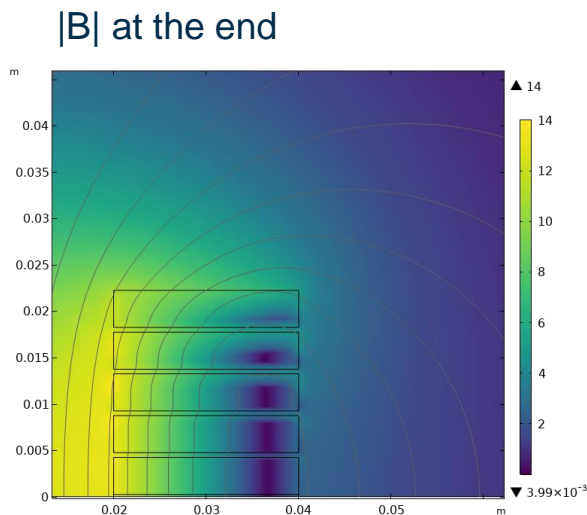
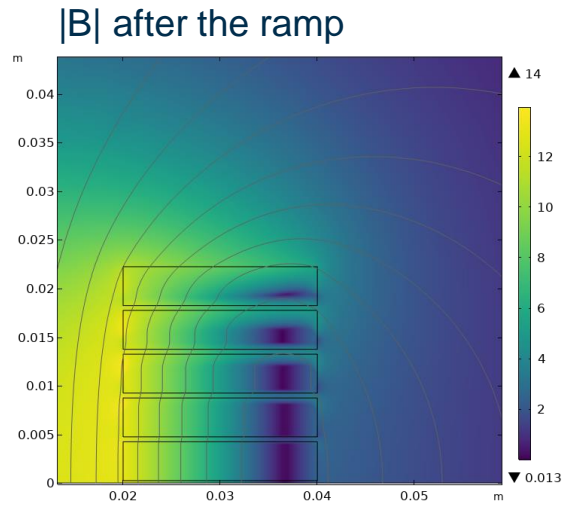
□ From this method we find a maximum input current, $I_{max} = 308.6$ A

□ The next analysis will consider a maximum input current of $0.7 \cdot I_{max} \rightarrow I_{op} = 216$ A

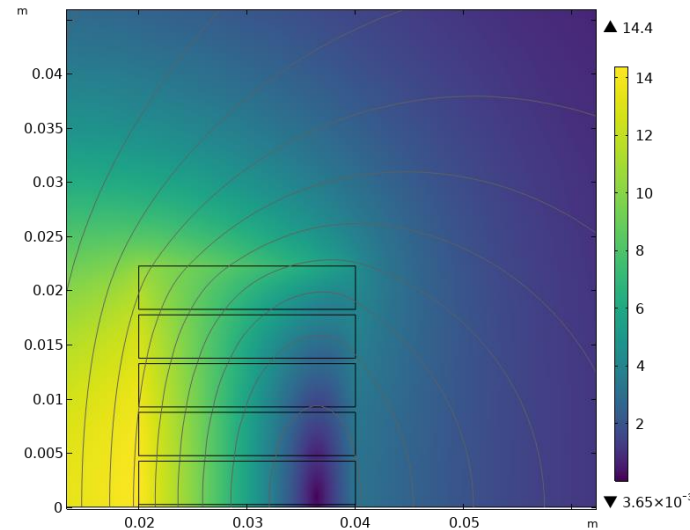
Magnetic field distribution in/around multiple pancake coils



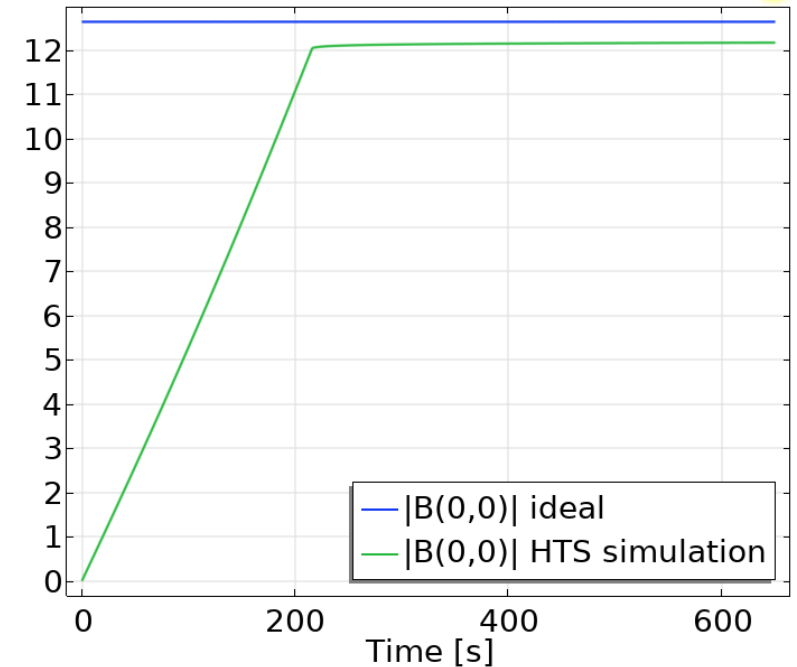
Magnetic field distribution: comparison between T-A formulation and uniform J distribution



$|B|$ with uniform current density distribution (ideal)

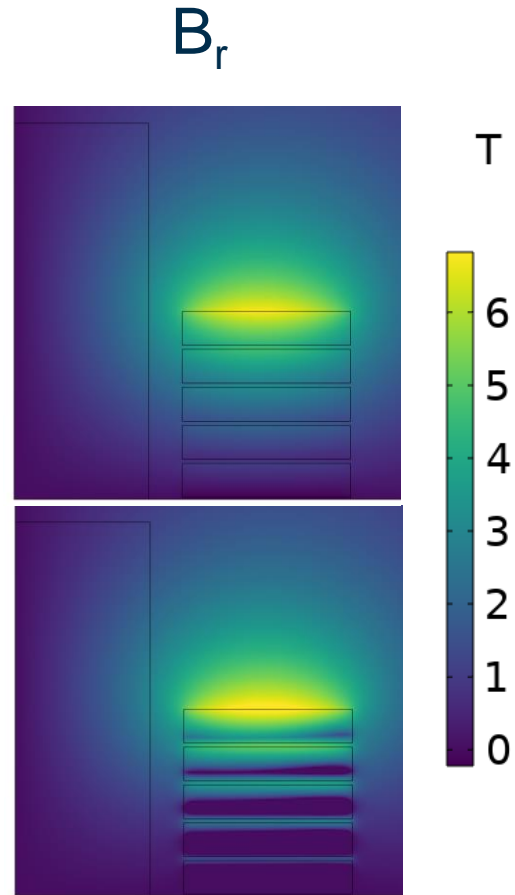


$|B(0,0)|$ [T]

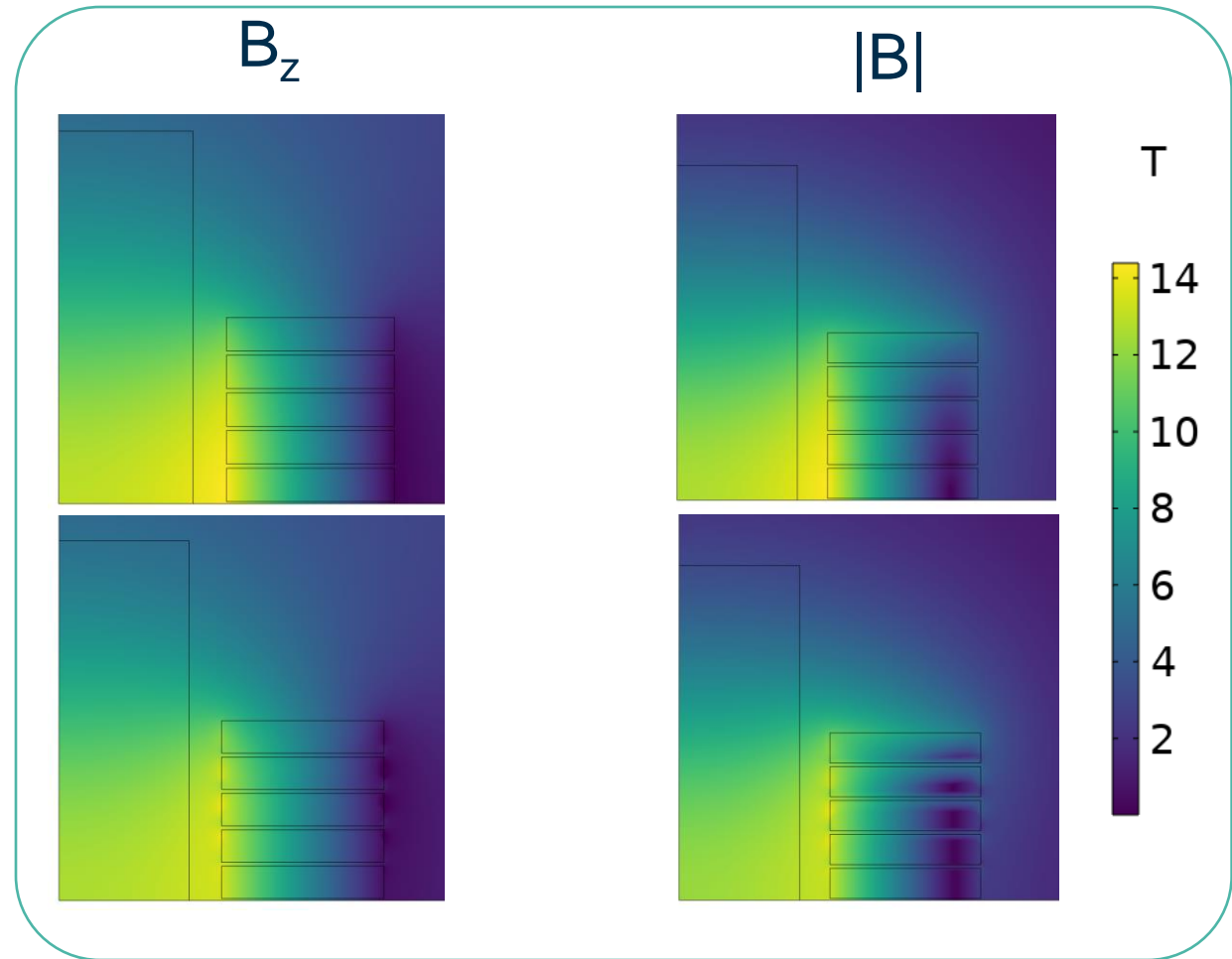


Magnetic field distribution: comparison between T-A formulation and uniform J distribution

