

# Phenomenology of Vector-like Quark Models

Yasuhiro Okada (KEK/Sokendai)

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# Contents of this talk

- Classification of vector-like  $t'$  models  
definitions, constraints, branching ratios
- Phenomenology of non-SM doublet model  
definition, constraints, flavor signals

This is an introduction to the next talk by Luca Panizzi on LHC signals of this model.

Reference:

- (1) G. Cacciapaglia, A.Deandrea, D.Harada, and Y. Okada, JHEP 11 (2010) 159
- (2) G. Cacciapaglia, A.Deandrea, L.Panizzi, N.Gaur, D.Harada, and Y. Okada, arXiv:1108.6329

# Vector-like quark models

- Many new physics models predicts vector-like quarks, especially extra top-like quarks.  
Little Higgs models. Extra-dim models.
- Phenomenologically less constrained than the chiral fourth generation model because of “decoupling” feature.
- Copious production at LHC.

# Our framework

- Include one vector-like representation of  $SU(2) \times U(1)$ .
- Study effects of new (large) Yukawa coupling constants.
- First consider only mixing between 3<sup>rd</sup> and 4<sup>th</sup> generation quarks. Later include mixings to light generation quarks.


# Classification of vector-like models

SM Yukawa coupling

$$\mathcal{L}_{\text{Yuk}} = -y_u \bar{q}_L H^c u_R - y_d \bar{q}_L H d_R + h.c.$$

Inclusion of new Yukawa coupling

$q_L \times H \times \psi$  :  $\psi$  SU(2) singlet or triplet

 : t' model

$$\psi = (1, \frac{2}{3}) = U \quad \psi = (3, \frac{2}{3}) = \{X, U, D\}^T$$

$$\psi = (1, -\frac{1}{3}) = D \quad \psi = (3, -\frac{1}{3}) = \{U, D, X\}^T$$

$u_R (d_R) \times H \times \psi$  :  $\psi$  SU(2) doublet

$$\psi = (2, \frac{1}{6}) = \{U, D\}^T$$

SM doublet : (Two new Yukawa couplings)

$$\psi = (2, \frac{7}{6}) = \{X, U\}^T \quad \psi = (2, -\frac{5}{6}) = \{D, X\}^T$$

Non-SM doublet

Vector-like: a pair of  $\psi_L$  and  $\psi_R$  is introduced.

# Singlet case

$$\mathcal{L}_{\text{Yuk}} = -y_u \bar{q}_L H^c u_R - \lambda \bar{q}_L H^c U_R - M \bar{U}_L U_R + h.c.$$

$$\mathcal{L}_{\text{mass}} = -\frac{y_u v}{\sqrt{2}} \bar{u}_L u_R - x \bar{u}_L U_R - M \bar{U}_L U_R + h.c.,$$

$$(x = \frac{\lambda v}{\sqrt{2}})$$

t-t' mixing

$$\begin{pmatrix} \cos \theta_u^L & -\sin \theta_u^L \\ \sin \theta_u^L & \cos \theta_u^L \end{pmatrix} \begin{pmatrix} \frac{y_u v}{\sqrt{2}} & x \\ 0 & M \end{pmatrix} \begin{pmatrix} \cos \theta_u^R & \sin \theta_u^R \\ -\sin \theta_u^R & \cos \theta_u^R \end{pmatrix} = \begin{pmatrix} m_t & 0 \\ 0 & m_{t'} \end{pmatrix}$$

For large M;

$$\frac{y_u v}{\sqrt{2}} \sim m_t, \quad m_{t'} \sim M;$$

$$\sin \theta_u^L \sim \frac{x}{M}, \quad \sin \theta_u^R \sim \frac{m_t x}{M^2}.$$

The  $u_R$ - $U_R$  mixing case

=> The right-handed mixing angle is suppressed.

The left-handed angle can be large.

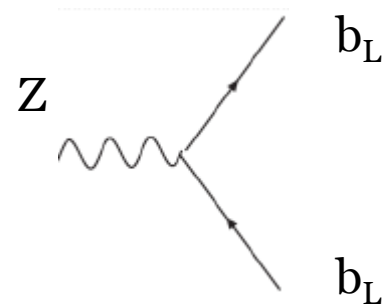
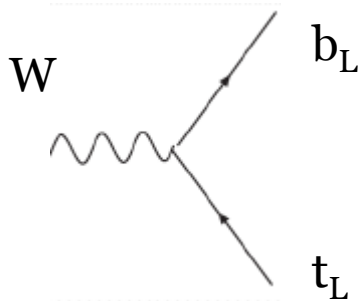
=> Sizable correction to the  $Wtb$  vertex.

# Triplet case

$$\begin{aligned}\mathcal{L}_{\text{Yuk}} &= -y_u \bar{q}_L H^c u_R - \lambda \bar{q}_L \tau^a H^c \psi_R^a - M \bar{\psi}_L \psi_R + h.c. \\ &= -\frac{y_{uv}}{\sqrt{2}} \bar{u}_L u_R - \frac{\lambda v}{\sqrt{2}} \bar{u}_L U_R - \lambda v \bar{d}_L D_R - M (\bar{U}_L U_R + \bar{D}_L D_R + \bar{X}_L X_R) + h.c.\end{aligned}$$

(Y=2/3 case: similar for Y=-1/3 case)

Large left-handed mixing for t-t'  
 Large left-handed mixing for b-b'  
 => corrections to the Wtb and the Zbb vertexes



# doublet case

SM doublet

$$\begin{aligned}\mathcal{L}_{\text{Yuk}} &= -y_u \bar{q}_L H^c u_R - \lambda_u \bar{\psi}_L H^c u_R - \lambda_d \bar{\psi}_L H d_R - M \bar{\psi}_L \psi_R + h.c. \\ &= -\frac{y_u v}{\sqrt{2}} \bar{u}_L u_R - \frac{\lambda_u v}{\sqrt{2}} \bar{U}_L u_R - \frac{\lambda_d v}{\sqrt{2}} \bar{D}_L d_R - M (\bar{U}_L U_R + \bar{D}_L D_R) + h.c.\end{aligned}$$

