

QCD Measurements with the CMS Detector

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◆ **Soft QCD**

- charged particle spectra and pseudorapidity distributions
- charged particle multiplicities
- strange particle production
- particle correlations
- underlying event

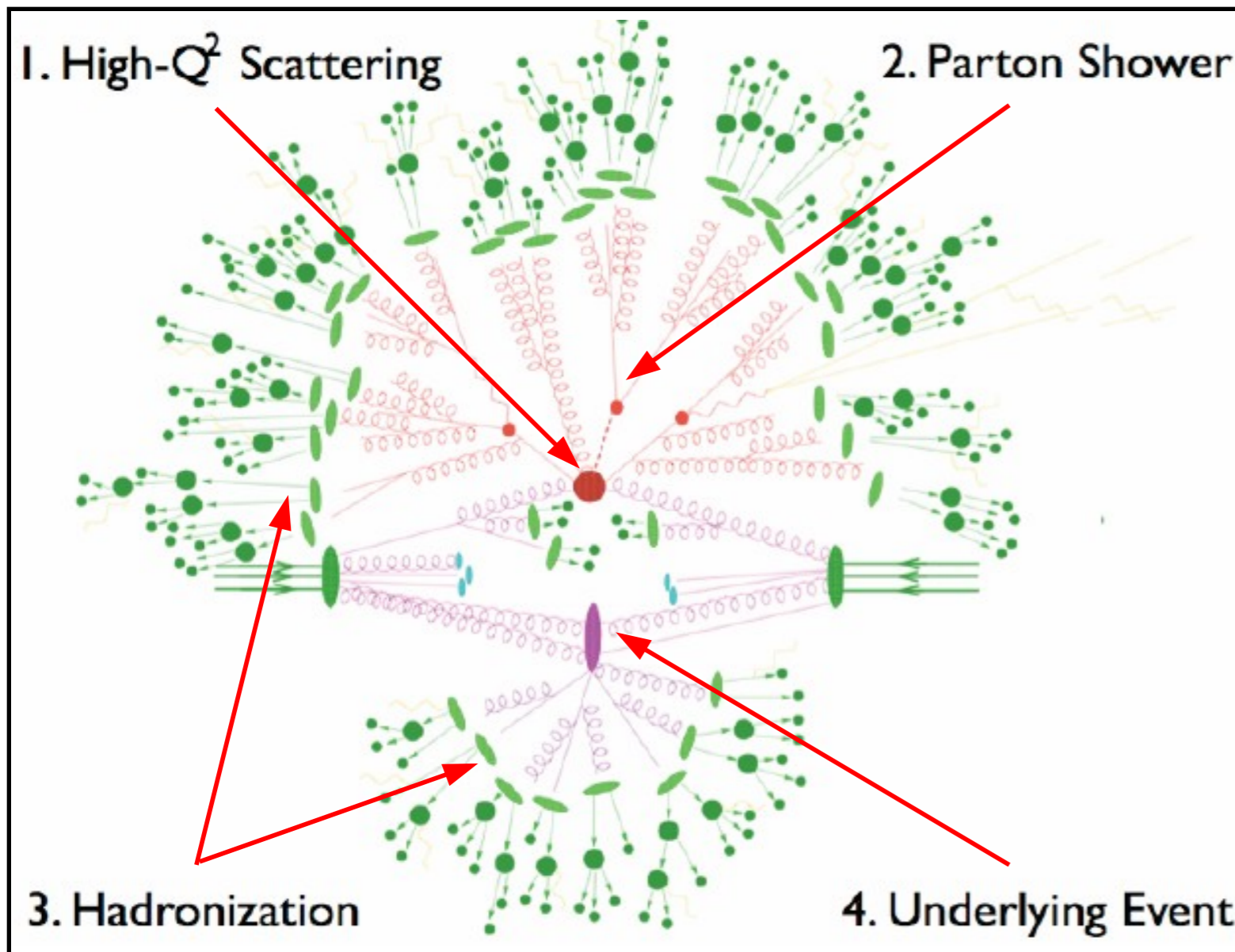
◆ **Jet measurements**

- inclusive jet & dijet production
- dijet angular distributions & azimuthal decorrelations
- hadronic event shapes
- $3j/2j$ ratio

◆ **Photon measurements**

- inclusive photon production
- di-photon production

Proton-Proton Collisions & QCD



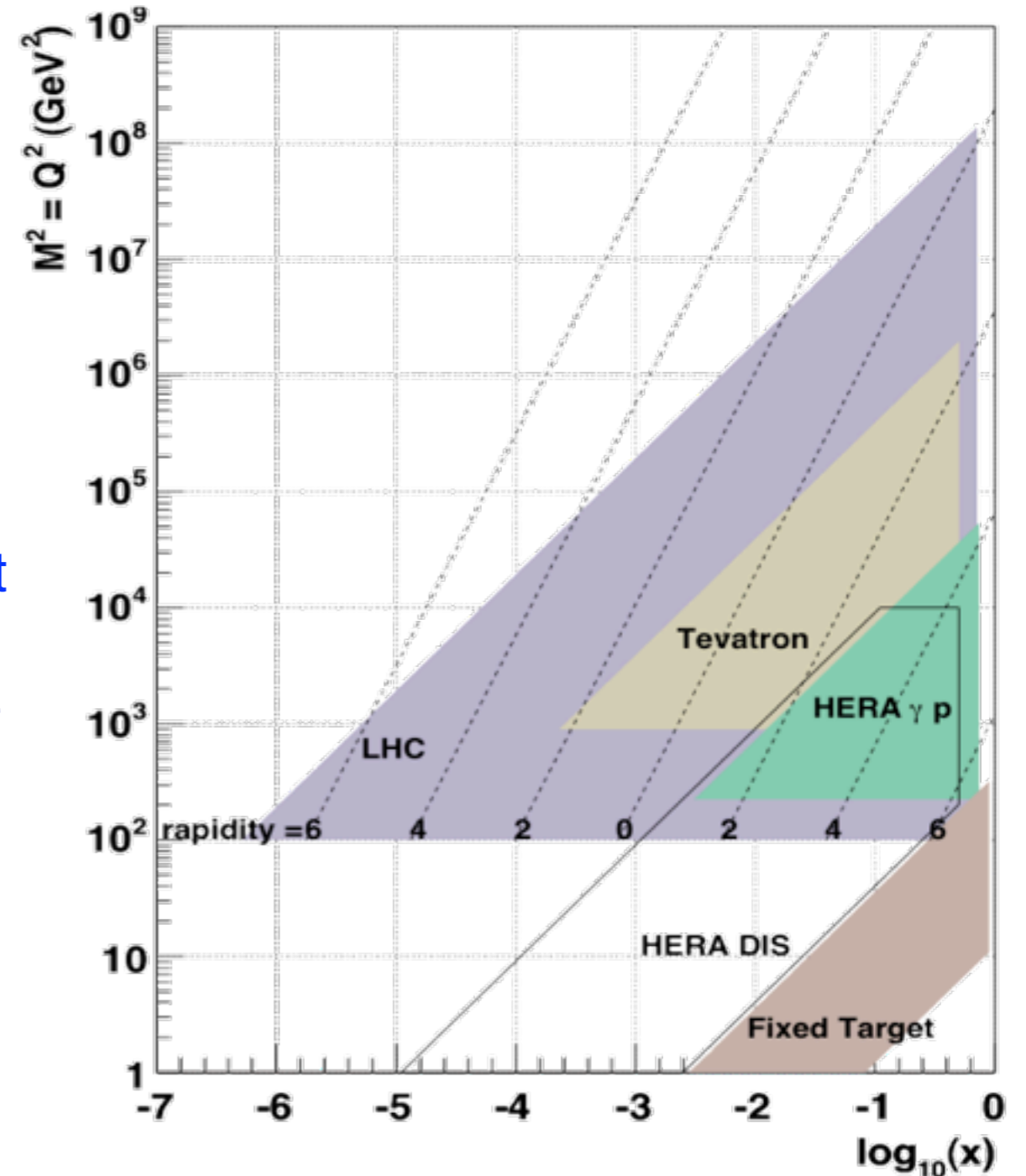
- ◆ pp collisions reveal multiple aspects of QCD:
 - perturbative behavior at the hard scattering scale
 - parton showers
 - multiple parton interactions
 - hadronization
 - structure of the proton
- ◆ QCD is a remarkable theory which deserves to be explored in detail
- ◆ even more important: before we can claim ANY signal of New Physics, we must understand this immensely complicated environment

❖ Unique opportunity to explore a large phase space:

- higher LHC collision energy
- capabilities of the detectors

❖ Specific areas of interest:

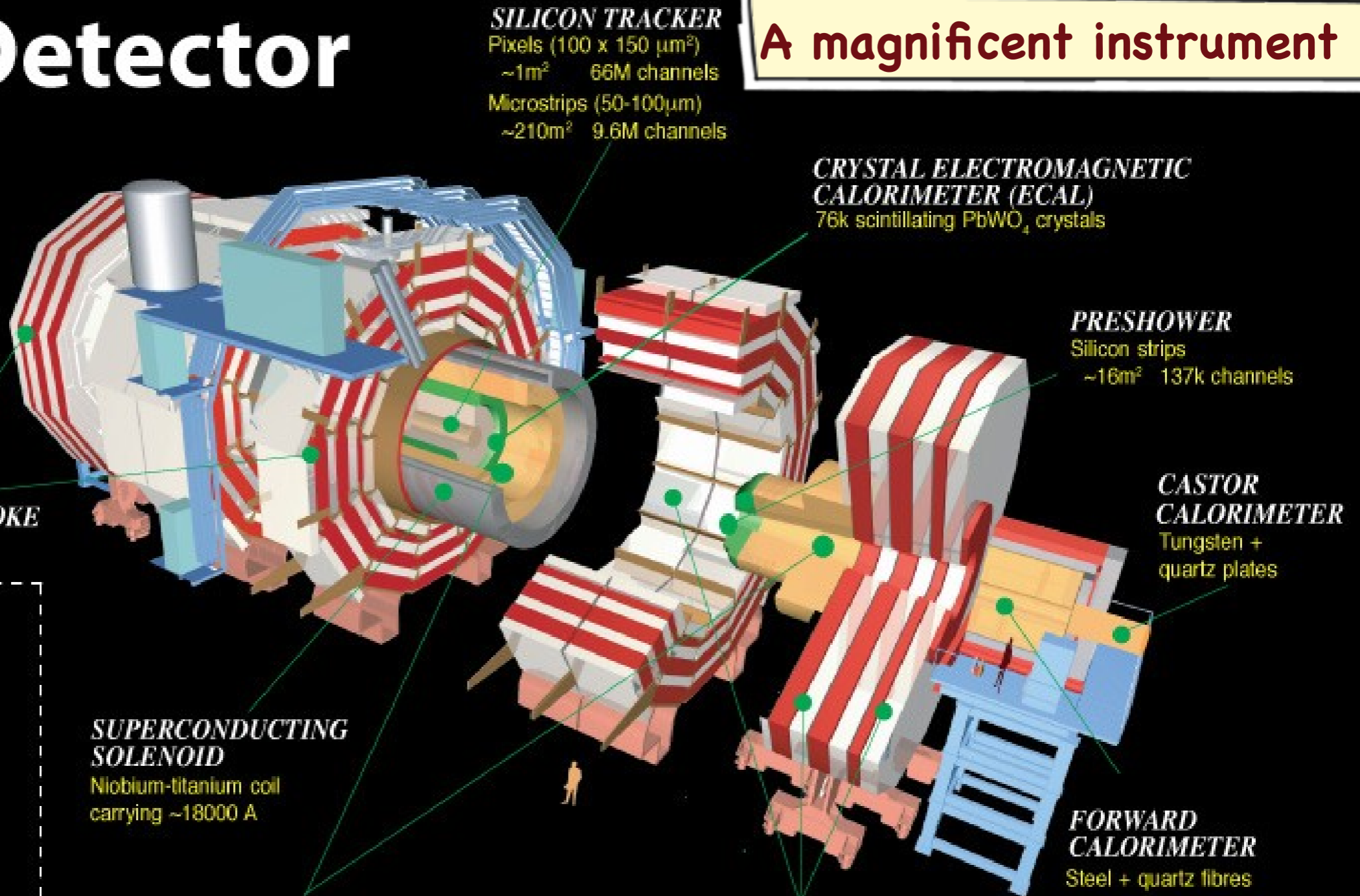
- understand the soft particle production
- understand the underlying event activity. Is it universal in the various processes?
- do the perturbative calculations describe the data accurately enough?
- differentiate between the various PDF sets
- reduce the uncertainty of the gluon PDF
- understand the multijet production
- improve the Monte-Carlo generators



CMS Detector

A magnificent instrument !!!

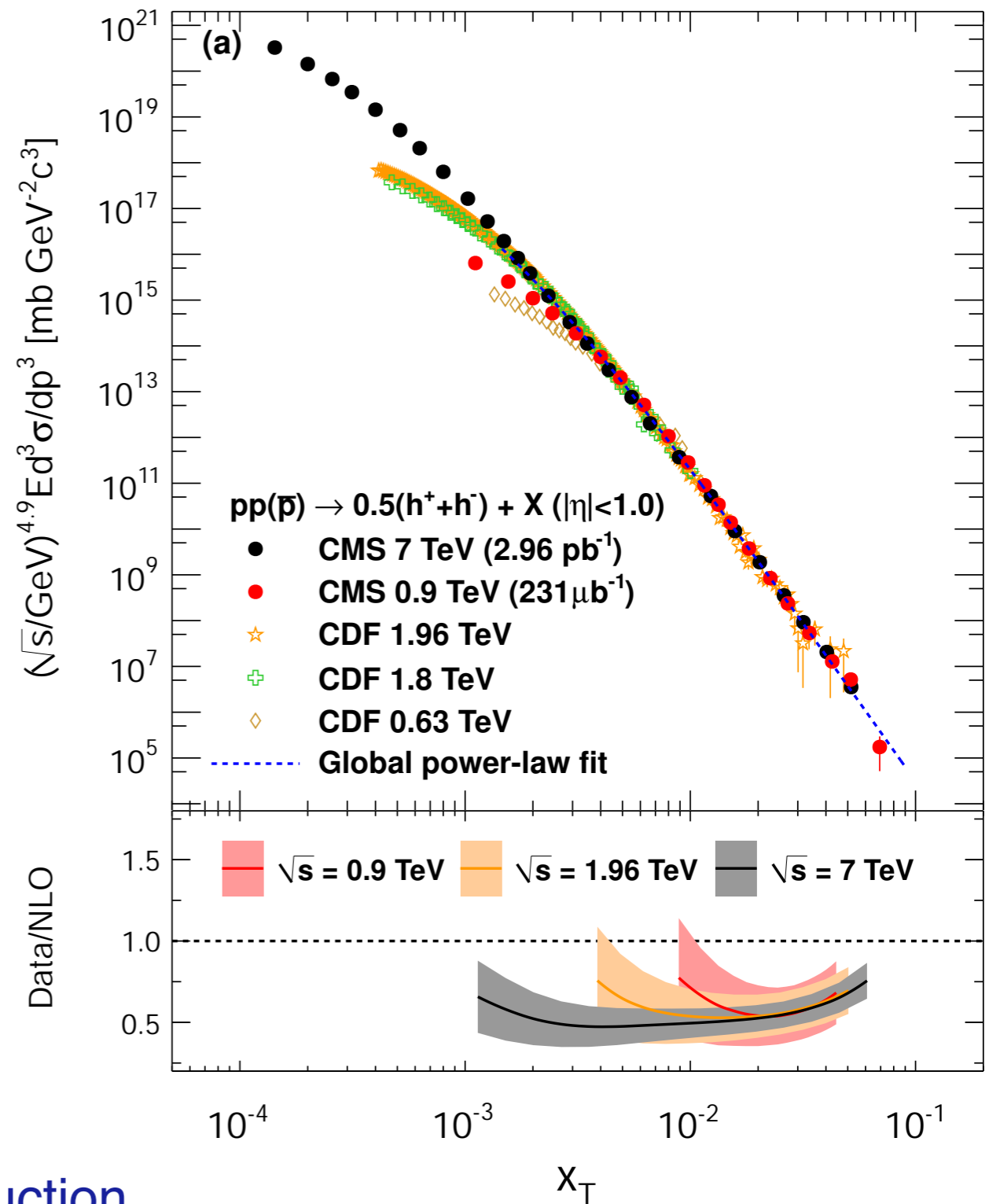
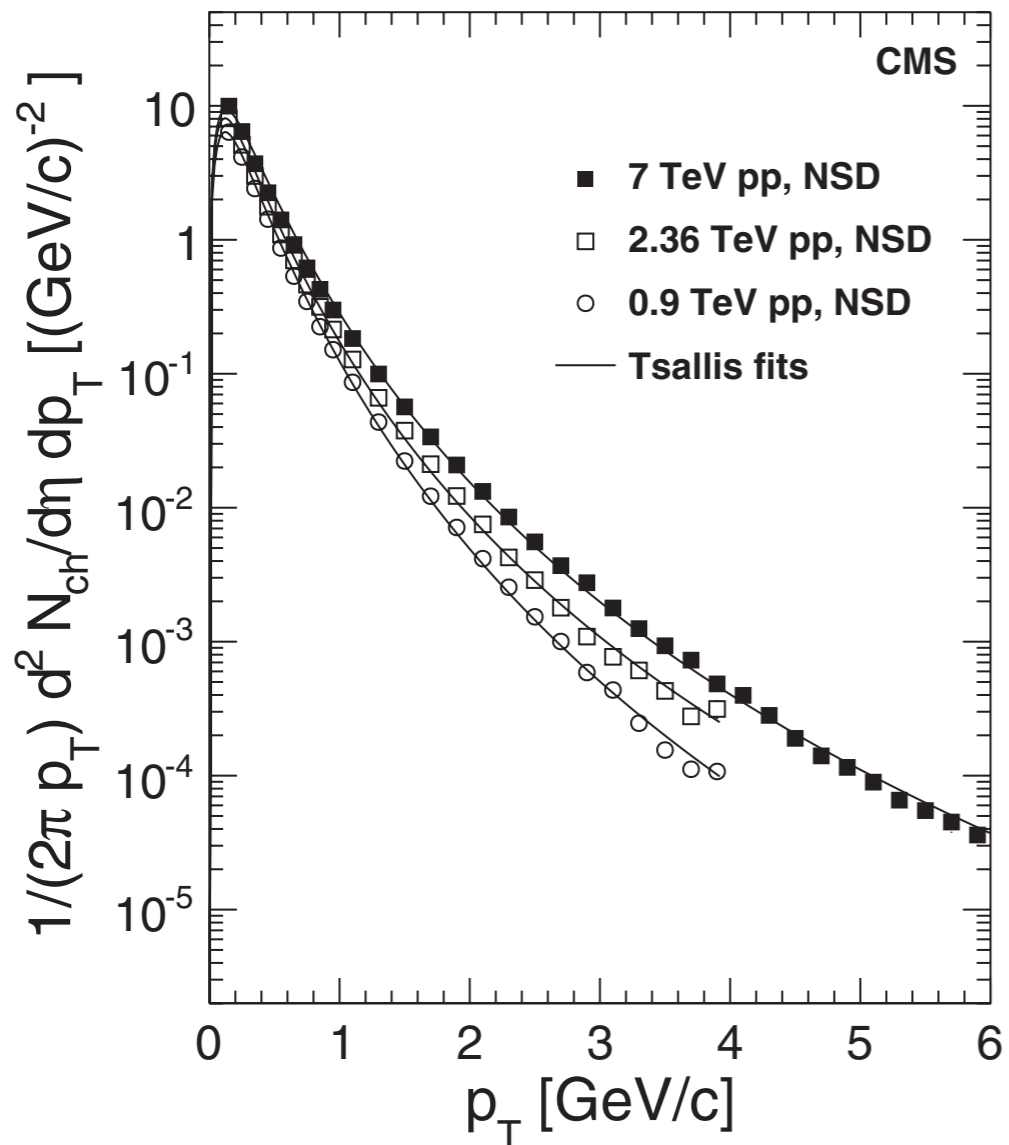
Pixels
 Tracker
 ECAL
 HCAL
 Solenoid
 Steel Yoke
 Muons



Total weight : 14000 tonnes
 Overall diameter : 15.0 m
 Overall length : 28.7 m
 Magnetic field : 3.8 T

Soft QCD Measurements

Charged Hadron Spectra

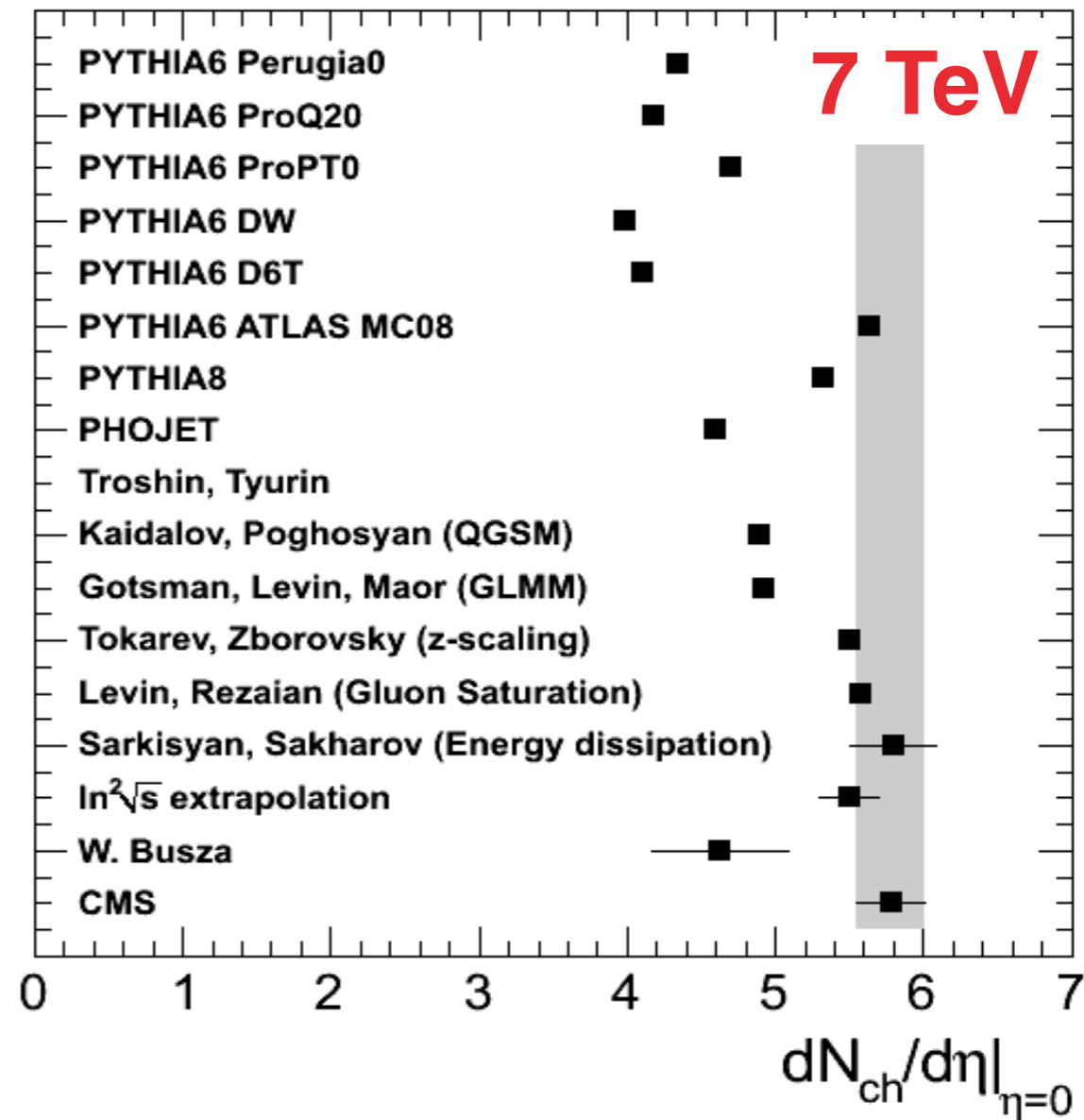
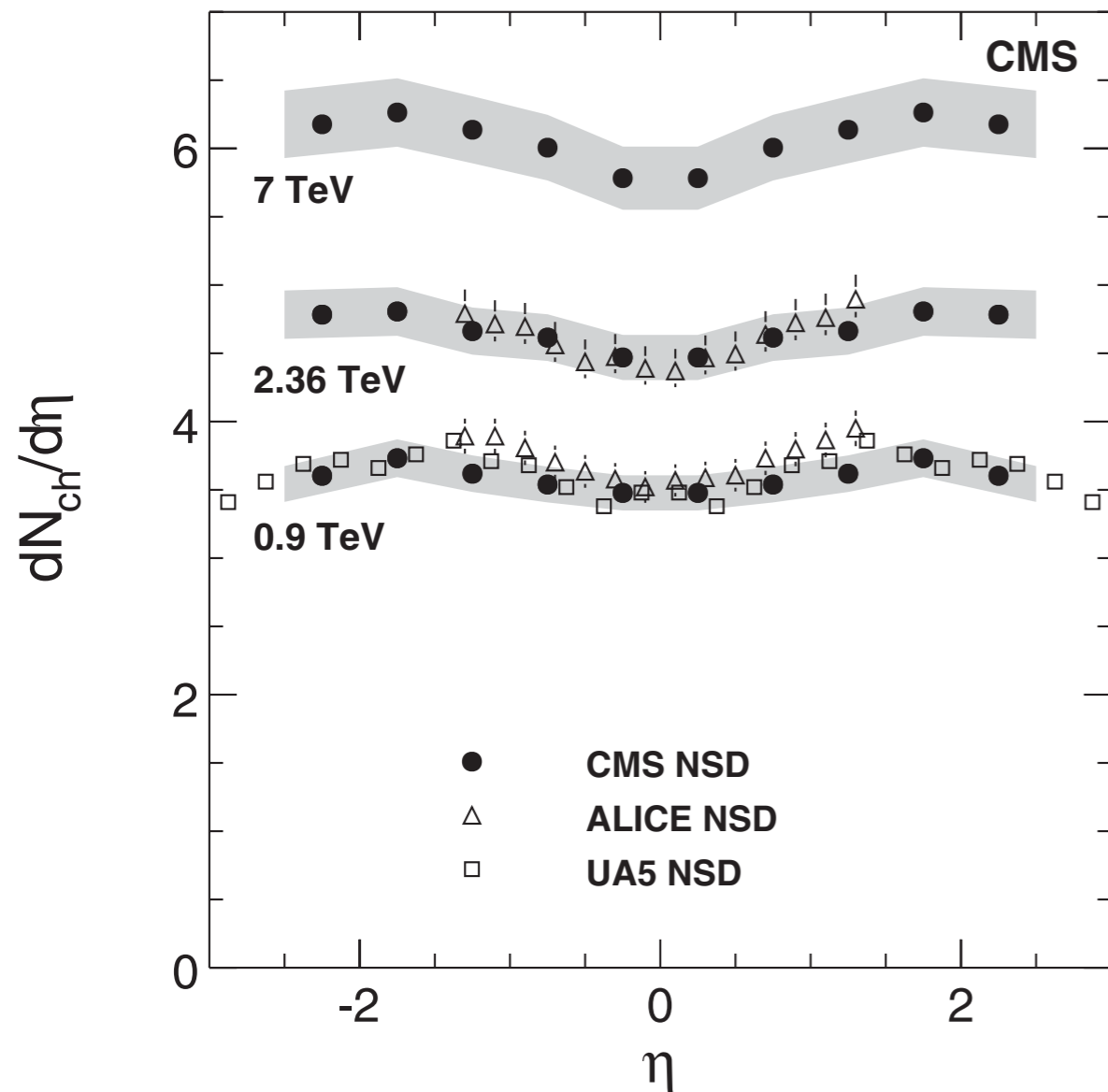


- ◆ p_T spectra described well by Tsallis fits
- ◆ scaling behavior with \sqrt{s} at high x_T
- ◆ NLO predictions overestimate particle production

