

New Spectroscopy of Heavy Mesons

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How to (try to) understand the properties of recently discovered states
using the heavy quark limit

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Open charm/beauty states

- $D_0(2308)$, $D'_1(2440)$
- $D_{s0}^*(2317)$, $D'_{s1}(2460)$
- $D(2550)$, $D(2600)$, $D(2750)$, $D(2760)$
- $D_{sJ}(2632)$
- $D_{sJ}(2860)$, $D_{sJ}(2710)$, $D_{sJ}(3040)$

- $B_1(5734)$, $B_2^*(5738)$
- $B_{s1}(5830)$, $B_{s2}^*(5840)$

Open charm/beauty states

- $D_0(2308)$, $D'_1(2440)$
- $D_{s0}^*(2317)$, $D'_{s1}(2460)$
- $D(2550)$, $D(2600)$, $D(2750)$, $D(2760)$
- ~~$D_{sJ}(2632)$~~ \longrightarrow Seen only by SELEX, never confirmed
- $D_{sJ}(2860)$, $D_{sJ}(2710)$, $D_{sJ}(3040)$

- $B_1(5734)$, $B^*_2(5738)$
- $B_{s1}(5830)$, $B^*_{s2}(5840)$

Open charm/beauty states

- $D_0(2308), D'_1(2440)$

- $D_{s0}^*(2317), D'_{s1}(2460)$

- $D(2550), D(2600), D(2750), D(2760)$

- ~~$D_{sJ}(2632)$~~ \longrightarrow Seen only by SELEX, never confirmed

- $D_{sJ}(2860), D_{sJ}(2710), D_{sJ}(3040)$

- $B_1(5734), B_2^*(5738)$

- $B_{s1}(5830), B_{s2}^*(5840)$

Hadrons containing a single heavy quark Q

Spin of the heavy quark and of the light degrees of freedom decoupled in the $m_Q \rightarrow \infty$ limit

Spin symmetry

$$\vec{J}_M = \vec{s}_\ell + \vec{s}_Q \quad \text{spin}$$

$$\vec{s}_\ell = \vec{L} + \vec{s}_q \quad \text{angular momentum of the light degrees of freedom (conserved)}$$

Mesons classified as **doublets** the members of which have

$$J = s_\ell \pm \frac{1}{2}$$

The heavy quark flavour becomes irrelevant as $m_Q \rightarrow \infty$

Flavour symmetry



possibility to relate charm and beauty hadron properties

HQ limit for meson doublets and strong decays to light pseudoscalars

The two states within a given doublet are degenerate

They have the same total width

The sum of the partial widths of a state in a doublet to a state in another doublet with emission of a light meson is the same for the two states of a doublet

Spin symmetry predicts the ratios of partial decay widths for a given state

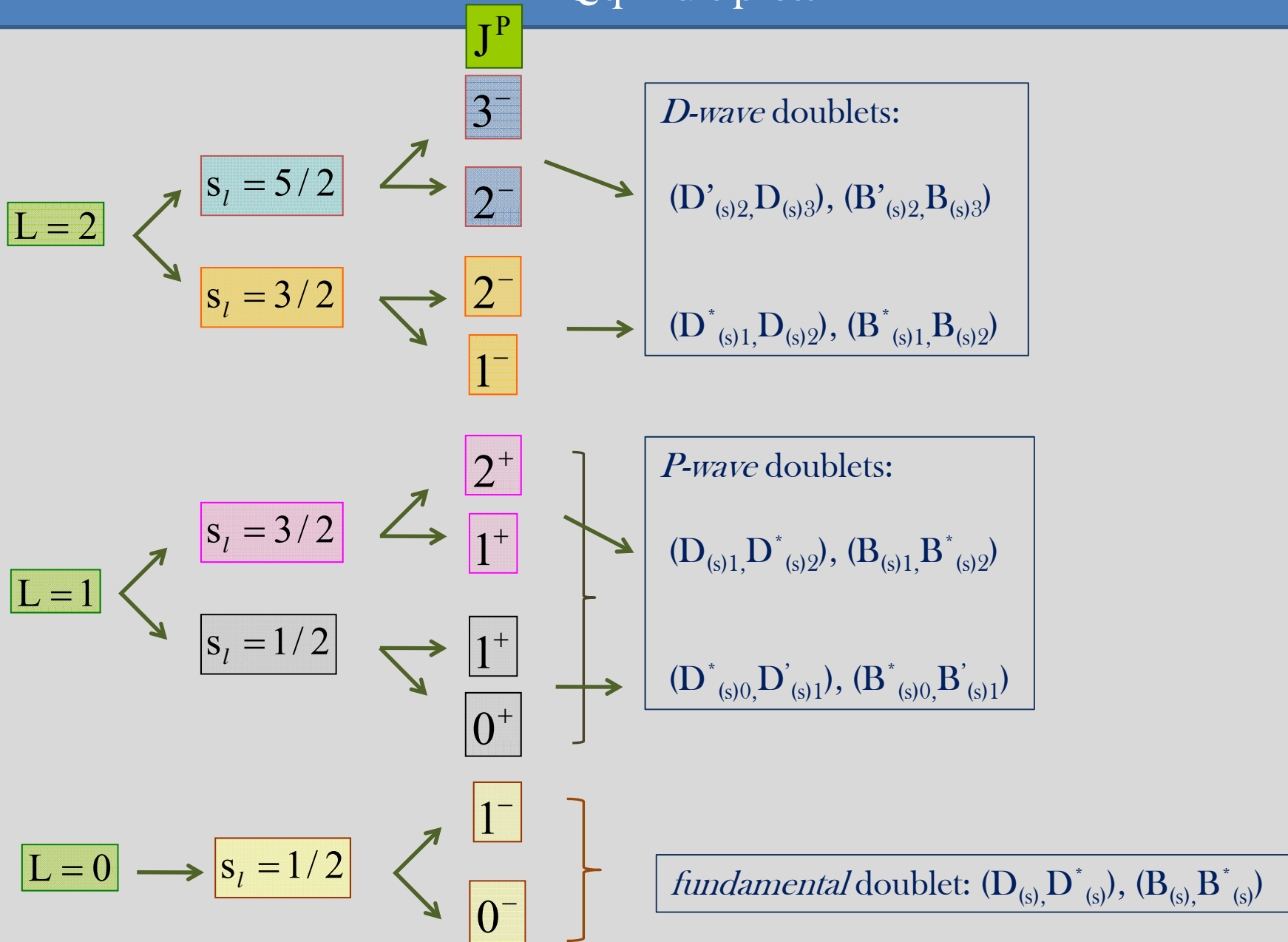
Partial decay widths are independent on the HQ flavour

Mass splittings among the doublets are independent of the HQ flavour

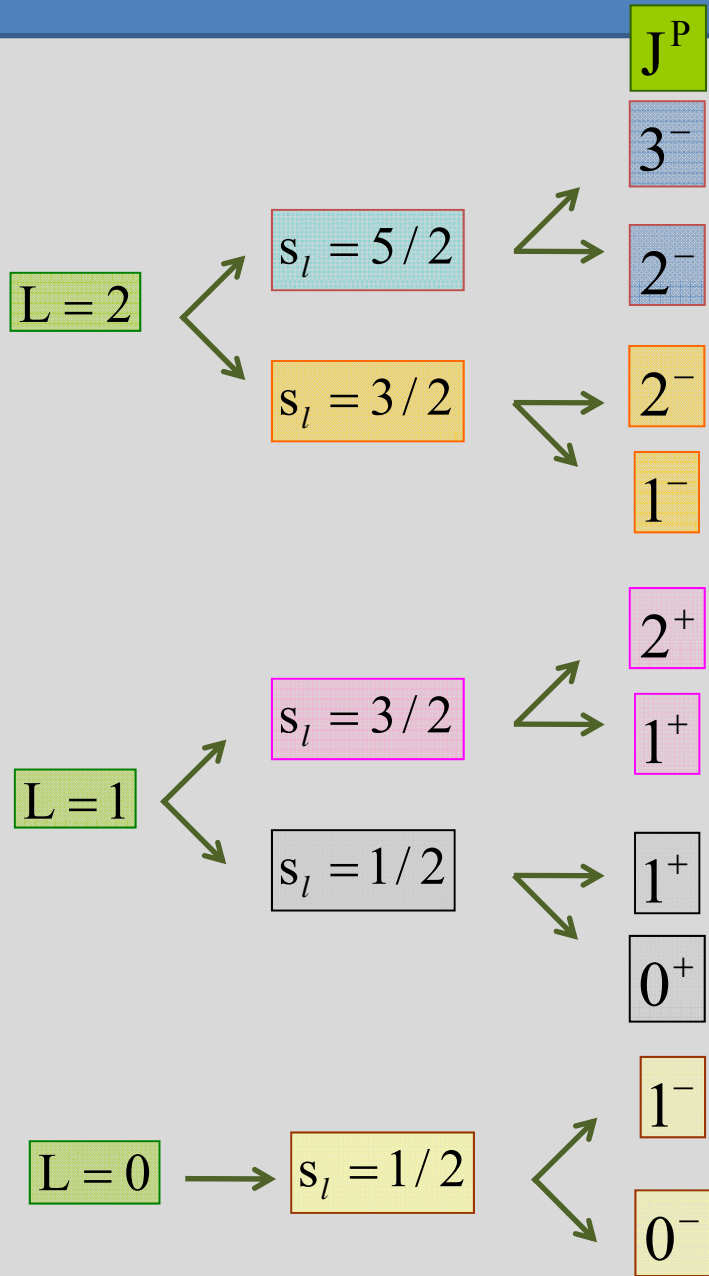
Spin
symmetry

Flavour
symmetry

Qq̄ multiplets



Qq̄ multiplets

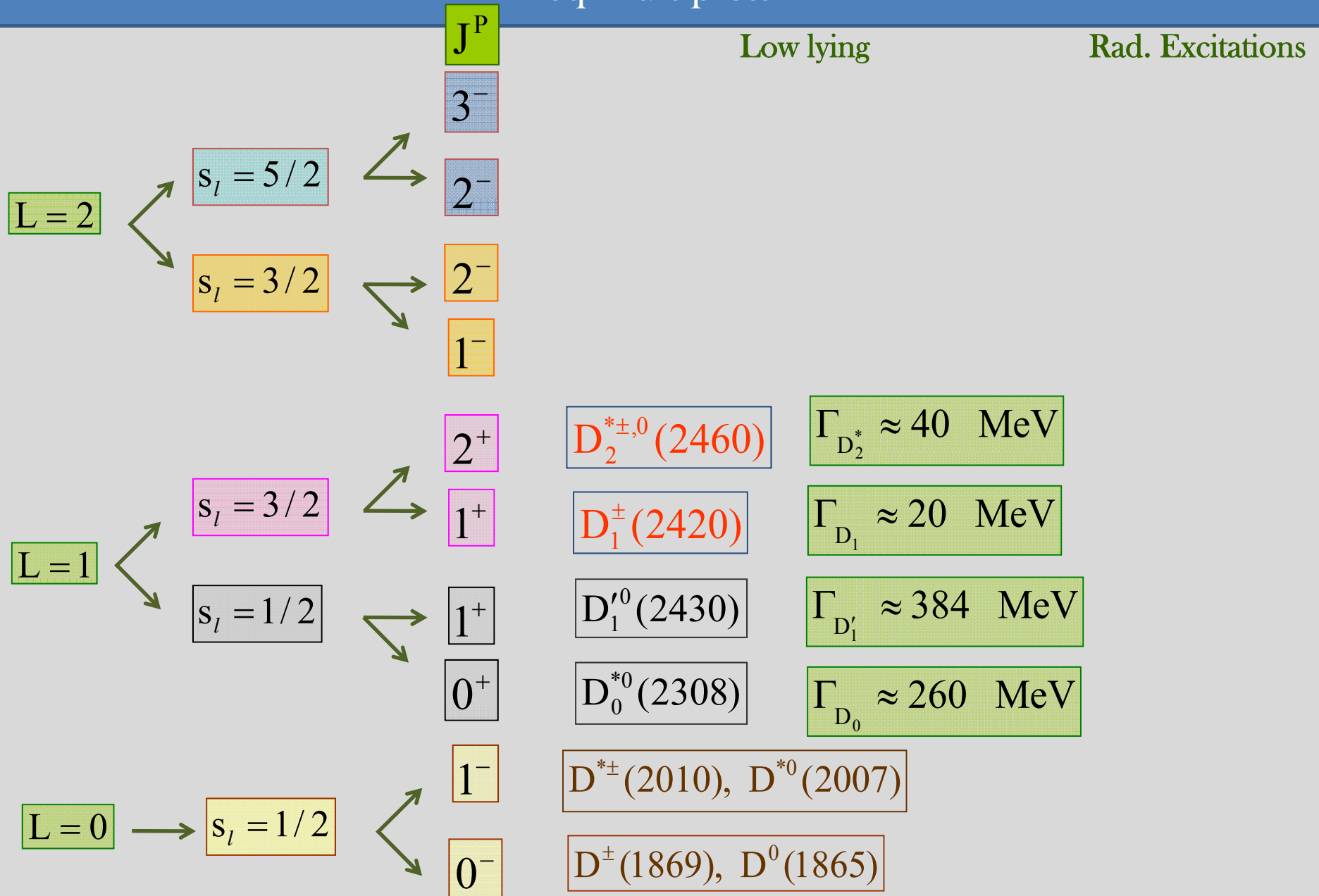


Strong transitions between multiplets

$\frac{3^+}{2} \rightarrow \frac{1^-}{2} + \text{pseudoscalar meson}$
 d-wave transition
 $\frac{3^+}{2}$ mesons are expected to be narrow

