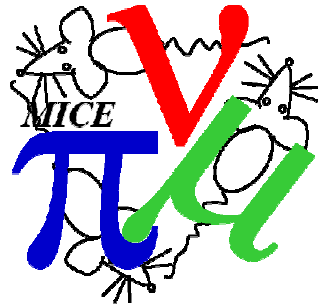
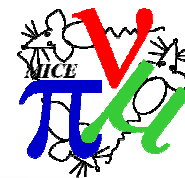


Measurement of Muon Cooling for a Future Neutrino Factory

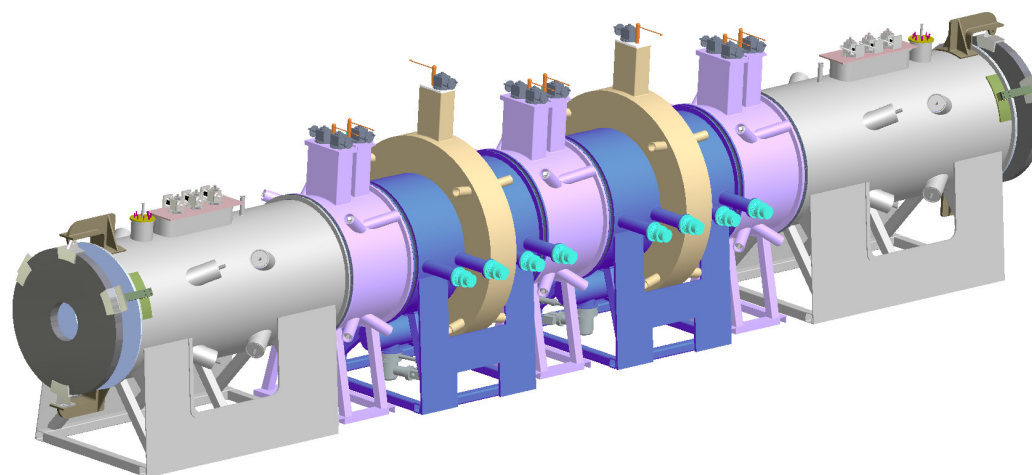


Chris Rogers,
Imperial College London,
on behalf of the MICE Collaboration

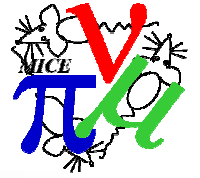
Overview



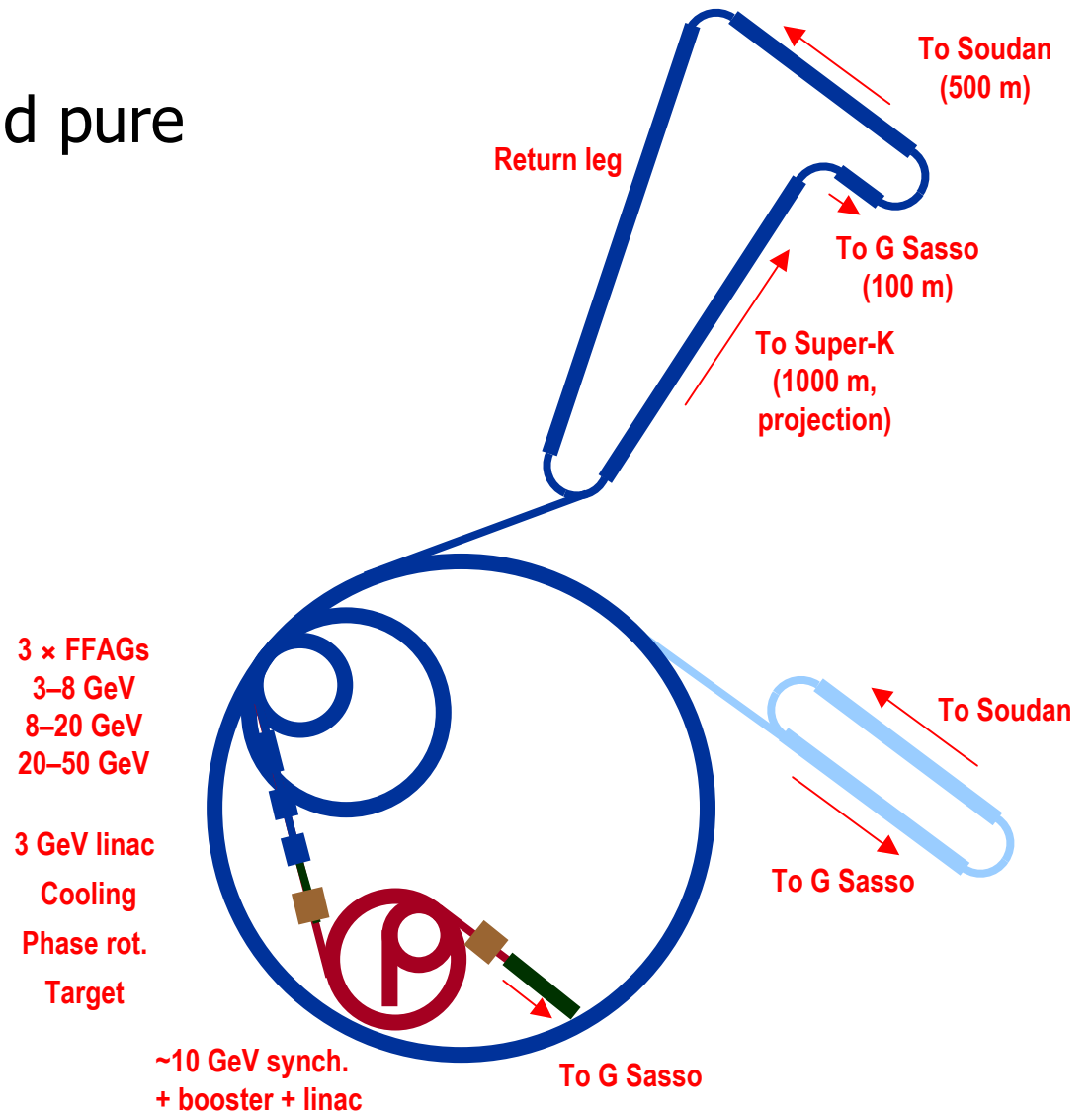
- MICE and muon cooling
- Accelerator simulation
 - Solenoids
 - Liquid Hydrogen
 - RF Cavities
- Simulated transverse emittance resolution



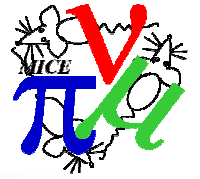
Neutrino Factory



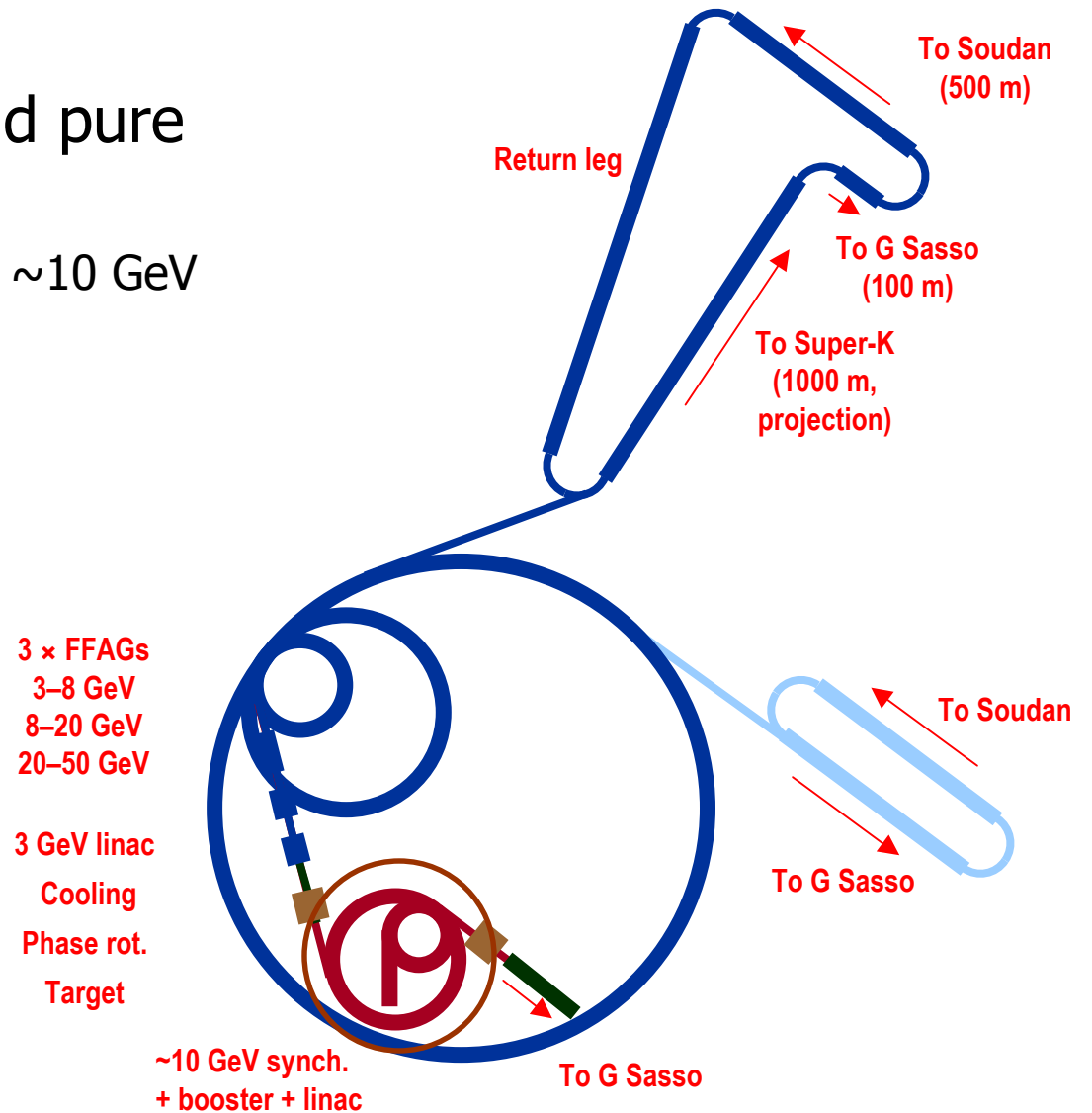
- Intense, high energy and pure source of neutrinos



