

# Measurement of top quark properties at Tevatron

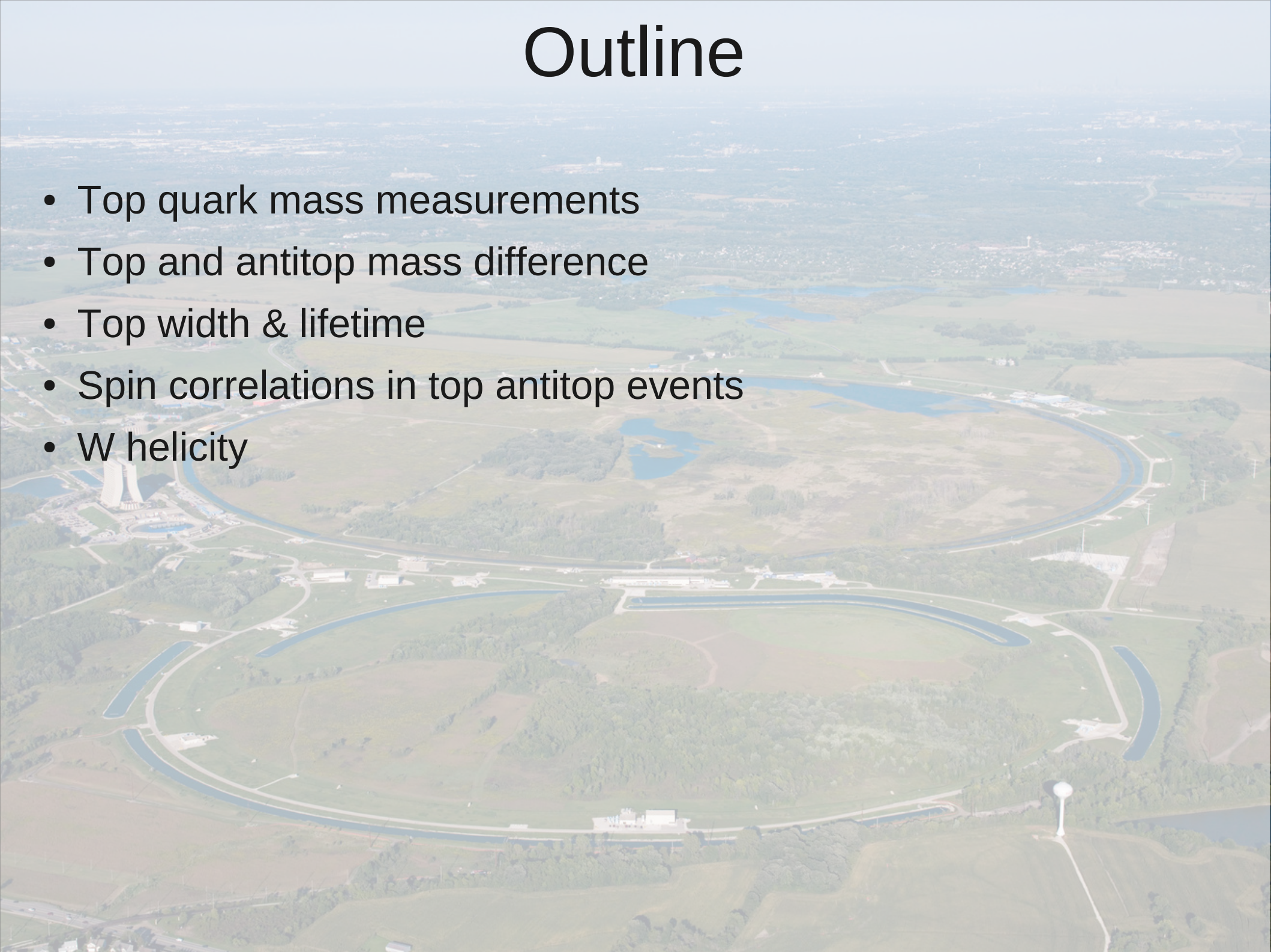
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(Czech Technical University in Prague)  
for DØ and CDF Collaborations

Heavy Quarks and Leptons  
June 11 – 15, 2012

# Outline

- Top quark mass measurements
- Top and antitop mass difference
- Top width & lifetime
- Spin correlations in top antitop events
- W helicity



# RunII (2001-2011)

Chicago

$\sim 10\text{fb}^{-1}$



**Tevatron**  
 $\sqrt{s} = 1.96\text{TeV}$

p

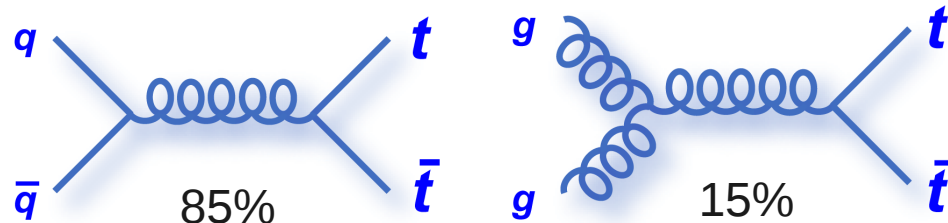
$\bar{p}$

Main injector  
& Recycler

 Fermilab

# Top quark

- High mass and short lifetime
  - good for measuring properties
  - sensitive to physics beyond SM



- Almost  $10\text{fb}^{-1}$  data
  - thousands of events
  - precision measurement of top properties

- SM top quark  $\rightarrow Wb \approx 100\%$ 
  - different final states given by W decay

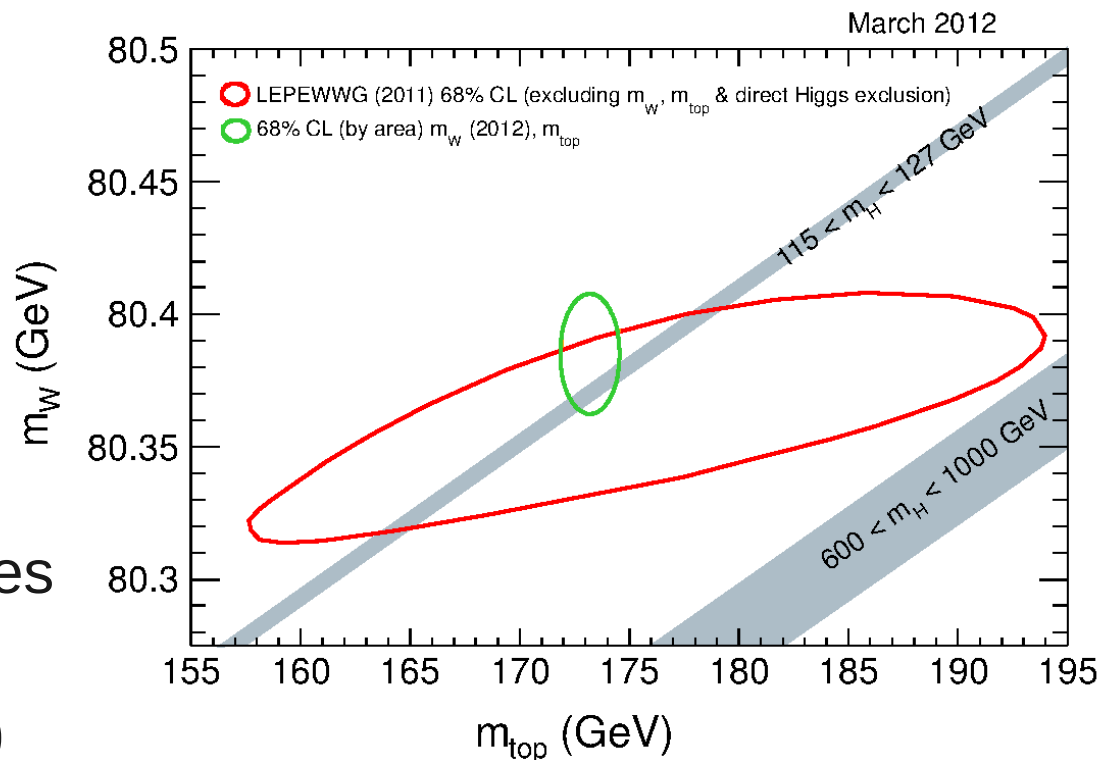
- l+jets  $\sim 30\%$
- dilepton  $\sim 5\%$
- all-jets  $\sim 46\%$
- tau