PRL 105 (2010) 022002
JHEP 08 (2011) 086

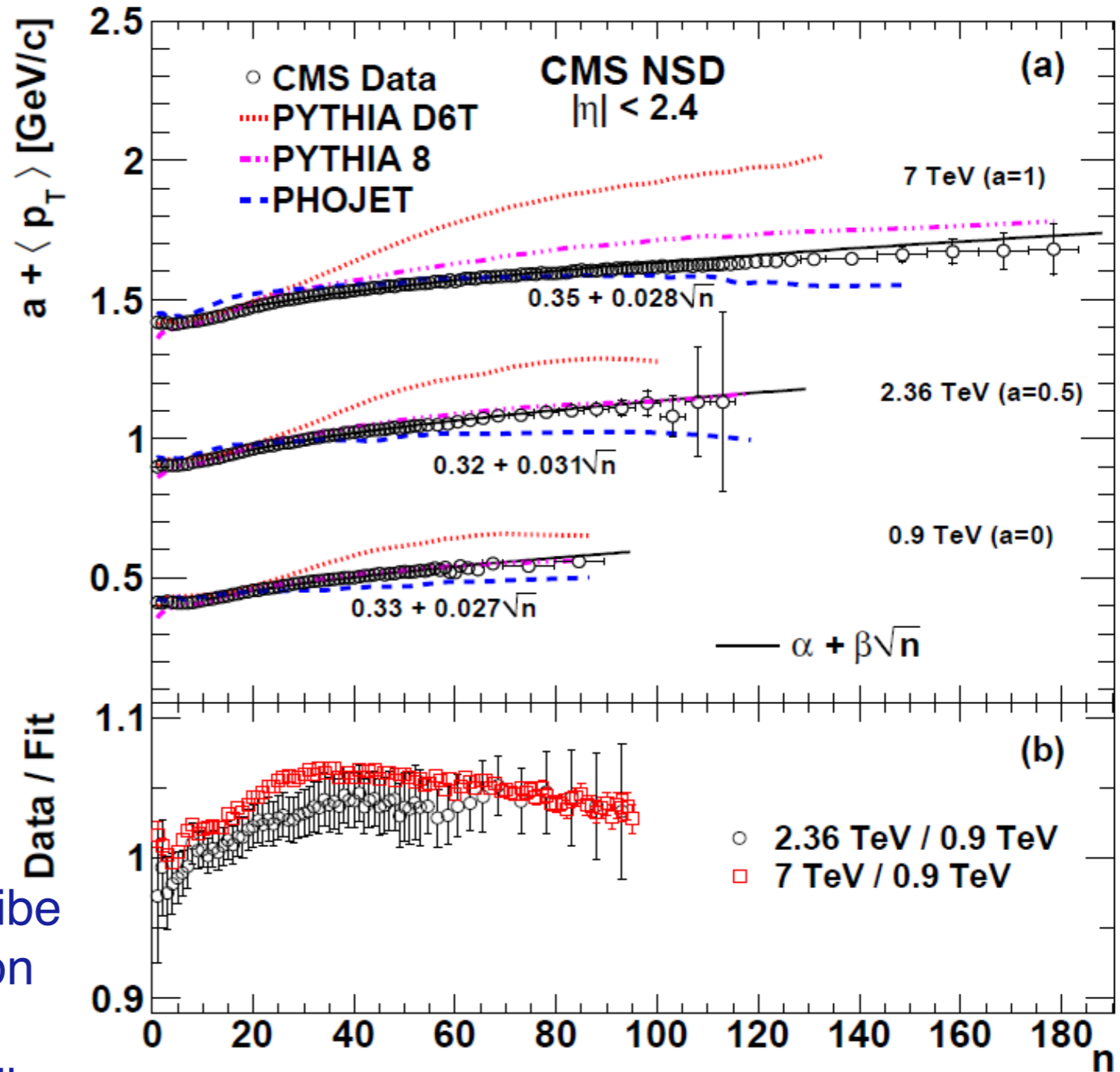
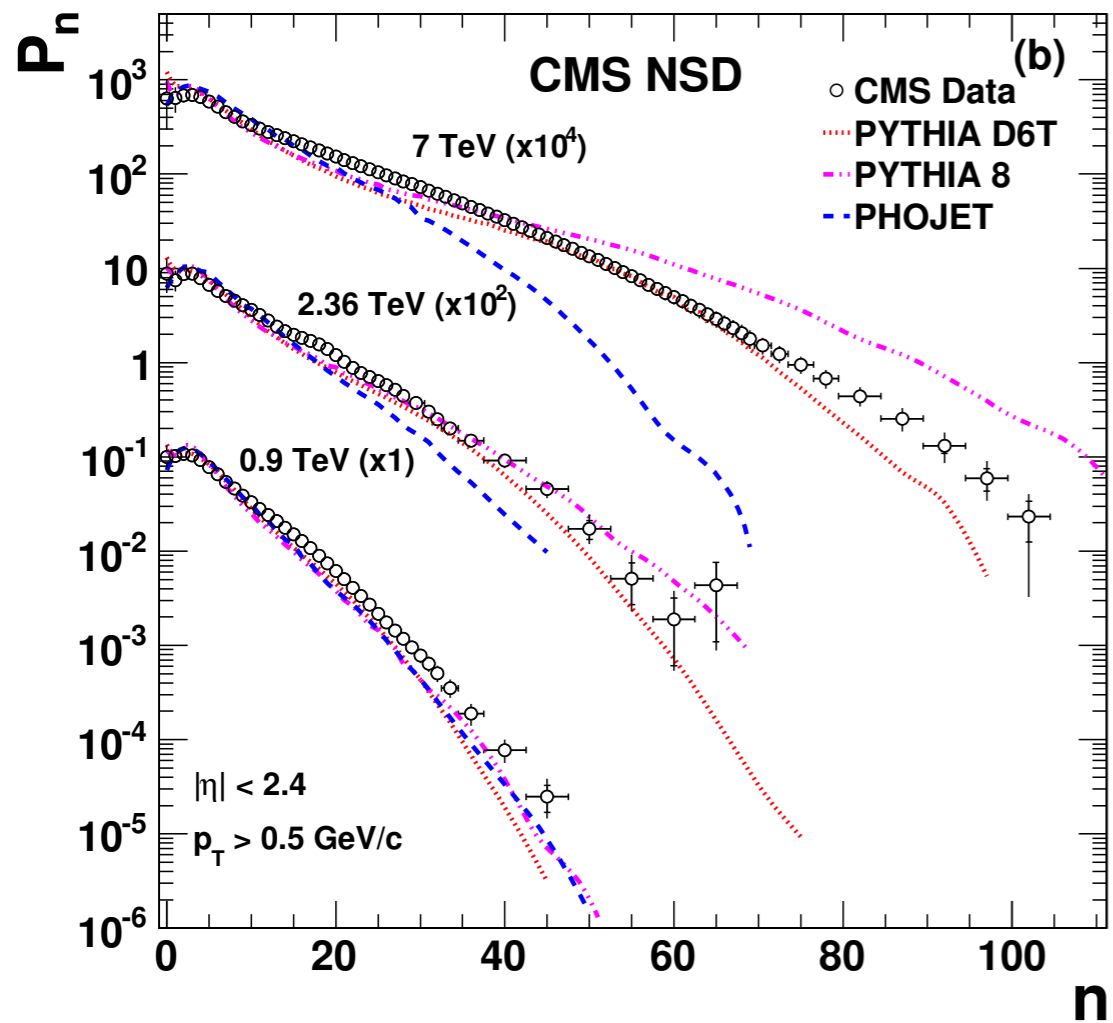


Charged Hadron Pseudorapidity Distributions



- ◆ CMS measurements in agreement with other experiments
- ◆ pre-LHC Monte-Carlo tunes predict lower particle densities
 - ATLAS tune in agreement
- ◆ some analytic models are in reasonable agreement

Charged Hadron Multiplicity

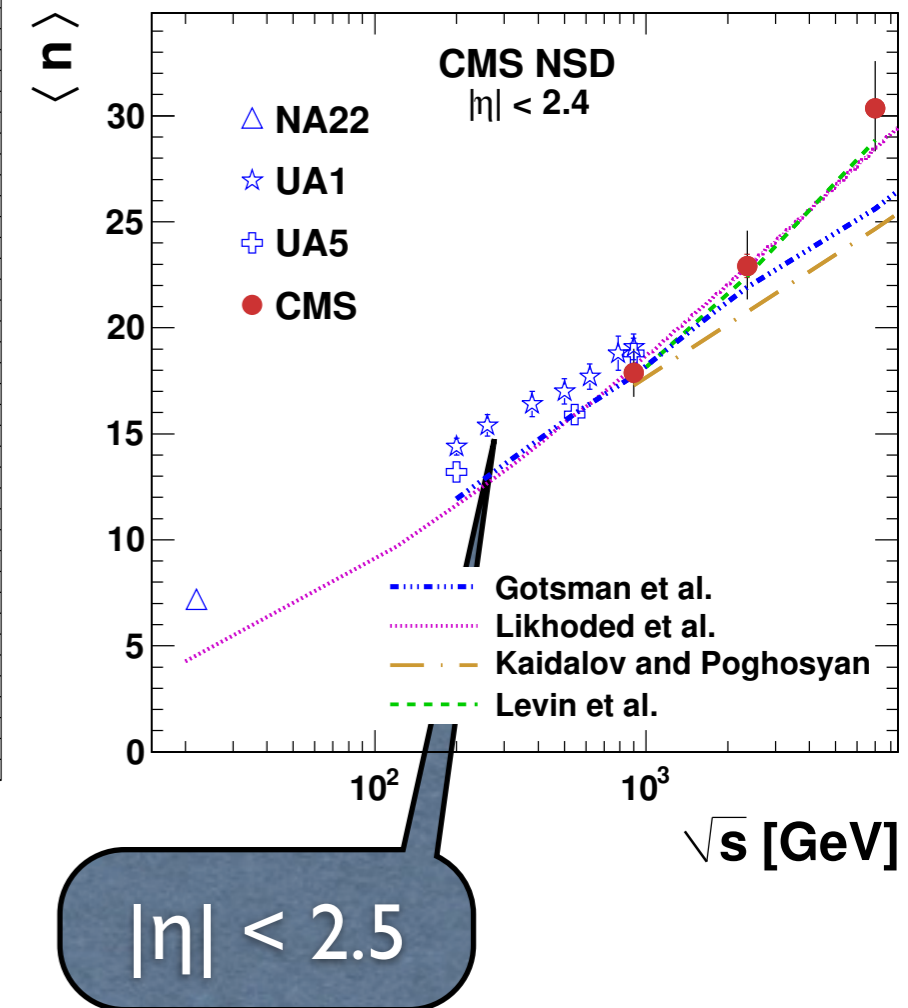
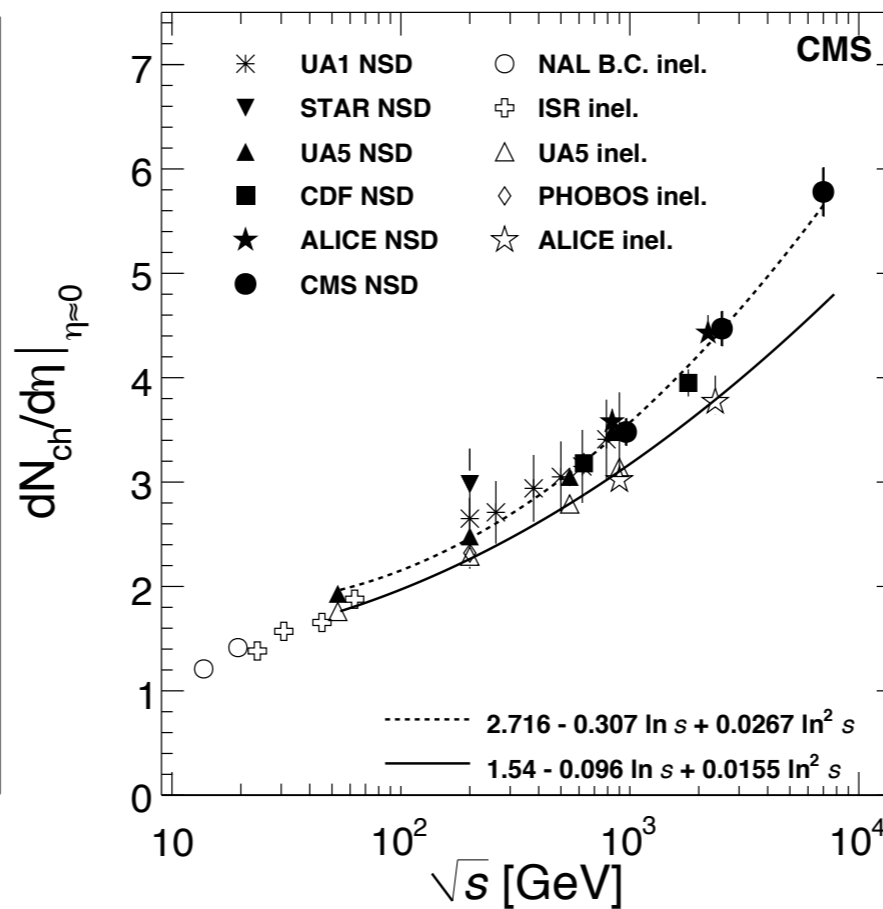
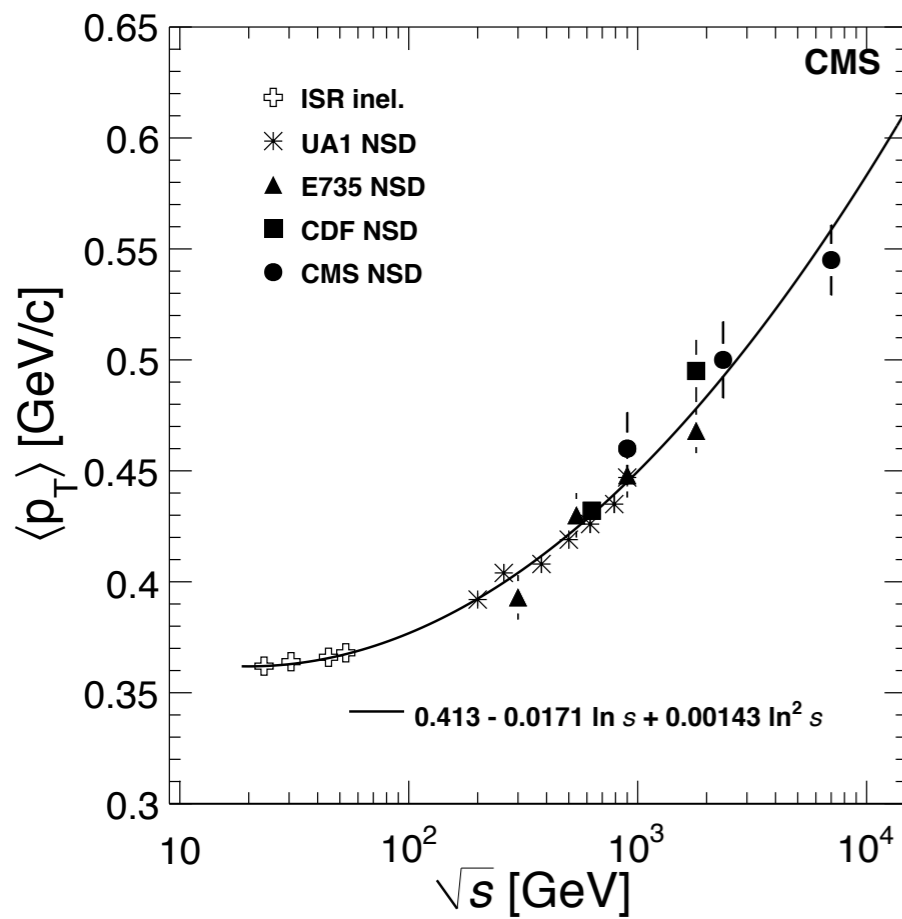


Data / Fit

- ◆ no Monte-Carlo generator can describe the multiplicity distributions at all collision energies
- ◆ no Monte-Carlo generator can describe simultaneously the multiplicity and the average p_T

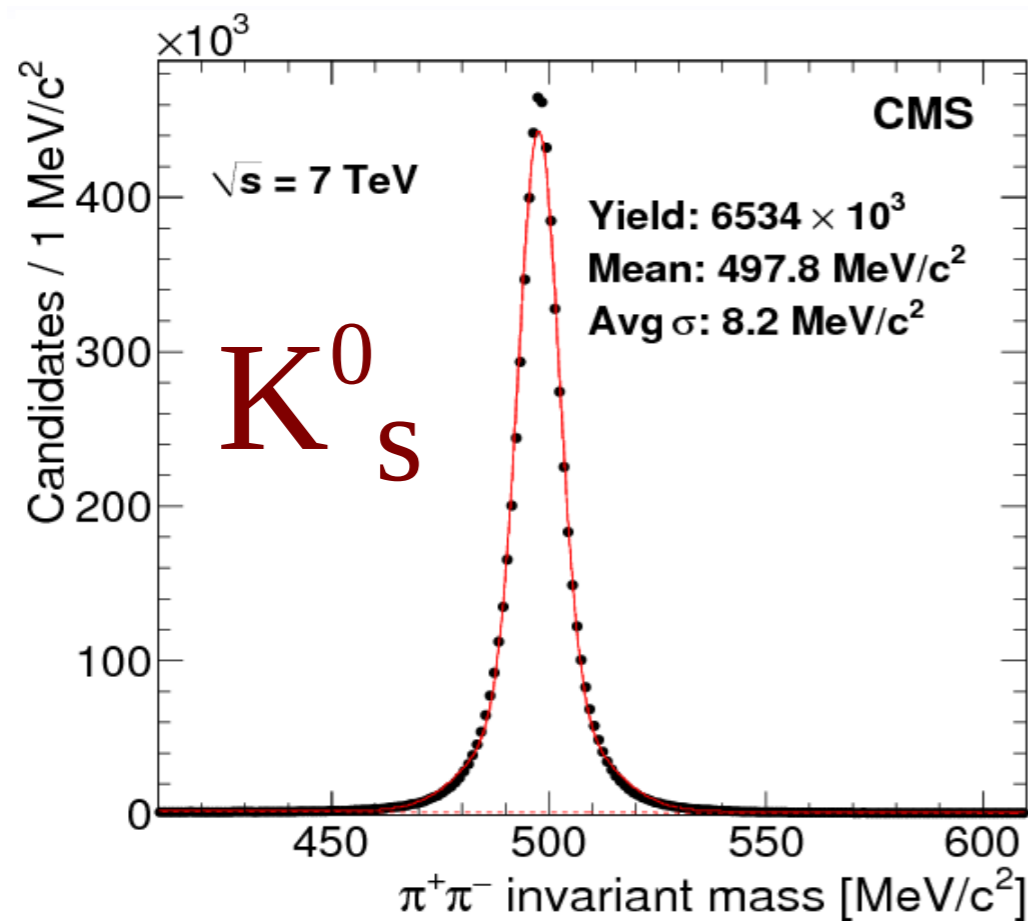
JHEP 01 (2011) 079

Collision-Energy Dependence

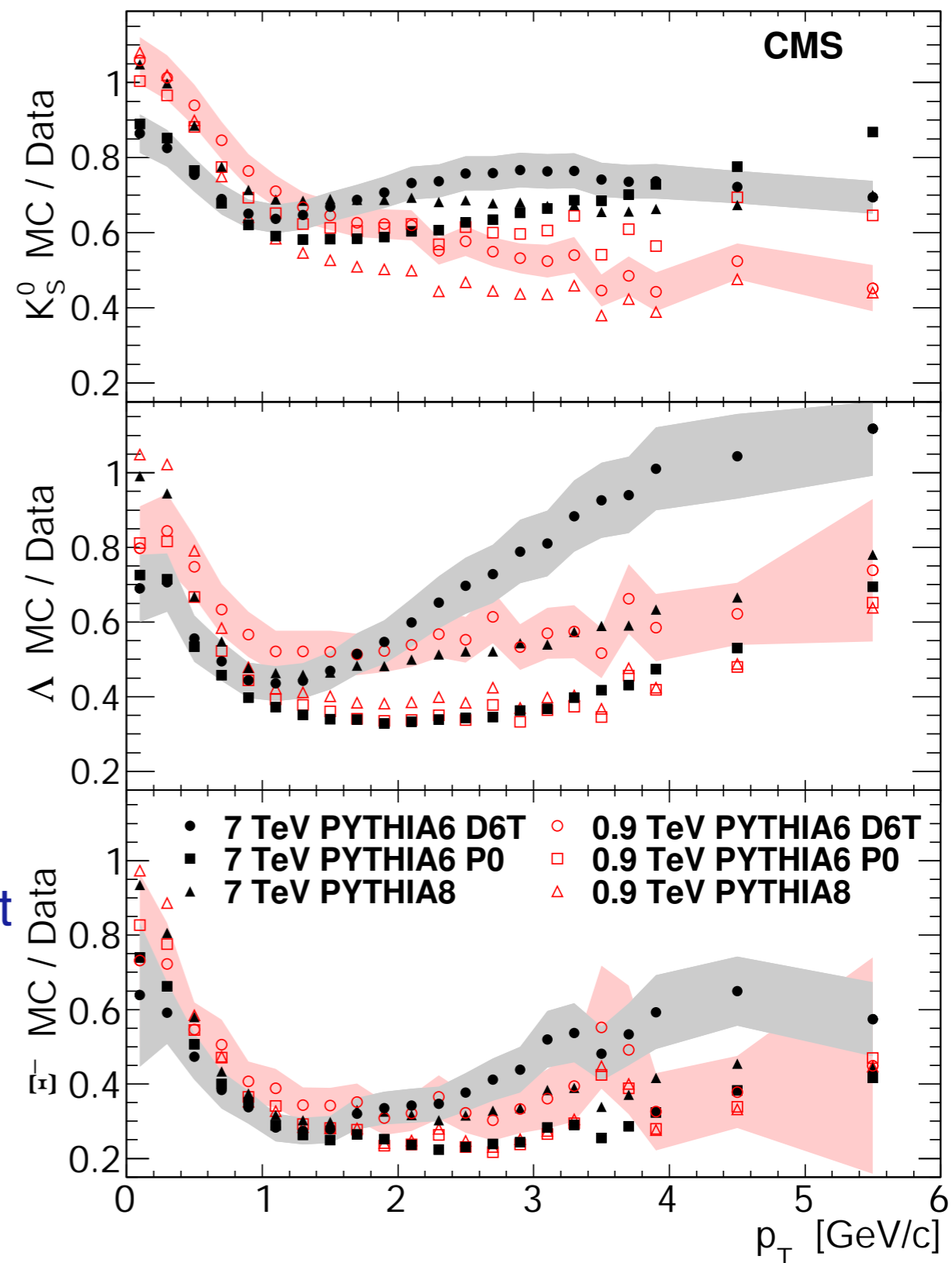


- ◆ CMS measurements in three collision energies: 0.9, 2.36, 7 TeV
- ◆ in agreement with other experiments
- ◆ sharp increase of particle production towards $\sqrt{s} = 7$ TeV

Strange Particle Production



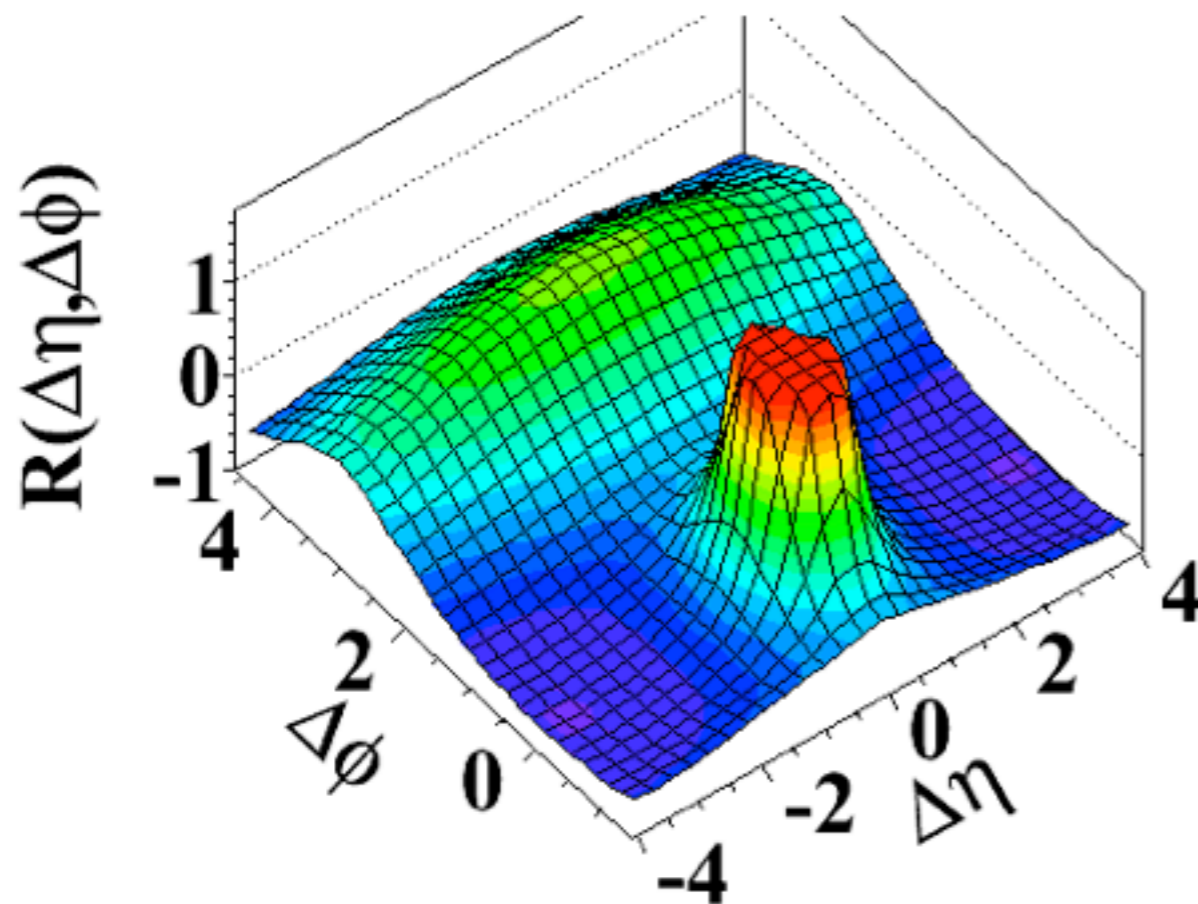
- ◆ strange particle production is a sensitive test of Monte-Carlo tunes
- ◆ significant discrepancies observed between data and pre-LHC tunes of PYTHIA
- ◆ largest deviation for Ξ^- at both collision energies (0.9 & 7 TeV)