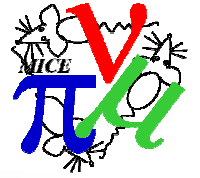
Neutrino Factory



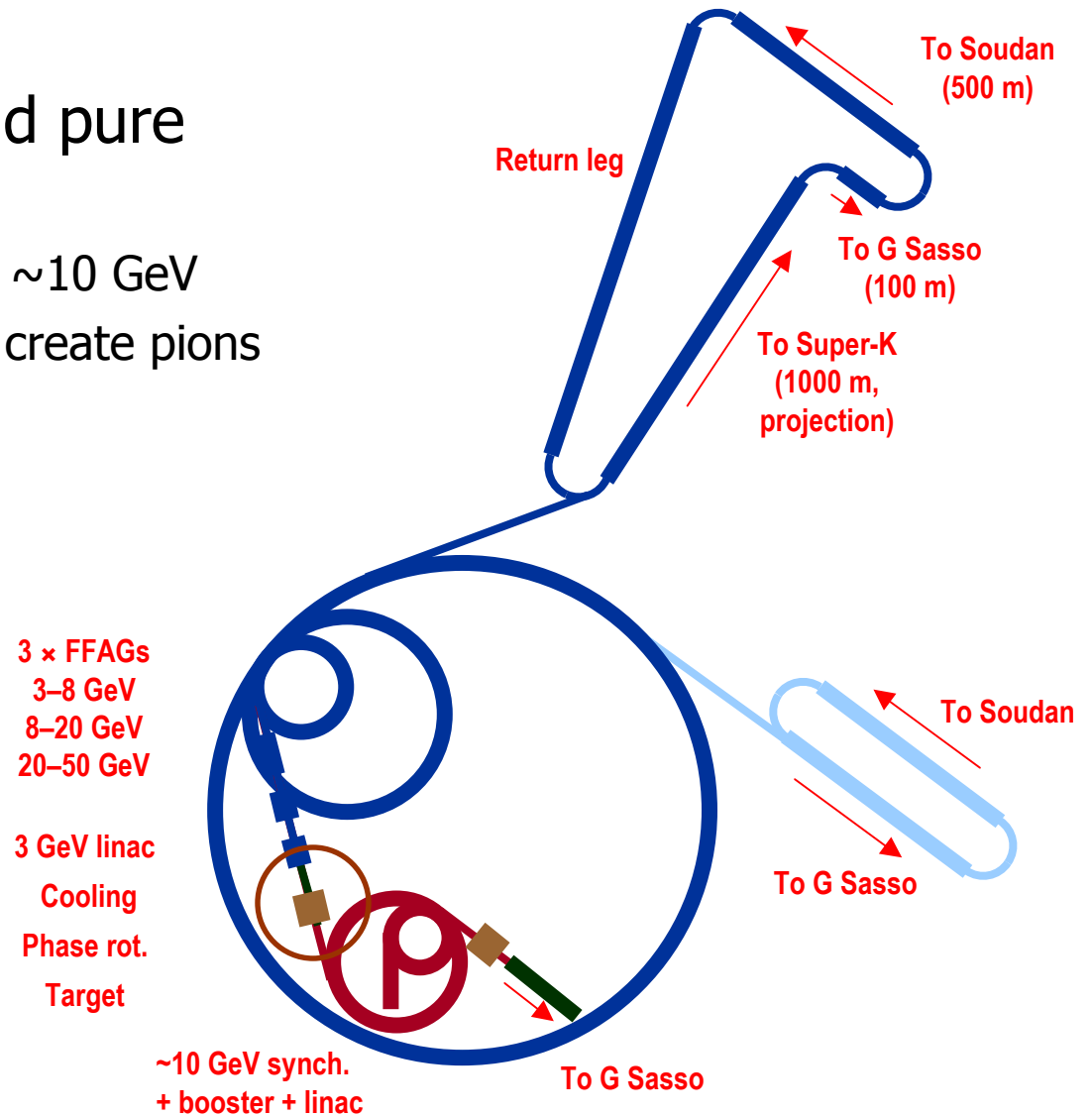
- Intense, high energy and pure source of neutrinos
 - Proton beam accelerated to ~ 10 GeV



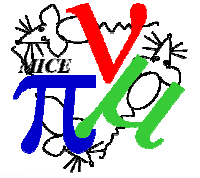
Neutrino Factory



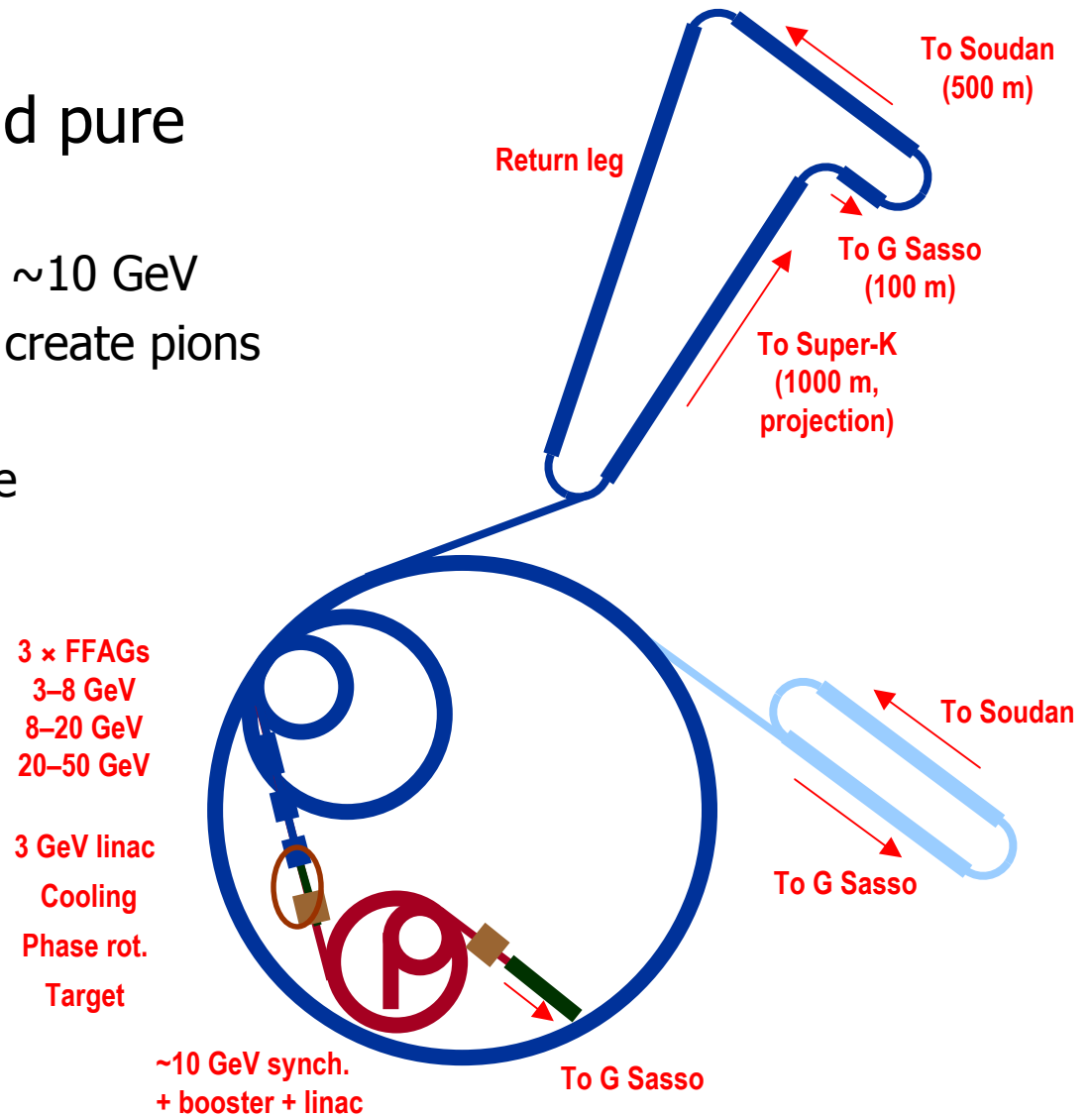
- Intense, high energy and pure source of neutrinos
 - Proton beam accelerated to ~ 10 GeV
 - Protons fired onto target to create pions