Top Pair Decay Channels

$\bar{c}s$	electron+jets	muon+jets	tau+jets	all-hadronic	
$\bar{u}d$					
$\tau^-$					
$\mu^-$	$e\mu$	$\mu\mu$	$\mu\tau$	muon+jets	
$e^-$	$e\tau$	$e\mu$	$e\tau$	electron+jets	
$W$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$

# Top mass

- Free parameter in SM
- With  $W$ -boson mass constraints on the SM Higgs
- Two main methods
  - template method – compare distribution of an observable in data with MC  $s+b$  templates for different masses
  - matrix element method (ME)
    - calculate per event signal & background probabilities for given top mass using convolution of leading order matrix element and transfer function that describes detector resolution
    - only main backgrounds (ME requires significant CPU time)
    - ensemble tests + calibration (using only LO approximation)
- Reduce JES uncertainty by in situ calibration using  $W$  boson mass

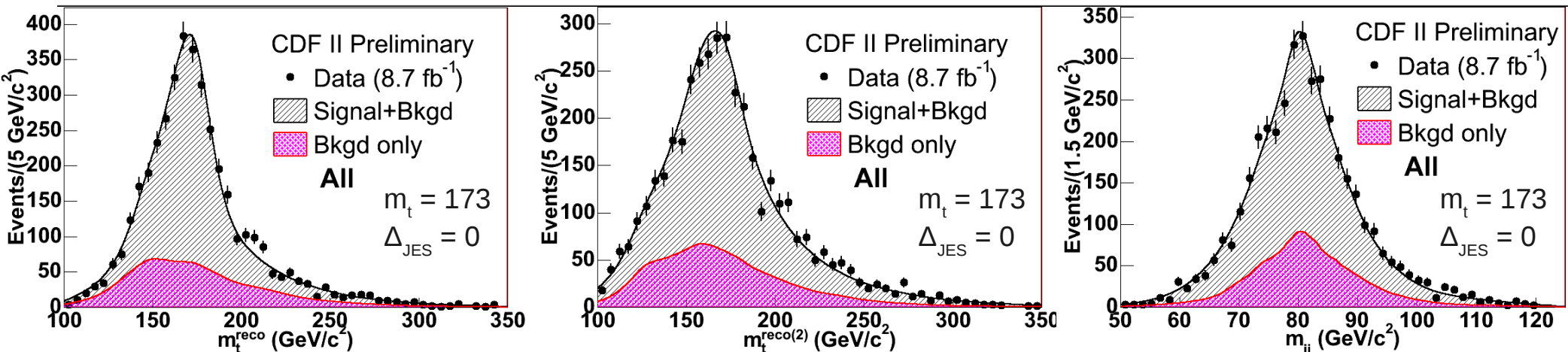


# Mass in l+jets channel

all data

- Template method with full CDF RunII dataset  $8.7\text{fb}^{-1}$
- Minimize  $\chi^2$  to kinematics of the  $t\bar{t}$  system
- Templates  $(m_t^{\text{reco}}, m_t^{\text{reco}(2)}, m_{jj})$  for signal and background
  - $m_t \times \Delta_{\text{JES}}$  grid, for 0,1,2 b tagged jets and 4 or >4 jets
- Maximum likelihood – product of per event probabilities
  - product over all categories, quadratic fit on  $(m_t \times \Delta_{\text{JES}}$  grid)

	0-tag	1-tagL	1-tagT	2-tagL	2-tagT
W+jets,QCD,...	$963.5 \pm 229.3$	$234.7 \pm 61.1$	$144.0 \pm 40.9$	$19.9 \pm 5.5$	$13.8 \pm 4.2$
$t\bar{t}$	$644.8 \pm 86.3$	$695.0 \pm 86.7$	$867.3 \pm 107.6$	$192.3 \pm 29.7$	$303.7 \pm 46.6$
Observed Events	1627	882	997	208	275



# Mass in l+jets channel

- Jet Energy Scale dominant systematic
  - in-situ – only global scale of JES
  - special JES for jet from b quark
  - NN to improve calorimeter energy based on momentum provided by tracker

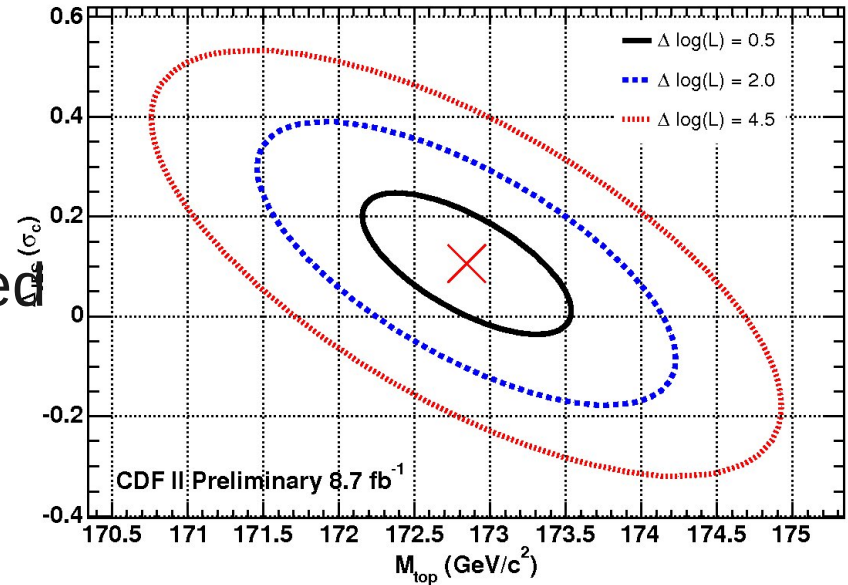
- Systematically dominated

- Most precise single method

$172.85 \pm 0.71(\text{stat}) \pm 0.84(\text{syst}) \text{ GeV}/c^2$   
 $172.85 \pm 1.10 \text{ GeV}/c^2$  (precision  $\pm 0.64\%$ )



CDF Note 10761 (2012)



CDF II Preliminary 8.7 fb<sup>-1</sup>

Systematic	GeV/c <sup>2</sup>
Residual JES	0.52
Generator	0.56
Next Leading Order	0.09
PDFs	0.08
b jet energy	0.10
b tagging efficiency	0.03
Background shape	0.20
gg fraction	0.03
Radiation	0.06
MC statistics	0.05
Lepton energy	0.03
MHI	0.07
Color Reconnection	0.21
Total systematic	0.84

- Matrix element method used by DØ on 3.6fb<sup>-1</sup>
  - flavor dependent jet energy scale


$174.94 \pm 0.83(\text{stat}) \pm 0.78(\text{JES}) \pm 0.96(\text{syst}) \text{ GeV}/c^2$   
 $174.94 \pm 1.49 \text{ GeV}/c^2$  (precision  $\pm 0.85\%$ )



PRD 84, 032004 (2011)


# Mass in dilepton channel

- Neutrino weighting,  $5.3\text{fb}^{-1}$ 
  - kinematically underconstrained
    - can't use in situ calibration
    - using the one from  $l+jets$
    - integration over  $\eta$  distribution of both neutrinos  $\rightarrow$  kinematics solutions + weight (MET)
  - independently  $ee$ ,  $e\mu$ ,  $\mu\mu$
  - JES still main systematic uncertainty
  - most precise in dilepton (stat. limited)

