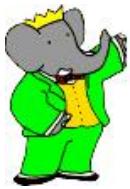




# Measuring $|V_{ub}|$ from Semileptonic B Decays

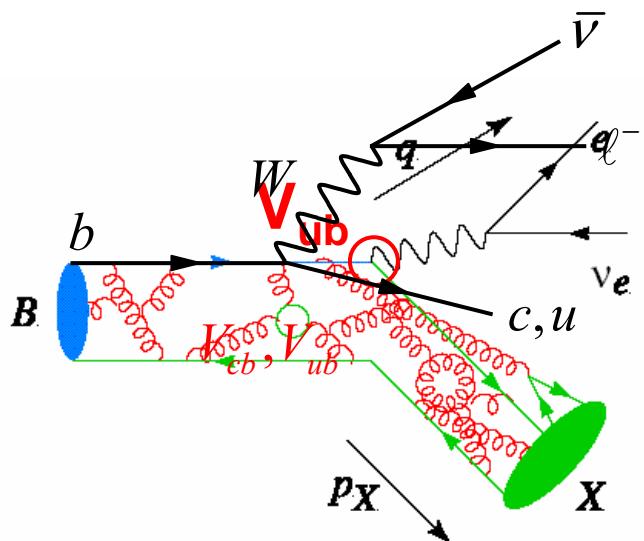
Wolfgang Menges  
Queen Mary, University of London, UK

Institute of Physics: Particle Physics 2006  
11<sup>th</sup> April 2006

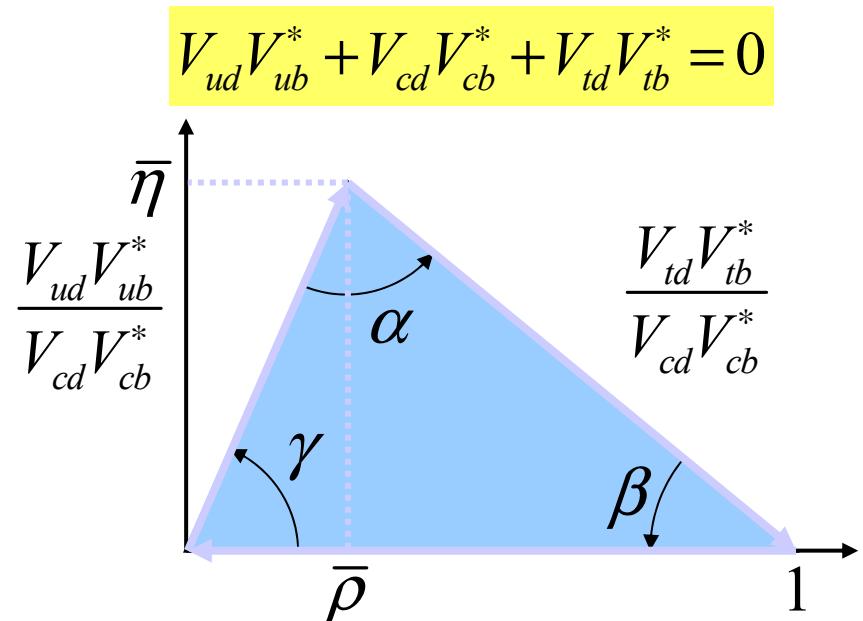


# Introduction

- CP violation is described by the CKM matrix in the SM
- the consistency of the Unitarity Triangle is tested by measuring its angles and sides
- one side is related to  $|V_{ub}|$
- $|V_{ub}|$  can be measured in semileptonic, charmless B decays



