

Detectors for Muon Colliders

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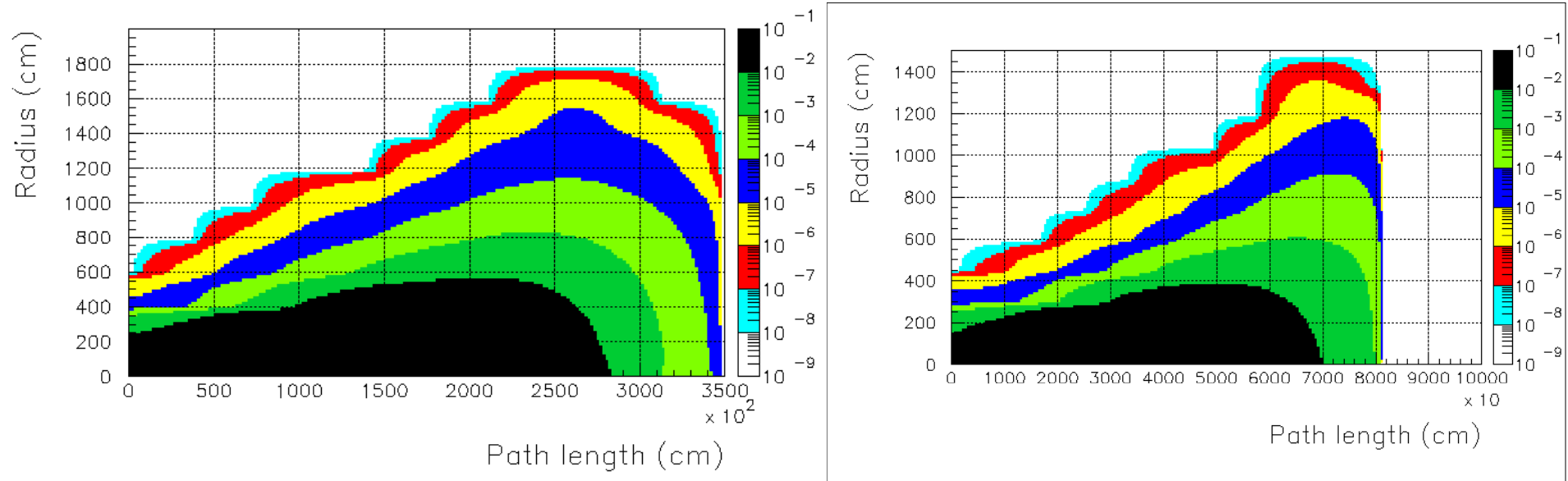
Summary of talk

- Backgrounds and radiation near accelerator
- Neutrino Induced Radiation
- Halo Backgrounds
- Pair production at IP
- Muon Decay Background at IP
 - » Design of Interaction area shielding
 - » Neutrons
 - » Photons
 - » Bethe-Heitler Muons
- Detector Options
- Detector Simulation plans
- Measurement of energy scale using $g-2$ precession

Muon Colliders then and now

Root(s) TeV	0.1	0.1 Scan width	0.4	3.0	1.5
Proton Energy GeV	16		16	16	8
Bunches/ beam	1		2	2	1
Luminosit y 10^{34} cm ² /s	2.2×10^{31}	10^{31}	10^{33}	7×10^{34}	1.3×10^{34}
Higgs/yr	3.9×10^3	4×10^3			

Backgrounds and radiation near accelerator-MARS calculations

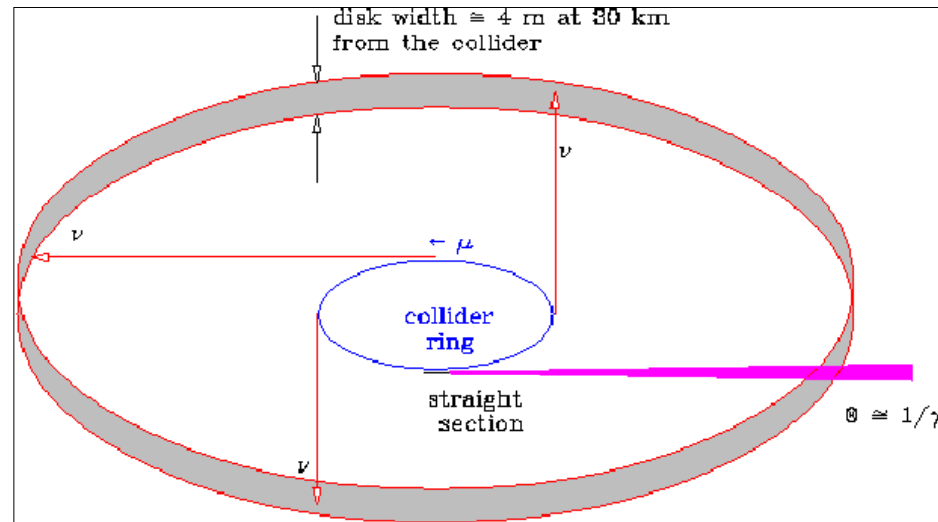


- Isodose contours in soil/rock for 2 TeV and 250 GeV muons extracted from ring at 3×10^{13} /second. Right scale is dose rate in rem/s.

Backgrounds and radiation near accelerator

- 4 Tev collider has the following activation levels immediately and 1 day after turn off after 5 years of operation.
 - » Inside face of shield 9000 (4000)mrem/hr
 - » Outside face of shield 200(170)mrem/hr
 - » Outside of coils 30(14)mrem/hr
 - » Outside of yoke 3(1.4)mrem/hr
- Muons lost from collider have a range of 3.5Km (800 m) at 2TeV(250GeV) beam energy in soil/rock of density 2.24g/cm^3 .
- To confine this radiation beneath the ground, one can deflect extracted beams down by 4.5 mrad at 2TeV and 10 mrad at 250 GeV .
- Federal limit is reached at maximum radii of 18m (2TeV) and 14.5 m (250 GeV)

Neutrino Induced Radiation



$$DB = 4.4 \times 10^{-24} I_{\mu} E^3 t \langle B \rangle / (Bd)$$

Where $DB(Sv)$ is the radiation dose acquired over time t sec in the plane of a bending field B (Tesla) in a circular collider of energy E (TeV) and average field $\langle B \rangle$ (Tesla) and muon current of I_{μ} (muons/sec/sign) buried at depth d (meters)

Neutrino radiation

- In the case of a high beta straight section of length l (meters),

$$D_s = 6.7 \times 10^{-24} I_\mu E^3 \dagger l \langle B \rangle / d$$

- For a low beta IP region, these formulae do not apply, since they assume that the divergence angles of the beam $\ll 1/\gamma$.
- For 3 TeV Com energy, $I_\mu = 6 \times 10^{20} \mu/\text{yr}$, $\langle B \rangle = 6\text{T}$, $B = 10\text{T}$ and $d = 500\text{m}$ and taking the federal off site limit $D_{\text{fed}} = 1\text{mS}_V/\text{year}$ (100 mrem/year) the annual dose D_B in the plane of the bending dipole is

$$D_B = 1.07 \times 10^{-5} S_V = 1\% D_{\text{fed}}.$$

For a straight section of length 0.6m,

$$D_s = 9.7 \times 10^{-5} S_V = 10\% D_{\text{fed}}.$$

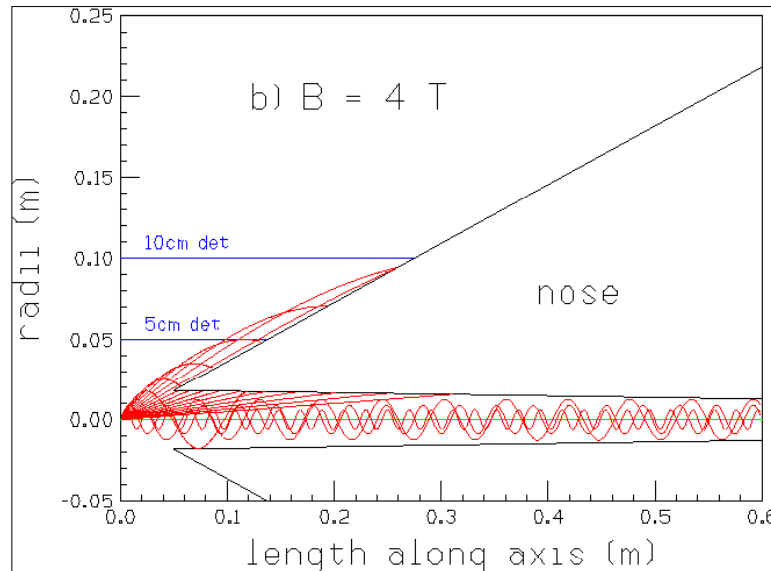
Beam manipulation tricks can be played. We feel that 3 TeV collider can be buried at ~ 300 meters.

Halo Background

- More work needs to be done in calculating injection losses and to develop a credible model for beam halo and beam losses.
- Beam gas scattering has been studied and shown to be a negligible source of beam halo generation.
- Beam-beam effects need further study.
- A scraper system has been studied and shown to suppress halos by a factor of 10^3 .

