

# Particle Physics Foundations of Dark Matter, Dark Energy, and Inflation

**ROCKY I: DARK MATTER (WEDNESDAY, 11:00)**

**ROCKY II: DARK ENERGY (THURSDAY, 11:00)**

**ROCKY III: INFLATION (FRIDAY, 11:00)**

# $\Lambda$ CDM: The Standard Model



"How helpful is astronomy's pedantic accuracy, which I used to secretly ridicule!"

*Einstein's to Arnold Sommerfeld on December 9, 1915 (measurements of the perihelion advance of Mercury)*

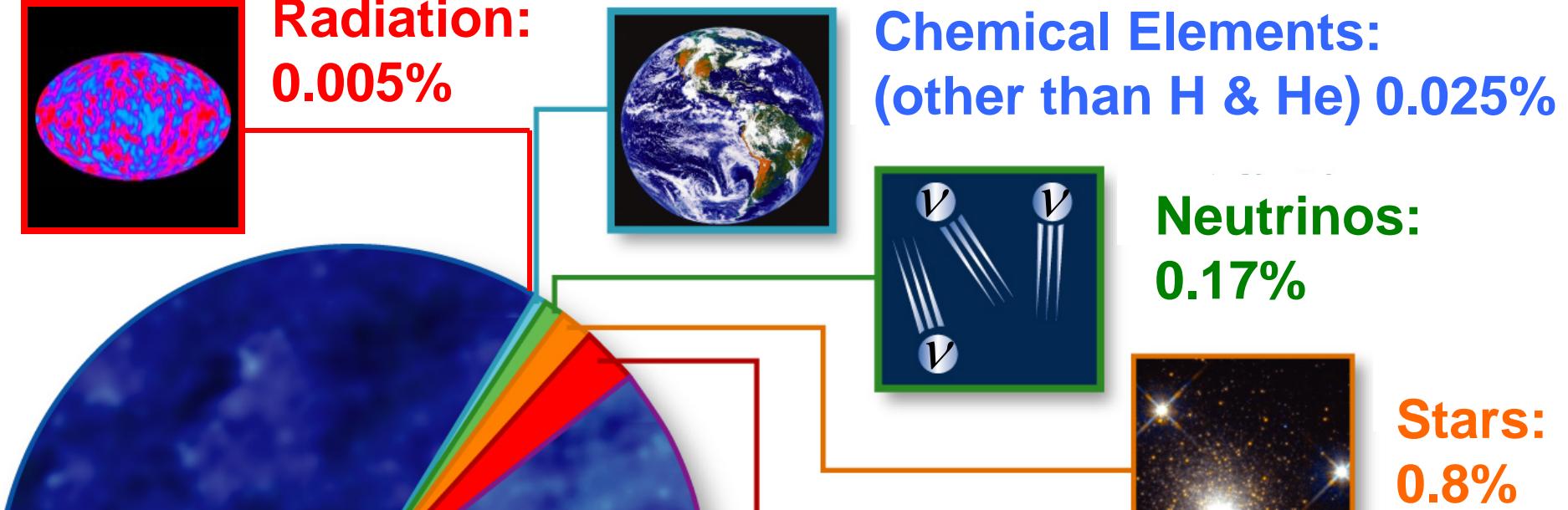


DA

I

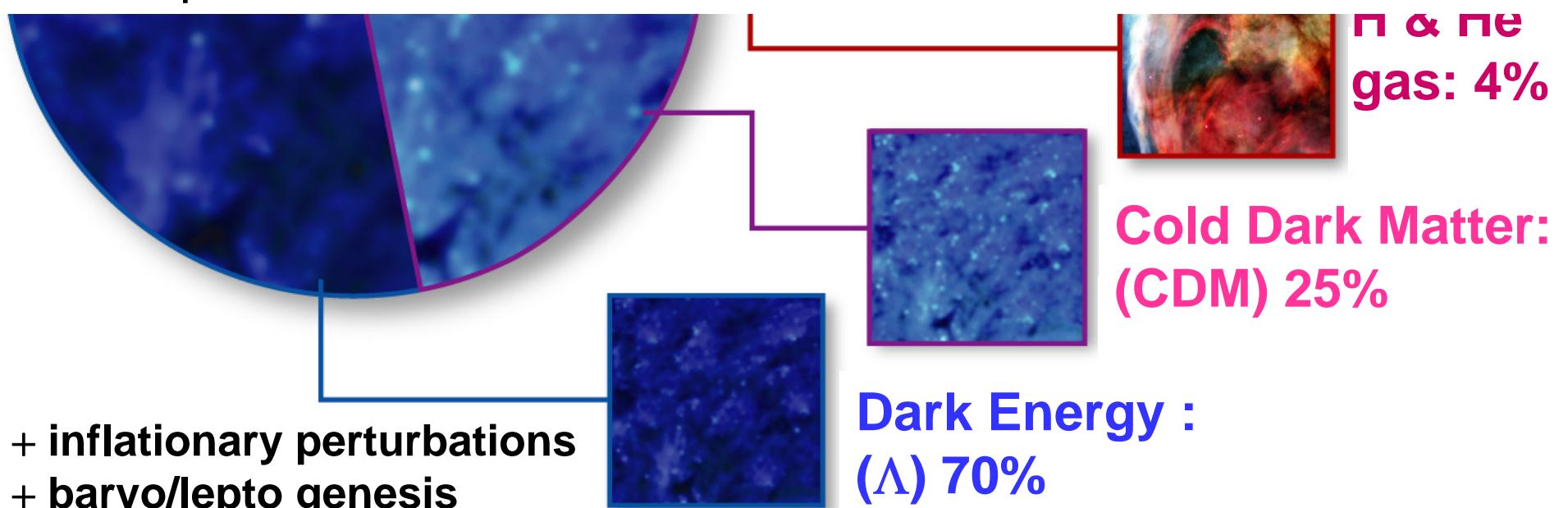
DA

## Beyond Standard Model Physics



If I had been present at creation, I would have suggested a simpler scheme.

- Alfonse the Wise



# Ninety-Five Percent of the Universe

Dark Matter (25%)

Pulls things together

Attractive gravity

New particle species?

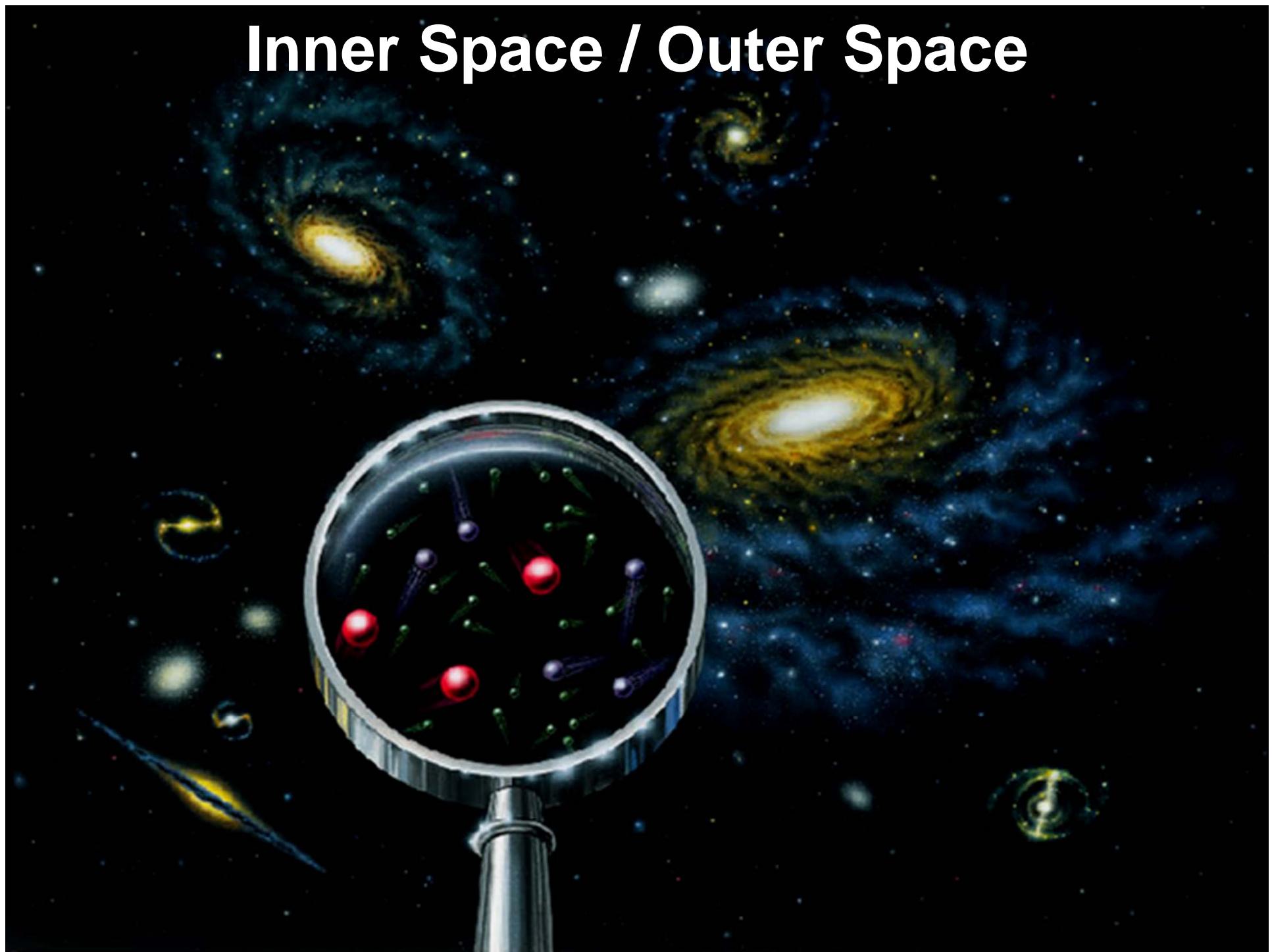
Dark Energy (70%)

Pushes things apart

Repulsive gravity

Weight of space?

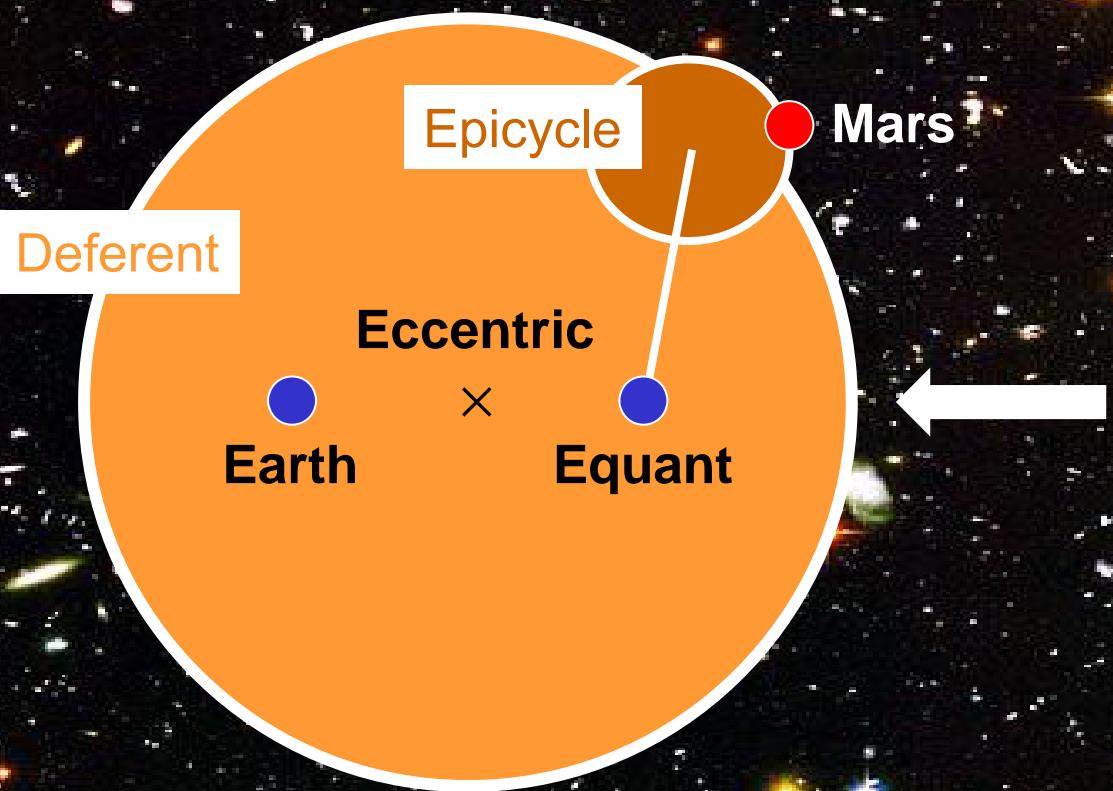
# Inner Space / Outer Space



The construction of a model... consists of snatching from the enormous and complex mass of facts called reality a few simple, easily managed key points which becomes for certain purposes a substitute for reality itself.