$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



## Experimental challenge:

- suppress continuum background
- suppress charm decay

## Theoretical challenge:

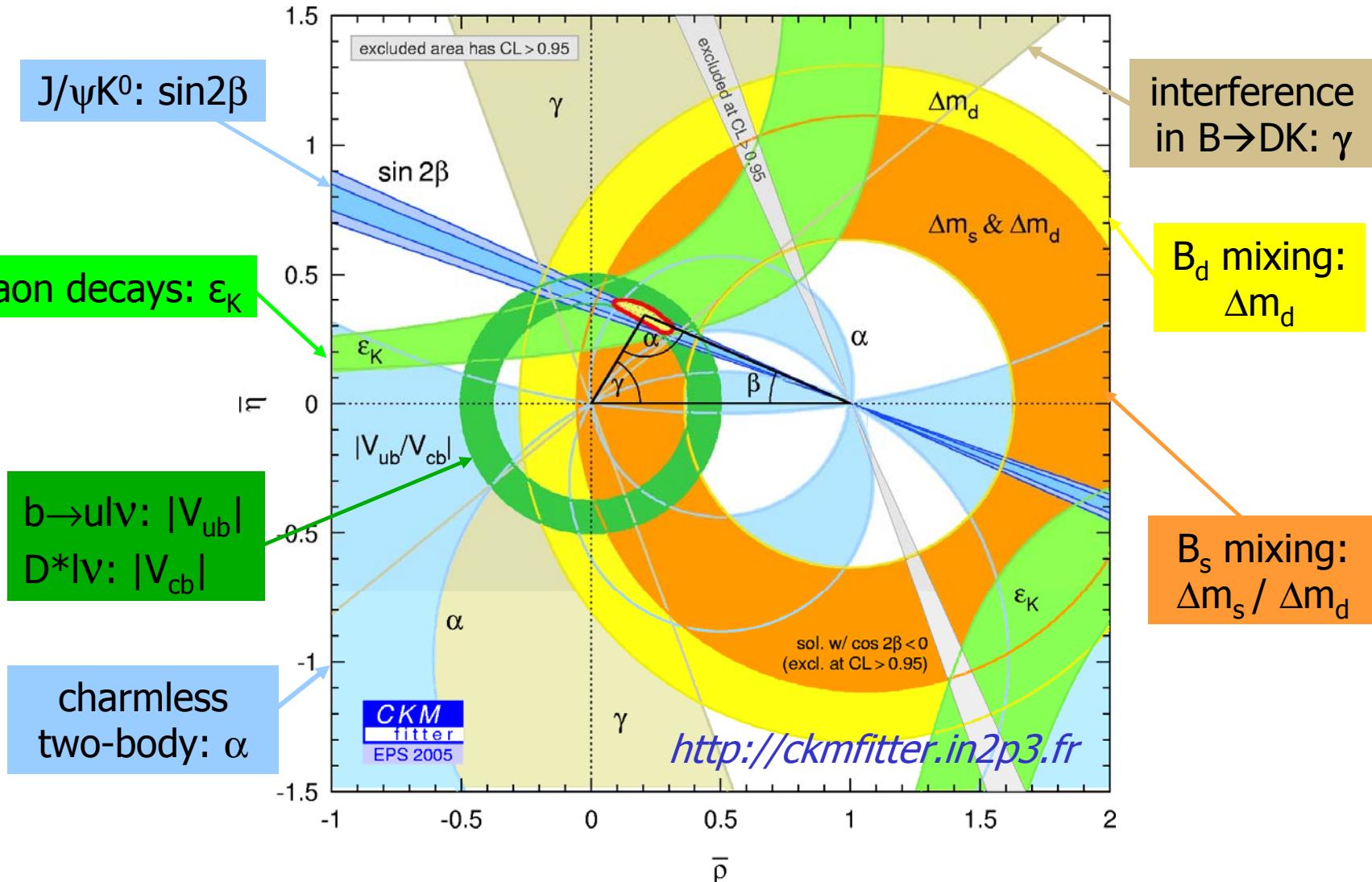
- extrapolate from partial to total BF



# Unitarity Triangle Fits

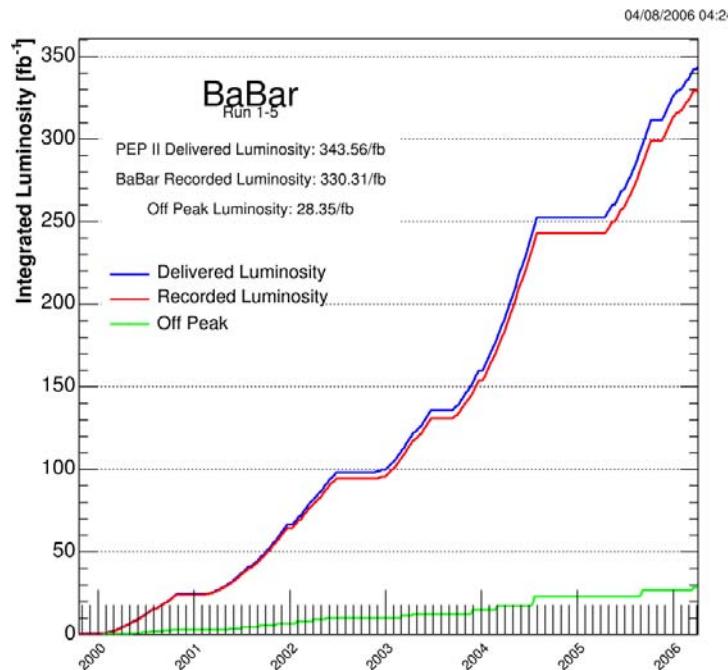
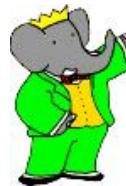