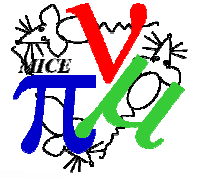
Neutrino Factory



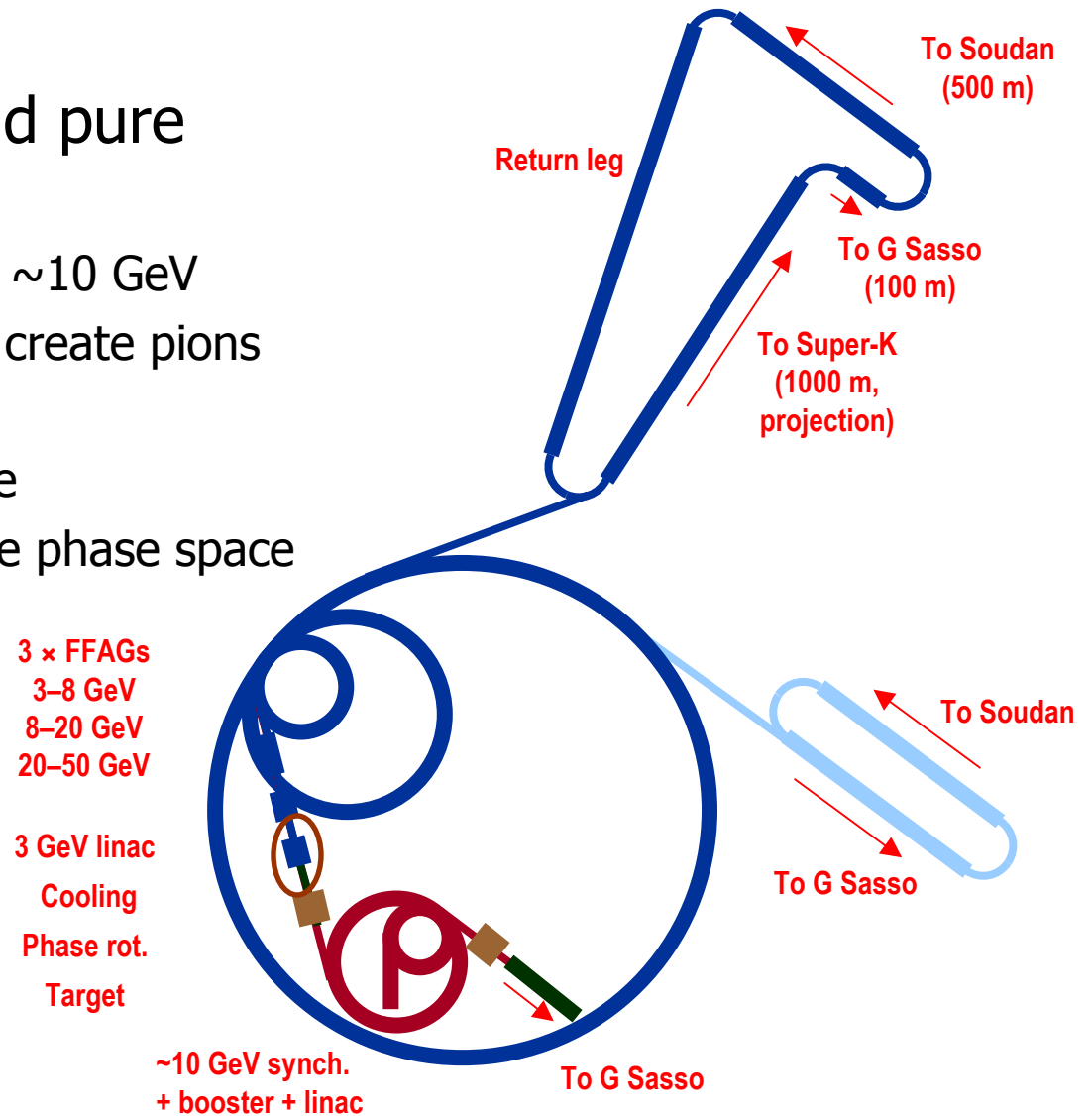
- Intense, high energy and pure source of neutrinos
 - Proton beam accelerated to ~ 10 GeV
 - Protons fired onto target to create pions
 - Pions decay to muons
 - Muon beam is very large



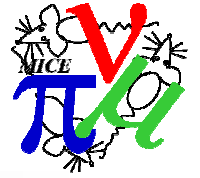
Neutrino Factory



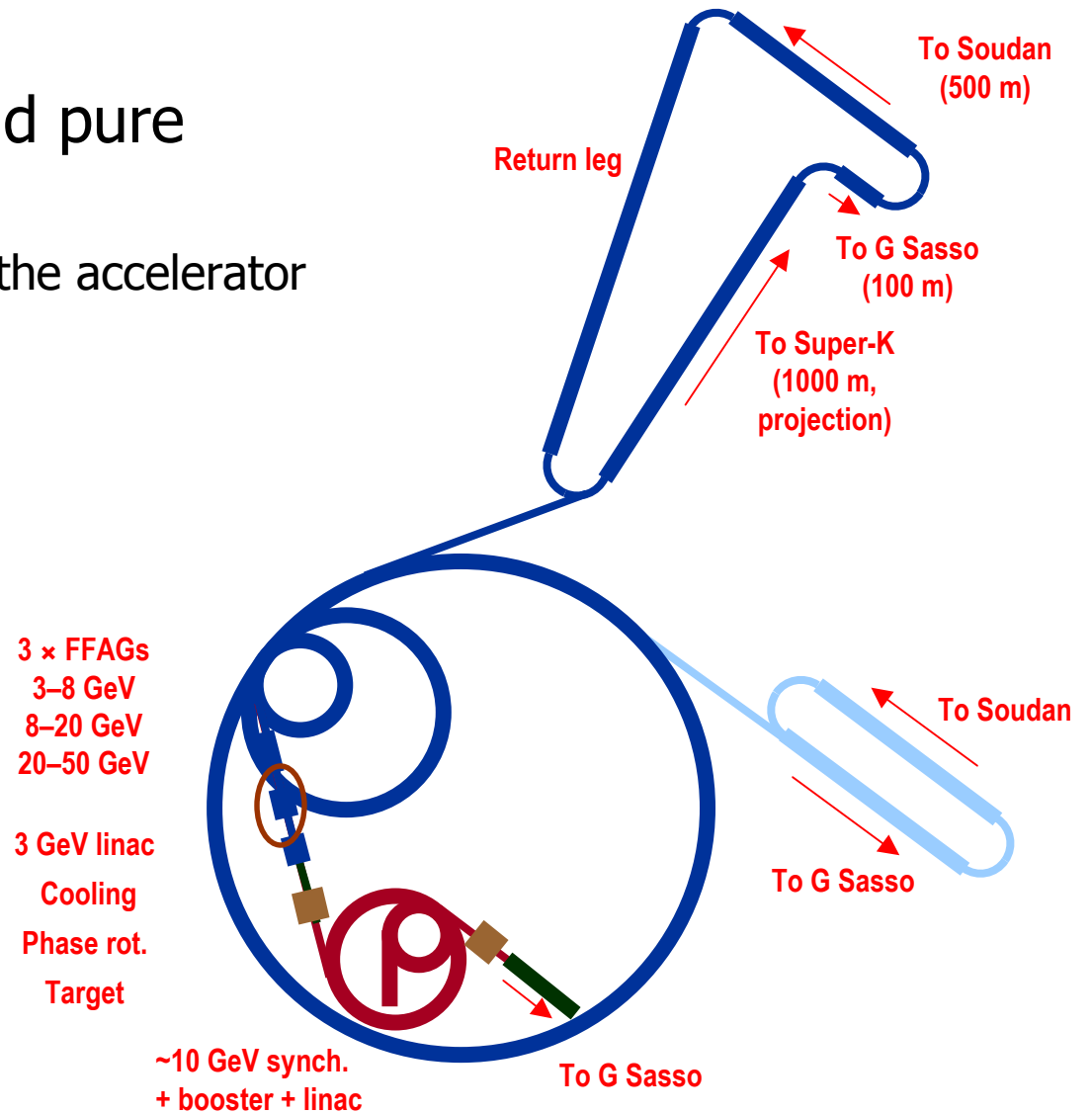
- Intense, high energy and pure source of neutrinos
 - Proton beam accelerated to ~ 10 GeV
 - Protons fired onto target to create pions
 - Pions decay to muons
 - Muon beam is very large
 - Beam rotated in energy-time phase space to fit into cooling section



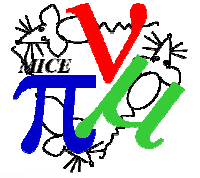
Neutrino Factory



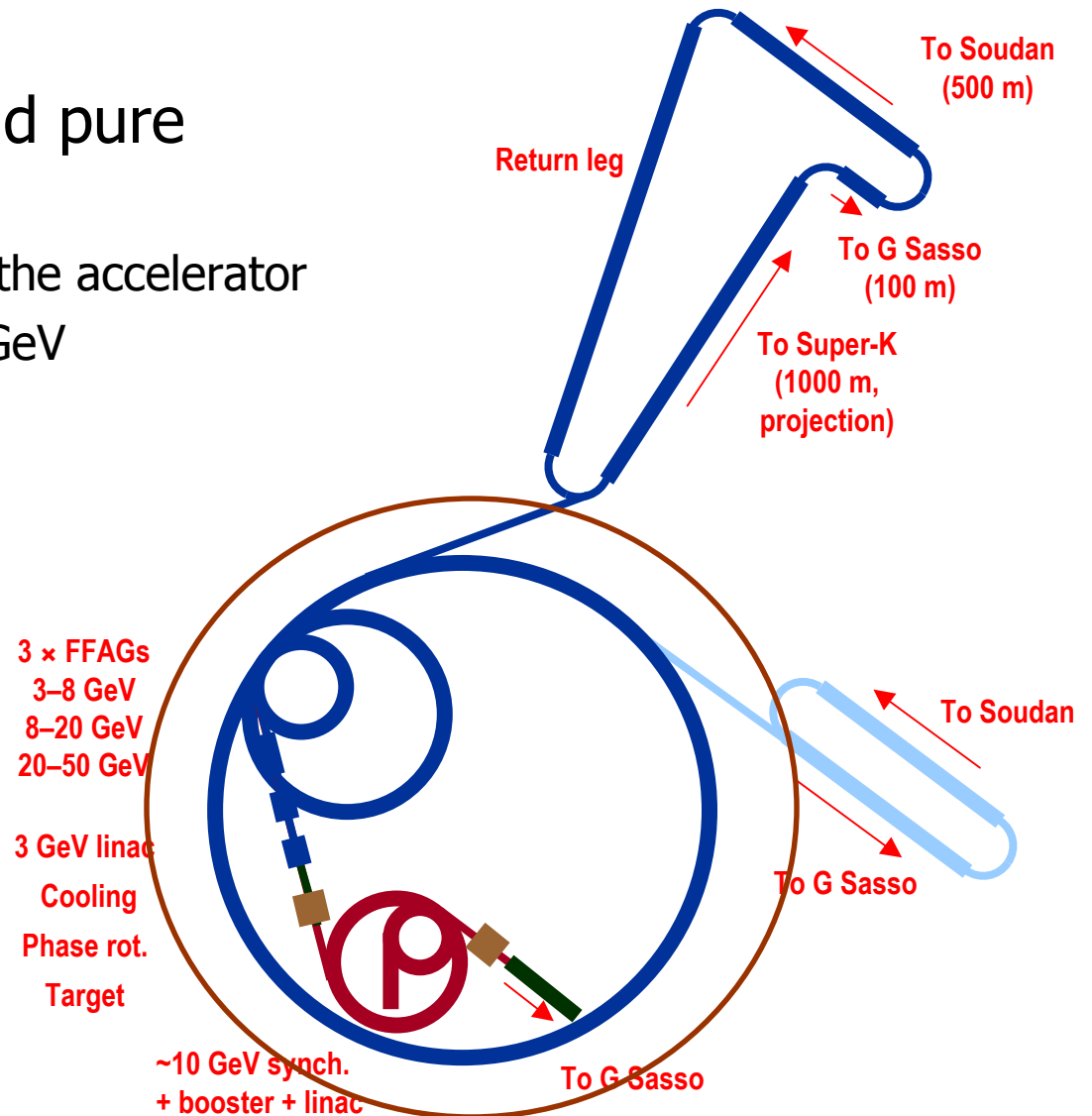
- Intense, high energy and pure source of neutrinos
 - Muon beam cooled to fit in the accelerator