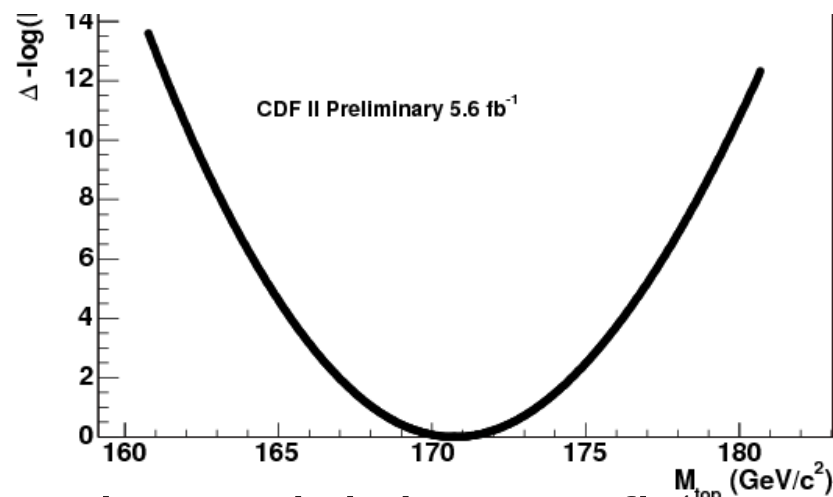
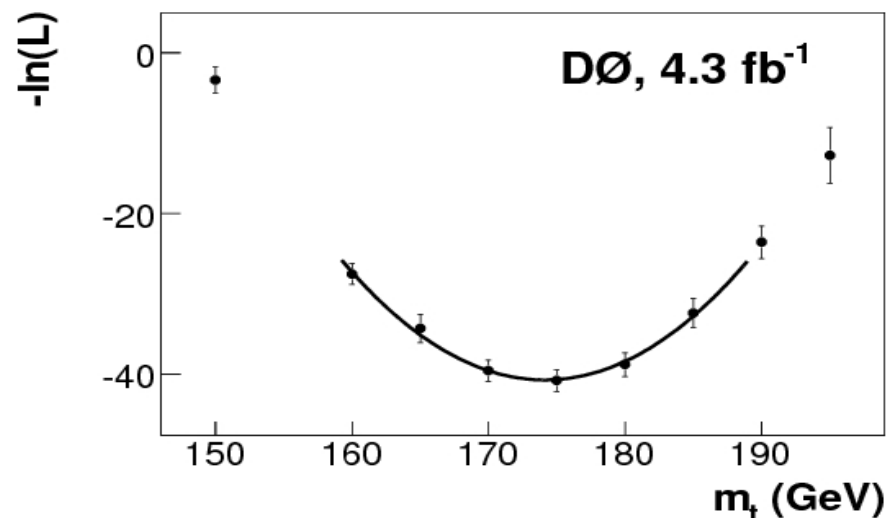
$174.0 \pm 2.4$  (stat)  $\pm 1.4$  (syst)  $\text{GeV}/c^2$    
 $174.0 \pm 2.8$   $\text{GeV}/c^2$  (precision  $\pm 1.6\%$ )

submitted to PRL (2012), arXiv 1201.5172


- Matrix Element,  $5.4\text{fb}^{-1}$

$173.3 \pm 1.8$ (stat)  $\pm 2.4$ (syst)  $\text{GeV}/c^2$    
 $173.3 \pm 3.0$   $\text{GeV}/c^2$  (precision  $\pm 1.8\%$ )

PRL 107, 082004 (2011)



- Neutrino weighting,  $5.3\text{fb}^{-1}$

$170.3 \pm 2.0$ (stat)  $\pm 3.1$ (syst)  $\text{GeV}/c^2$    
 $170.3 \pm 3.7$   $\text{GeV}/c^2$  (precision  $\pm 2.2\%$ )

PRL 107, 082004 (2011)



# Mass in all-jets channel

- Template method with in situ JES,  $5.8\text{fb}^{-1}$ 
  - 6-8 jets (consider leading 6)
  - NN to select signal

b-tagging	Signal	Background	Observed
1-tag	$1712 \pm 77$	$604 \pm 50$	2256
$\geq 2$ -tags	$305 \pm 22$	$316 \pm 26$	600

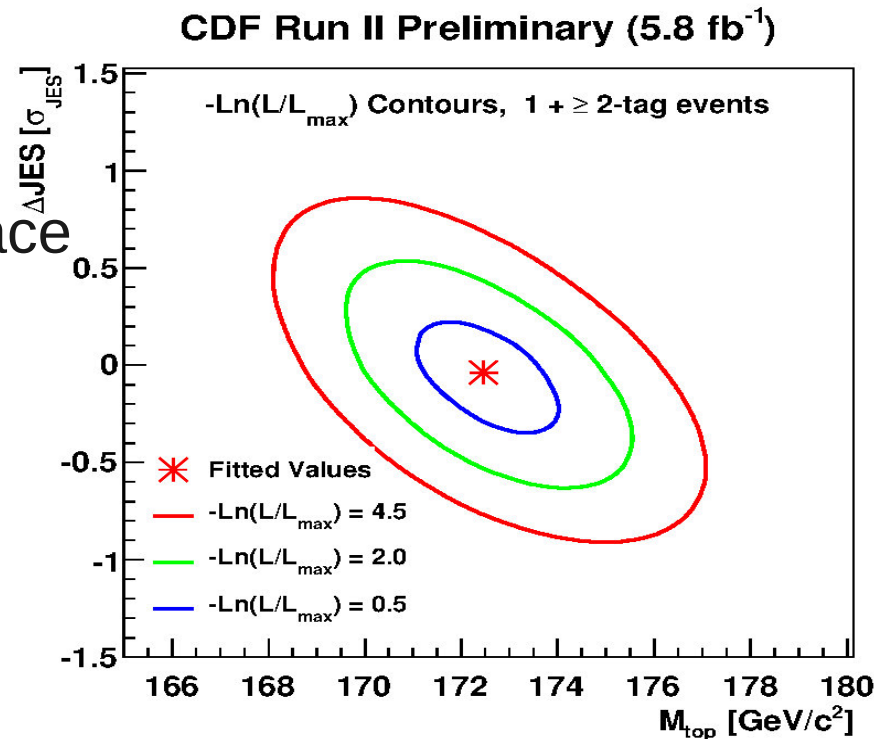
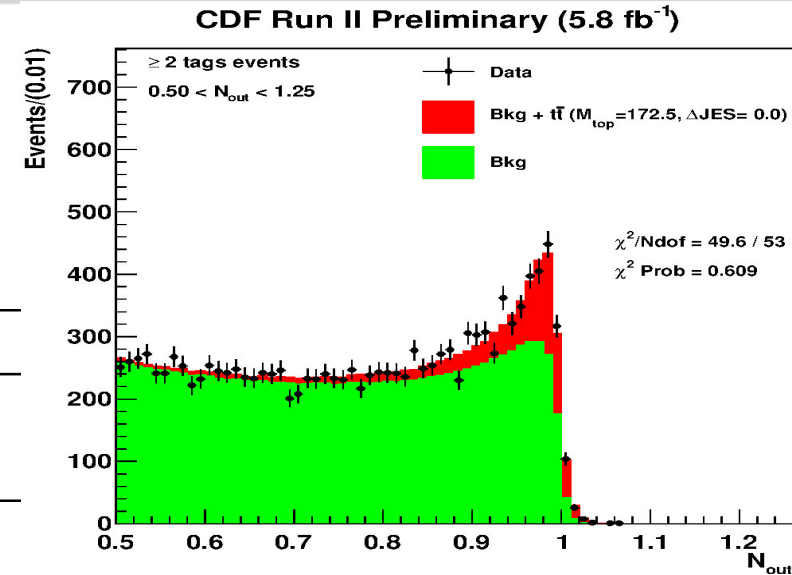
- combinations (1 btag 30, 2 btags 6,  $\geq 2$  btags 18)

- Data driven background
  - QCD can't reliably model this phasespace
  - based on tag rate parametrization
- Systematic dominated s+b modeling