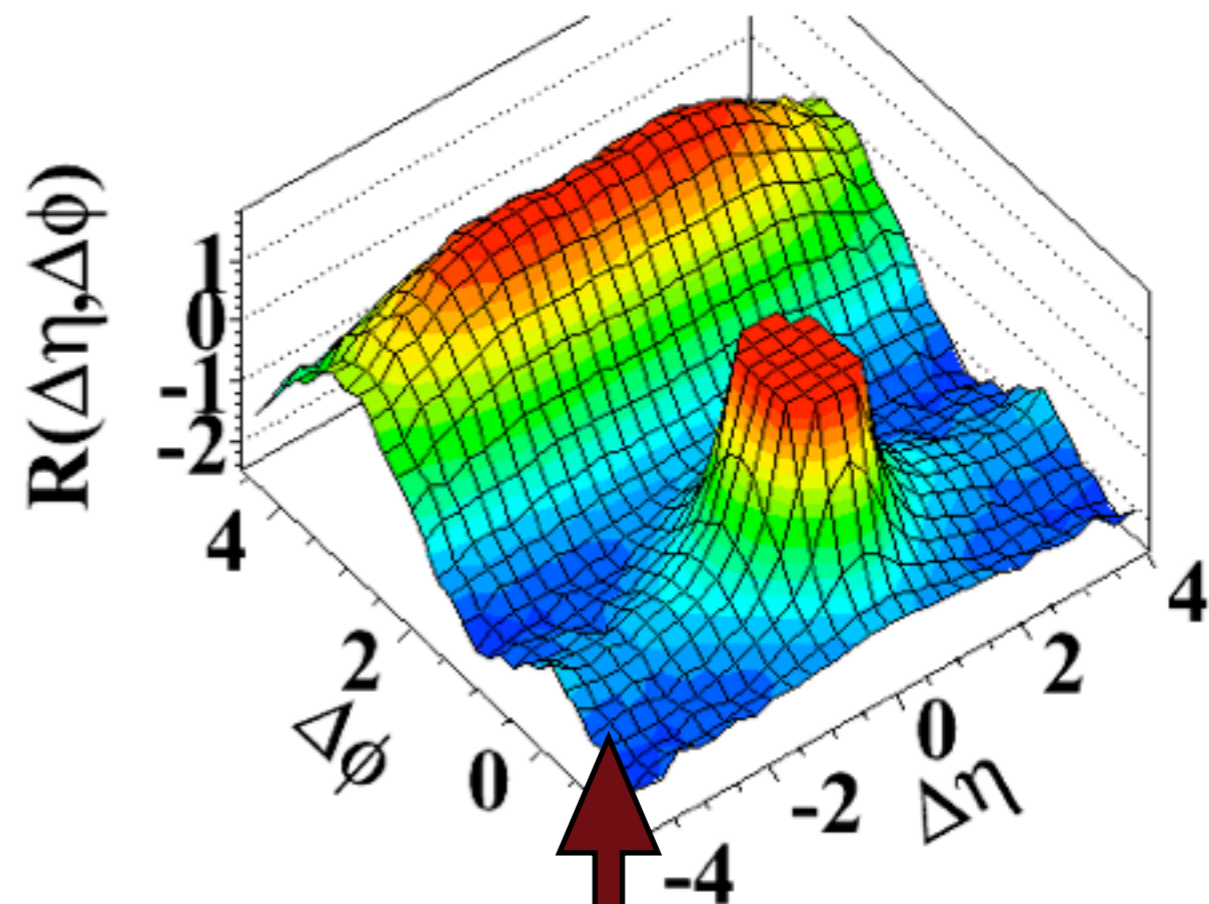
JHEP 05 (2011) 064

Particle Correlations

(b) CMS MinBias, $1.0\text{GeV}/c < p_T < 3.0\text{GeV}/c$



(d) CMS $N \geq 110$, $1.0\text{GeV}/c < p_T < 3.0\text{GeV}/c$

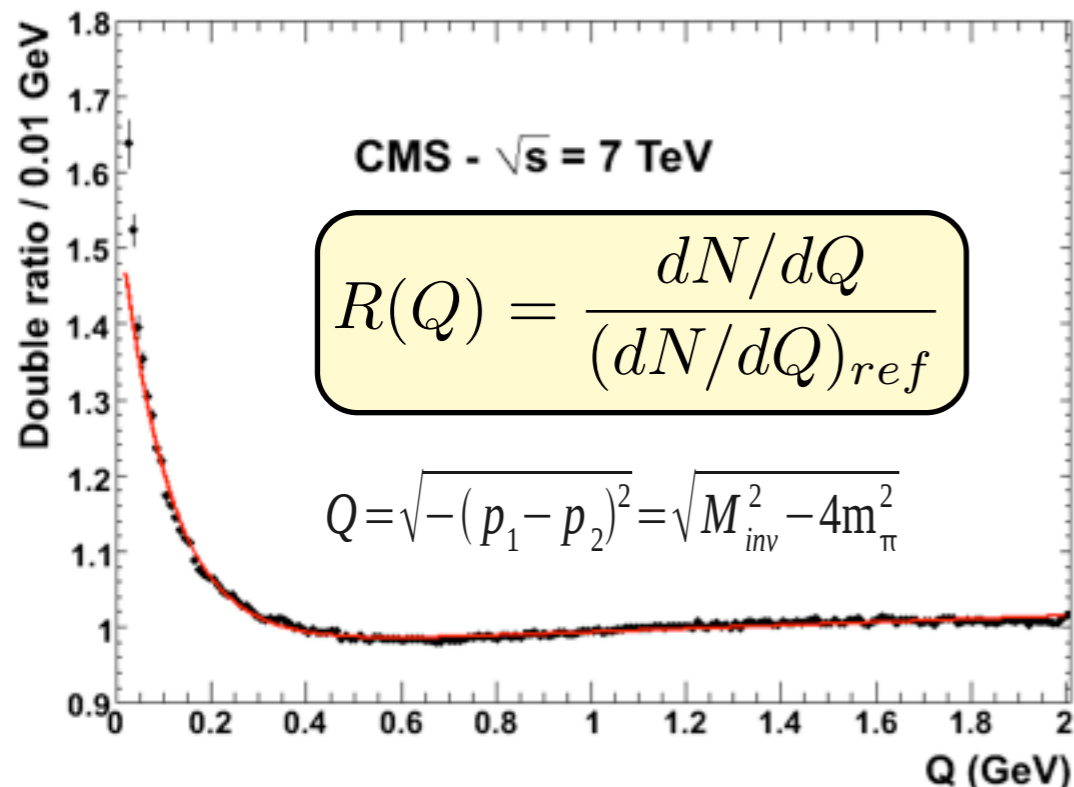
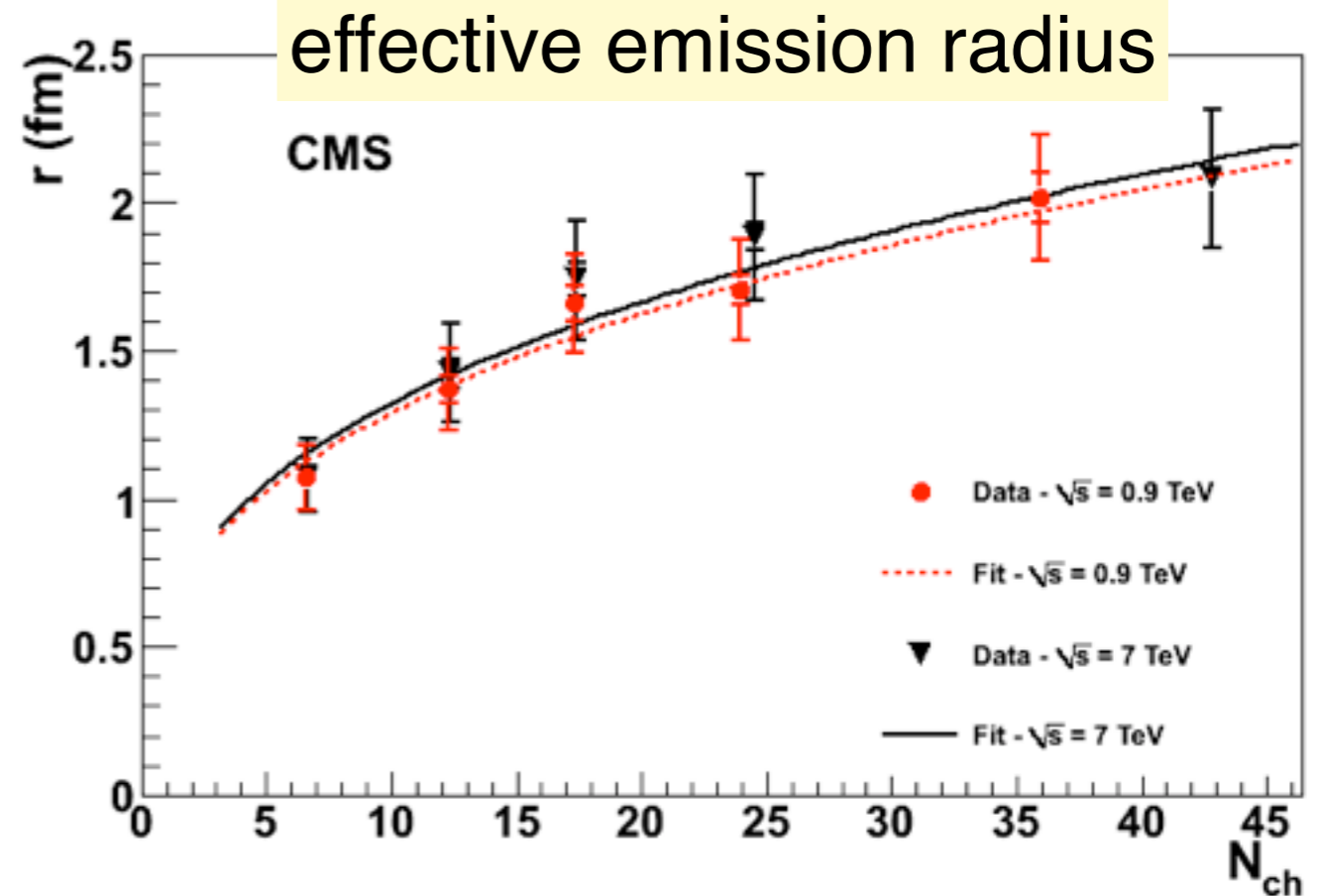
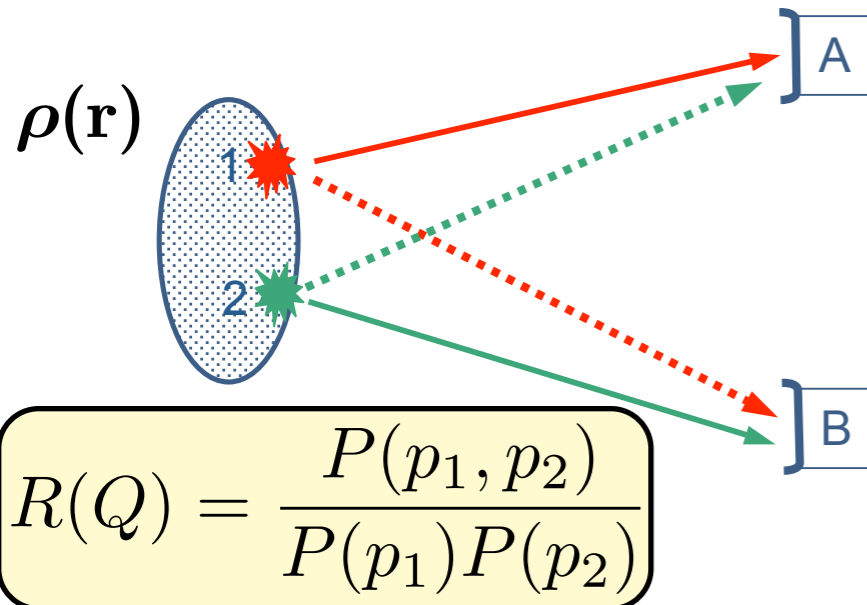


Near-side ($\Delta\phi \sim 0$), long range angular correlations at **high multiplicities** and intermediate p_T

JHEP 09 (2010) 091

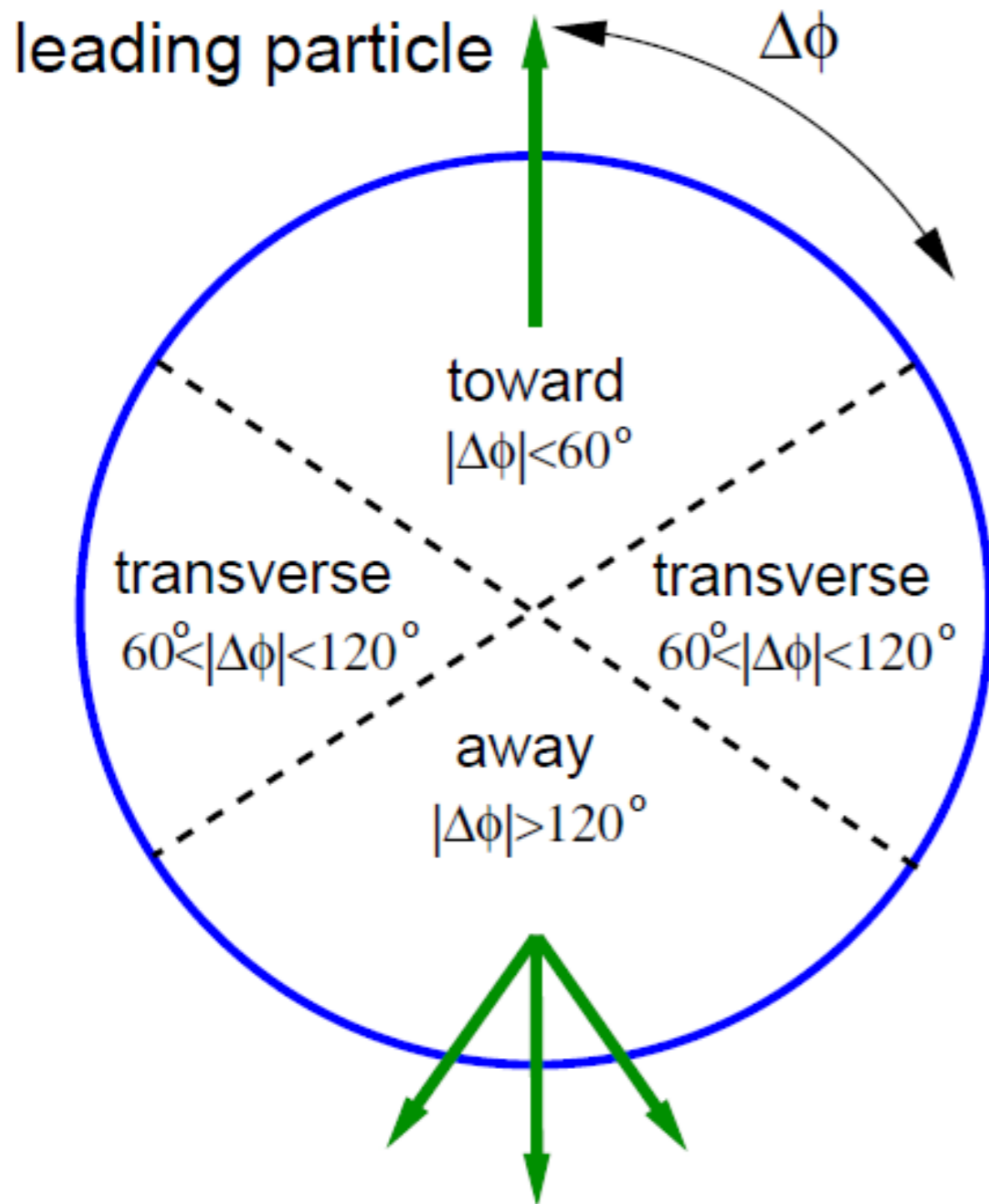
- ◆ two-particle correlations in $\Delta\eta$ and $\Delta\phi$
- ◆ various regions of interest:
 - particles inside a jet ($\Delta\eta, \Delta\phi \sim 0$)
 - particles of “back-to-back” jets ($\Delta\phi \sim \pi$)
- ◆ first observation of near-side, long range correlations at high multiplicities
 - not predicted by MC
 - sign of nuclear medium effects?

Bose-Einstein Correlations



- ◆ correlations between identical bosons with overlapping wave functions
- ◆ production probability enhancement at low Q
- ◆ provides information about the size of the emitting source
- ◆ ratio to reference sample with no correlations

Underlying Event (I)



◆ the “underlying event” consists of everything else except for the hard interaction

- multiple parton interactions
- initial and final state radiation
- beam remnants

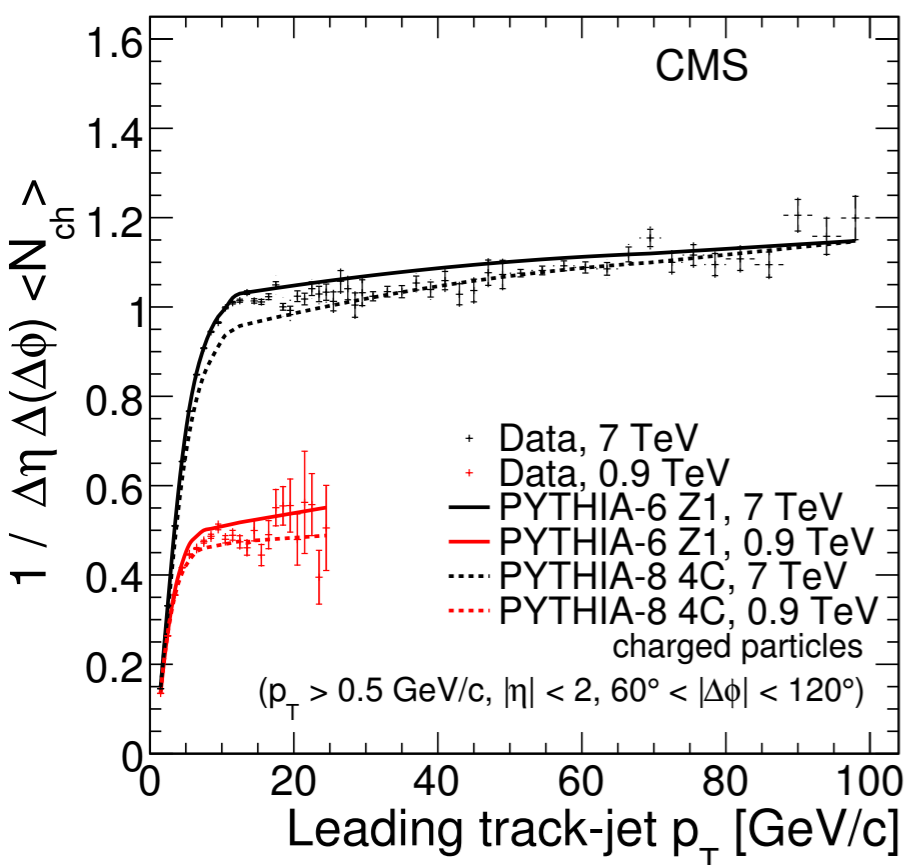
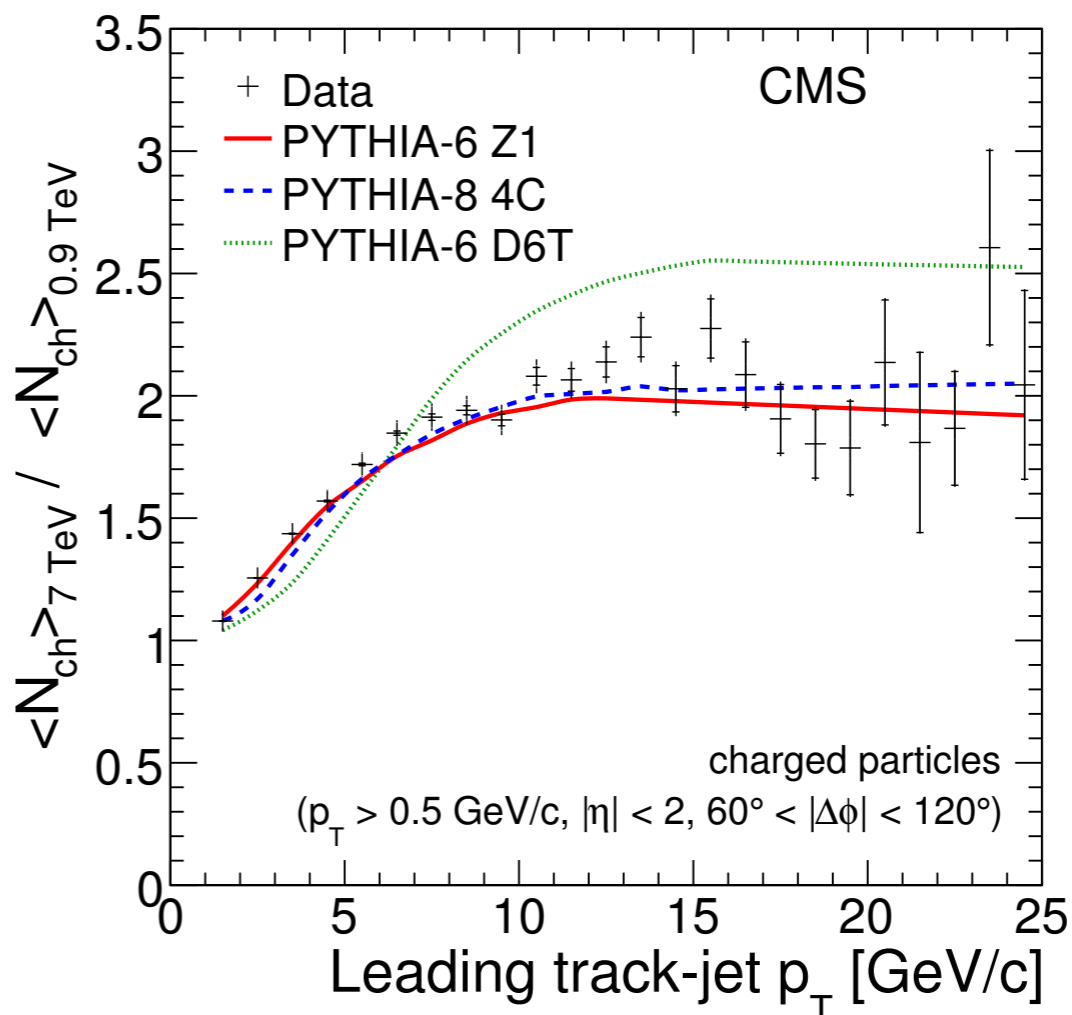
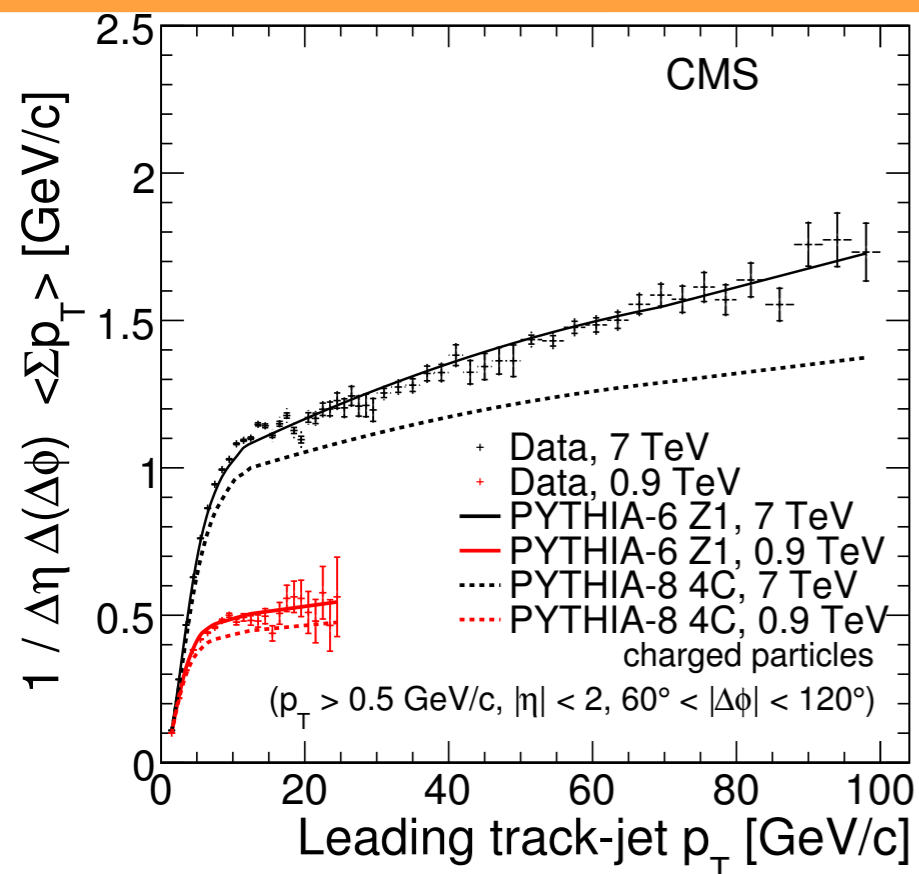
◆ the event is divided in three regions

- **toward** (defined by the leading particle / jet)
- **away**
- **transverse** (sensitive to UE)

◆ two observables quantify the UE activity

- multiplicity density of charged hadrons
- scalar sum p_T density of charged hadrons

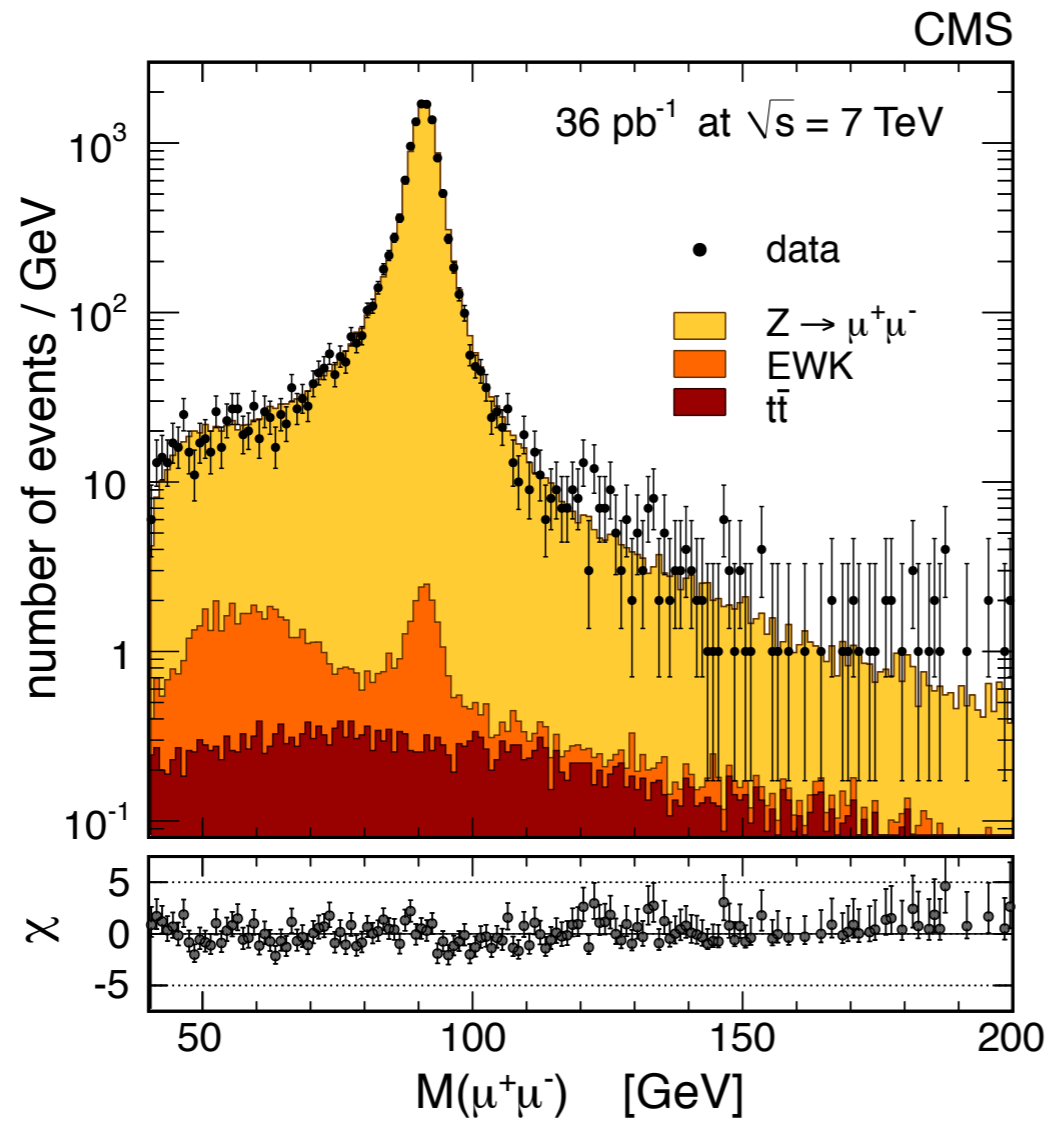
Underlying Event (II)



- ◆ the hard scale of the event is defined by the hardest track-jet
- ◆ the UE activity shows a sharp increase up to $p_T \sim 10$ GeV, followed by a plateau (saturation region)
- ◆ the UE activity increases by a factor ~ 2 from 0.9 to 7 TeV
- ◆ pre-LHC tunes do not describe the UE, but newer tunes do