Two new Yukawa coupling constants

Small left-handed mixing angle for t-t' and b-b'  
 Large right-handed mixing angle for t-t' and b-b'  
 $\Rightarrow$  Zbb constraint to  $x_b = \lambda_d v / \sqrt{2}$

Non-SM doublet

$$\begin{aligned}\mathcal{L}_{\text{Yuk}} &= -y_u \bar{q}_L H^c u_R - \lambda \bar{\psi}_L H u_R - M \bar{\psi}_L \psi_R + h.c. \\ &= -\frac{y_u v}{\sqrt{2}} \bar{u}_L u_R - \frac{\lambda v}{\sqrt{2}} \bar{U}_L u_R - M (\bar{U}_L U_R + \bar{X}_L X_R) + h.c.\end{aligned}$$

Small left-handed mixing angle for t-t'  
 Large right-handed mixing angle for t-t'  
 $\Rightarrow$  No strong constraints from Wbt and Zbb



# Allowed parameter space

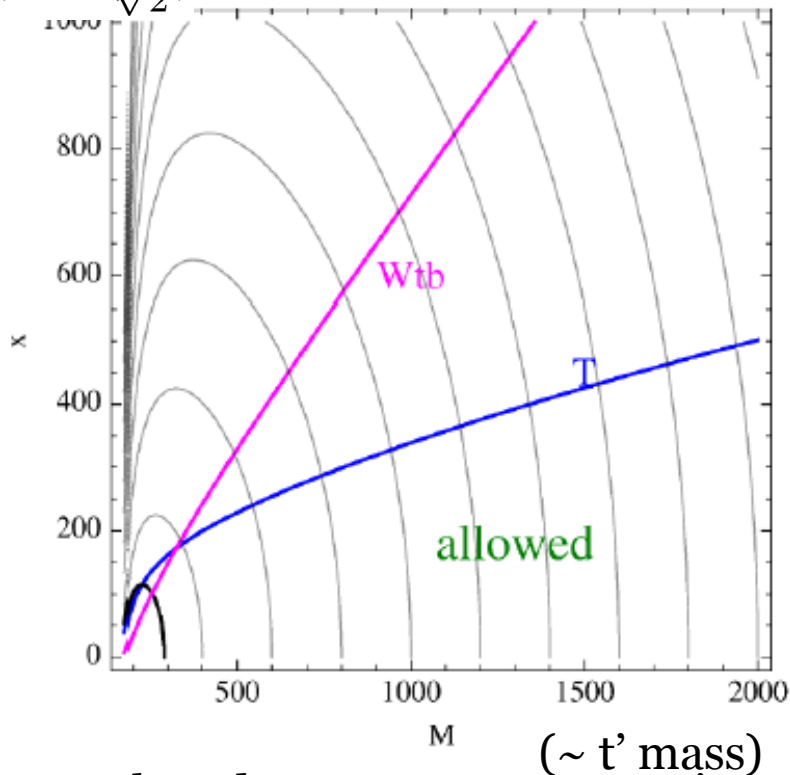
We have derive allowed parameter regions based on Wtb, Zbb and the T parameter constrains

$$\delta g_{Wtb} \pm 20\%; \delta g_{Zbb}^L \pm 1\%; \delta g_{Zbb}^R \pm 20\%; -0.2 < \delta T < 0.4$$

T parameter : A constraint from precise electroweak measurements

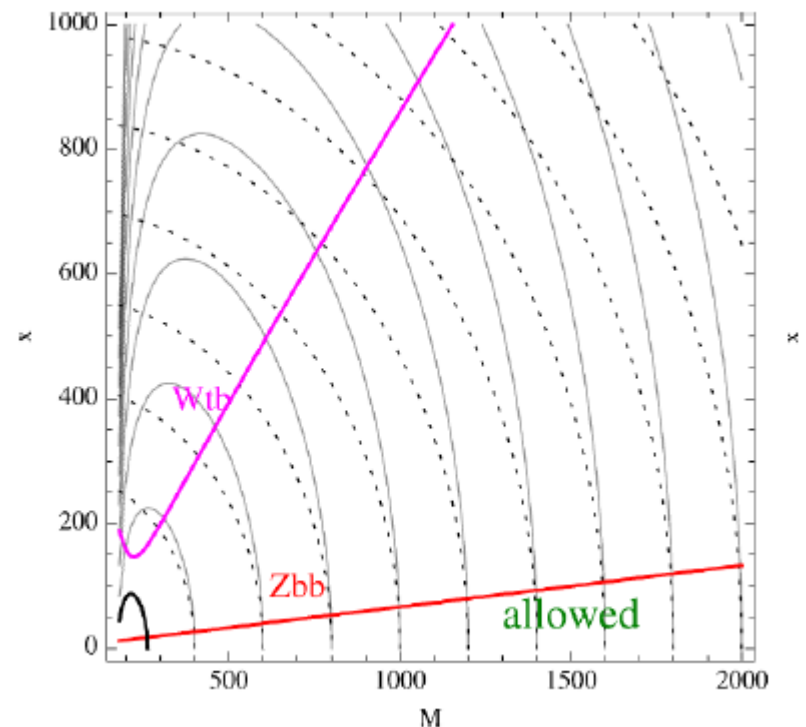
$$(x = \frac{\lambda v}{\sqrt{2}})$$

Singlet case



Wtb and T parameter constrains are important .