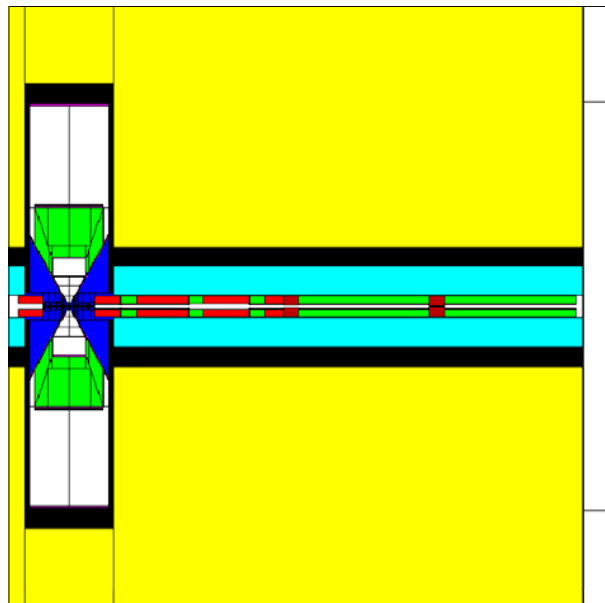
e^+e^- pair production at IP

- Coherent beam-beam electron pair production (beamstrahlung) has been shown to be negligible.
- Incoherent production ($\mu\mu \rightarrow \mu\mu ee$) in the 4 TeV collider case is significant-10mb of cross section!



- Electrons with momenta from 3.8 MeV to 3000 MeV for the 4 Tesla solenoid detector.

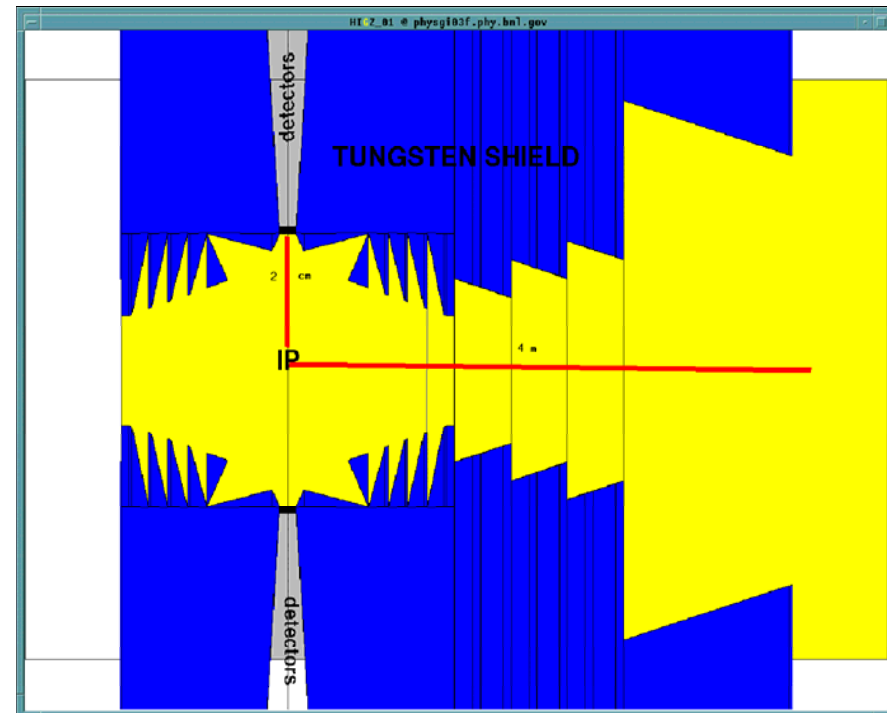
Muon decay background-Design of shielding



- Region up to 130 m from the IP for 4 TeV collider. Triangular blue regions represent tungsten shielding. Red areas represent quadrupoles in beamline. Geant calculations done. Detector (white +green) is 10 m in diameter and 20 meters long.

Muon decay background-Design of shielding

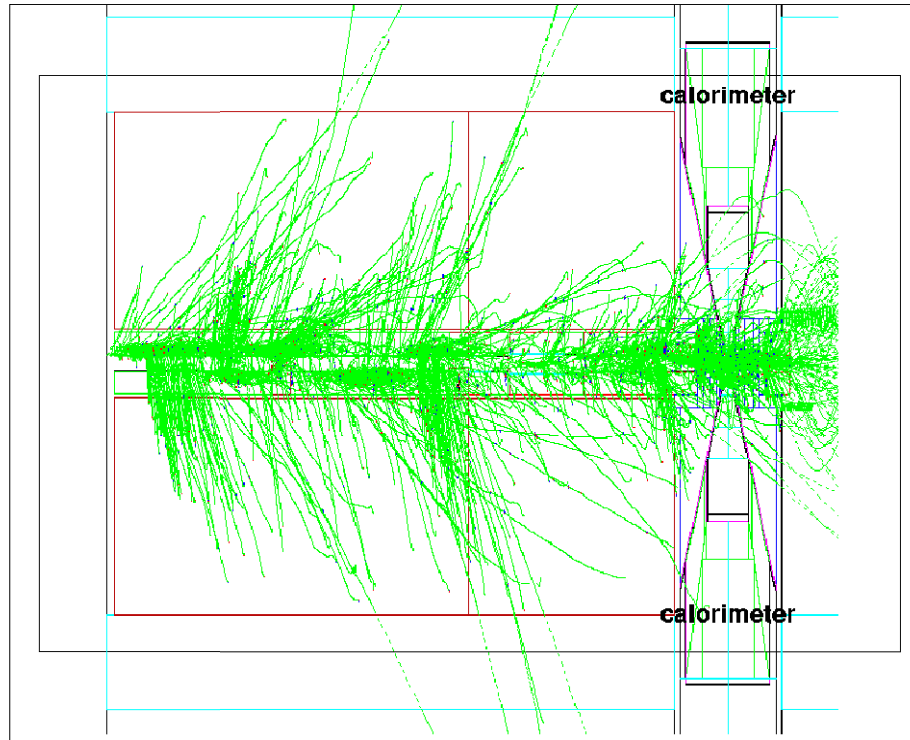
- IP design for 100GeV CoM collider. It is designed so that the detector is not connected by a straight line with any surface hit by decay electrons in forward or backward directions. Y axis goes to 6 cm and X axis 4 meters from IP.



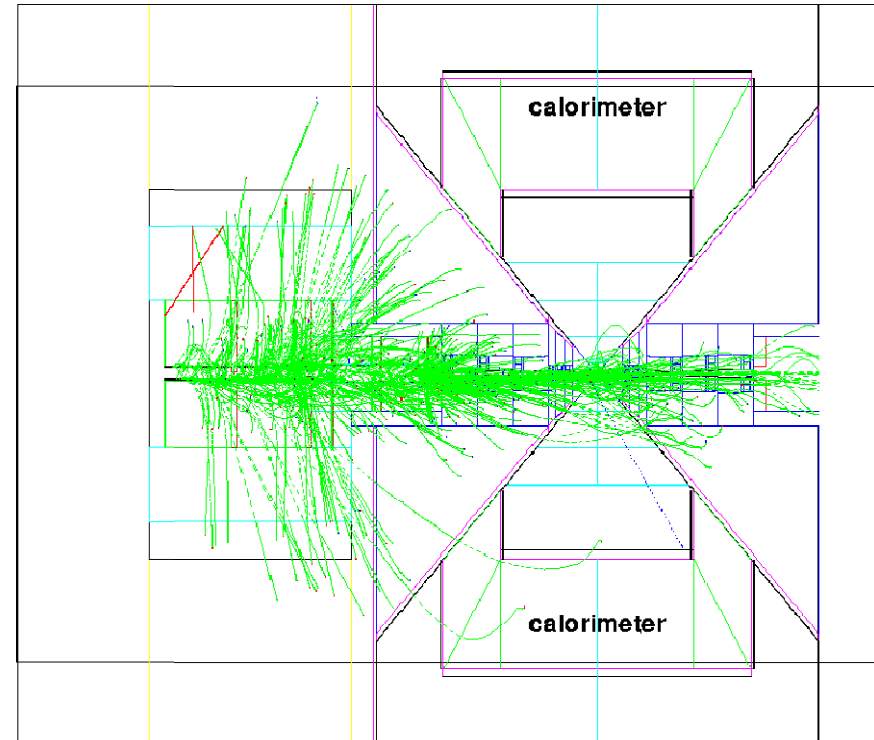
Muon Decay backgrounds

- For a 4 TeV CoM collider, 4×10^{12} muon per bunch and 4×10^5 muon decays per meter.
- The off-energy, off-axis electrons undergo brehmsstrahlung when they traverse magnetic fields. When they exit the beam pipe, they produce electromagnetic showers and to a lesser extent hadrons and muons (Bethe-Heitler muons).
- The showers produce
 - » Low energy photons of ~ 1 MeV. These enter the detector and produce knock-on electrons.
 - » Photons interact with nuclei (Giant dipole resonance) and produce neutrons. These enter the detector and produce knock-on protons.
 - » Muon pairs are produced instead of electron pairs ($\sim 1/10^4$) by photons in EM showers. These are called Bethe_Heitler muons and cause problems when they are energetic and enter the detector