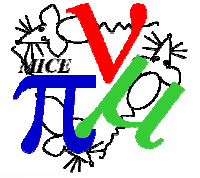
Neutrino Factory



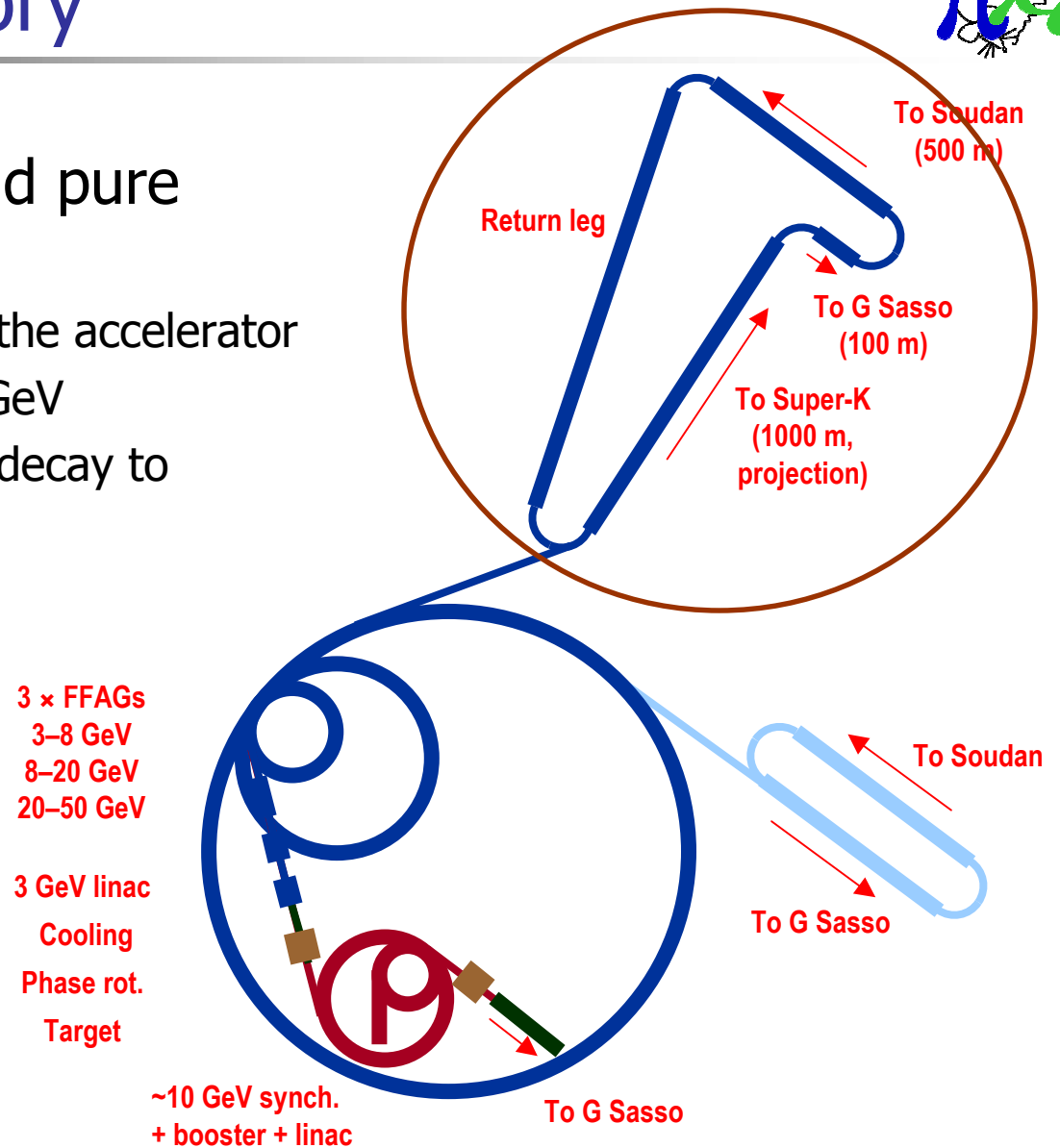
- Intense, high energy and pure source of neutrinos
 - Muon beam cooled to fit in the accelerator
 - Muons accelerated to ~ 50 GeV



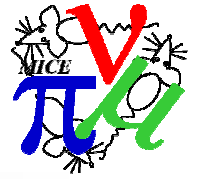
Neutrino Factory



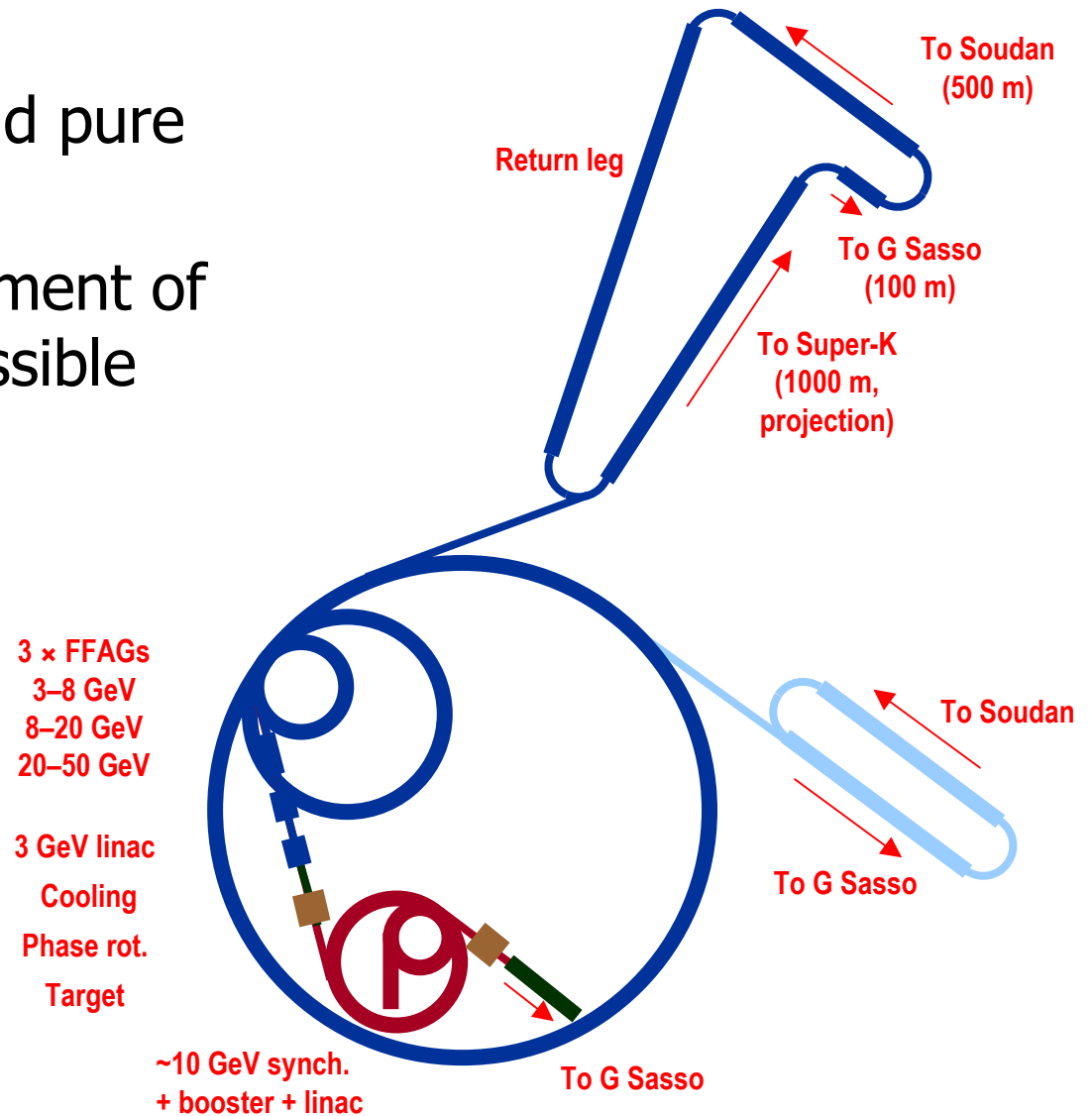
- Intense, high energy and pure source of neutrinos
 - Muon beam cooled to fit in the accelerator
 - Muons accelerated to ~ 50 GeV
 - Muons stored in a ring and decay to neutrinos in long straights



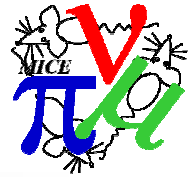
Neutrino Factory



- Intense, high energy and pure source of neutrinos
- High precision measurement of neutrino mixing and possible leptonic CP violation