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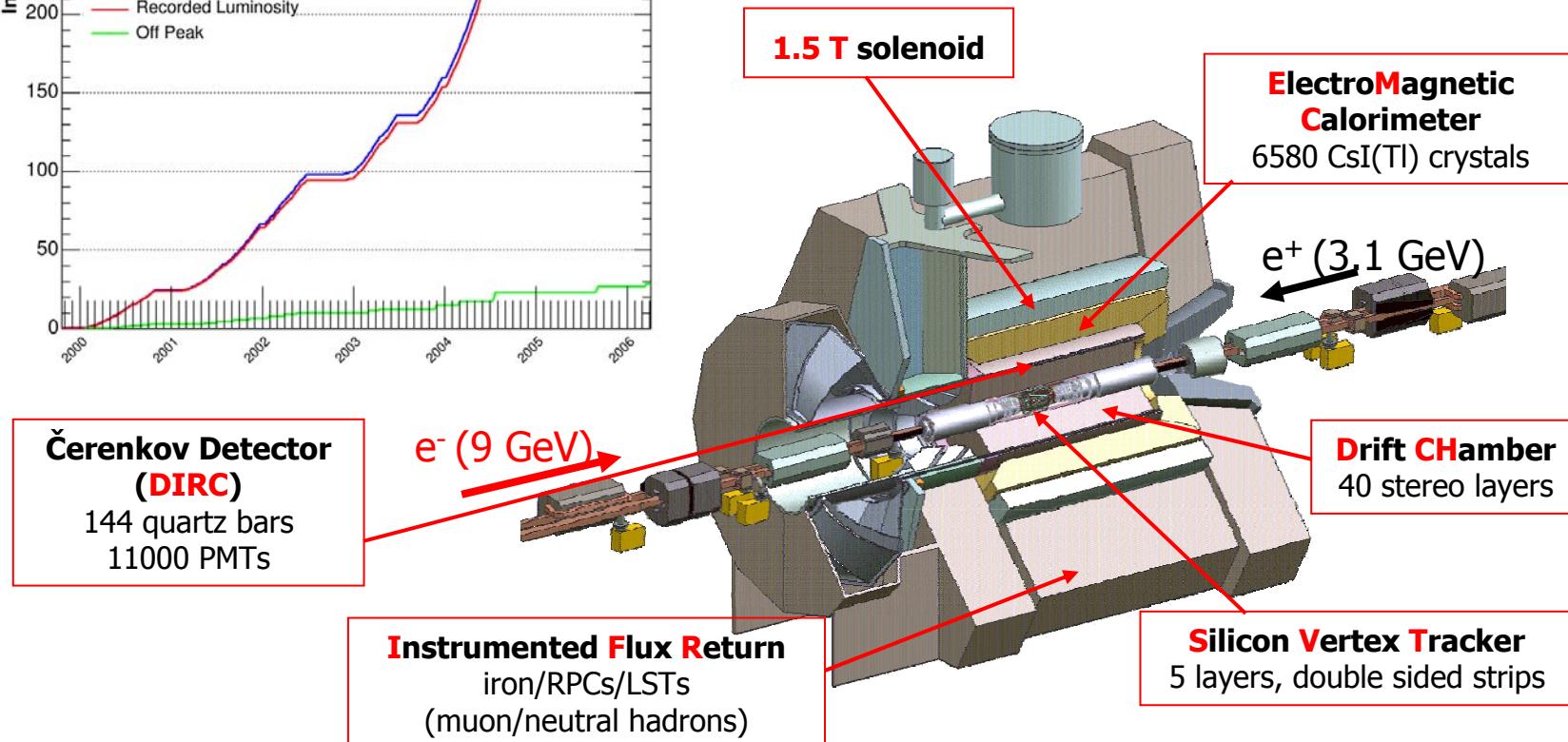




# PEP2 and BaBar Detector

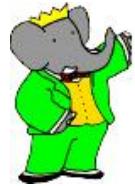


Collected luminosity:  $\sim 330 \text{ fb}^{-1}$   
Analysed Luminosity:  $80/210 \text{ fb}^{-1}$