$172.5 \pm 1.4(\text{stat}) \pm 1.4(\text{syst}) \text{ GeV}/c^2$   
 $172.5 \pm 2.0 \text{ GeV}/c^2$  (precision  $\pm 1.1\%$ )



CDF Note 10456 (2011)



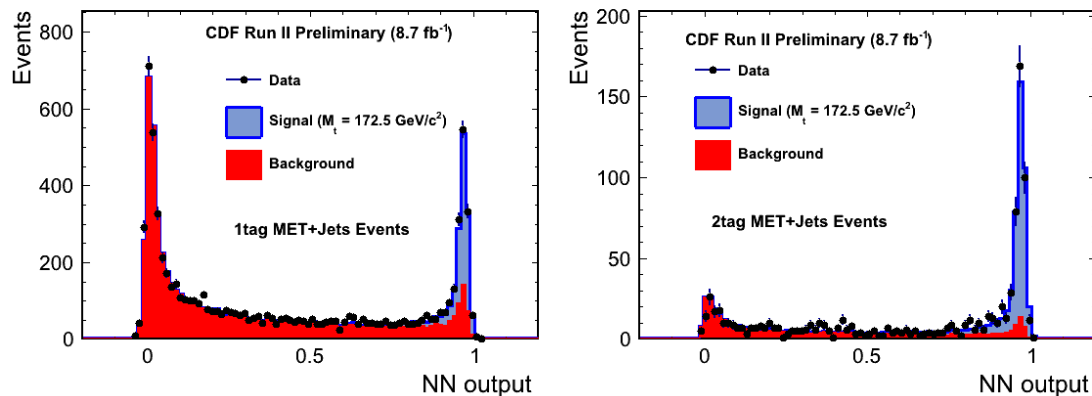
# Mass in MET + jets channel

all data

- Template method with full CDF RunII dataset  $8.7\text{fb}^{-1}$ 
  - same approach as in l+jets
- Catching all events missed in channels with MET

b-tagging	Signal	Background	Total Expected	Observed
1tag	$1228.1 \pm 144.2$	$713.3 \pm 61.3$	$1941.4 \pm 156.7$	2102
2tag	$552.5 \pm 73.3$	$168.6 \pm 43.9$	$721.1 \pm 85.4$	775

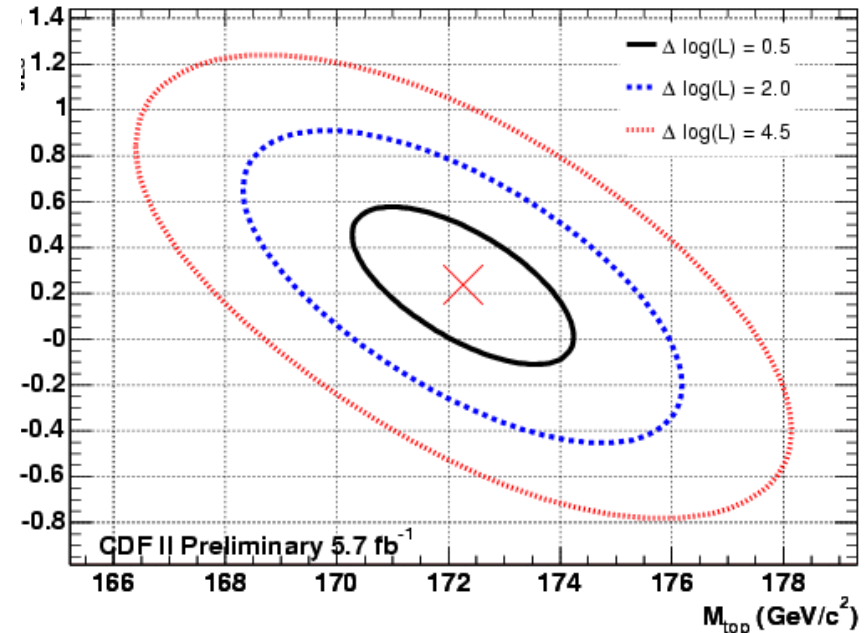
- Data driven background (similar to alljet)
- NN trained to get cleaner signal



$171.3 \pm 1.4(\text{stat}) \pm 0.9(\text{syst}) \text{ GeV}/c^2$   
 $171.3 \pm 1.7 \text{ GeV}/c^2$  (precision  $\pm 1.4\%$ )