Bethe-Heitler Muons



4 TeV cms collider- $x = 130\text{m}$,
 $y = 4\text{m}$. $< 1\%$ tracks end in
calorimeter

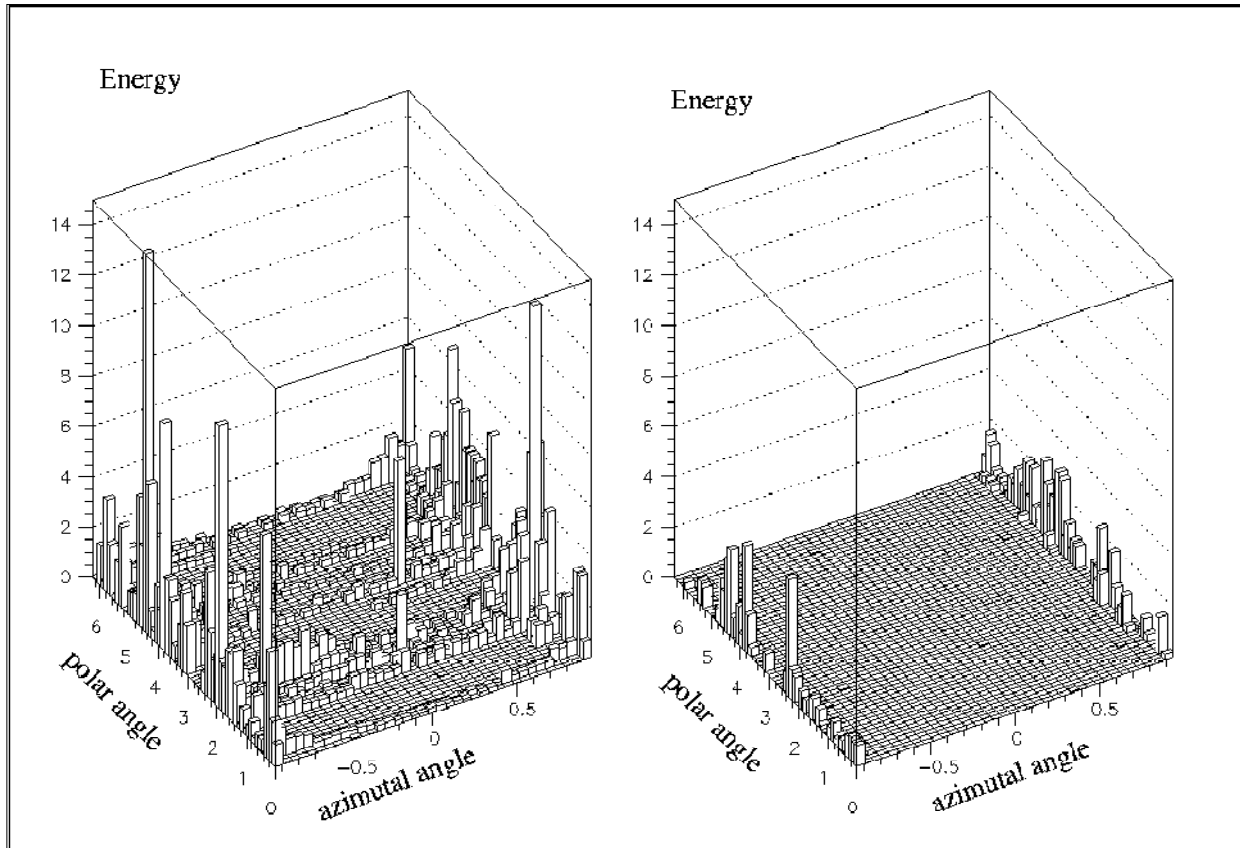


100 GeV cms collider- $x = 20\text{m}$,
 $y = 4\text{m}$. $< 0.5\%$ tracks end in
calorimeter

Bethe-Heitler Muons

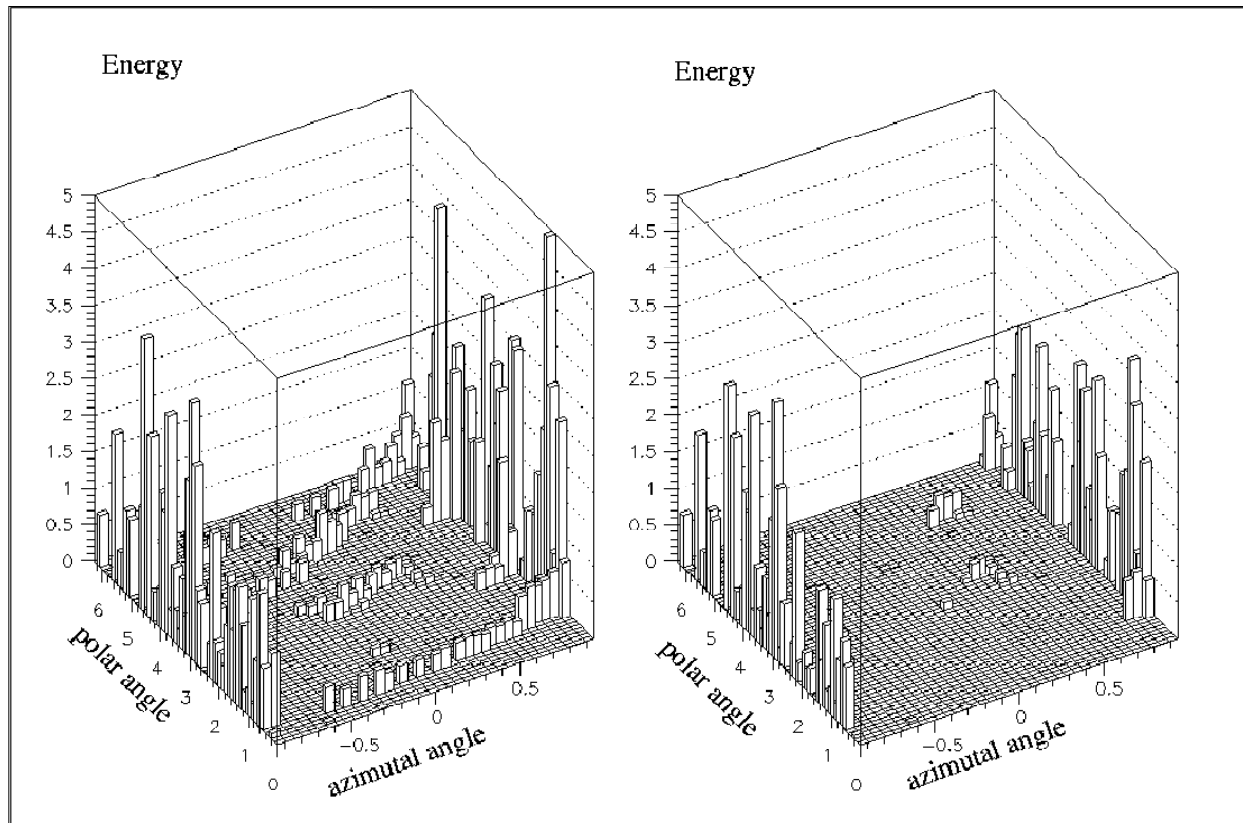
<i>CoM Collider Energy (TeV)</i>	<i>4</i>	<i>0.5</i>	<i>0.1</i>
<i>Assumed source length</i>	~ 30	33	20
<i>$\mu(p_\mu > 1 \text{ GeV}/c)$ per electron</i>	5.4×10^{-4}	8.3×10^{-5}	9.6×10^{-5}
<i>Beam μ's per bunch</i>	2×10^{12}	2×10^{12}	4×10^{12}
<i>Bethe-Heitler μ's per crossing</i>	28000	17500	6100
<i>$\langle p_\mu \rangle$ initial GeV</i>	22	9.5	4.4
<i>μ's in calorimeter</i>	220	160	25
<i>Deposited energy GeV/muon</i>	2.9	1.3	0.4
<i>Total deposited energy GeV</i>	640	210	10
<i>Pedestal Subtracted E dep. GeV</i>	50	25	1
<i>Fluctuation in E dep. GeV</i>	55	15	1
<i>Transverse energy GeV(p.s)</i>	15	15	.5
<i>Fluctuation E trans</i>	40	8	0.5