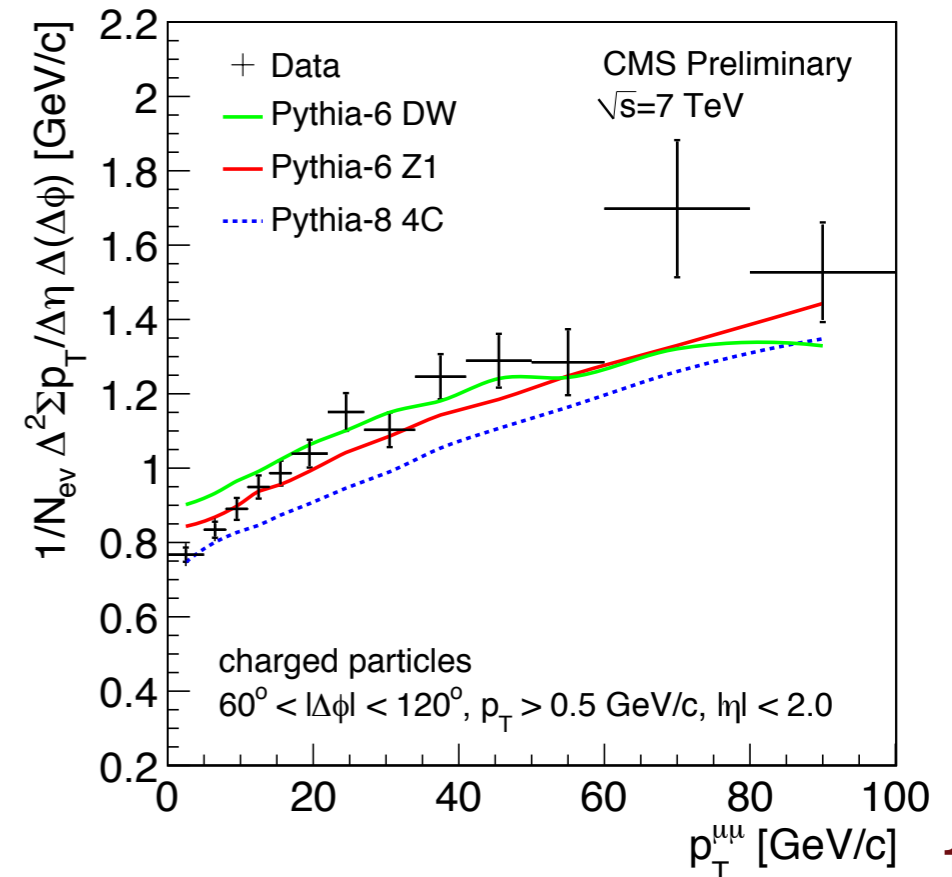
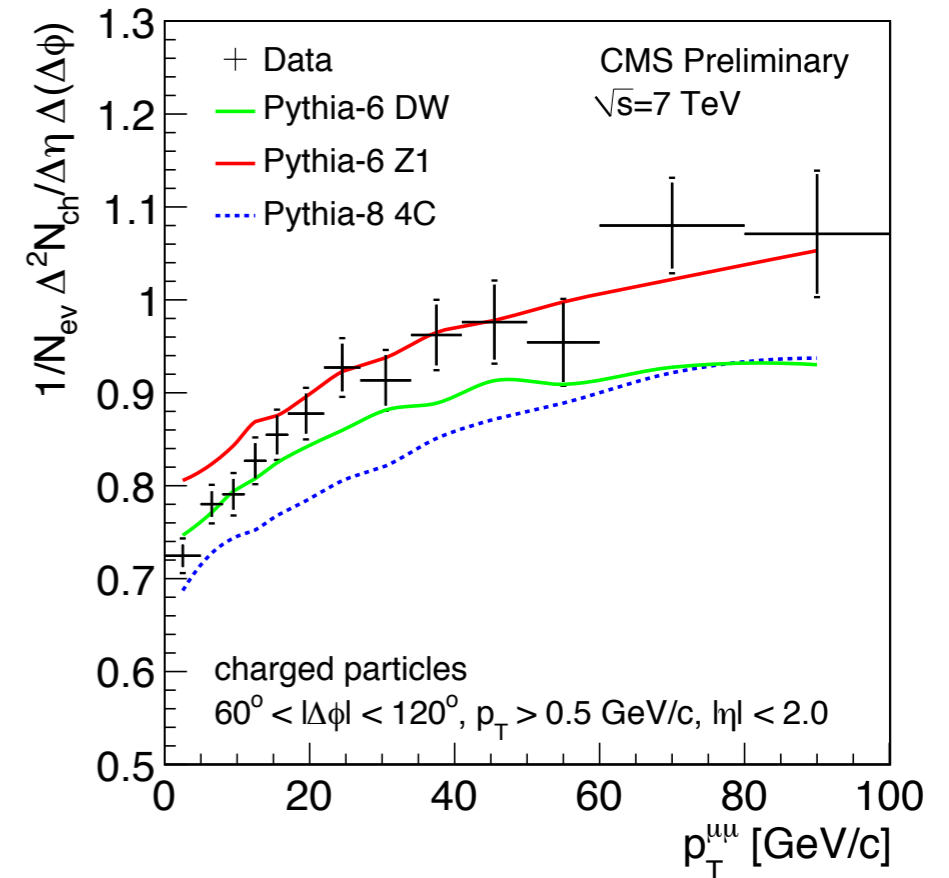
JHEP 09 (2011) 109

Underlying Event in DY Events



- ◆ UE activity in Drell-Yan events
- ◆ the hard scale of the events is practically defined by the Z pole
- ◆ explore the saturation region
- ◆ newer tunes of Pythia6 describe the data well

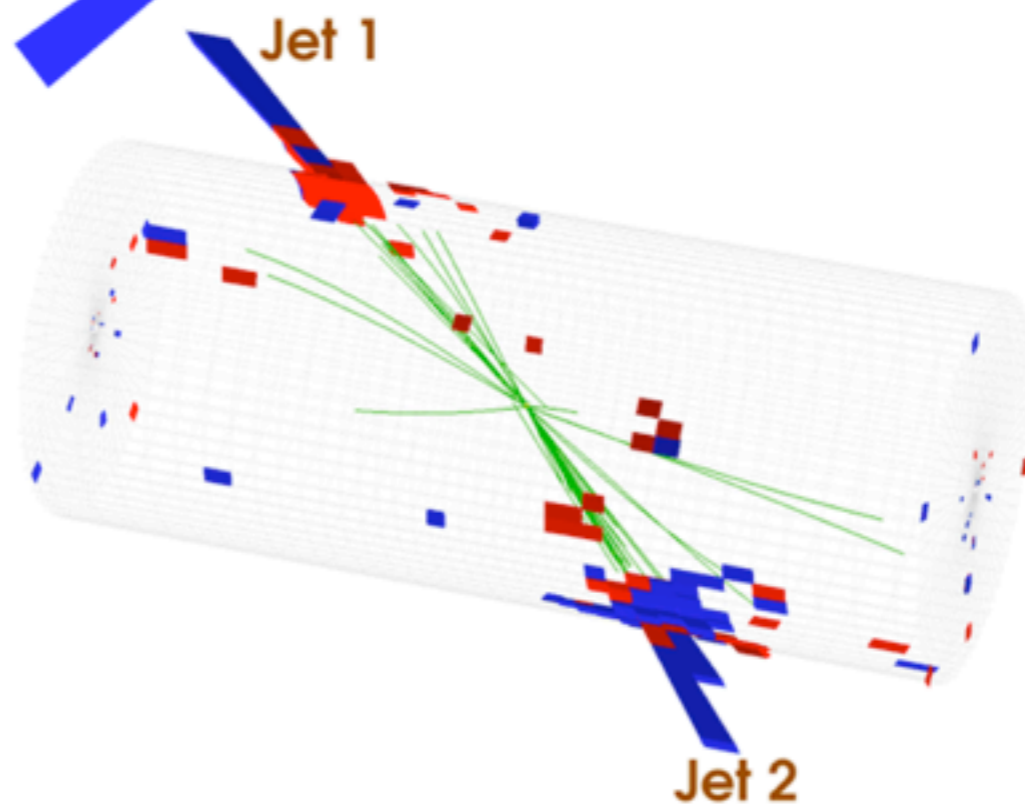
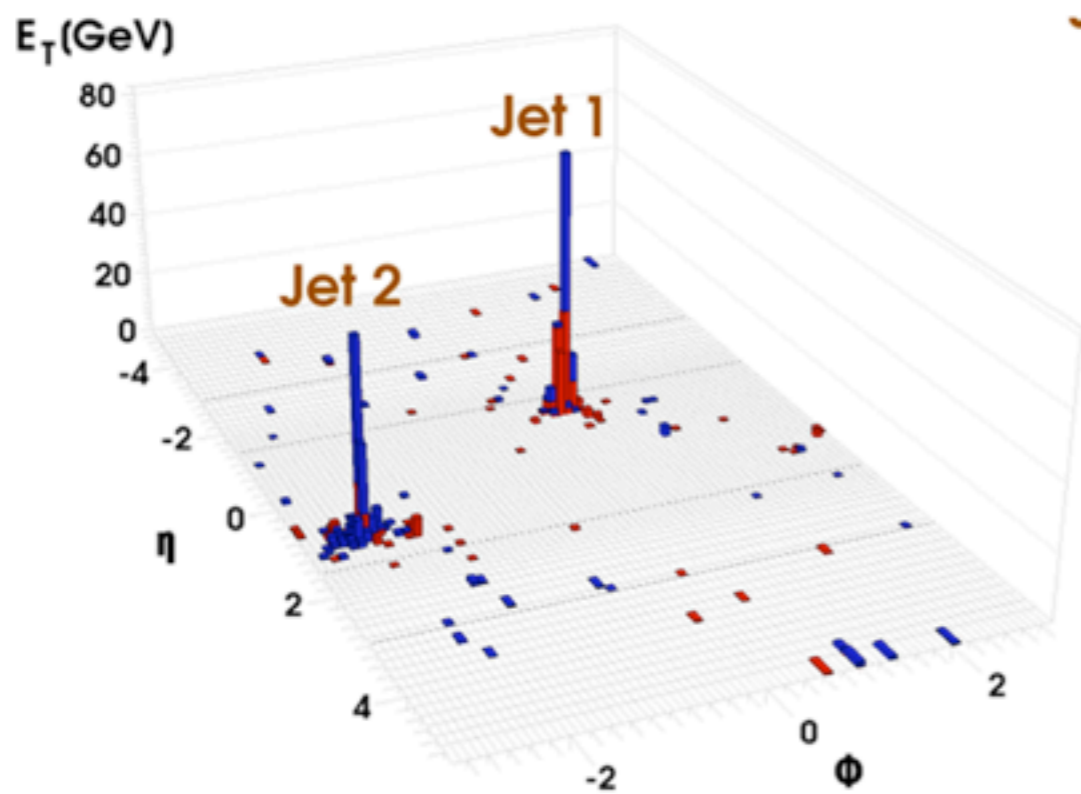
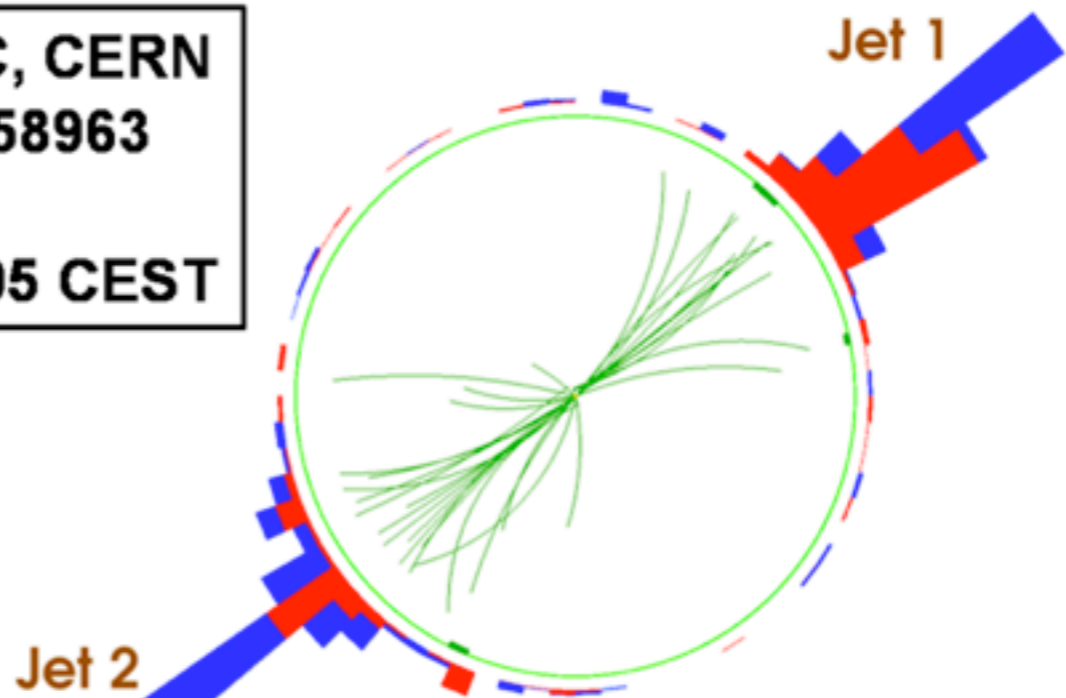
PAS-QCD-10-040



Measurements with Jets



CMS Experiment at LHC, CERN
Run 133450 Event 16358963
Lumi section: 285
Sat Apr 17 2010, 12:25:05 CEST

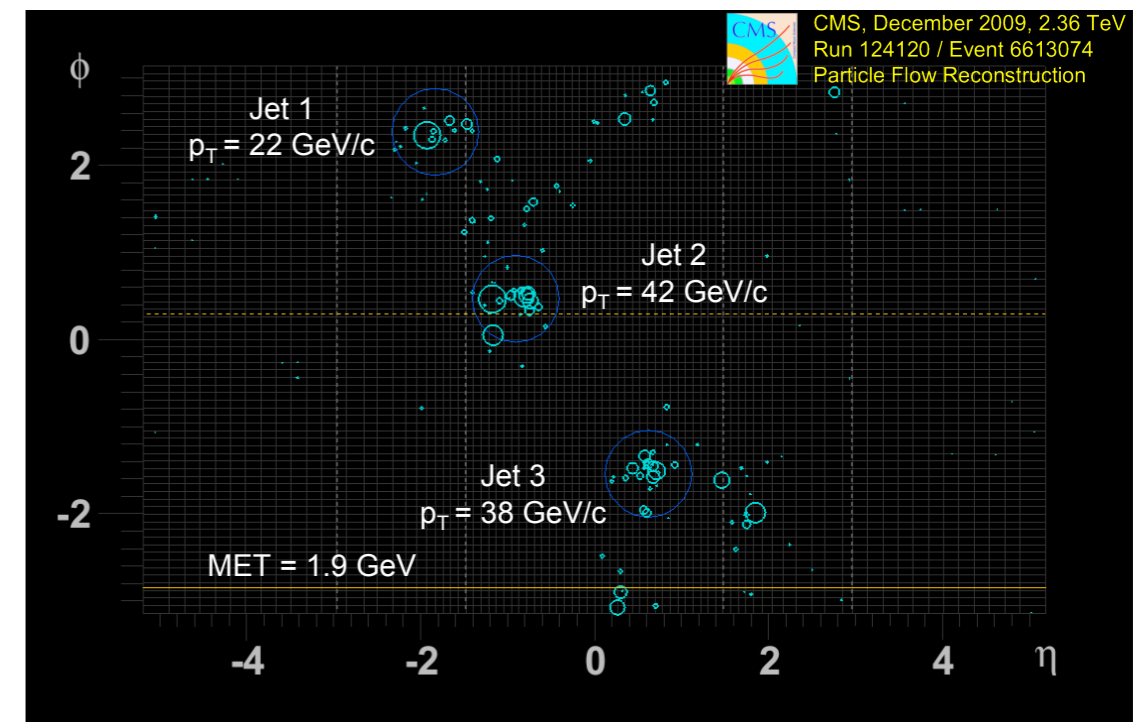
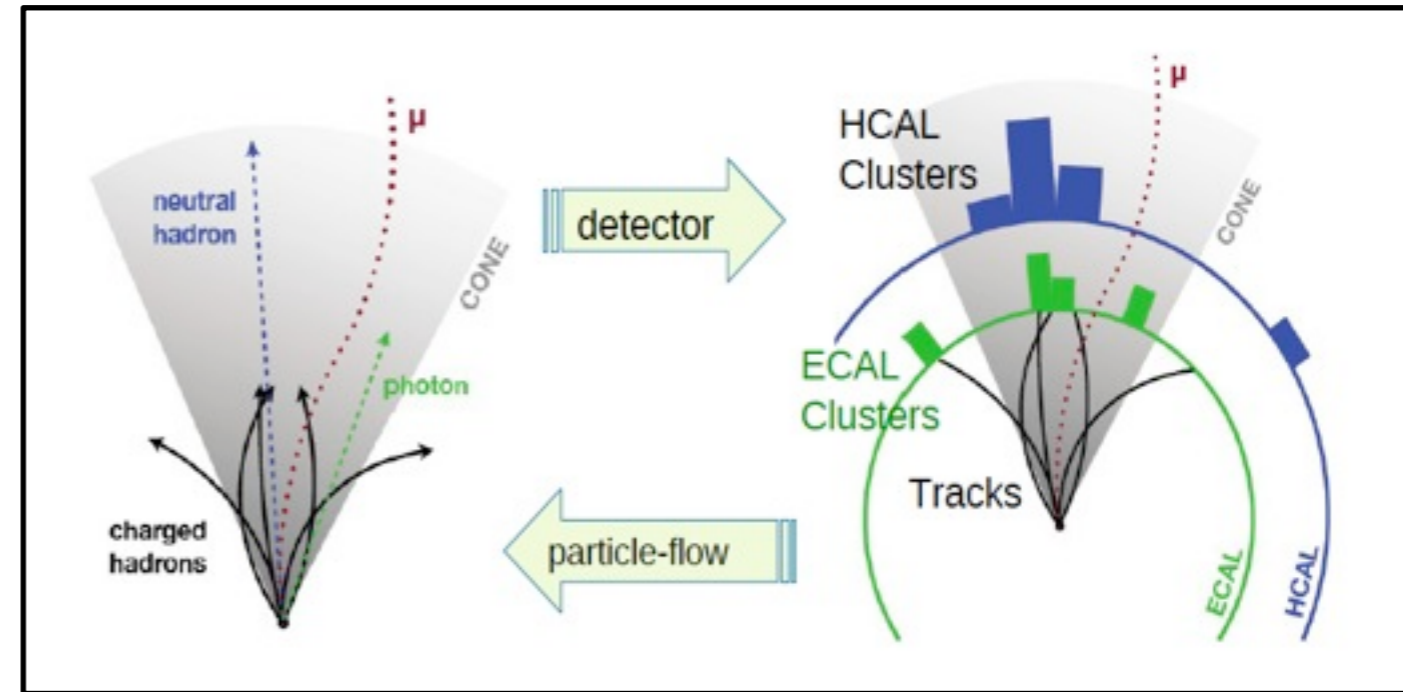


◆ Sophisticated “particle flow” reconstruction algorithm

- exploits the excellent tracker performance and the fine ECAL granularity

◆ Reconstructed individual particles according to their detection signature

- **charged hadrons** (tracks + linked ECAL/HCAL deposits)
- **neutral hadrons** (unlinked HCAL deposits)
- **photons** (unlinked ECAL deposits)
- **electrons** (tracks + linked ECAL deposits with $E/p \sim 1$)
- **muons** (tracks + muon chamber hits)

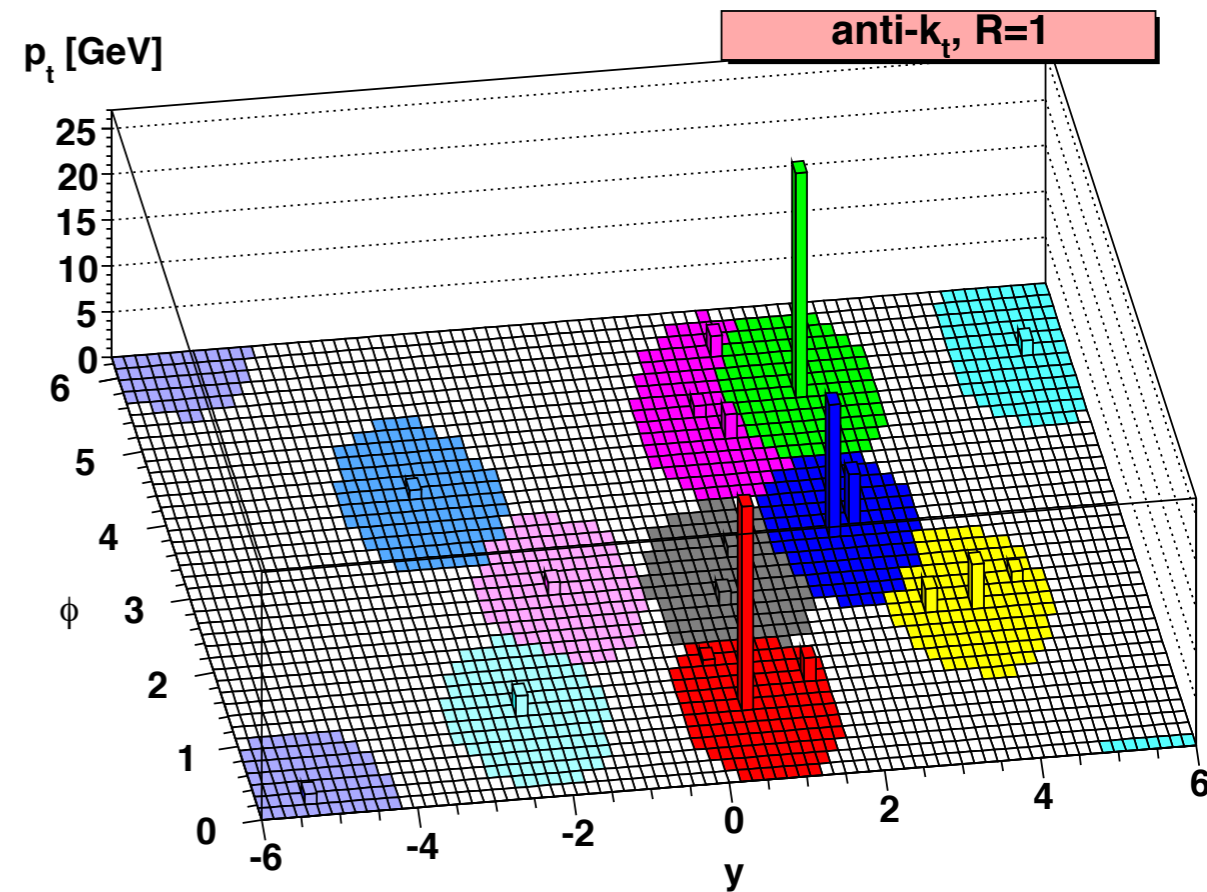


Jet Clustering

- ◆ ***anti-k_T* clustering algorithm:**
 - sequential recombination (*k_T* family)
 - infrared and collinear safety
 - geometrically well defined (circular shape in the y - ϕ plane)
 - tends to cluster around the hard energy depositions
 - distance parameter $R=0.5$ (default) & 0.7

- ◆ ***“E-scheme”* jet reconstruction**
 - 4-momentum summation
 - massive jets

- ◆ **Inputs to the jet clustering algorithm**
 - 4-momentum vectors of the reconstructed particles

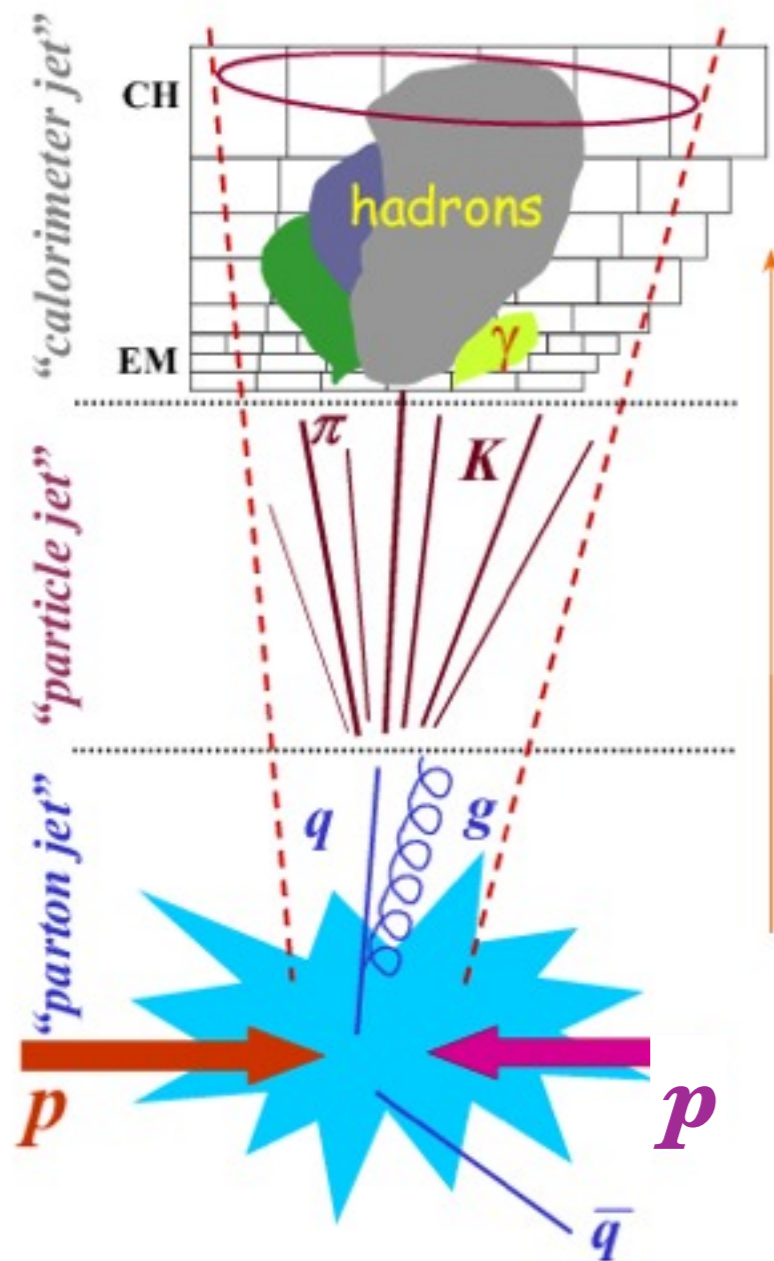


$$d_{ij} = \min \left(p_{Ti}^{-2}, p_{Tj}^{-2} \right) \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = p_{Ti}^{-2}$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

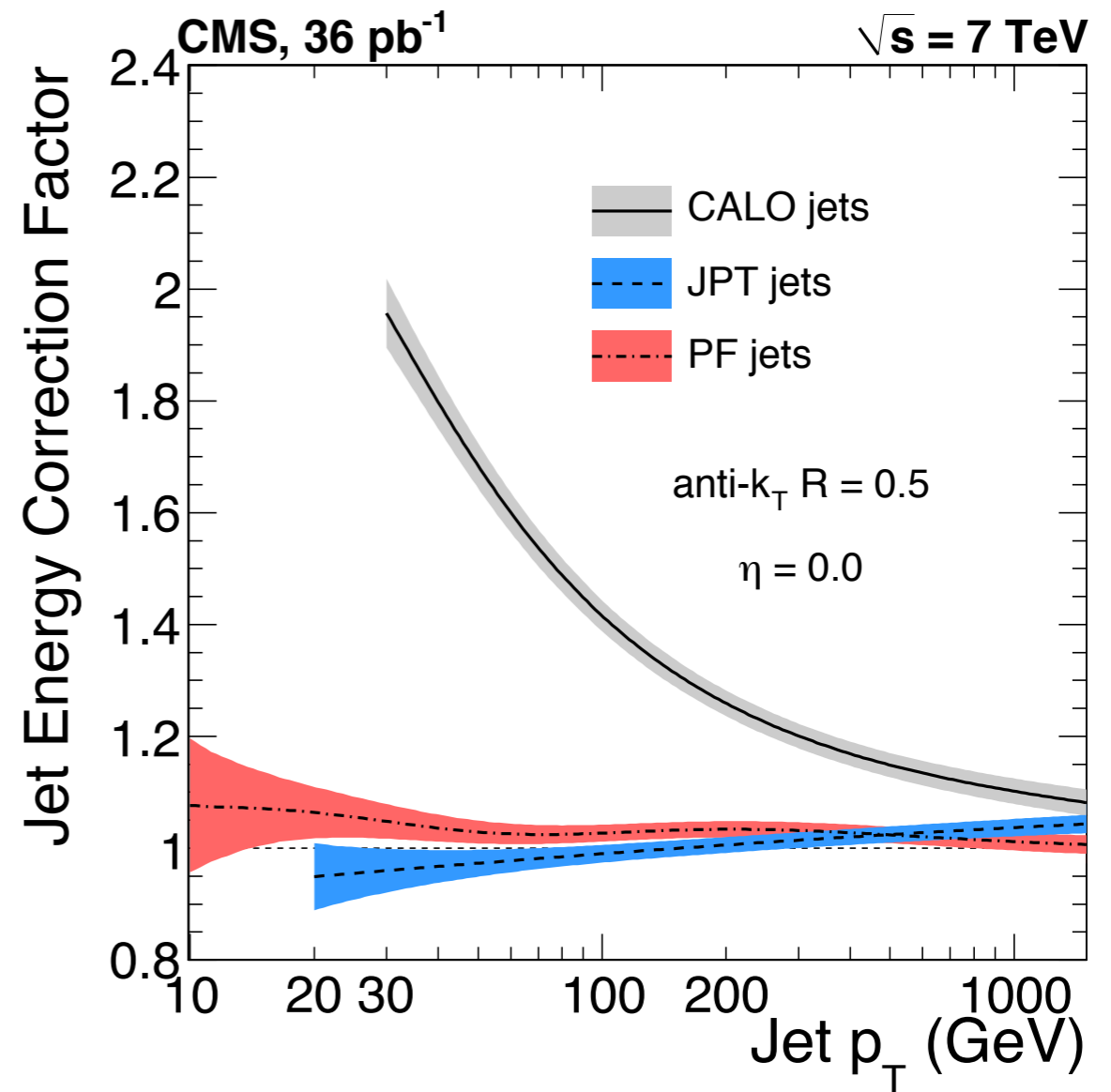
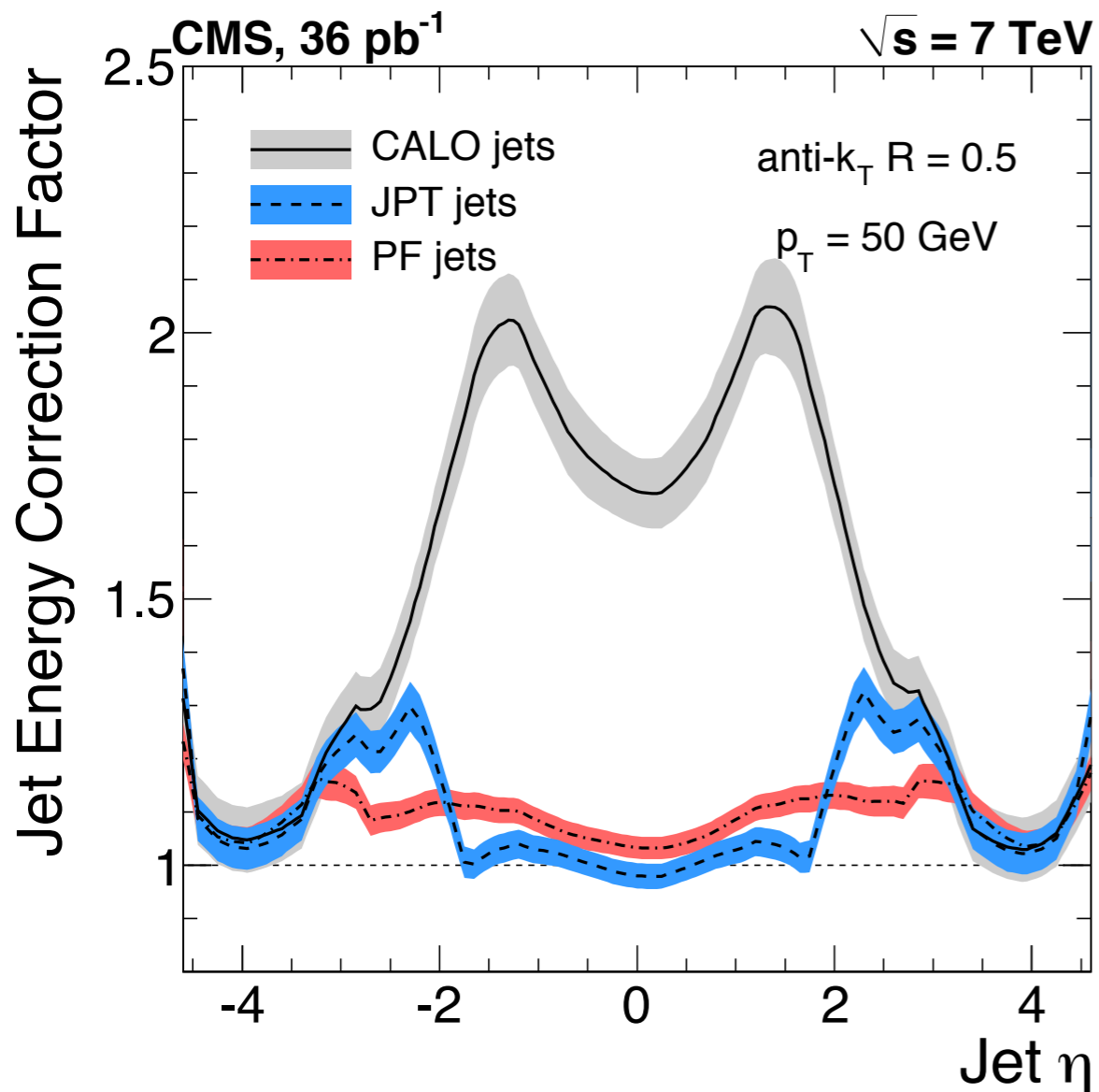
Jet Energy Calibration (overview)