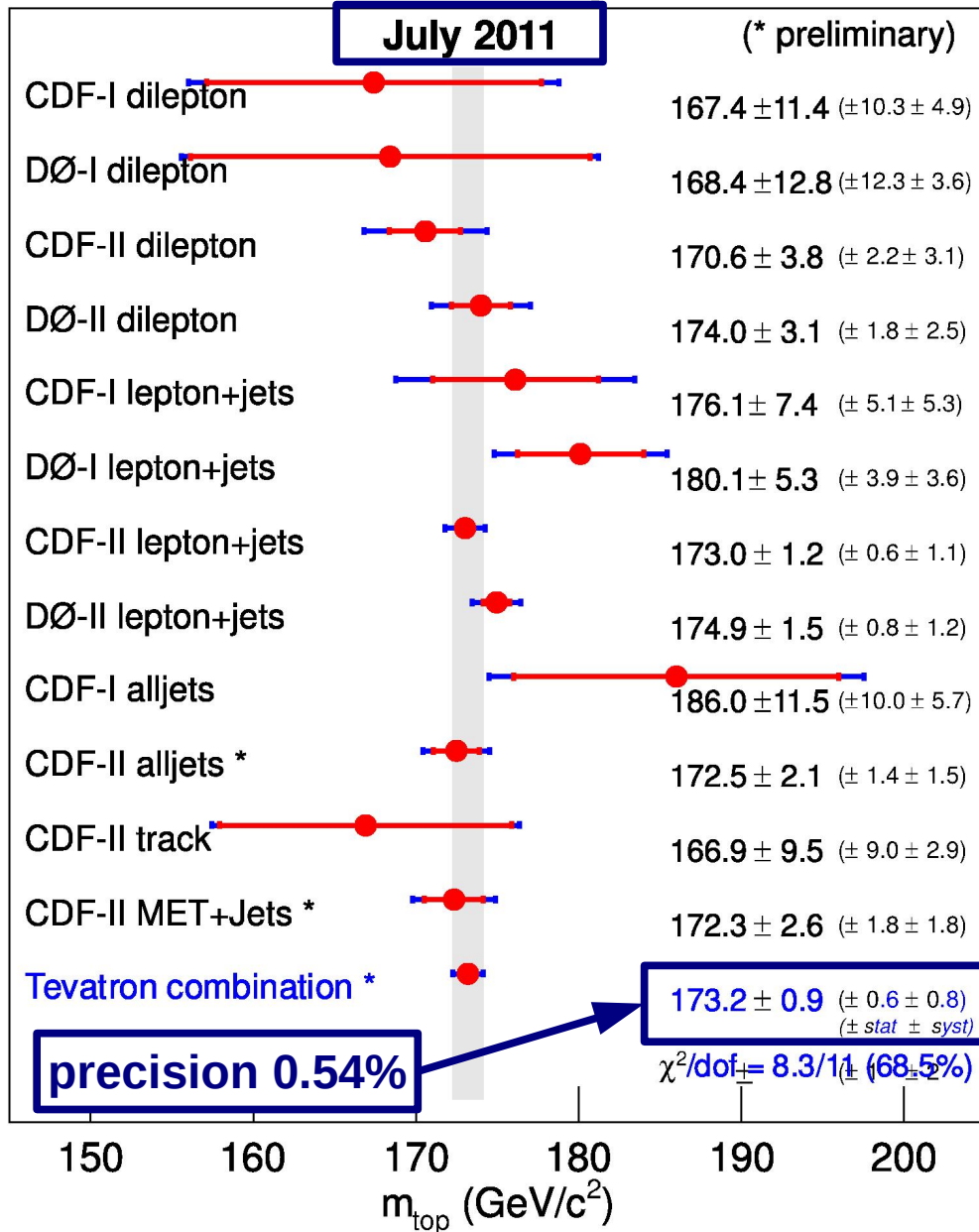


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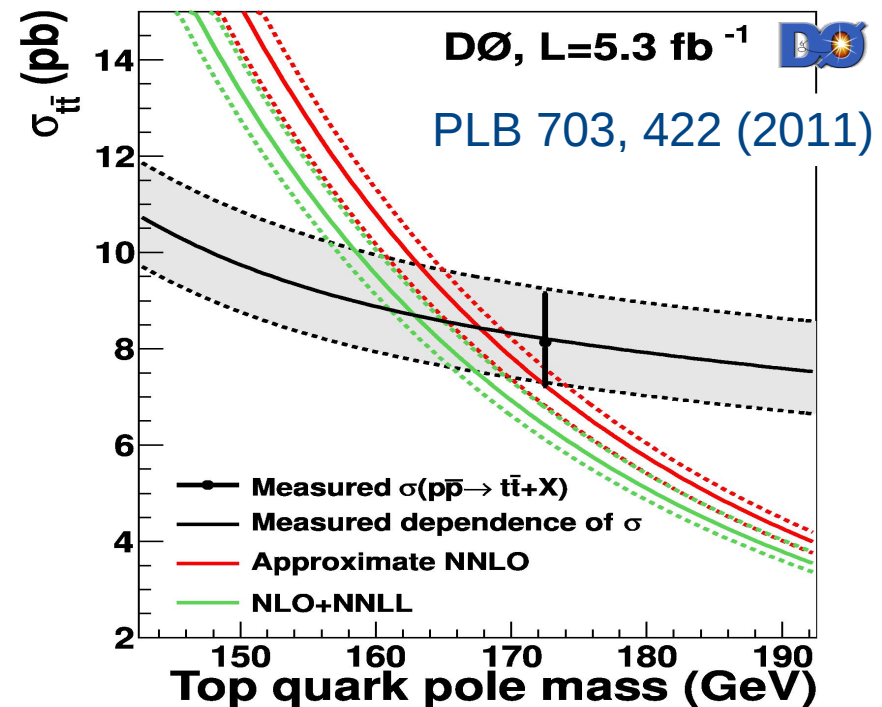


# Tevatron top mass combination

## Mass of the Top Quark



- Up to 5.8fb<sup>-1</sup>, [arXiv:1107.5255](https://arxiv.org/abs/1107.5255)
  - with all data measurement of the mass approaching 1 GeV uncertainty
- Top mass definition (comes from MC templates, calibration)
  - mass from cross section

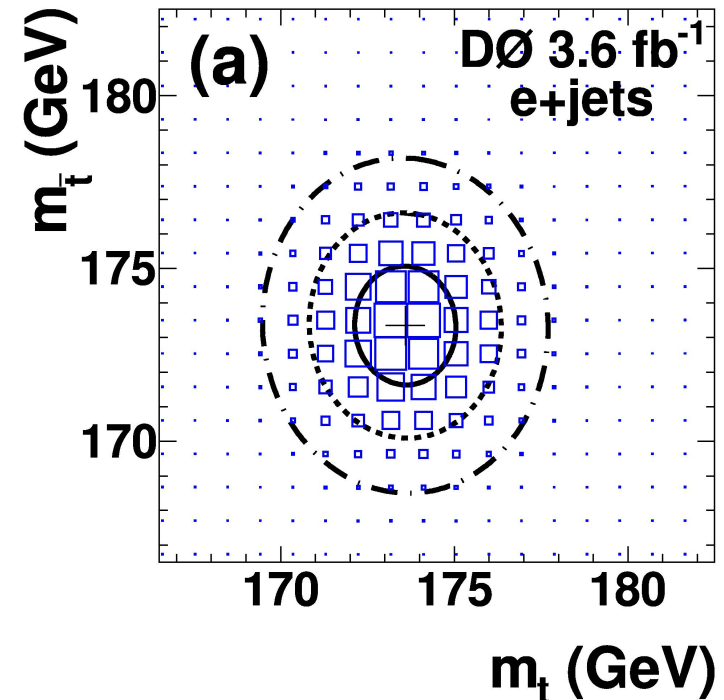
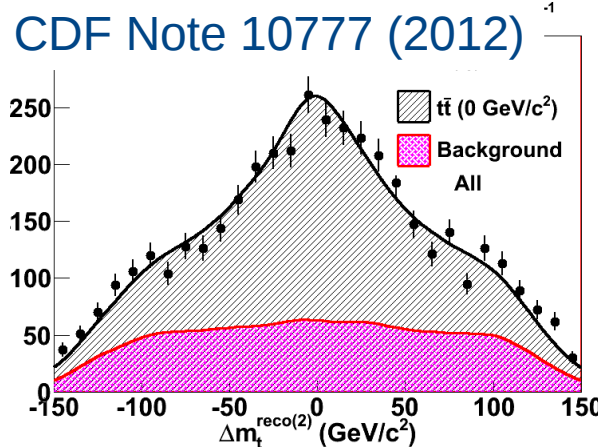
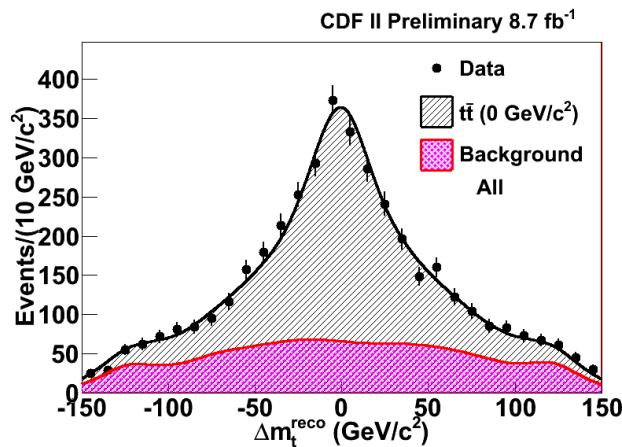
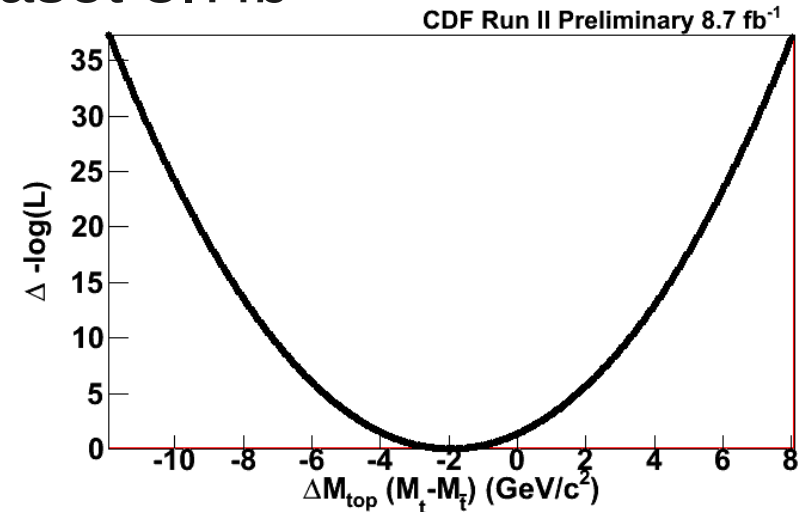


# Mass difference

all data

- Template method with full CDF RunII dataset  $8.7\text{fb}^{-1}$ 
  - look for difference top-antitop mass
  - check of CPT invariance in top sector
  - same procedure  $l+jets$  mass, but  $m_t \neq m_{\bar{t}}$
  - in agreement with SM (no difference)

$$\Delta M_{\text{top}} = -1.95 \pm 1.11(\text{stat}) \pm 0.59(\text{syst}) \text{ GeV}/c^2$$