Bethe-Heitler Muons



LHS 4 TeV collider. RHS with 1 ns timing cut

Bethe-Heitler Muons

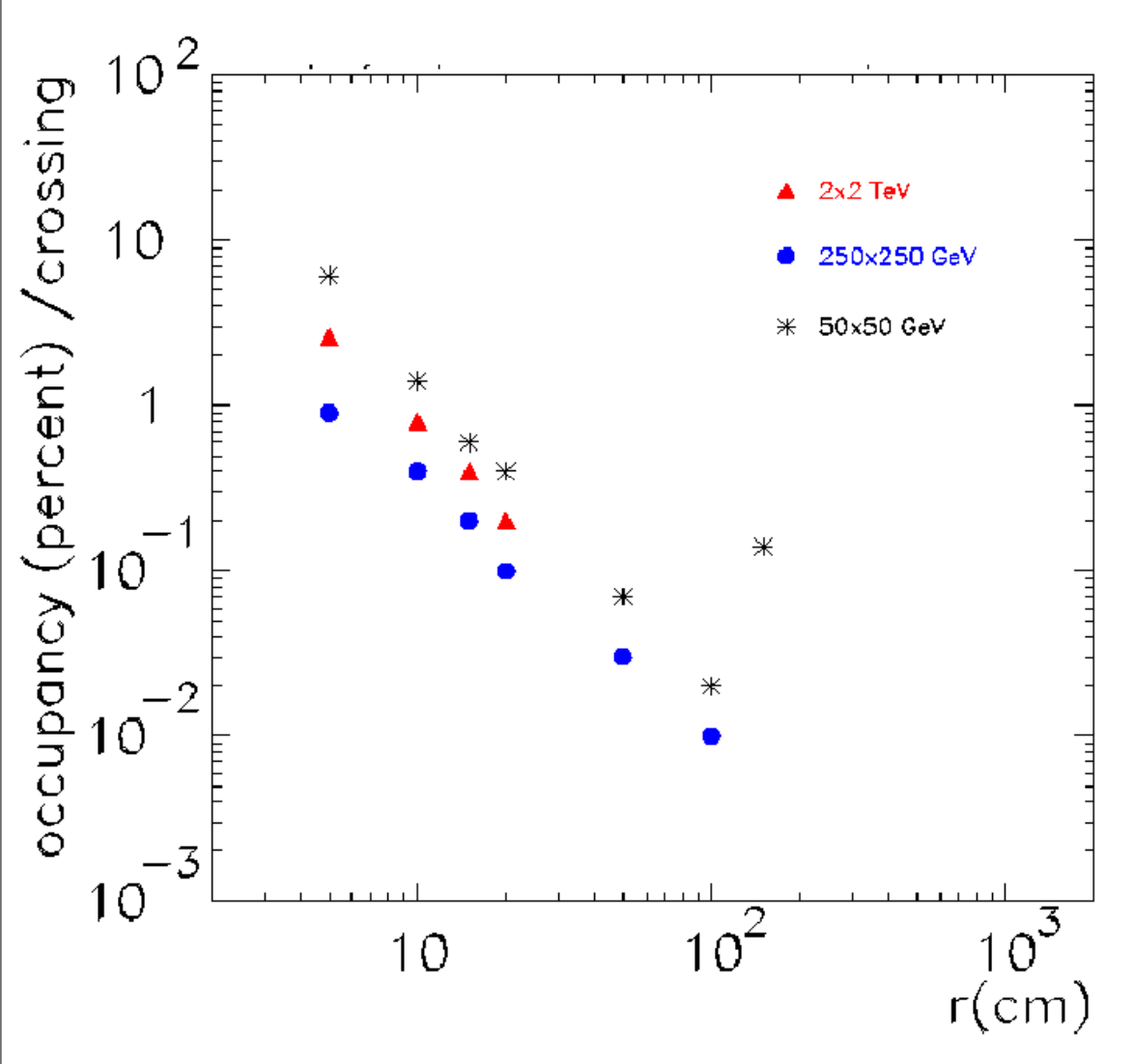


0.5 TeV cms collider. RHS with 1 ns timing cut

Background Summary

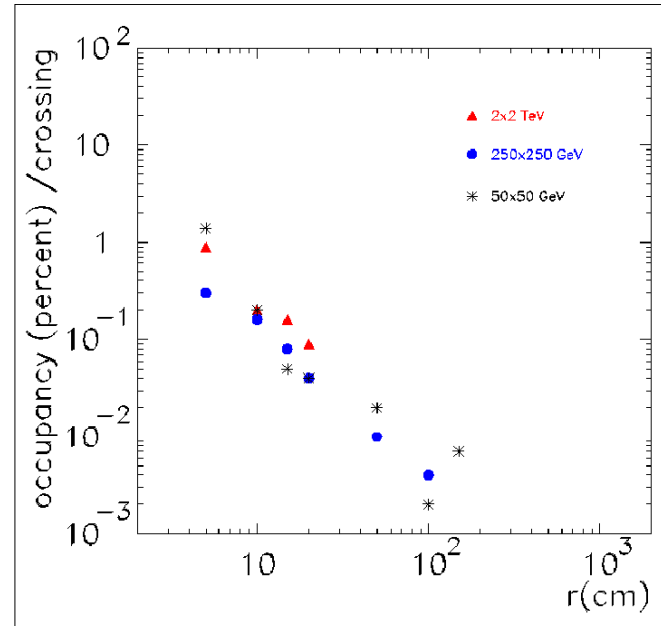
Neutral particles

Occupancy for 300 micron square silicon pads as a function of cms energy and radius from IP



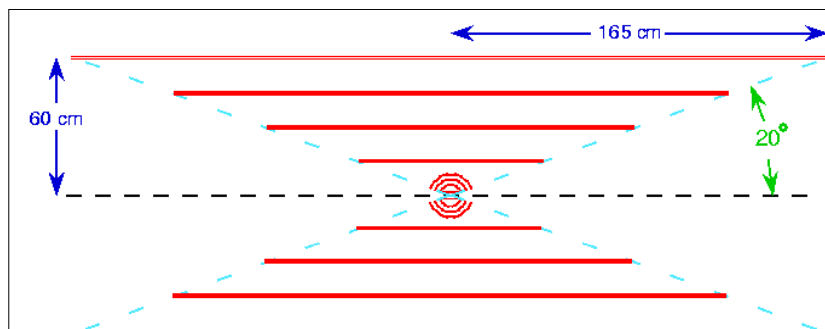
Background Summary

Charged particles



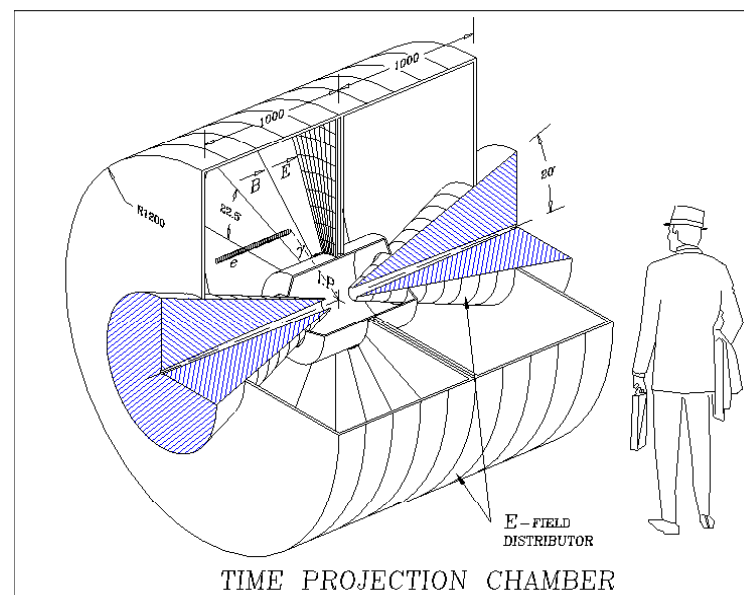
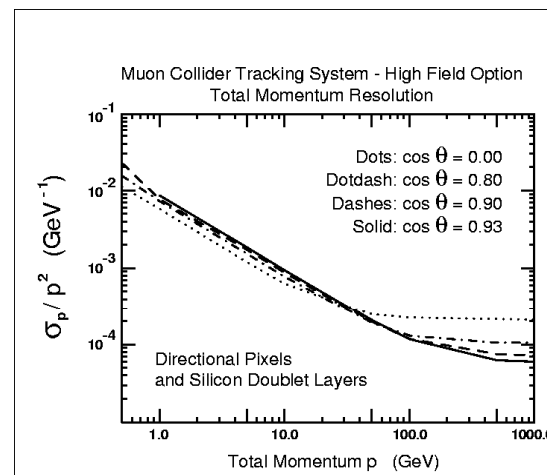
<i>Radius</i>	<i>cm</i>	<i>5</i>	<i>10</i>	<i>20</i>	<i>100</i>
<i>Photon hits</i>	cm^{-2}	26	6.6	1.6	0.06
<i>Neutron hits</i>	cm^{-2}	0.06	0.08	0.2	0.04
<i>Charged hits</i>	cm^{-2}	8	1.2	0.2	0.01
<i>Total hits</i>	cm^{-2}	34	8	2	0.12
<i>Pixel size</i>	$\mu\text{m} \times \mu\text{m}$	60 x 150	60 x 150	300x300	300 x 300
<i>Total occupancy</i>	%	0.6	0.14	0.4	0.02
<i>Occupancy from Charged particles</i>	%	0.14	0.02	0.04	0.002