- ◆ **Average correction of a detector jet to the particle level**
 - multiplicative factor to the entire jet 4-momentum vector
- ◆ **Offset correction to account for noise & pile-up**
- ◆ **Calibration based on the MC JEC**
- ◆ **Residual correction from in-situ measurements**
 - relative JES vs η from dijet p_T balancing
 - absolute JES vs p_T from γ/Z + jet p_T balance
- ◆ **Default JEC refers to the QCD flavor composition**
 - flavor dependence up to 2-3% for PF jets

$$\mathcal{C} = C_{\text{off}}(p_T^{\text{raw}}) \cdot C_{\text{MC}}(p_T', \eta) \cdot C_{\text{rel}}(\eta) \cdot C_{\text{abs}}$$

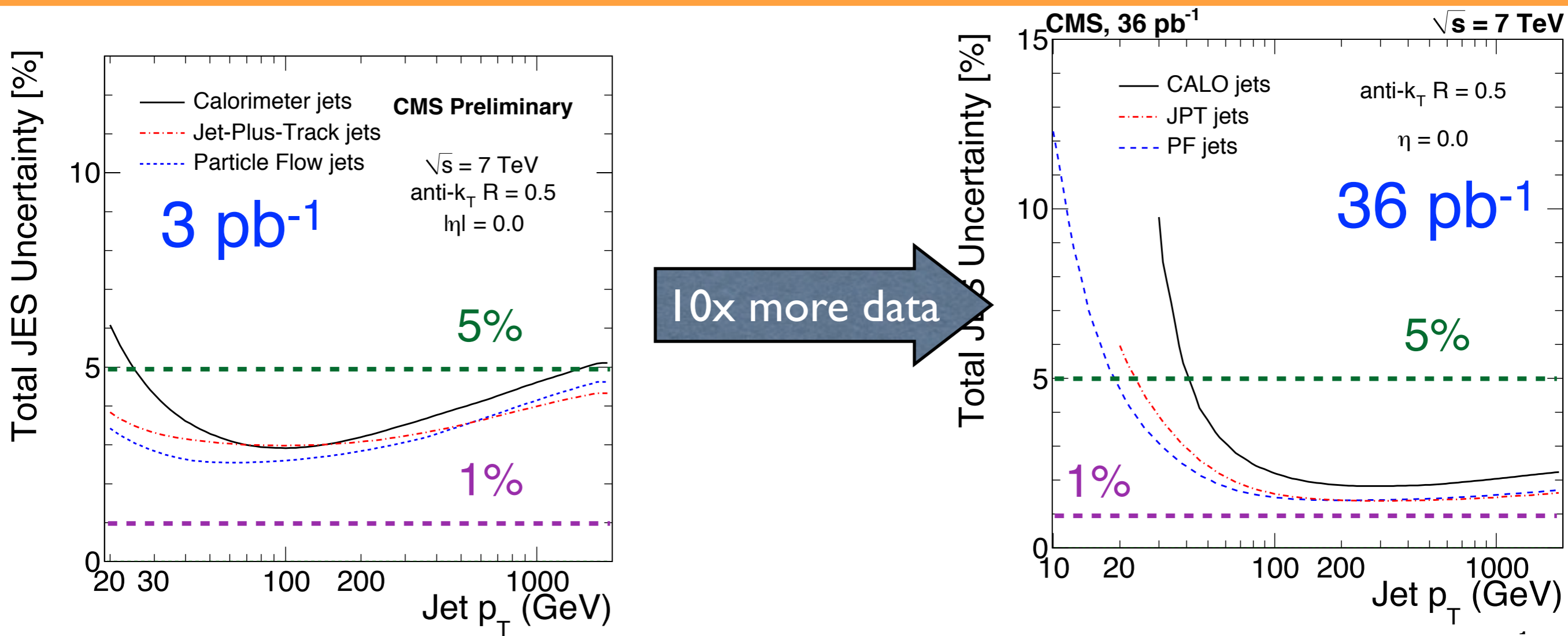
Jet Energy Calibration



- ◆ **Simple calorimetric jets require a large correction factor**
 - non-compensating calorimetric system
- ◆ **Particle-flow jets require a small correction factor (< 10%)**
 - huge improvement compared to the calorimetric jet performance

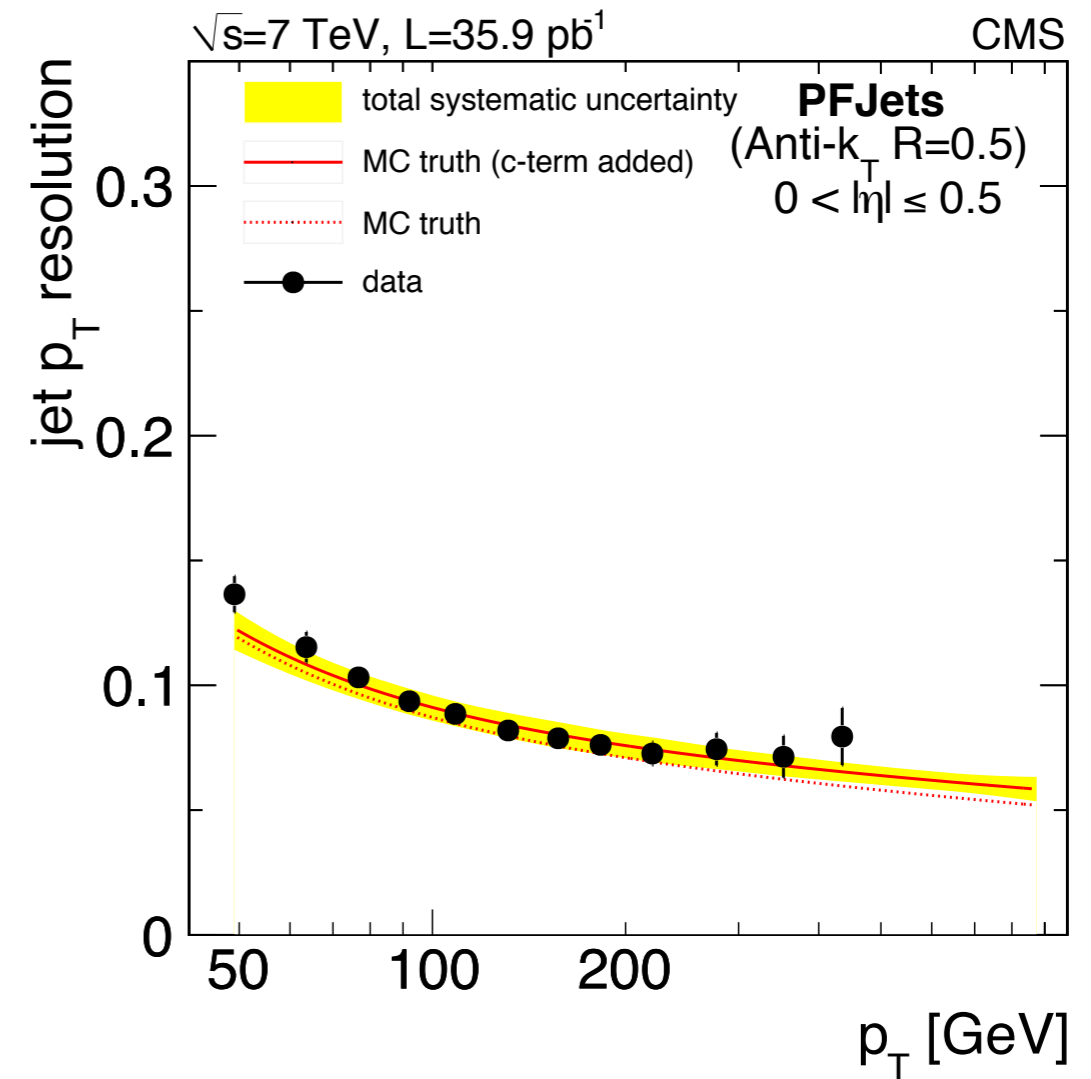
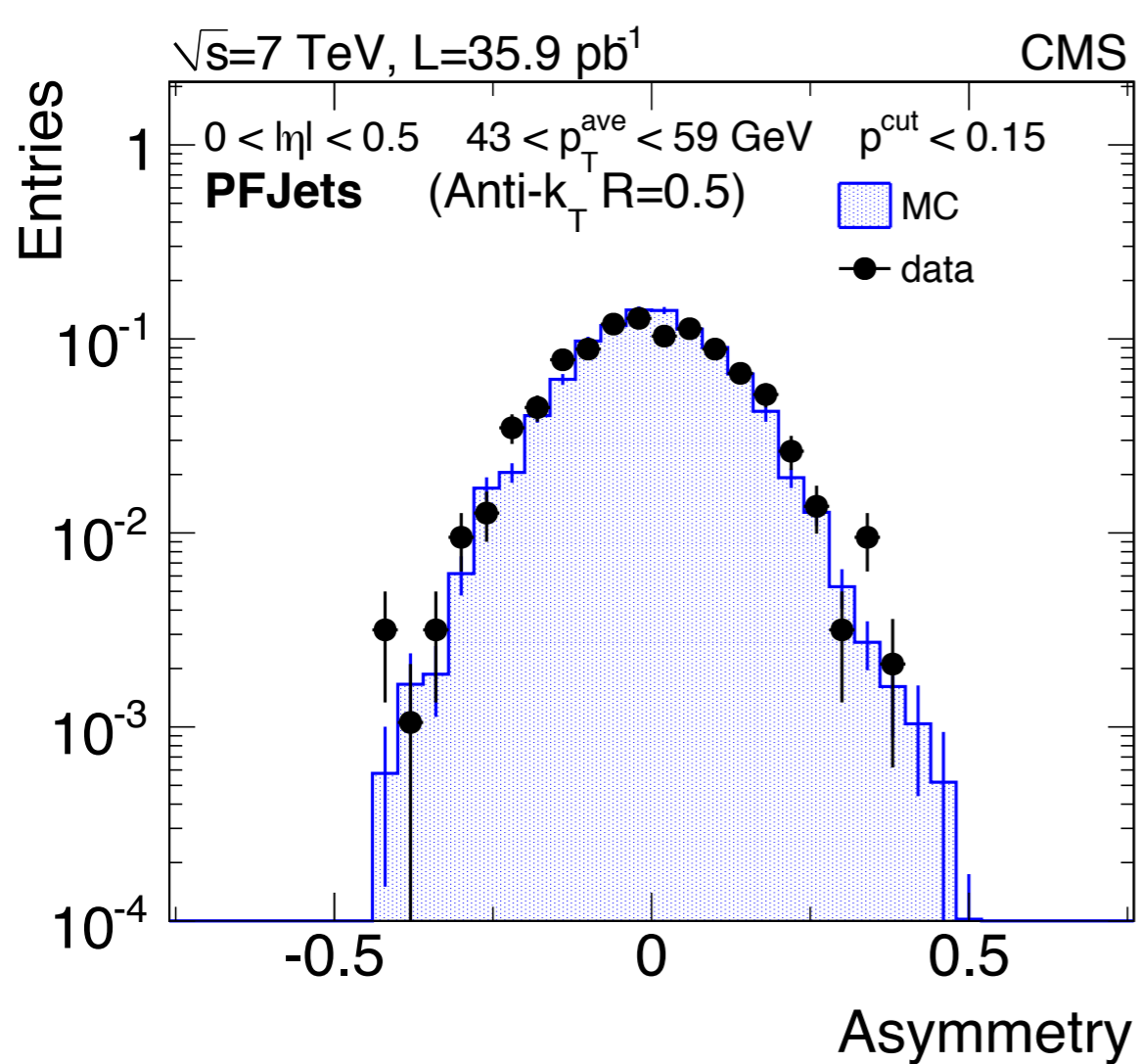
[arXiv:1107.4277](https://arxiv.org/abs/1107.4277)

Jet Energy Scale Uncertainty



- ◆ **JES uncertainty achieved in 2010: better than 3% for $p_T > 30 \text{ GeV}$**
 - significant improvement compared to the estimate with the first 3 pb⁻¹
- ◆ **the jet measurements published by CMS use the 3 pb⁻¹ JES**
 - the JES derivation is a very time consuming procedure
- ◆ **the goal of 1% JES is realistic with the 2011 data**

Jet p_T Resolution



◆ **Measured in data**

- **better than 10% for PF jets with $p_T > 80$ GeV**
- dijet asymmetry method
- photon + jet p_T balance

◆ **Simulated resolution systematically better**

- by 10-20% (relative) depending on η

[arXiv:1107.4277](https://arxiv.org/abs/1107.4277)



Inclusive Jet Cross Section

◆ Double-differential inclusive jet cross section vs jet p_T and y

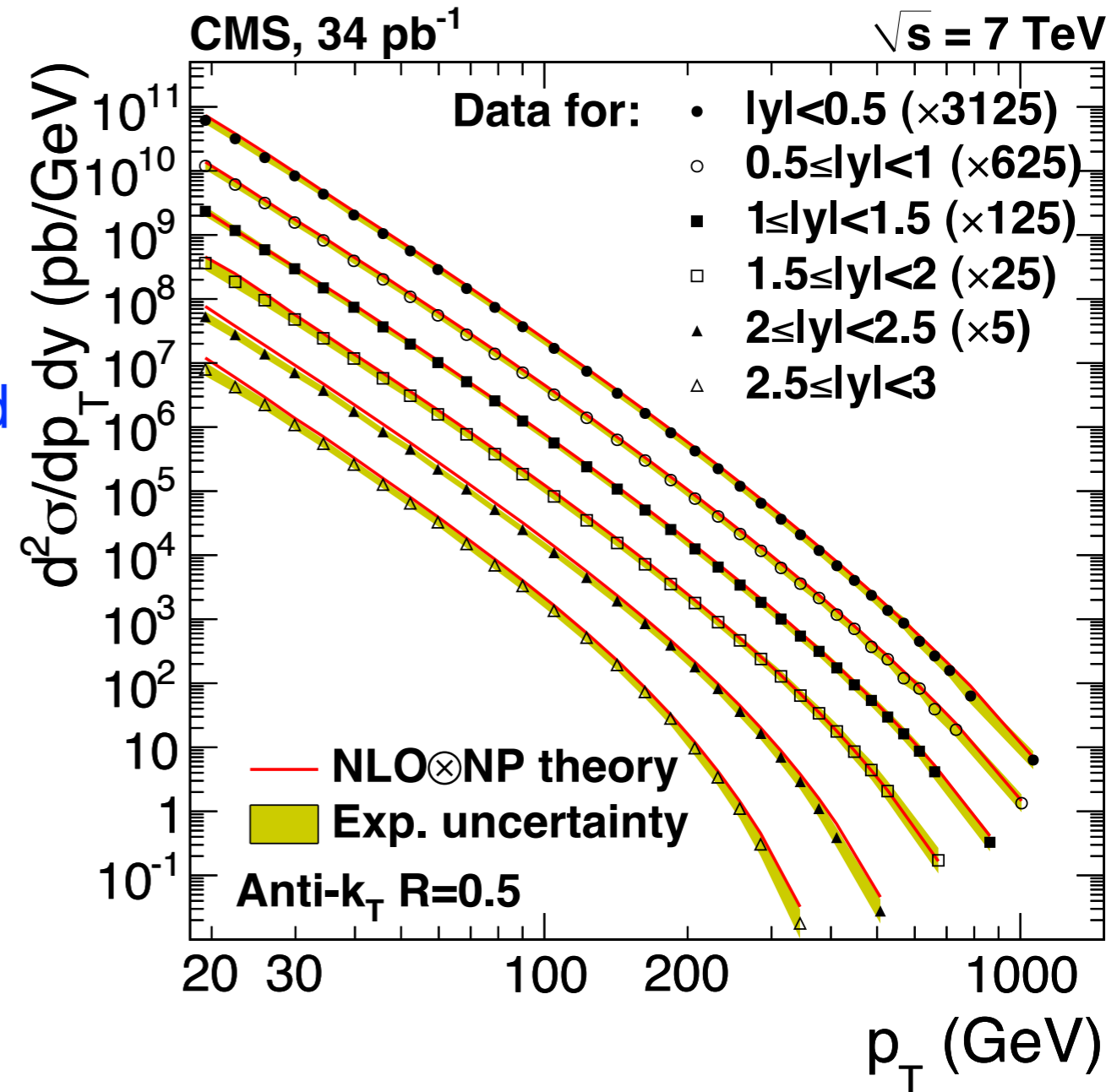
- using anti- k_T PF jets with $R=0.5$
- 34 pb^{-1}
- p_T range from 18 GeV to 1.1 TeV
- 6 rapidity bins, up to $|y|=3.0$ (the forward region $3.0 < |y| < 5.0$ is covered by another, dedicated measurement)

◆ Unfolding

- simple bin-by-bin correction using the ansatz method

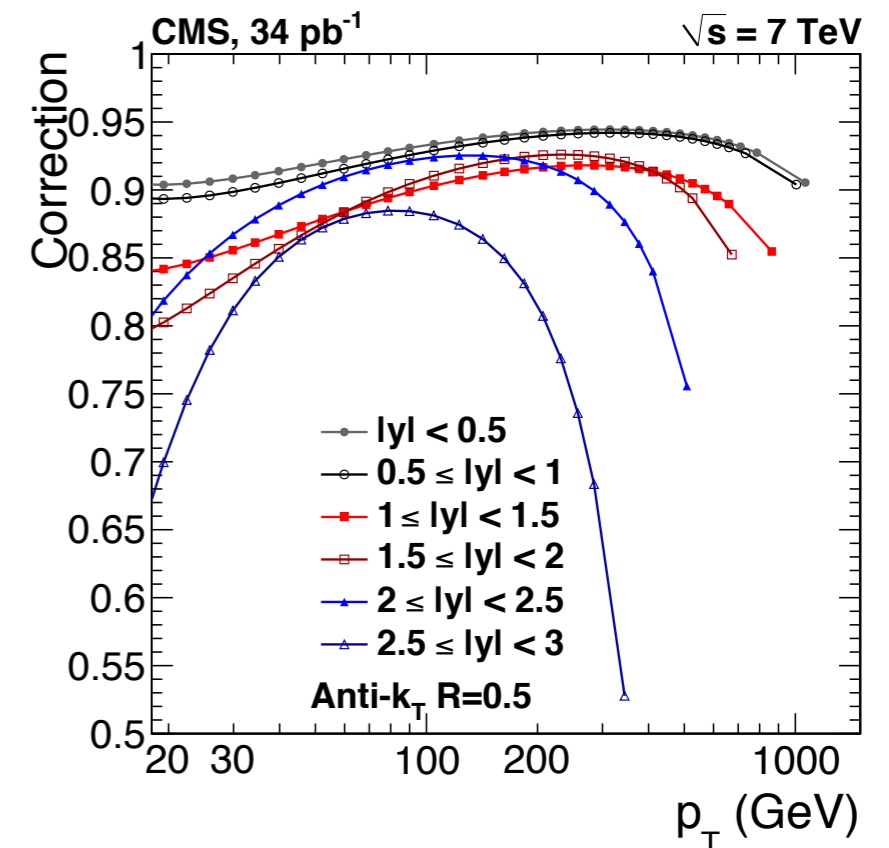
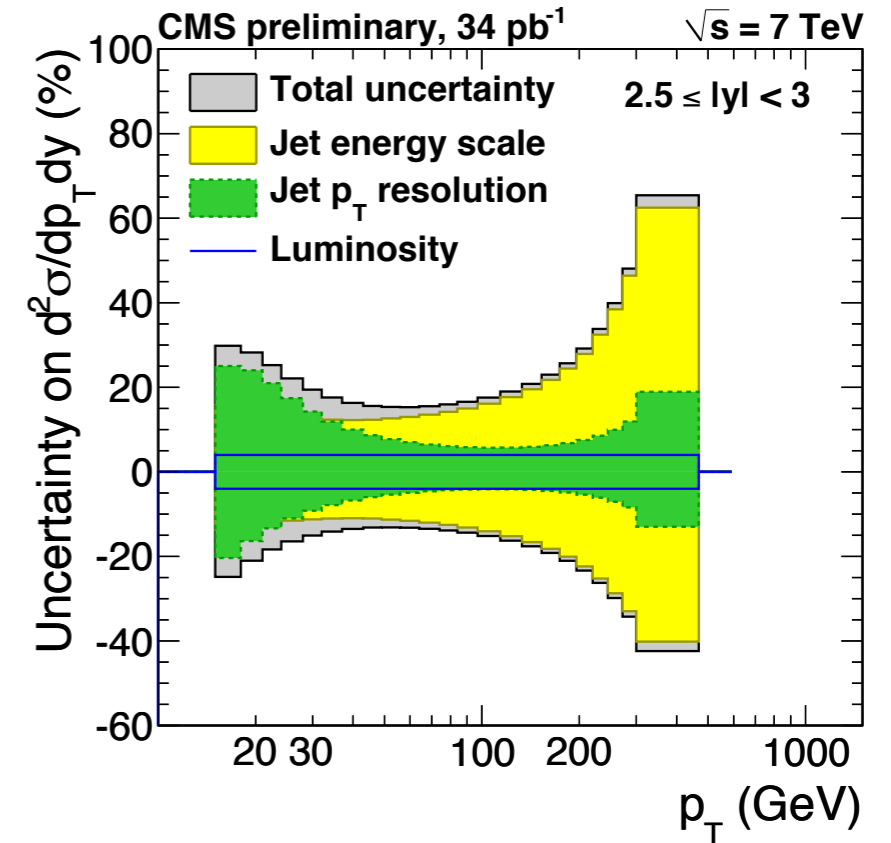
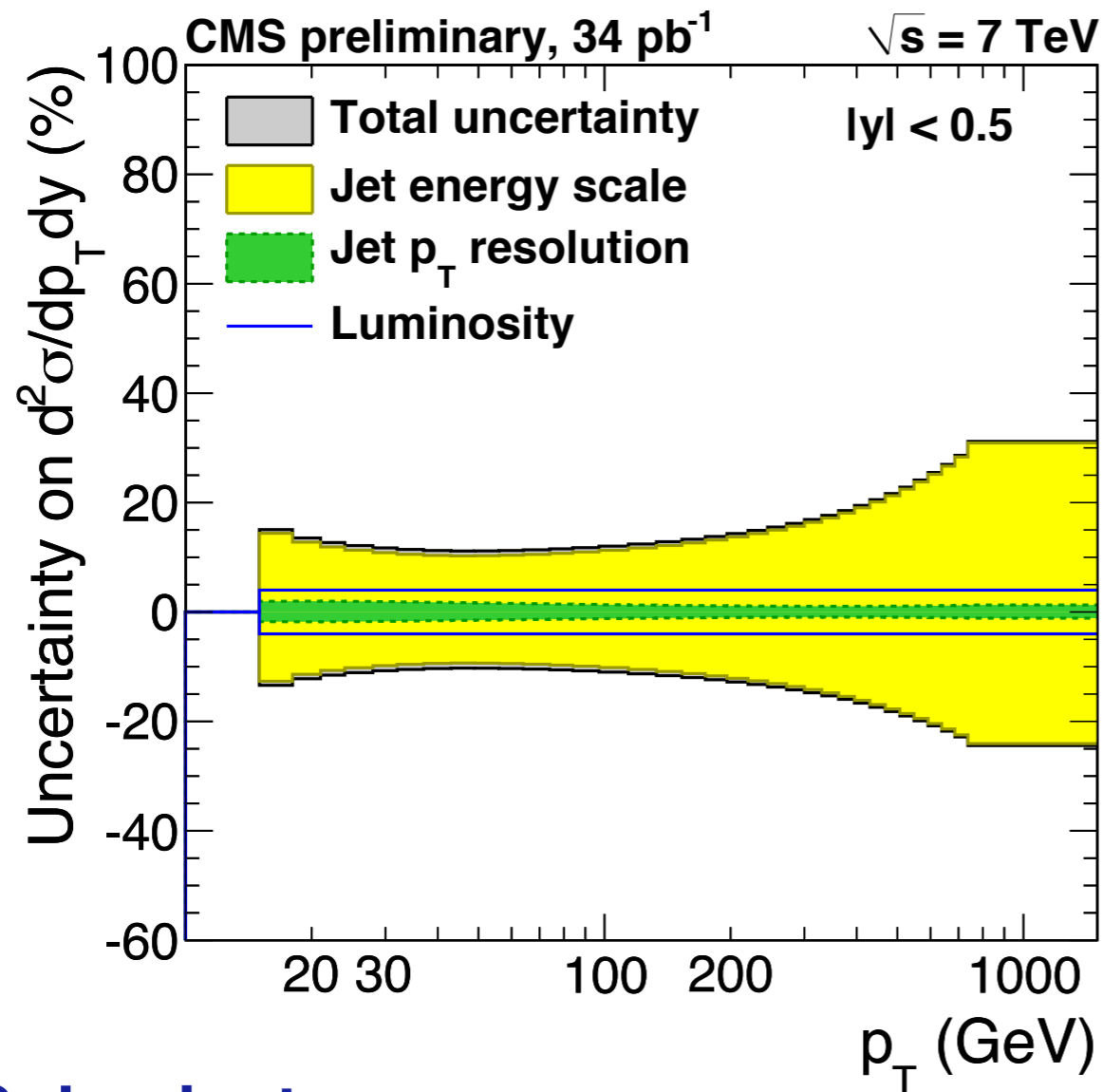
◆ Theory

- NLOJet++ (*fastNLO*)



PRL 107 (2011) 132001

Experimental Uncertainties



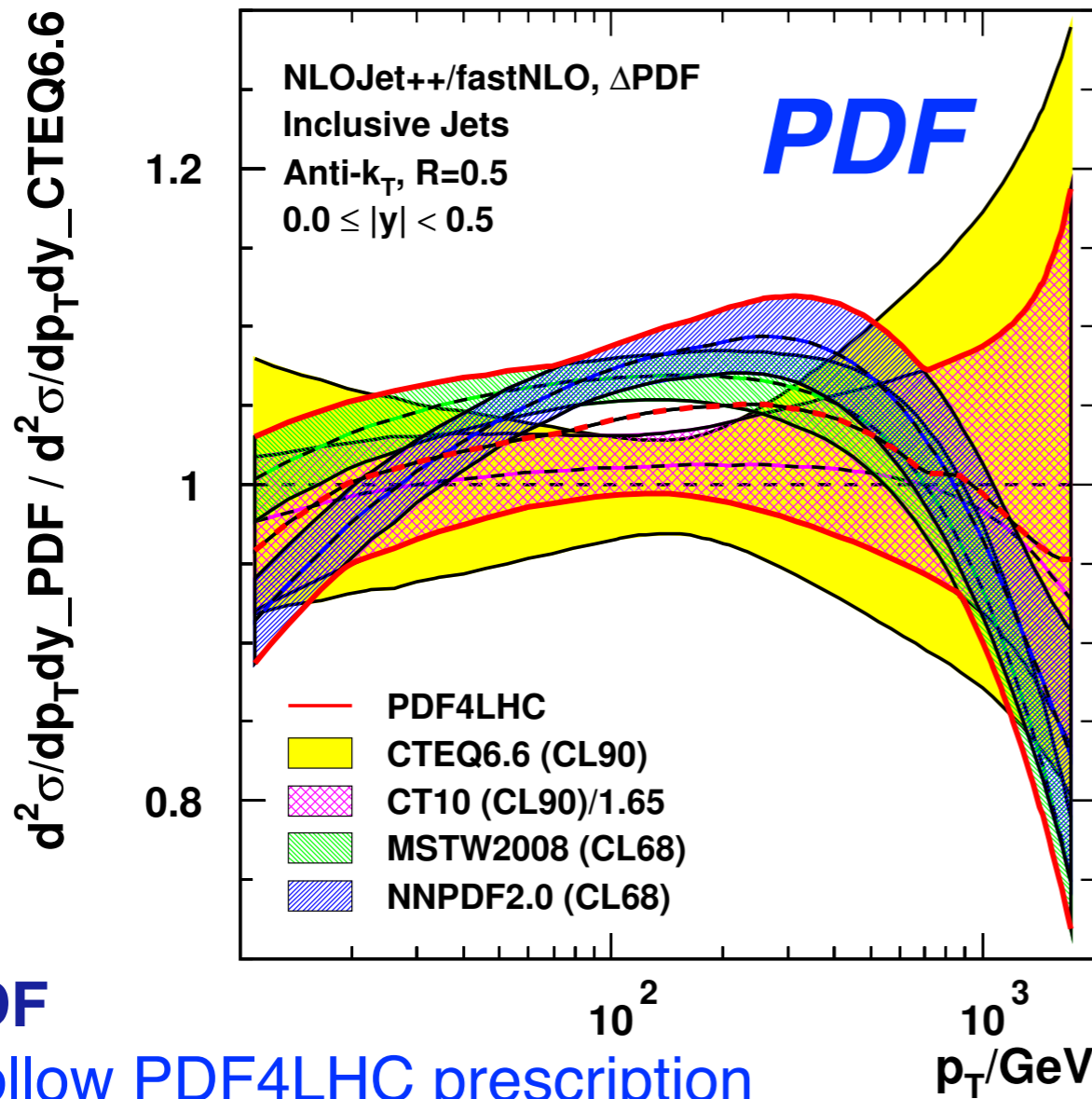
◆ JES dominates

- falling spectrum: 1% JES uncertainty corresponds to 5-10% cross-section unc.