- Matrix element method,  $3.6\text{fb}^{-1}$

$$\Delta M_{\text{top}} = -0.8 \pm 1.8(\text{stat}) \pm 0.5(\text{syst}) \text{ GeV}/c^2$$



PRD 84, 052005 (2011)

# Top quark width

- Indirect measurement from single top quark t-channel cross section and ratio  $B(t \rightarrow Wb)/B(t \rightarrow Wq)$

$$R = B(t \rightarrow Wb)/B(t \rightarrow Wq) = 0.90 \pm 0.04$$

$$|V_{tb}| = 0.95 \pm 0.02$$



PRL, 121802 (2011)

$$\Gamma_p \equiv \Gamma(t \rightarrow Wb) \approx \sigma_{t\text{-channel}}^{\text{meas}}$$

$$\Gamma_t = \frac{\Gamma_p}{B(t \rightarrow Wb)} = \frac{\sigma_{t\text{-channel}}^{\text{meas}} \Gamma(t \rightarrow Wb)^{\text{SM}}}{B(t \rightarrow Wb) \sigma_{t\text{-channel}}^{\text{SM}}}$$

- NLO prediction  $\Gamma_t = 1.33 \text{ GeV}$

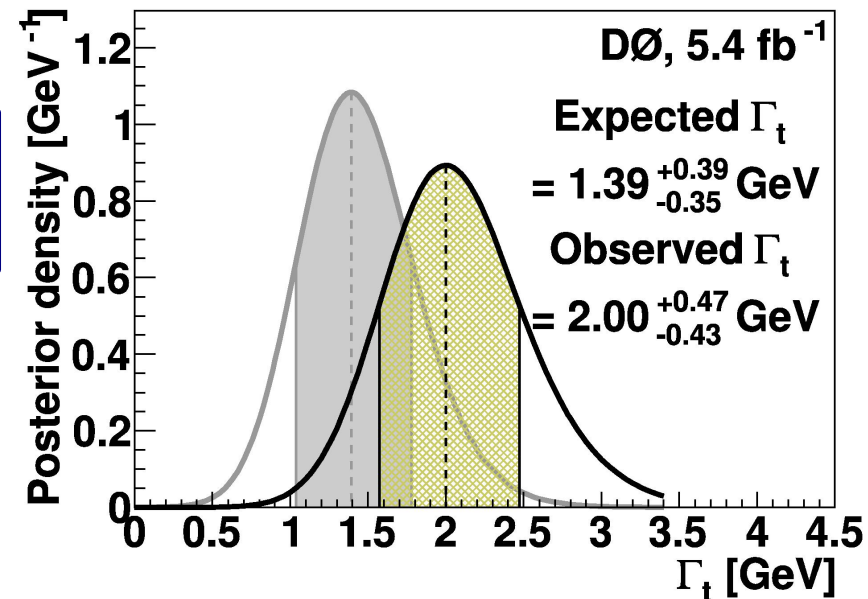
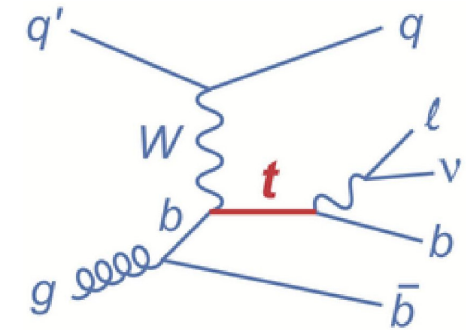
$$\Gamma_t = 2.00^{+0.47}_{-0.43} \text{ GeV}$$

$$\tau_t = (3.29^{+0.90}_{-0.63}) \times 10^{-25} \text{ (h}/\Gamma_t\text{)}$$



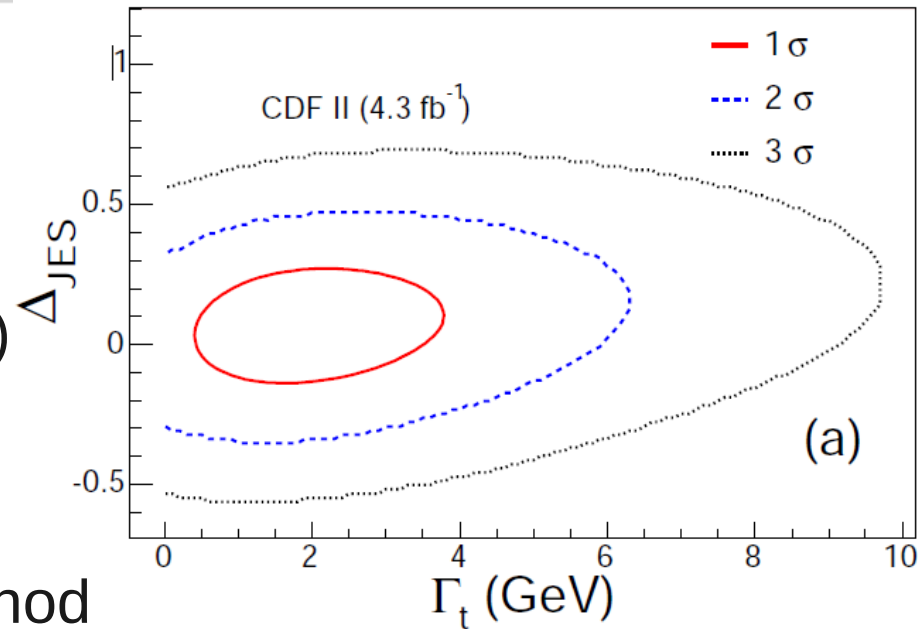
PRD 85, 091104 (2012)

- hadronization time scale  $3.3 \times 10^{-24} \text{ s}$   
 $\Rightarrow$  top quark decay before hadronization



# Top quark width

- Direct measurement in l+jets,  $4.3\text{fb}^{-1}$ 
  - template method with different top quark  $\Gamma_t$  and in situ JES
  - subsamples with 1,2 b-tags (diff. s+b)
  - comparing s + b probability density
    - unbinned maximum likelihood
  - limits on  $\Gamma_t$  via Feldman-Cousins method



$\Gamma_t < 7.6\text{ GeV @ 95\% CL}$   
 $0.3 < \Gamma_t < 4.4\text{ GeV @ 68\% CL}$



PRL 105, 232003 (2010)

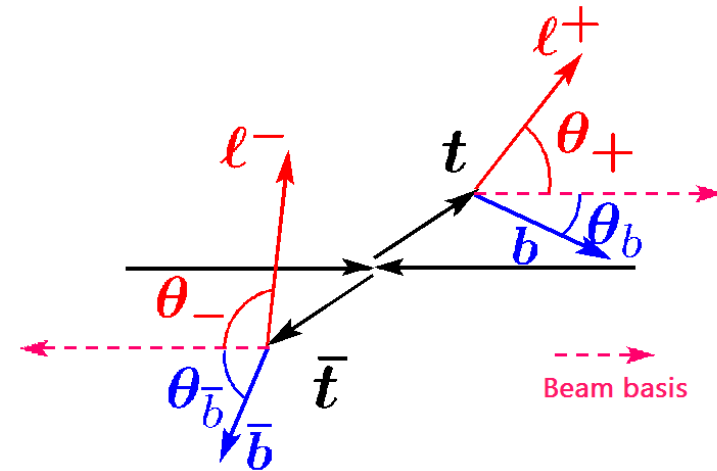
# Spin correlations

- SM predict top quark polarized
  - polarization of top quark spin observed through correlations between flight directions of decay products

- $t\bar{t}$  correlation spin strength  $C$   $[-1, 1]$

$$\frac{1}{\sigma_{t\bar{t}}} \frac{d^2 \sigma_{t\bar{t}}}{d \cos \theta_+ d \cos \theta_-} = \frac{1 + C \cos \theta_+ \cos \theta_-}{4}$$

- SM predicts  $C = 0.777^{+0.027}_{-0.042}$  (beam basis)
  - sensitive to non-SM