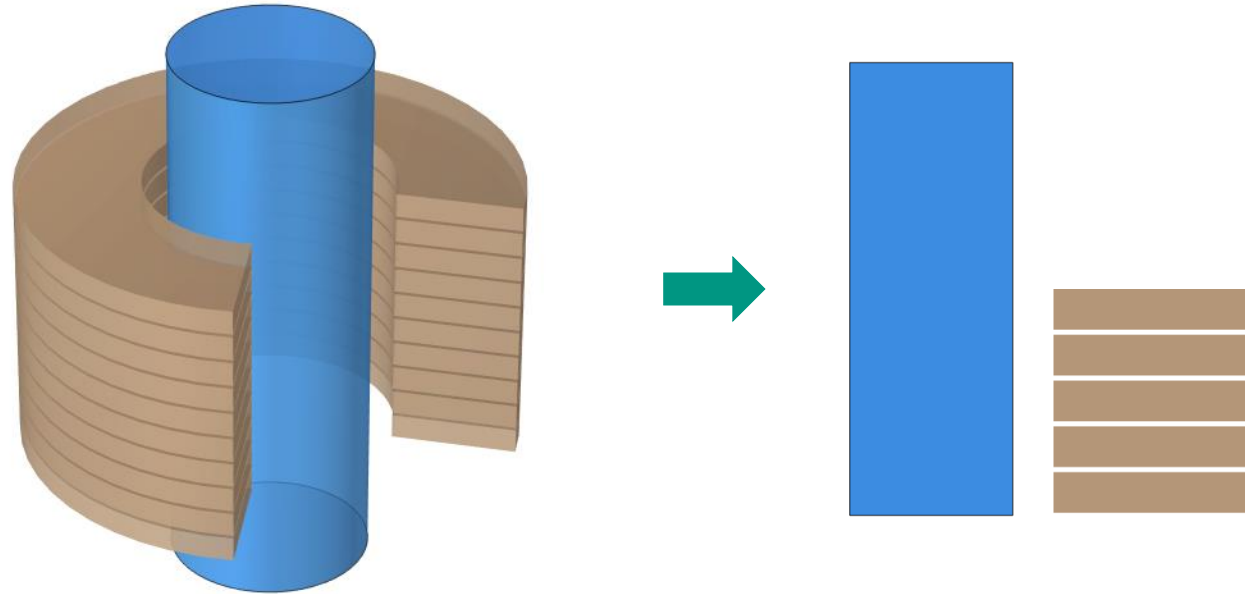
Uniform current distr.



T-A formulation



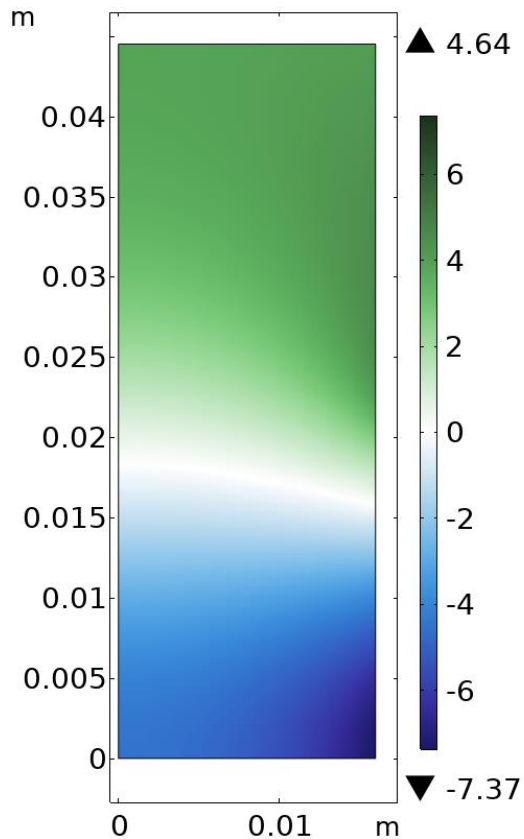
Quantification of the difference with respect to results obtained with uniform J distribution



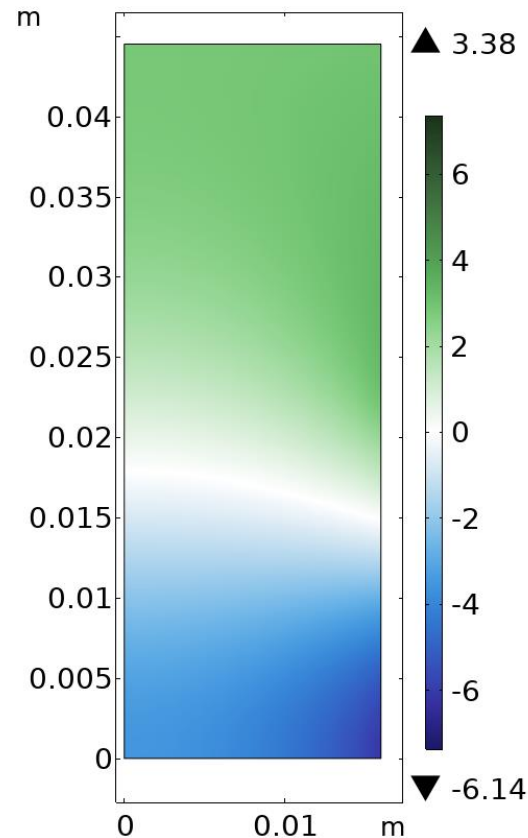
Magnetic field evaluated in a cylindrical volume extending outside the coil

Quantification of the difference with respect to results obtained with uniform J distribution

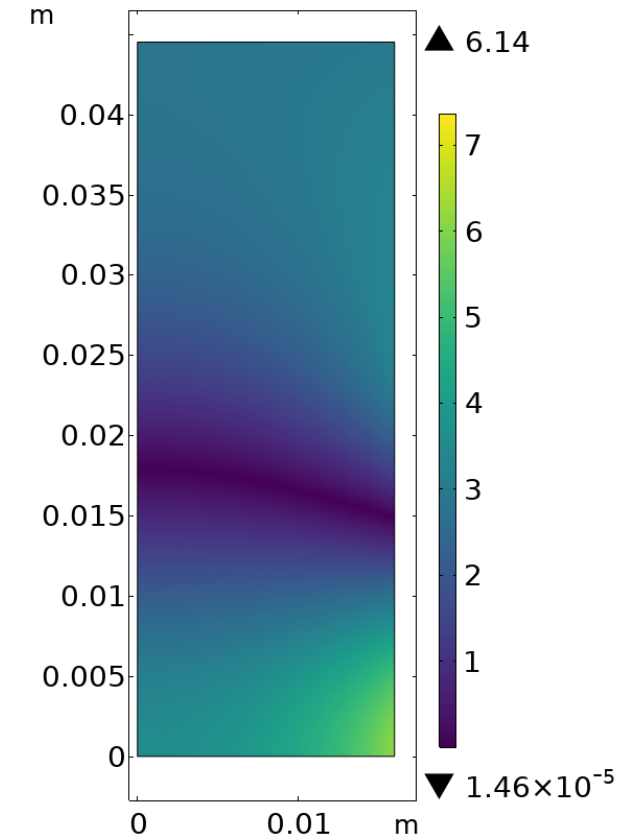
$\Delta|B|/Bid$ [%] after the ramp



$\Delta|B|/Bid$ [%] at the end



$|\Delta|B||/Bid$ [%] at the end



Slight decrease of the error after relaxation

Absolute value of error

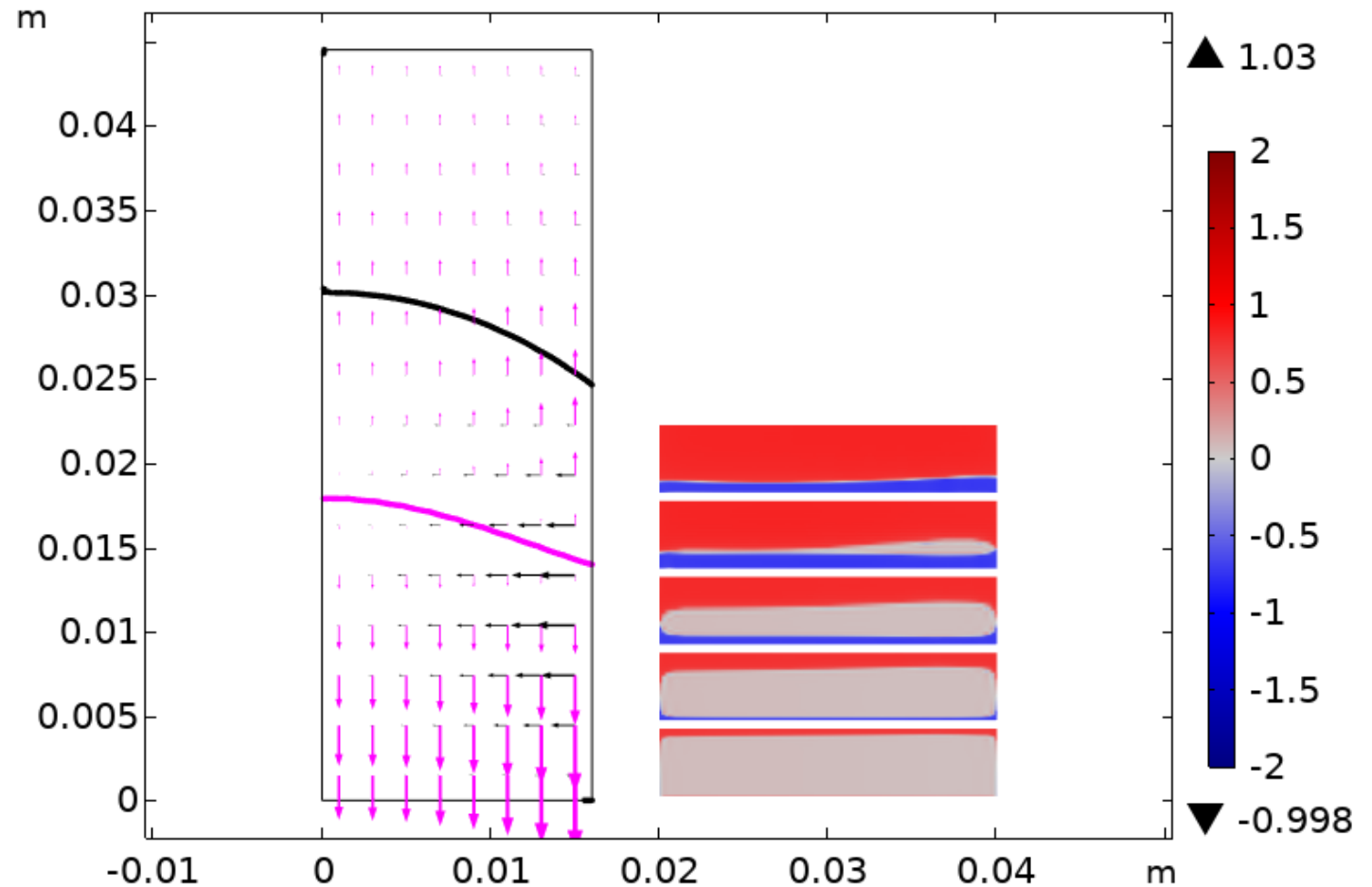
Quantification of the difference with respect to results obtained with uniform J distribution