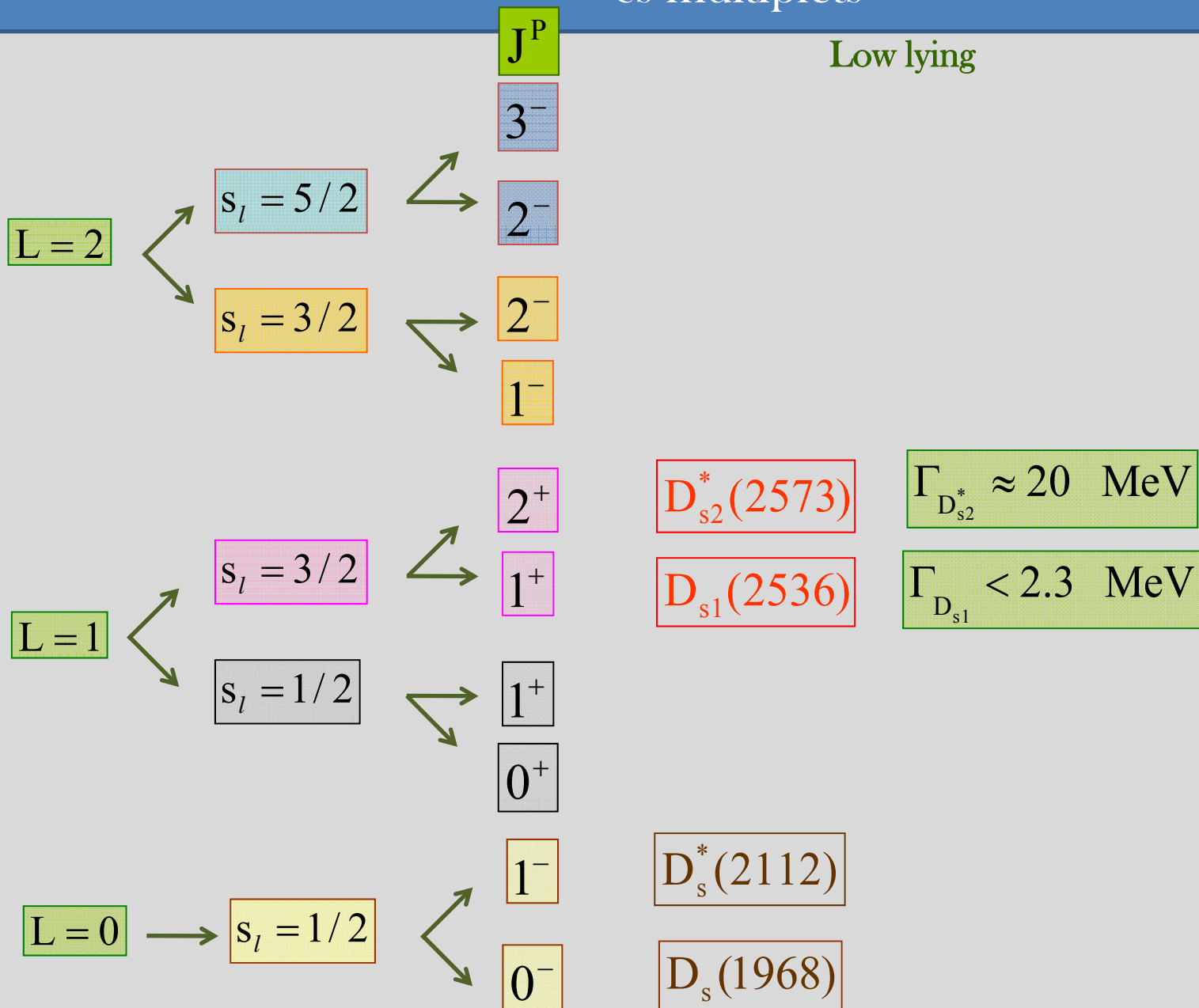
$\frac{1^+}{2} \rightarrow \frac{1^-}{2} + \text{pseudoscalar meson}$
 s-wave transition
 $\frac{1^+}{2}$ mesons are expected to be **broad**

$c\bar{q}$ multiplets

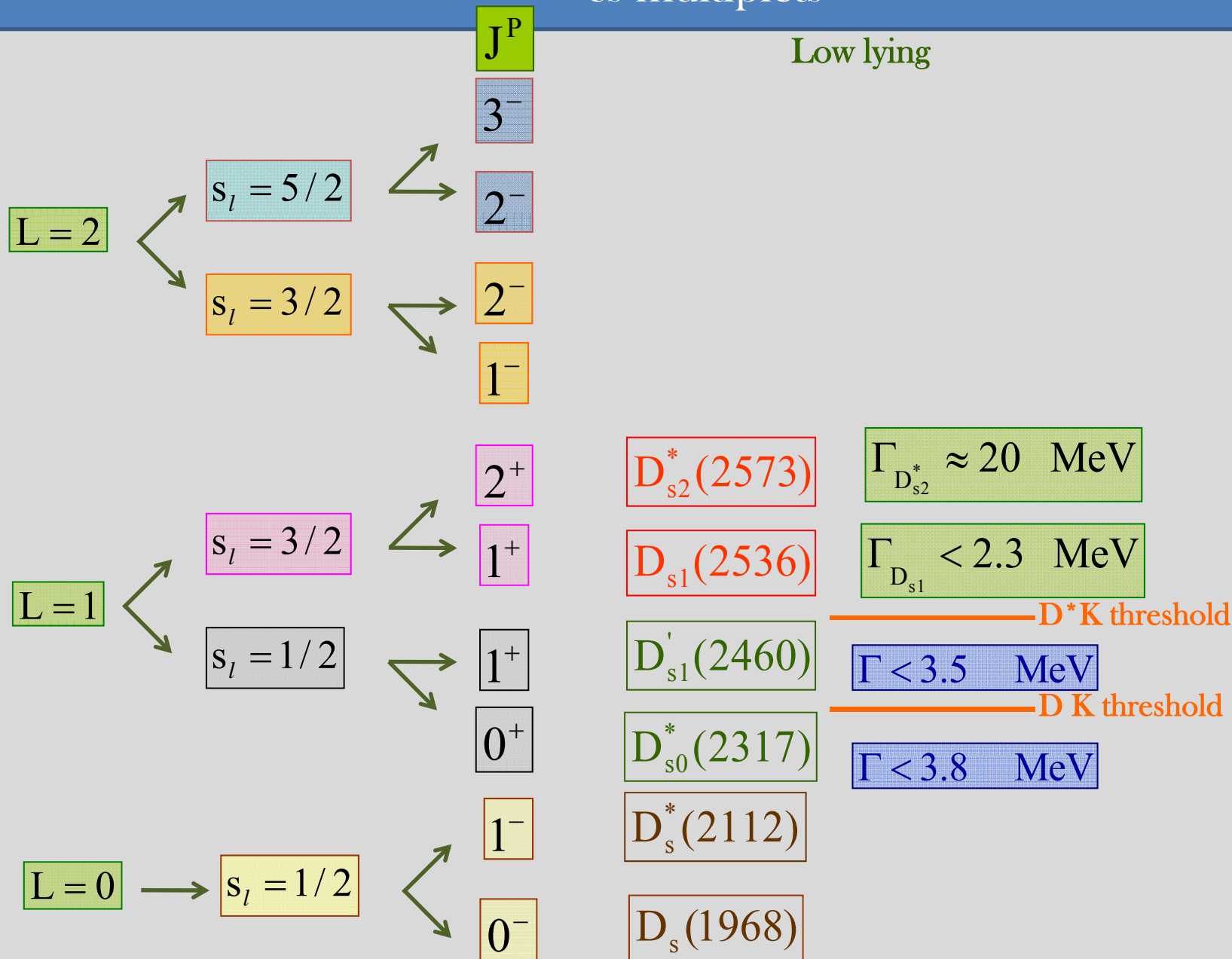


$c\bar{s}$ multiplets

Low lying

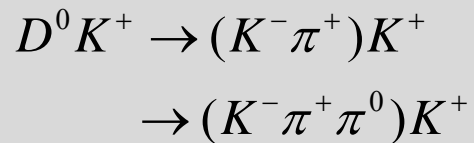


$c\bar{s}$ multiplets

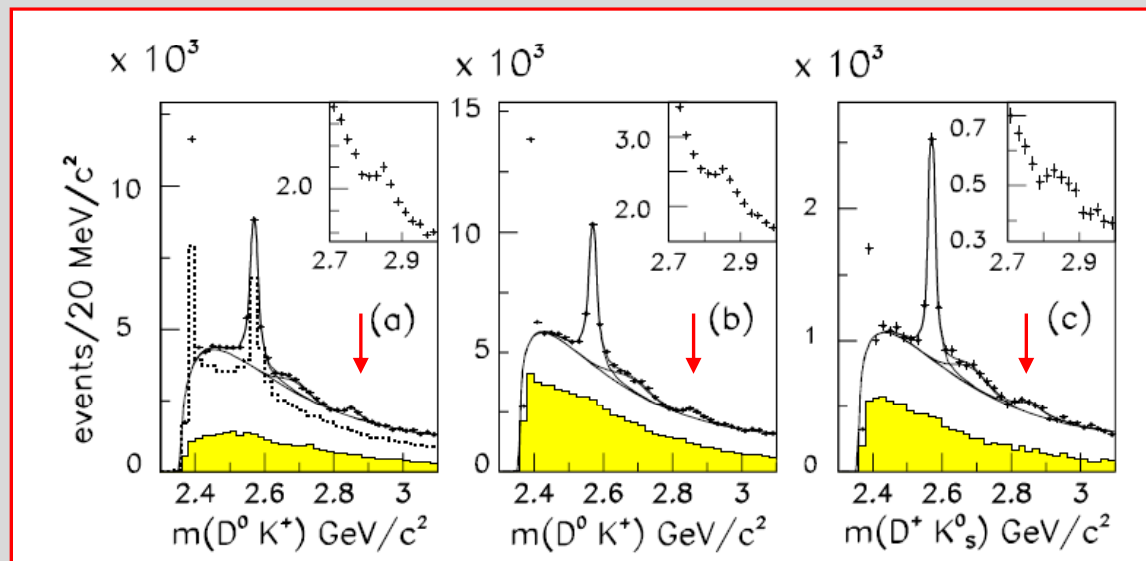


$D_{sJ}(2860)$

- Discovered by BaBar Collab.
- Reconstructed in



and in $D^+ K_S^0$



$$M = 2856.6 \pm 1.5 \pm 5.0 \quad \text{MeV}$$

$$\Gamma = 48 \pm 7 \pm 10 \quad \text{MeV}$$

BaBar Collab., PRL 97 (06) 222001

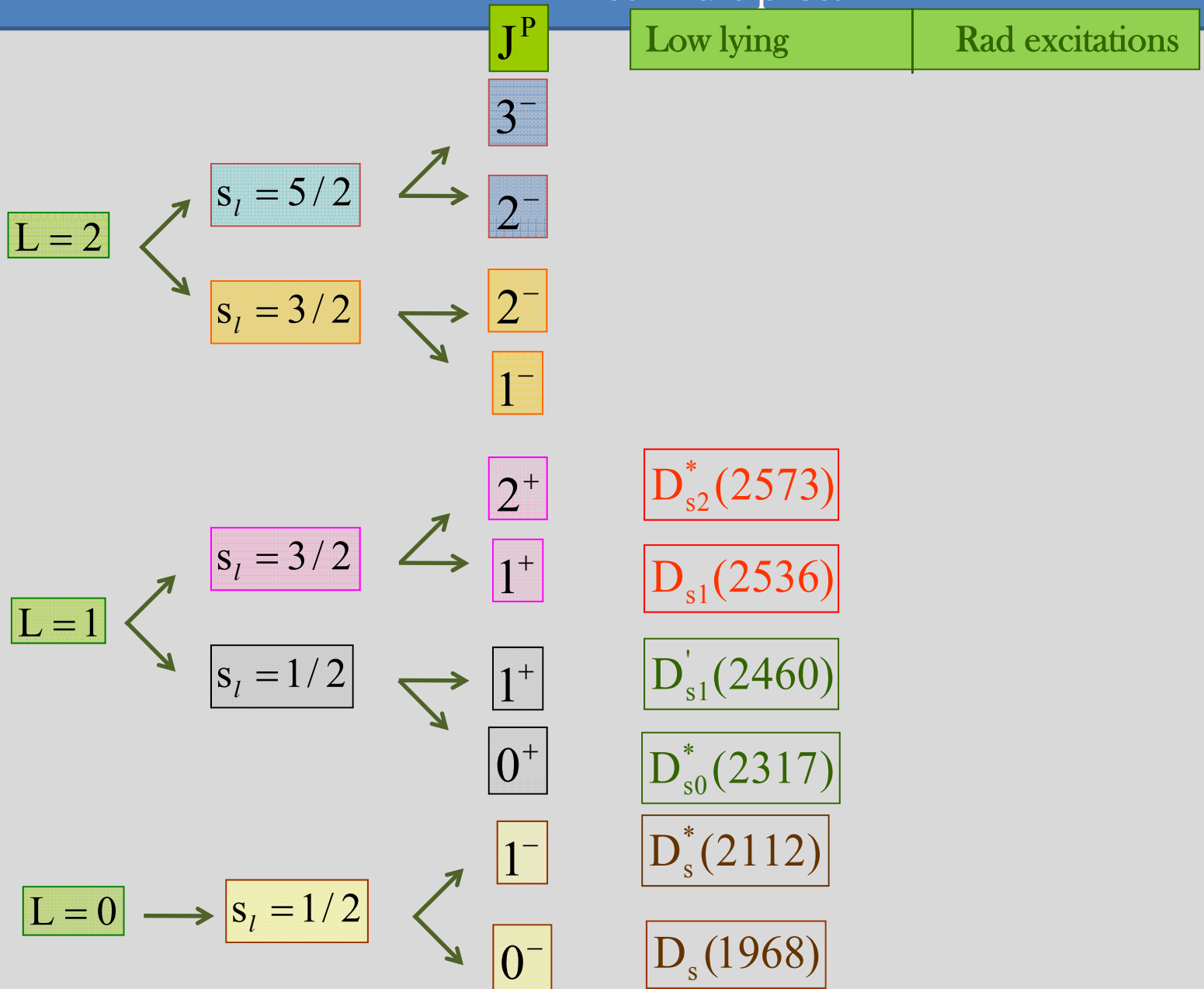
Quantum number assignment required in order to identify it