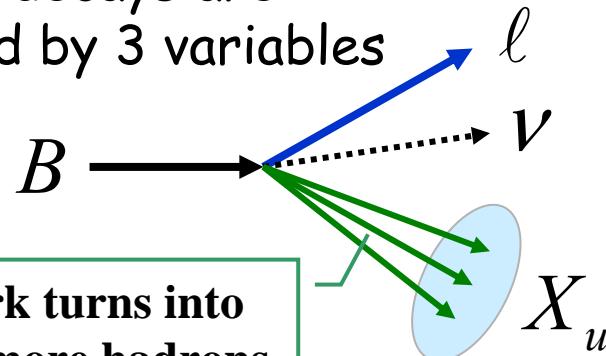




# Inclusive $b \rightarrow ul\nu$ : Strategies



- $B \rightarrow X_u/\nu$  decays are described by 3 variables



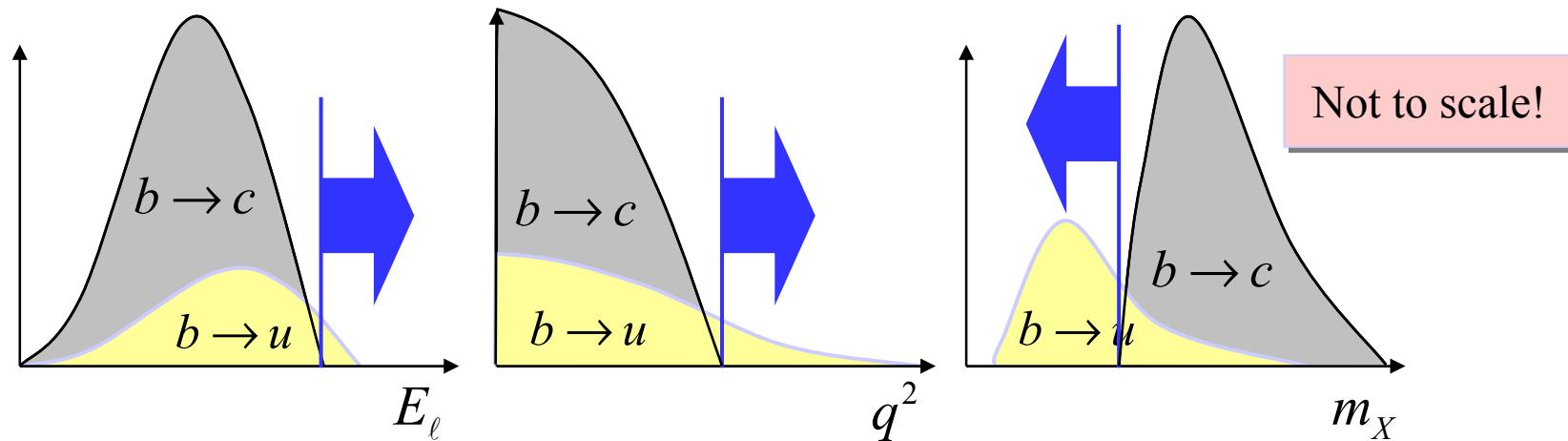
$E_l$  = lepton energy

$q^2$  = lepton-neutrino mass squared

$m_X$  = hadron system mass

- Signal events have smaller  $m_X$   
 $\rightarrow$  larger  $E_l$  and  $q^2$

$$\frac{\Gamma(b \rightarrow u\ell\bar{\nu})}{\Gamma(b \rightarrow c\ell\bar{\nu})} \approx \frac{|V_{ub}|^2}{|V_{cb}|^2} \approx \frac{1}{50}$$





# Lepton Endpoint



BABAR PRD73:012006,2006

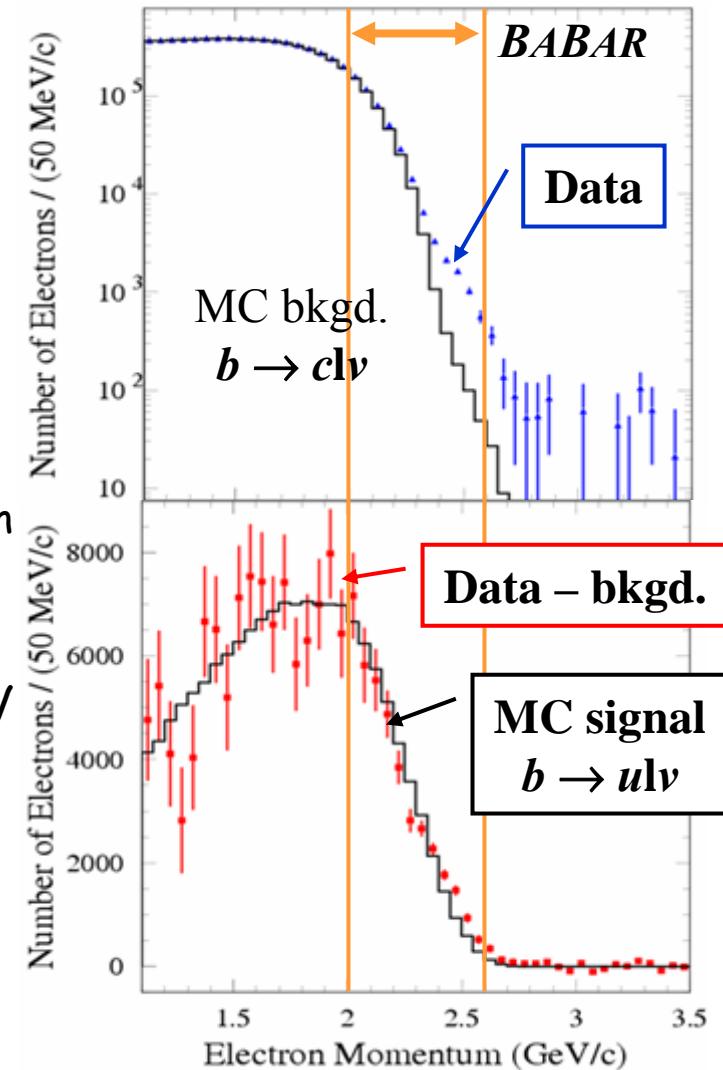
Select electrons with  $2.0 < E_e < 2.6 \text{ GeV}$