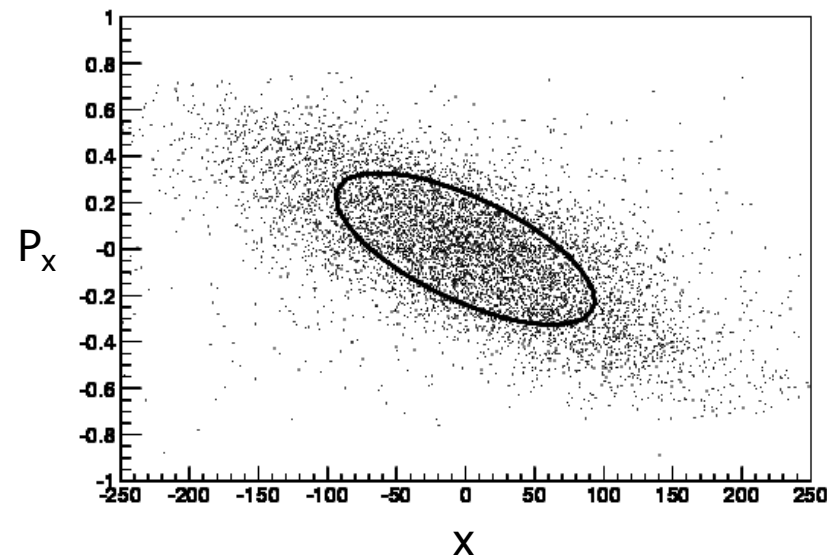


Beam Emittance



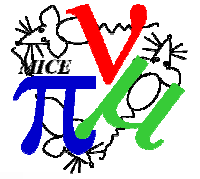
- Define “beam size” in a $2N$ dimensional phase space by quantity called beam emittance, ϵ_n
 - Volume of an ellipse aligned with beam at 1 rms

$$\epsilon_n = \frac{2^N \sqrt{|\mathbf{V}|}}{m}$$

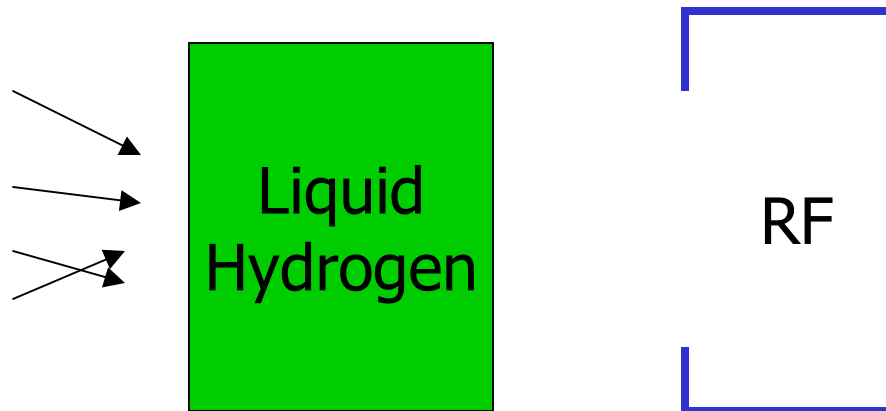


- Where \mathbf{V} is the covariance matrix of canonical phase space coordinates e.g. x, y, p_x, p_y

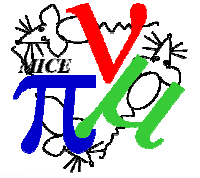
Muon Cooling



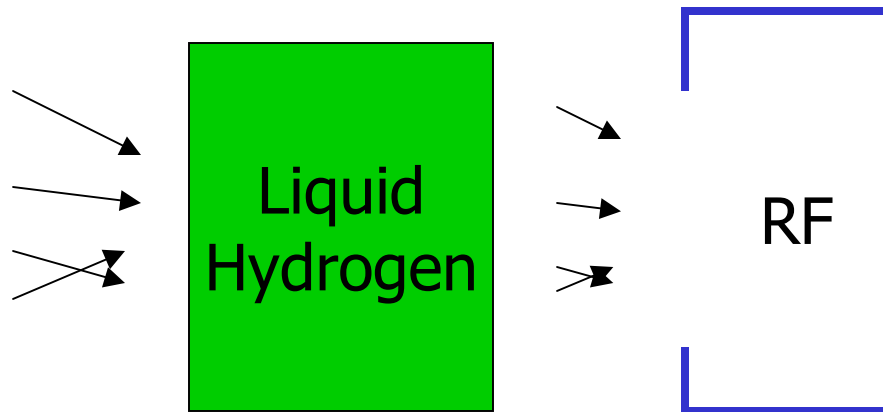
- Muon cooling increases beam phase space density using material placed across the beamline



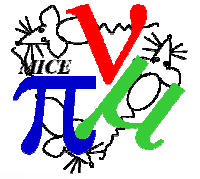
Muon Cooling



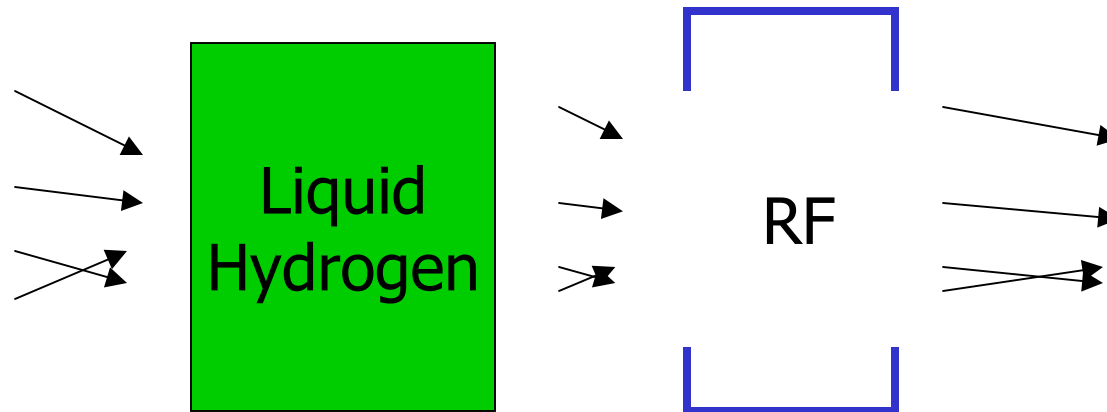
- Muon cooling increases beam phase space density using material placed across the beamline



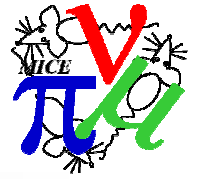
Muon Cooling



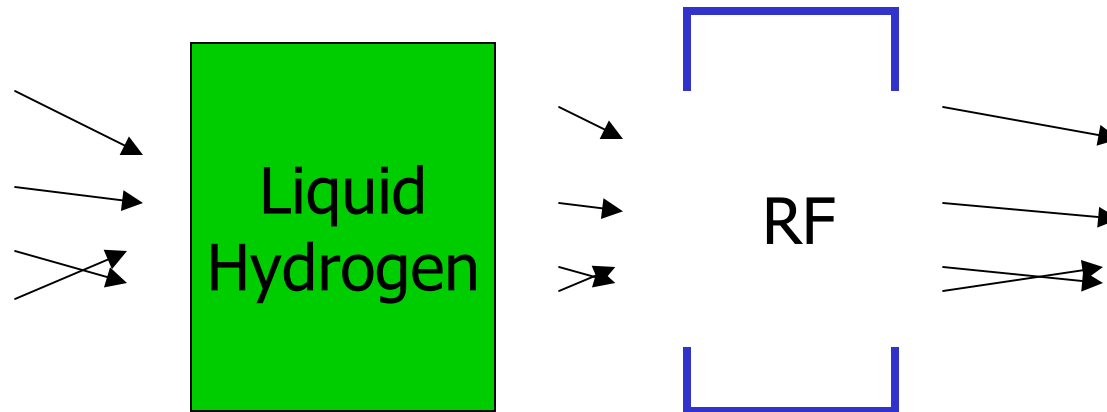
- Muon cooling increases beam phase space density using material placed across the beamline



Muon Cooling

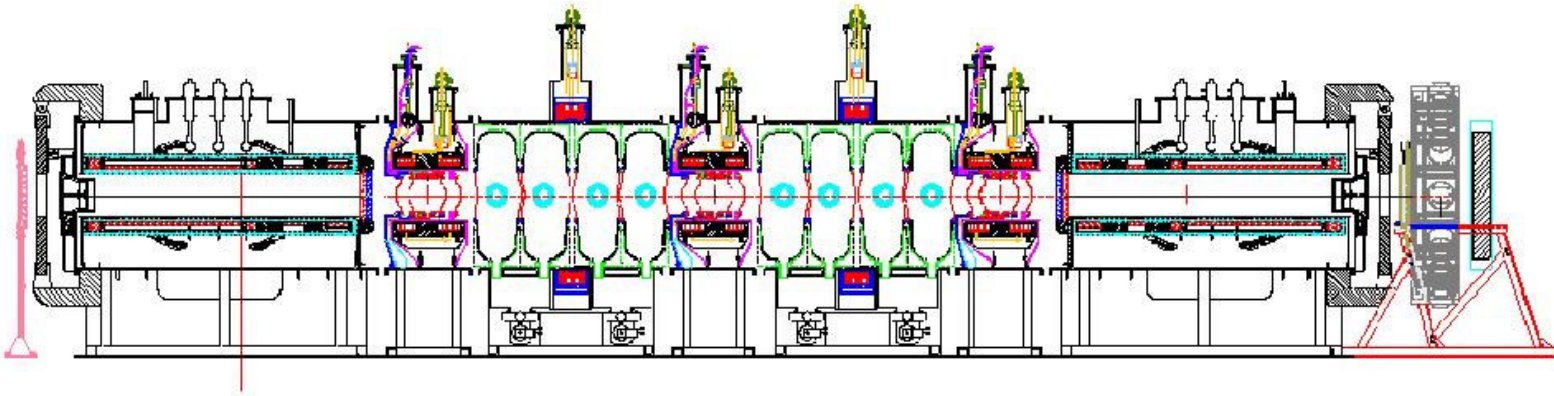
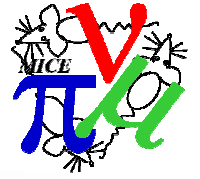


- Muon cooling increases beam phase space density using material placed across the beamline