R-direction arrows: $B_r_{HTS}-B_r_{unif}$

Z-direction arrows: $B_z_{HTS}-B_z_{unif}$

Black isoline: $B_r_{HTS}-B_r_{unif}=0$

Magenta isoline: $B_z_{HTS}-B_z_{unif}=0$



Field Quality optimization

Increasing the input current

Effect of input current on field quality
(with respect to field obtained with
corresponding uniform current
distribution)

1. $0.5 \times I_c = 154\text{A}$

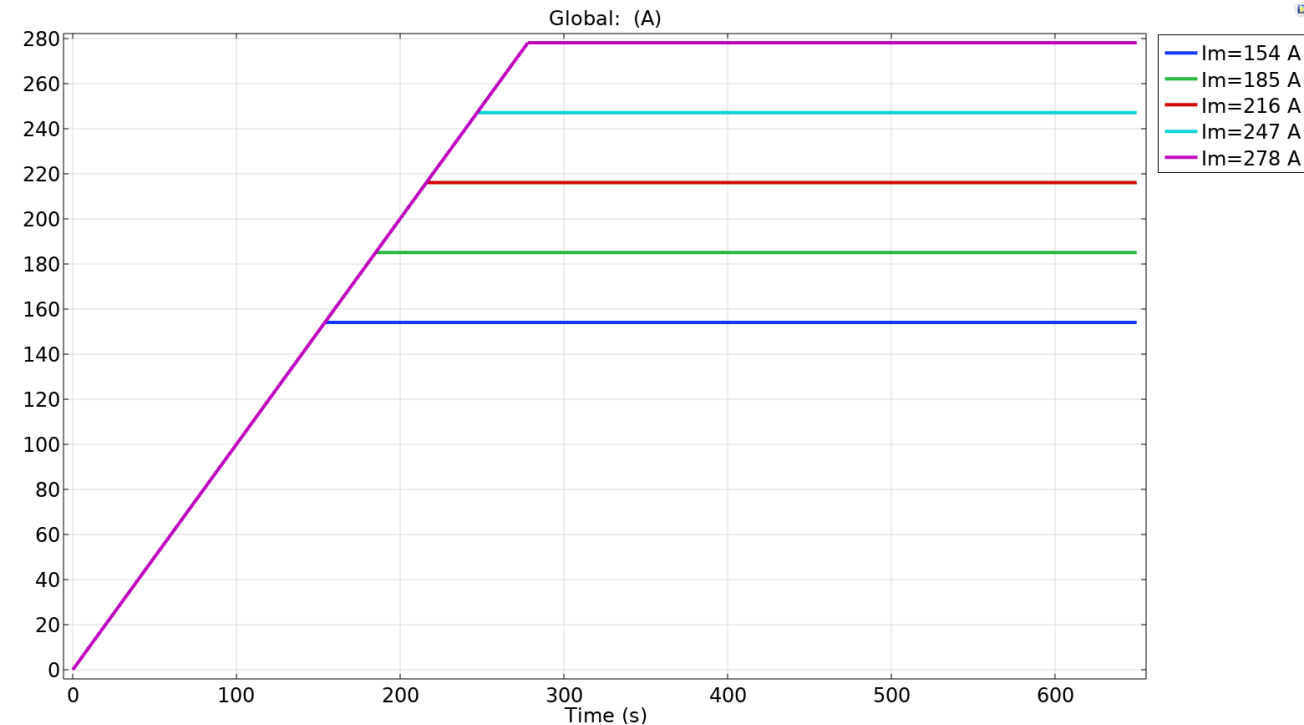
2. $0.6 \times I_c = 185\text{ A}$

3. $0.7 \times I_c = 216\text{ A}$

4. $0.8 \times I_c = 247\text{ A}$

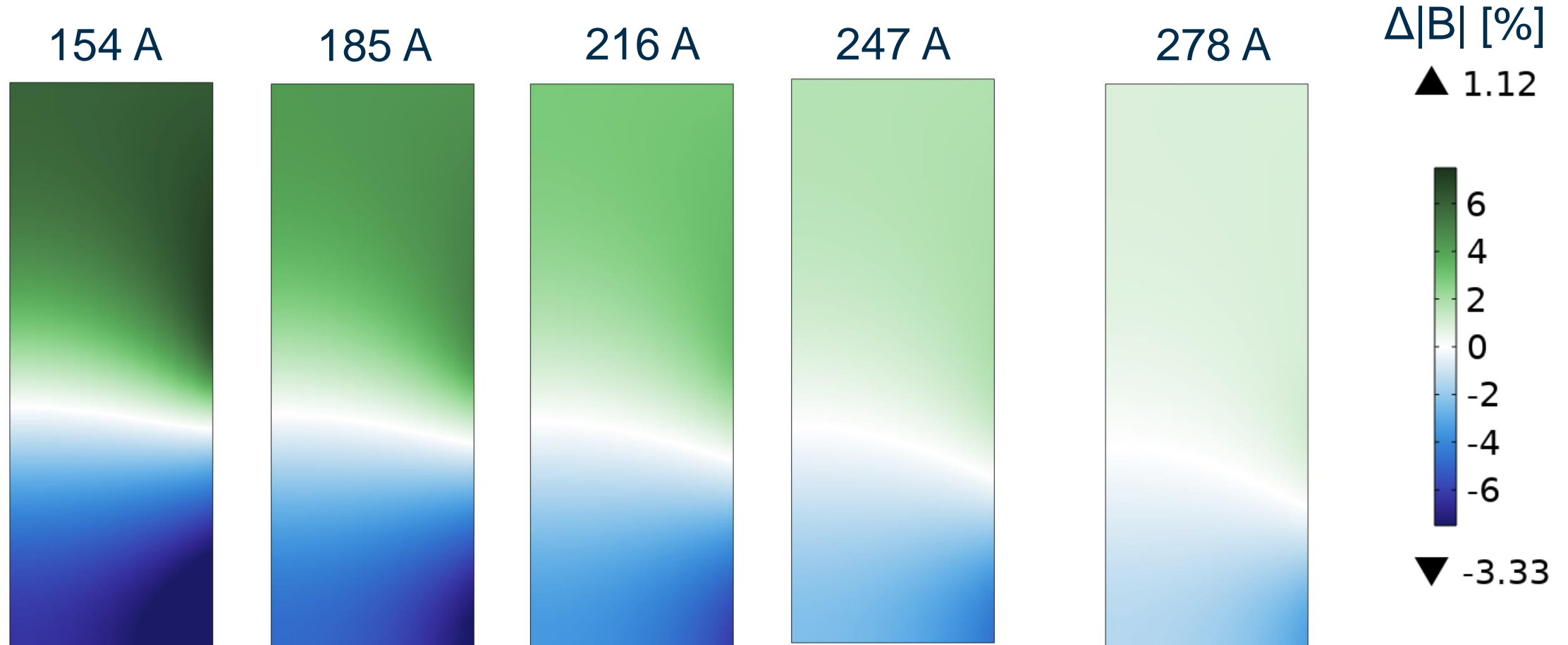
5. $0.9 \times I_c = 278\text{ A}$

All simulations run with a ramp of 1 A/s



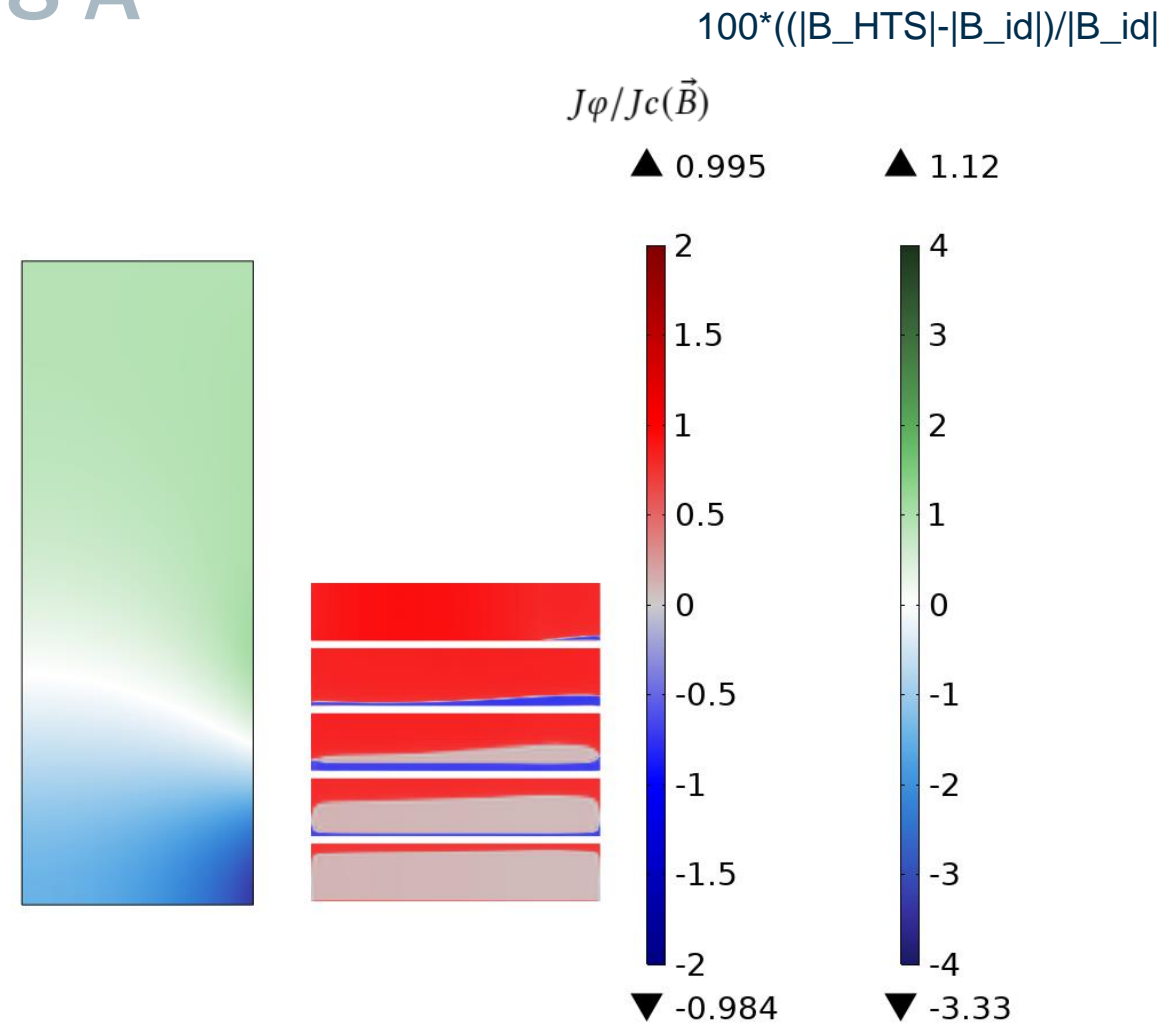
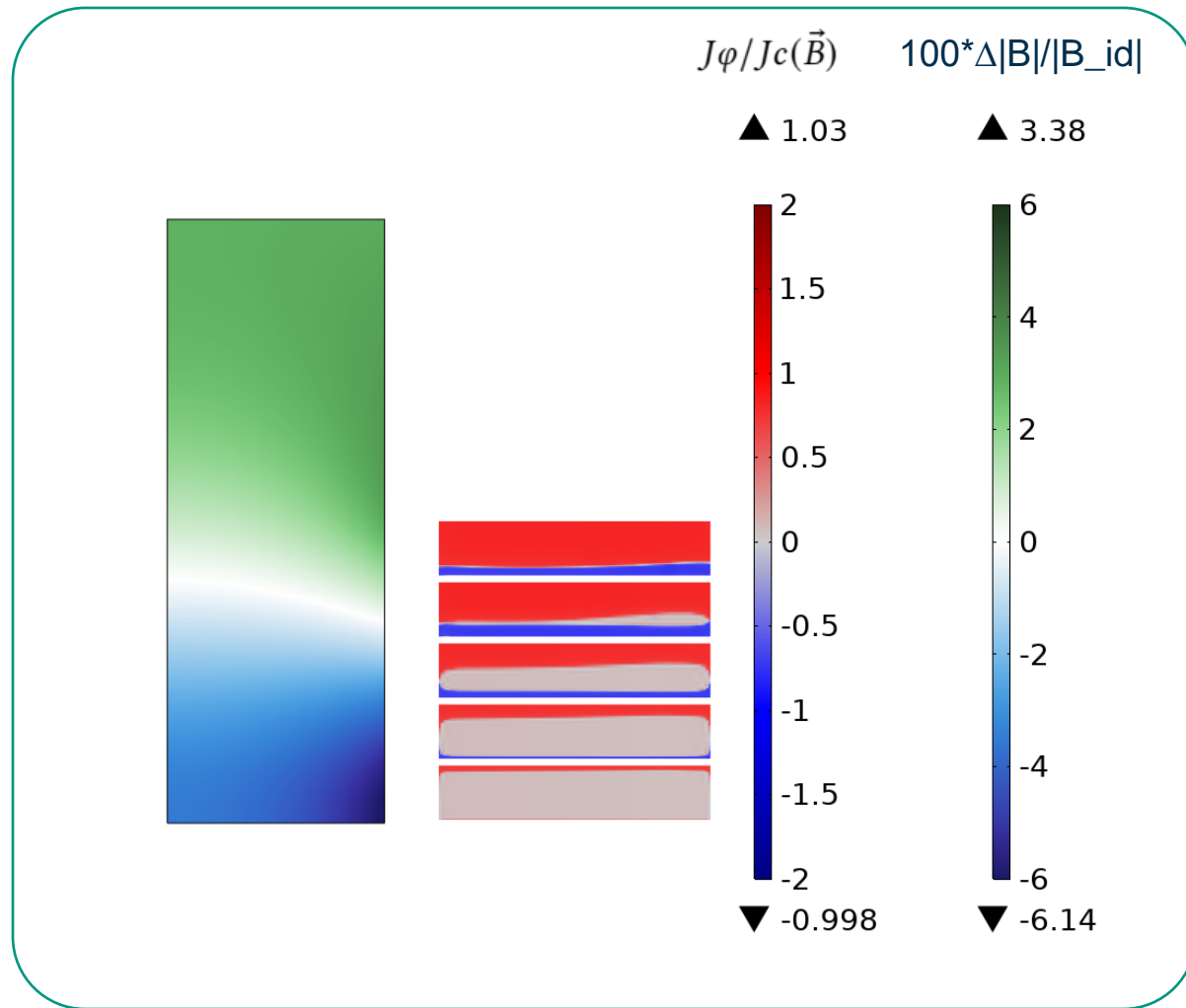
Effect of increasing input current