- Push below the charm threshold
  - Larger signal acceptance
  - Smaller theoretical error
- Accurate subtraction of background is crucial!
  - off-resonance data
  - events with  $p_e > 2.8 \text{ GeV}$
  - fit  $b \rightarrow cl\nu$  composition in bkg subtraction
- Measure the partial BF
- S/B = 1/15 for the endpoint  $E_e > 2.0 \text{ GeV}$

$$\Delta B (10^{-4}) = 5.72 \pm 0.41_{\text{stat}} \pm 0.65_{\text{sys}}$$

Luminosity:  $80 \text{ fb}^{-1}$

total BF is  $\sim 2 \times 10^{-3}$



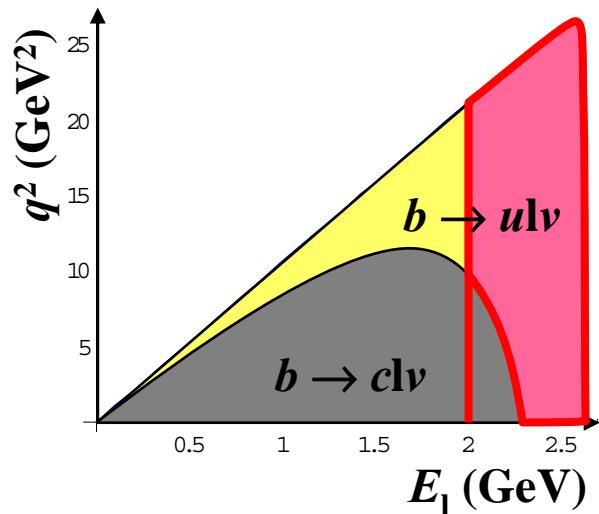


# $E_l$ and $q^2$



BABAR PRL 95:111801

- Try to improve signal-to-background
- Use  $p_\nu = p_{\text{miss}}$  in addition to  $p_e \rightarrow$  calculate  $q^2$



- Define  $s_h^{\max}(E_l, q^2)$  = the maximum  $m_X$  squared
  - Cutting at  $s_h^{\max} < m_D^2$  removes  $b \rightarrow c/\bar{\nu}$  while keeping most of the signal
- $S/B = 1/2$  achieved for  $E_l > 2.0$  GeV and  $s_h^{\max} < 3.5$   $\text{GeV}^2$

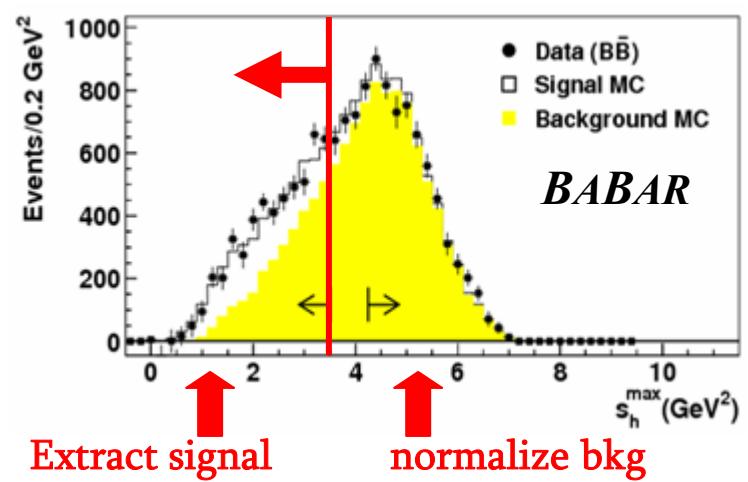
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Measured partial BF:

$$\Delta B (10^{-4}) 3.54 \pm 0.33 \text{stat} \pm 0.34_{\text{sys}}$$

Luminosity:  $80 \text{ fb}^{-1}$

Smaller systematic errors



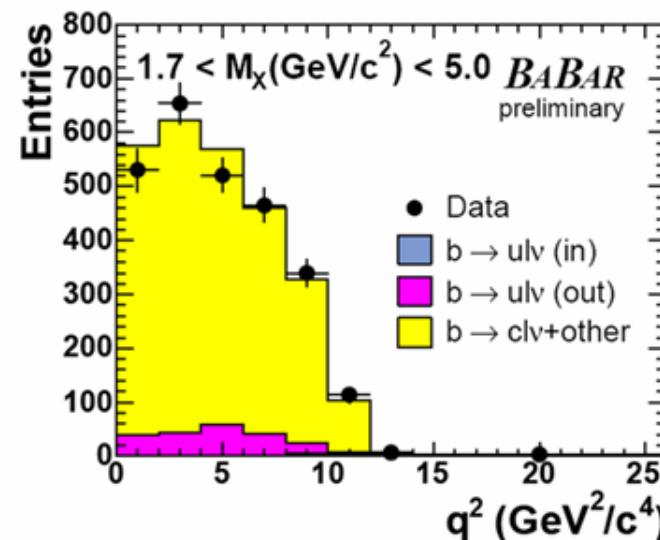
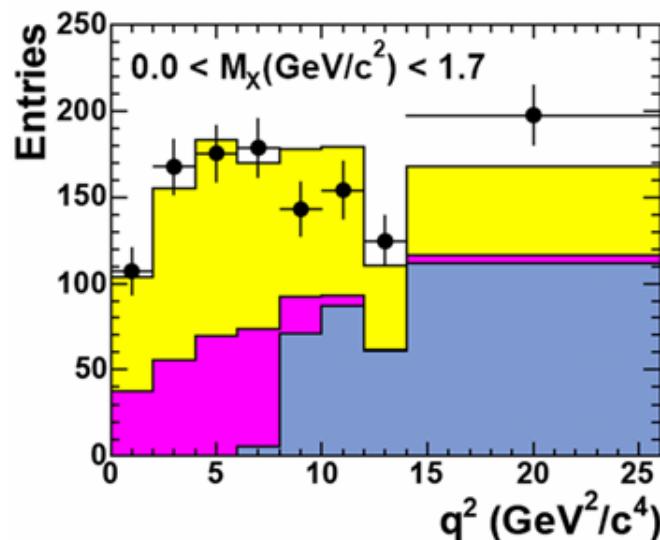
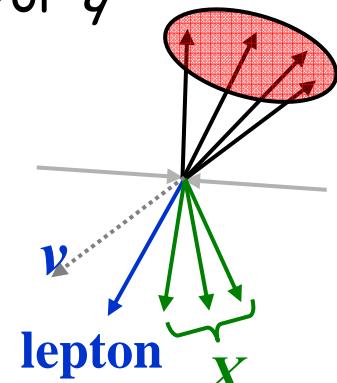


# $m_X$ and $q^2$



BABAR hep-ex/0507017

- Must **reconstruct all decay products** to measure  $m_X$  or  $q^2$ 
  - Use (fully-reconstructed) hadronic B tag
- Suppress  $b \rightarrow c l \nu$  by vetoing against  $D^{(*)}$  decays
  - Reject events with  $K$
  - Reject events with  $B^0 \rightarrow D^{*+} (\rightarrow D^0 \pi^+) l \nu$
- Measure the partial BF in regions of  $(m_X, q^2)$ 
  - $m_X < 1.7 \text{ GeV}$  and  $q^2 > 8 \text{ GeV}^2$ :  
 $\Delta B (10^{-4}) = 8.7 \pm 0.9_{\text{stat}} \pm 0.9_{\text{sys}}$       Luminosity:  $211 \text{ fb}^{-1}$





# $|V_{ub}|$ from Branching Fraction



For converting a branching fraction into  $|V_{ub}|$  the phase space acceptance is needed:

$$|V_{ub}| = \sqrt{\frac{\Delta B(B \rightarrow X_u \ell \nu)}{\Delta \zeta \cdot \tau_B}}$$

Results of different calculations/HQE parameters using the same partial branching fraction:

Example for  $m_x/q^2$

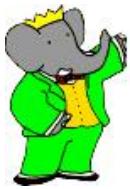
$$1) |V_{ub}| = (5.00 \pm 0.37_{\text{exp}} \pm 0.46_{\text{SF}} \pm 0.28_{\text{theo}}) \times 10^{-3}$$

$$2) |V_{ub}| = (4.65 \pm 0.34_{\text{exp}} {}^{+0.46}_{-0.38_{\text{SF}}} \pm 0.23_{\text{theo}}) \times 10^{-3}$$

$$3) |V_{ub}| = (4.82 \pm 0.36_{\text{exp}} \pm 0.46_{\text{SF+theo}}) \times 10^{-3}$$

$$4) |V_{ub}| = (4.86 \pm 0.36_{\text{exp}} \pm 0.22_{\text{theo}}) \times 10^{-3}$$