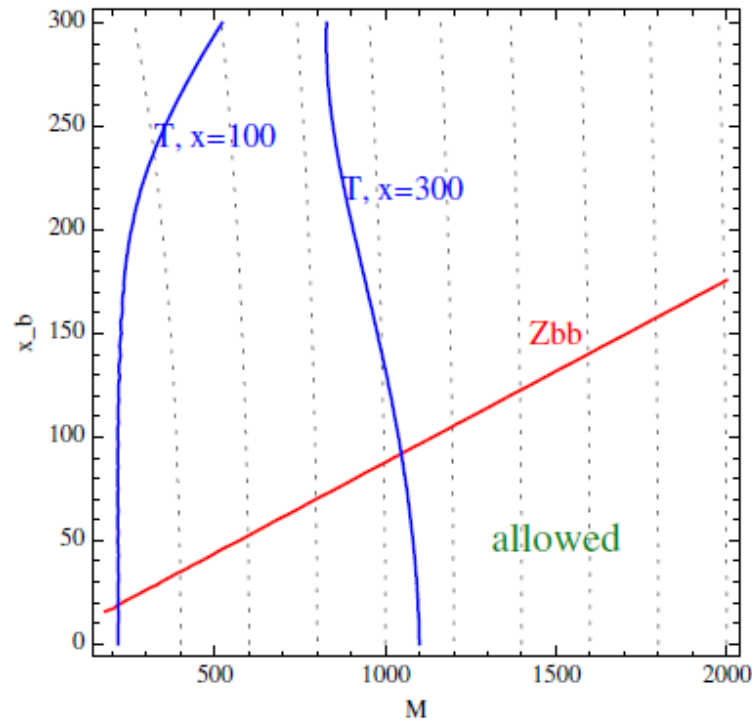
Triplet (Y=2/3 )case



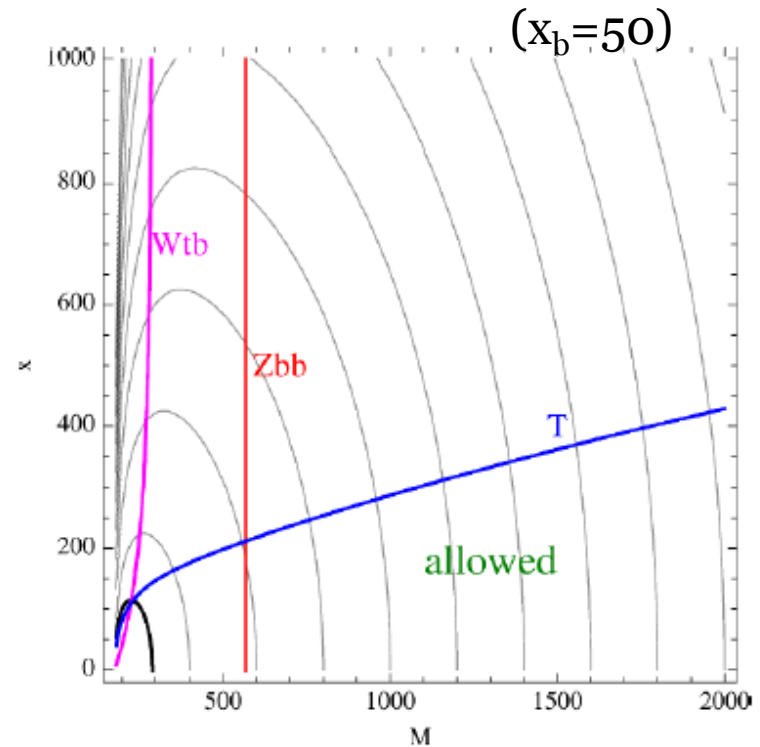
Zbb constaint is very strong

# SM doublet

$$x_b = \frac{\lambda_d v}{\sqrt{2}}$$

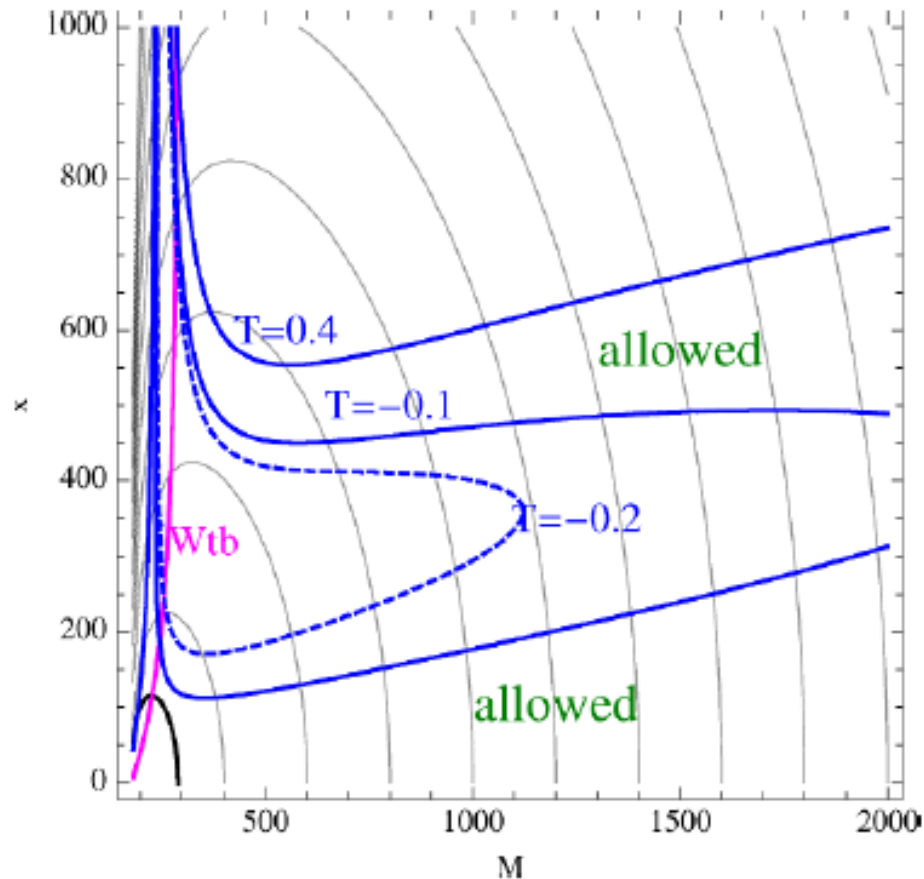


$$x = \frac{\lambda_u v}{\sqrt{2}}$$



The  $Z_{bb}$  vertex and the  $T$  parameter constrain  $x_b$  and  $x$  respectively.