From $I_m=154$ A to $I_m=278$ A

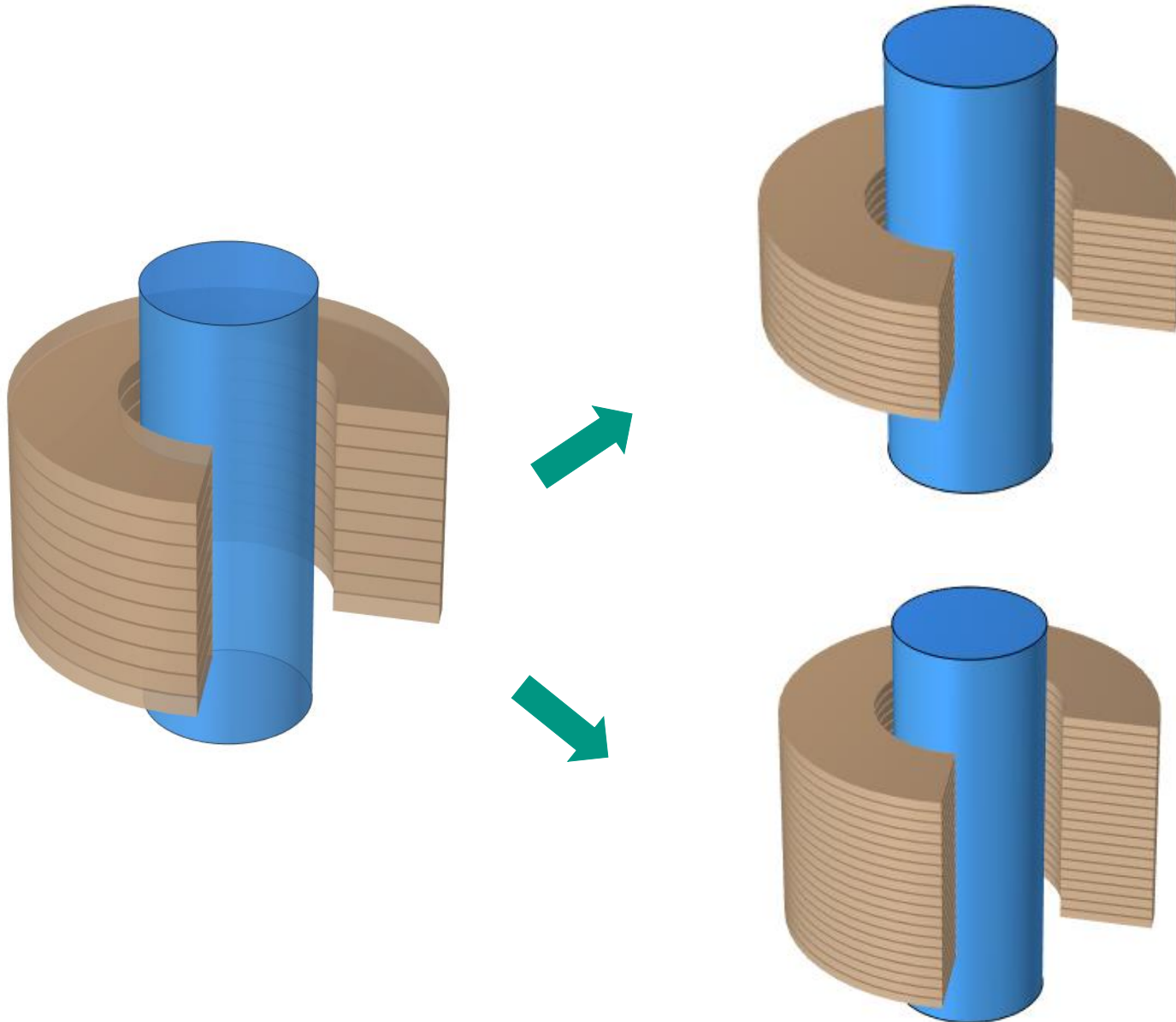


Effect of increasing input current

Comparison: $I_m=216$ A vs $I_m=278$ A



Effect of using narrower tapes



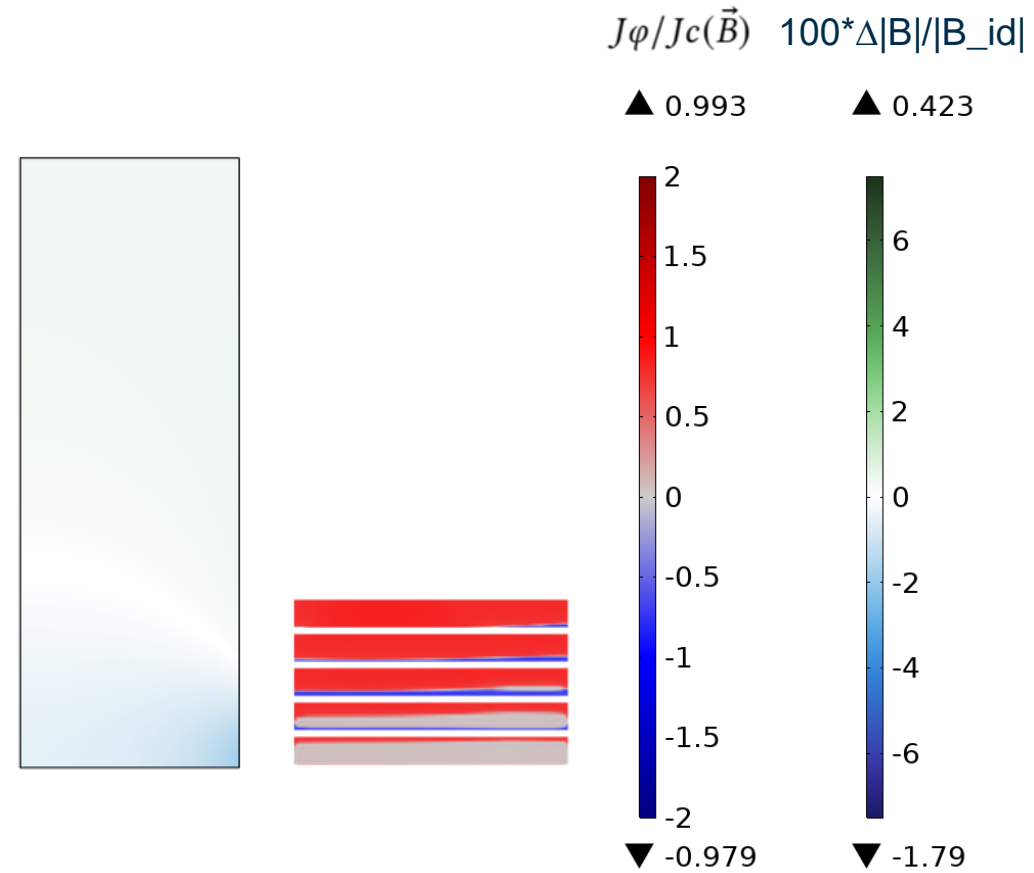
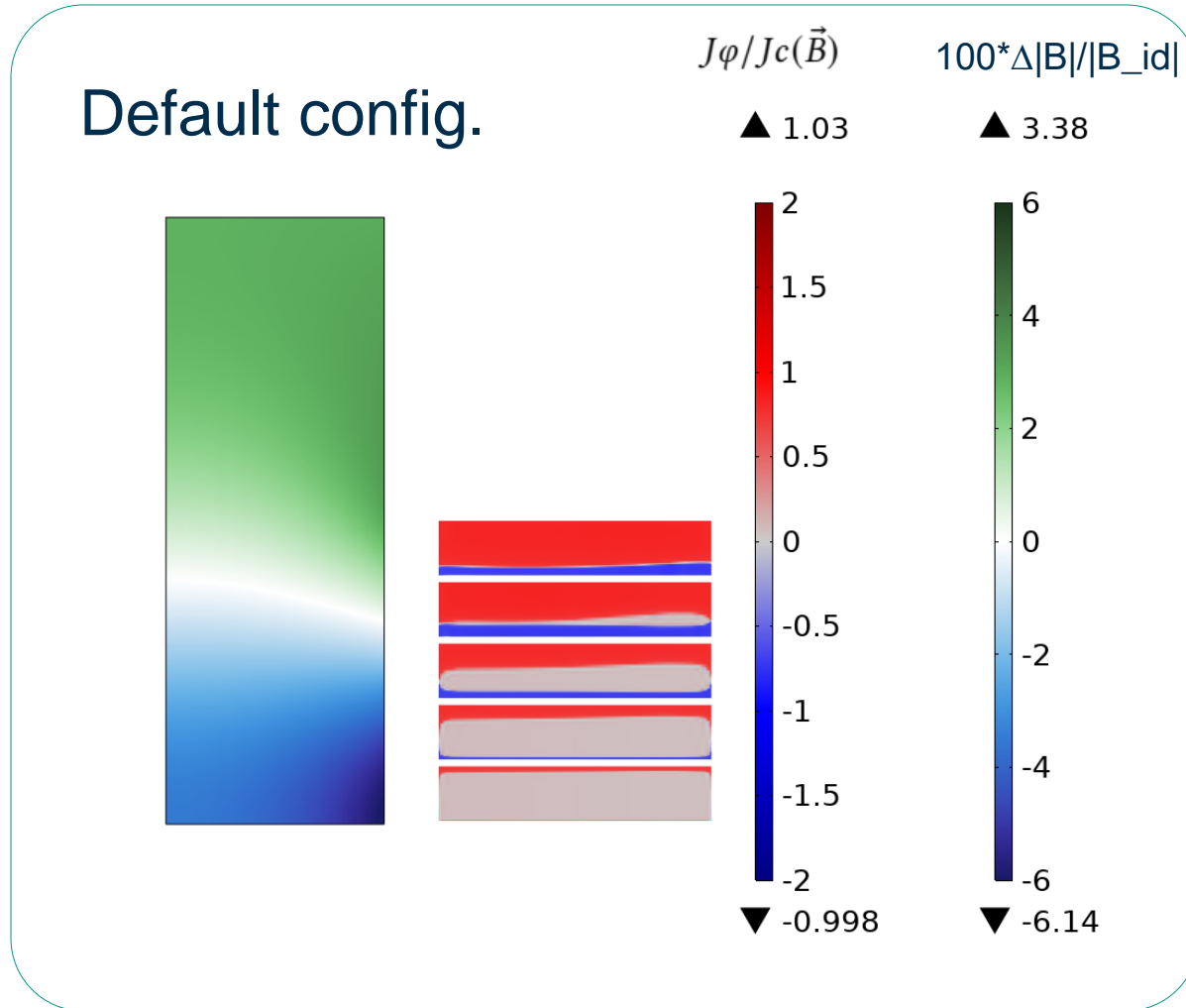
Case 1