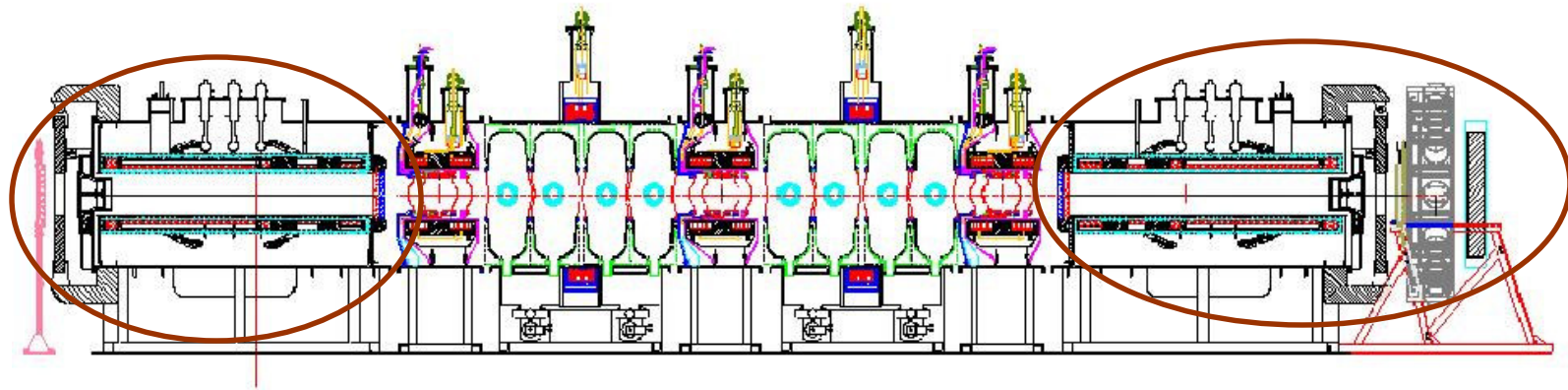
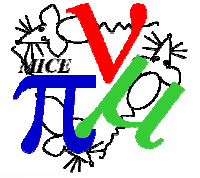
- By cooling we can fit more muons into our accelerator and improve the neutrino rate
- Liquid Hydrogen is the optimal material to use
 - Multiple scattering heats the beam
 - Liquid Hydrogen has more dE/dx vs multiple scattering

Muon Ionisation Cooling Experiment



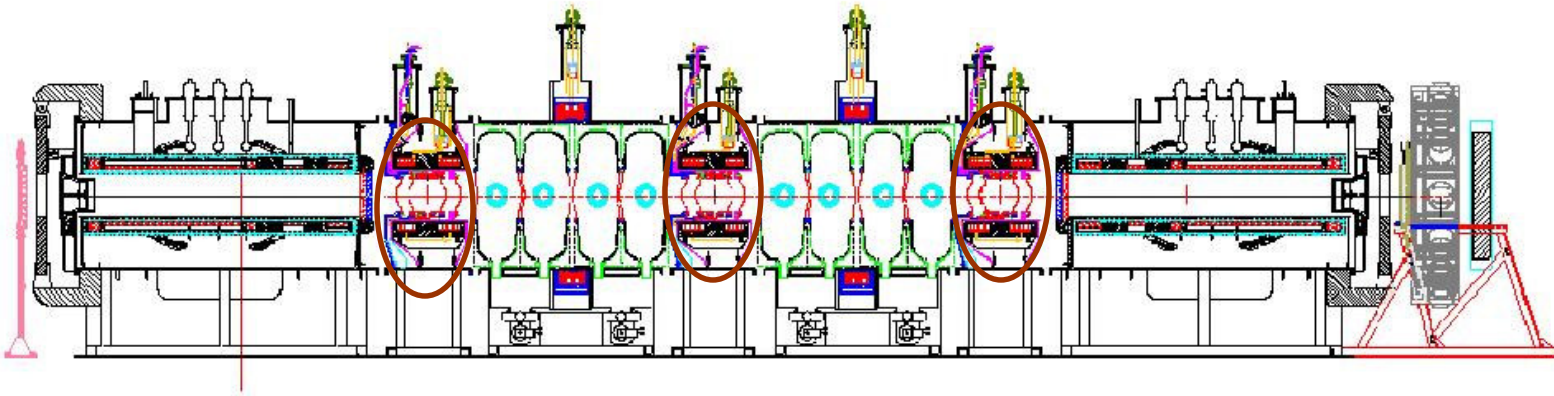
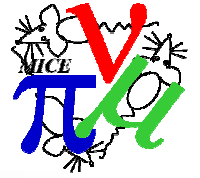
- Aim is to measure reduction in beam emittance over a cell of a cooling channel

Muon Ionisation Cooling Experiment



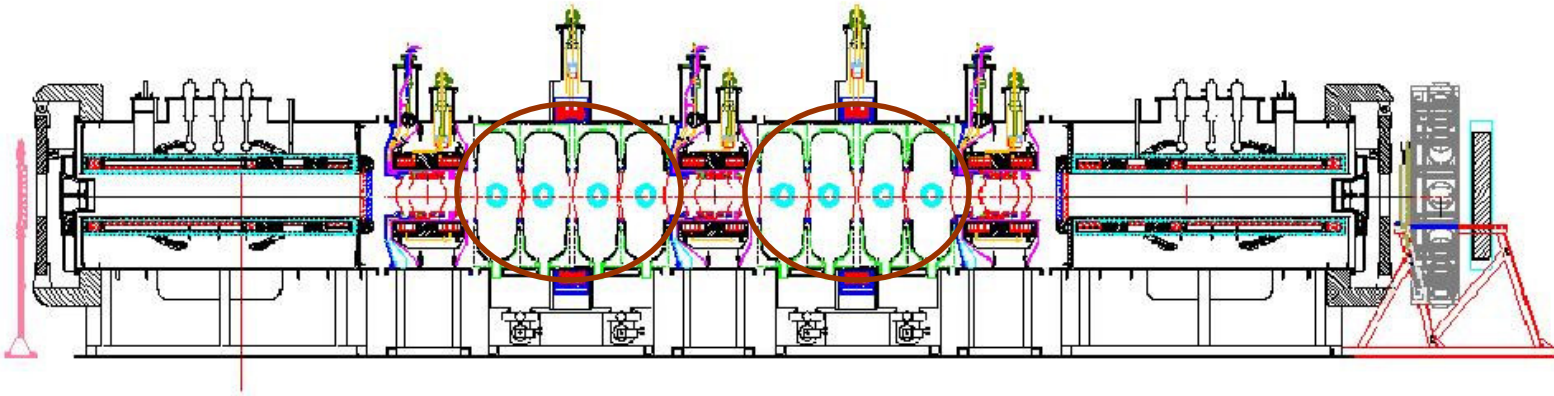
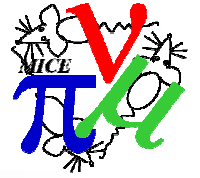
- Aim is to measure reduction in beam emittance over a cell of a cooling channel
 - Detectors measure phase space vector of particles and distinguish muons from pions and electrons

Muon Ionisation Cooling Experiment



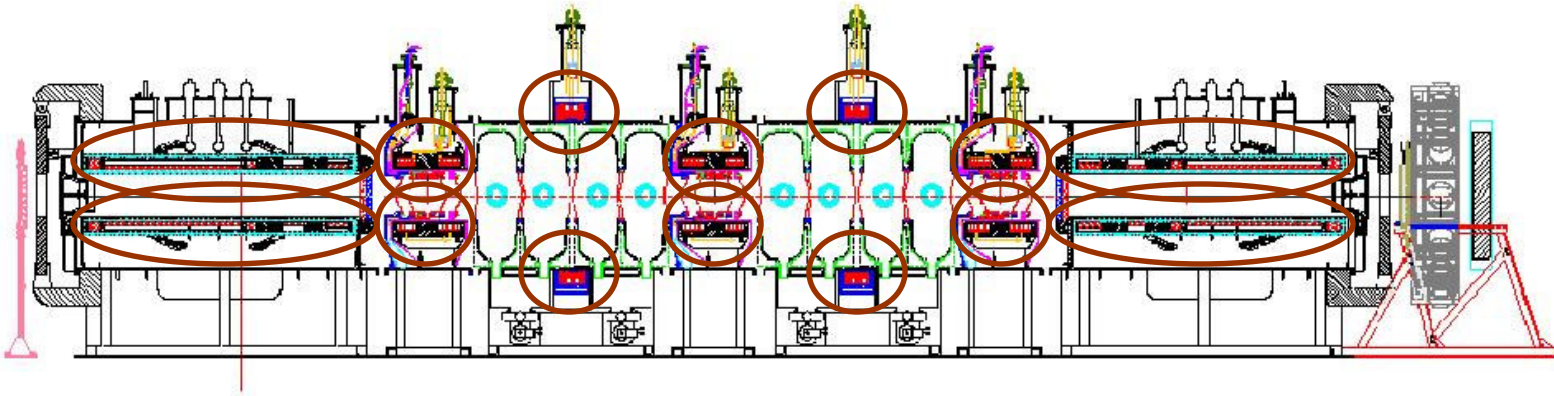
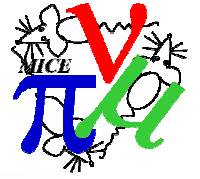
- Aim is to measure reduction in beam emittance over a cell of a cooling channel
 - Detectors measure phase space vector of particles and distinguish muons from pions and electrons
 - Liquid Hydrogen absorbers provide cooling

Muon Ionisation Cooling Experiment



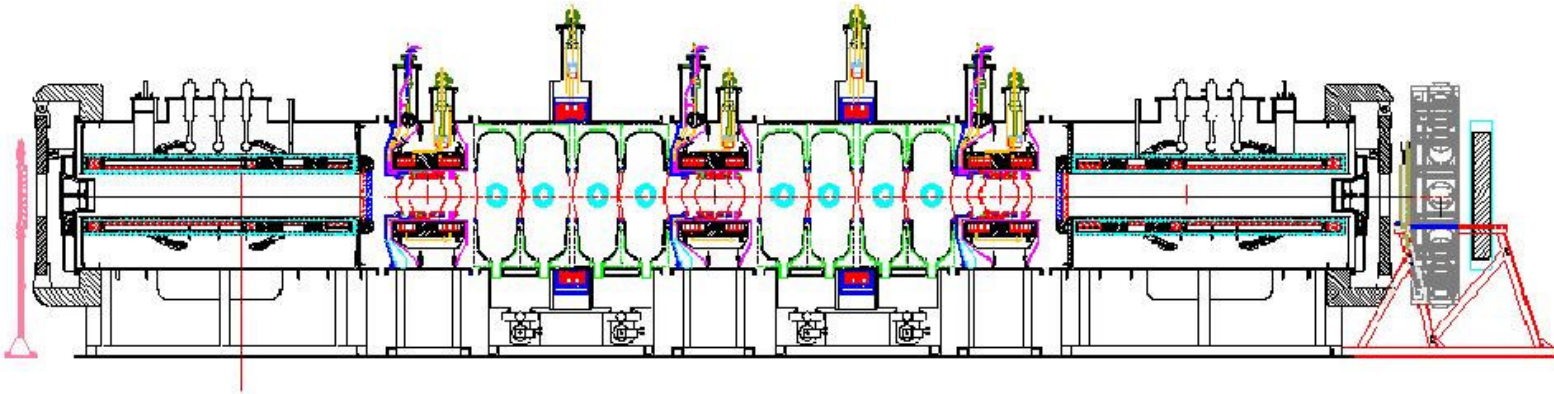
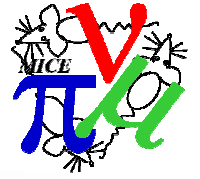
- Aim is to measure reduction in beam emittance over a cell of a cooling channel
 - Detectors measure phase space vector of particles and distinguish muons from pions and electrons
 - Liquid Hydrogen absorbers provide cooling
 - RF Cavities keep beam momentum \sim constant