# Non-SM doublet



Only T parameter is a strong constraint. A large new Yukawa coupling constant is allowed.

# Decay branching ratios

In all cases,  $t' \rightarrow Wb$ ,  $t' \rightarrow Zt$ ,  $t' \rightarrow ht$  are main decay modes.

Loop induced decays  $t' \rightarrow t \gamma$  and  $t \rightarrow t g$  are  $O(10^{-6})$  and  $O(10^{-5})$

$m_{t'} = 500 \text{ GeV}$

case	$Wb$	$Zt$	$ht$	$\gamma t$	$gt$
Singlet, $x = 10$	0.50	0.17	0.33	$4 \times 10^{-6}$	$2.7 \times 10^{-5}$
Singlet, $x = 200$	0.50	0.15	0.29	$3 \times 10^{-6}$	$1.6 \times 10^{-5}$
SM doublet, $x = 10$	0.95	0.017	0.03	$0.21 \times 10^{-6}$	$0.2 \times 10^{-5}$
SM doublet, $x = 100$ ( $x_b=50$ )	0.24	0.26	0.50	$4 \times 10^{-6}$	$2.2 \times 10^{-5}$
Non-SM doublet, $x = 10$	0.09	0.37	0.61	$6 \times 10^{-6}$	$15 \times 10^{-5}$
Triplet A ( $Y=2/3$ ), $x = 10$	0.36	0.22	0.42	$7.2 \times 10^{-6}$	$2.4 \times 10^{-5}$
Triplet B ( $Y=-1/3$ ), $x = 10$	0.01	0.41	0.58	$3.5 \times 10^{-6}$	$7.1 \times 10^{-5}$

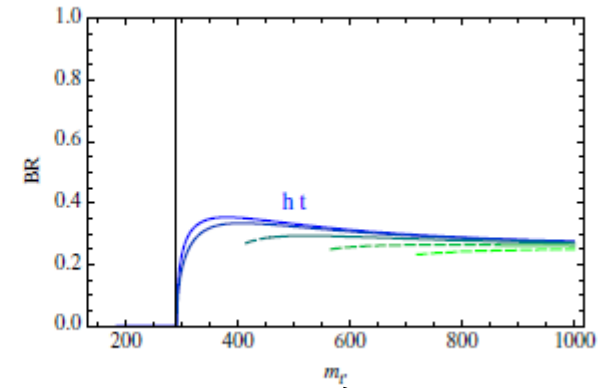
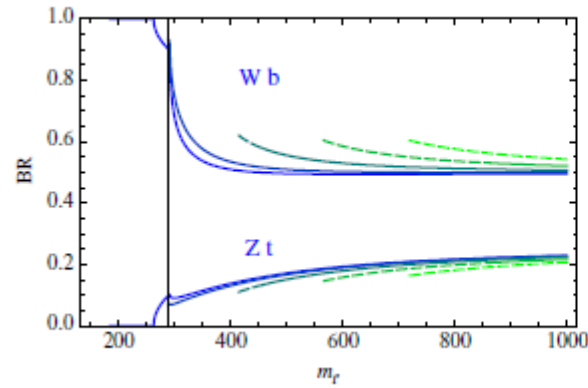
Large mass limit  
( $m_{t'} = \infty$ )

case	$Wb$	$Zt$	$ht$
singlet	0.5	0.25	0.25
SM doublet	$x_b^2 / (x_b^2 + x^2)$	$0.5x^2 / (x_b^2 + x^2)$	$0.5x^2 / (x_b^2 + x^2)$
Non-SM doublet	0	0.5	0.5
Triplet A	0.5	0.25	0.25
Triplet B	0	0.5	0.5

Understood by  
the equivalence  
theorem  
(C.P.Yuan's talk)

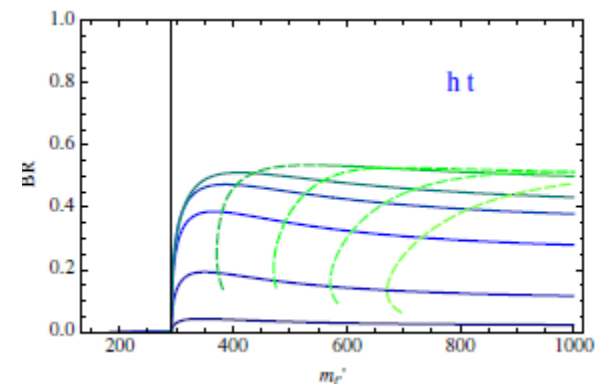
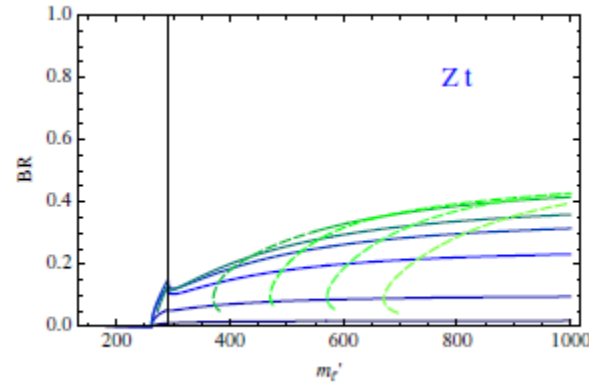
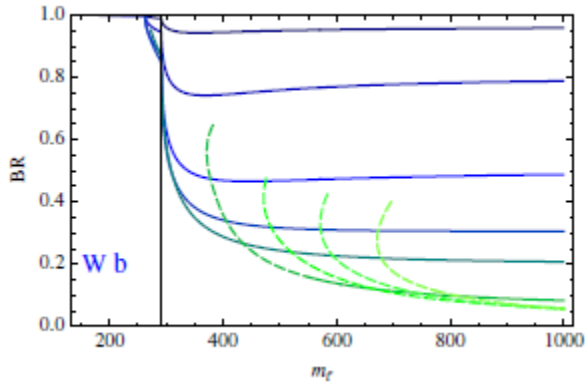
## Singlet