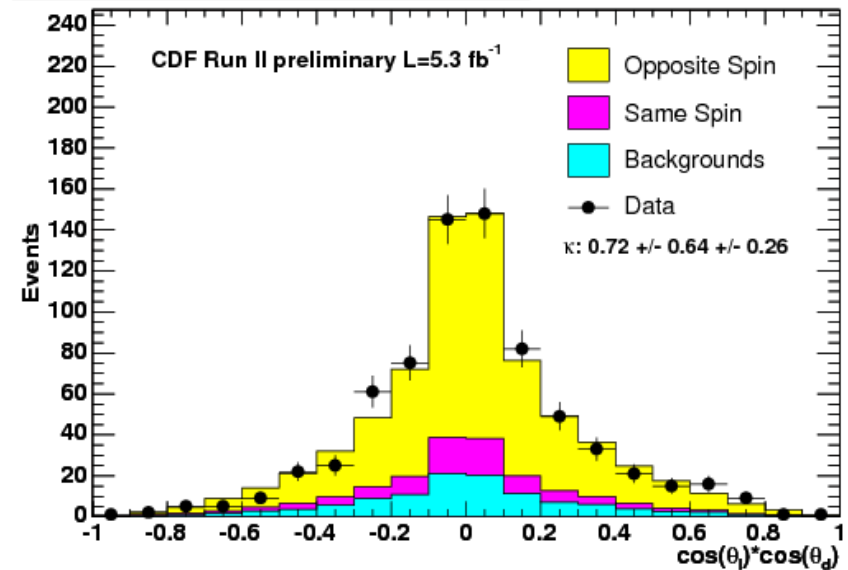


$$C = \frac{N_{\parallel} - N_{\perp}}{N_{\parallel} + N_{\perp}}$$

# Spin correlations – template methods

- Using templates for  $\cos\theta_-\cos\theta_+$
- Binned maximum likelihood for  $C_{\text{meas}}$
- Statistically limited
- Consistent with SM

Beam Basis Bilinear  $\text{Cos}(\theta_-)\text{Cos}(\theta_+)$



$C = 0.04 \pm 0.56(\text{stat+syst}), \text{ dilepton}, 5.1\text{fb}^{-1}$



CDF Note 10719 (2011)

$C = 0.72 \pm 0.69(\text{stat+syst}), \text{ l+jets}, 5.3\text{fb}^{-1}$

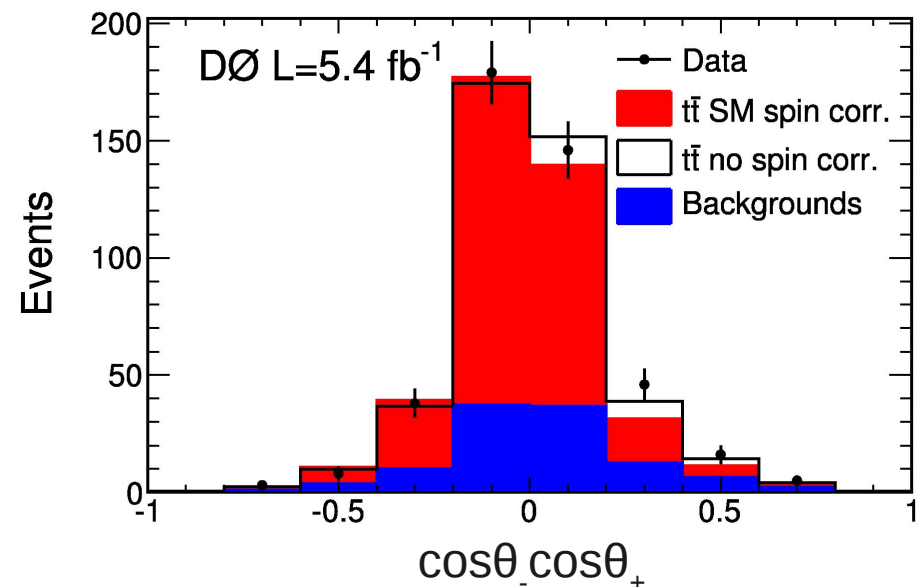


CDF Note 10211 (2011)

$C = 0.10 \pm 0.45(\text{stat+syst}), \text{ l+jets}, 5.3\text{fb}^{-1}$



PLB 702, 16 (2011)





# Spin correlations – ME

- ME for hypothesis with ( $H=c$ ) and without ( $H=u$ ) spin correlations

$$R = \frac{P_{sig}(x, H = c)}{P_{sig}(x, H = u) + P_{sig}(x, H = c)}$$

- distributions of  $R$  for  $t\bar{t}$  MC (c/u)

- Better sensitivity

$C = 0.57 \pm 0.31(\text{stat+syst})$ , dilepton,  $5.4\text{fb}^{-1}$  

PRL 107, 031001 (2011)

$C = 0.89 \pm 0.33(\text{stat+syst})$ , l+jets,  $5.3\text{fb}^{-1}$  

Combined l+jets + dilepton:

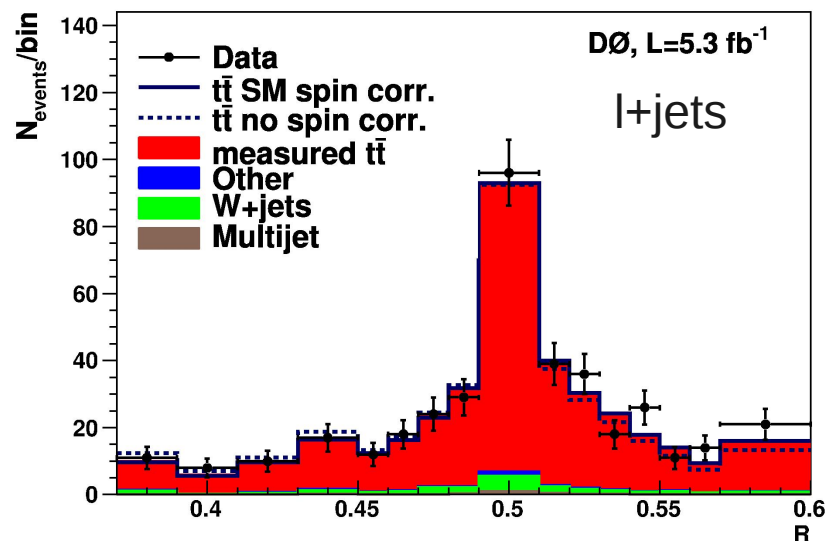
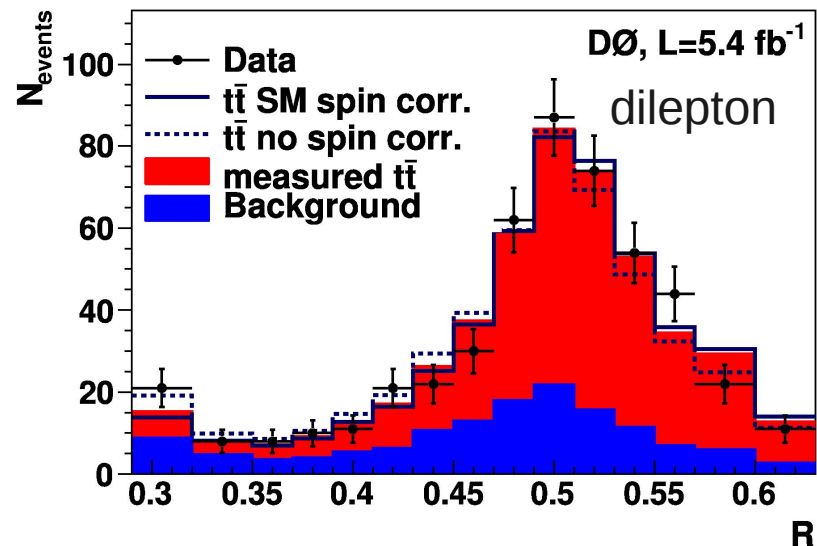
$C = 0.66 \pm 0.23(\text{stat+syst})$