Muon Ionisation Cooling Experiment



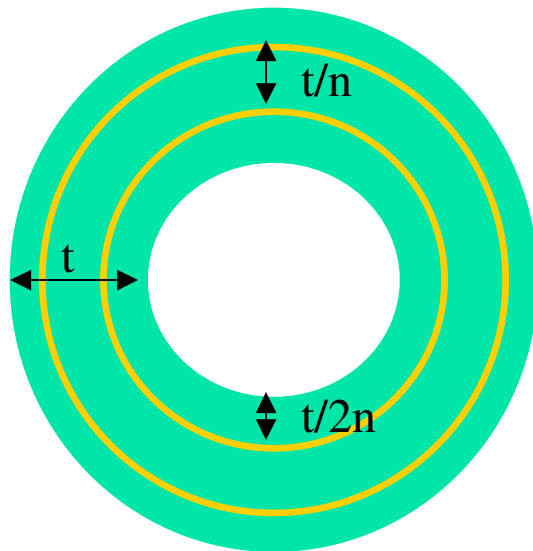
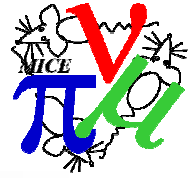
- Aim is to measure reduction in beam emittance over a cell of a cooling channel
 - Detectors measure phase space vector of particles and distinguish muons from pions and electrons
 - Liquid Hydrogen absorbers provide cooling
 - RF Cavities keep beam momentum \sim constant
 - Coils provide transverse focusing

Muon Ionisation Cooling Experiment



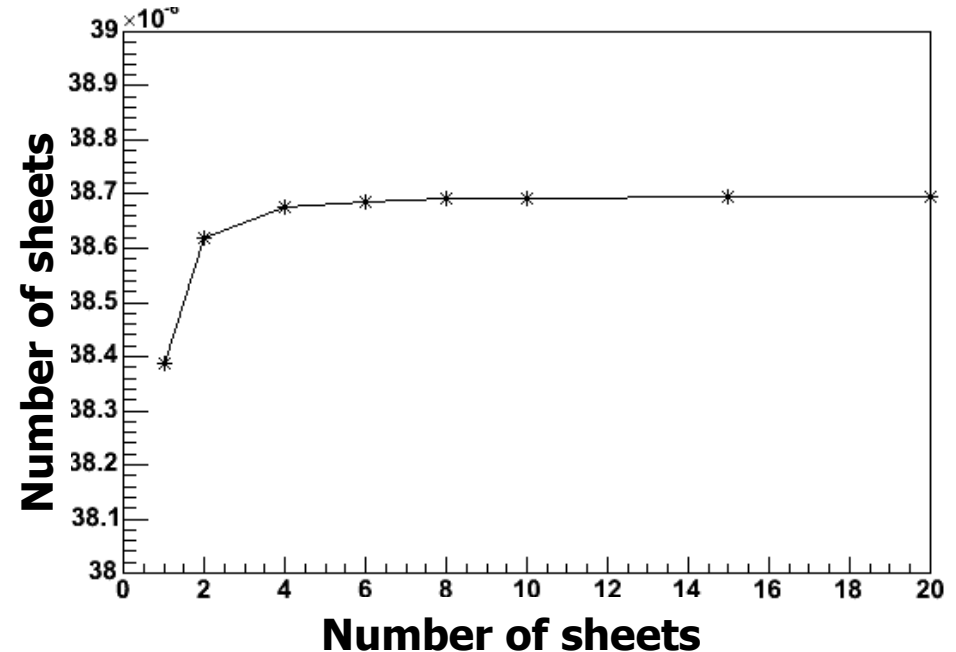
- Aim is to measure reduction in beam emittance over a cell of a cooling channel
- Challenging to build
- Ionisation cooling has never been demonstrated
- Reproduce and measure emittance to unprecedented 0.1% precision
- Simulated in MICE's customised accelerator, detector and beam optics package G4MICE, based in GEANT4

Solenoid Simulation



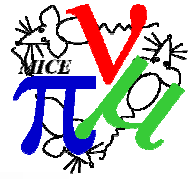
n = number of sheets
 t = thickness

Solenoid B-field model

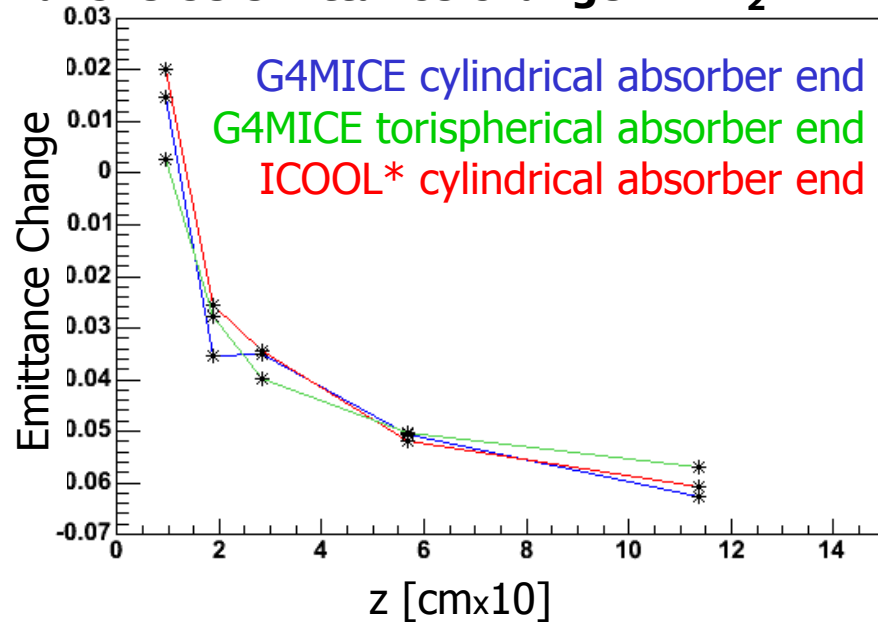


- Solenoid simulated using concentric cylindrical current sheets
 - Analytical model for one sheet is well known
 - In the limit of a large number of sheets, expect to achieve good field model
 - We will measure the fields and compare with this model

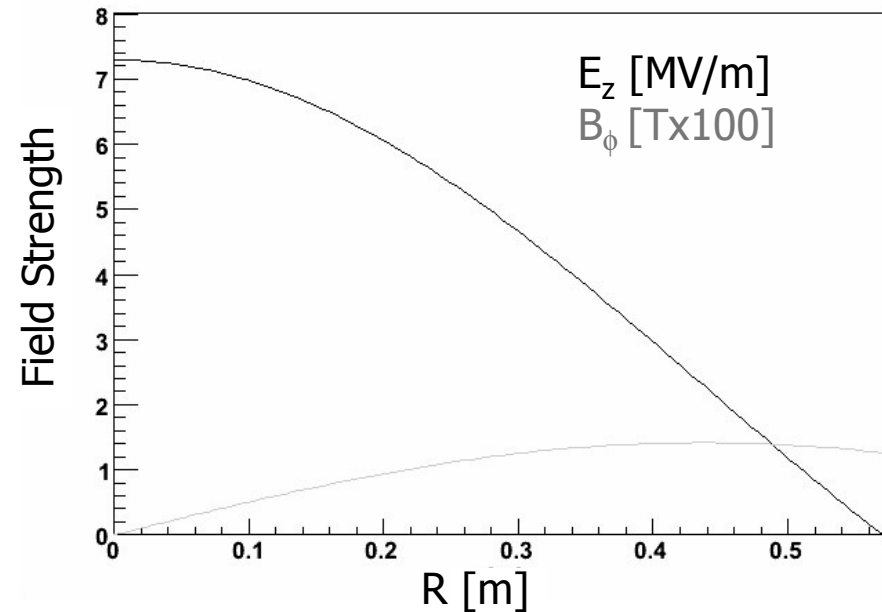
Liquid Hydrogen and RF Simulation



Transverse emittance change in LH₂



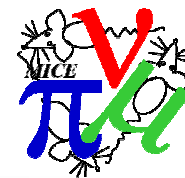
Fields in RF cavity



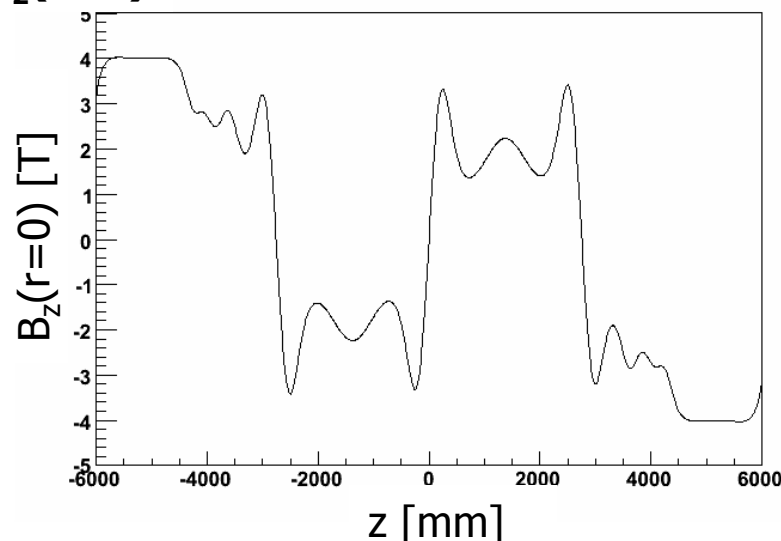
- Simulated cooling power for a typical MICE beam in a liquid Hydrogen absorber
 - Compare G4MICE with a well known software package
 - Compare realistic absorber with cylindrical absorber
- Simulated accelerating field in a MICE RF Cavity