( $x=10, 100, 200, 300, 400\text{GeV}$ )



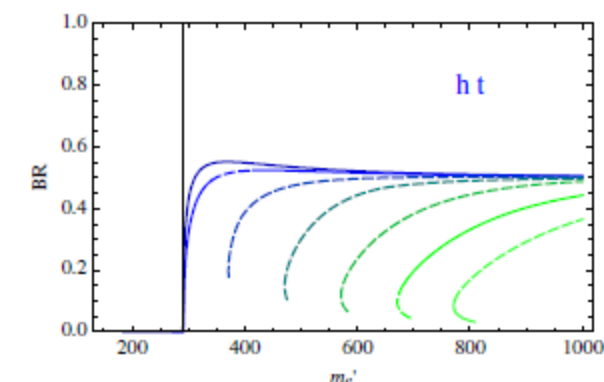
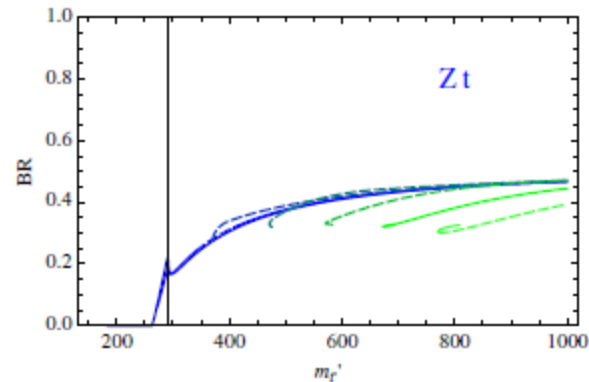
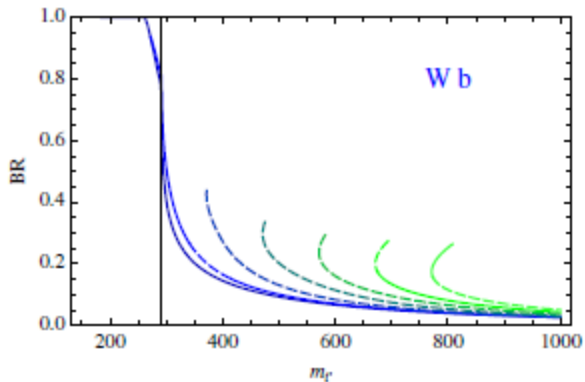
## SM doublet

( $x_b=50\text{GeV}, x=10, 25, 50, 75, 100, 200, 300, 400, 500\text{GeV}$ )



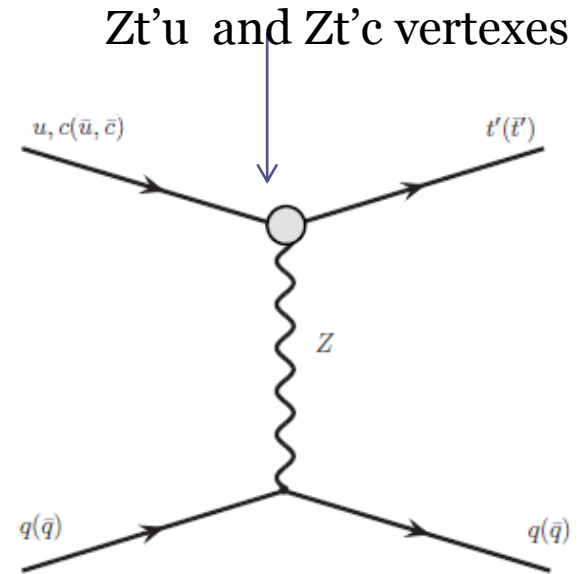
## Non-SM doublet

( $x=10, 100, 200, 300, 400, 500, 600\text{GeV}$ )

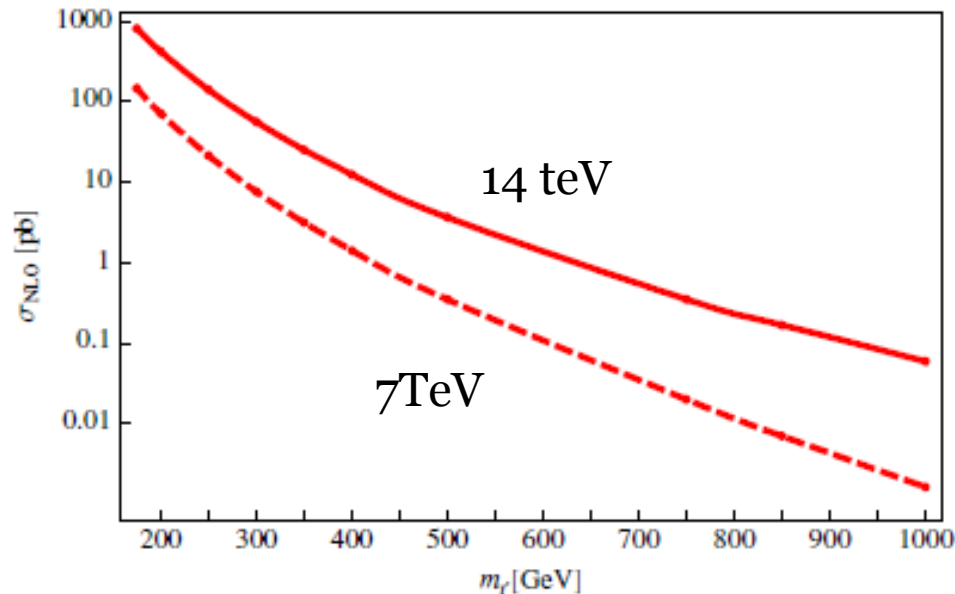


# Phenomenology of non-SM doublet

- Parameter constraints are weak. A large new Yukawa coupling constant is allowed.
- A right-handed up-type flavor changing neutral current exists at the tree level.
- Possible large single  $t'$  production at LHC.
- Need to include  $t'$  mixing to light quarks