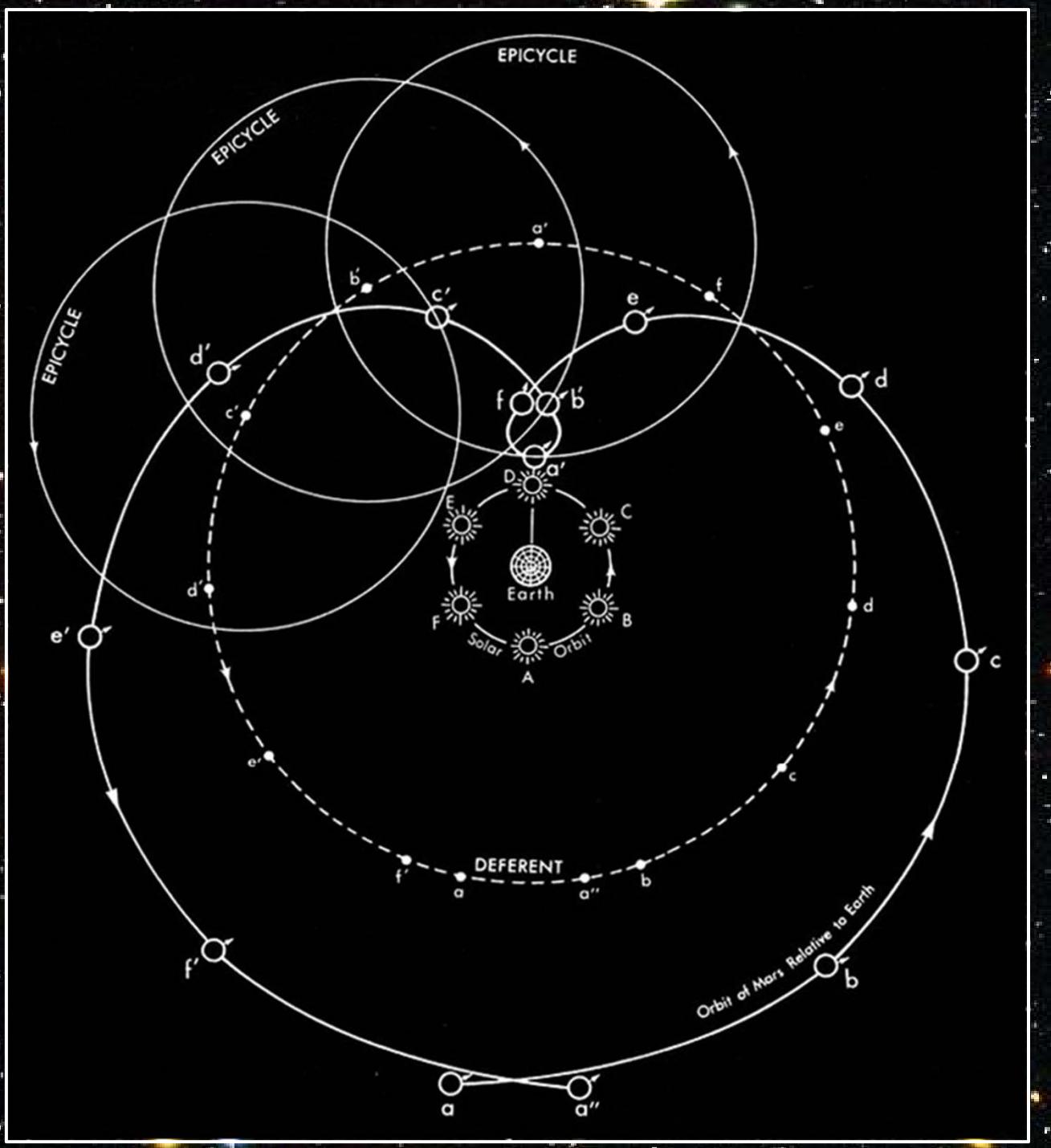
Evsey Dómar

*20<sup>th</sup>-century economist*

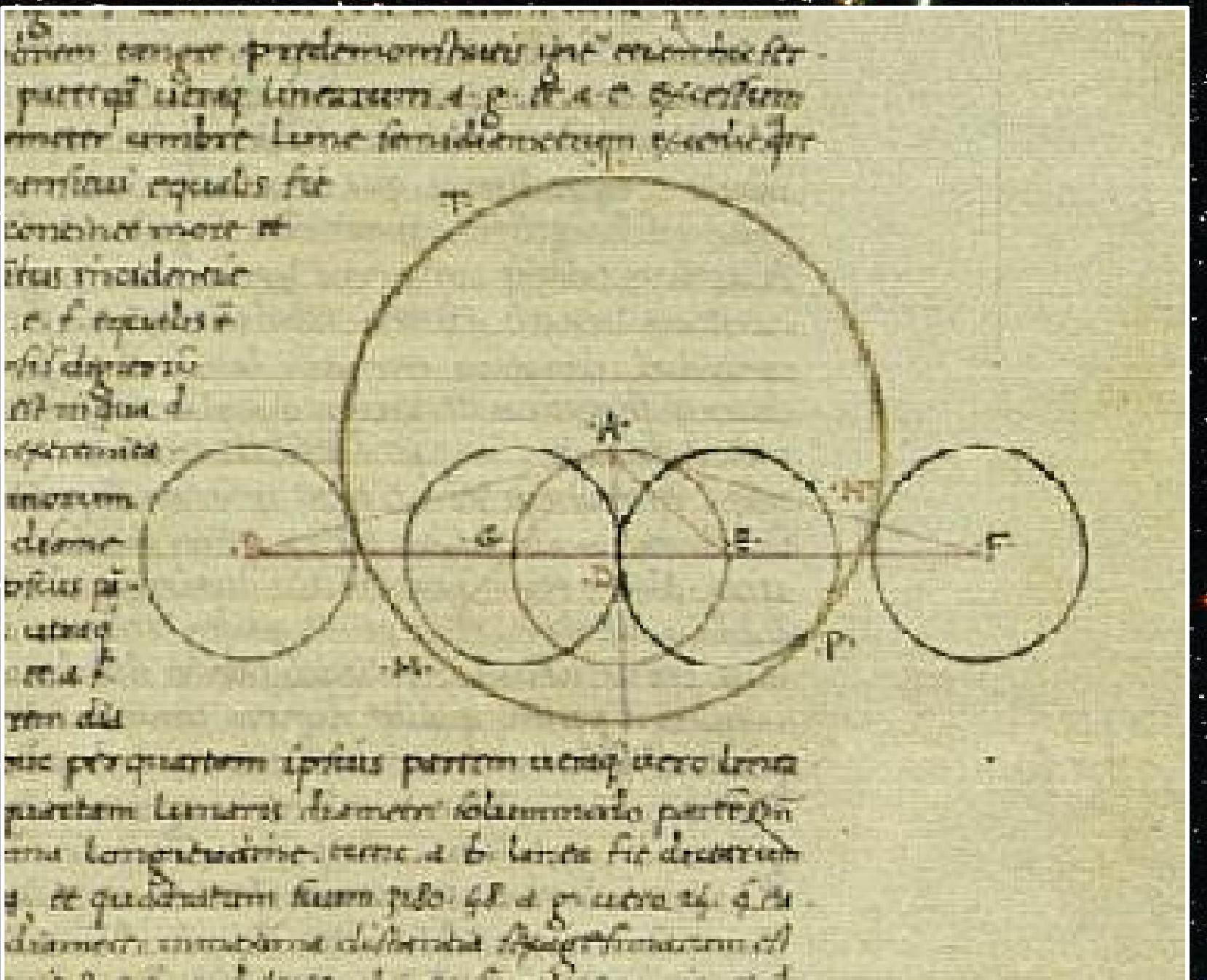


This cosmological model  
agreed with observations  
for 1300 years!

# A Previous Consensus Convergence Dominant Best-Fit Standard Cosmological Model

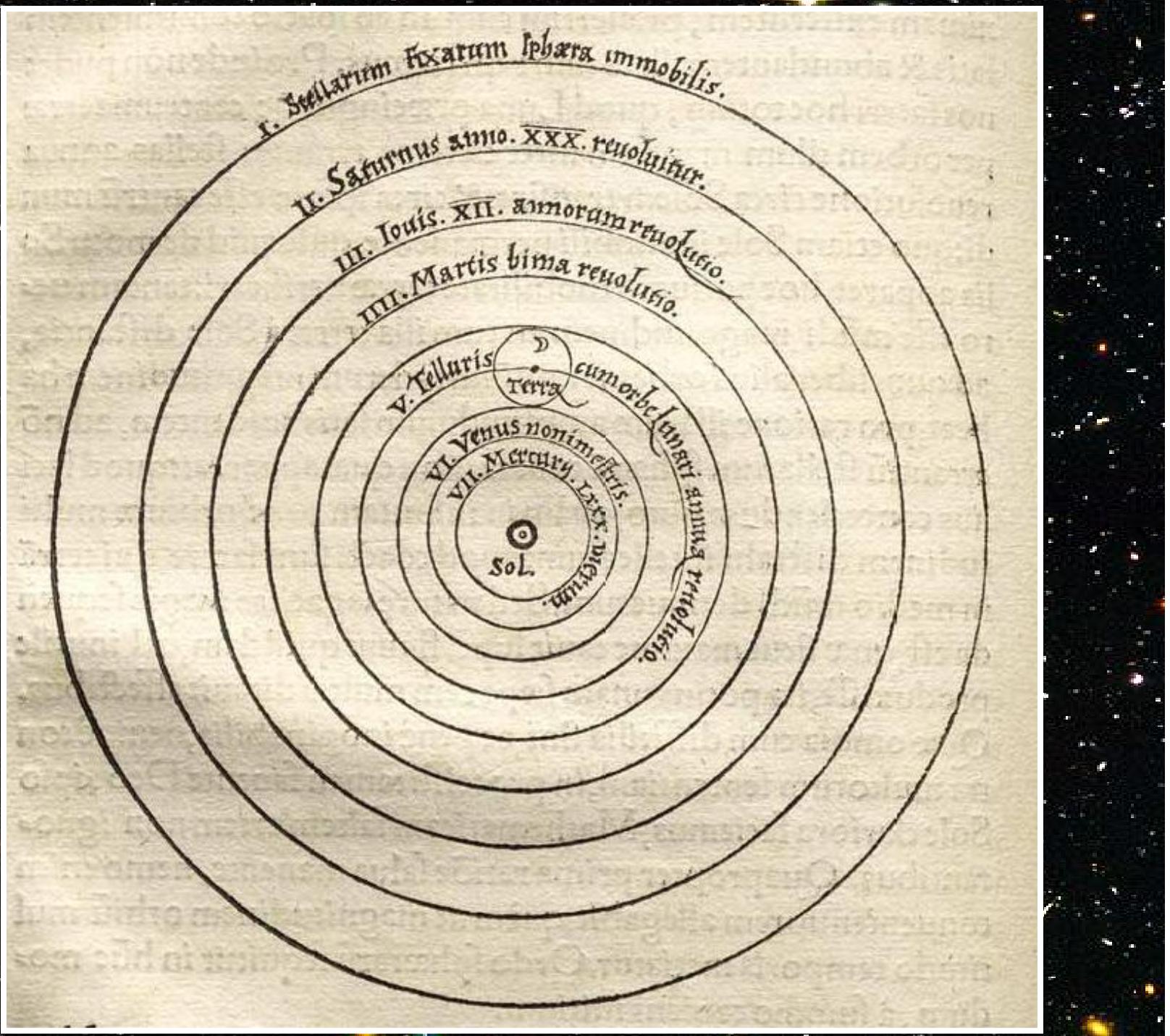


# Ptolemaic System The Almagest



George Trebizond's Latin translation (ca. 1451) of Almagest

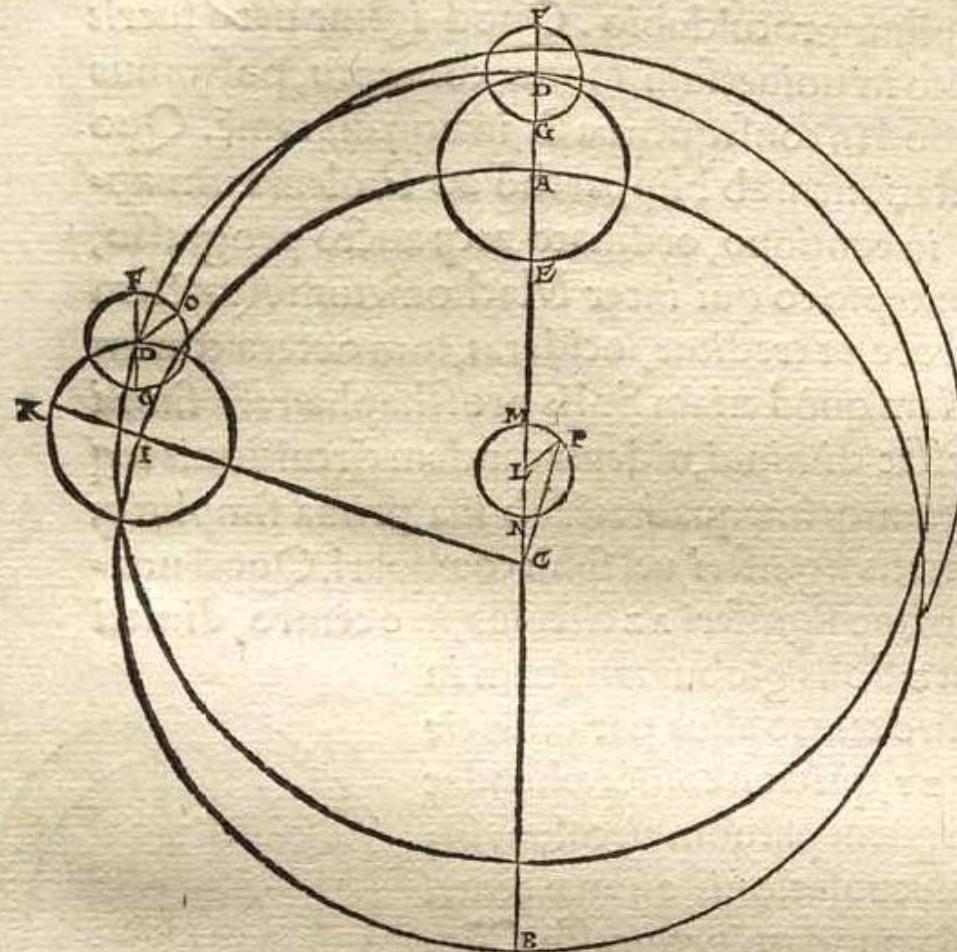
# Copernican System *De Revolutionibus*, Book I



# Copernican System De Revolutionibus, Book III.

quoqz epicyclum hoc modo. Sit mundo ac Soli homocentrus A.B, & A.C.B diameter, in qua summa absis contingat. Et facto in A centro epicyclus describatur D.E, ac rursus in D centro epicycli- um F.G, in quo terra uersetur, omniaqz in eodem plano zodiaci.

Sitqz epicycli primi motus in succedētia, ac annuus fe- rē, secūdi qz hoc est D, simi- liter annuus, sed in præce- dentia, ambo rumqz ad A.C lineam pares sint reuolutio- nes. Rursus cētrum terræ ex F in præce- dentia addat parumper ipsi D. Ex hoc manifestū est



quod cum terra fuerit in F, maximum efficiet Solis apo geum, in G minimum: in medijs autem circumferentijs ipsius F.G epi- cyclij faciet ipsum apogeum præcedere uel securi. auctum dimi-

# Dark Matter

IN THIS HOME  
WAS BORN FRITZ ZWICKY -  
THE ASTRONOMER  
WHO DISCOVERED  
NEUTRON STARS  
AND THE DARK MATTER  
IN THE UNIVERSE.

Varna, Bulgaria

Galaxy Clusters (e.g., Coma)



Fritz Zwicky 1930s

Swiss ETHZ  
Weyl & Scherrer

# Dark Matter

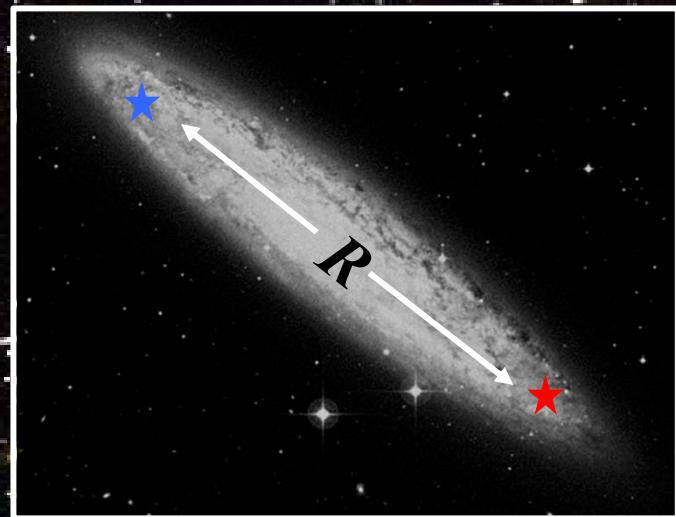
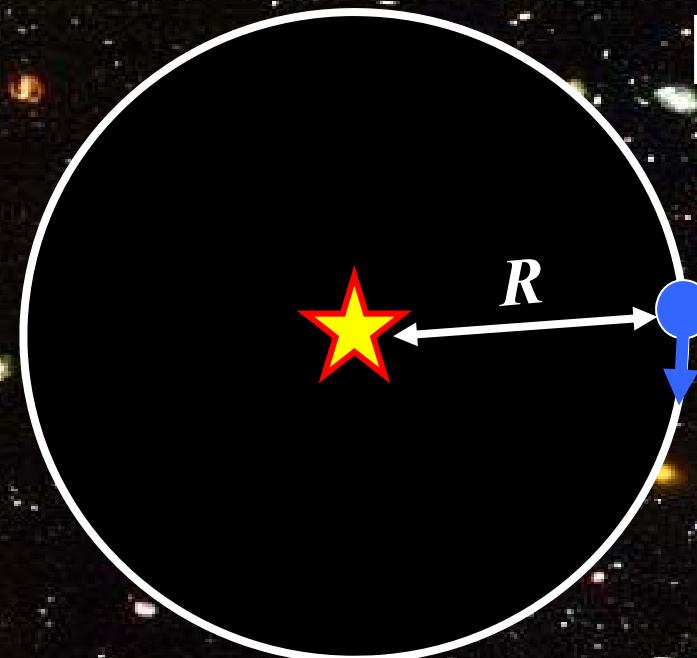
$$V^2 = \frac{G_N M_{\odot}}{R}$$