Possibilities: - low lying state not yet observed

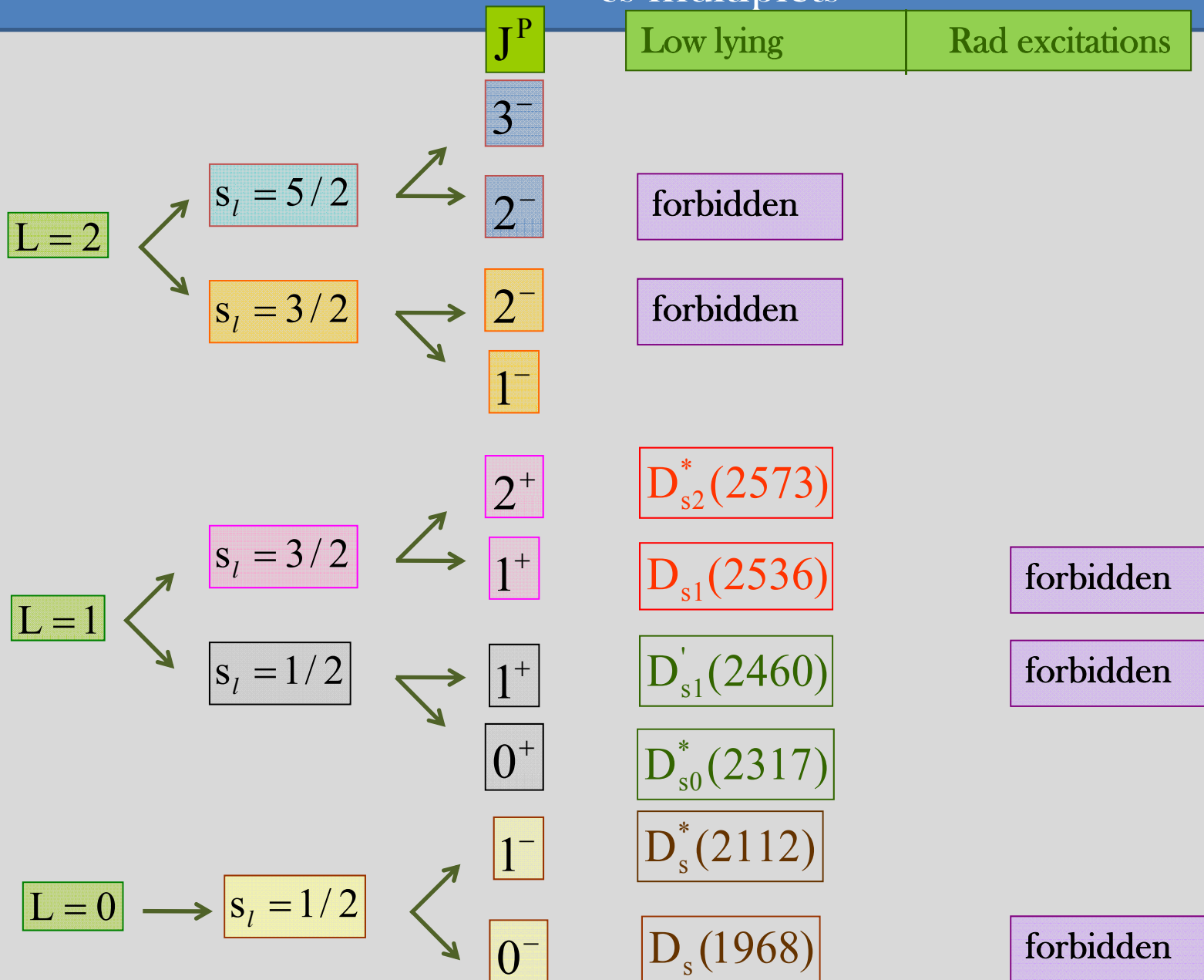
- radial excitation of an already observed state

Only states that can decay to the observed mode DK are allowed

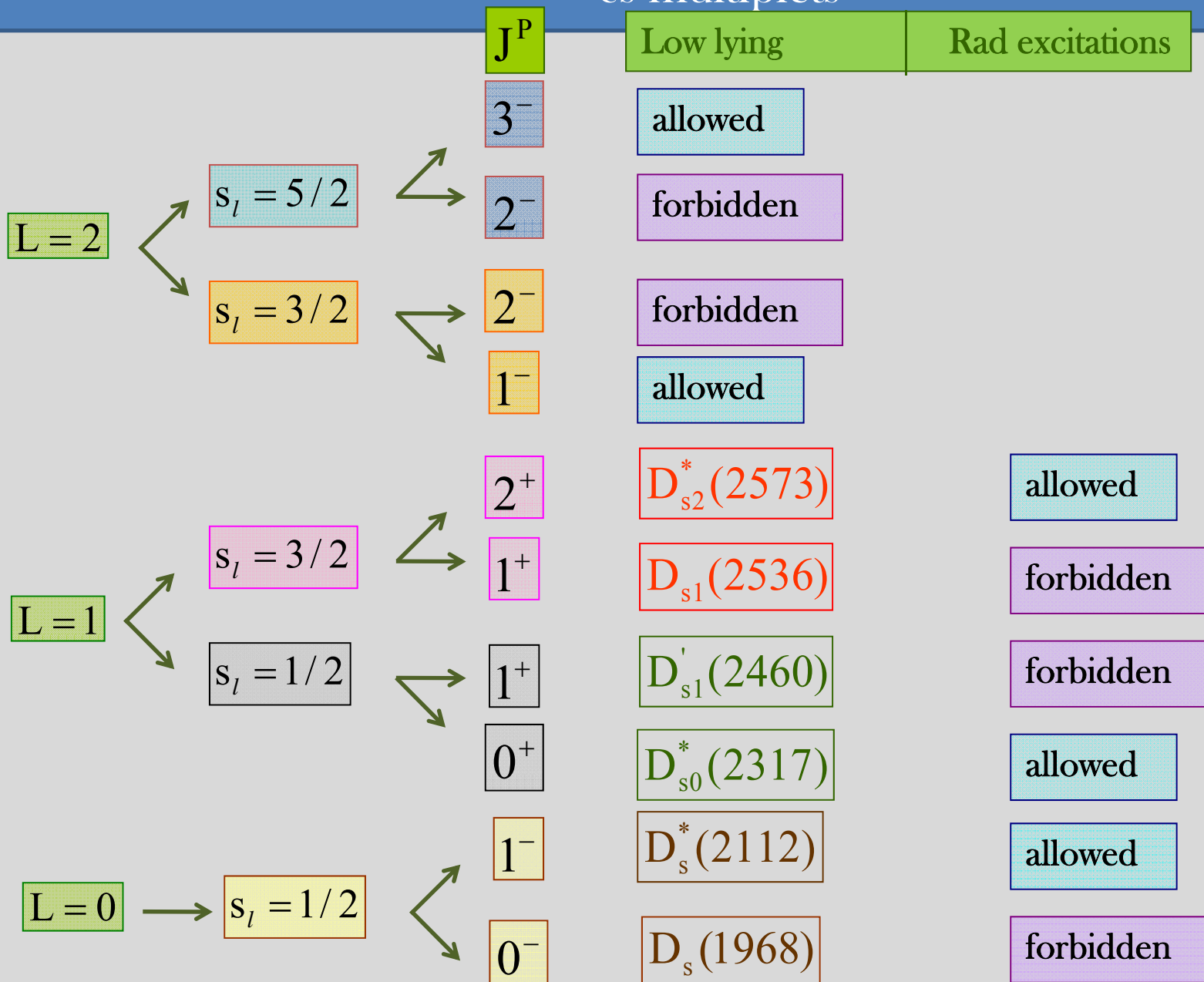
$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



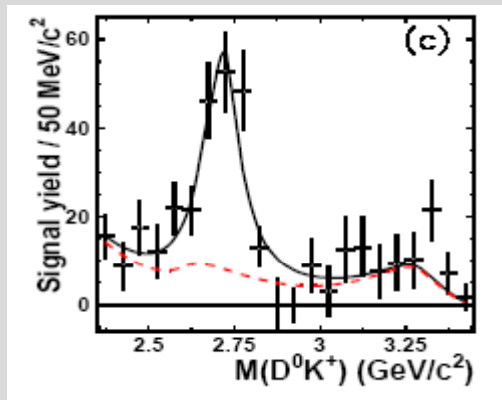
$D_{sJ}(2710)$

Belle Collab.: analysis of the mode

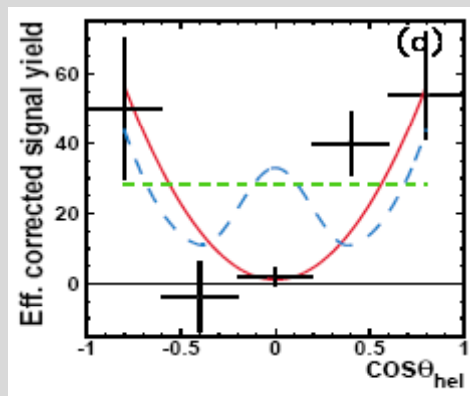


New resonance decaying to $D^0 K^+$ with:

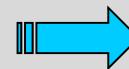
$$M = 2708 \pm 9 \pm_{10}^{11} \text{ MeV} \quad \Gamma = 108 \pm 23 \pm_{31}^{36} \text{ MeV}$$