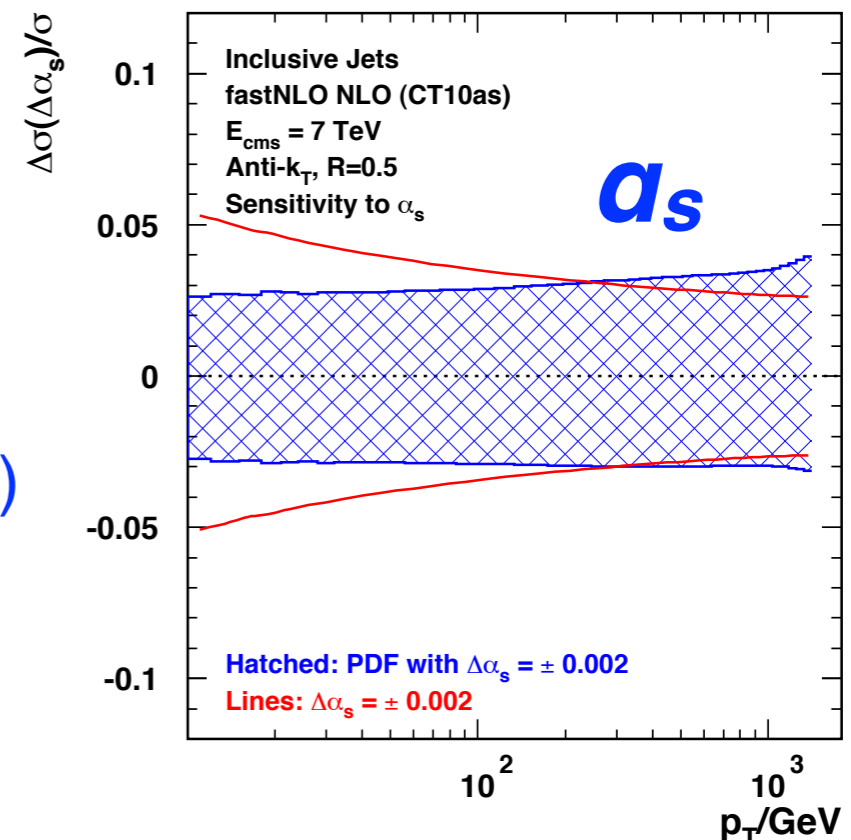
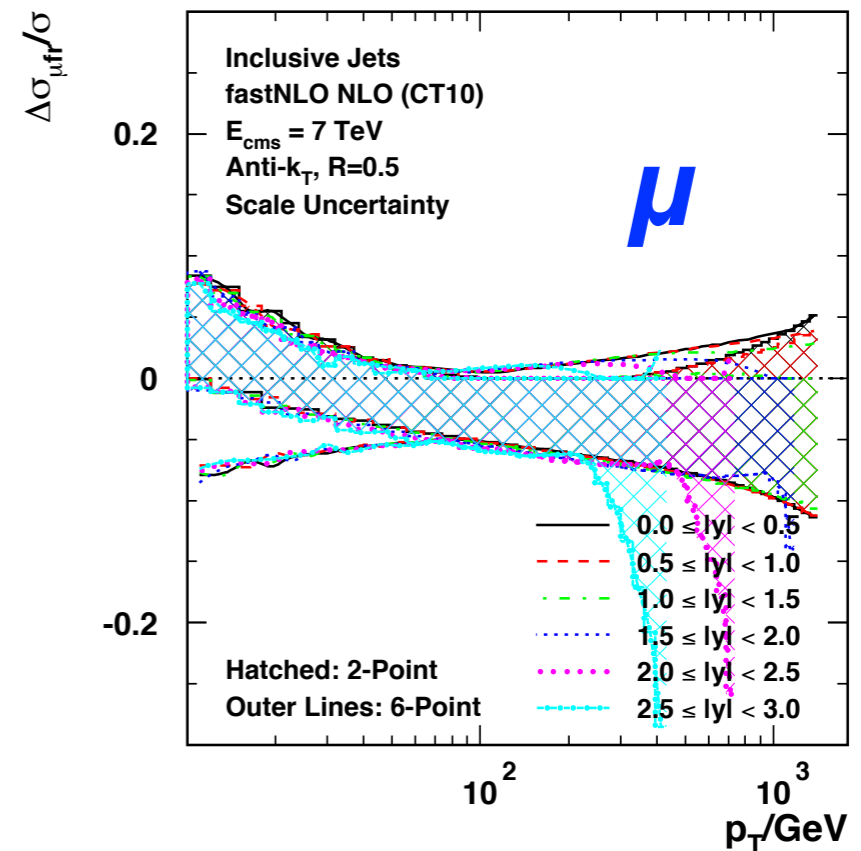
◆ Resolution enters through unsmearing

- significant at high rapidity

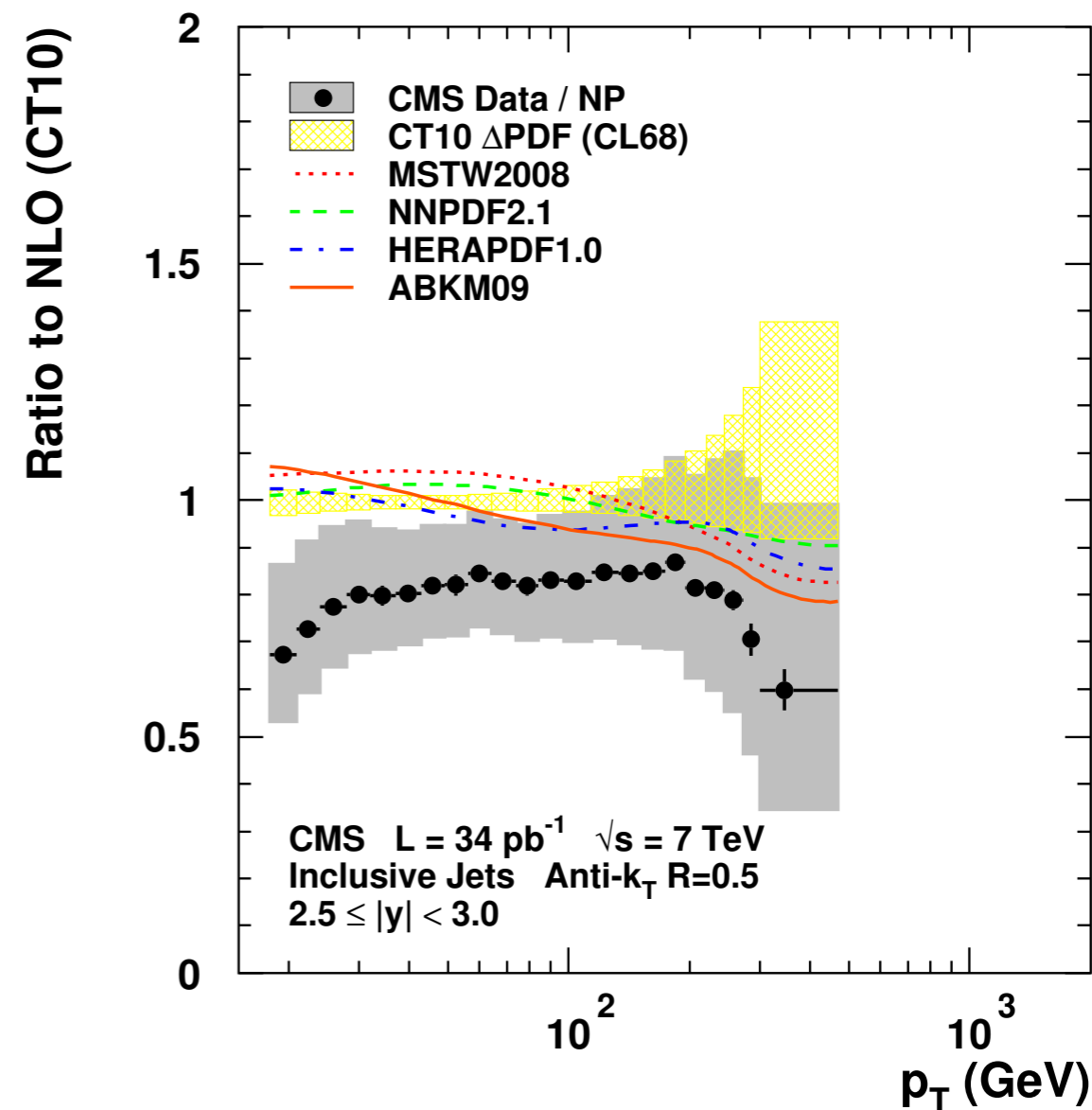
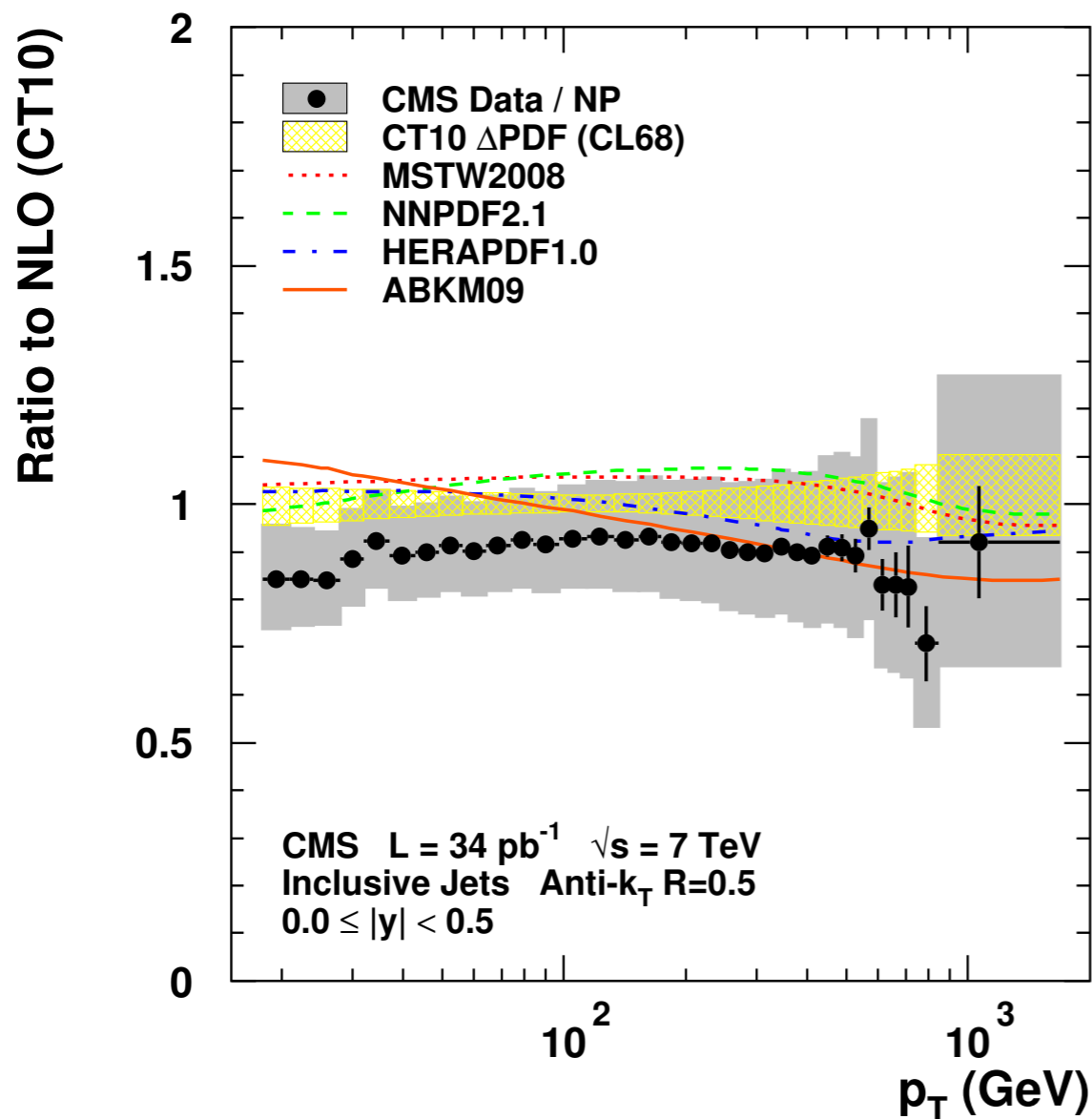
Theory Uncertainties



- ◆ PDF
 - follow PDF4LHC prescription
- ◆ scale ($\mu_R = \mu_F = p_T$)
 - 6 point variation: $(\mu_R/p_T, \mu_F/p_T) = (0.5, 0.5) \dots (1, 2)$
- ◆ $\Delta\alpha_s = \pm 0.002$ (CT10)
- ◆ NP correction
 - estimated with Pythia6 and Herwig++
 - dominant uncertainty at low p_T



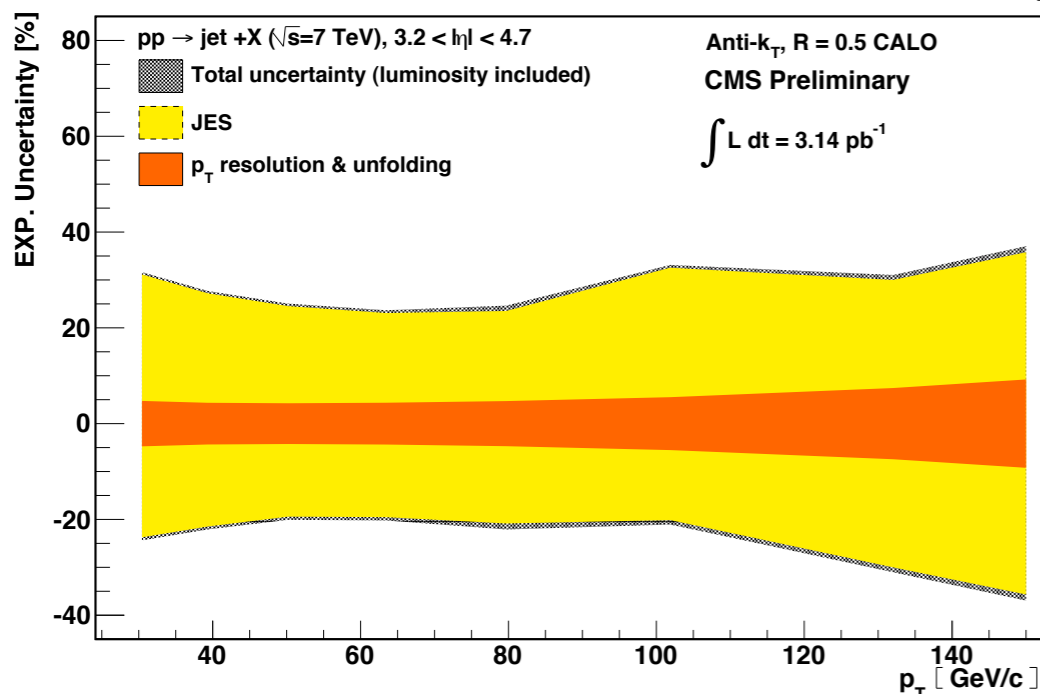
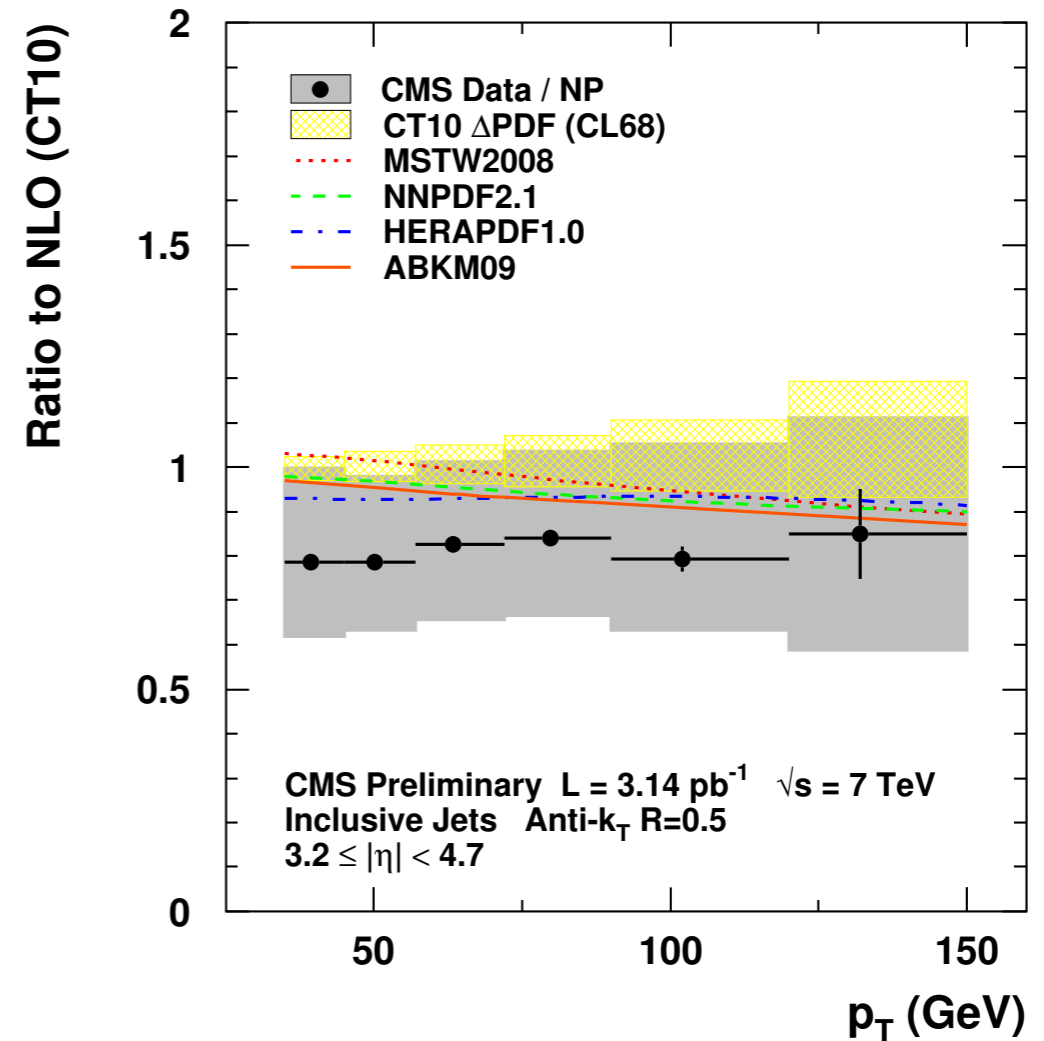
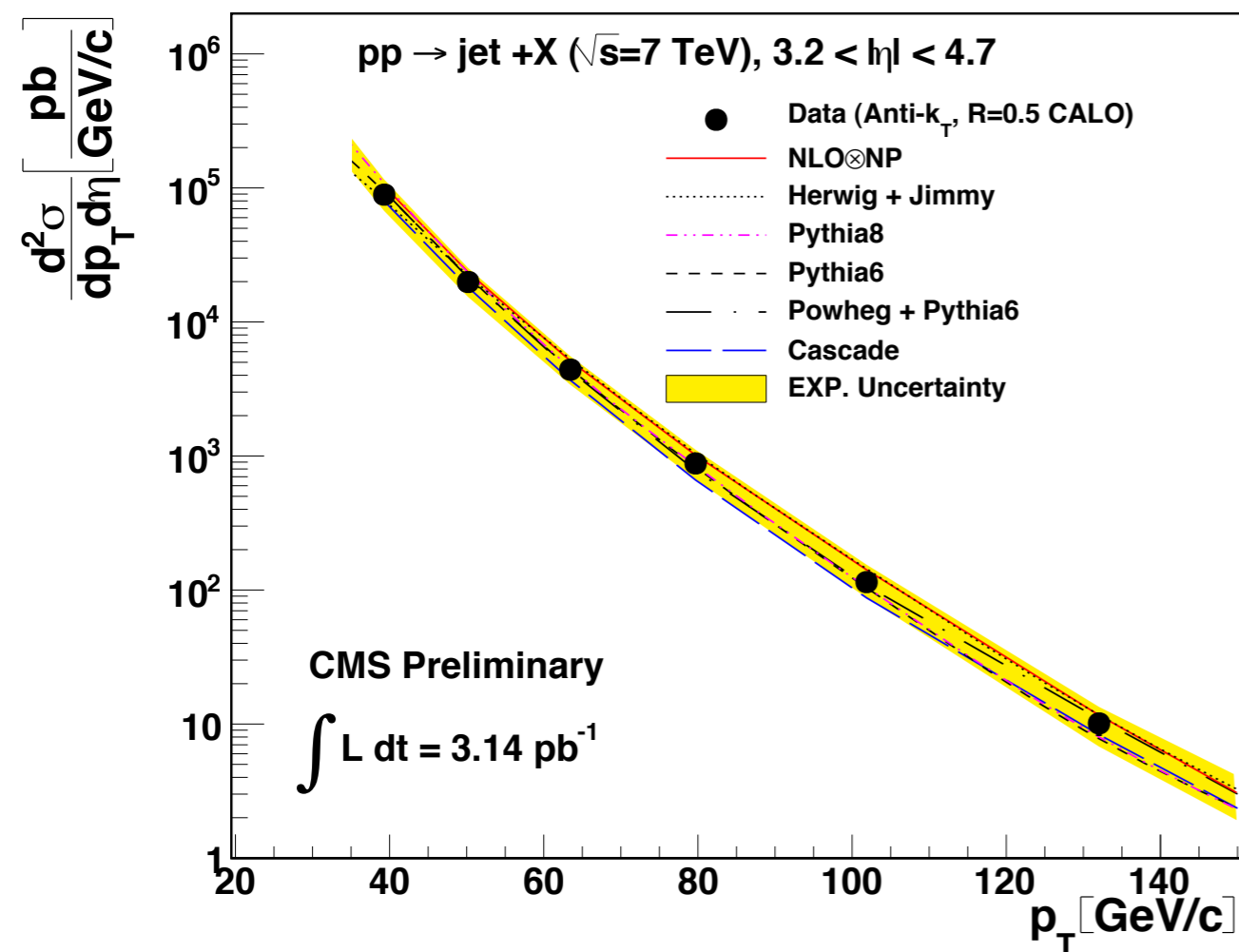
PDF Comparisons



◆ Comparison with various PDF sets

- compatibility with all PDFs in the central rapidity bins
- better agreement at higher jet p_T ($> 100 \text{ GeV}$) but NP correction uncertainties large at low p_T
- the agreement slightly worsens in the outer rapidity bins

CMS-NOTE-2011-004



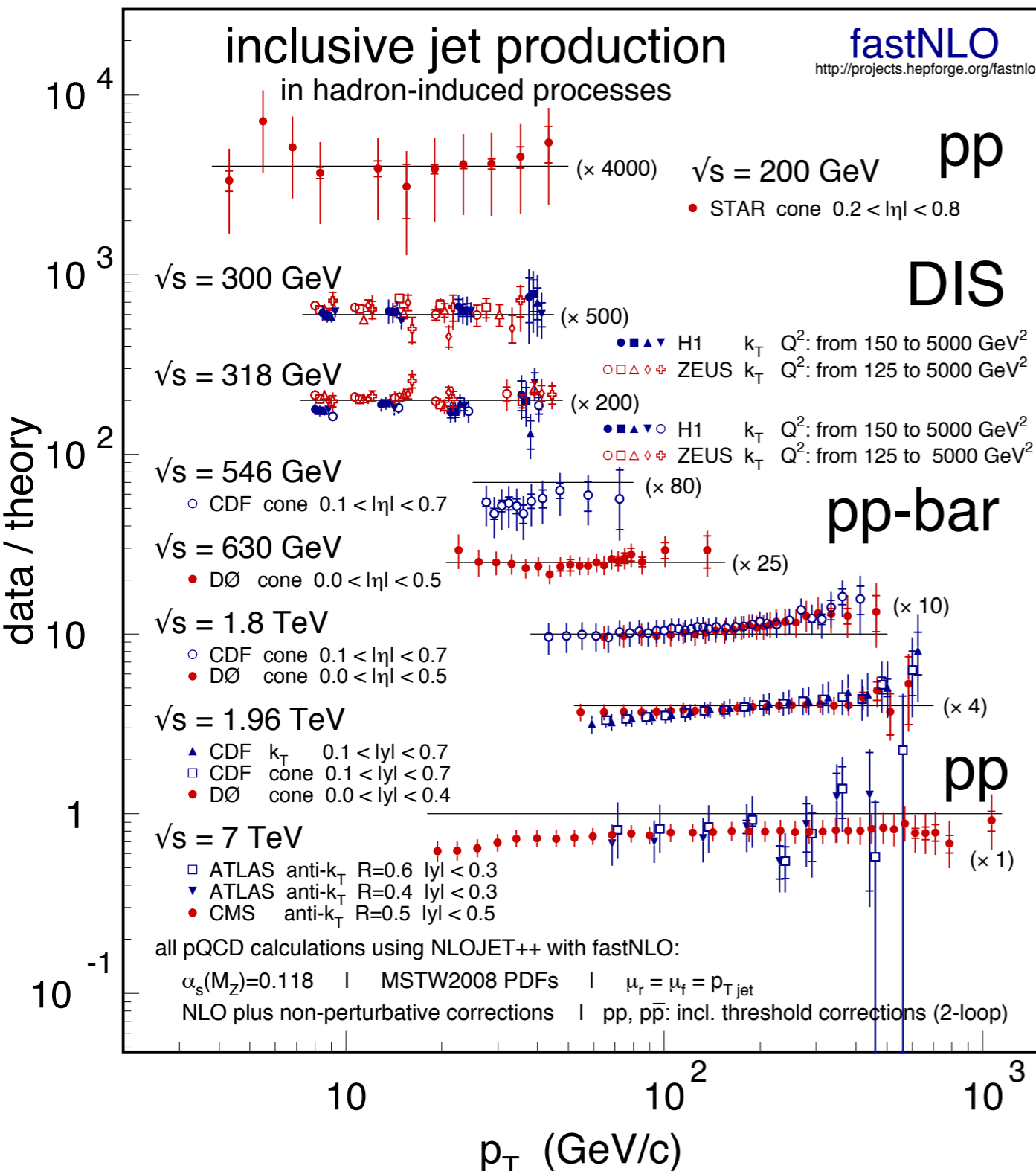
◆ Inclusive forward jet production cross section