measure  $v$  &  $R \rightarrow M_{\odot}$

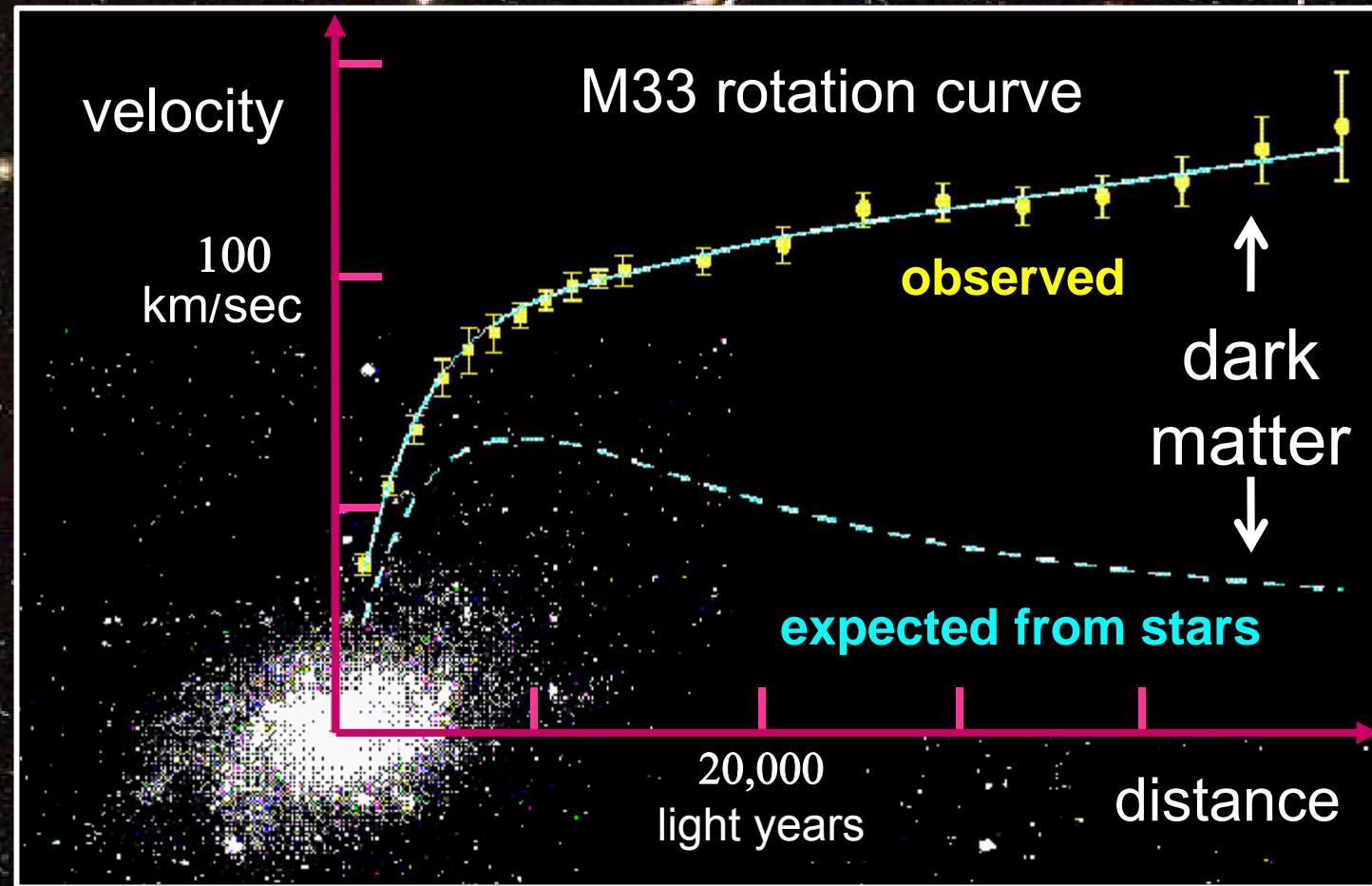
$$V^2 = \frac{G_N M_{$$

measure  $v$  &  $R \rightarrow M_{$

“outside” of galaxy, measure  $v$  &  $R \rightarrow M_{\text{GALAXY}}$



# Dark Matter



Vera Rubin 1970s

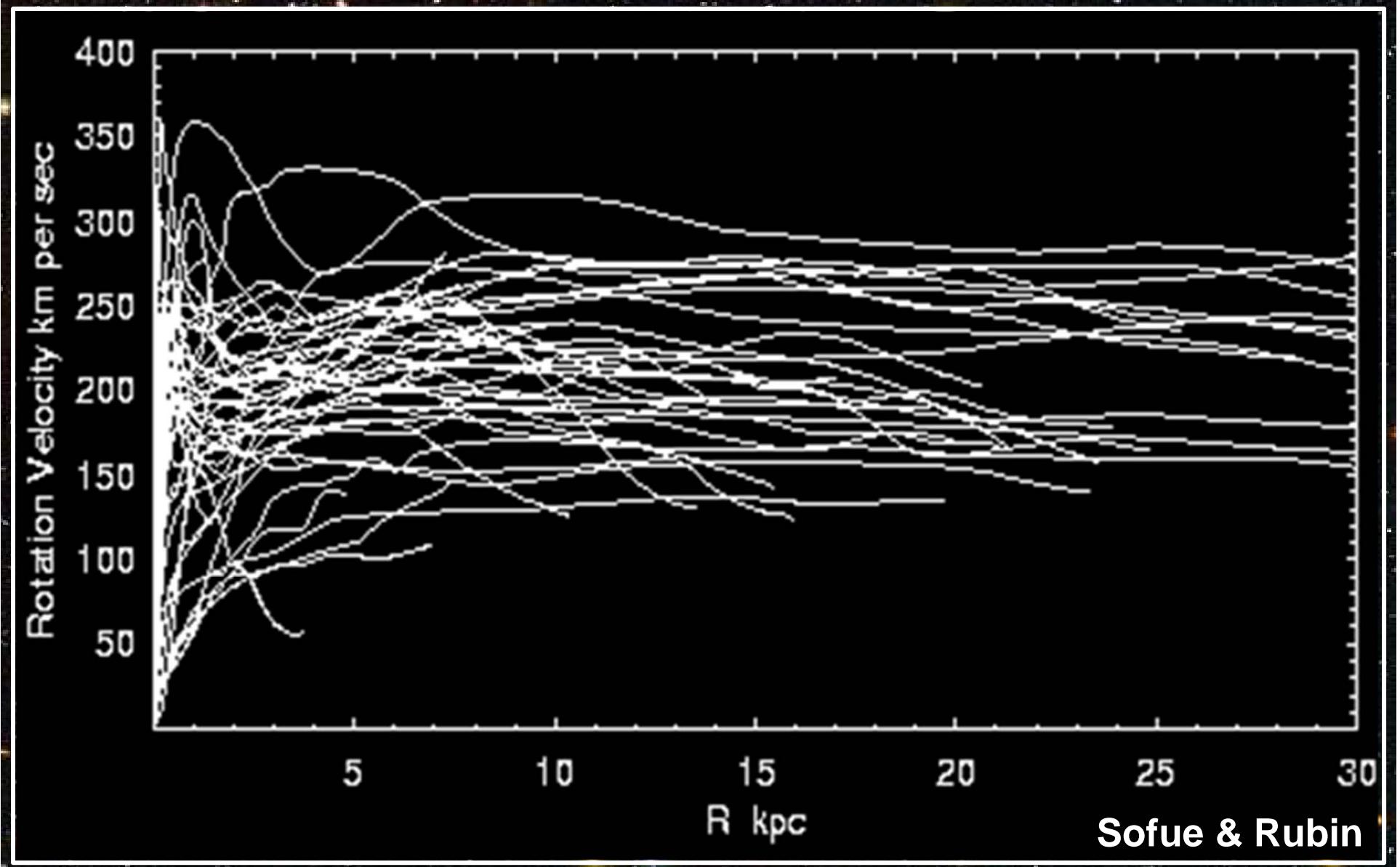
Individual Galaxies (e.g., M33)

# Dark Matter

CO – central regions

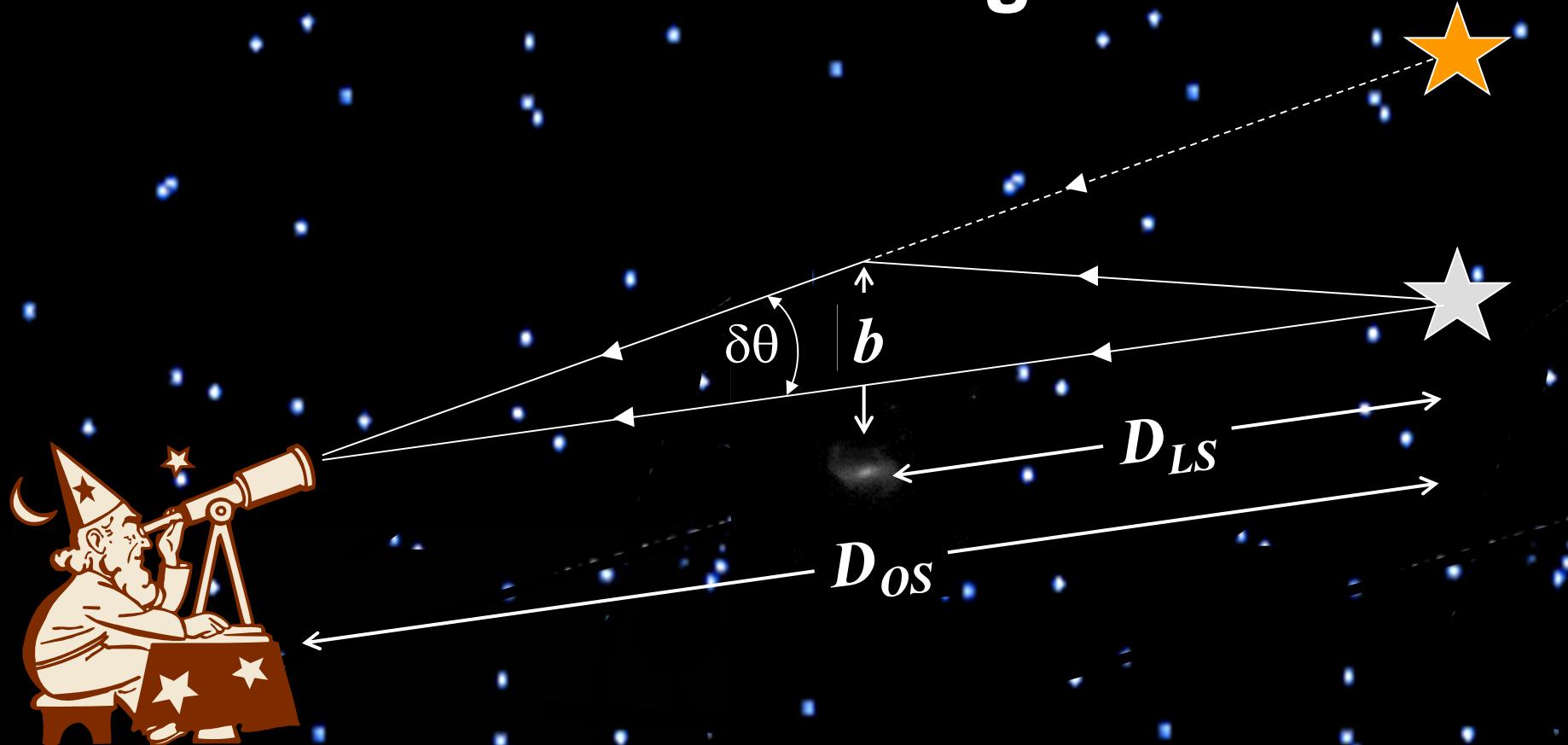
Optical – disks

HI – outer disk & halo



Sofue & Rubin

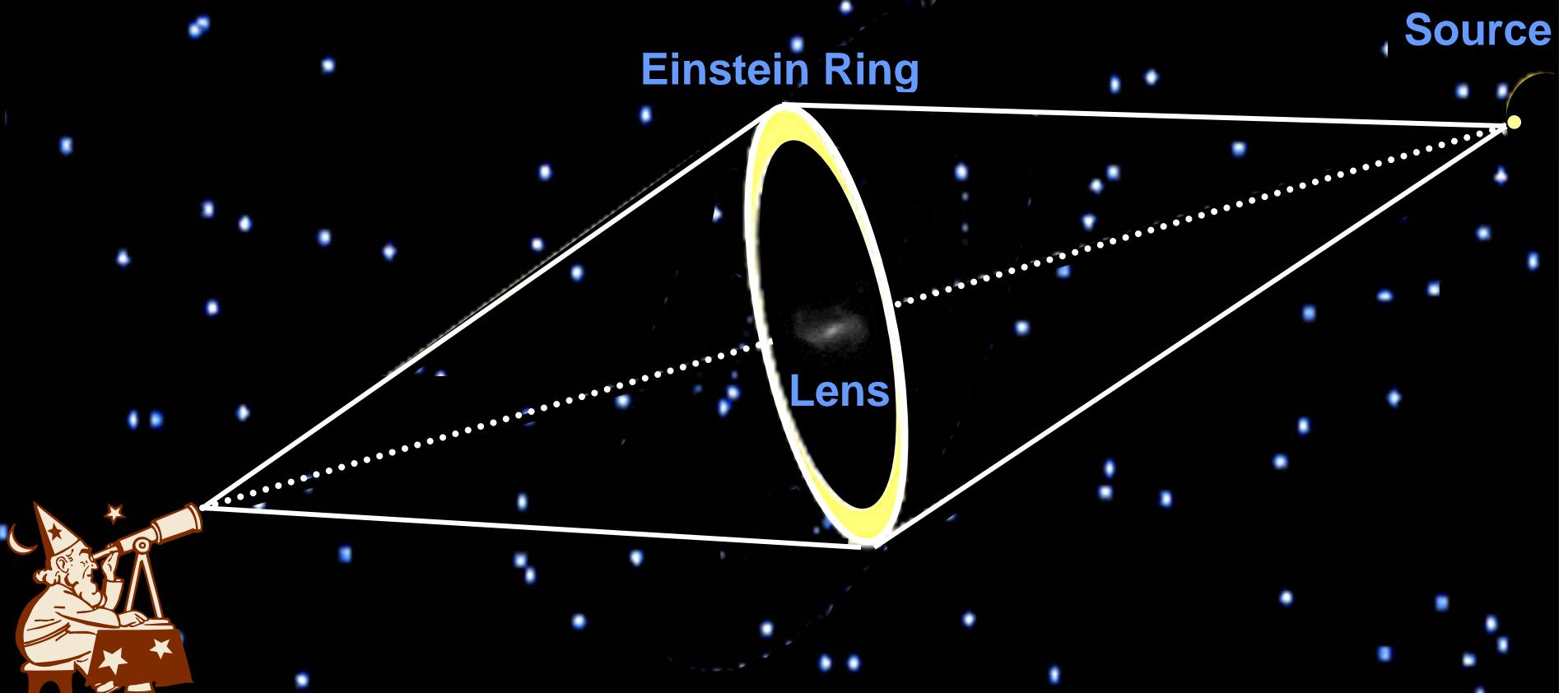
# Weak Lensing



observe  
deflection  
angle

$$\delta\theta = \frac{4GM}{b} \frac{D_{LS}}{D_{OS}}$$

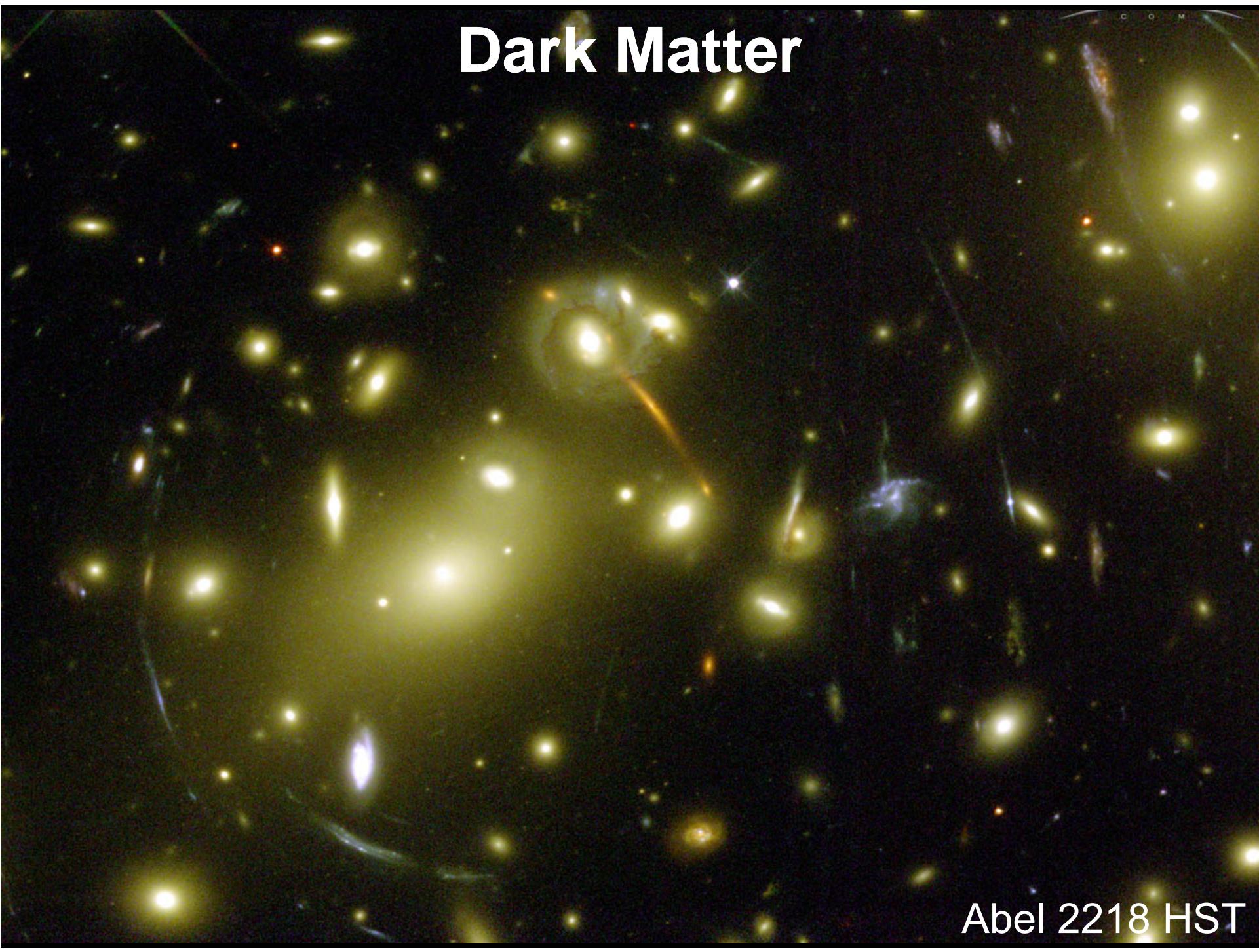
# Einstein Ring



Observer

Mass of lens determines angular size of ring





# Dark Matter

Abel 2218 HST

# Periodic Table – Chemist

# Periodic Table – Cosmologist

H

He

Metals

Metals

# The Universe Today

73% **Hydrogen** ( $10^{-5}$   $^2\text{H}$ -deuterium)