Detector Scenarios

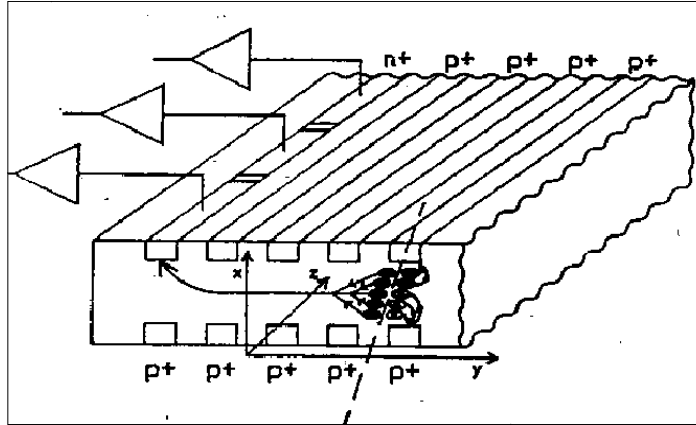


Silicon pixels surrounded by microstrips

TPC suitable for 3TeV collider. Gas with no hydrogen to minimize knockon protons

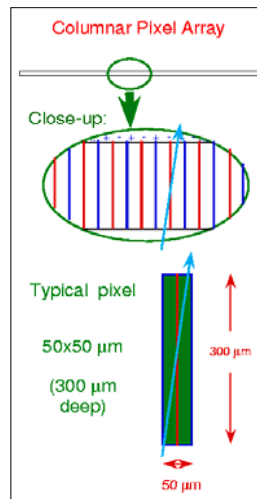


Detector Scenarios-Silicon

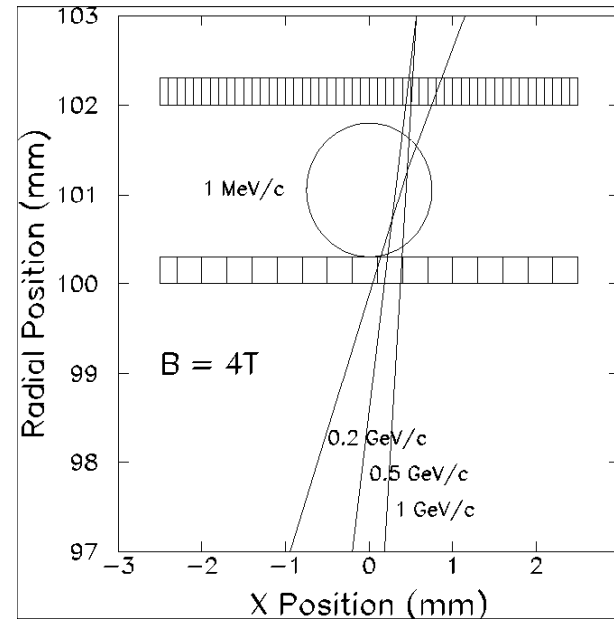


Silicon drift vertex detector

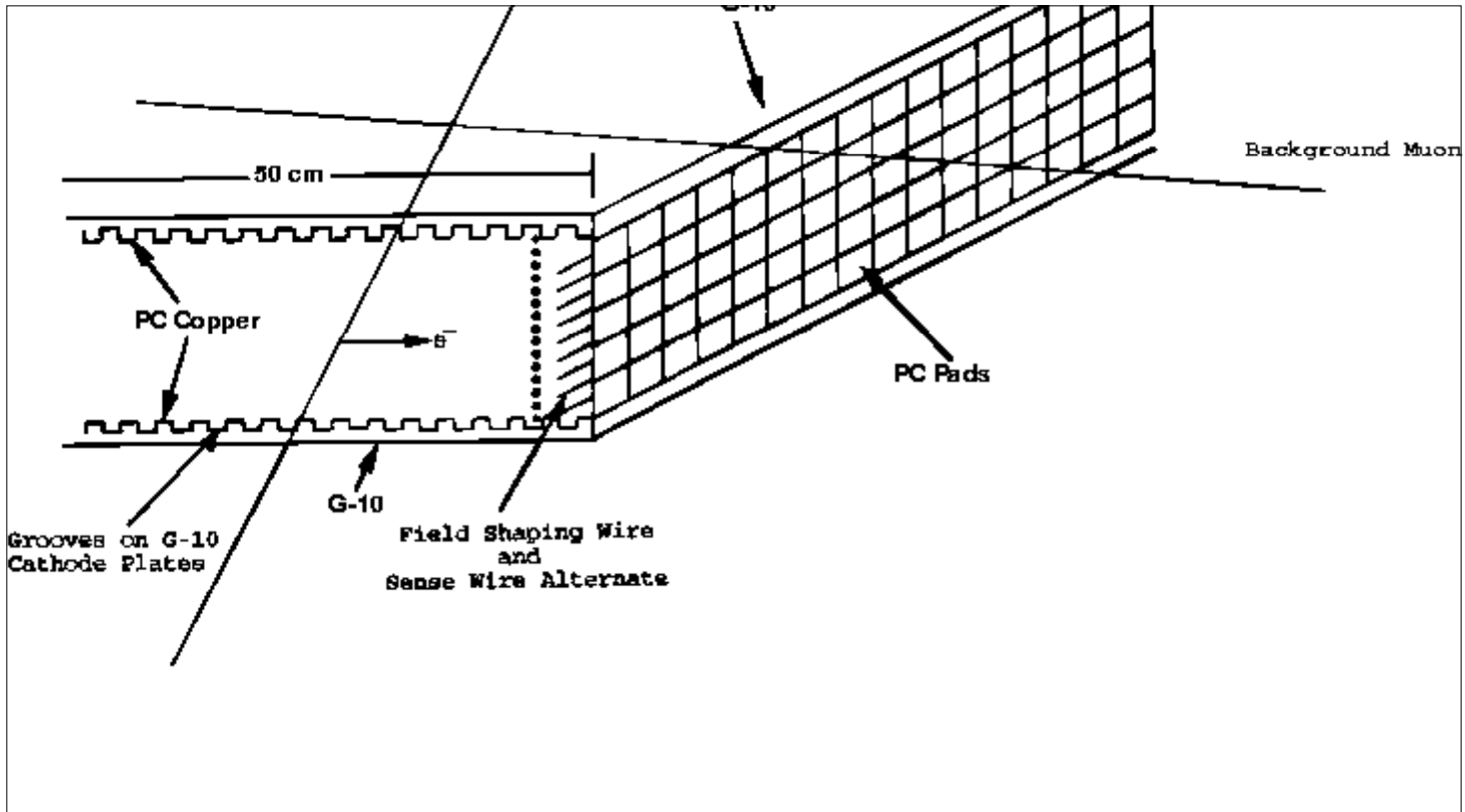
Columnar pixels



Pixel telescope



Muon Drift chambers with pads



**Effect of requiring Pixel Microtelescope
micro-coincidence**

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Paul Lebrun

At large angle ~ 60 degrees
~ 2,000 hits/layer, in the
same 10 degree cone
(perp. to the jet), at
the outer layers.

Projected onto
one doublet layer
at $r = 25$ cm

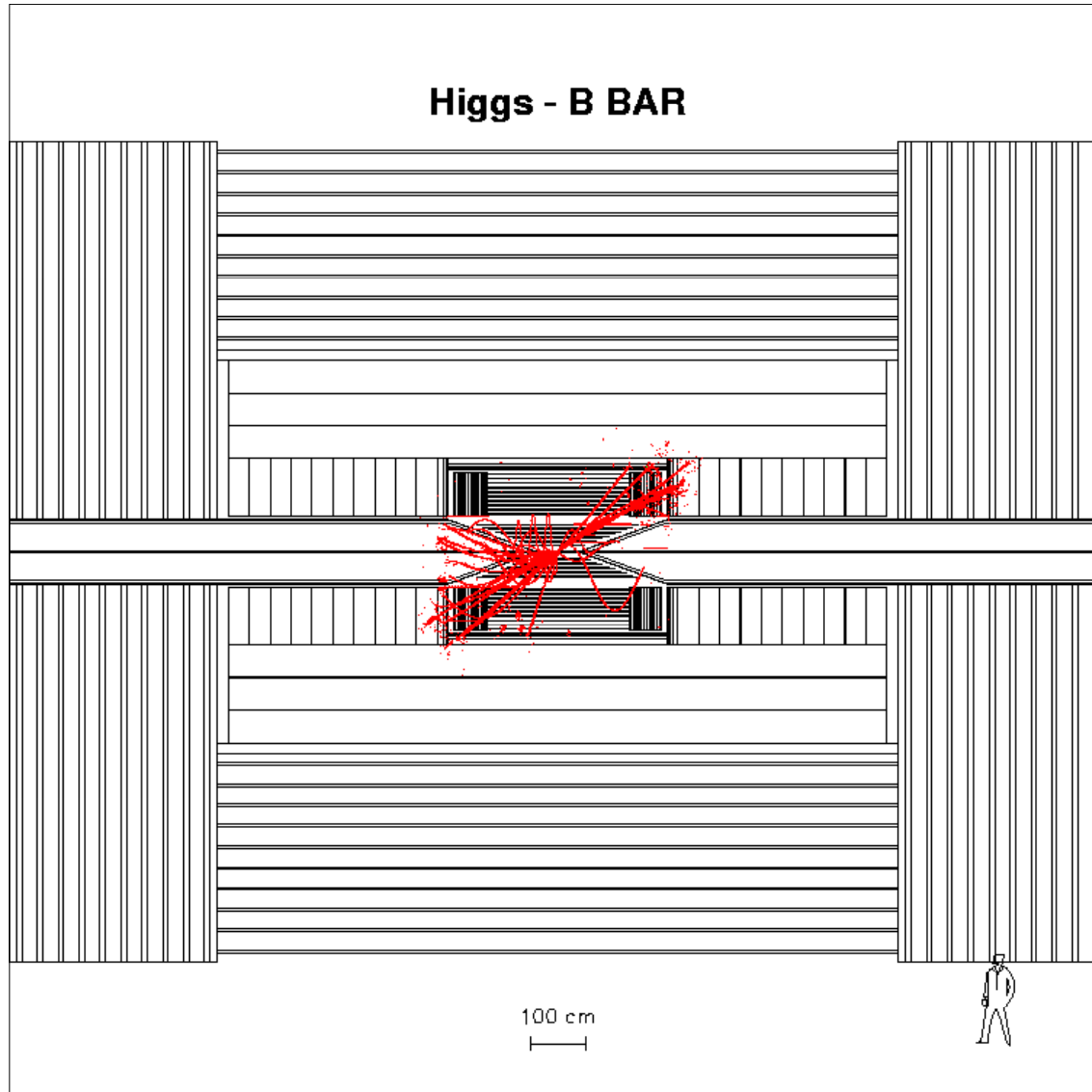
Tungsten

After cuts...,
only ~20 bck.
hits remains.

Tungsten

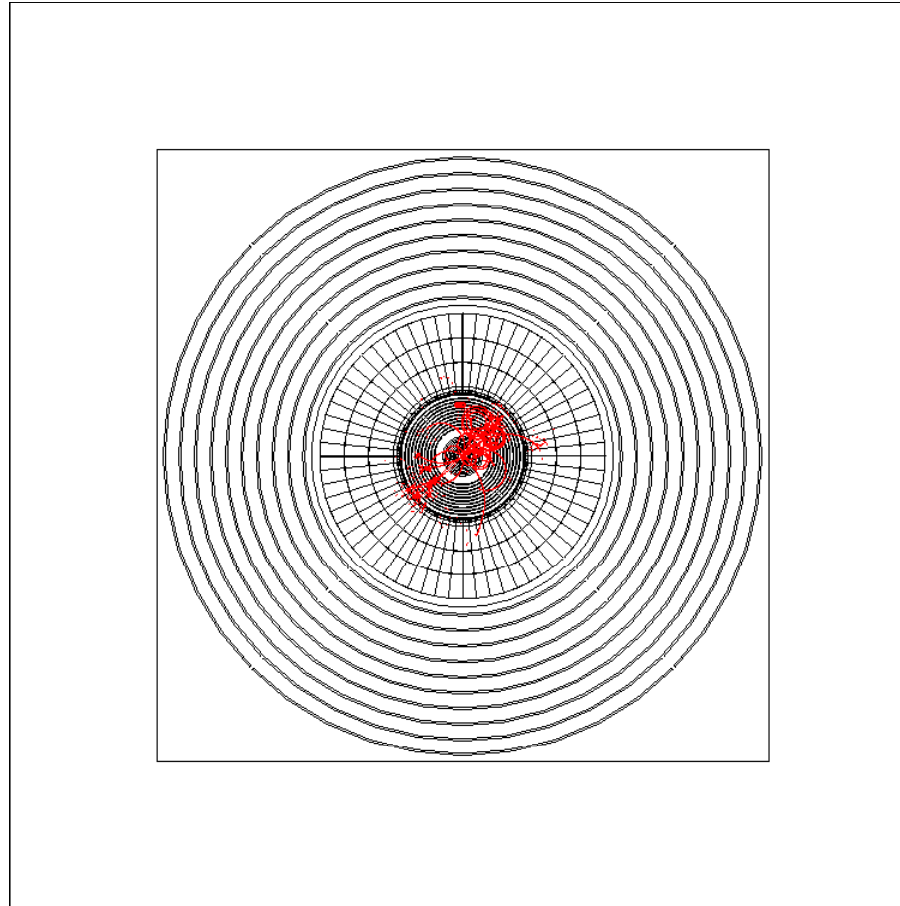
I.P.