- measurement dominated by the JES uncertainty
- good agreement with the MC predictions
- compatible with the NLO prediction

CMS-FWD-10-003

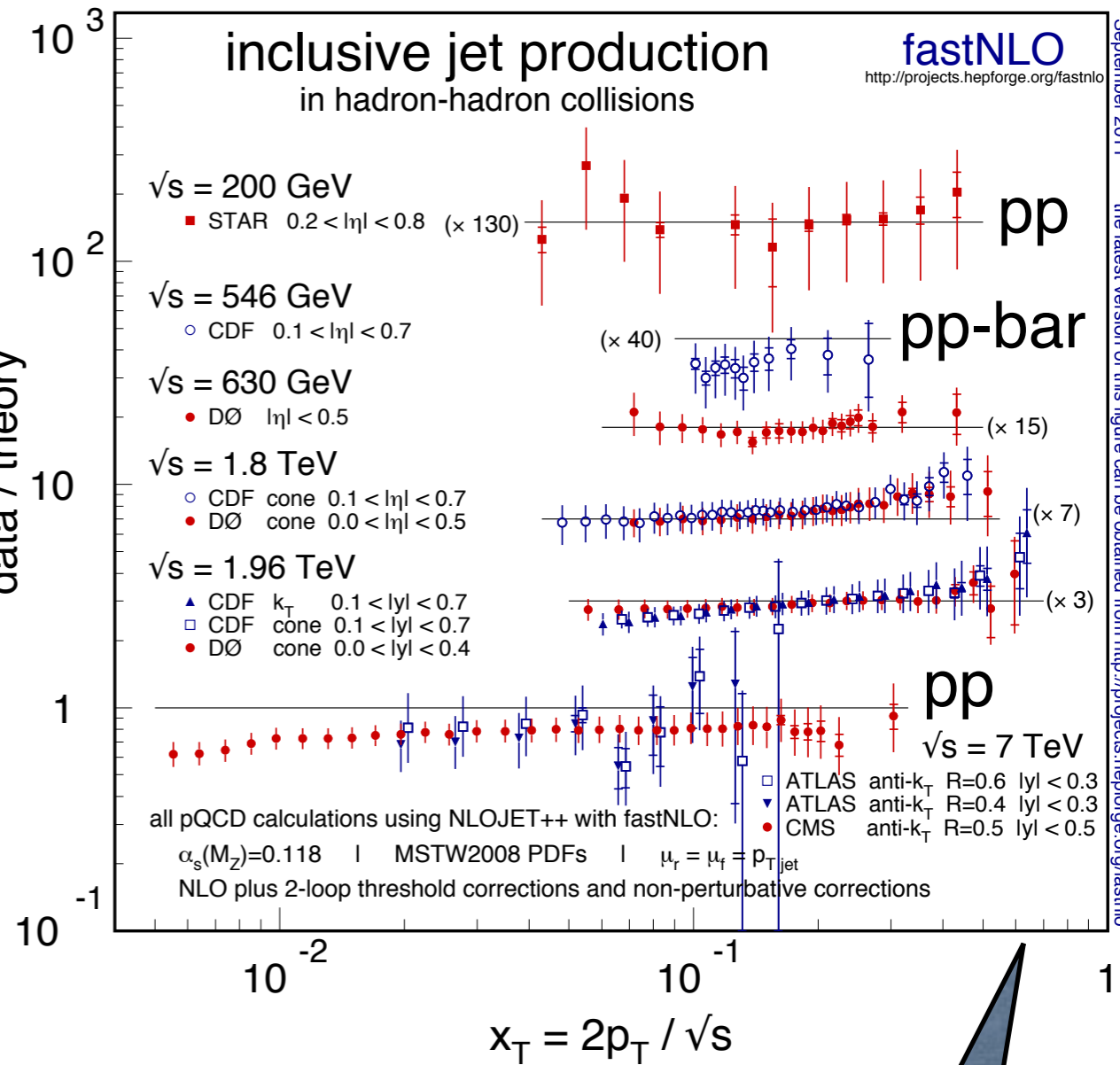


Inclusive Jets: the Big Picture



September 2011

the latest version of this figure can be obtained from <http://projects.hepforge.org/fastnlo>



September 2011

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The 2011 LHC data of $\sim 5\text{fb}^{-1}$ extend to $x_T \sim 0.6$

arXiv:1109.1310



Dijet Cross Section

◆ Double-differential inclusive dijet cross section vs dijet invariant mass and l_{\max}

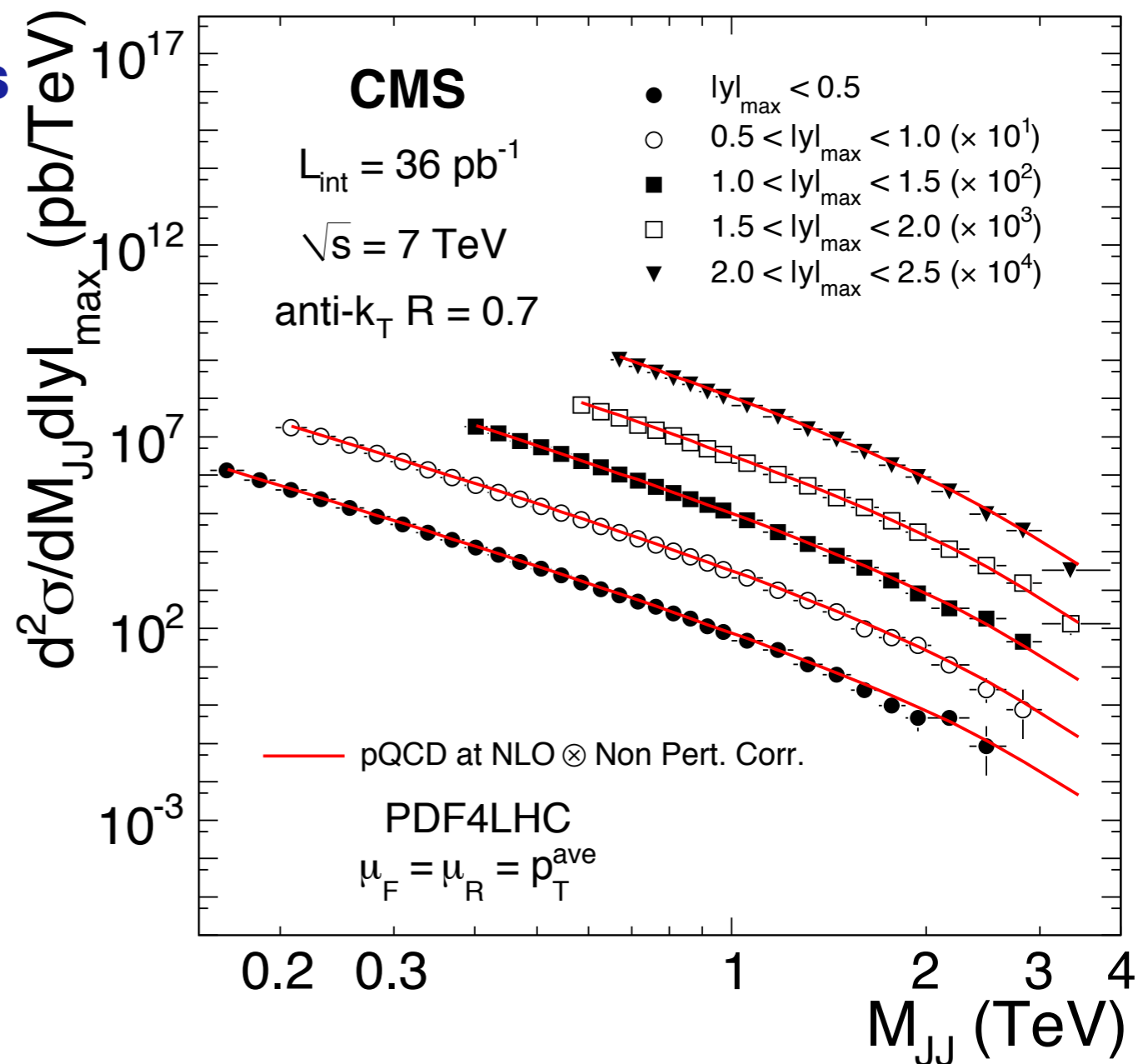
- using anti- k_T PF jets with **$R=0.7$**
- 36 pb^{-1}
- $p_{T,1} > 60 \text{ GeV}$, $p_{T,2} > 30 \text{ GeV}$
- mass range from 0.16 to 3.5 TeV
- 5 bins of l_{\max} , up to 2.5

◆ Unfolding

- simple bin-by-bin correction using MC smearing

◆ Theory

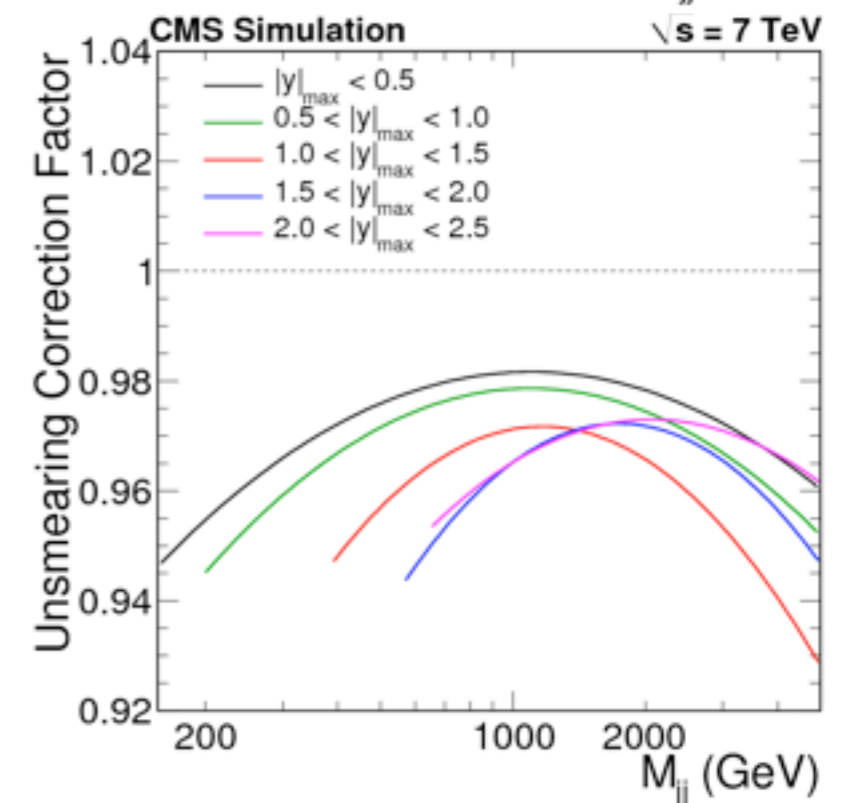
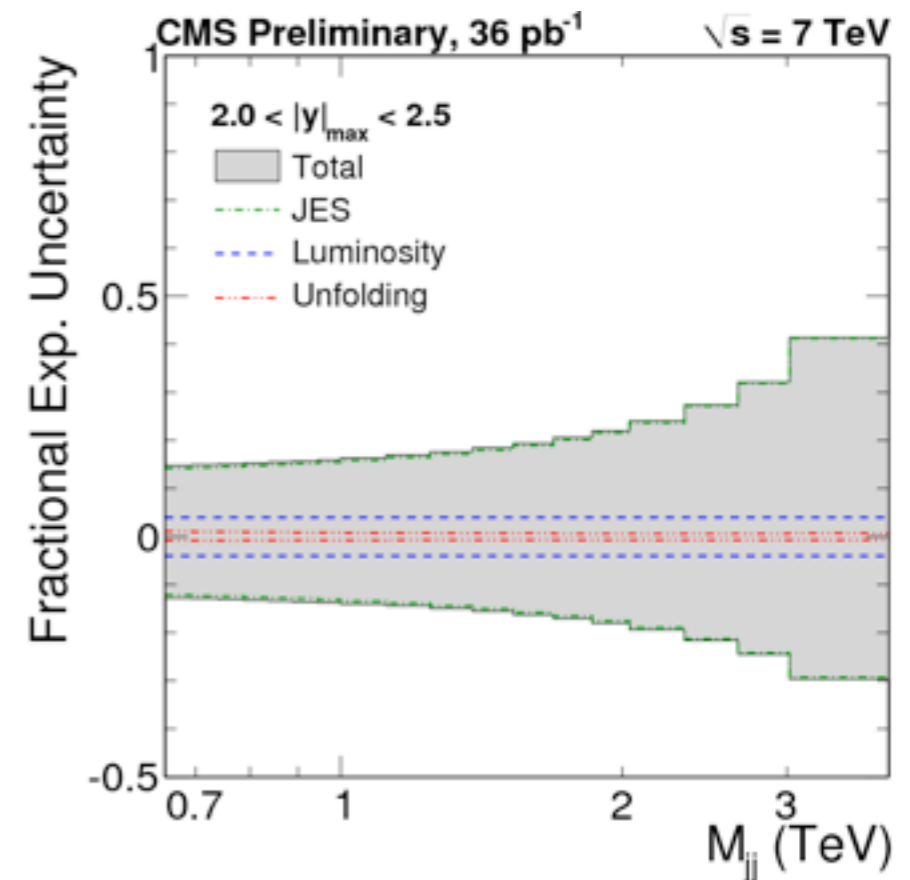
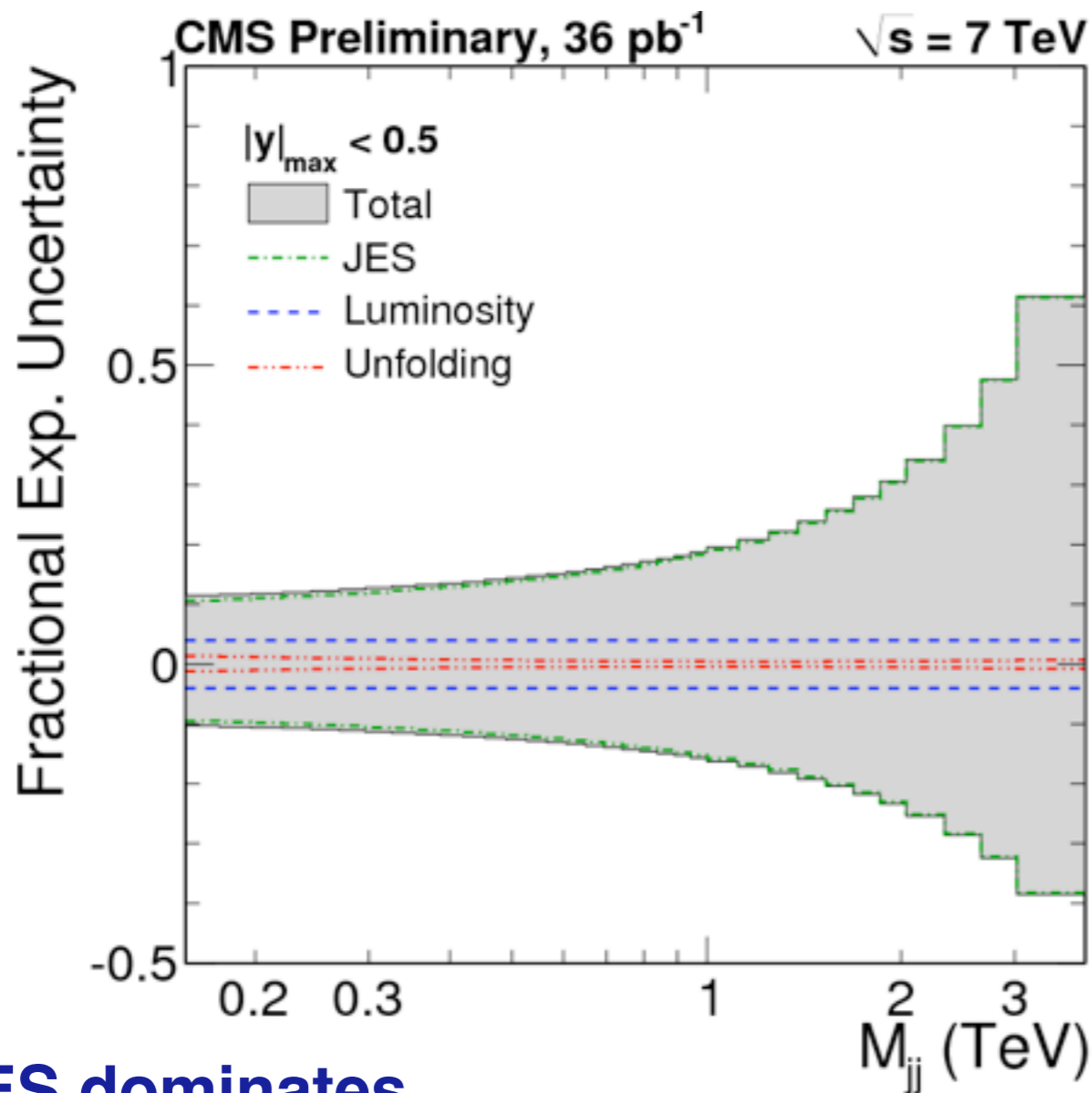
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Experimental Uncertainties

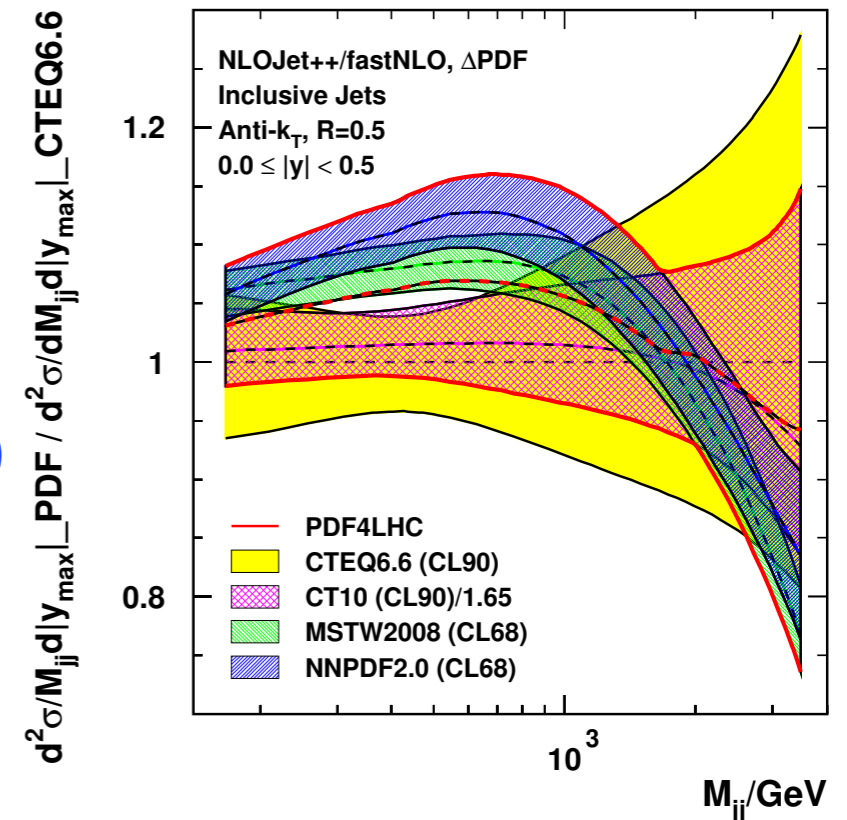
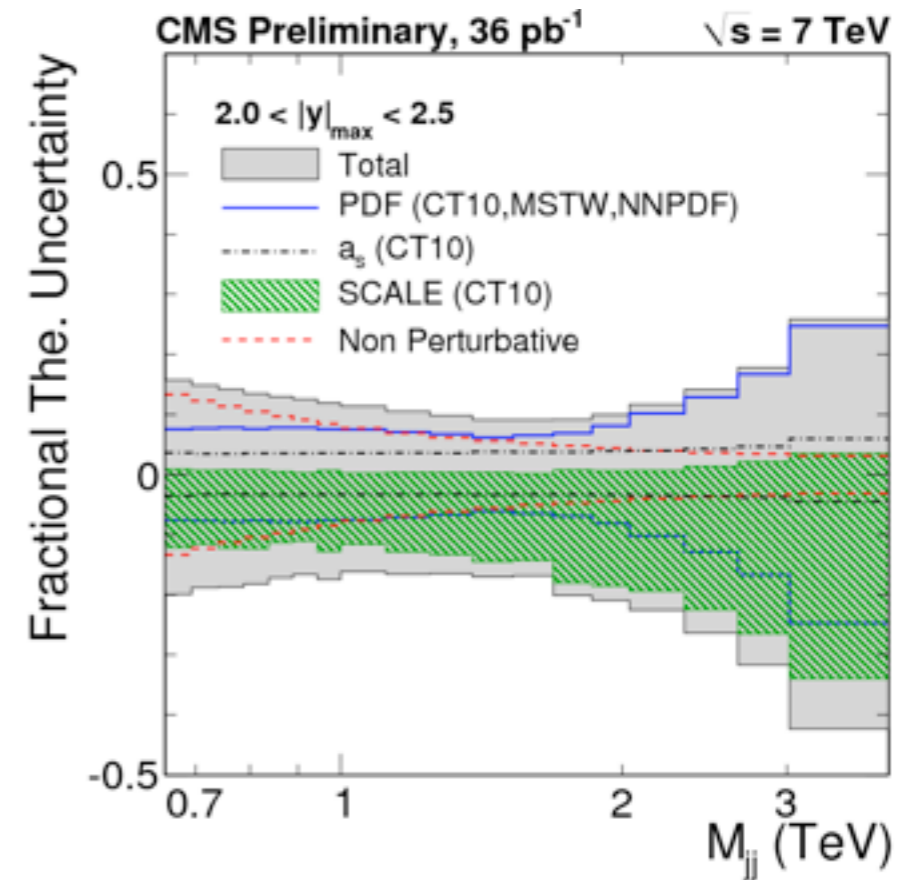
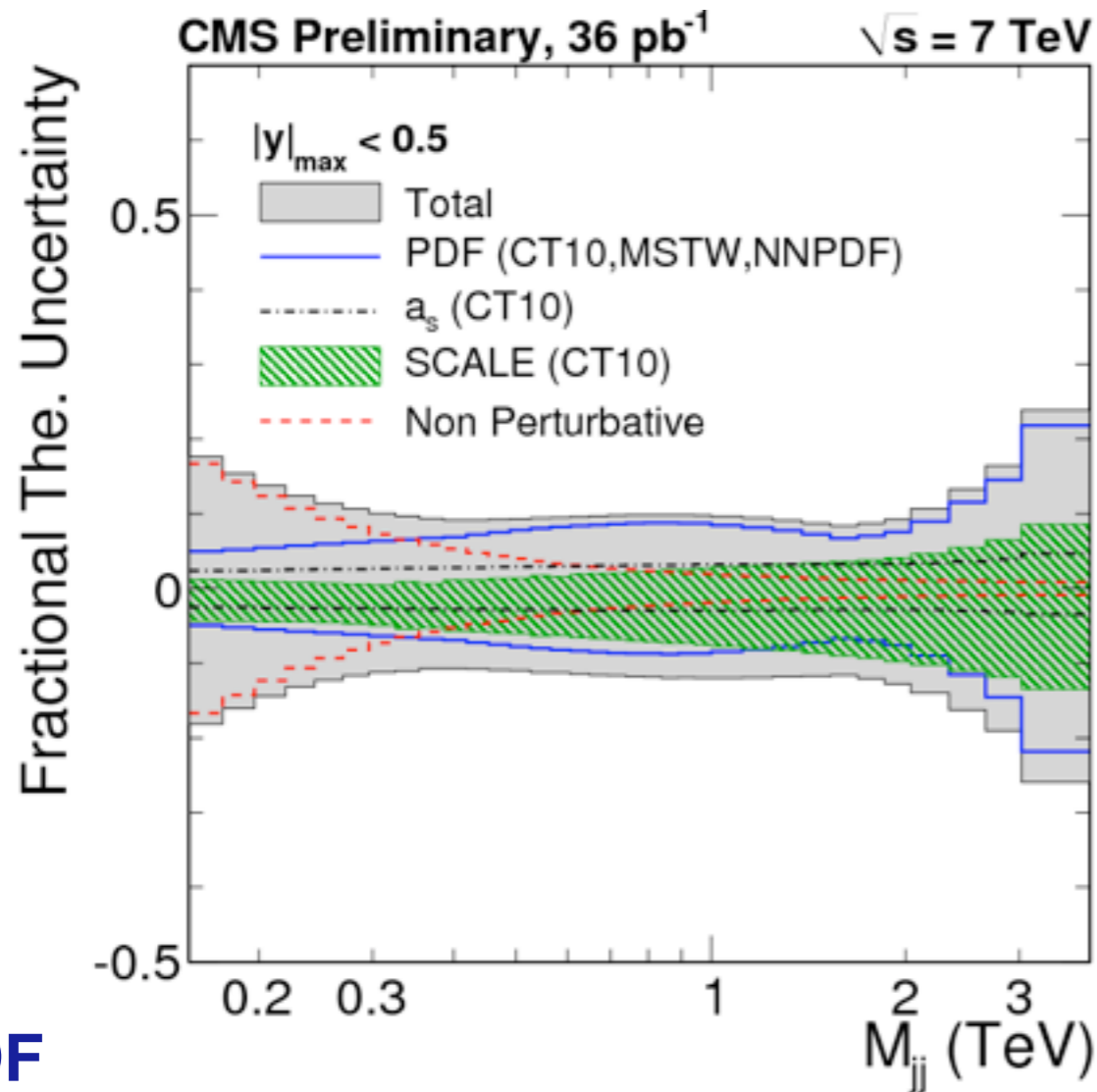


◆ JES dominates

- falling spectrum: 1% JES uncertainty corresponds to 5-10% cross-section unc.