$t'$  pair production cross section



## Non-SM doublet model with three flavor mixing

$$\mathcal{L}_{\text{yuk}} = -y_u^{i,j} \bar{Q}_L^i H^c u_R^j - y_d^{i,j} \bar{Q}_L^i H d_R^j - \lambda^j \bar{\psi}_L H u_R^j$$

$$\begin{aligned} \mathcal{L}_{\text{mass}} = & -(\bar{d}_L, \bar{s}_L, \bar{b}_L) \cdot \tilde{V}_{CKM} \cdot \begin{pmatrix} \tilde{m}_d & & \\ & \tilde{m}_s & \\ & & \tilde{m}_b \end{pmatrix} \cdot \begin{pmatrix} d_R \\ s_R \\ b_R \end{pmatrix} \\ & - (\bar{u}_L, \bar{c}_L, \bar{t}_L, \bar{U}_L) \cdot \begin{pmatrix} \tilde{m}_u & & & 0 \\ & \tilde{m}_c & & 0 \\ & & \tilde{m}_t & 0 \\ x_1 & x_2 & x_3 & M \end{pmatrix} \cdot \begin{pmatrix} u_R \\ c_R \\ t_R \\ U_R \end{pmatrix} - M \bar{X}_L X_R + h.c. \end{aligned}$$

We can take  $x_3$  and  $M$  to be real and  $x_1$  and  $x_2$  to be complex.

## Mixing matrixes

Off-diagonal part (1-4, 2-4 components) is suppressed by light quark masses,

$$M_u = V_L \cdot \begin{pmatrix} m_u & & & \\ & m_c & & \\ & & m_t & \\ & & & m_{t'} \end{pmatrix} \cdot V_R^\dagger$$

Correction to the CKM matrix

$$\mathcal{L}_{W^\pm} = \frac{g}{\sqrt{2}} (\bar{u}_L, \bar{c}_L, \bar{t}_L, \bar{U}_L) \cdot \begin{pmatrix} 1 & & & \\ & 1 & & \\ & & 1 & \\ 0 & 0 & 0 & \end{pmatrix} \cdot \gamma^\mu \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} W_\mu^\pm + h.c.$$

$$g_{WL}^{Ij} = \frac{g}{\sqrt{2}} V_{CKM}^{Ij} = \frac{g}{\sqrt{2}} V_L^\dagger \cdot \begin{pmatrix} \tilde{V}_{CKM} \\ 0 & 0 & 0 \end{pmatrix}$$

Unitarity of 3x3 matrix is a slightly violated



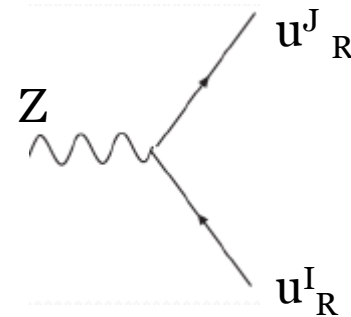
## Z boson FCNC coupling

$$\mathcal{L}_Z = \frac{g}{c_W} (\bar{u}_L, \bar{c}_L, \bar{t}_L, \bar{U}_L) \cdot \left[ \left( \frac{1}{2} - \frac{2}{3}s_W^2 \right) \begin{pmatrix} 1 & & & \\ & 1 & & \\ & & 1 & \\ & & & 1 \end{pmatrix} - \begin{pmatrix} & & & \\ & & & \\ & & & \\ & & & 1 \end{pmatrix} \right] \gamma^\mu \cdot \begin{pmatrix} u_L \\ c_L \\ t_L \\ U_L \end{pmatrix} Z_\mu$$

$$g_{ZL}^{IJ} = \frac{g}{c_W} \left( \frac{1}{2} - \frac{2}{3}s_W^2 \right) \delta^{IJ} - \frac{g}{c_W} V_L^{*,4I} V_L^{4J}$$

$$g_{ZR}^{IJ} = \frac{g}{c_W} \left( -\frac{2}{3}s_W^2 \right) \delta^{IJ} - \frac{1}{2} \frac{g}{c_W} V_R^{*,4I} V_R^{4J}$$

The most important phenomenological effects arise from the right-handed Z-boson FCNC coupling.



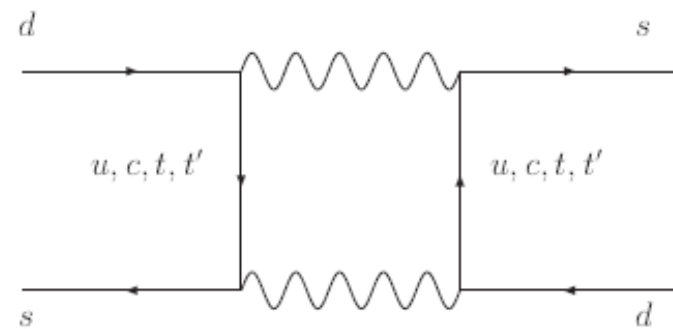
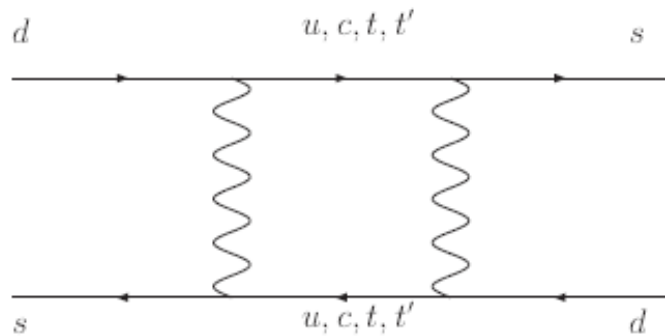
# Constraints on $V_R^{41}$ and $V_R^{42}$

Constraints on  $V_R$  come from right handed Z-FCNC processes.  
Most important processes are DD mixing and atomic parity violation .