$$1^- \rightarrow 0^- 0^- \text{ implies } P=-1$$

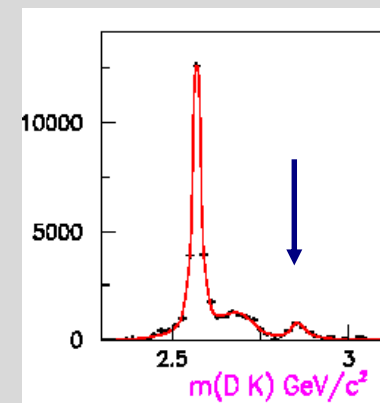


- J=0
- J=1
- J=2

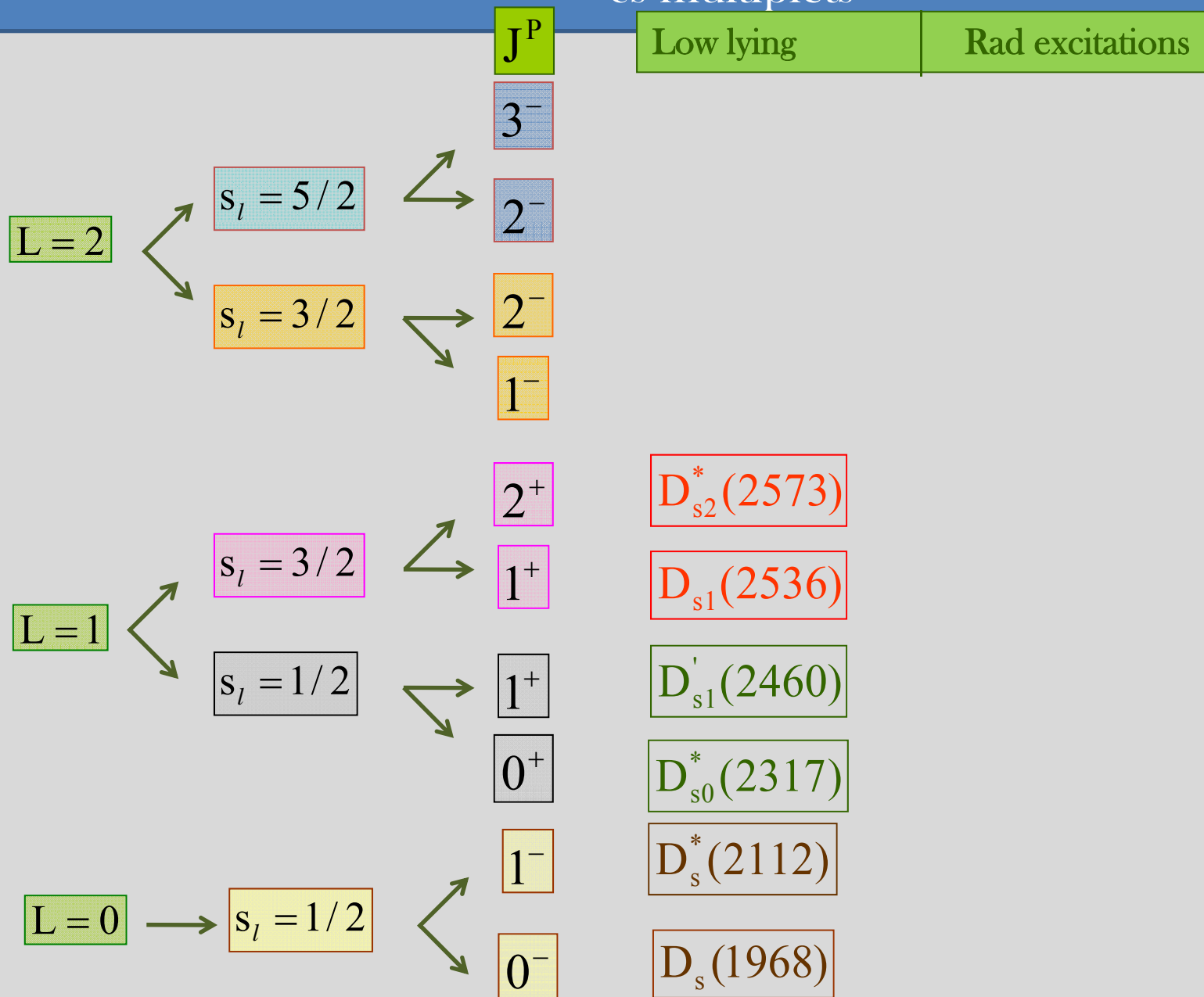


$J^P=1^-$ favoured

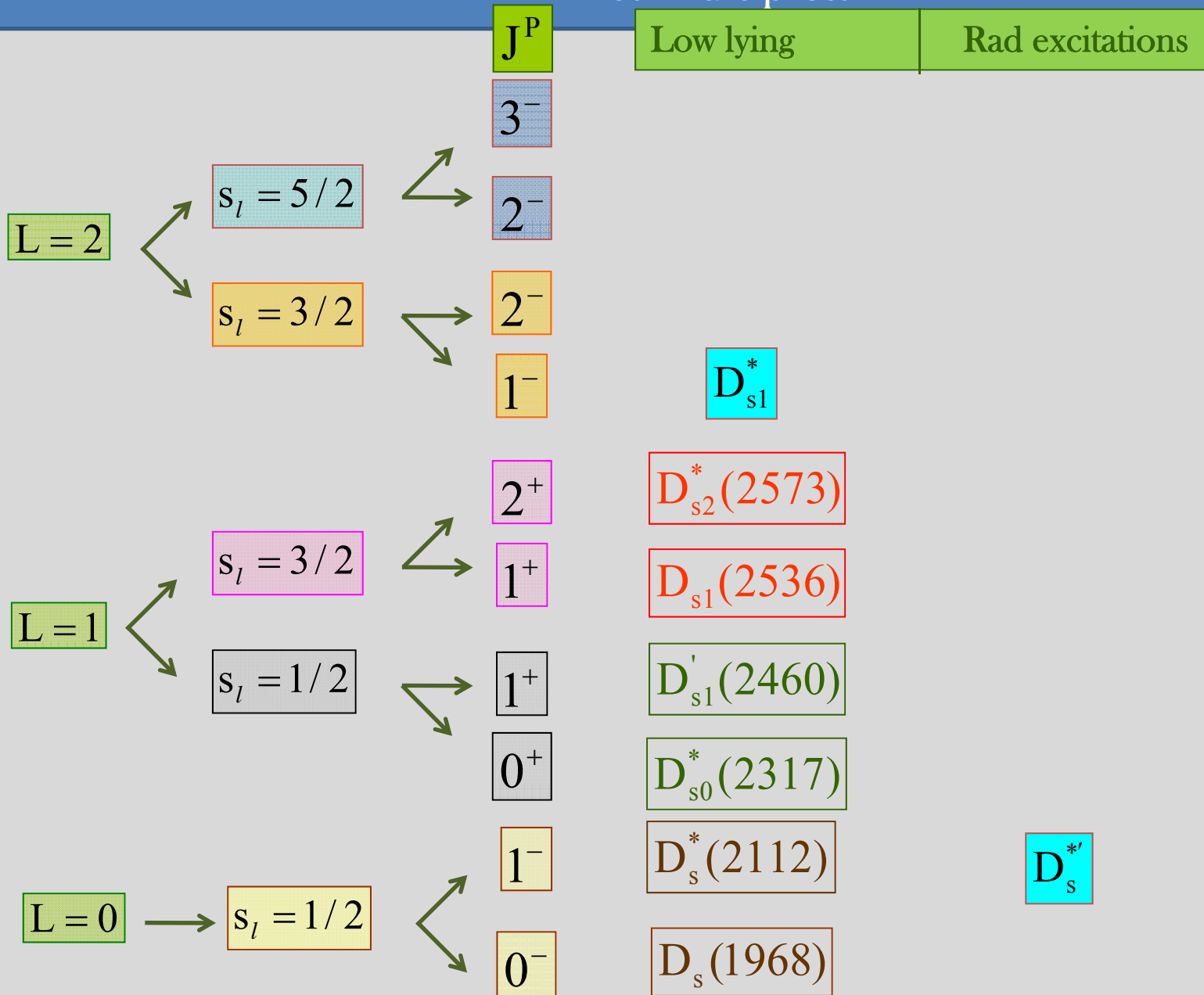
A broad structure at $M=2688 \text{ MeV}$ with $\Gamma=112 \text{ MeV}$ was found by BaBar in the DK mass distribution



$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



D_{sJ}(2860) & D_{sJ}(2710)

predictions on allowed decay rates can help to distinguish among the various possibilities

HQ limit: the members of the doublets are described by effective fields:

L=0	{	$S_\ell^P = \frac{1}{2}^-$	$H_a = \frac{1+\not{v}}{2} [P_{a\mu}^* \gamma^\mu - P_a \gamma_5]$
L=1	{	$S_\ell^P = \frac{1}{2}^+$	$S_a = \frac{1+\not{v}}{2} [P_{1a}'^{\mu} \gamma_\mu \gamma_5 - P_{0a}^*]$
		$S_\ell^P = \frac{3}{2}^+$	$T_a^\mu = \frac{1+\not{v}}{2} \left\{ P_{2a}^{\mu\nu} \gamma_\nu - P_{1a\nu} \sqrt{\frac{3}{2}} \gamma_5 \left[g^{\mu\nu} - \frac{1}{3} \gamma^\nu (\gamma^\mu - v^\mu) \right] \right\}$
L=2	{	$S_\ell^P = \frac{3}{2}^-$	$X_a^\mu = \frac{1+\not{v}}{2} \left\{ P_{2a}^{*\mu\nu} \gamma_5 \gamma_\nu - P_{1a\nu}' \sqrt{\frac{3}{2}} \left[g^{\mu\nu} - \frac{1}{3} \gamma^\nu (\gamma^\mu - v^\mu) \right] \right\}$
		$S_\ell^P = \frac{5}{2}^-$	$X_a'^{\mu\nu} = \frac{1+\not{v}}{2} \left\{ P_{3a}^{\mu\nu\sigma} \gamma_\sigma - P_{2a}'^{\alpha\beta} \sqrt{\frac{5}{3}} \gamma_5 \left[g_\alpha^\mu g_\beta^\nu - \frac{1}{5} \gamma_\alpha g_\beta^\nu (\gamma^\mu - v^\mu) - \frac{1}{5} \gamma_\beta g_\alpha^\mu (\gamma^\nu - v^\nu) \right] \right\}$

D_{sJ}(2860) & D_{sJ}(2710)

Interactions with the emission of a light pseudoscalar meson described by effective Lagrangian terms

$$\mathcal{L}_H = g \text{Tr}[\bar{H}_a H_b \gamma_\mu \gamma_5 \mathcal{A}_{ba}^\mu], \quad \mathbf{H} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_S = h \text{Tr}[\bar{H}_a S_b \gamma_\mu \gamma_5 \mathcal{A}_{ba}^\mu] + \text{h.c.}, \quad \mathbf{S} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_T = \frac{h'}{\Lambda_\chi} \text{Tr}[\bar{H}_a T_b^\mu (i D_\mu \mathcal{A} + i \not{D} \mathcal{A}_\mu)_{ba} \gamma_5] + \text{h.c.}, \quad \mathbf{T} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_X = \frac{k'}{\Lambda_\chi} \text{Tr}[\bar{H}_a X_b^\mu (i D_\mu \mathcal{A} + i \not{D} \mathcal{A}_\mu)_{ba} \gamma_5] + \text{h.c.}, \quad \mathbf{X} \longrightarrow \mathbf{H} \pi$$

$$\mathcal{L}_{X'} = \frac{1}{\Lambda_\chi^2} \text{Tr}[\bar{H}_a X_b'^{\mu\nu} [k_1 \{D_\mu, D_\nu\} \mathcal{A}_\lambda + k_2 (D_\mu D_\nu \mathcal{A}_\lambda + D_\nu D_\lambda \mathcal{A}_\mu)]_{ba} \gamma^\lambda \gamma_5] + \text{h.c.}, \quad \mathbf{X}' \longrightarrow \mathbf{H} \pi$$

$$\mathcal{A}_{\mu ba} = \frac{i}{2} (\xi^\dagger \partial_\mu \xi - \xi \partial_\mu \xi^\dagger)_{ba}$$

$$\xi = e^{\frac{i\mathcal{M}}{f_\pi}}$$

$$\mathcal{M} = \begin{pmatrix} \sqrt{\frac{1}{2}}\pi^0 + \sqrt{\frac{1}{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\sqrt{\frac{1}{2}}\pi^0 + \sqrt{\frac{1}{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\sqrt{\frac{2}{3}}\eta \end{pmatrix}$$

Analogous terms describe interactions involving radial excitation doublets: $g \rightarrow \tilde{g}$, $h \rightarrow \tilde{h}, \dots$

$D_{sJ}(2860)$: results for width ratios

P. Colangelo, S. Nicotri, FDF
PLB 642, 48

	$D_{sJ}(2860)$	$D_{sJ}(2860) \rightarrow DK$	$\frac{\Gamma(D_{sJ}(2860) \rightarrow D^* K)}{\Gamma(D_{sJ}(2860) \rightarrow DK)}$	$\frac{\Gamma(D_{sJ}(2860) \rightarrow D_s \eta)}{\Gamma(D_{sJ}(2860) \rightarrow DK)}$
1	$s_l^P = \frac{1}{2}^-, J^P = 1^-, n = 2$	p-wave	1.23	0.27
2	$s_l^P = \frac{1}{2}^+, J^P = 0^+, n = 2$	s-wave	0	0.34
3	$s_l^P = \frac{3}{2}^+, J^P = 2^+, n = 2$	d-wave	0.63	0.19
4	$s_l^P = \frac{3}{2}^-, J^P = 1^-, n = 1$	p-wave	0.06	0.23
5	$s_l^P = \frac{5}{2}^-, J^P = 3^-, n = 1$	f-wave	0.39	0.13

Would explain the observed narrowness

$D_{sJ}(2860)$

Our supported option:

5

$$s_\ell^P = \frac{5}{2}^-, J^P = 3^-, n = 1$$

- **Signal expected in D^*K**
- Small signal expected also in $D_s \eta$

In this case the small width can be attributed to the suppression due to the kaon momentum factor:

$$\Gamma(D_{sJ} \rightarrow DK) = \frac{6}{35} \frac{(k_1 + k_2)^2}{\pi f_\pi^2 \Lambda_\chi^4} \frac{M_D}{M_{D_{sJ}}} q_K^7 \left. \vphantom{\Gamma(D_{sJ} \rightarrow DK)} \right\} \text{f-wave transition}$$



Assuming the experimentally measured width would predict in the typical range of these couplings $k_1 + k_2 \approx 0.5$

The spin 2 partner could decay in p-wave due to the effect of $1/m_Q$ corrections



may escape detection

Our conclusion:

$D_{sJ}(2860)$ is likely to be a $J^P=3^-$ state



Should decay to D^*K

Identifying $D_{sJ}(2710)$ through its decay modes

P. Colangelo, S. Nicotri, M. Rizzi, FDF
Phys. Rev. D77, 014012

$$R_1 = \frac{\Gamma(D_{sJ} \rightarrow D^* K)}{\Gamma(D_{sJ} \rightarrow DK)}$$

$$R_2 = \frac{\Gamma(D_{sJ} \rightarrow D_s \eta)}{\Gamma(D_{sJ} \rightarrow DK)}$$

$$R_3 = \frac{\Gamma(D_{sJ} \rightarrow D_s^* \eta)}{\Gamma(D_{sJ} \rightarrow DK)}$$



the dependence on the (unknown) couplings drops out

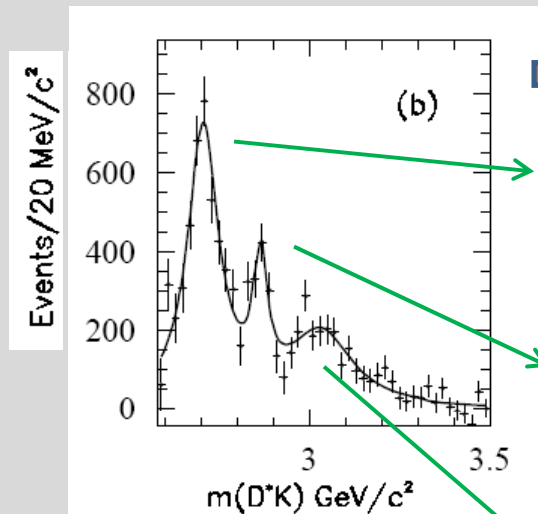
	$R_1 \times 10^2$	$R_2 \times 10^2$	$R_3 \times 10^2$
$D_s^{*'}$	91 ± 4	20 ± 1	5 ± 2
D_{s1}^*	4.3 ± 0.2	16.3 ± 0.9	0.18 ± 0.07



The $D^* K$ decay is the signal that must be investigated in order to distinguish the two possible assignments

BaBar Analysis of D^*K final states

- D^*K invariant mass spectrum (background-subtracted)