26% **Helium** ( $10^{-5}$   $^3\text{He}$ )

1% **Metals**

## The Universe 3 minutes AB

76% **Hydrogen** ( $10^{-5}$   $^2\text{H}$ -deuterium)

24% **Helium** ( $10^{-5}$   $^3\text{He}$ )

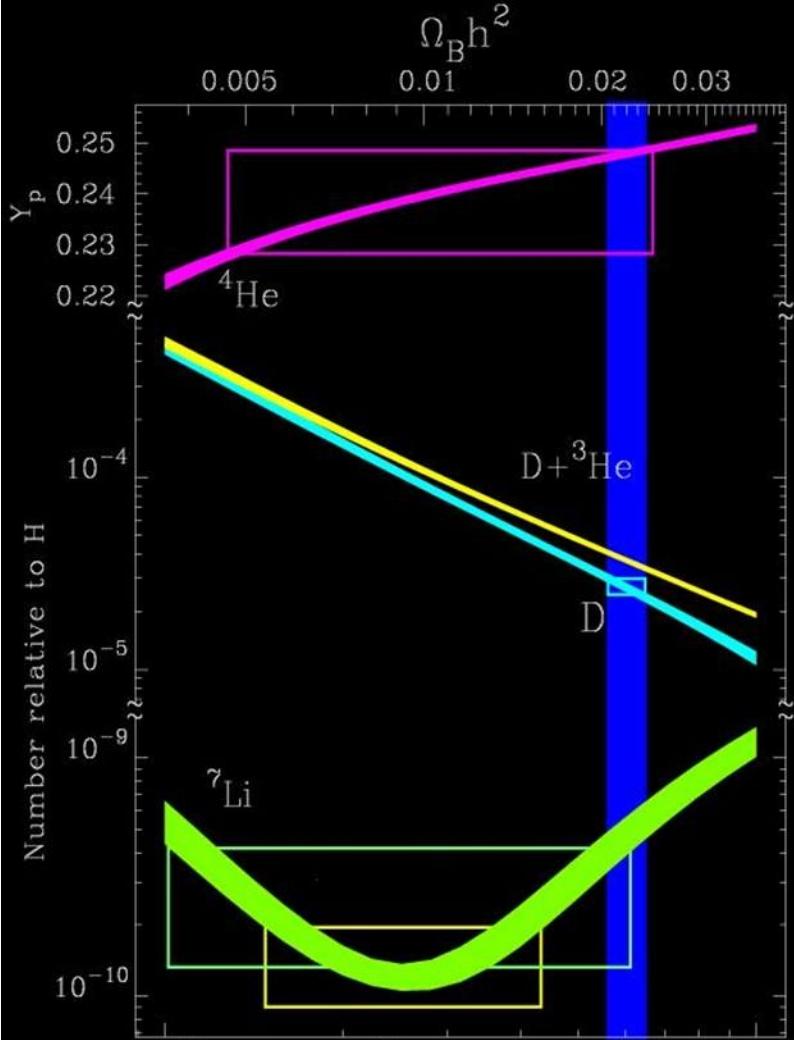
$10^{-8}\%$  **Lithium**

**Big Bang Nucleosynthesis (BBN)**

# Dark Matter

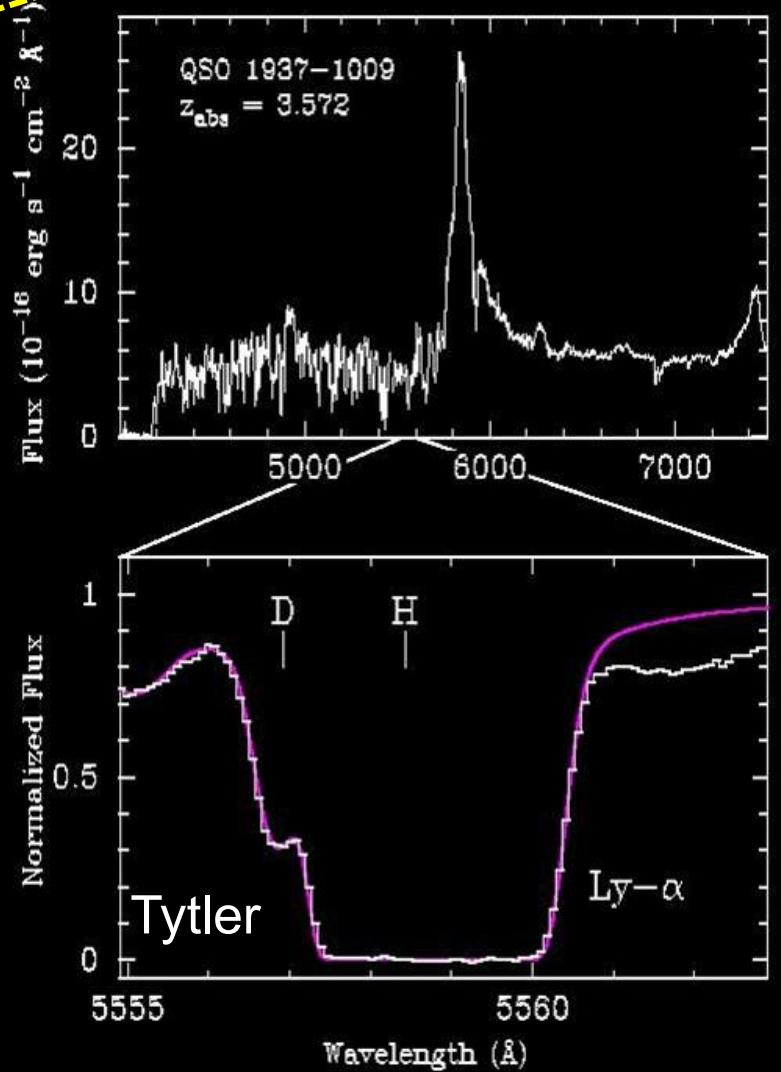
$$\Omega_B h^2 \sim 0.02$$

$$H_0 = 100h \text{ km s}^{-1} \text{ Mpc}^{-1}$$



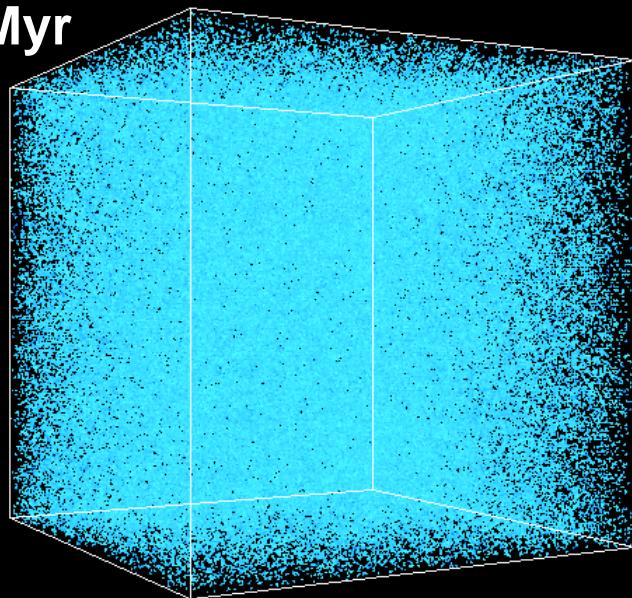
WMAP:  $\Omega_B h^2 = 0.0229 \pm 0.00073$

$$\Omega_i = \frac{\rho_i}{3H_0^2/8\pi G}$$

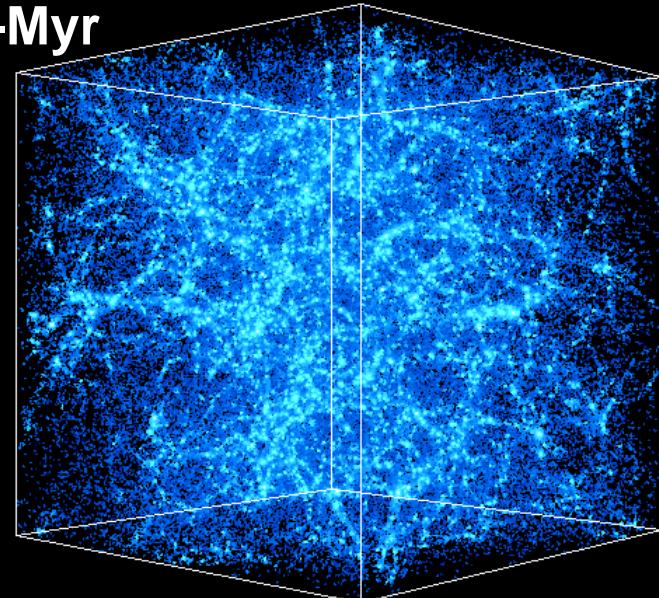


# Structure Formation

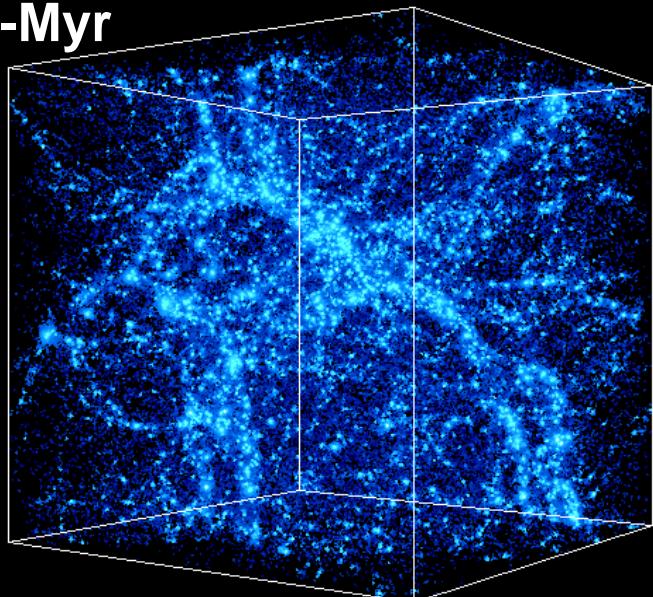
100 Myr



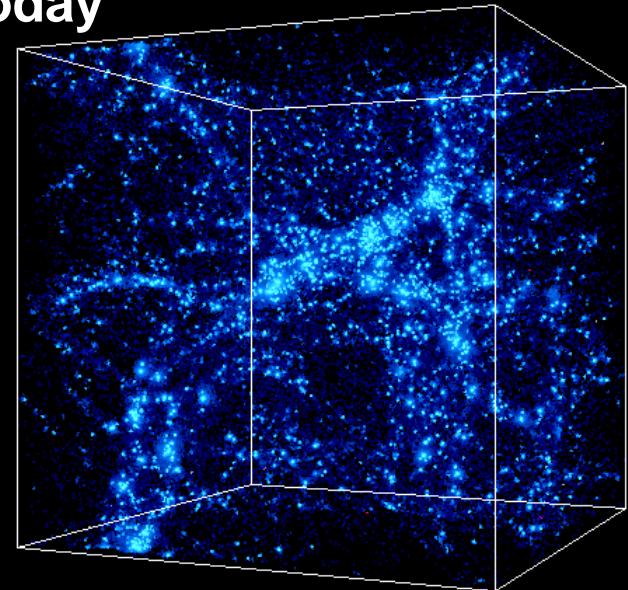
1 M-Myr



5 M-Myr

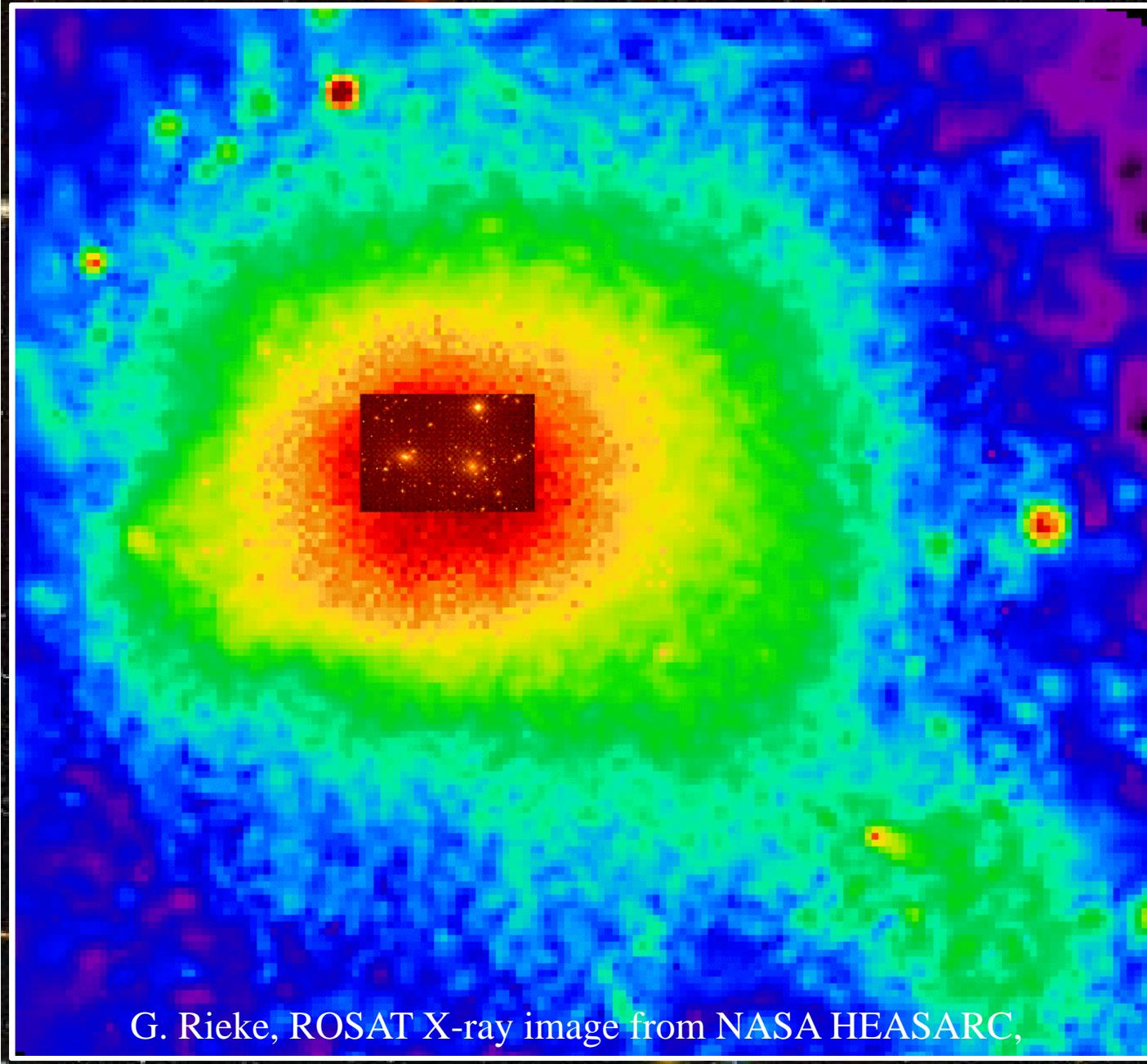


today



Kravtsov

# X-Ray Temperature of Galaxy Clusters



Coma cluster  
in X rays with  
visual image  
superimposed

X-Ray  
temperature  
measures  
depth of  
gravitational  
potential ✓

# Dark Matter



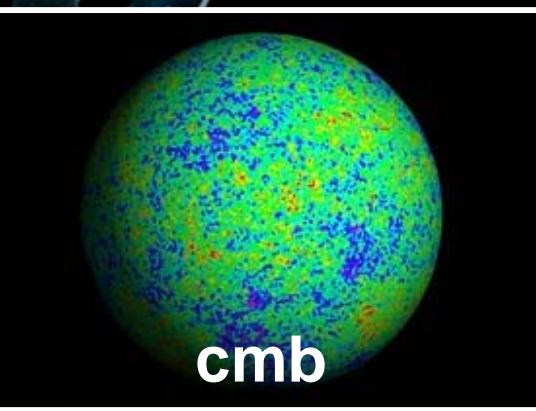
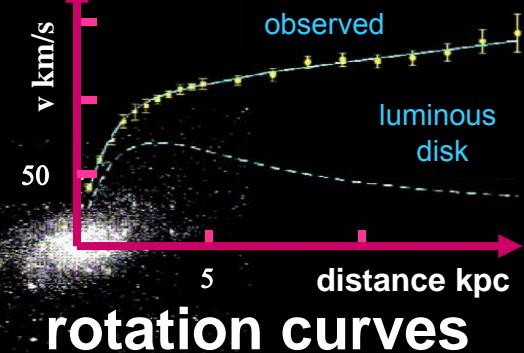
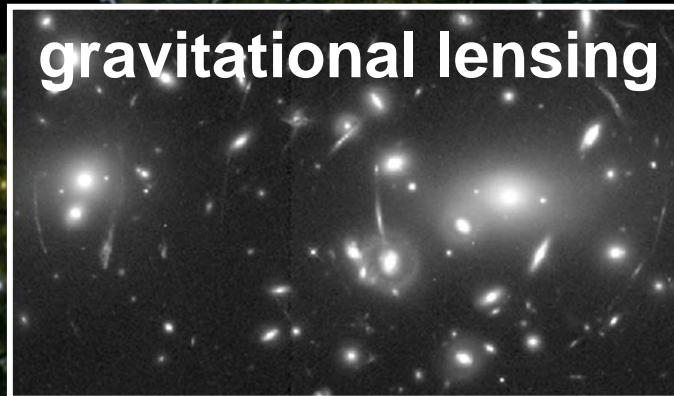
Chandra Science Center