$D_0-\bar{D}_0$ mixing	$ V_R^{41}   V_R^{42}  < 3.2 \times 10^{-4}$
APV in Cs	$ V_R^{41}  < 7.8 \times 10^{-2}$
LEP1, charm couplings	$ V_R^{42}  < 0.2$
Tevatron: $t \rightarrow Zc, Zu$	$ V_R^{43}  \sqrt{ V_R^{41} ^2 +  V_R^{42} ^2} < 0.28  V_{tb} $
$D$ meson decays	none

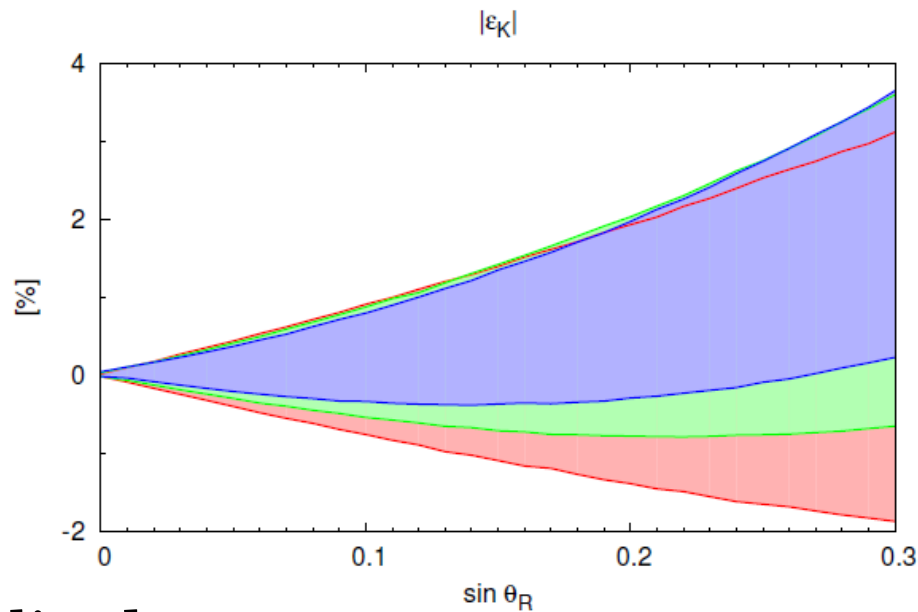
# Contribution to KK and BB mixing

We have calculated Kaon,  $B_d$ , and  $B_s$  mixing amplitudes including  $t'$  loop contribution. Deviations from the SM is not very large in general. For the  $B_s$  mixing, we find that a sizable change of the  $B_s$  box phase is possible. This can be distinguished at the LHCb experiment.



$\varepsilon_K$ 

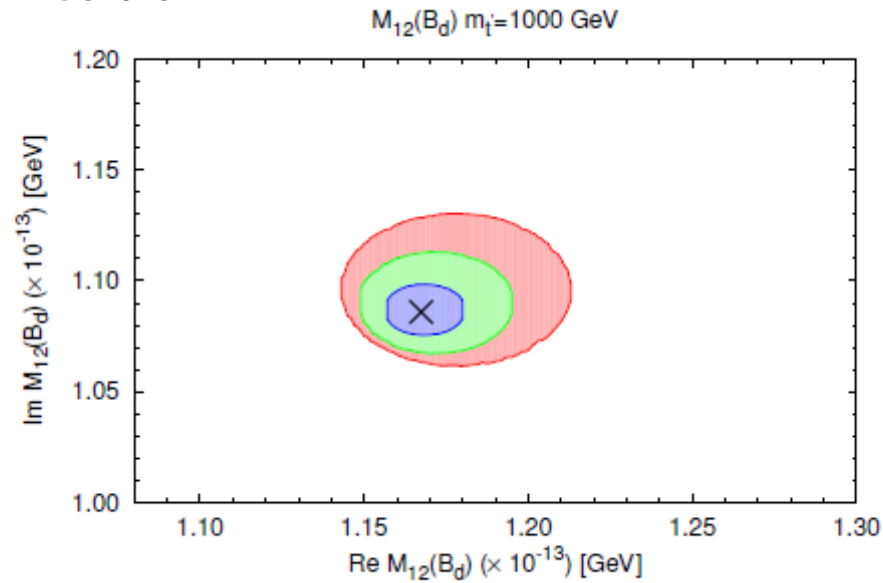
Less than 5%



$M=350$  GeV (blue)  
 $500$  GeV (green)  
 $1000$  GeV (red)