Detector Simulation



Oct 23,2007

Detector Simulation



Jul 21,1999

Rajendran Raja, Mutac Review, FNAL

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Oct 23,2007

Rajendran Raja, Topical Workshop on Neutrino Factory and Muon Collider, Coseners House

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Simulation Questions to be answered

- Can one optimize the lattice near the interaction region to reduce the backgrounds further? (2 man-years)
- Can one do b-tagging using silicon pixels given the large number of hits caused by the photon background? (1 m.y.)
- What is the efficiency vs. purity of b-tagging? (1 m.y.)
- Can c-tagging be contemplated? (0.5 m.y.)

Simulation Questions to be answered

- How can one design a fast vertex algorithm so that silicon hits are readout only for projective coincidences in a pixel micro-telescope? (1 m.y.)
- Will a TPC work at all energies as an outer tracker? (1 m.y.)
- What segmentation does the calorimeter need to possess to pattern recognize Bethe-Heitler muons? (0.5 m.y.)
- What e/π ratio, linearity and resolution are necessary for the calorimeter? (0.5 m.y.)

Simulation Questions to be answered

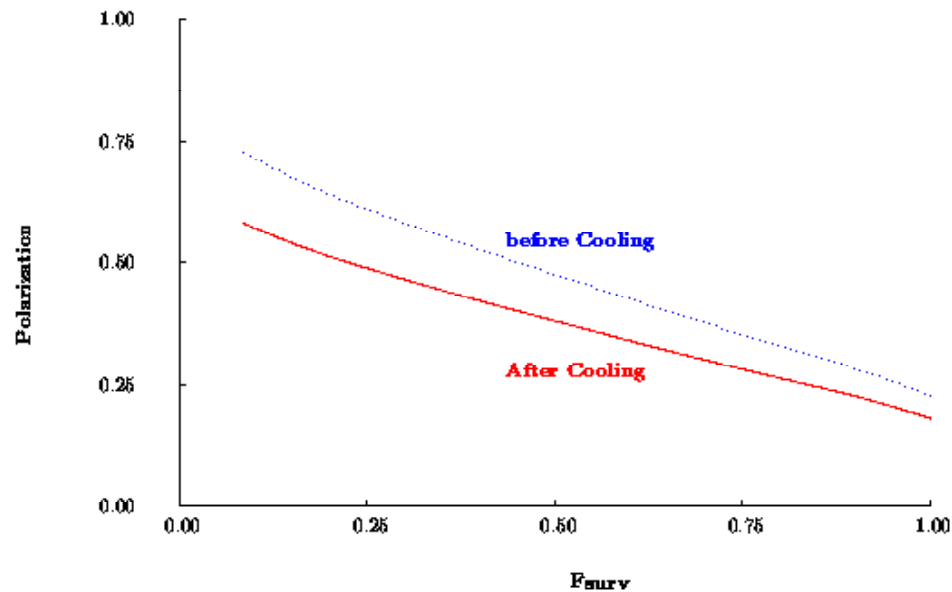
- Are there calorimeters that will permit the measurement of arrival times to 1 ns? (0.5 m.y.)
- How much distortion is there in the measured energies of jets and electrons as a function of background? (0.5 m.y.)
- Can one compute the pedestal energy deposits in the calorimeter resulting from the heavy neutron background which will vary as a function of the turn by turn muon intensity? (0.5 m.y.)

Simulation Questions to be answered

- Do we need a muon system? Or is it better to have a deeply segmented calorimeter that will pattern recognize muons as minimum ionizing tracks? (0.5 m.y.)
- Can one detect forward going muons from the interactions? (0.5 m.y.)
- How do we compare with the NLC in those physics channels outlined above that can be realized in both types of accelerator? (2 m.y.)

Muon Collider Physics—Polarization Precession

- Polarization of muons will play a crucial role in many physics areas.
- Both charges polarizable.
- Physics with rotating polarization addressed by Grzadkowski, Gunion et al Nucl.Phys.B583:49-75,2000



Calibrating the energy of the collider to $1E-6$

Bargmann-Michel-Telegdi Equation

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S}$$

$$\vec{\Omega} = -\frac{e}{m\gamma} \left((1+a\gamma)\vec{B}_\perp + (1+a)\vec{B}_\parallel - \left(a\gamma + \frac{\gamma}{1+\gamma} \right) \vec{\beta} \times \frac{\vec{E}}{c} \right)$$

$$\vec{\Omega} = \vec{\Omega}_{\text{cyc}} (1+a\gamma)$$

$$a = (g-2)/2$$

B_\perp, B_\parallel are the components of magnetic field
perpendicular and parallel particle direction

This equation controls the evolution of the spin vector \vec{S} . Polarization is the average of the spin vectors over the muon ensemble. Per revolution spin rotates by $a\gamma 2\pi$ radians more than momentum

Method described in R.Raja and A. Tollestrup, Phys. Rev. D58(1998)013005

Decay particle energy distribution

In the muon rest frame, E is the energy of the electron. Its fractional energy expressed in terms of the maximum energy ($m_\mu/2$) is x . N is the number of muon decays. θ is the angle of the electron in the muon center of mass w.r.t muon direction. $\langle E \rangle$ is the average electron energy and $\langle P_L \rangle$ is the average longitudinal electron momentum in the muon rest frame.

P is the z component of the muon polarization along the muon direction. \hat{P} is charge* P of the muon.

$$x = 2E / m_\mu$$

$$\frac{d^2 N}{dx d \cos \theta} = N(x^2(3-2x) - \hat{P}x^2(1-2x)\cos\theta)$$

$$\langle E \rangle = \frac{m_\mu}{2N} \iint x \frac{d^2 N}{dx d \cos \theta} dx d \cos \theta = \frac{7}{10} \frac{m_\mu}{2}$$

$$\langle P_L \rangle = \frac{m_\mu}{2N} \iint x \cos \theta \frac{d^2 N}{dx d \cos \theta} dx d \cos \theta = \frac{\hat{P}}{10} \frac{m_\mu}{2}$$

Muon neutrinos have identical distribution to electrons. Electron anti-neutrinos have the following distribution.

$$\frac{d^2 N}{dx d \cos \theta} = 6(x^2(1-x) - \hat{P}x^2(1-x)\cos\theta)$$

$$\langle E \rangle = \frac{6}{20} m_\mu$$

$$\langle P_L \rangle = -\frac{\hat{P}}{10} m_\mu$$

Electron energy distributions

$$\langle E_{lab} \rangle = \frac{7}{20} E_{\mu} \left(1 + \frac{\beta}{7} \hat{P}\right)$$

$$E(t) = N e^{-\alpha t} \left(\frac{7}{20} E_{\mu} \left(1 + \frac{\beta}{7} (\hat{P} \cos \omega t + \phi)\right) \right)$$

$$\omega = \gamma \frac{g-2}{2} 2\pi$$

$$\alpha = \frac{t_{circ}}{\tau_{life}} = \frac{2\pi m_{\mu}}{0.3 B c t_{life}}$$

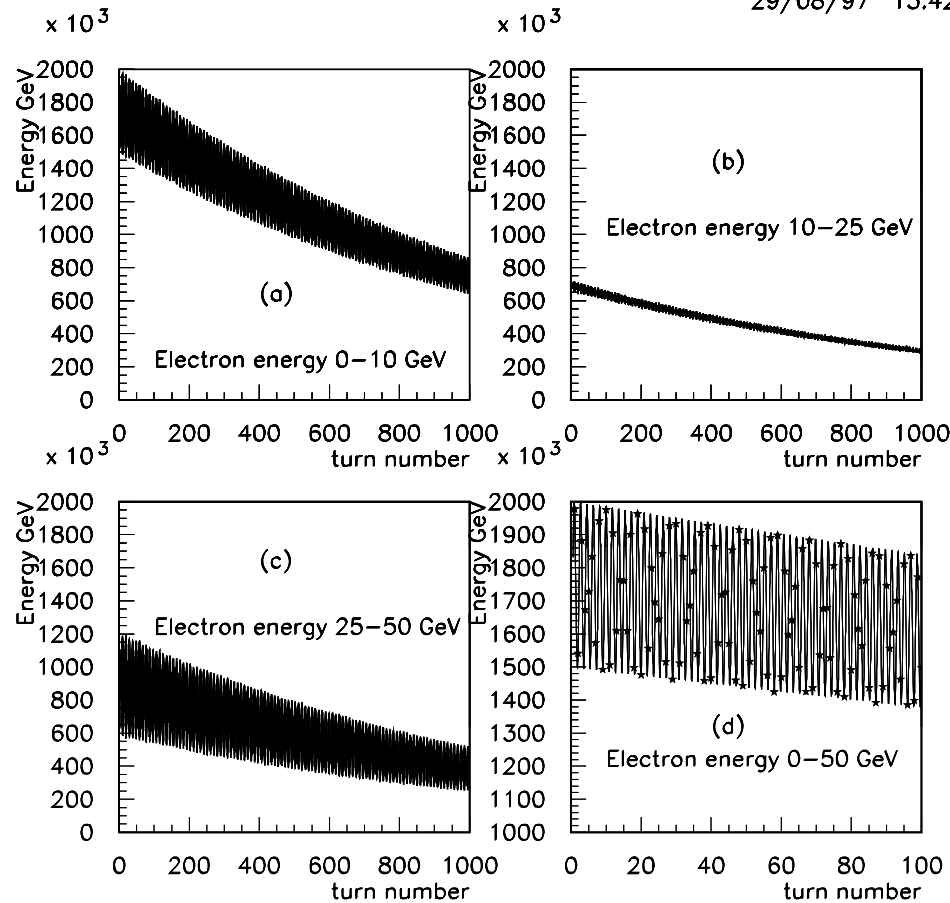
$$f(t) = A e^{-Bt} (C \cos(D + Et) + F)$$

$\langle E_{lab} \rangle$ is the average electron energy in lab. $E(t)$ is the total electron energy during turn t . Determine ω to get γ . γ information also present in α .