10 Pancakes half tape width
Same input current
Double J_c (realistic?)

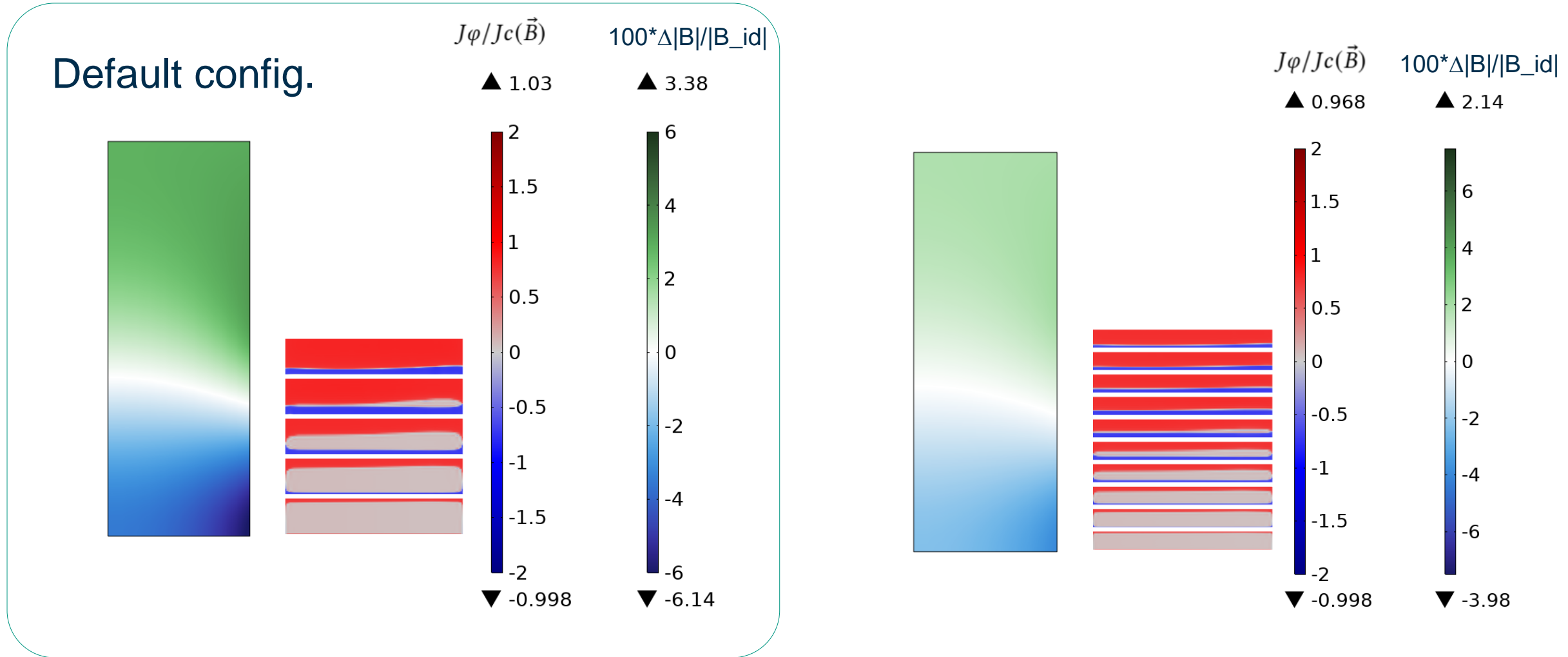
Case 2

20 Pancakes half tape width
Half input current
Same J_c

Effect of using narrower tapes: case 1

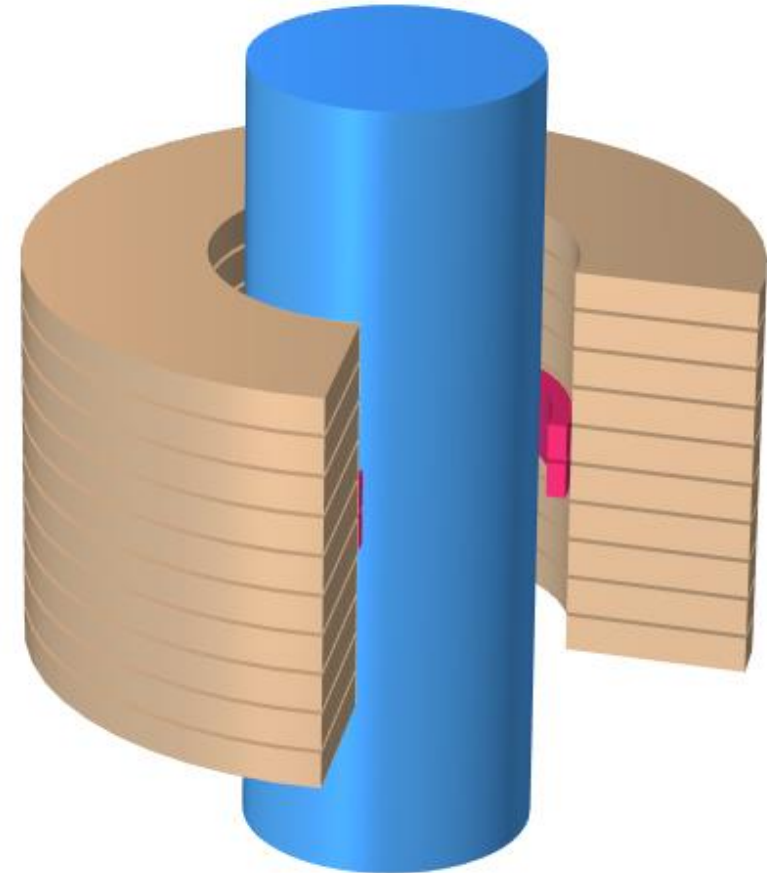


Effect of using narrower tapes: case 2

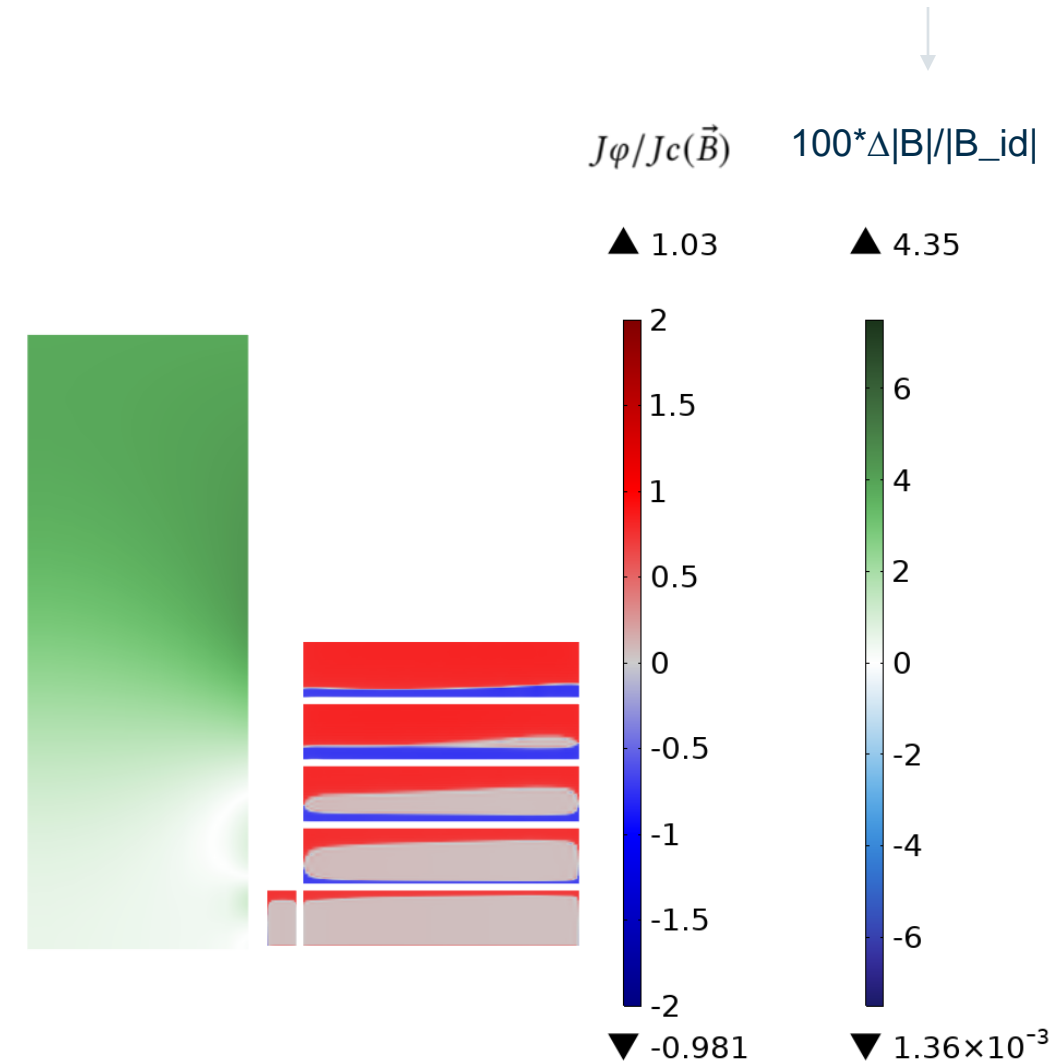
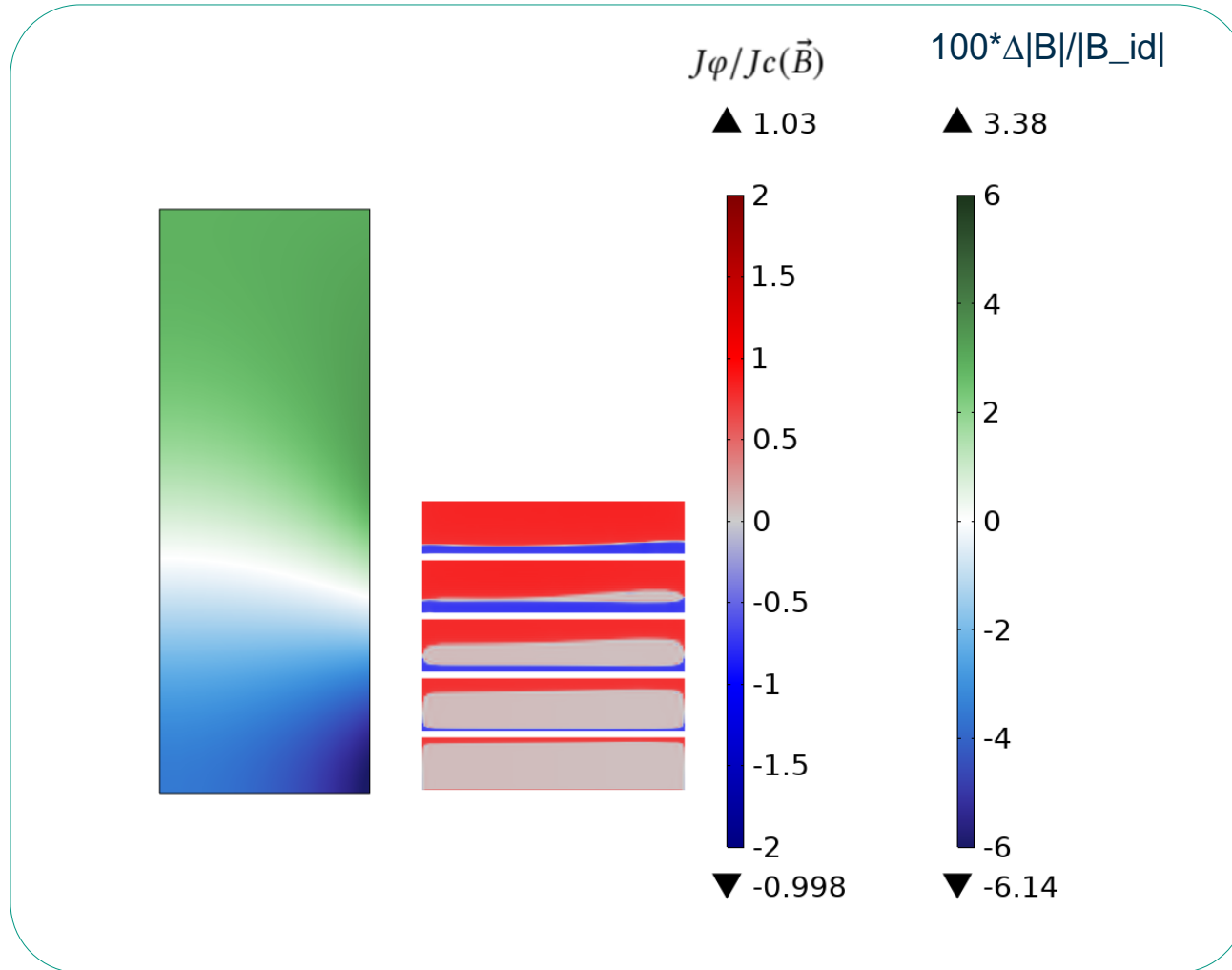


Can we reduce the error with additional coils?

- ❑ Double pancake coil to compensate the field distortion caused by screening currents
- ❑ Field correction of 0.5 T in (0,0)
- ❑ Series connection → 37 turns in each additional pancake coil