Three peaks are visible:

$$m(D_{s1}^*(2710)^+) = 2710 \pm 2_{stat} \pm 12_{syst} \text{ MeV}$$

$$\Gamma(D_{s1}^*(2710)^+) = 149 \pm 7_{stat} \pm 52_{syst} \text{ MeV}$$

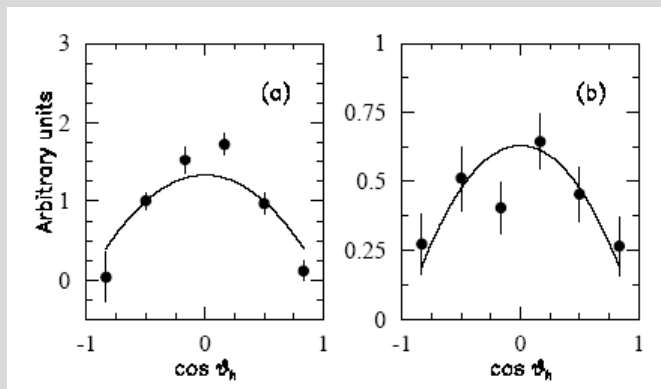
$$m(D_{sJ}(2860)^+) = 2862 \pm 2_{stat} \pm 5_{syst} \text{ MeV}$$

$$\Gamma(D_{sJ}(2860)^+) = 48 \pm 3_{stat} \pm 6_{syst} \text{ MeV}$$

$$m(D_{sJ}(3040)^+) = 3044 \pm 8_{stat} \pm 30_{syst} \text{ MeV}$$

$$\Gamma(D_{sJ}(3040)^+) = 239 \pm 35_{stat} \pm 46_{syst} \text{ MeV}$$

- angular analysis



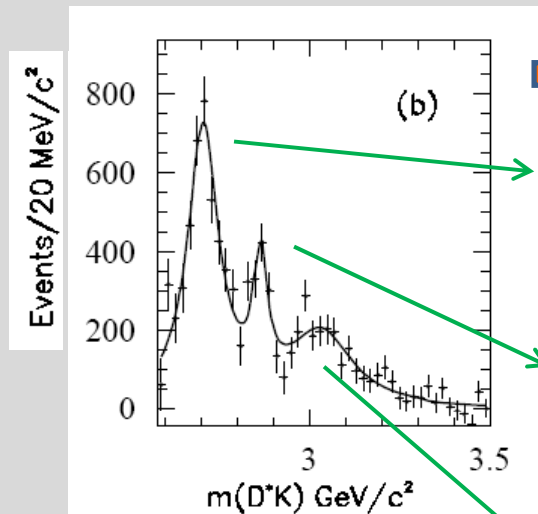
The angular distribution is consistent with the expectations for states with natural parity ($0^+, 1^-, 2^+, 3^-, \dots$) for $D_{s1}(2710)$ and $D_{sJ}(2860)$

excluded by the observation of the D^*K mode

BaBar, PRD80 (09)092003

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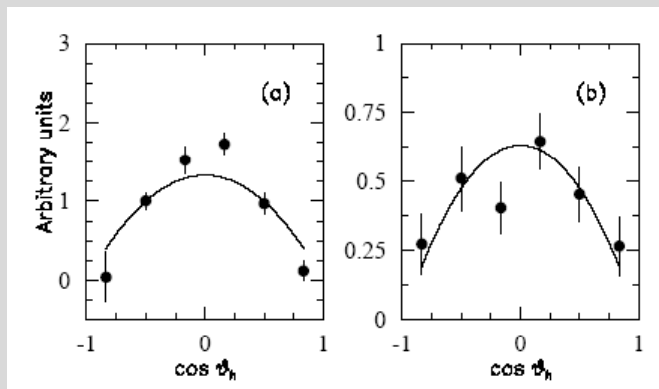
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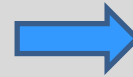
BaBar, PRD80 (09)092003

to be discussed later...

BaBar Analysis of D^*K final states

Branching fractions

$$\frac{B(D_{s1}(2710)^+ \rightarrow D^*K)}{B(D_{s1}(2710)^+ \rightarrow DK)} = 0.91 \pm 0.13_{stat} \pm 0.12_{syst}$$



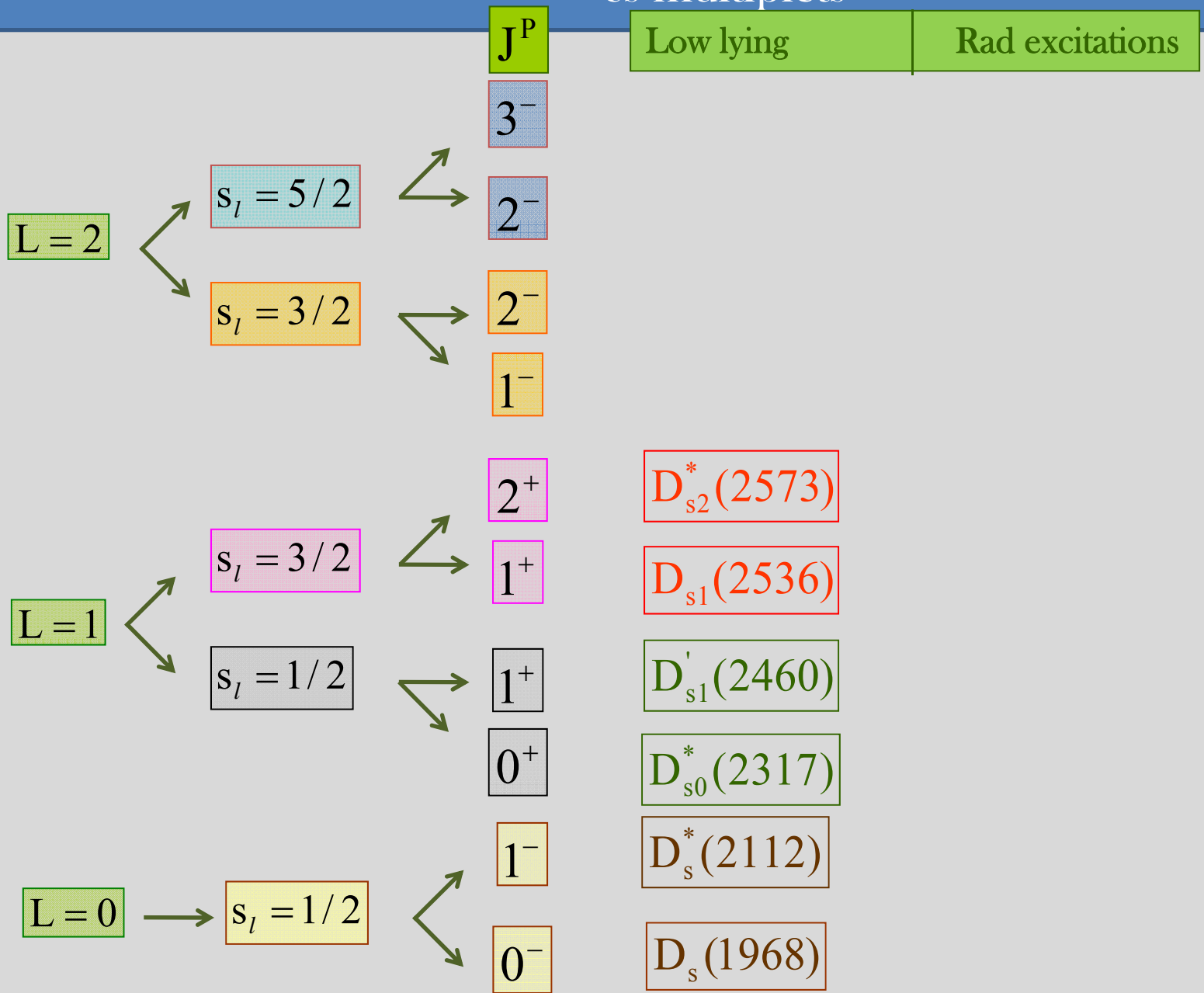
Supports the identification of $D_{s1}(2710)$ with 2^3S_1 (first radial excitation of D_s^*)

$$\frac{B(D_{sJ}(2860)^+ \rightarrow D^*K)}{B(D_{sJ}(2860)^+ \rightarrow DK)} = 1.10 \pm 0.15_{stat} \pm 0.19_{syst}$$

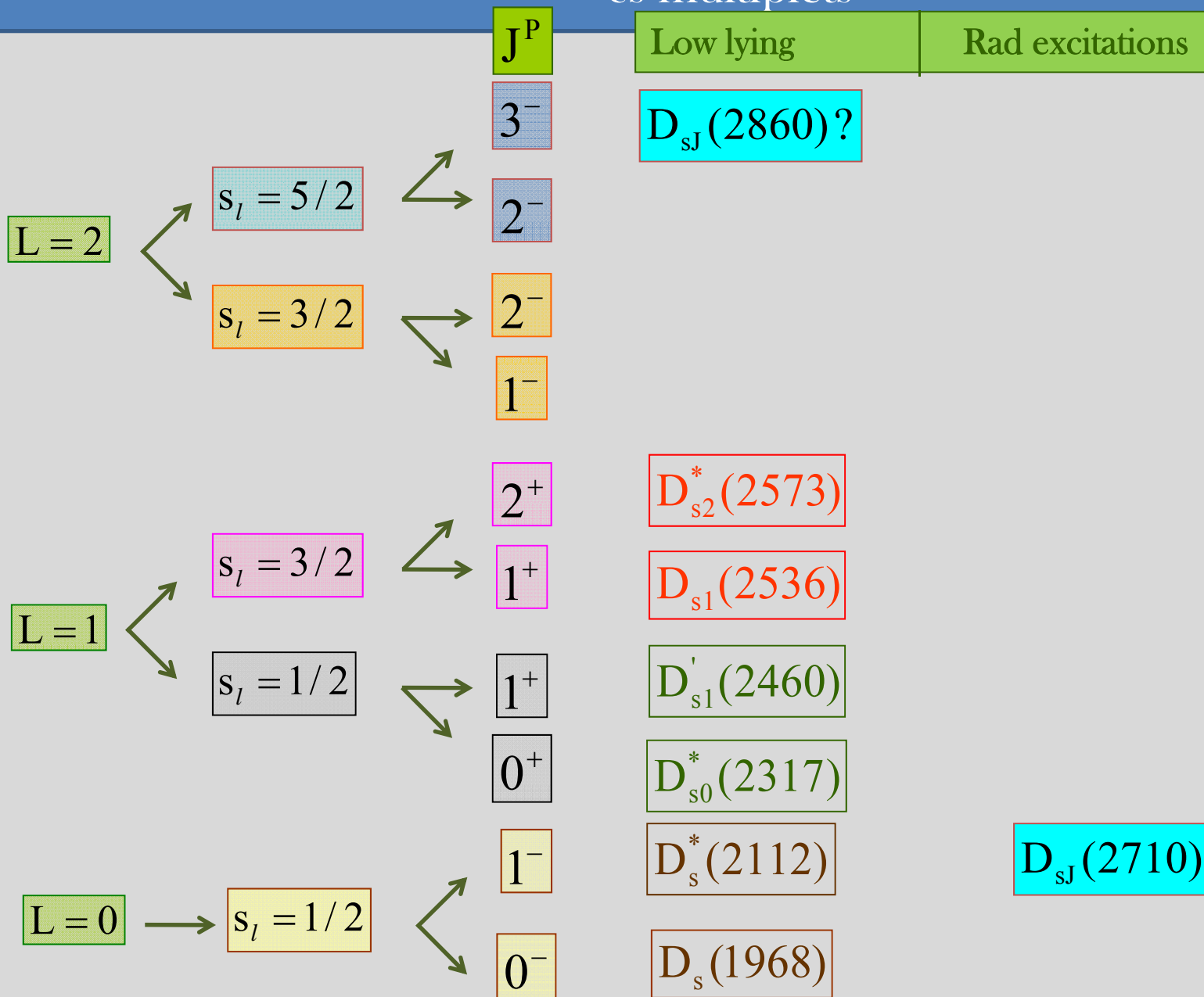


Does not support or discard unambiguously any interpretation:
still to be understood

$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$c\bar{q}$ mesons

BaBar observes four new states with charm and without strangeness:

BaBar, PRD 82 (10) 111101

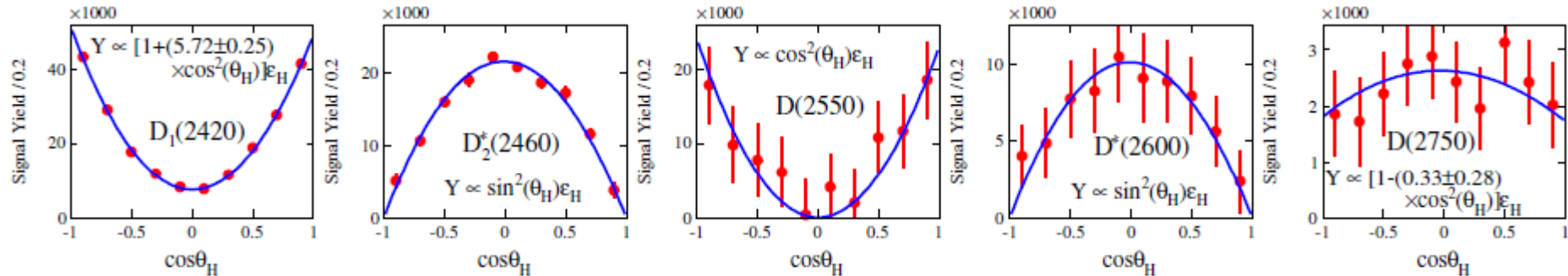
state	Mass (MeV)	Width (MeV)	decays to
$D(2550)^0$	$2539.4 \pm 4.5 \pm 6.8$	$130 \pm 12 \pm 13$	$D^{*+}\pi^-$
$D^*(2600)^0$	$2608.7 \pm 2.4 \pm 2.7$	$93 \pm 6 \pm 13$	$D^+\pi^-, D^{*+}\pi^-$
$D^*(2600)^+$	$2608.7 \pm 2.4 \pm 2.7$	$93 \pm 6 \pm 13$	$D^0\pi^+$
$D(2750)^0$	$2752.4 \pm 1.7 \pm 2.7$	$71 \pm 6 \pm 11$	$D^{*+}\pi^-$
$D^*(2760)^0$	$2763.3 \pm 2.3 \pm 2.3$	$60.9 \pm 5.1 \pm 3.6$	$D^+\pi^-$
$D^*(2760)^+$	$2769.7 \pm 3.8 \pm 1.5$	$60.9 \pm 5.1 \pm 3.6$	$D^0\pi^+$