$f(t)$ is the fitting function. MINUIT used to fit and extract information.

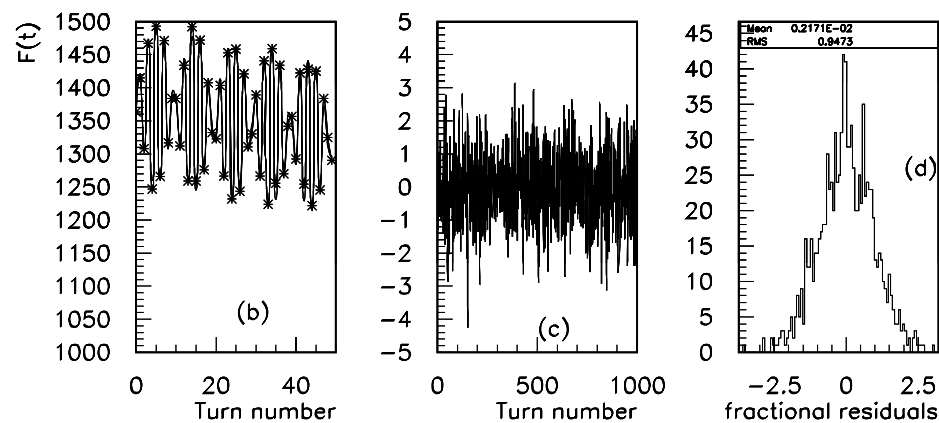
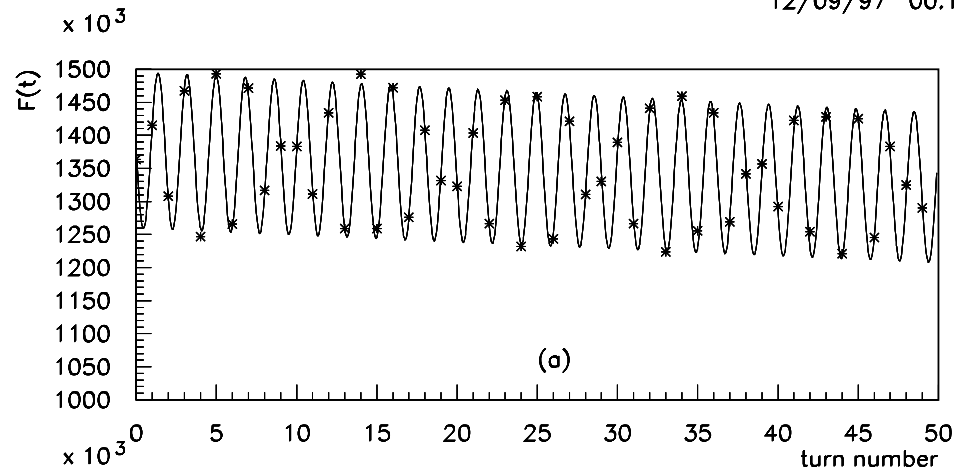
Electron lab energy spectrum $Pol=1.0$, 100K decays

29/08/97 13.42



Fit to 50 GeV μ^- , $P=0.26$ $\delta p/p=0.03E-2$

12/09/97 00.13



$\delta\gamma/\gamma$ vs measurement error and Polarization $\delta p/p=0.03E-2$

12/09/97 00.20

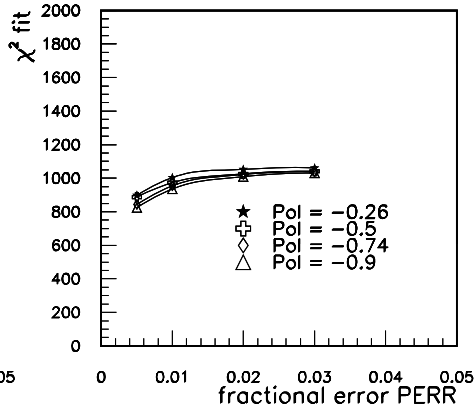
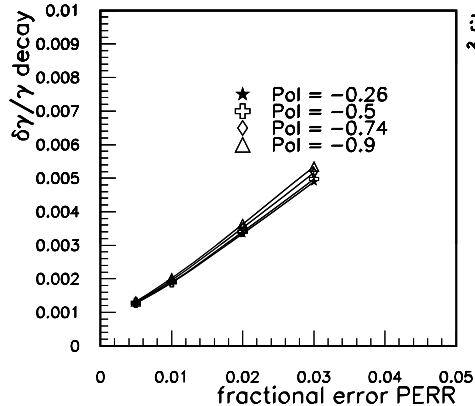
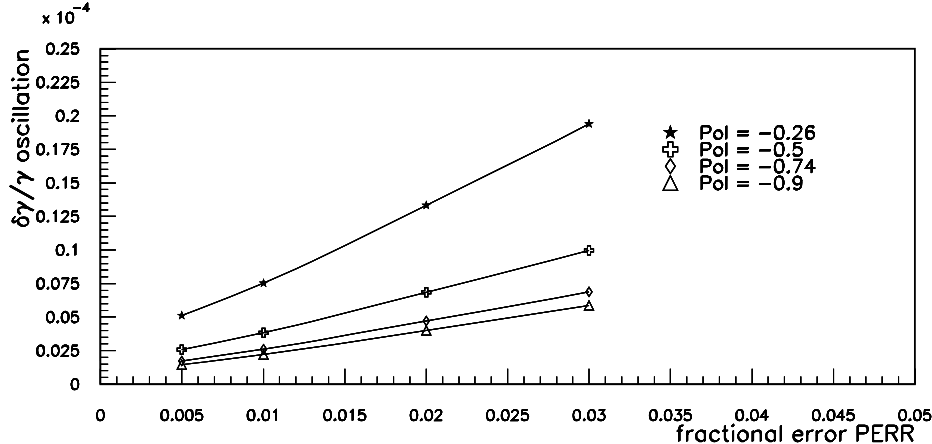


Table of fit parameters

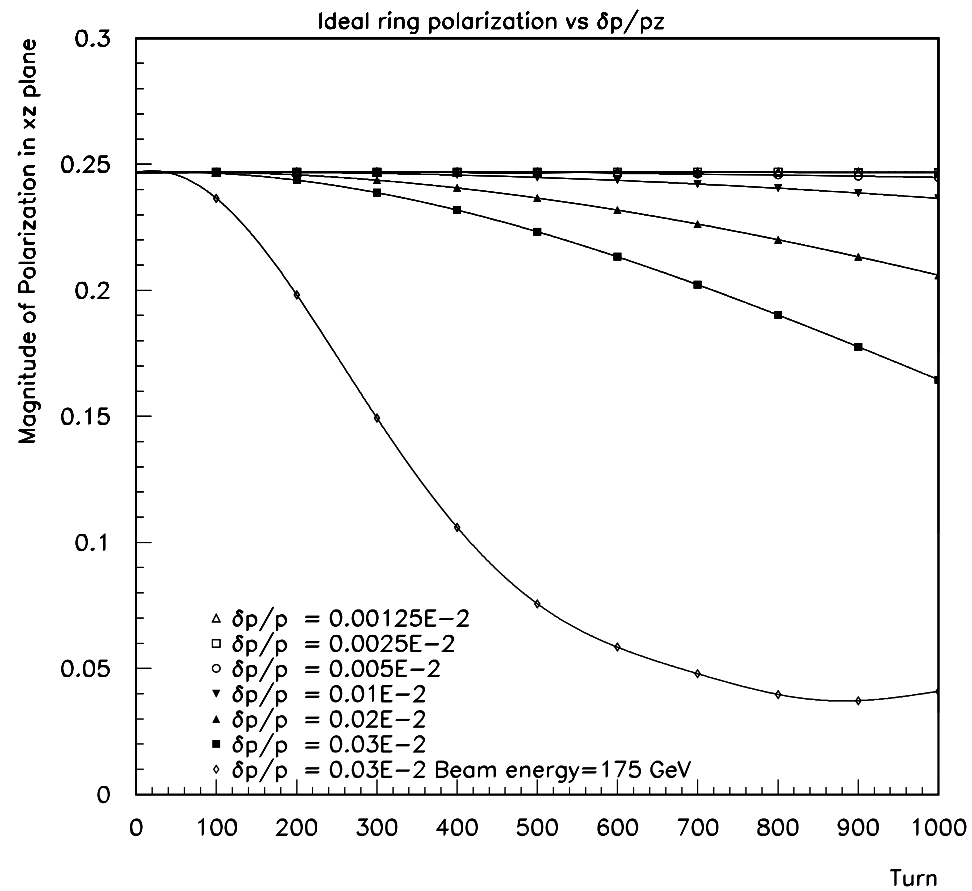
\hat{P}	PERR	Number of electrons sampled	$\delta\gamma/\gamma_{oscillations}$	$\delta\gamma/\gamma_{decay}$	χ^2 for NDF=1000
-0.90	0.50E-02	41261	0.14568E-05	0.13227E-02	824.
-0.90	0.10E-01	10315	0.22147E-05	0.20124E-02	936.
-0.90	0.20E-01	2579	0.39999E-05	0.36398E-02	1009.
-0.90	0.30E-01	1146	0.58659E-05	0.53457E-02	1030.
-0.74	0.50E-02	41261	0.17418E-05	0.13019E-02	843.
-0.74	0.10E-01	10315	0.26183E-05	0.19591E-02	954.
-0.74	0.20E-01	2579	0.46981E-05	0.35229E-02	1021.
-0.74	0.30E-01	1146	0.68765E-05	0.51672E-02	1039.
-0.50	0.50E-02	41261	0.25903E-05	0.12813E-02	888.
-0.50	0.10E-01	10315	0.38407E-05	0.19029E-02	973.
-0.50	0.20E-01	2579	0.68338E-05	0.33972E-02	1026.
-0.50	0.30E-01	1146	0.99744E-05	0.49749E-02	1041.
-0.26	0.50E-02	41261	0.51242E-05	0.12688E-02	898.
-0.26	0.10E-01	10315	0.75317E-05	0.18791E-02	1004.
-0.26	0.20E-01	2579	0.13324E-04	0.33447E-02	1053.
-0.26	0.30E-01	1146	0.19380E-04	0.48950E-02	1061.