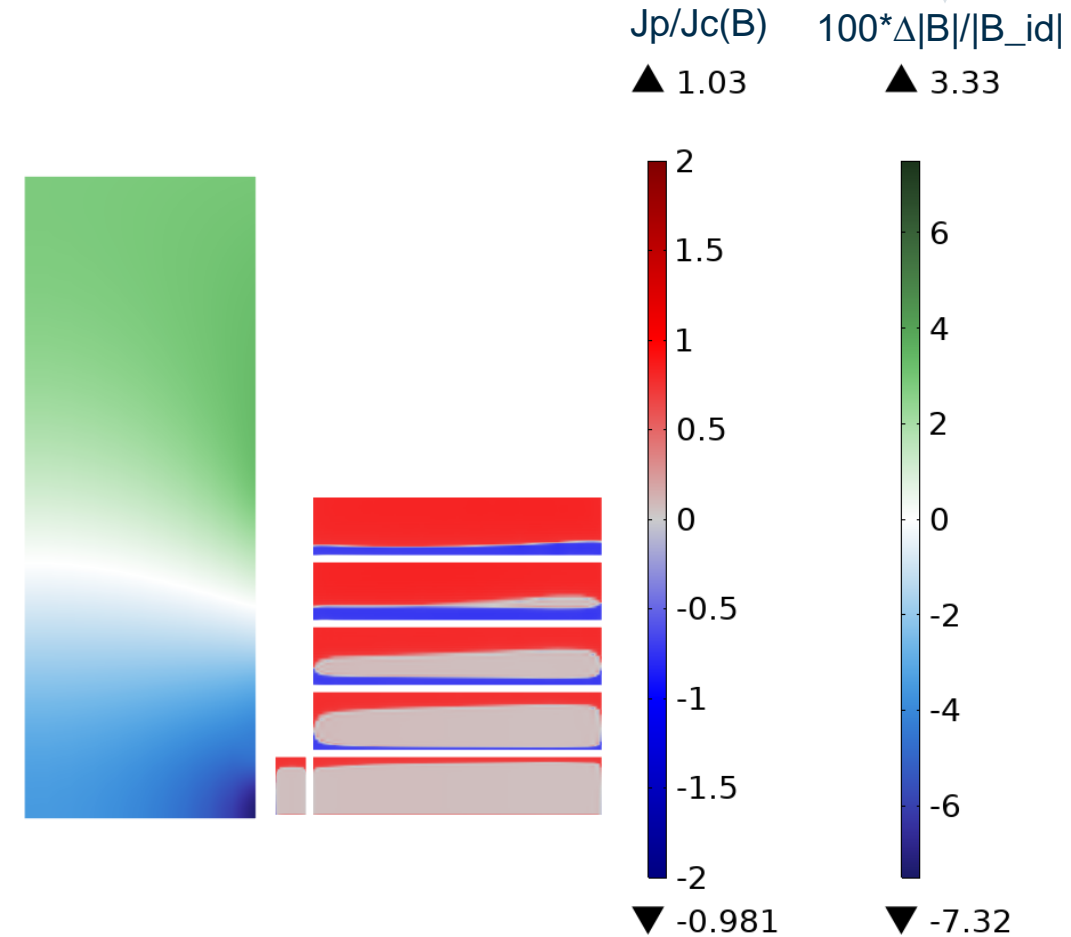
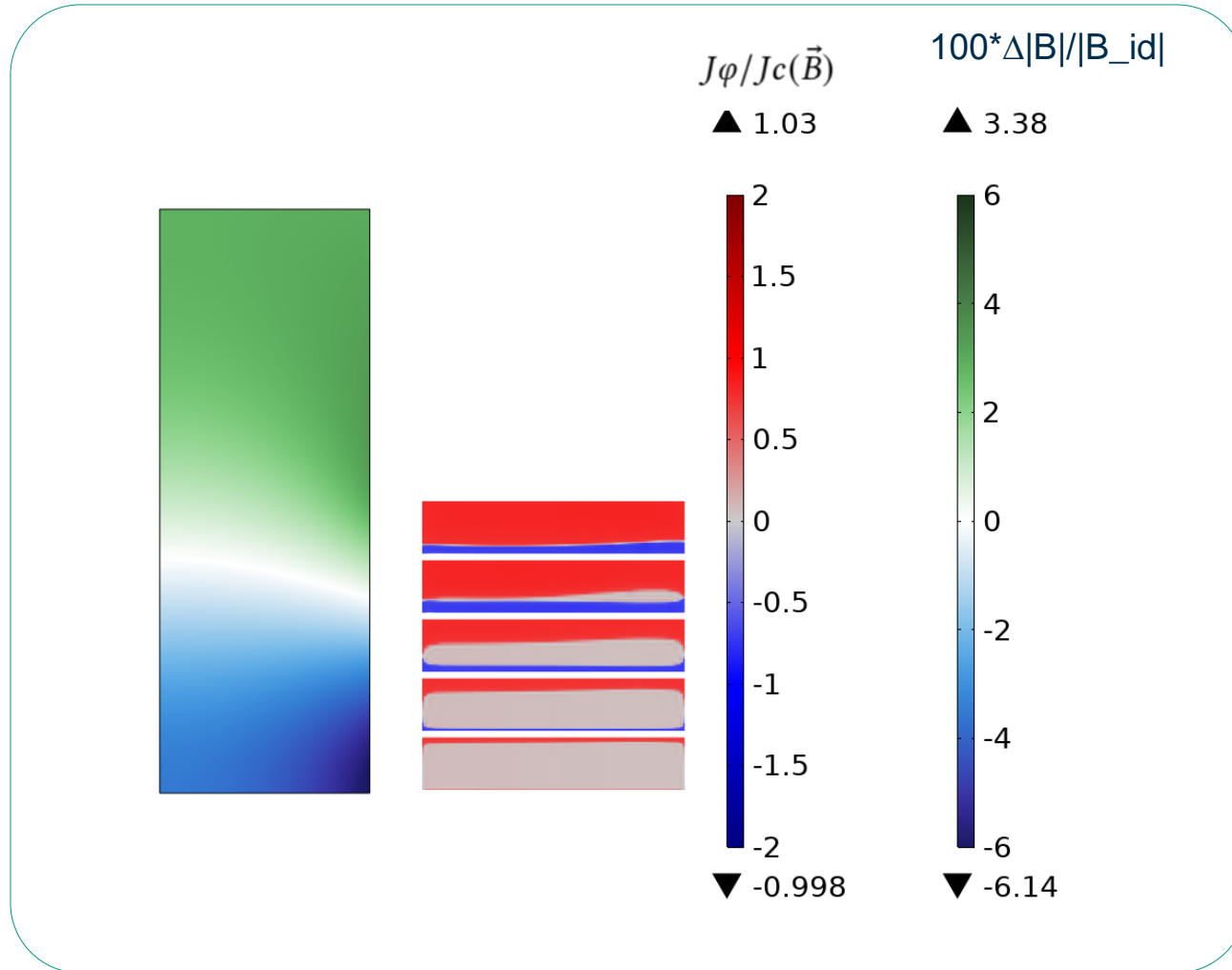
Effect of additional pancake coils



Error evaluated against result with uniform current distr. for default configuration (without extra pancake)

Effect of additional pancake coils

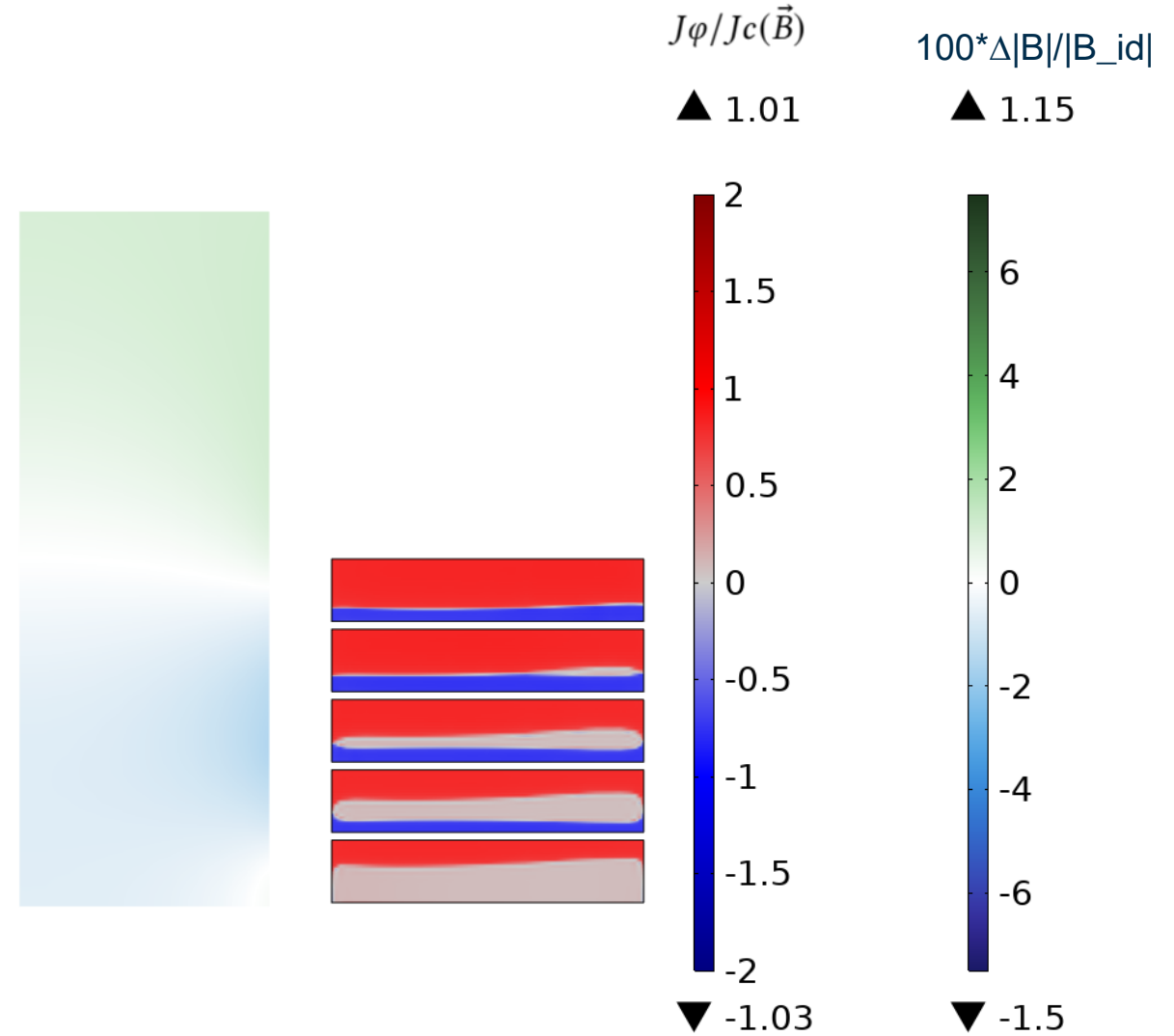
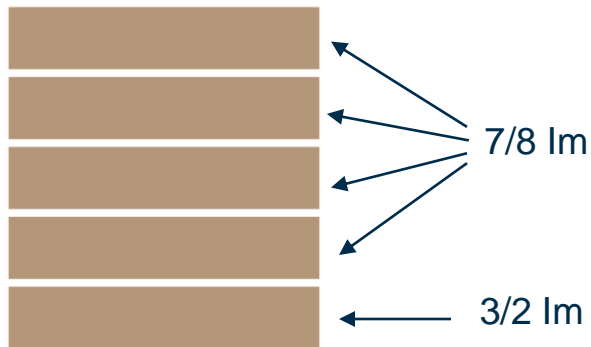
B_id including double pancake



When compared against result with uniform current distr. for the analyzed configuration (with extra pancake), error increases