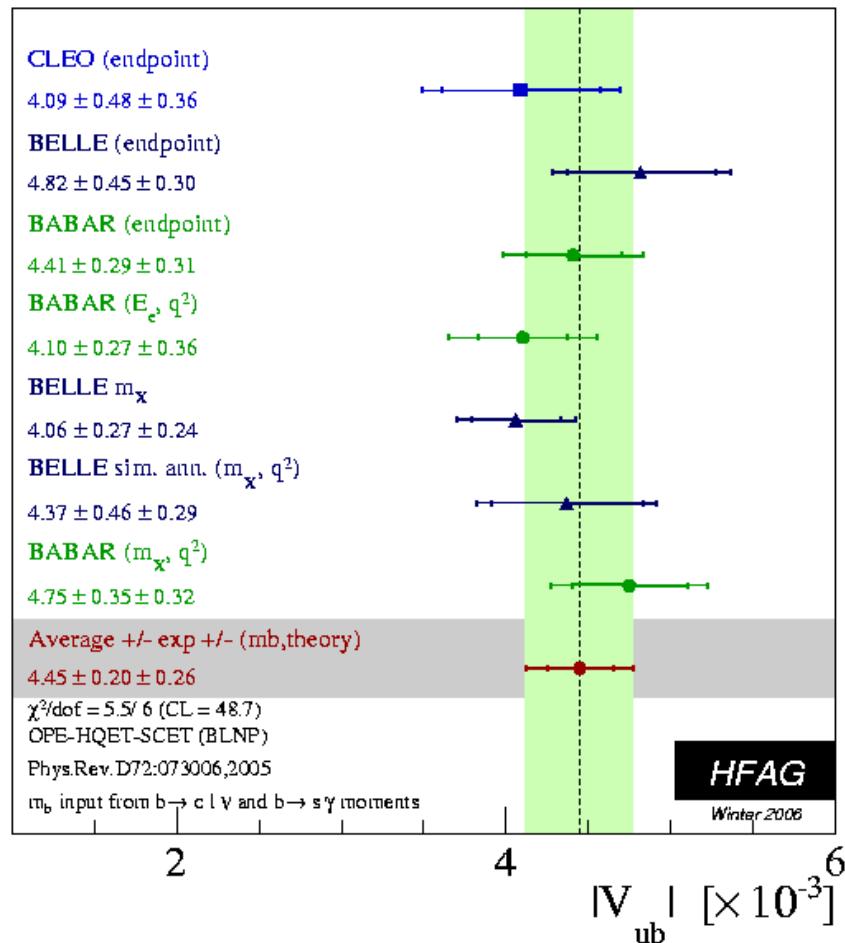
- 1) BLNP: BaBar  $B \rightarrow X_c \ell \nu$  moments  
 $m_b(\text{SF}) = 4.61 \pm 0.08 \text{ GeV}$   
 $\mu_\pi^2(\text{SF}) = 0.15 \pm 0.07 \text{ GeV}^2$
- 2) BLNP: Belle  $B \rightarrow X_s \gamma$  spectrum  
 $m_b(\text{SF}) = 4.52 \pm 0.07 \text{ GeV}$   
 $\mu_\pi^2(\text{SF}) = 0.27 \pm 0.23 \text{ GeV}^2$
- 3) BLL: BaBar  $B \rightarrow X_c \ell \nu$  moments  
 $m_b(1S) = 4.74 \pm 0.06 \text{ GeV}$
- 4) DGE: HFAG average  
 $m_b(\overline{\text{MS}}) = 4.20 \pm 0.04 \text{ GeV}$



# Status of Inclusive $|V_{ub}|$

$|V_{ub}|$  world average summer 2006

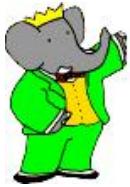
BLNP + SF from  $b \rightarrow c\bar{v}$ ,  $b \rightarrow s\gamma$



$|V_{ub}|$  determined to  $\pm 7.4\%$

Statistical	$\pm 2.2\%$
Expt. syst.	$\pm 2.7\%$
$b \rightarrow c\bar{v}$ model	$\pm 1.9\%$
$b \rightarrow u\bar{v}$ model	$\pm 2.1\%$
SF params. ( $m_b, \mu_\pi^2$ )	$\pm 4.1\%$
Theory	$\pm 4.2\%$

- The SF parameters can be improved with  $b \rightarrow s\gamma$ ,  $b \rightarrow c\bar{v}$  measurements
- What's in the theory error? Subleading SF and Weak Annihilation effects.