TABLE I. Results of fits for $\delta\gamma/\gamma$ as a function of polarization \hat{P} and noise PERR. Also shown

is the χ^2 of the fit for 1000 turns.

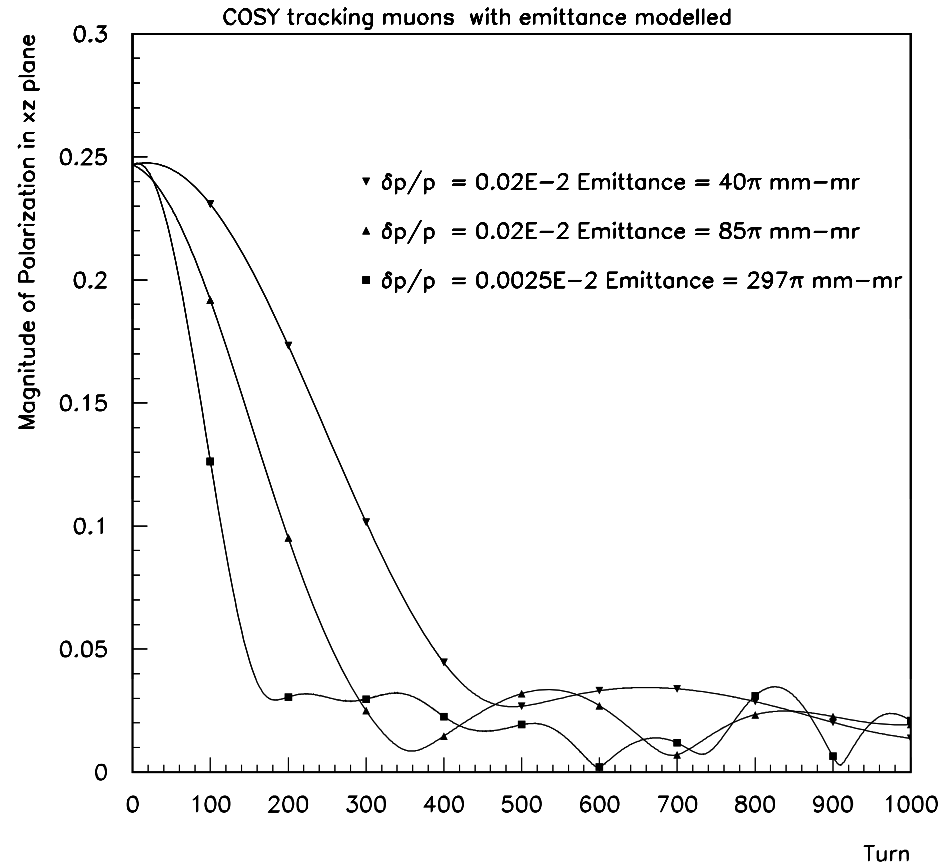
Polarization vs turn for various $\delta p/p$

23/11/97 19.40

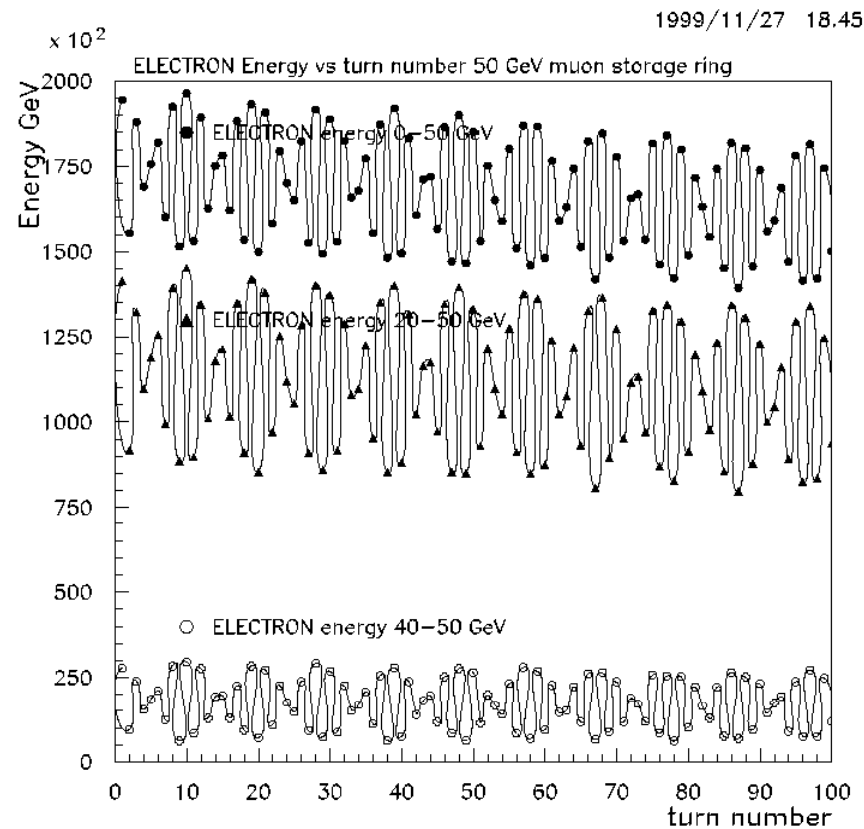


Polarization of 1000 muons vs turn number in COSY

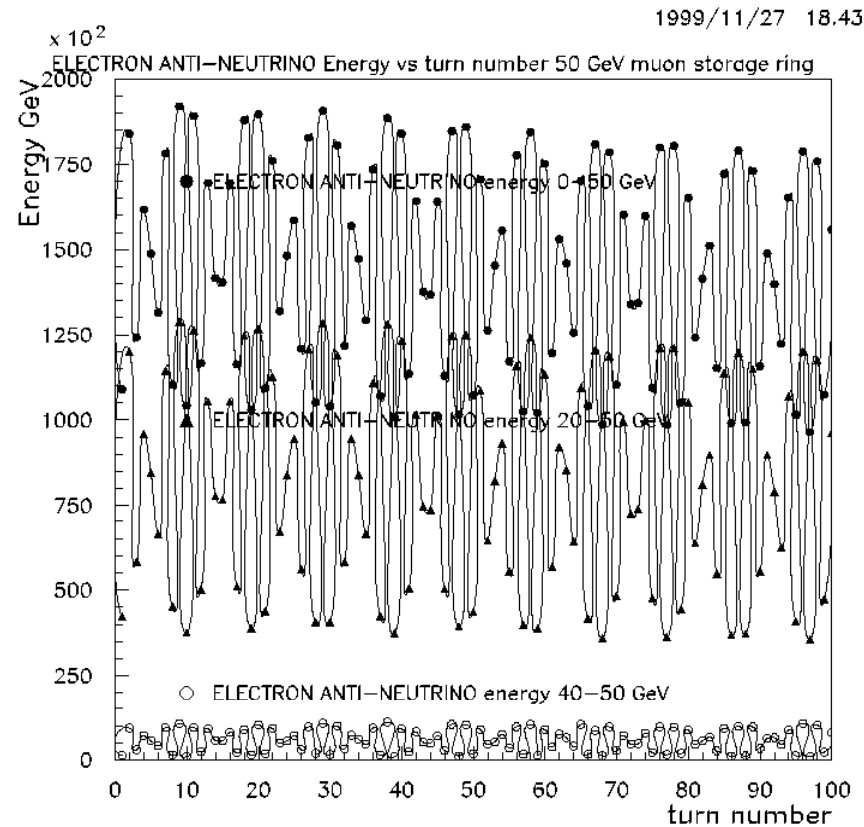
22/11/97 18.43



Energy distribution of electrons



Energy distribution of electron anti-neutrinos



Conclusions

- Small amounts of polarization are valuable.(~10%)
- Muon Collider detectors can be made to work
- The biggest challenge to my mind is the targetry, collection and phase rotation scheme. We should consider making a proposal to FNAL to build such a device for the period when the Tevatron shuts down that is ready to take beam either from the present booster or from Project X when it turns on. The opportunities are ripe for the picking.
- This effort must be started soon and can go concurrently with the cooling demonstrations.
-