*ICOOL simulation code, Fernow, Proc. Particle Accelerator Conference 1999

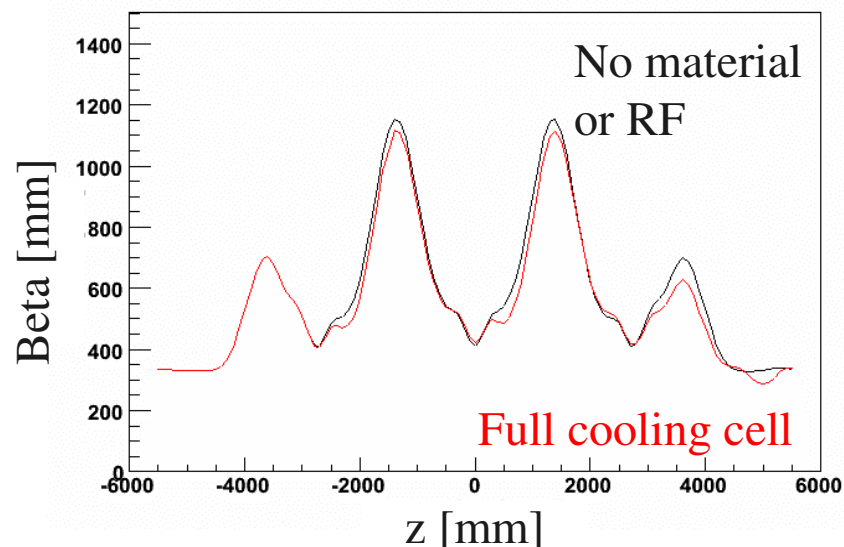
MICE Baseline Magnetic Lattice



$B_z(r=0)$

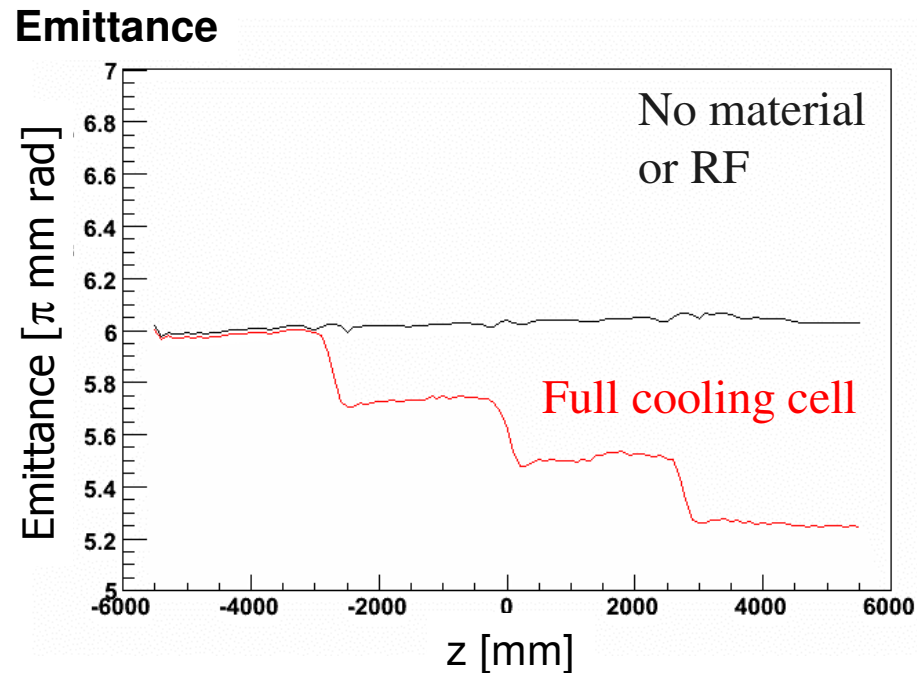
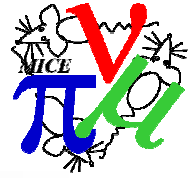


Beta function



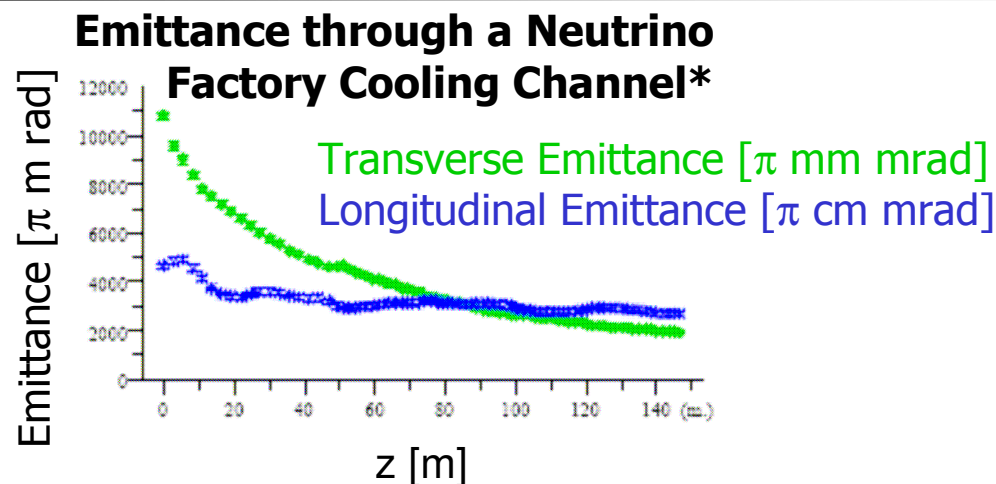
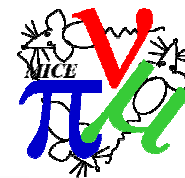
- 8 coils of cooling lattice chosen to:
 - Maximise beam accepted into cooling channel
 - Focus muons at the absorbers
 - Minimise scraping
- 6 coils in Spectrometer solenoids provide up to 4T field constant to 1% over fiducial volume
- 4 matching coils control beam from spectrometer to cooling lattice

Simulated Cooling Performance



- Simulated cooling performance for typical beams
 - Simulated using MICE's customised beam tracking, detector modelling and beam optics analysis package based on GEANT4
 - Simulated for a typical MICE case
 - MICE is designed to run with many different input emittances and input momenta

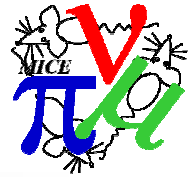
Measurement Requirement



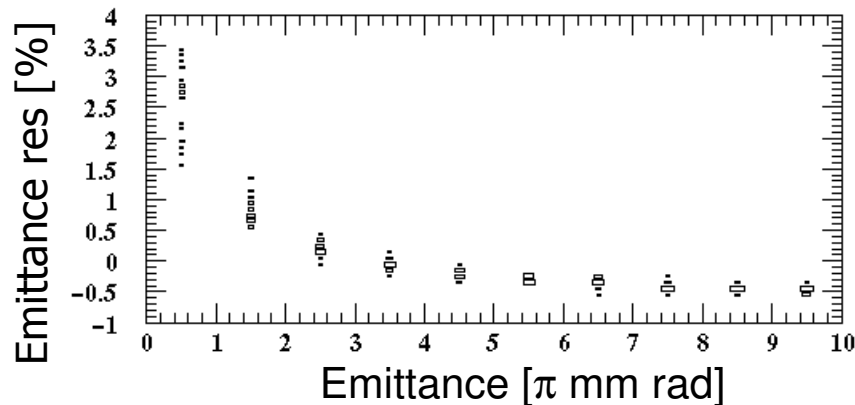
- Desire to extrapolate measurement from 1 cell to many
- Small error on a single cell measurement has a significant impact on prediction of emittance for many cells
- In practice several measurements will be made with different emittance beams for a given setting
 - But the errors will not be independent

*Feasibility Study II of a Muon Based Neutrino Source, 2001, ed. Ozaki, Palmer, Zisman, Gallardo

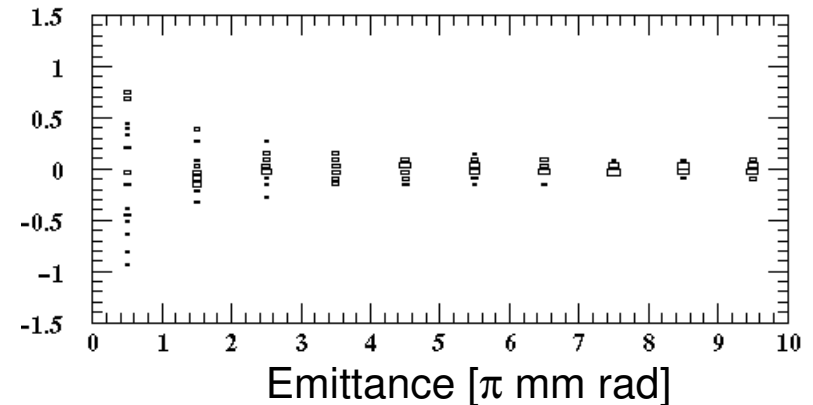
Simulated Transverse Emittance Resolution



Emittance Resolution without calibration*



Emittance Resolution with ideal calibration*

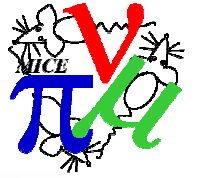


- Emittance resolution better than 0.5% for beam emittances in the region of interest
- Most of the error can be removed by careful calibration
 - Emittance resolution limited by statistics for a given measurement given a very precise calibration
 - Even if we can only estimate the resolutions to $\sim 10\%$, we can still measure emittance to the desired precision

*C.Rogers, M. Ellis, Proc. Particle Accelerator Conference 2005, MPE013



Summary



- MICE looking to measure emittance to high precision
 - Unprecedented precision for emittance measurement
- Detector design is approaching completion
 - High resolution tracking and time of flight measurements
 - Precise particle identification
- Construction of MICE has begun
- First beam October 2007