# Exclusive $b \rightarrow ul\nu$

- Measure specific final states, e.g.,  $B \rightarrow \pi l \nu$ 
  - Can achieve good signal-to-background ratio
  - Branching fractions are  $O(10^{-4}) \rightarrow$  statistics limited
- Need form factors to extract  $|V_{ub}|$ 

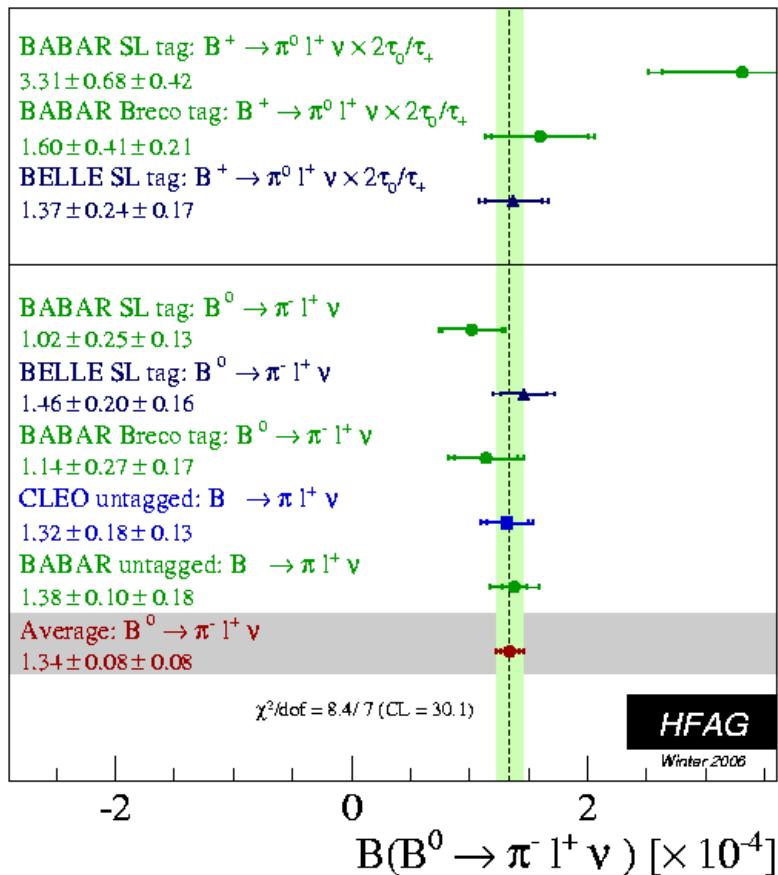
$$\frac{d\Gamma(B \rightarrow \pi l \nu)}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{ub}|^2 p_\pi^3 |f_+(q^2)|^2$$

One FF for  $B \rightarrow \pi l \nu$   
(massless lepton)

  - Theo. Uncertainties complementary to inclusive approach!
- $f_+(q^2)$  calculations exist based on:
  - Lattice QCD ( $q^2 > 15 \text{ GeV}^2$ )
    - “quenched” calculations  $\rightarrow 15\%$  uncertainty
    - new unquenched calculations (hep-lat/0409116, 0408019)
  - Light Cone Sum Rules ( $q^2 < 14 \text{ GeV}^2$ )  $\rightarrow 10\%$  uncertainty
  - Quark models (ISGW2) ... and other approaches

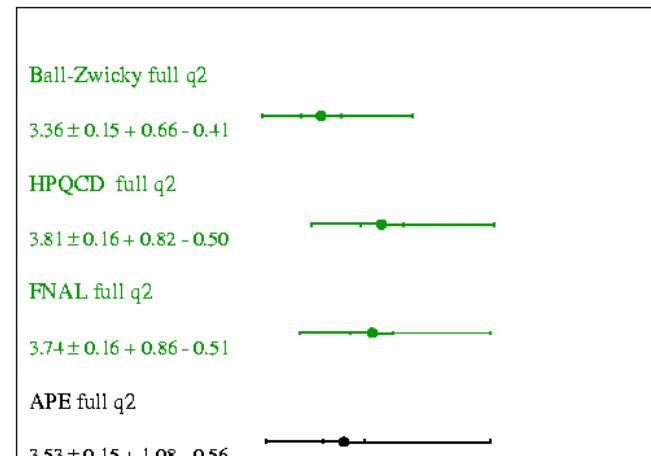


# Status of Exclusive $|V_{ub}|$

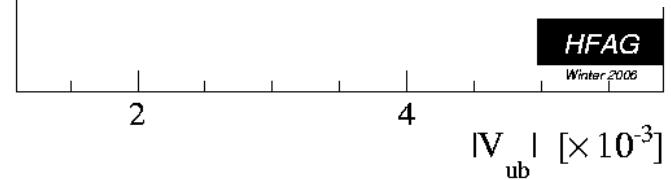


incl.  $|V_{ub}| [10^{-3}] = 4.45 \pm 0.20 \pm 0.26$   
 (BLNP)

- use BF and FF predictions to calculate  $|V_{ub}|$
- needs also assumption of shape of full  $q^2$  range



All calculations consistent!





# The Unitarity Triangle: 2004 → 2006



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- Precise determination of  $|V_{ub}|$  complements  $\sin 2\beta$  to test the validity of the Standard Model
  - 7.4% accuracy achieved so far → 5% possible?