# Dark Matter

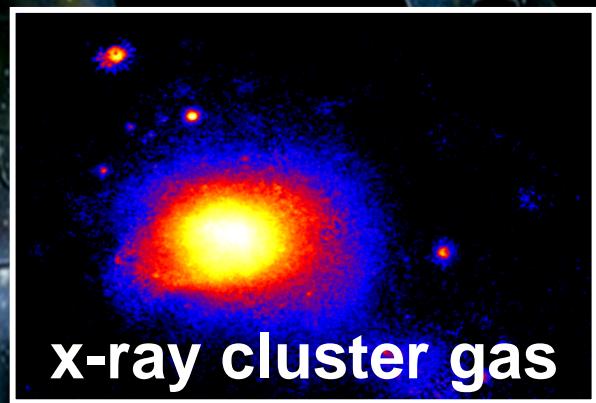
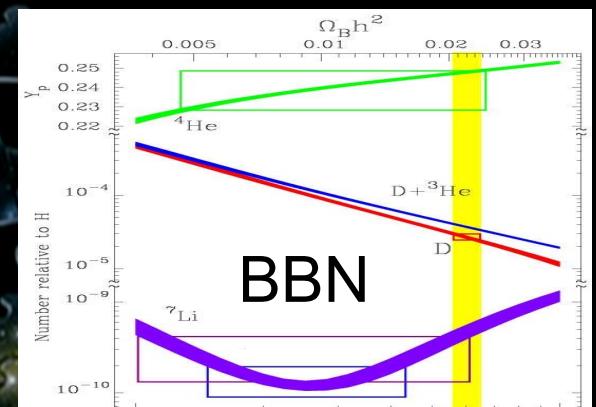
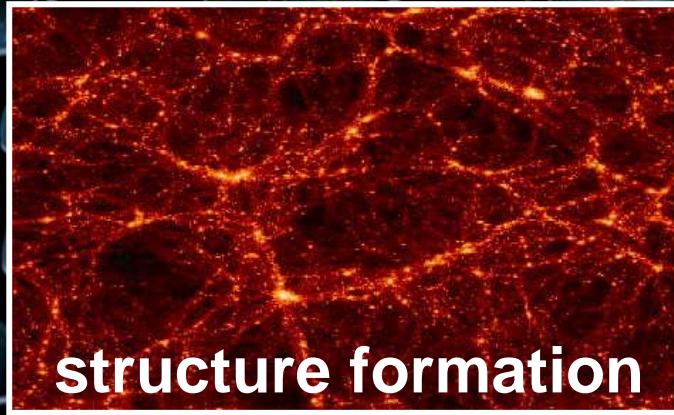
cluster dynamics



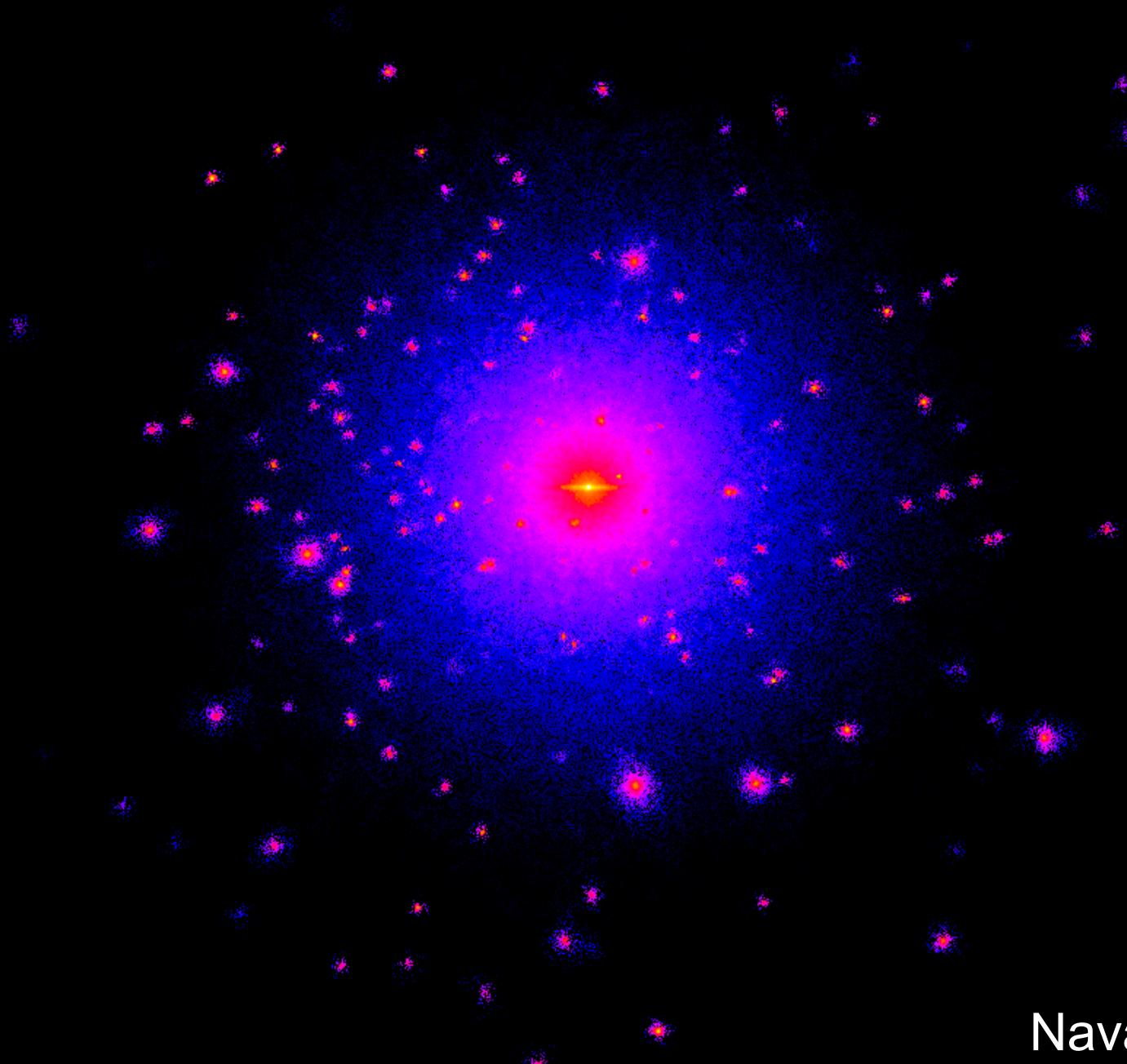
gravitational lensing



structure formation



# Dark Matter



Navarro, et al.

## simulation

SECOND EDITION 1989

sim-sim  
simson  
simul  
simulacral, a.  
simulacre  
simulacrum  
simulance  
simuland  
simulant, a. and n.  
simular, n. and a.  
simulate, ppl. a.  
simulate, v.  
simulated, ppl. a.  
simulately, adv.  
**simulation**  
simulative, a.  
simulator  
simulatory, a.  
simulcast, v.  
simule, v.  
simuler  
simulfix  
simuliid, n. and a.  
simulium  
simultal, a.  
simultanagnosia  
simultane, v.  
Simultaneism  
simultaneity  
simultaneous, a.  
simultaneously, adv.  
simultaneousness  
simultation  
simulty<sup>1</sup>

Pronunciation Spellings Etymology Quotations Date chart

**1. a.** The action or practice of simulating, with intent to deceive; false pretence, deceitful profession.

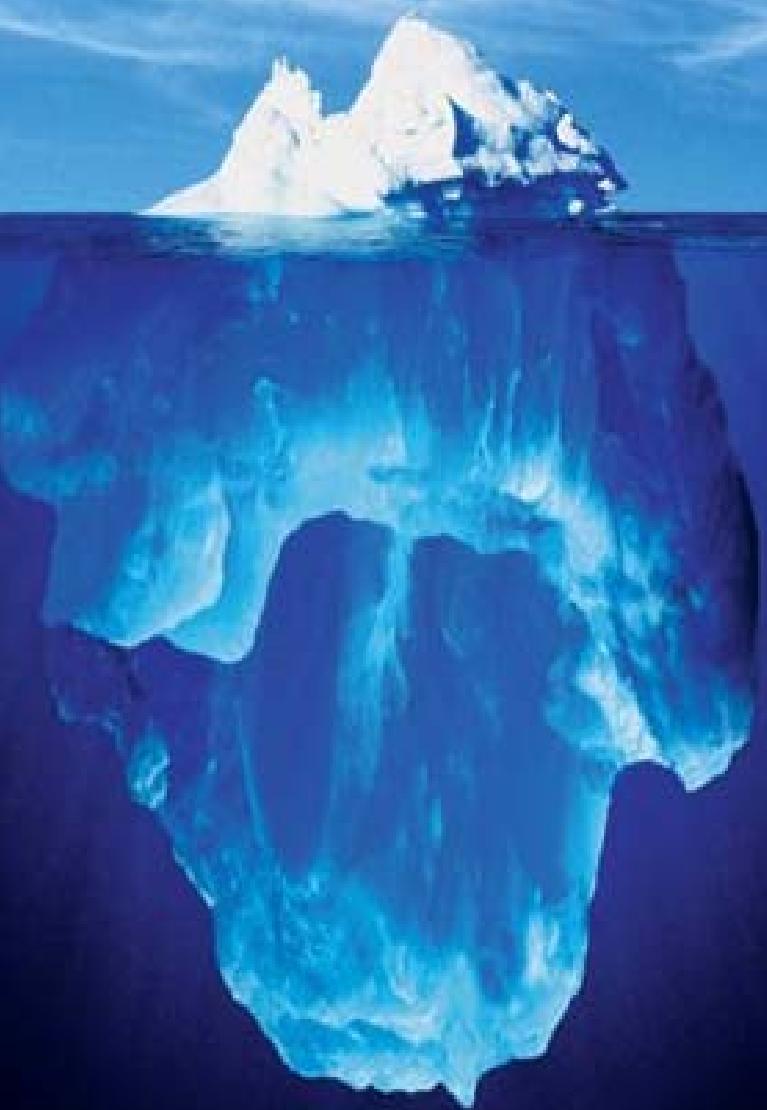
**1340** *Ayenb.* 23 And þerof wexeþ uele zennes, ase arisþhalf; þet is to wytene: lozengerie, simulacion. **c1400** *Rom. Rose* 7230 He nys no full good champioun That dredith such similacioun. **1412-20** *LYDG. Chron. Troy* iv. 4504 Amonge hem silfe to bringe in tresoun, Feyned troupe and symulacioun. **1542** *UDALL Erasm. Apoph.* 170 He..did with mutual simulacion on his partie cover & kepe secrete the colorable dooynge of the saied feloe. **1577** tr. *Bullinger's Decades* (1592) 319 This precept doth commaunde vs..that..wee doe our neighbor harme..neither by simulation nor dissimulation. **1611** *SPEED Hist. Gt. Brit.* vi. (1632) 114 His nature relishing too much of the Punick craft and simulation. **1692** *SOUTH Serm.* (1697) I. 525 A Deceiving by Actions, Gestures, or Behaviour, is called Simulation, or Hypocrisie. **1711** *STEELE Tatler* No. 213 ¶1 Simulation is a Pretence of what is not, and Dissimulation a Concealment of what is. **1788** *WESLEY Wks.* (1872) VII. 43 Simulation is the seeming to be what we are not; dissimulation, the seeming not to be what we are. **1836** *LANDOR Pericles & Aspasia* Wks. 1846 II. 379, I wish he were as pious as you are: occasionally he appears so. I attacked him on his simulation. **1872** *SHIPLEY Gloss. Eccl. Terms* 71 Fraud., whether it consists in simulation or dissimulation.

**b.** Tendency to assume a form resembling that of something else; unconscious imitation.

**1870** *MARCH Anglo-Saxon Gram.* 28 *Simulation.* The feigning a connection with words of similar sound is an important fact in English and other modern languages: asparagus > sparrow-grass.

**2.** A false assumption or display, a surface resemblance or imitation, *of* something.

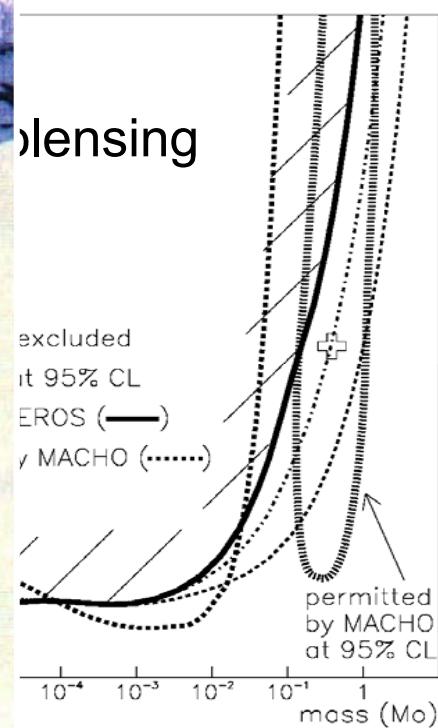
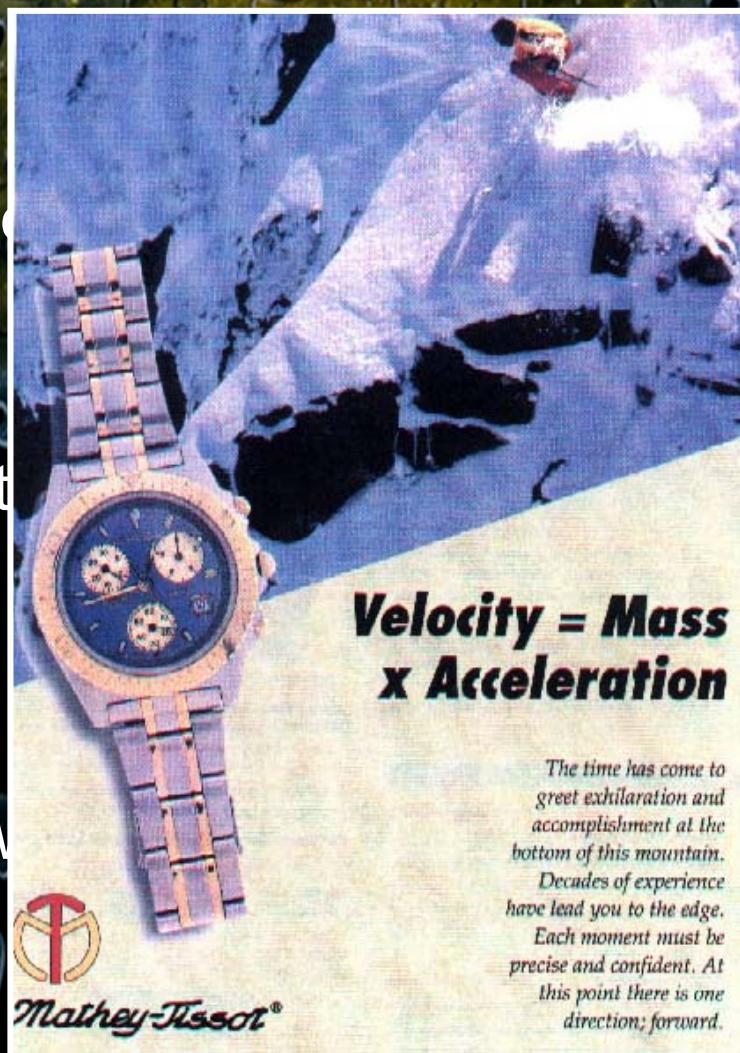
# Dark Matter



Most of the matter is dark and it's not even “normal” stuff!