$c\bar{q}$ mesons

Study of the distribution in the helicity angle θ_H for the final state $D^* \pi$

BaBar, PRD 82 (10) 111101

Angle between the primary π and the slow π from D^* decay



Godfrey & Isgur (85)

State	Predicted mass	J^P	$\cos\theta_H$ distribution
$D_0^1(2S)$	2.58 GeV/ c^2	0^-	$\propto \cos^2\theta_H$
$D_1^3(2S)$	2.64 GeV/ c^2	1^-	$\propto \sin^2\theta_H$
$D_1^1(1P)$	2.44 GeV/ c^2	1^+	$\propto 1 + h\cos^2\theta_H$
$D_0^3(1P)$	2.40 GeV/ c^2	0^+	Decay not allowed
$D_1^3(1P)$	2.49 GeV/ c^2	1^+	$\propto 1 + h\cos^2\theta_H$
$D_2^3(1P)$	2.50 GeV/ c^2	2^+	$\propto \sin^2\theta_H$
$D_2^1(1D)$	~ 2.83 GeV/ c^2	2^-	$\propto 1 + h\cos^2\theta_H$
$D_1^3(1D)$	2.82 GeV/ c^2	1^-	$\propto \sin^2\theta_H$
$D_2^3(1D)$	~ 2.83 GeV/ c^2	2^-	$\propto 1 + h\cos^2\theta_H$
$D_3^3(1D)$	2.83 GeV/ c^2	3^-	$\propto \sin^2\theta_H$



Consistent with assignments of

- Natural parity for $D^*(2600)$
- $J^P=0^+$ for $D(2550)$

Comparison with potential model
Seems to indicate that
($D(2750), D^*(2760)$) are $L=2$ states

$c\bar{q}$ mesons

BaBar observes four new states with charm and without strangeness:

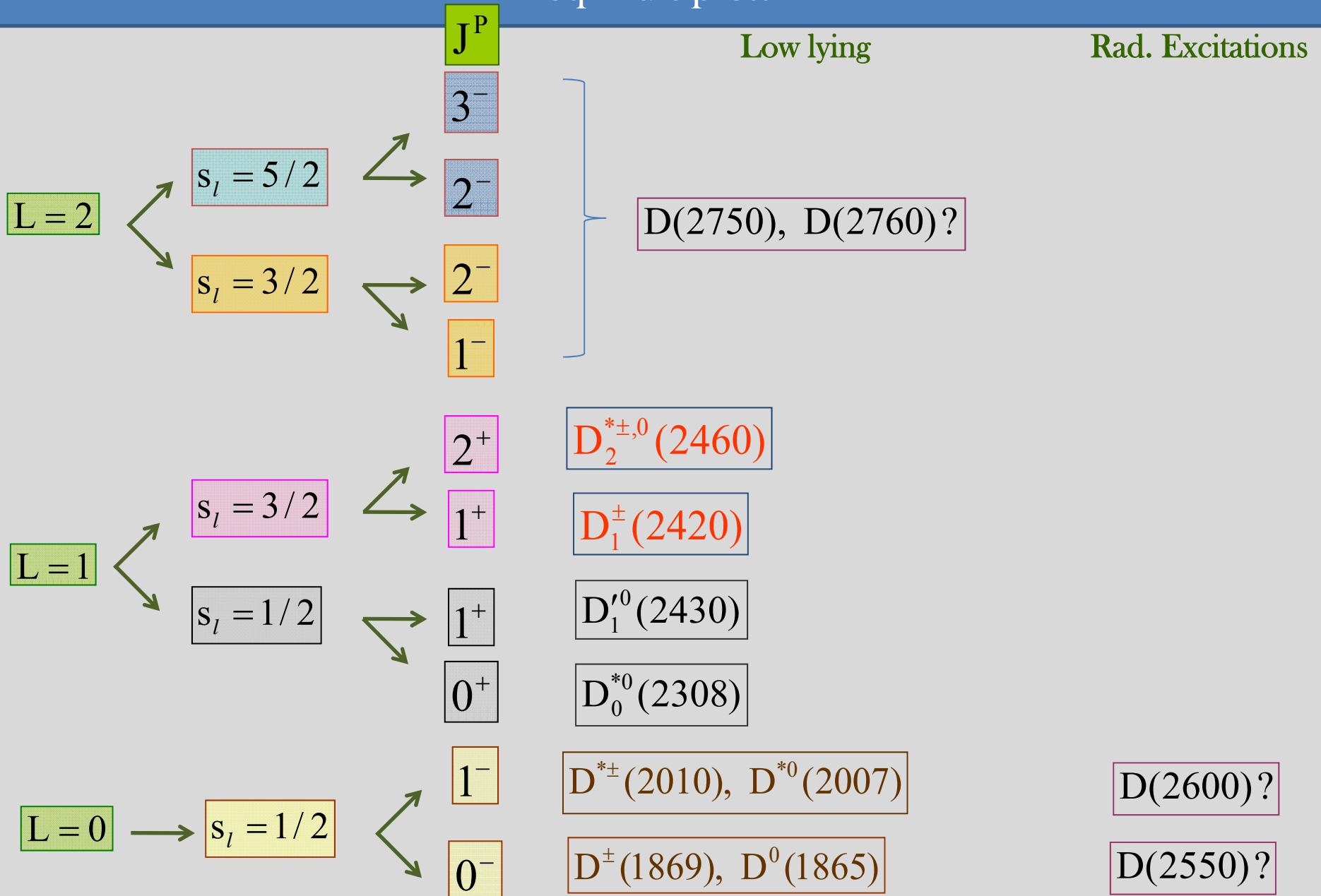
BaBar, PRD 82 (10) 111101

state	Mass (MeV)	Width (MeV)	decays to
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$D^*(2600)^+$	$2608.7 \pm 2.4 \pm 2.7$	$93 \pm 6 \pm 13$	$D^0\pi^+$
$D(2750)^0$	$2752.4 \pm 1.7 \pm 2.7$	$71 \pm 6 \pm 11$	$D^{*+}\pi^-$
$D^*(2760)^0$	$2763.3 \pm 2.3 \pm 2.3$	$60.9 \pm 5.1 \pm 3.6$	$D^+\pi^-$
$D^*(2760)^+$	$2769.7 \pm 3.8 \pm 1.5$	$60.9 \pm 5.1 \pm 3.6$	$D^0\pi^+$

likely to be L=2 states

likely to be the radial excitations of (D,D*)

$c\bar{q}$ multiplets



Experimental ratios:

$$\frac{B(D^*(2600)^0 \rightarrow D^+ \pi^-)}{B(D^*(2600)^0 \rightarrow D^{*+} \pi^-)} = 0.32 \pm 0.02 \pm 0.09,$$
$$\frac{B(D^*(2760)^0 \rightarrow D^+ \pi^-)}{B(D(2750)^0 \rightarrow D^{*+} \pi^-)} = 0.42 \pm 0.05 \pm 0.11.$$



These ratios together with masses and widths can be used to check the BaBar assignments

Branching fraction Ratio

P. Colangelo & FDF, in preparation

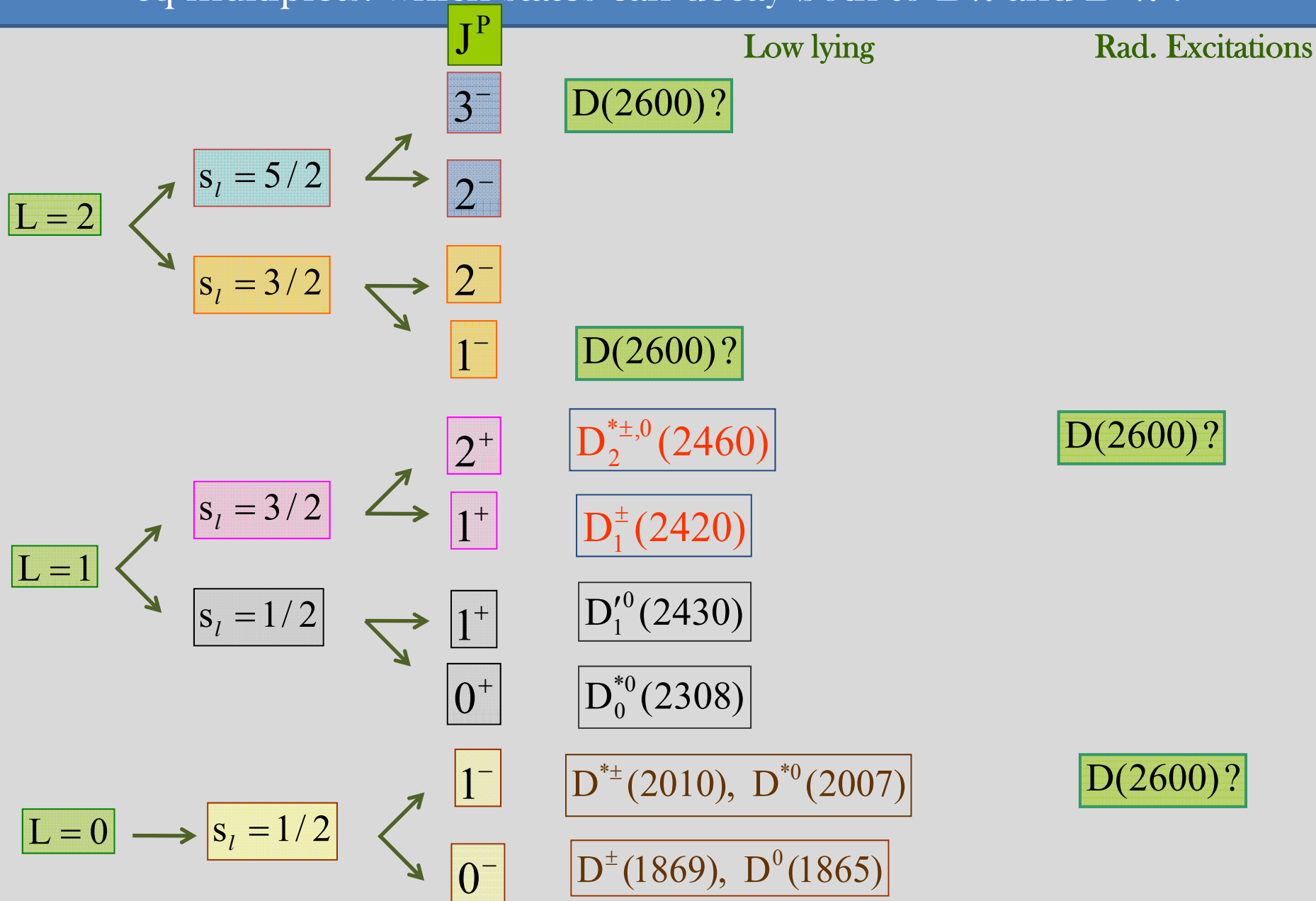
Identifying $D^{*0}(2600)$ with the first radial excitation of D^{*0}
we obtain:

$$\frac{\mathcal{B}(D^{*0}(2600) \rightarrow D^+\pi^-)}{\mathcal{B}(D^{*0}(2600) \rightarrow D^{*+}\pi^-)} = 0.822 \pm 0.003$$

while BaBar finds:

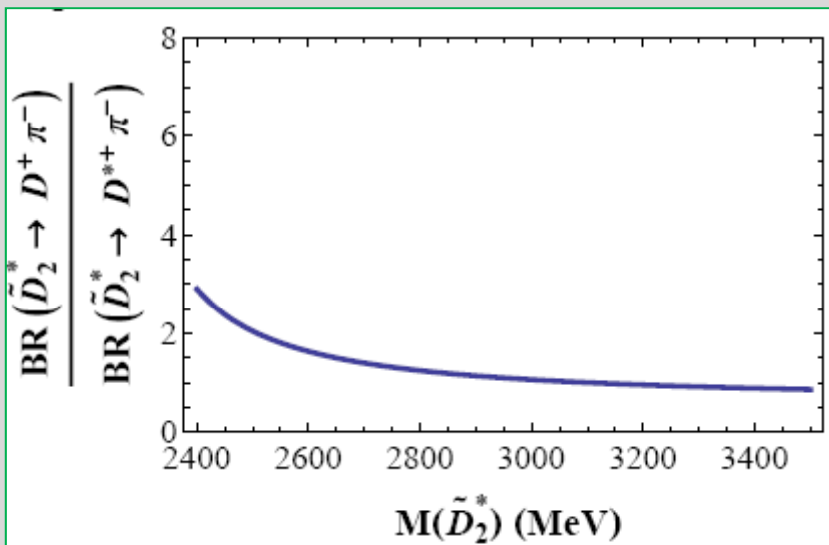
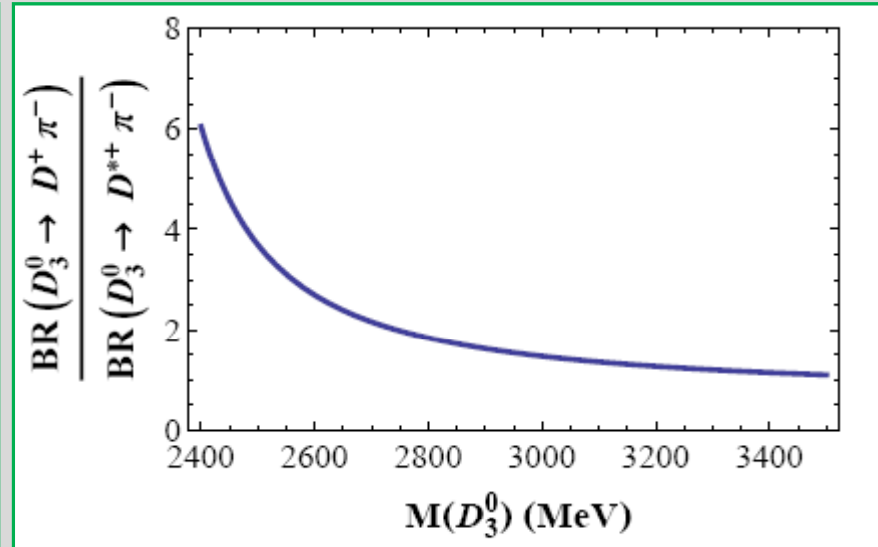
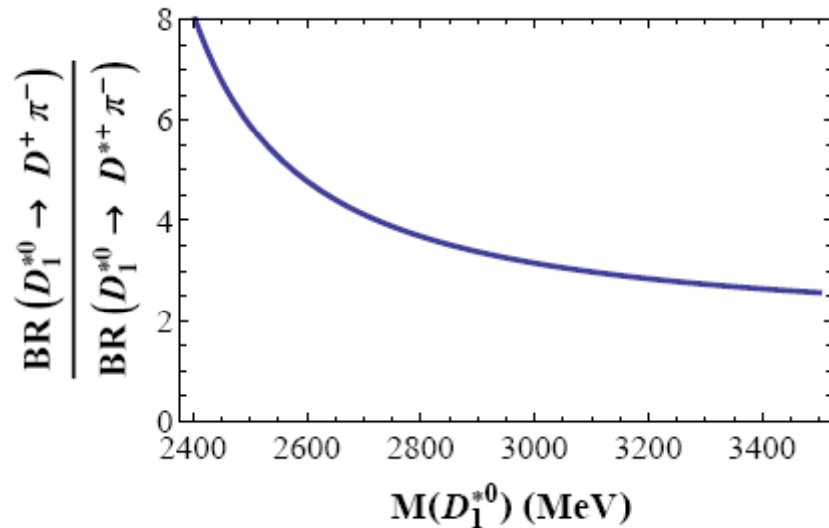
$$\frac{\mathcal{B}(D^{*0}(2600) \rightarrow D^+\pi^-)}{\mathcal{B}(D^{*0}(2600) \rightarrow D^{*+}\pi^-)} = 0.32 \pm 0.02 \pm 0.09$$

$c\bar{q}$ multiplets: which states can decay both to $D\pi$ and $D^*\pi$?



$c\bar{q}$ multiplets: which states can decay both to $D\pi$ and $D^*\pi$?

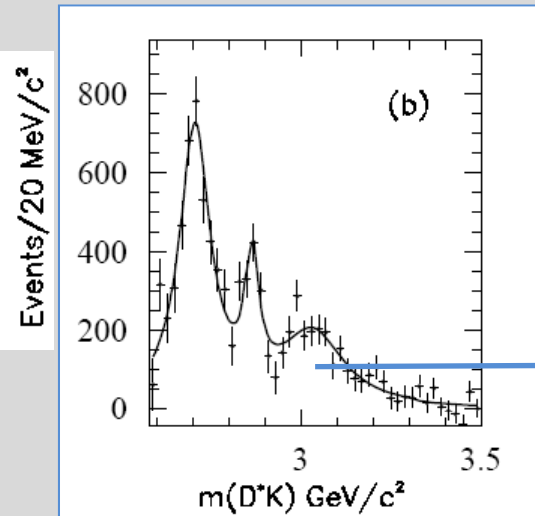
Branching fraction ratios for the other three possibilities: vs the mass of the decaying meson



No assignment to a meson of mass 2600 MeV would reproduce the exp result:

Either HQ symmetry is strongly violated or a revision of the experimental analysis is required

$D_{sJ}(3040)$



$$M(D_{sJ}(3040)) = 3044 \pm 8_{\text{stat}} \left(\begin{smallmatrix} +30 \\ -5 \end{smallmatrix} \right)_{\text{syst}} \text{ MeV}$$
$$\Gamma(D_{sJ}(3040)) = 239 \pm 35_{\text{stat}} \left(\begin{smallmatrix} +46 \\ -42 \end{smallmatrix} \right)_{\text{syst}} \text{ MeV}$$

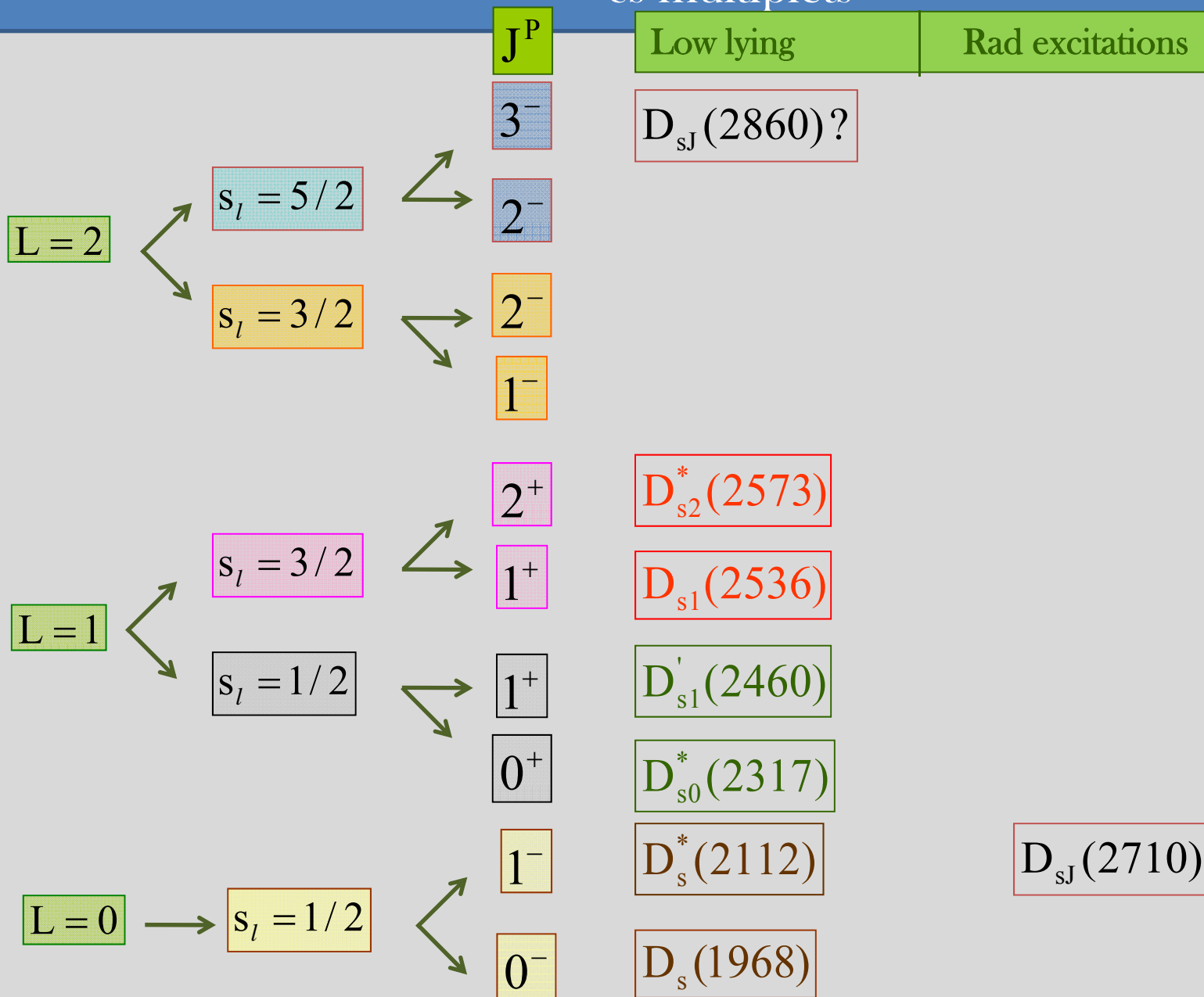
The only additional information is that it decays