Alternative: increasing the current of the internal pancakes

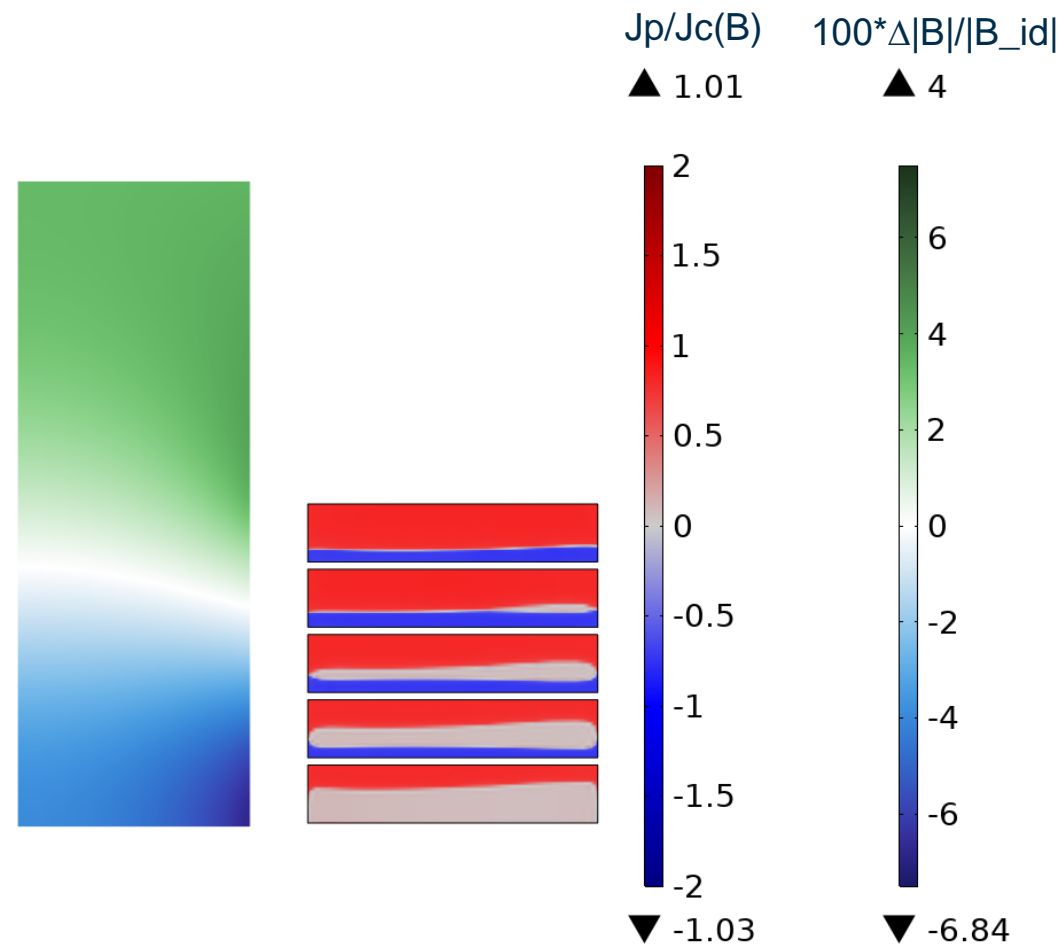
- ❑ Current in central pancake increased by 50 %
- ❑ Current in other pancakes reduced accordingly



Error evaluated against result with uniform current distr. for default configuration (same current in each pancake)

Alternative: increasing the current of the internal pancakes

▪ B_id with same input current



Again, when compared against result with uniform current distr. for the analyzed configuration (more current in central pancakes), error increases

Summary

- ❑ **Homogenized T-A formulation: efficient tool to evaluate influence of screening currents on magnetic field**
- ❑ **Field distributions compared with those obtained with model based on uniform current distribution for different magnet configurations**
- ❑ **Same approach can be used to study field uniformity in a region of interest**

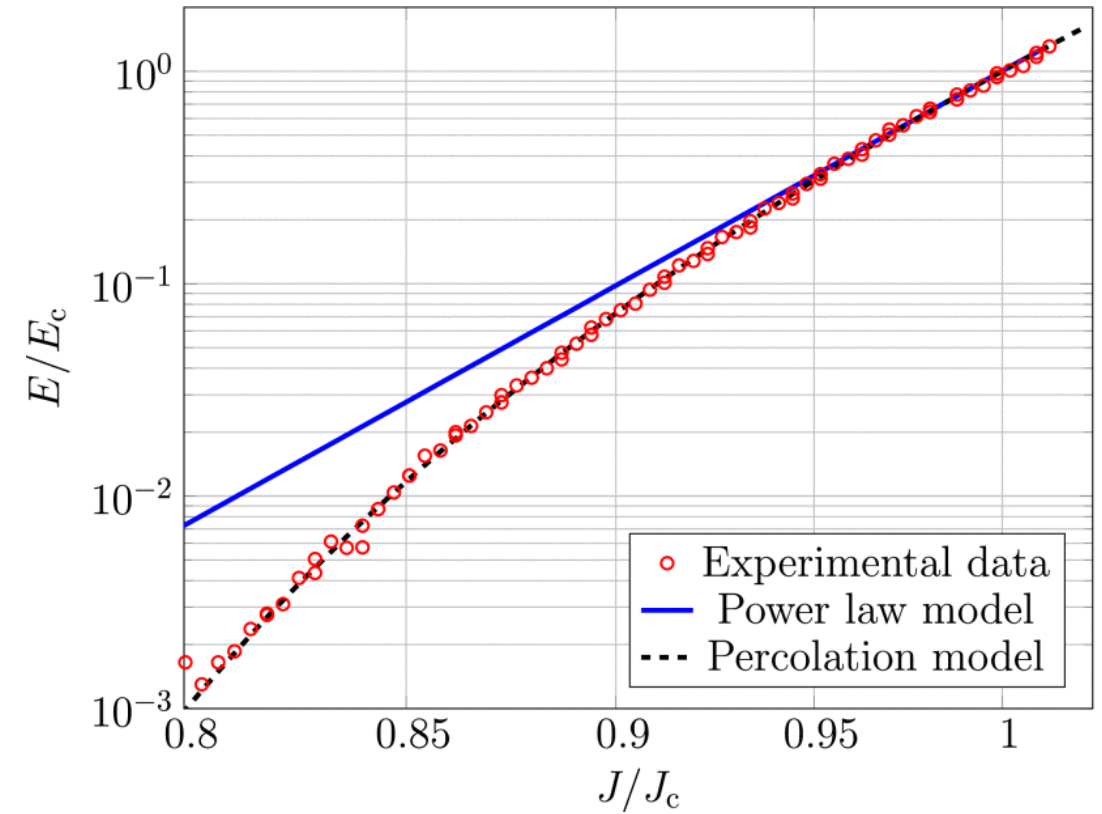
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Beyond the E - J power-law



Beyond the E - J power-law

Power law near E_c

$$E = E_c \left(\frac{J}{J_c} \right)^n$$

Different behavior at low electric fields

Important for slow ramps, e.g. magnets

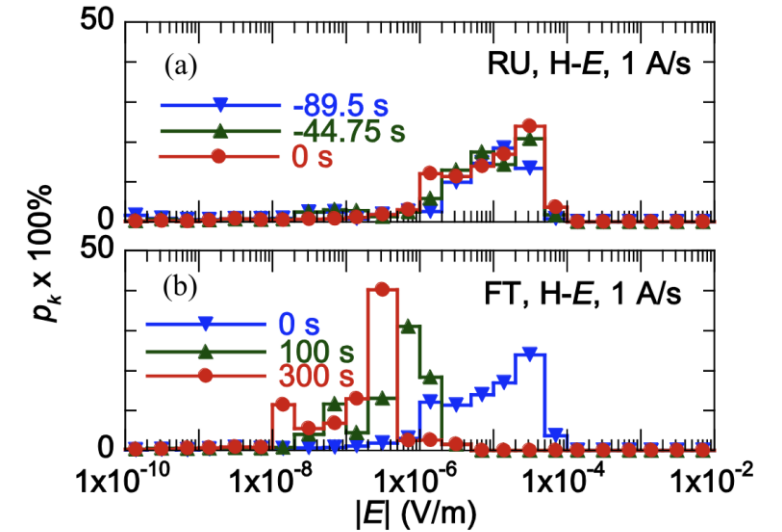
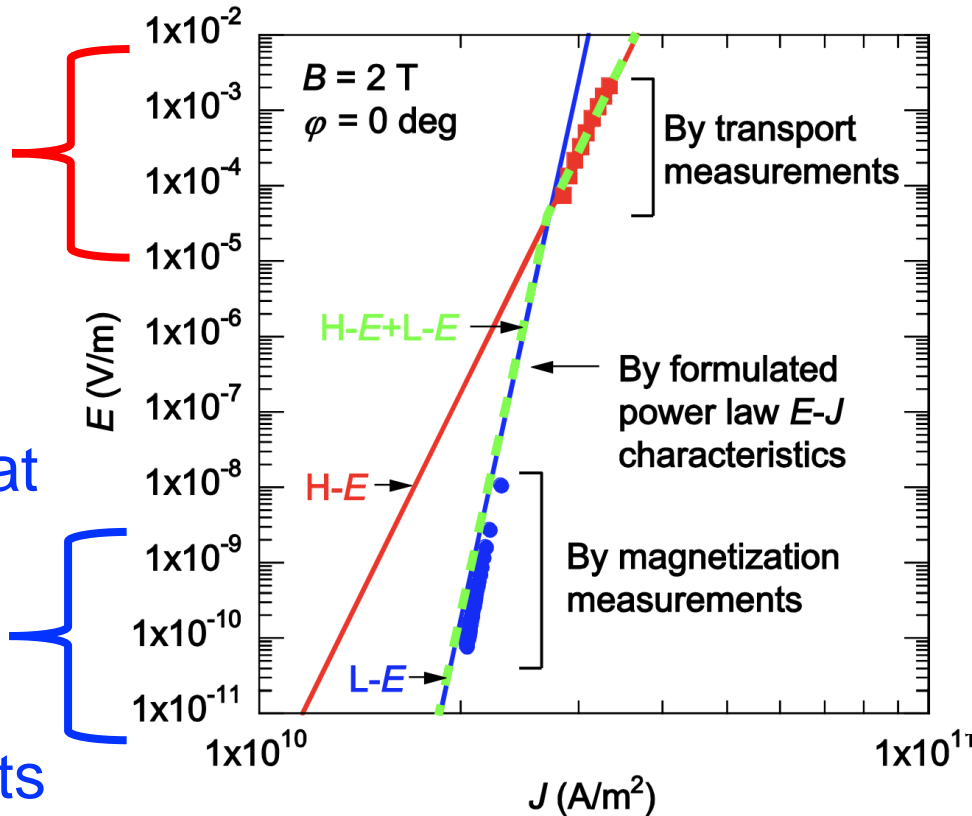


Fig. 5. Temporal evolution of the weighted probability p_k when E - J characteristic is H- E and ramp-up rate is 1 A/s at (a) the ramp up phase and (b) flat top. The ramp up phase begins at -179 s .

Next steps

- 1. Apply this tool to cases of interest**
- 2. Compare with case of NI coils (different model)**
- 3. Extend these tools to 3D (non-planar coils)**