# Dark Matter

- Modified Newtonian Dynamics
- Rogue Planets
- Mass challenged (e.g., galaxy rotation curves)
- Black holes
- Particle relic from the Big Bang



# Particle Dark Matter

- neutrinos
  - sterile neutrinos, gravitinos
  - Lightest supersymmetric particle
  - Lightest Kaluza-Klein particle
  - B.E.C.s, axions, axion clusters
  - solitons (Q-balls, B-balls, odd-balls, ...)
  - supermassive wimpzillas
- 
- (hot)  
(warm)  
(cold)  
(cold)
- thermal relics  
nonthermal relics

## Mass range

$10^{-22} \text{ eV}$  ( $10^{-56} \text{ g}$ ) B.E.C.s  
 $10^{-8} M_\odot$  ( $10^{+25} \text{ g}$ ) axion clusters

## Interaction strength range

Only gravitational: wimpzillas  
Strongly interacting: B balls

**NEUTRINO MASS AND MIXING  
IMPLIED BY UNDERGROUND DEFICIT OF LOW ENERGY MUON-NEUTRINO EVENTS**

John G. LEARNED, Sandip PAKVASA, and Thomas J. WEILER <sup>1</sup>

*Department of Physics and Astronomy, University of Hawaii at Manoa, Honolulu, HI 96822, USA*

Received 14 March 1988

Recent observations of a deficit of cosmic ray muon-neutrino interactions in underground detectors suggest that the muon neutrinos may have oscillated to another state. We examine possible neutrino mass and mixing patterns, and their implications for vacuum and matter effects on solar neutrinos, on neutrinos passing through the earth, and on terrestrial neutrino beams. By invoking the see-saw mechanism of neutrino mass generation, we draw inferences on closure of the universe with neutrino masses, on the number of generations, on t-quark and fourth generation masses, and on the Peccei-Quinn symmetry breaking scale. Testable predictions are suggested.

e find

(6)

flux is de-  
to estimate  
increased by

as much as 50%. (b) Atmospheric electron-neutrinos and muon-neutrinos (not antineutrinos) coming through the earth at  $E_\nu \sim 50 - 150$  GeV have matter-enhanced oscillations and the muon-neutrinos down/up flux ratio should be even larger than the nonmatter-enhanced expectation (for energies  $\sim 1$

**(d) Relic tau neutrinos have sufficient energy density to close the university**

angle is

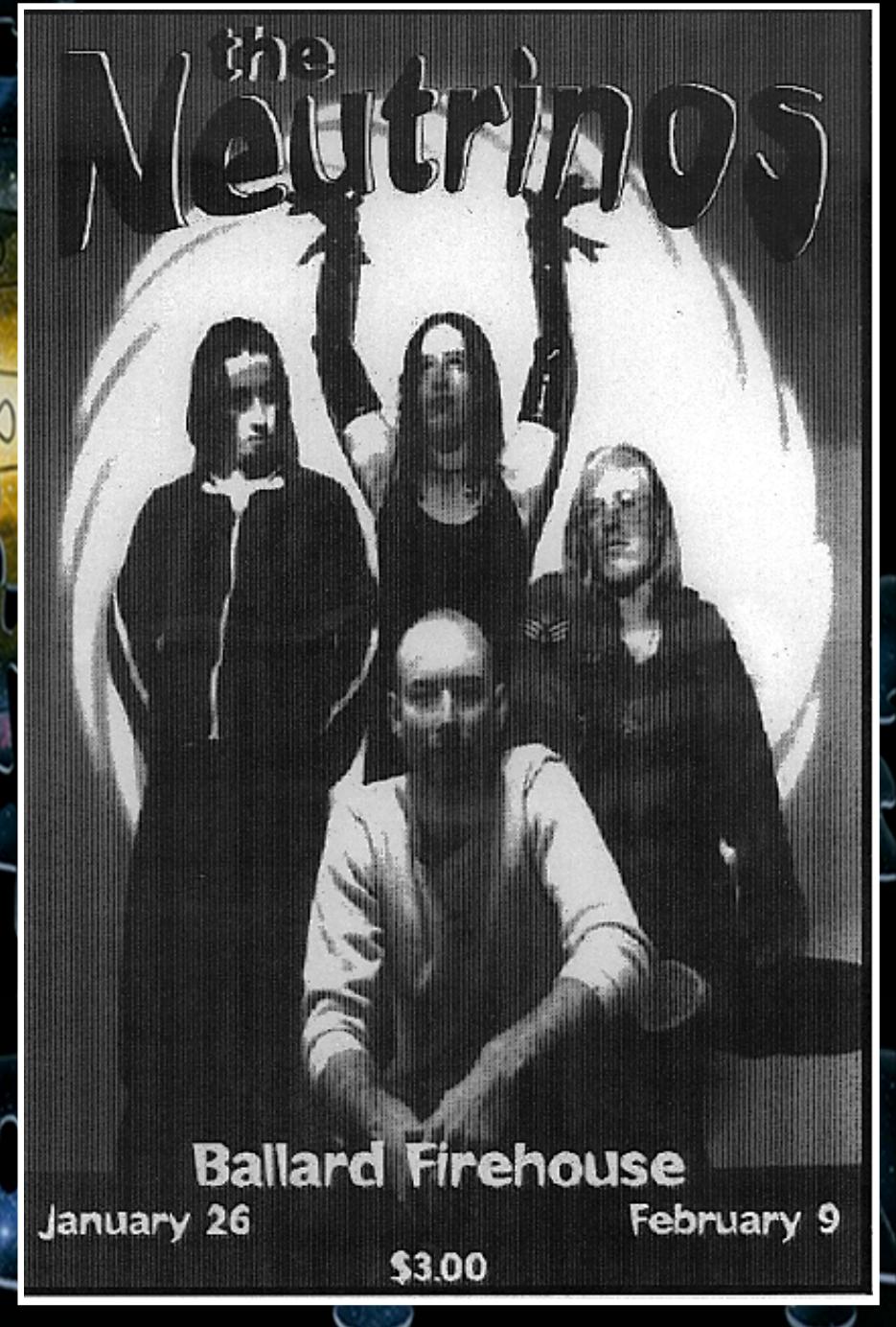
(8)

und (from  
are forced

(d) Relic tau neutrinos have sufficient energy density to close the university [11] (thus favoring hot dark matter over cold): the tau-neutrino mass may be determined from the time spread of events from a galactic supernova. (e) There are only three generations: the mass of a fourth-generation heavy lepton is bounded from below by the UA1 data [12] and from

# WIMPy Neutrinos

- **Neutrinos exist:**  
three active + sterile?
- **Neutrinos have mass:**  
Atmospheric ( $10^{-2}$  eV)  
Solar ( $10^{-3}$  eV)
- **Contribute to  $\Omega$**   
hot thermal relic:  
$$\Omega_{\nu\nu} \approx -\frac{m_\nu}{47 \text{ eV}}$$
- **Not most of dark matter**  
too light! too hot!



# Particle Dark Matter

- neutrinos
  - sterile neutrinos, gravitinos
  - Lightest supersymmetric particle
  - Lightest Kaluza-Klein particle
  - B.E.C.s, axions, axion clusters
  - solitons (Q-balls, B-balls, odd-balls, ...)
  - supermassive wimpzillas
- 
- (hot)  
(warm)  
(cold)  
(cold)
- thermal relics  
nonthermal relics

## Mass range

$10^{-22} \text{ eV}$  ( $10^{-56} \text{ g}$ ) B.E.C.s  
 $10^{-8} M_\odot$  ( $10^{+25} \text{ g}$ ) axion clusters

## Interaction strength range

Only gravitational: wimpzillas  
Strongly interacting: B balls

# WIMPy Sterile Neutrinos (or Gravitinos)



- weaker interactions
- decouple earlier
- diluted more
- can have larger mass
- smaller velocity than neutrinos: “warm”

Particle models with sterile neutrinos (or gravitinos) in desired mass range are “unfashionable” (IMO).

# Particle Dark Matter

- neutrinos
  - sterile neutrinos, gravitinos
  - Lightest supersymmetric particle
  - Lightest Kaluza-Klein particle
  - B.E.C.s, axions, axion clusters
  - solitons (Q-balls, B-balls, odd-balls, ...)
  - supermassive wimpzillas
- 
- (hot)  
(warm)  
(cold)  
(cold)
- thermal relics  
nonthermal relics

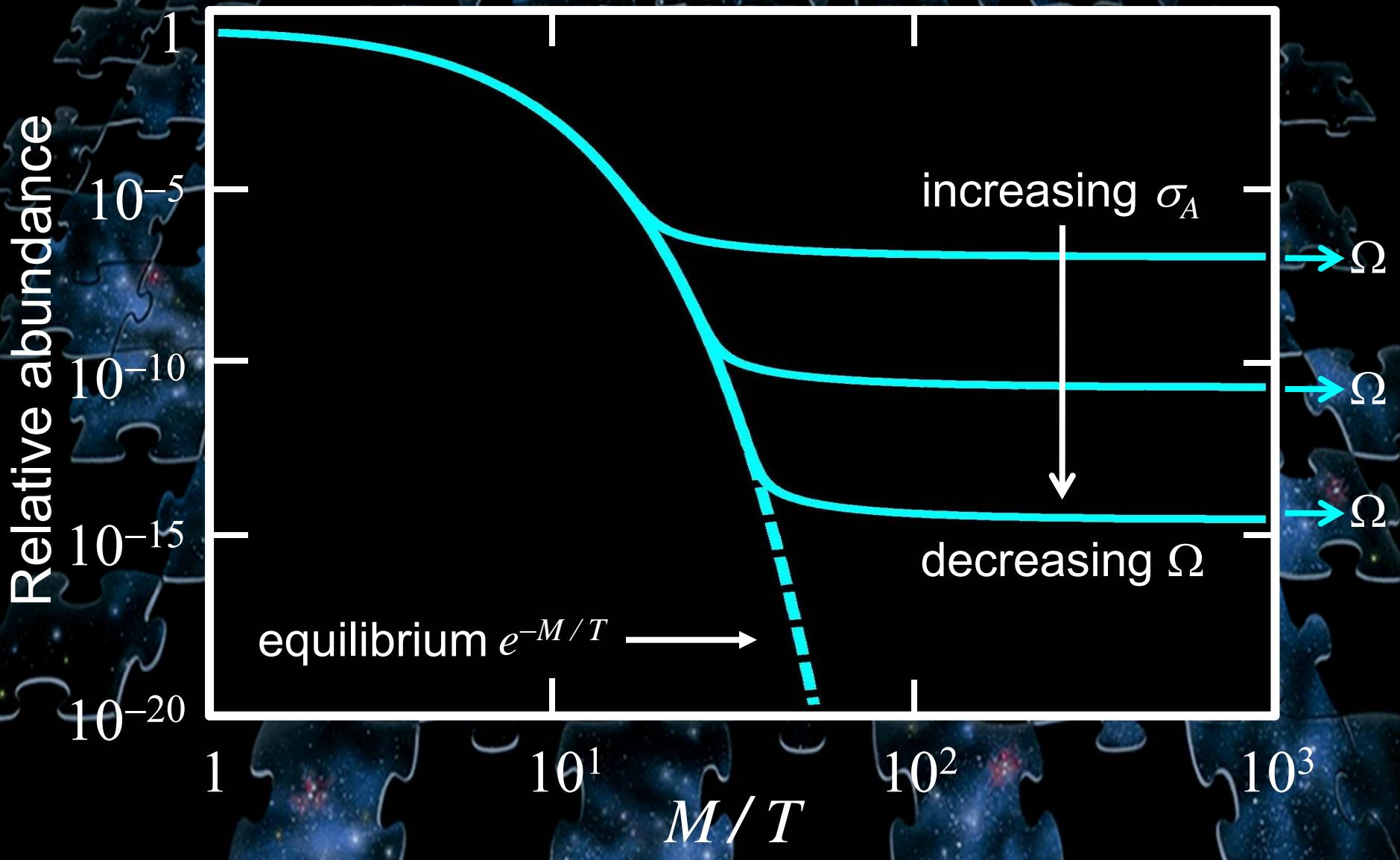
## Mass range

$10^{-22} \text{ eV}$  ( $10^{-56} \text{ g}$ ) B.E.C.s  
 $10^{-8} M_\odot$  ( $10^{+25} \text{ g}$ ) axion clusters

## Interaction strength range

Only gravitational: wimpzillas  
Strongly interacting: B balls

# Cold Thermal Relics\*



\* An object of particular veneration.



# Fermi National Accelerator Laboratory

FERMILAB-Pub-77/41-THY  
May 1977

## Cosmological Lower Bound on Heavy Neutrino Masses

BENJAMIN W. LEE \*  
Fermi National Accelerator Laboratory, Batavia, Illinois 60510

AND

STEVEN WEINBERG \*\*  
Stanford University, Physics Department, Stanford, California 94305

### ABSTRACT

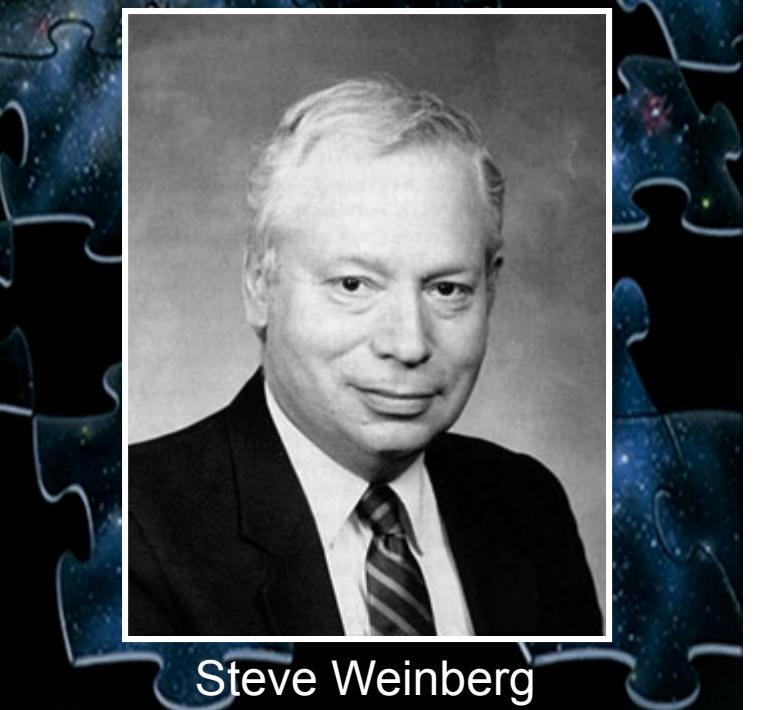
The present cosmic mass density of possible stable neutral heavy leptons is calculated in a standard cosmological model. In order for this density not to exceed the upper limit of  $2 \times 10^{-29} \text{ g/cm}^3$ , the lepton mass would have to be greater than a lower bound of the order of 2 GeV.

---

\*\* On leave 1976-7 from Harvard University.



Ben Lee (1935 — June 1977)



Steve Weinberg

$$\frac{dn}{dt} = -\frac{3\dot{R}}{R} n - \langle\sigma v\rangle n^2 + \langle\sigma v\rangle n_0^2 . \quad (2)$$

Here  $n$  is the actual number density of heavy neutrinos at time  $t$ ;  $R$  is the cosmic scale factor;  $\langle\sigma v\rangle$  is the average value of the  $L^0 L^0$  annihilation cross-section times the relative velocity and  $n_0$  is the number density of heavy neutrinos in thermal (and chemical) equilibrium<sup>6</sup>:

$$n_0(T) = \frac{2}{(2\pi)^3} \int_0^\infty 4\pi p^2 dp \left[ \exp\left(\frac{(m_L^2 + p^2)^{1/2}}{kT}\right) + 1 \right]^{-1} . \quad (3)$$

(We use units with  $M=c=1$  throughout.)