$\rightarrow D^*K$	YES
$\rightarrow DK$	NO

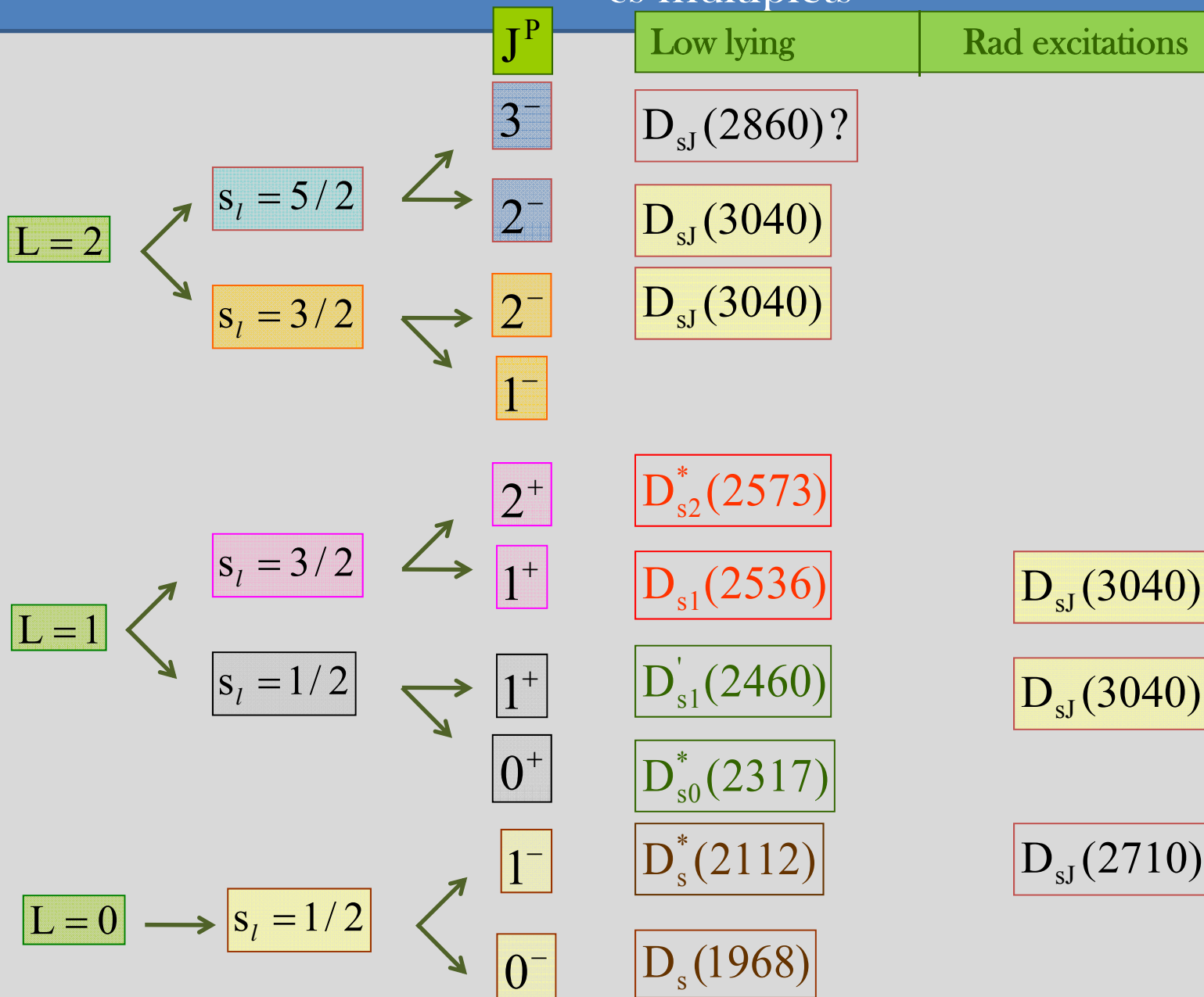


$$J^P = 1^+, 2^-, 3^+, \dots$$

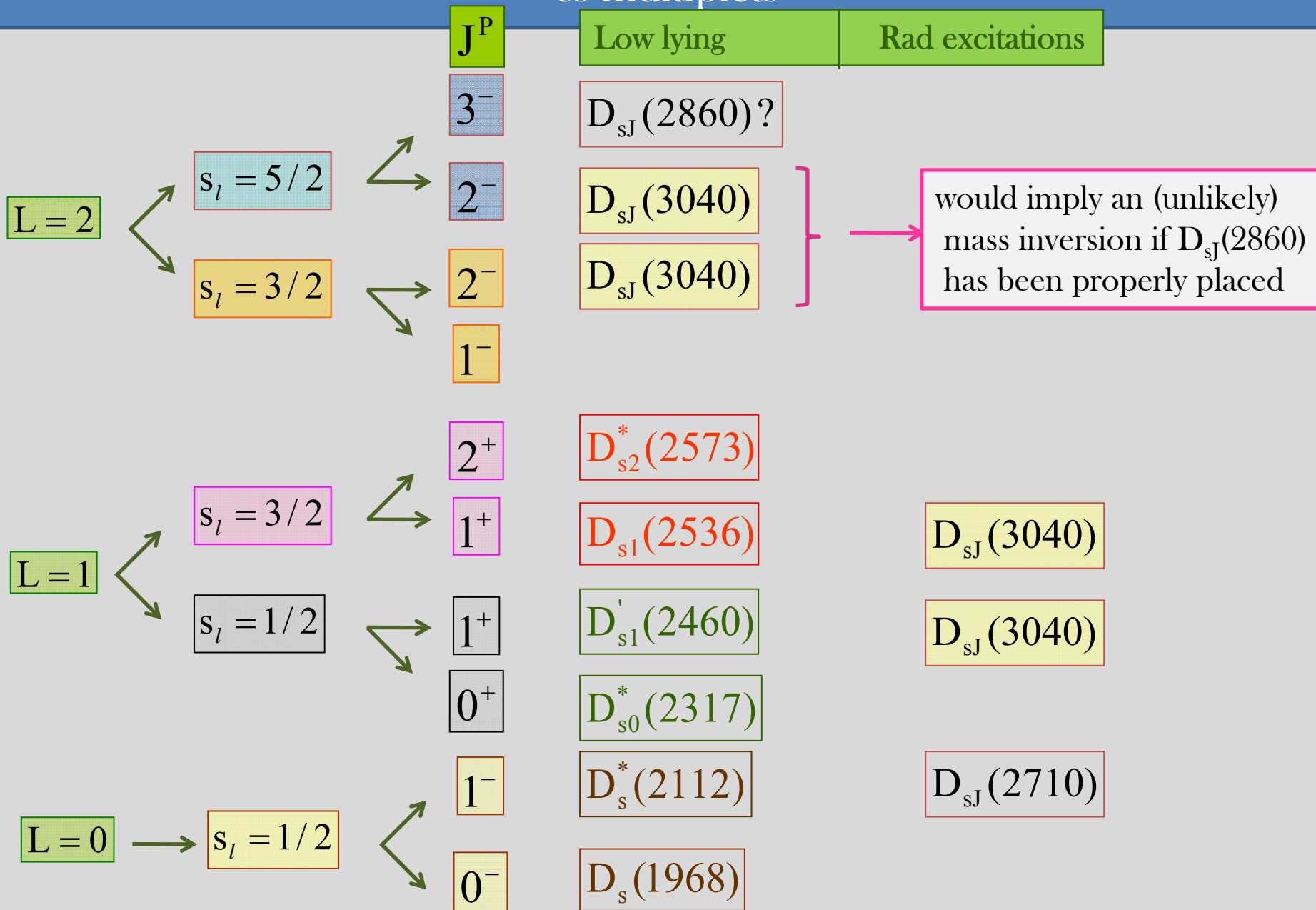
$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$c\bar{s}$ multiplets



$D_{sJ}(3040)$: how to discriminate among the four possibilities?

- info from Relativistic Quark Model (RQM)

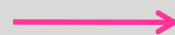


$$\begin{aligned}
 M(\tilde{D}_{s1})^{(\text{RQM})} &= 3114 \text{ MeV}, \\
 M(\tilde{D}'_{s1})^{(\text{RQM})} &= 3165 \text{ MeV}, \\
 M(D_{s2})^{(\text{RQM})} &= 2953 \text{ MeV}, \\
 M(D_{s2}^{*'})^{(\text{RQM})} &= 2900 \text{ MeV}.
 \end{aligned}$$

- Allowed strong decays:

- to $D_{(s)}^*$ + light pseudoscalar meson

$$D^*K, D_{s1}^*\eta$$



$$R_1 = \frac{\Gamma(D_{sJ}(3040) \rightarrow D_s^* \eta)}{\Gamma(D_{sJ}(3040) \rightarrow D^* K)}$$

- to members of higher doublets + a light pseudoscalar meson

$$\begin{aligned}
 &D_0^*K, D_{s0}^*, D_1'K \\
 &D_1K, D_2^*K
 \end{aligned}$$

- to $D_{(s)}$ + a light vector meson

$$DK^*, D_s \phi$$

$D_{sJ}(3040)$: how to discriminate among the four possibilities?

Decay modes	$\tilde{D}'_{s1} (n = 2, J_{s\ell}^P = 1_{1/2}^+)$	$\tilde{D}_{s1} (n = 2, J_{s\ell}^P = 1_{3/2}^+)$	$D_{s2} (n = 1, J_{s\ell}^P = 2_{3/2}^-)$	$D_{s2}^* (n = 1, J_{s\ell}^P = 2_{5/2}^-)$
$D^*K, D_s^*\eta$	s wave	d wave	p wave	f wave
R_1	0.34	0.20	0.245	0.143
$D_0^*K, D_{s0}^*\eta, D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	...	d wave
D_2^*K	p wave	p wave	s wave	d wave
$DK^*, D_s\phi$	s wave $\Gamma \simeq 140$ MeV	s wave $\Gamma \simeq 20$ MeV	p wave Negligible	p wave Negligible
Spin partner				
	$\tilde{D}_{s0}^* (n = 2, J_{s\ell}^P = 0_{1/2}^+)$	$\tilde{D}_{s2}^* (n = 2, J_{s\ell}^P = 2_{3/2}^+)$	$D_{s1}^* (n = 1, J_{s\ell}^P = 1_{3/2}^-)$	$D_{s3} (n = 1, J_{s\ell}^P = 3_{5/2}^-)$
$DK, D_s\eta$	s wave	d wave	p wave	f wave
$D^*K, D_s^*\eta$...	d wave	p wave	f wave
$D_0^*K, D_{s0}^*\eta$	d wave	...
$D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
D_2^*K	...	p wave	...	d wave

- \tilde{D}'_{s1} decays in s -wave to $D^*K, D_s^*\eta$ (broader), has the largest R_1 , the largest width to light vector mesons

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$D_{sJ}(3040)$: how to discriminate among the four possibilities?

Decay modes	$\tilde{D}'_{s1} (n = 2, J_{s\ell}^P = 1_{1/2}^+)$	$\tilde{D}_{s1} (n = 2, J_{s\ell}^P = 1_{3/2}^+)$	$D_{s2} (n = 1, J_{s\ell}^P = 2_{3/2}^-)$	$D_{s2}^* (n = 1, J_{s\ell}^P = 2_{5/2}^-)$
$D^*K, D_s^*\eta$	s wave	d wave	p wave	f wave
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$D_0^*K, D_{s0}^*\eta, D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	...	d wave
D_2^*K	p wave	p wave	s wave	d wave
$DK^*, D_s\phi$	s wave $\Gamma \simeq 140$ MeV	s wave $\Gamma \simeq 20$ MeV	p wave Negligible	p wave Negligible
Spin partner				
	$\tilde{D}_{s0}^* (n = 2, J_{s\ell}^P = 0_{1/2}^+)$	$\tilde{D}_{s2}^* (n = 2, J_{s\ell}^P = 2_{3/2}^+)$	$D_{s1}^* (n = 1, J_{s\ell}^P = 1_{3/2}^-)$	$D_{s3} (n = 1, J_{s\ell}^P = 3_{5/2}^-)$
$DK, D_s\eta$	s wave	d wave	p wave	f wave
$D^*K, D_s^*\eta$...	d wave	p wave	f wave
$D_0^*K, D_{s0}^*\eta$	d wave	...
$D_1'K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
D_2^*K	...	p wave	...	d wave

- \tilde{D}'_{s1} decays in s-wave to $D^*K, D_s^*\eta$ (broader), has the largest R_1 , the largest width to light vector mesons

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- the two 2^- states should not be observed in the decay to light vector mesons

$D_{sJ}(3040)$: how to discriminate among the four possibilities?

Decay modes	$\tilde{D}'_{s1} (n = 2, J_{s\ell}^P = 1_{1/2}^+)$	$\tilde{D}_{s1} (n = 2, J_{s\ell}^P = 1_{3/2}^+)$	$D_{s2} (n = 1, J_{s\ell}^P = 2_{3/2}^-)$	$D_{s2}^* (n = 1, J_{s\ell}^P = 2_{5/2}^-)$
$D^*K, D_s^*\eta$	s wave 0.34	d wave 0.20	p wave 0.245	f wave 0.143
R_1				
$D_0^*K, D_{s0}^*\eta, D_1^*K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	...	d wave
D_2^*K	p wave	p wave	s wave	d wave
$DK^*, D_s\phi$	s wave $\Gamma \simeq 140$ MeV	s wave $\Gamma \simeq 20$ MeV	p wave Negligible	p wave Negligible
Spin partner				
	$\tilde{D}_{s0}^* (n = 2, J_{s\ell}^P = 0_{1/2}^+)$	$\tilde{D}_{s2}^* (n = 2, J_{s\ell}^P = 2_{3/2}^+)$	$D_{s1}^* (n = 1, J_{s\ell}^P = 1_{3/2}^-)$	$D_{s3} (n = 1, J_{s\ell}^P = 3_{5/2}^-)$
$DK, D_s\eta$	s wave	d wave	p wave	f wave
$D^*K, D_s^*\eta$...	d wave	p wave	f wave
$D_0^*K, D_{s0}^*\eta$	d wave	...
D_1^*K	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
D_2^*K	...	p wave	...	d wave

- \tilde{D}'_{s1} decays in s -wave to $D^*K, D_s^*\eta$ (broader), has the largest R_1 , the largest width to light vector mesons
- the two 2^- states should not be observed in the decay to light vector mesons
- D_{s2} cannot decay to D_1K but should have the largest width to D_2^*K

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$D_{sJ}(3040)$: how to discriminate among the four possibilities?

Decay modes	$\tilde{D}'_{s1} (n = 2, J_{s\ell}^P = 1^+_{1/2})$	$\tilde{D}_{s1} (n = 2, J_{s\ell}^P = 1^+_{3/2})$	$D_{s2} (n = 1, J_{s\ell}^P = 2^-_{3/2})$	$D_{s2}^* (n = 1, J_{s\ell}^P = 2^-_{5/2})$
$D^*K, D_s^*\eta$	s wave 0.34	d wave 0.20	p wave 0.245	f wave 0.143
R_1				
$D_0^*K, D_{s0}^*\eta, D_1^*K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	...	d wave
D_2^*K	p wave	p wave	s wave	d wave
$DK^*, D_s\phi$	s wave $\Gamma \simeq 140$ MeV	s wave $\Gamma \simeq 20$ MeV	p wave Negligible	p wave Negligible
			Spin partner	
	$\tilde{D}_{s0}^* (n = 2, J_{s\ell}^P = 0^+_{1/2})$	$\tilde{D}_{s2}^* (n = 2, J_{s\ell}^P = 2^+_{3/2})$	$D_{s1} (n = 1, J_{s\ell}^P = 1^-_{3/2})$	$D_{s3} (n = 1, J_{s\ell}^P = 3^-_{5/2})$
$DK, D_s\eta$	s wave	d wave	p wave	f wave
$D^*K, D_s^*\eta$...	d wave	p wave	f wave
$D_0^*K, D_{s0}^*\eta$	d wave	...
D_1^*K	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
D_2^*K	...	p wave	...	d wave

- \tilde{D}'_{s1} decays in s -wave to $D^*K, D_s^*\eta$ (broader), has the largest R_1 , the largest width to light vector mesons
- the two 2^- states should not be observed in the decay to light vector mesons
- D_{s2} cannot decay to D_1K but should have the largest width to D_2^*K
- look at the features of the spin partner

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$D_{sJ}(3040)$: how to discriminate among the four possibilities?

Decay modes	$\tilde{D}'_{s1} (n = 2, J_{s\ell}^P = 1_{1/2}^+)$	$\tilde{D}_{s1} (n = 2, J_{s\ell}^P = 1_{3/2}^+)$	$D_{s2} (n = 1, J_{s\ell}^P = 2_{3/2}^-)$	$D_{s2}^* (n = 1, J_{s\ell}^P = 2_{5/2}^-)$
$D^*K, D_s^*\eta$	s wave 0.34	d wave 0.20	p wave 0.245	f wave 0.143
R_1				
$D_0^*K, D_{s0}^*\eta, D_1^*K$	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	...	d wave
D_2^*K	p wave	p wave	s wave	d wave
$DK^*, D_s\phi$	s wave $\Gamma \simeq 140$ MeV	s wave $\Gamma \simeq 20$ MeV	p wave Negligible	p wave Negligible
			Spin partner	
	$\tilde{D}_{s0}^* (n = 2, J_{s\ell}^P = 0_{1/2}^+)$	$\tilde{D}_{s2}^* (n = 2, J_{s\ell}^P = 2_{3/2}^+)$	$D_{s1} (n = 1, J_{s\ell}^P = 1_{3/2}^-)$	$D_{s3} (n = 1, J_{s\ell}^P = 3_{5/2}^-)$
$DK, D_s\eta$	s wave	d wave	p wave	f wave
$D^*K, D_s^*\eta$...	d wave	p wave	f wave
$D_0^*K, D_{s0}^*\eta$	d wave	...
D_1^*K	p wave	p wave	d wave	d wave
D_1K	p wave	p wave	s wave	d wave
D_2^*K	...	p wave	...	d wave

- \tilde{D}'_{s1} decays in s -wave to $D^*K, D_s^*\eta$ (broader), has the largest R_1 , the largest width to light vector mesons
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Concluding remarks

- all the observed $c\bar{s}$ states classified as ordinary mesons
- $D_{sJ}(2700)$ identified with D_s^{**}
- $D_J(2600)$ most likely its non strange partner: BR ratio to be reconsidered
- Still to be understood: $D_{sJ}(2860)$ ($J^P = 3^- ?$)
 $D_{sJ}(3040)$ → various allowed decay modes may help in the classification
- $D(2750)$ and $D(2760)$: probably $L=2$ states