Bd mixing amplitude

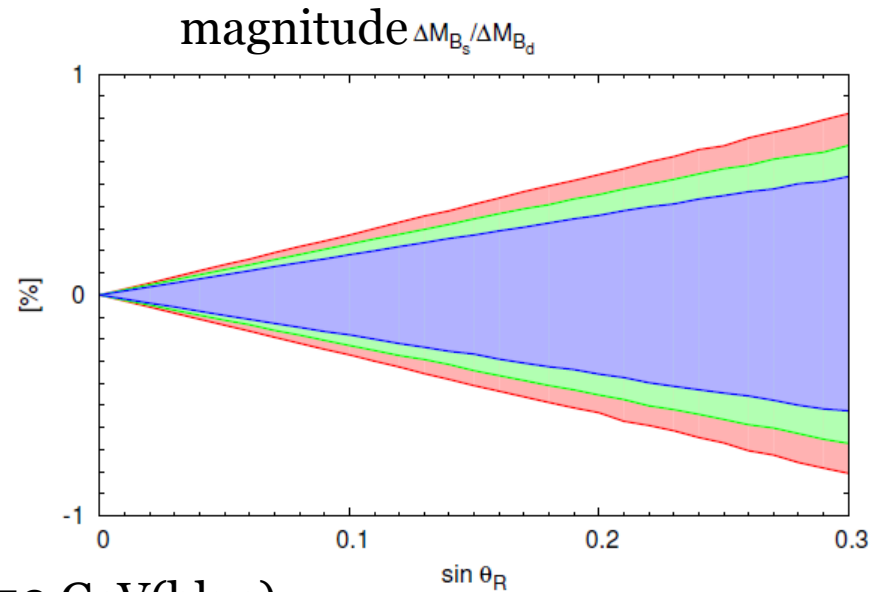
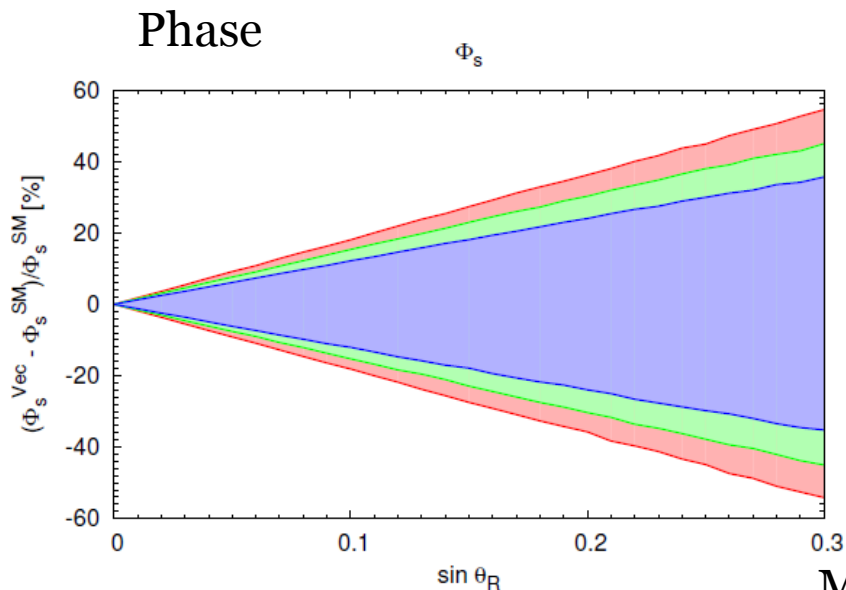
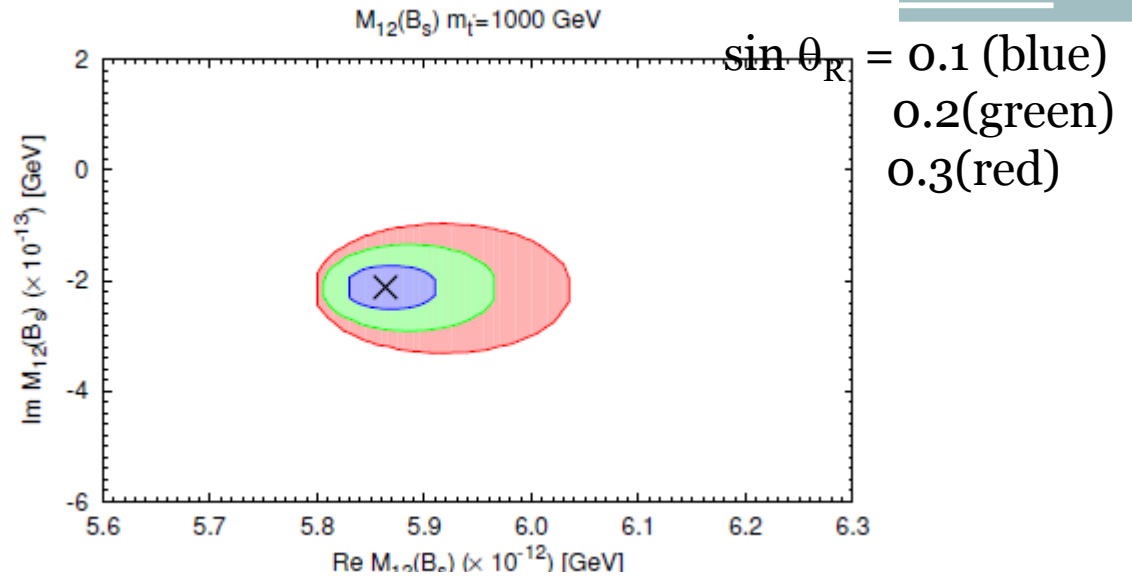
A few %



$\sin \theta_R = 0.1$  (blue)  
 $0.2$  (green)  
 $0.3$  (red)

# Bs mixing amplitude

The phase of the Bs mixing can be different from the SM up to 60%. Promising to be checked with CPV in  $B_s \rightarrow J/\psi \phi$ .



$M=350 \text{ GeV}$  (blue)  
 $500 \text{ GeV}$  (green)  
 $1000 \text{ GeV}$  (red)

# Summary

- We have clarified vector-like  $t'$  models.
- Phenomenological constraints on off-diagonal Yukawa coupling constants are quite different for various cases.
- FCNC decays  $t' \rightarrow Zt$ ,  $t' \rightarrow ht$  are as important as or more important than  $t' \rightarrow Wb$ .
- An interesting case is the non-SM doublet model where a large new Yukawa coupling constant is allowed.
- Right-handed Z boson FCNC processes and CP violation in the  $B_s$  mixing is promising flavor physics signals.
- Single  $t'$  production is an interesting possibility at LHC.