At the temperatures we are considering here, the energy

$$\frac{dn}{dt} = -\frac{3\dot{R}}{R} n - \langle\sigma v\rangle n^2 + \langle\sigma v\rangle n_0^2$$

where  $\rho$  is the energy density

$$\rho = N_F a T^4 = N_F \pi^2 (kT)^4 / 15 \quad (5)$$

with  $N_F$  an effective number of degrees of freedom, counting  $1/2$  and  $7/16$  respectively for each boson or fermion species and spin state. For temperatures in the range of 10-100 MeV (which most concern us here) we must include just  $\gamma, v_e, \bar{v}_e, v_\mu, \bar{v}_\mu, e^-$ , and  $e^+$ , so  $N_F = 4.5$ , a value we will adopt for most purposes. However, if current ideas about the strong interactions are correct, then  $N_F$  rises steeply at a temperature of order 500 MeV to a value<sup>7</sup>  $N_F \approx 30$ .

To estimate  $\langle\sigma v\rangle$ , we note that the heavy neutrinos must be quite non-relativistic at the temperature  $T_f$  where they freeze

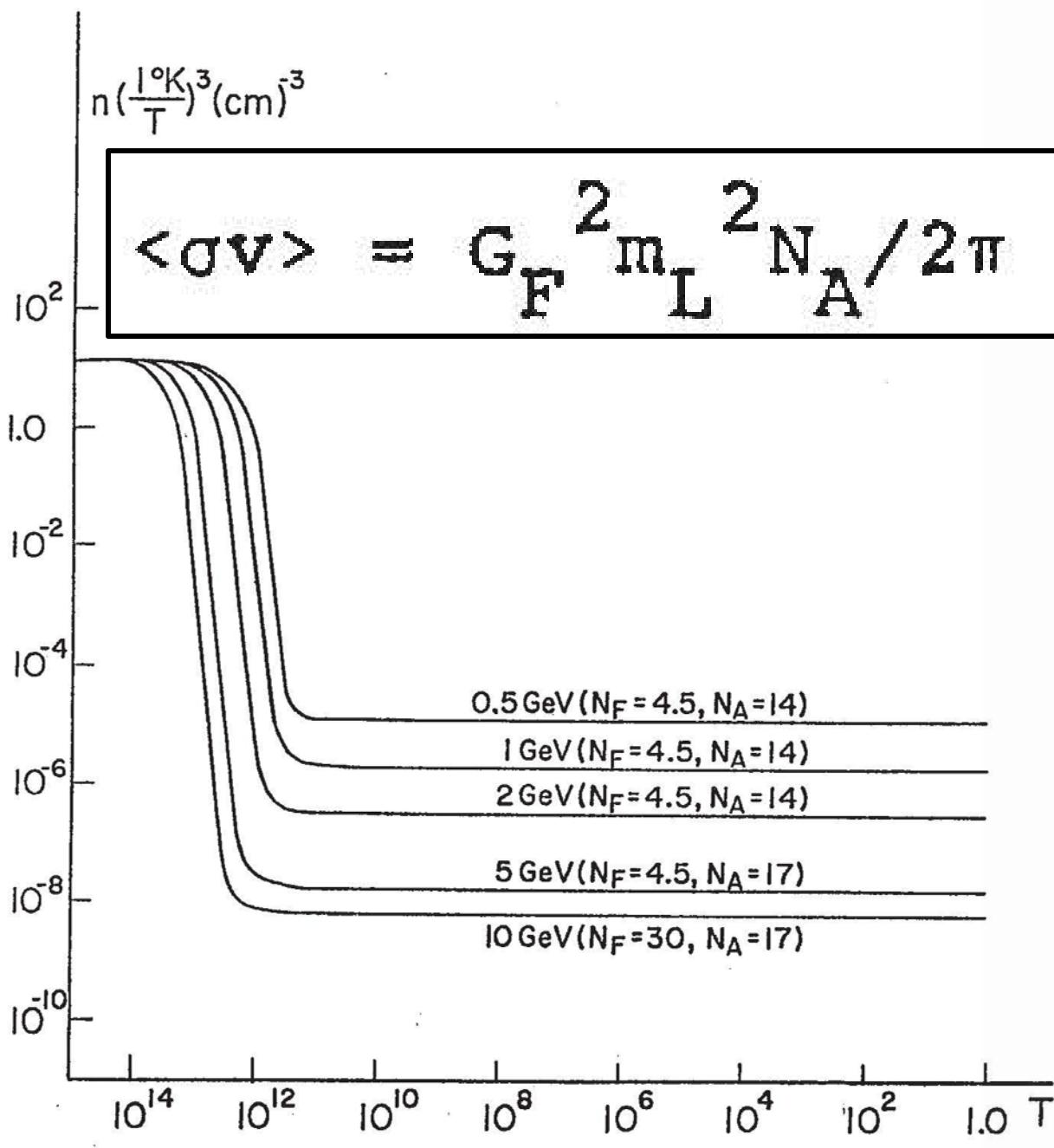
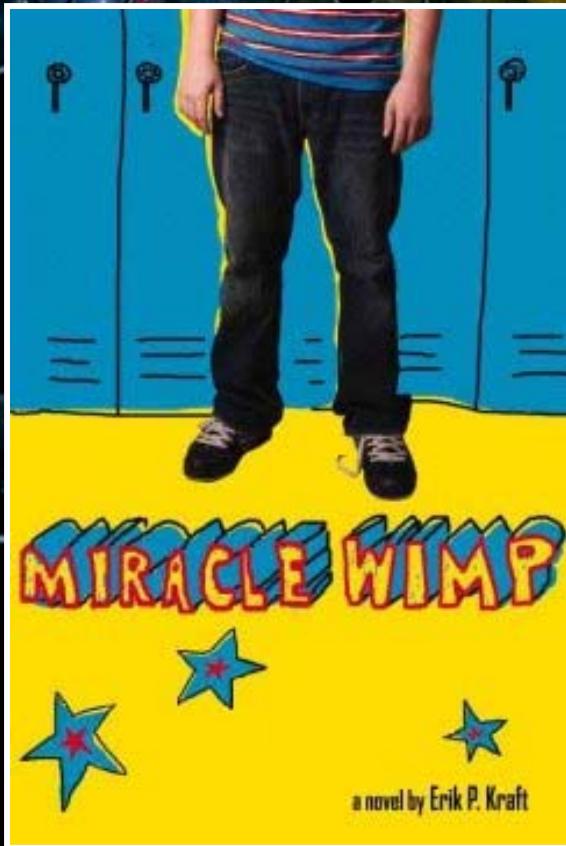


FIG. 1

# Cold Thermal Relics Are WIMPs

$\Omega \rightarrow$  Cross section (& mass ?) of order weak scale  
WIMP (Weakly Interacting Massive Particle)

## The WIMP Miracle



mir·a·cle  
\'mir-i-kəl\  
noun

1 : an extraordinary event manifesting divine intervention in human affairs

Coincidence or Causation?

# WIMPs

Goal: Discover dark matter and its role in shaping the universe

## Particle Physics:

Discover dark matter and learn how it is ...

... grounded in physical law

... embedded in an overarching physics model/theory

## Astro Physics:

Understand the role of dark matter in ...

... formation of structure

... evolution of structure

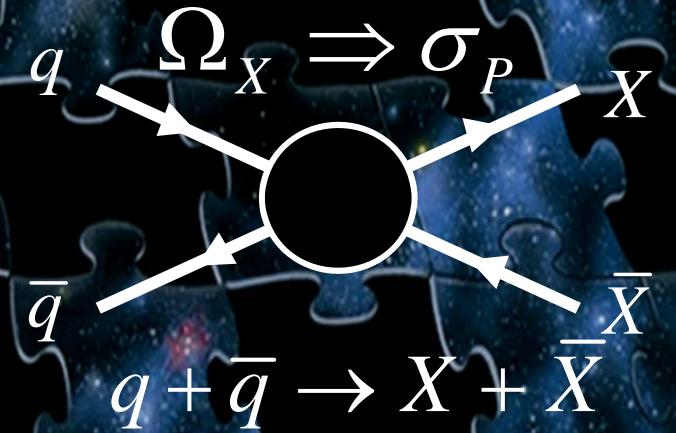
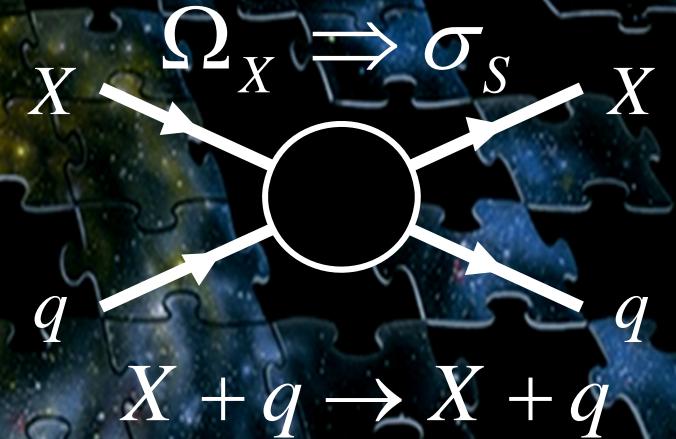
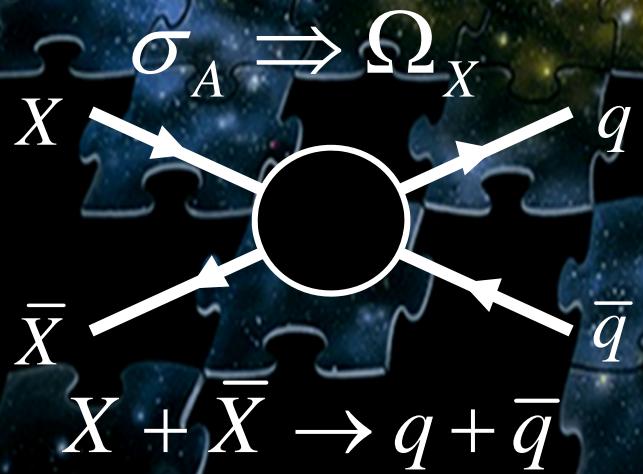
## WIMPs:

massive, stable, “weakly” interacting,  $SU(3)_C \times U(1)_{EM}$  singlet

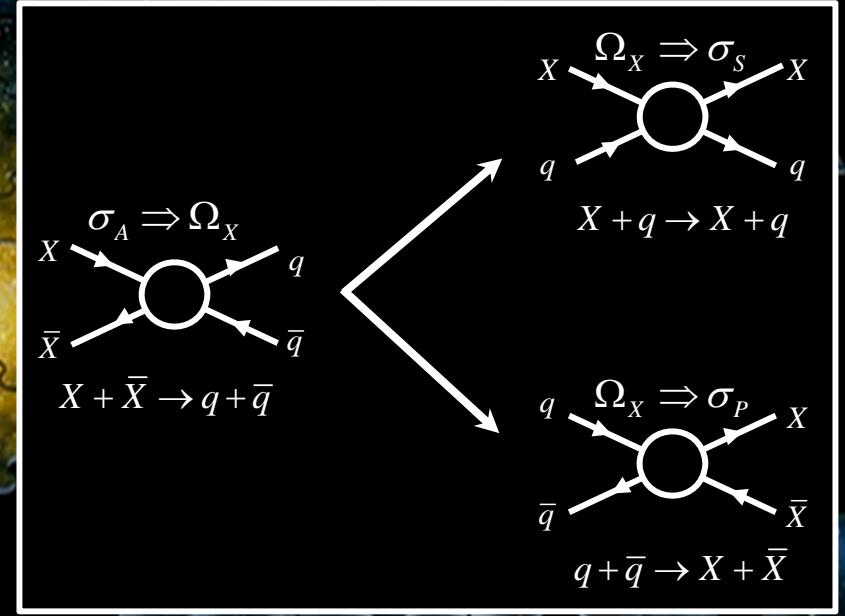
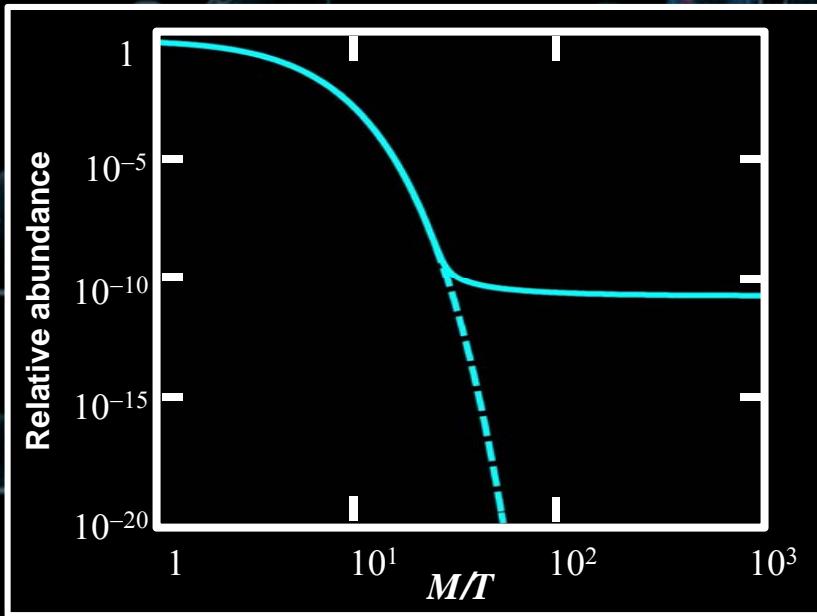
WIMP must be a *BSM* (but perhaps not far BSM) particle.

# WIMPs

Too good to be true?



# WIMPs



Not quite so simple:

- velocity dependence
- co-annihilation
- resonances
- superwimps
- dependence on  $M, g_*$ ,
- ...

Not quite so simple:

- velocity dependence
- local phase-space density
- flavor dependence
- co-production
- Sommerfield enhancement
- ...

## SUPERSYMMETRIC RELICS FROM THE BIG BANG\*

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(Revised 15 December 1983)

We consider the cosmological constraints on supersymmetric theories with a new, stable particle. Circumstantial evidence points to a neutral gauge/Higgs fermion as the best candidate for this particle, and we derive bounds on the parameters in the lagrangian which govern its mass and couplings. One favored possibility is that the lightest neutral supersymmetric particle is predomi-

# SUSY WIMPs

Favorite cold thermal relic: the neutralino

Neutralino:

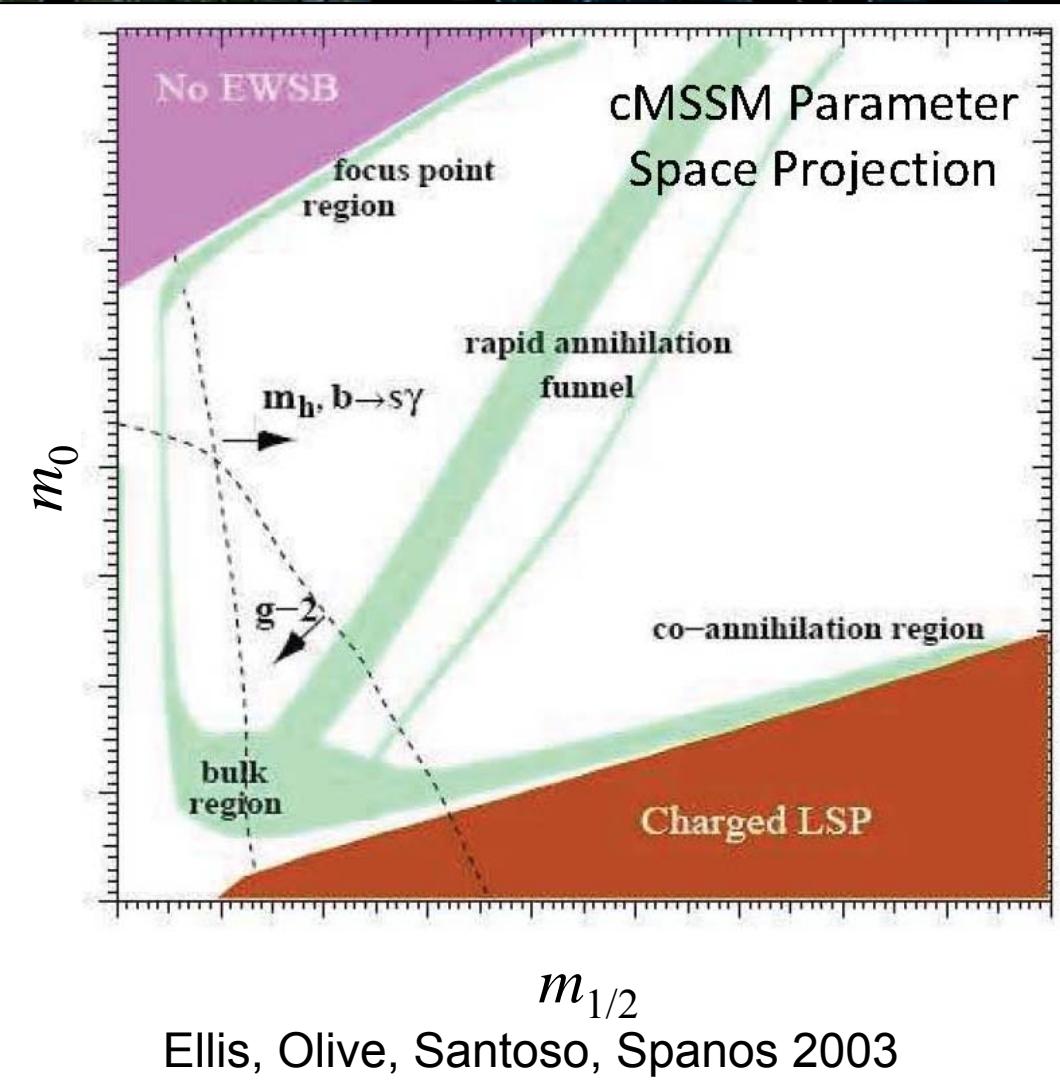
$$\tilde{\chi}^0 = \alpha \tilde{B} + \beta \tilde{W}^3 + \gamma \tilde{H}_1^0 + \delta \tilde{H}_2^0$$