$C > 0.26$  @ 95% CL

$C > 0.041$  @ 99.7% CL

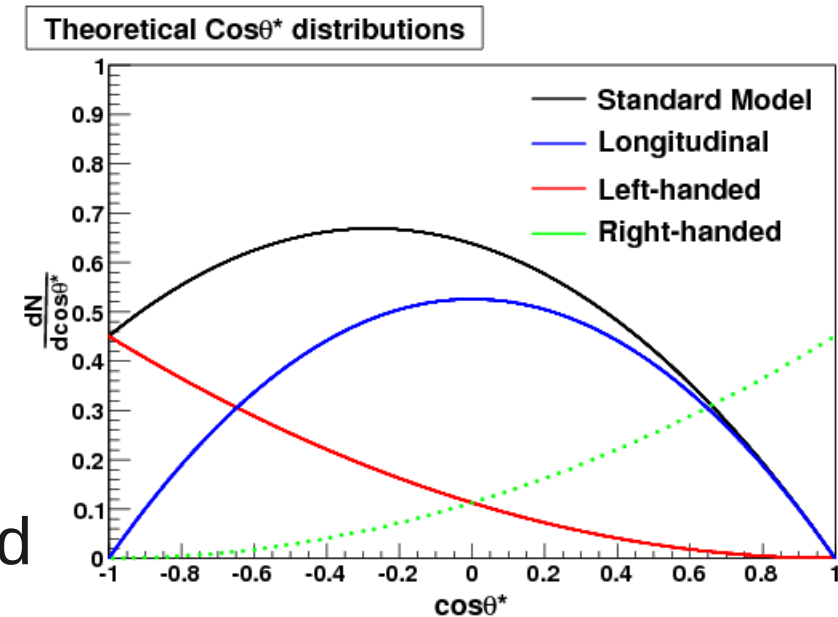
PRL 108, 032004 (2012)

- First evidence of non-zero SM spin correlation at 3.1 standard deviations



# W boson helicity

- Measured in  $t \rightarrow Wb$  ( $\sim 100\%$ )
- three possible helicity states
  - Longitudinal ( $f_0$ ), left ( $f_-$ ) and right ( $f_+$ ) handed
  - angular distribution of decay products in  $W$  rest frame
- in SM right-handed strongly suppressed
  - V – A interaction
  - fraction of  $f_0$ ,  $f_+$  and  $f_-$  depends on  $m_t$ ,  $m_W$
  - deviation would provide evidence BSM
    - non-SM contribution
    - difference in V – A structure of  $tWb$  vertex
- Measurement doesn't rely on SM constraints
  - simultaneous measurement of  $f_0$ ,  $f_+$



Standard model:  
 $f_0 = 69.6\%$   
 $f_- = 30.3\%$   
 $f_+ = 0.1\%$

# W boson helicity combination

- Combination of three published results
  - DØ, 5.4fb<sup>-1</sup>, l+jets and dilepton, binned Poisson likelihood  
PRD 83, 032009 (2011)
  - CDF, 5.1fb<sup>-1</sup>, dilepton, template method  
CDF Note 10543 (2011)
  - CDF, 2.7fb<sup>-1</sup>, l+jets, matrix element method  
PRL 105, 042002 (2010)
- First combination, improved sensitivity by factor ~ 2

- Systematic uncertainties
  - signal modeling (LO x NLO)

$$f_0 = 0.722 \pm 0.062(\text{stat}) \pm 0.052(\text{syst})$$

$$f_+ = -0.033 \pm 0.034(\text{stat}) \pm 0.031(\text{syst})$$



PRL 107, 031001 (2011)

- Matrix element, l+jets, 8.7fb<sup>-1</sup>

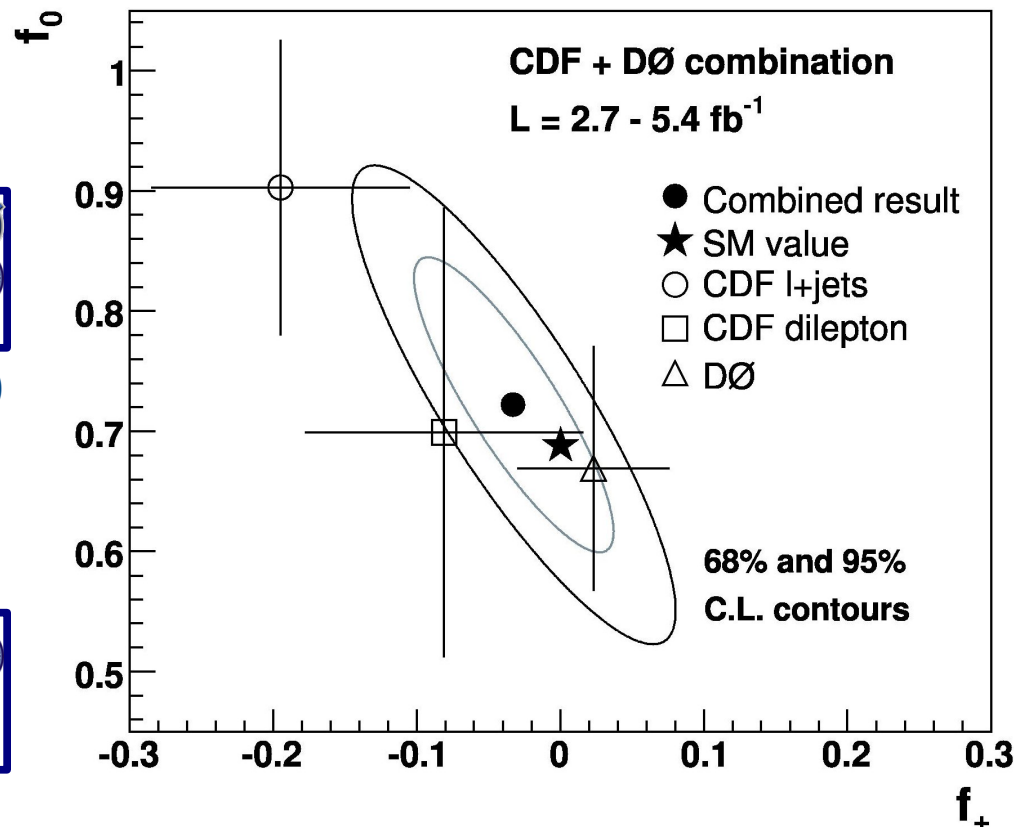
$$f_0 = 0.726 \pm 0.066(\text{stat}) \pm 0.067(\text{syst})$$

$$f_+ = -0.025 \pm 0.024(\text{stat}) \pm 0.040(\text{syst})$$



all data

CDF Note 10855 (2012)



# Conclusions

- Tevatron is making legacy measurement
  - several measurements use all RunII data
  - mass measured with precision 0.54%
    - final combination not yet done
    - improvements requires better understanding of systematic uncertainties
- Some measurements are complementary to LHC (e.g. spin correlations)
- A lot of top quark properties have been measured and tested to SM predictions

# Backup

# Search for LIV in top sector

- No limits on violation of Lorentz invariance exist in top quark sector
- Look for periodic oscillation in the number of  $t\bar{t}$  events observed in the Earth-based detector as a function of sidereal time
- The relevant time scale is the sidereal day (1 day)

$$\sigma_t \approx \sigma_{ave} (1 + f_{SME}(t))$$

No signs for LIV in top sector



- Look at distribution  $N_i \approx N_{tot} (L_i / L_{tot}) (1 + f_S f_{SME}(\Phi_i))$   
( $f_S$  – average fraction of signal events in data)

FERMILAB-PUB-12-085-E  
Accepted in PRL

- To simplify fitting  $f_{SME}$ , define  $R_i \equiv \frac{1}{f_S} \left( \frac{N_i / N_{tot}}{L_i / L_{int}} - 1 \right)$