$m_{\tilde{\chi}^0}$  and interactions:

100+ parameters of SUSY

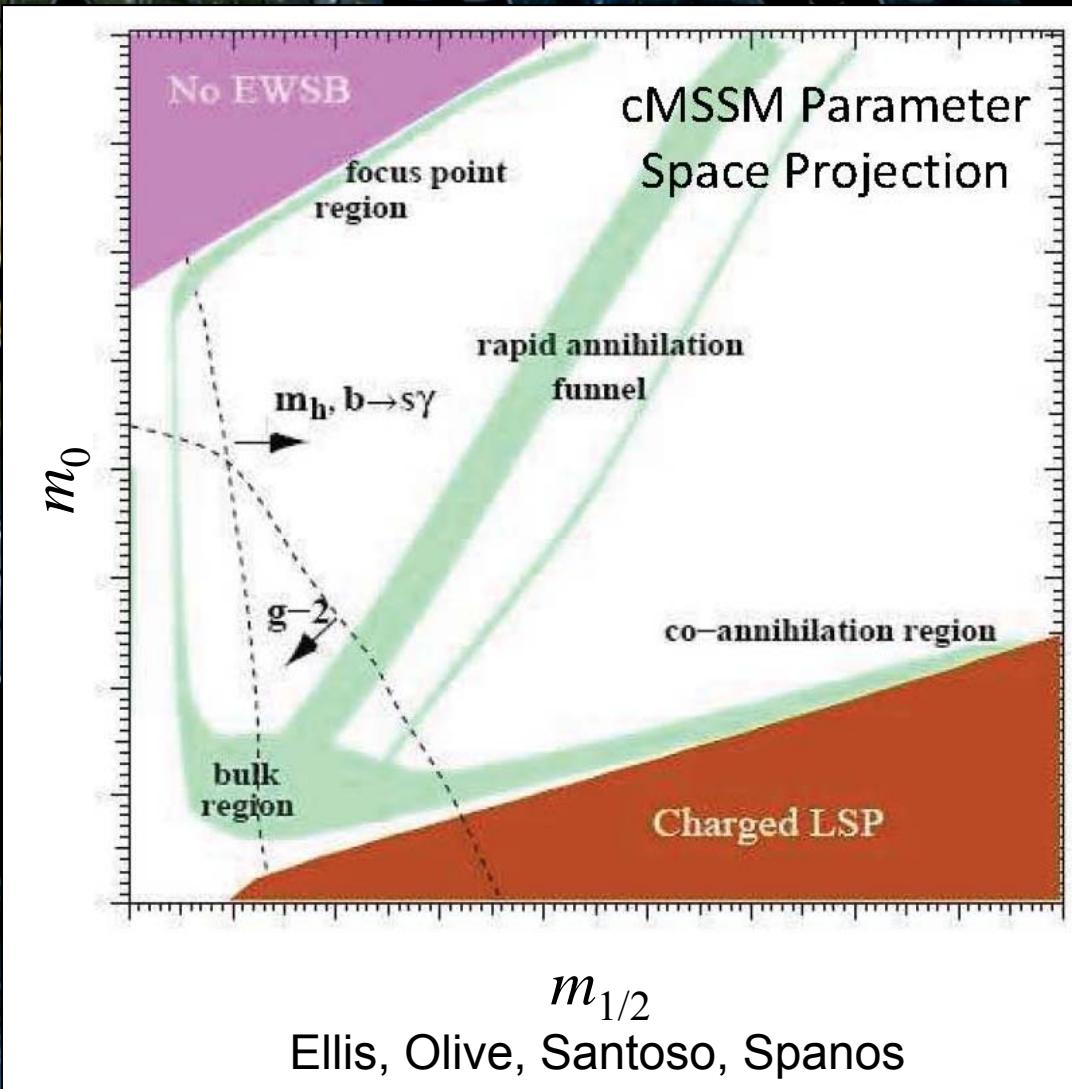
cMSSM

$m_0$ ,  $m_{1/2}$ ,  $\tan\beta$ ,  $A_0$ , sign  $\mu$



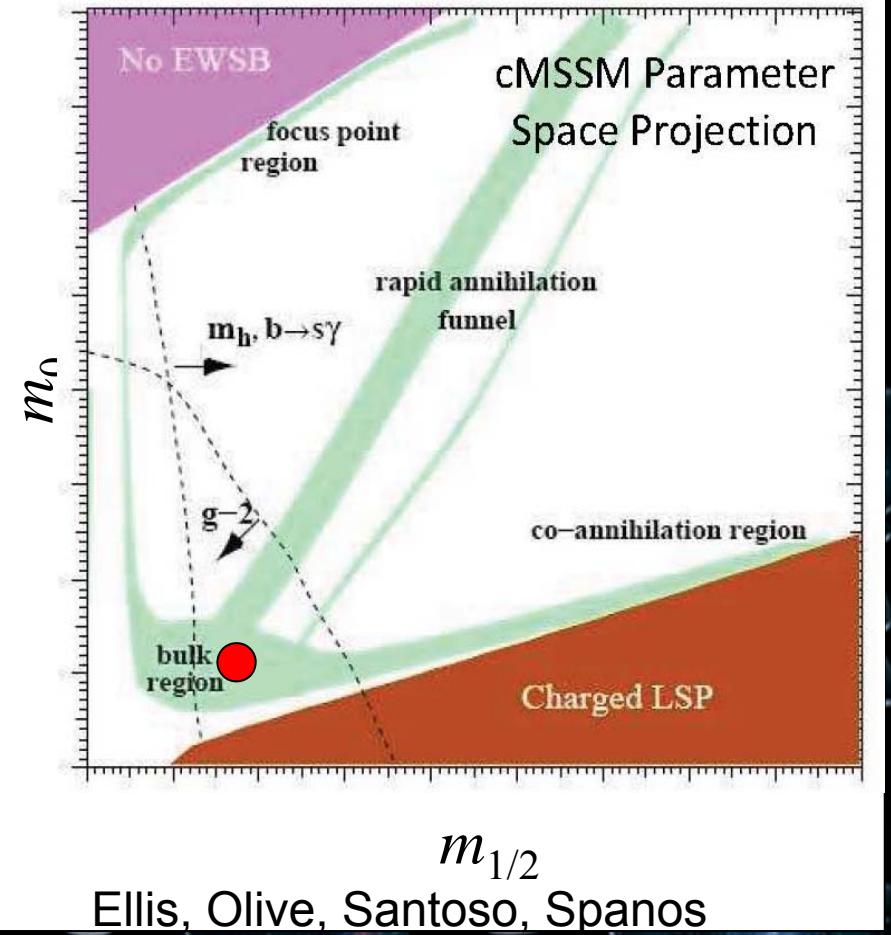
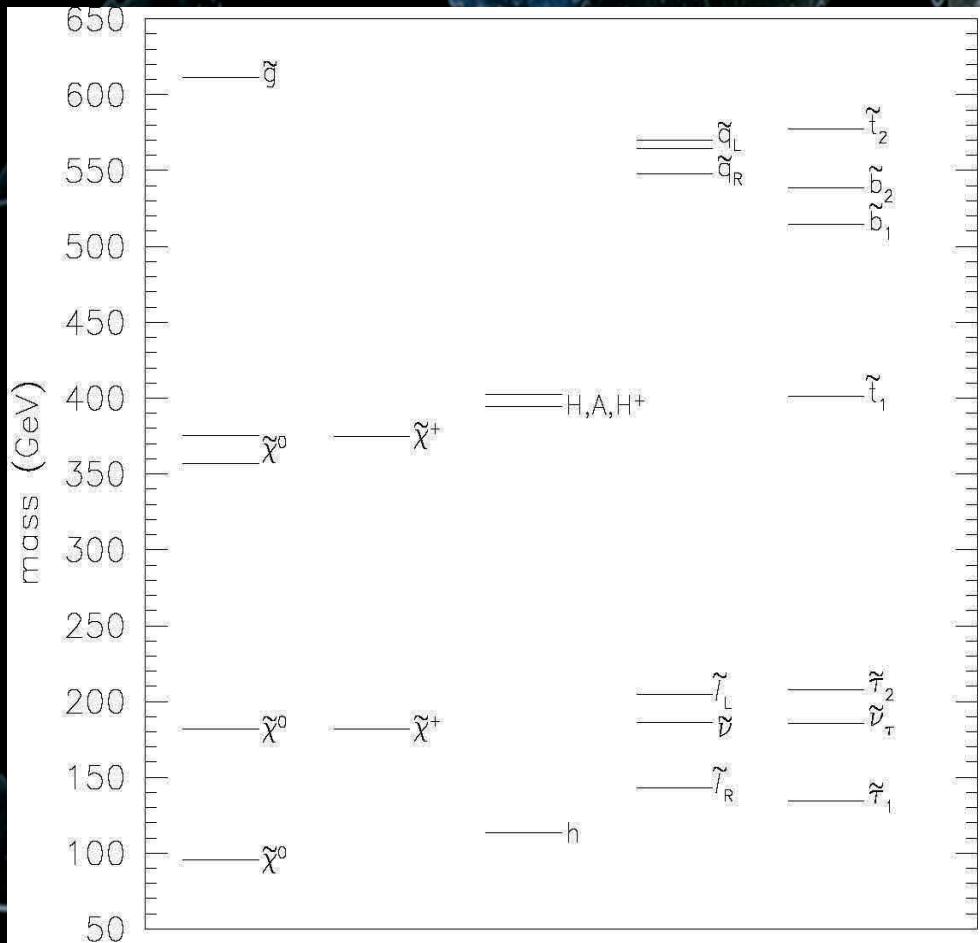
# SUSY WIMPs

- Typical SUSY models consistent w/ collider and other HEP data have too small annihilation cross section → too large  $\Omega$
- Need chicanery to increase annihilation cross section
  - $s$ -channel resonance through light  $H$  and  $Z$  poles
  - co-annihilation with  $\tilde{\chi}$  or  $\tilde{t}$
  - large  $\tan\beta$  ( $s$ -channel annihilation via broad  $A$  resonance)
  - high values of  $m_0$ —LSP Higgsino-like & annihilates into  $W$  &  $Z$  pairs (focus point)
  - ...
  - or, unconstrained



# SUSY WIMPs

Bulk Region: light superpartners



Ellis, Olive, Santoso, Spanos

LHC chewing away at allowed region,  
but too early to throw in the towelino.

# Kaluza-Klein WIMPs

Kolb & Slansky (84); Servant & Tait (02); Cheng, Feng & Matchev (02)



## Quantized Kaluza-Klein excitations

$$\begin{aligned} E^2 &= \vec{p}^2 + p_5^2 & p_5^2 &= n^2/R^2 \\ &= \vec{p}^2 + M_n^2 & M_n^2 &= n^2/R^2 \end{aligned}$$

Conservation of momentum  $\longrightarrow$  conservation of KK mode number

First excited mode ( $n = 1$ ) stable, mass  $R^{-1}$

need  
chiral  
fermions

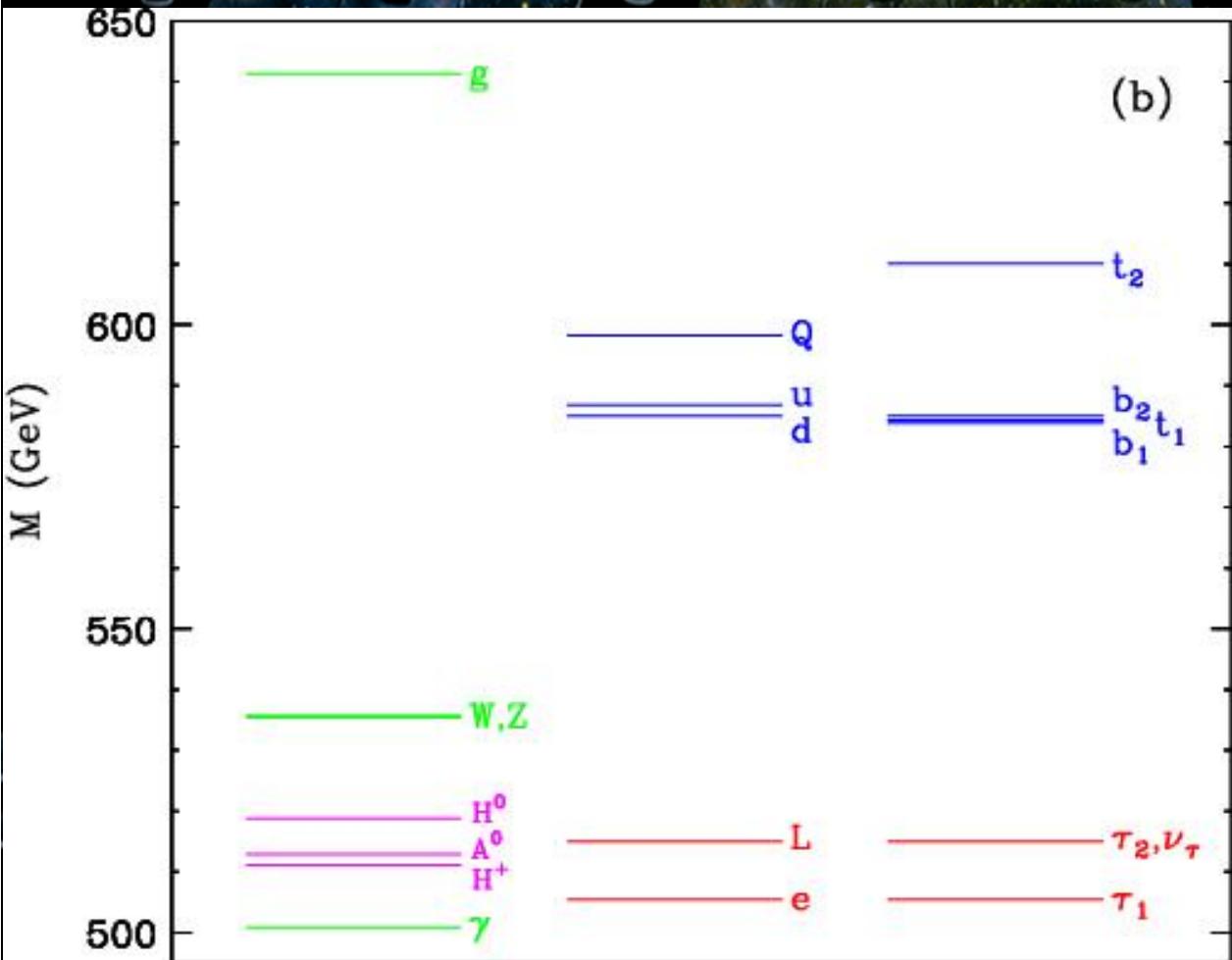


KK quantum number  $\longrightarrow$  KK parity

First excited mode ( $n = 1$ ) stable, mass  $R^{-1}$

# Kaluza-Klein WIMPs

$$R^{-1} = 500 \text{ GeV}$$



- LKP = KK photon  
Cheng, Matchev & Schmaltz
- Looks like SUSY  
Cheng, Matchev & Schmaltz
- Beware KK graviton  
Kolb, Servant & Tait
- Direct detection  
Servant & Tait  
Cheng, Feng & Matchev
- Indirect detection  
Bertrone, Servant, Sigl

LHC chewing away at allowed region