◆ Resolution enters through unsmearing

- up to 2-3%



◆ PDF

- follow PDF4LHC prescription

◆ scale ($\mu_R = \mu_F = \langle p_T \rangle$)

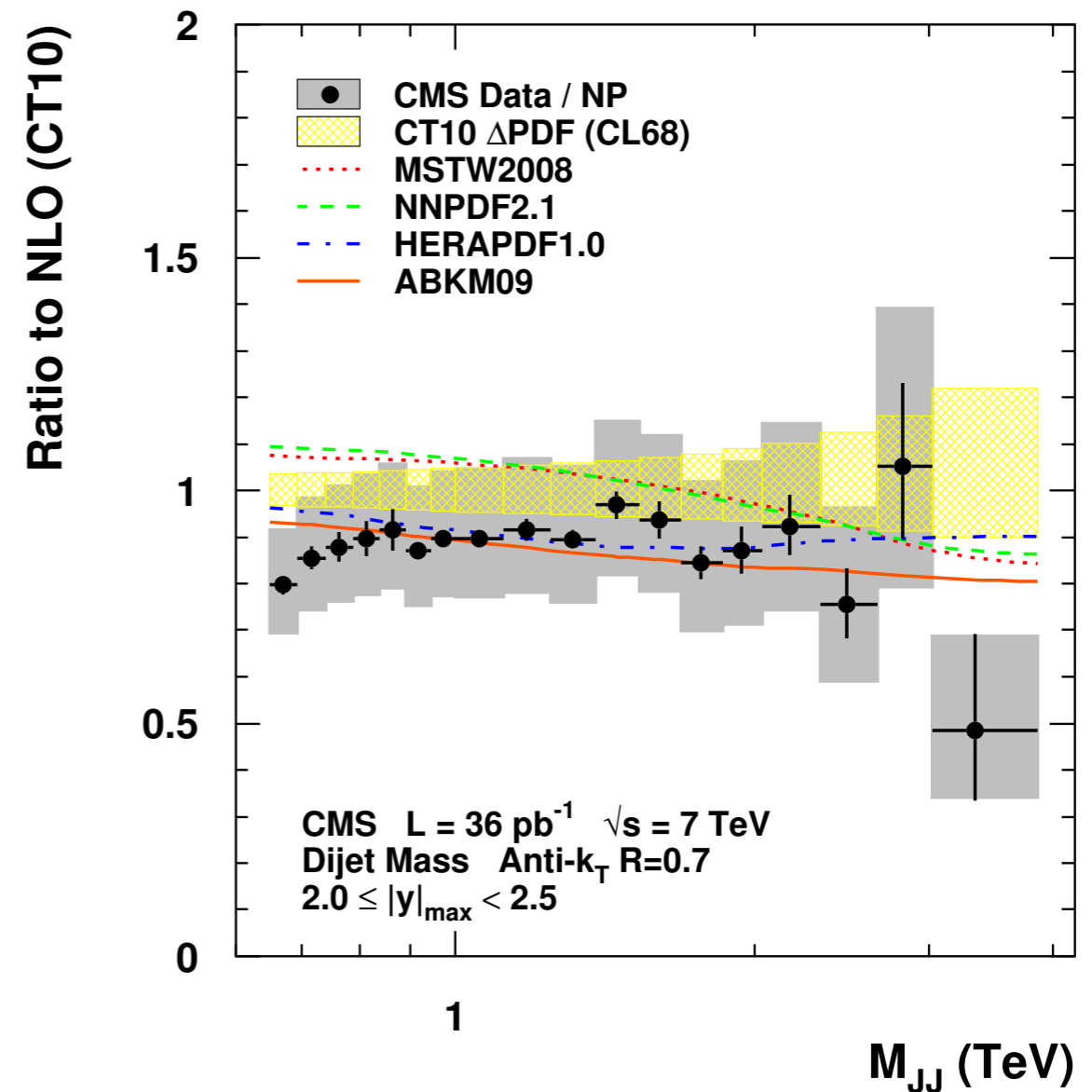
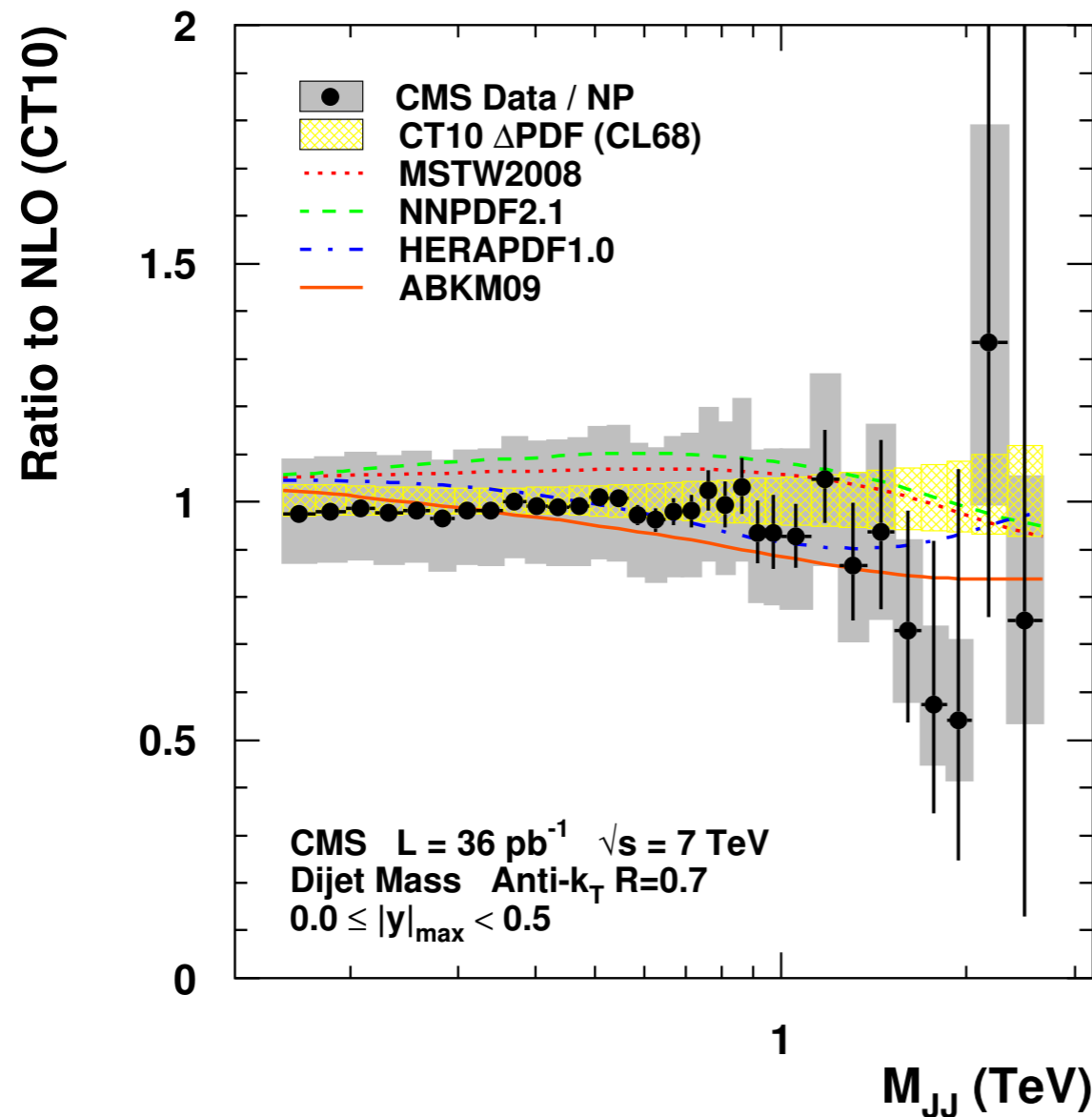
- 6 point variation: $(\mu_R/\langle p_T \rangle, \mu_F/\langle p_T \rangle) = (0.5, 0.5) \dots (1, 2)$

◆ $\Delta a_s = \pm 0.002$ (CT10)

◆ NP correction

- estimated with Pythia6 and Herwig++
- dominant uncertainty at low masses

PDF Comparisons

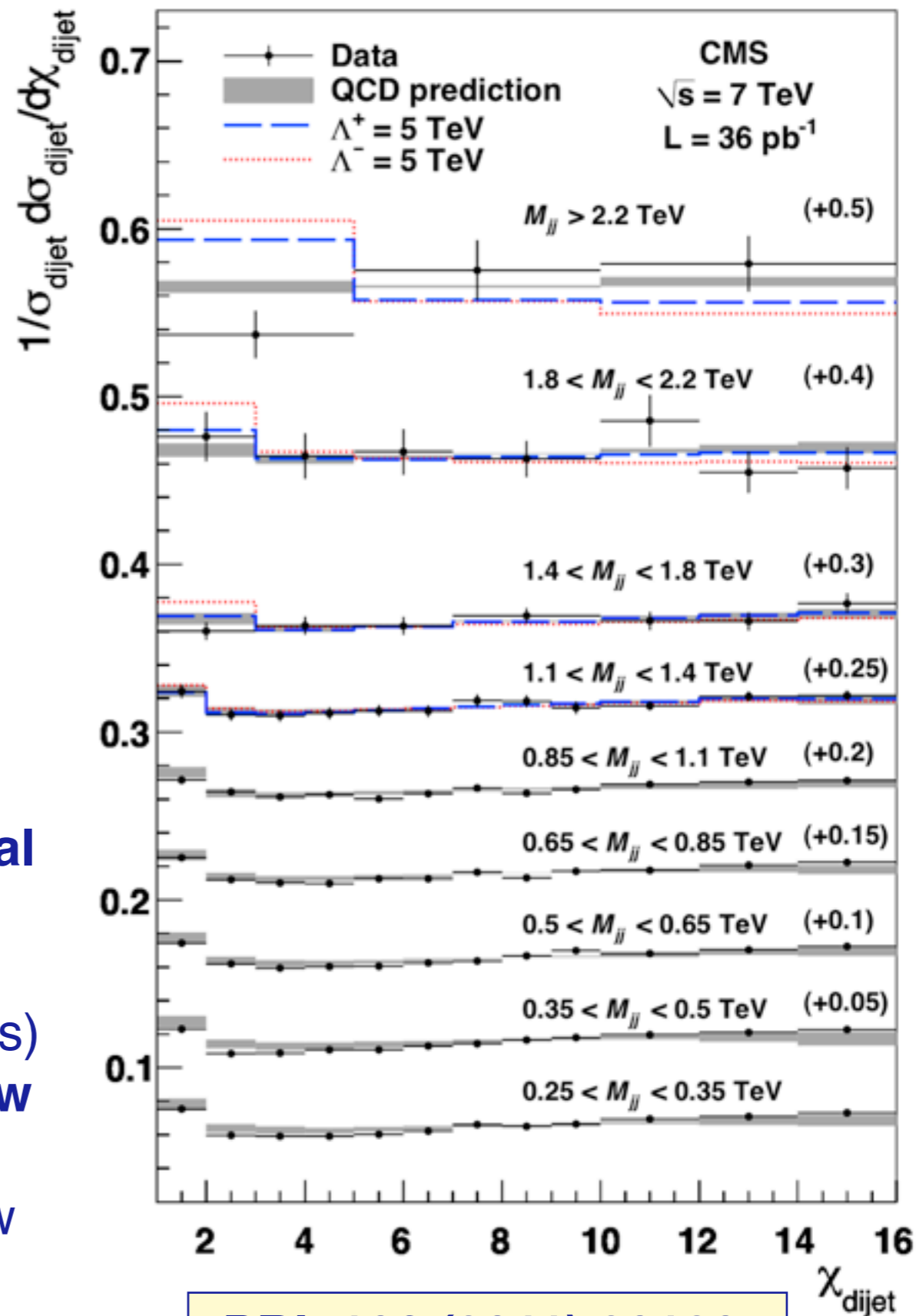
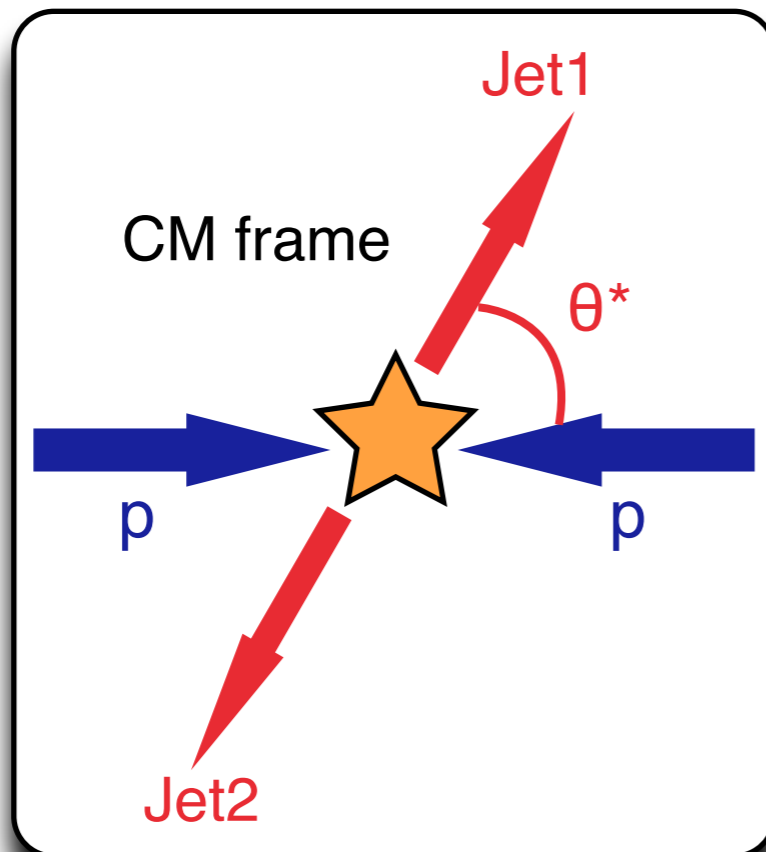


◆ Comparison to various PDF sets

- good agreement with all PDFs in the central rapidity bins
- agreement with CT10, MSTW2008, NNPDF2.1 worsens in the outer rapidity bins but improves for HERAPDF1.0 and ABKM09

Dijet Angular Distributions

$$\chi = e^{|y_1 - y_2|} \approx \frac{1 + |\cos \theta^*|}{1 - |\cos \theta^*|}$$



◆ The dijet angular distributions give additional insight to the QCD dynamics

- parton-parton scattering in QCD is *t-channel* dominated (Rutherford scattering at small angles)

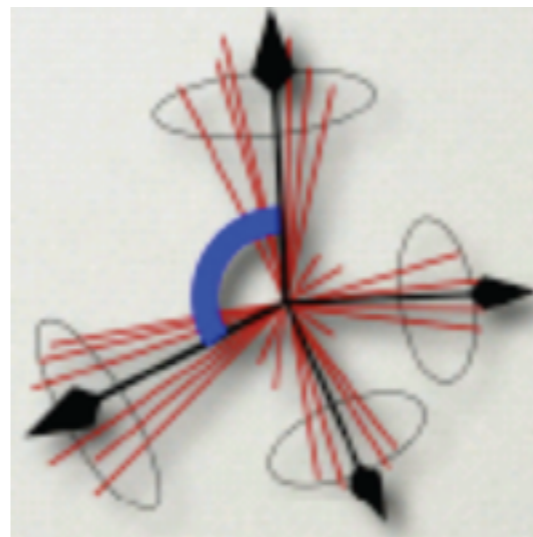
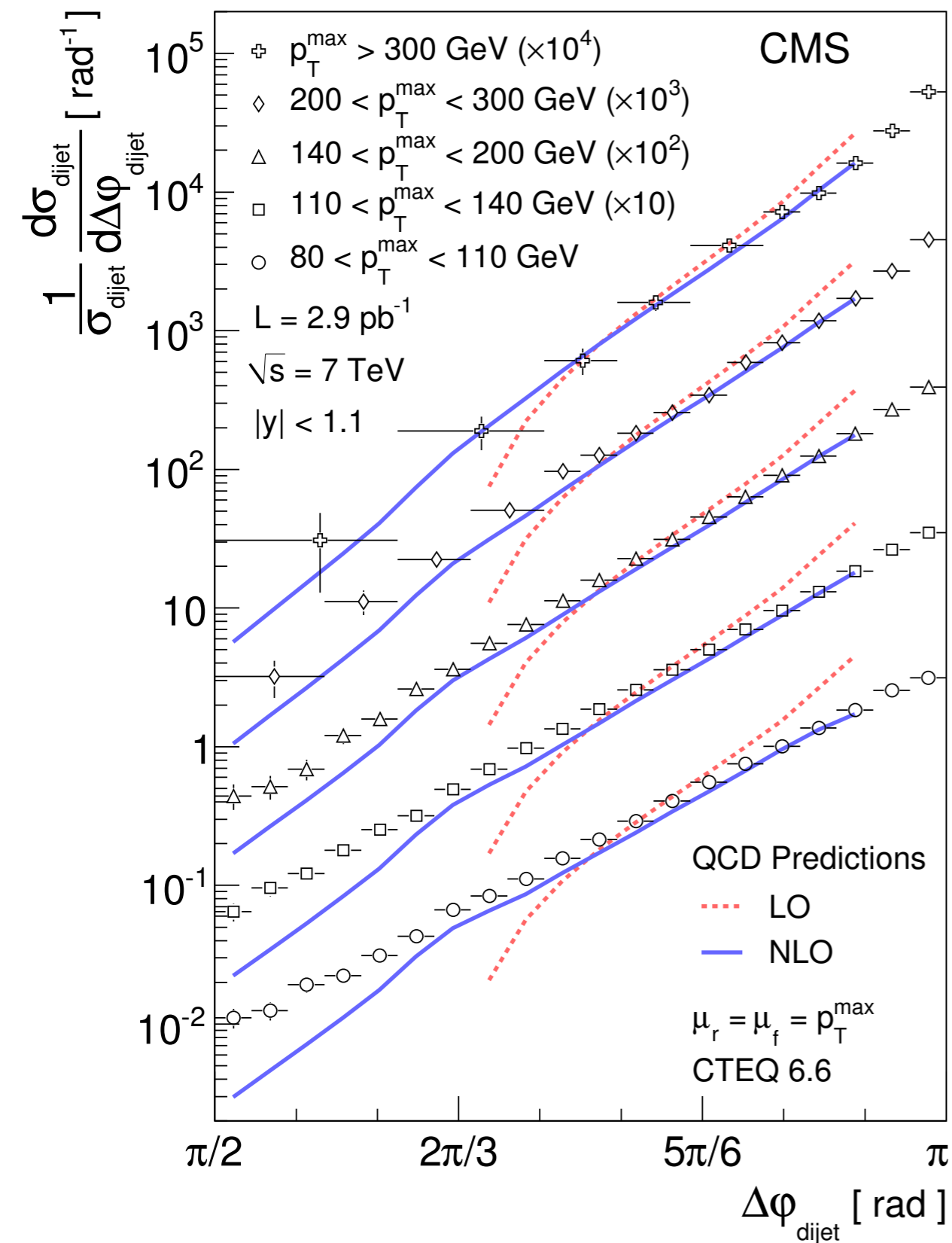
◆ Stringent test of pQCD and sensitivity to New Physics

- contact interactions or resonances would show deviation from QCD at large scattering angles

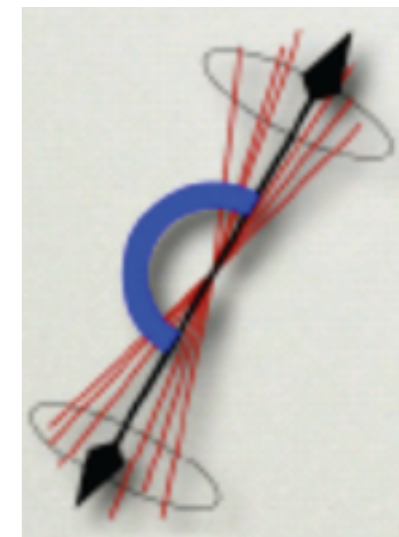
PRL 106 (2011) 201804



Dijet $\Delta\phi$ Distributions (vs NLO)



$$\Delta\phi \sim \frac{\pi}{2}$$

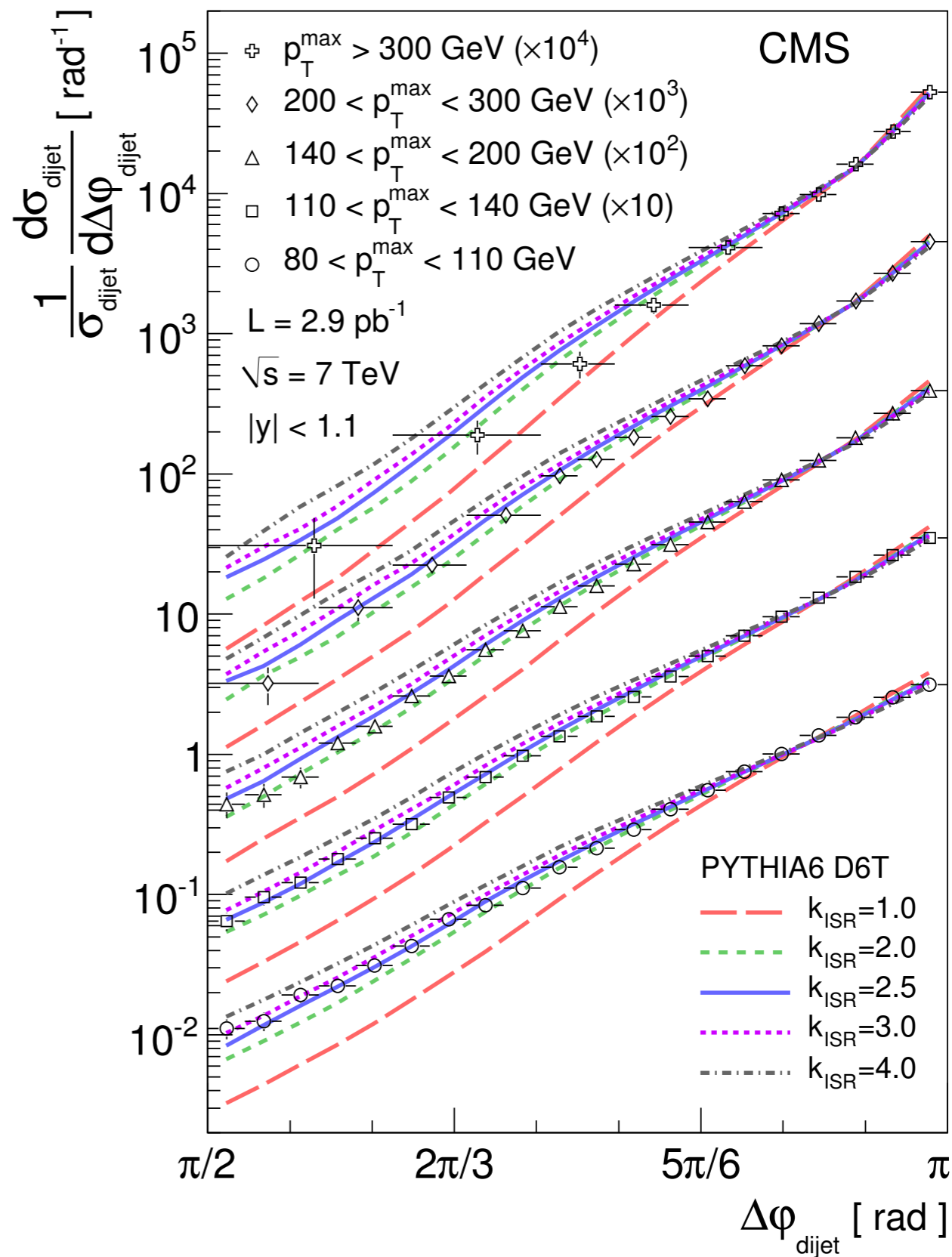
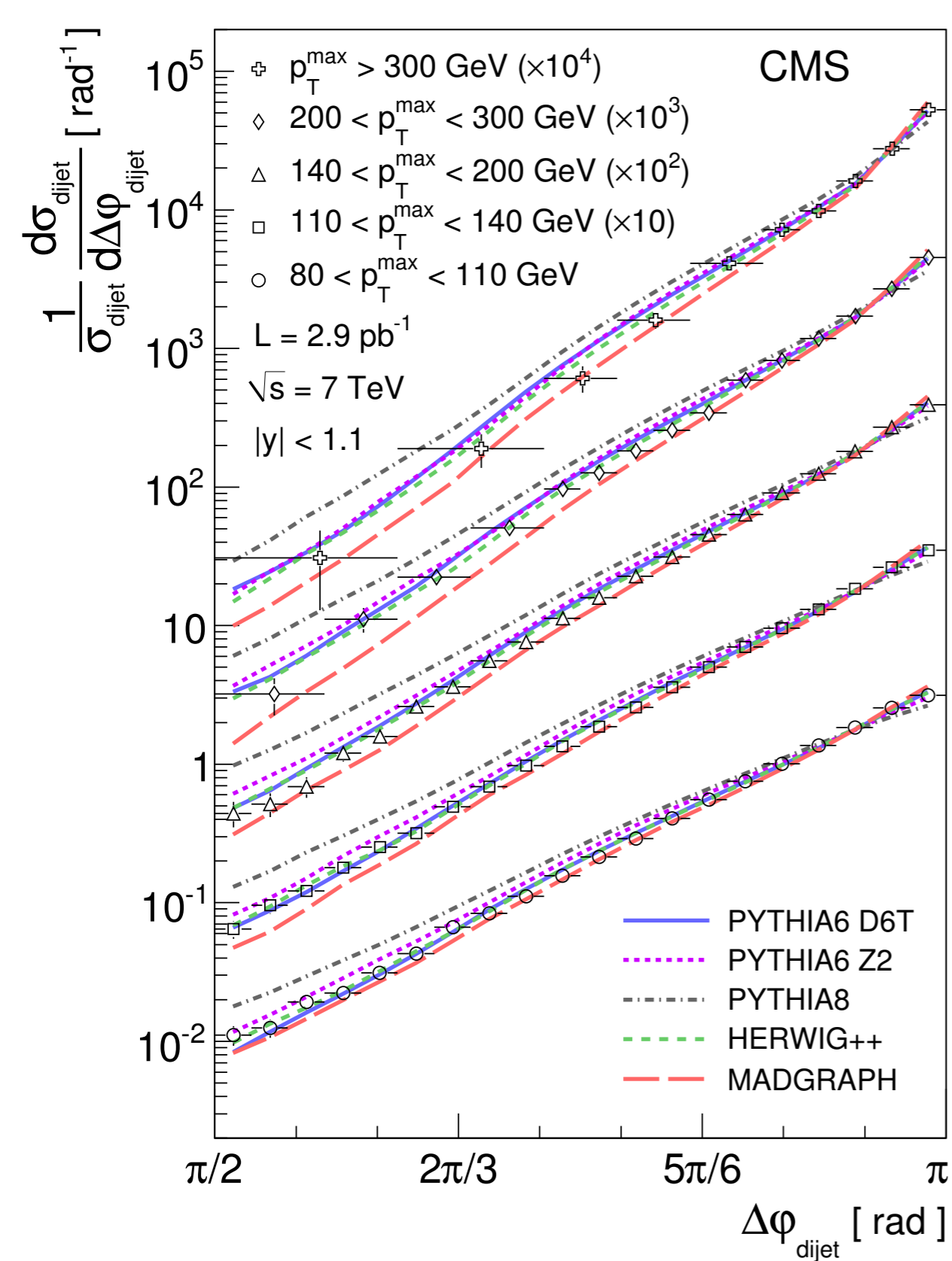


$$\Delta\phi \sim \pi$$

- ◆ **Normalized dijet cross section, as a function of $\Delta\phi$**
 - indirect probe of multijet topologies, without explicit reconstruction of additional jets
- ◆ **pQCD @ NLO is necessary to describe the azimuthal decorrelation**

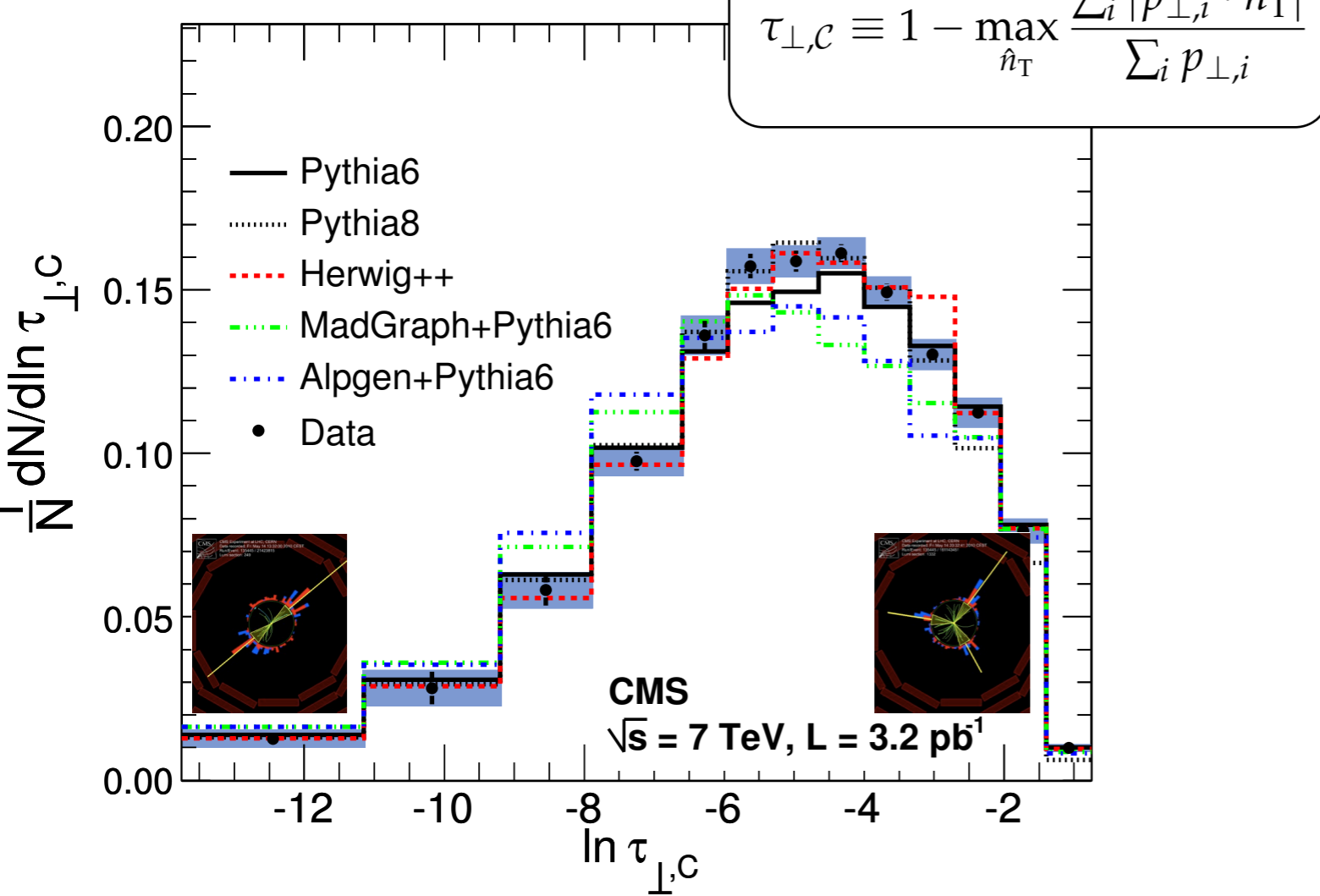
PRL 106 (2011) 122003

Dijet $\Delta\phi$ Distributions (vs MC generators)



Hadronic Event Shapes

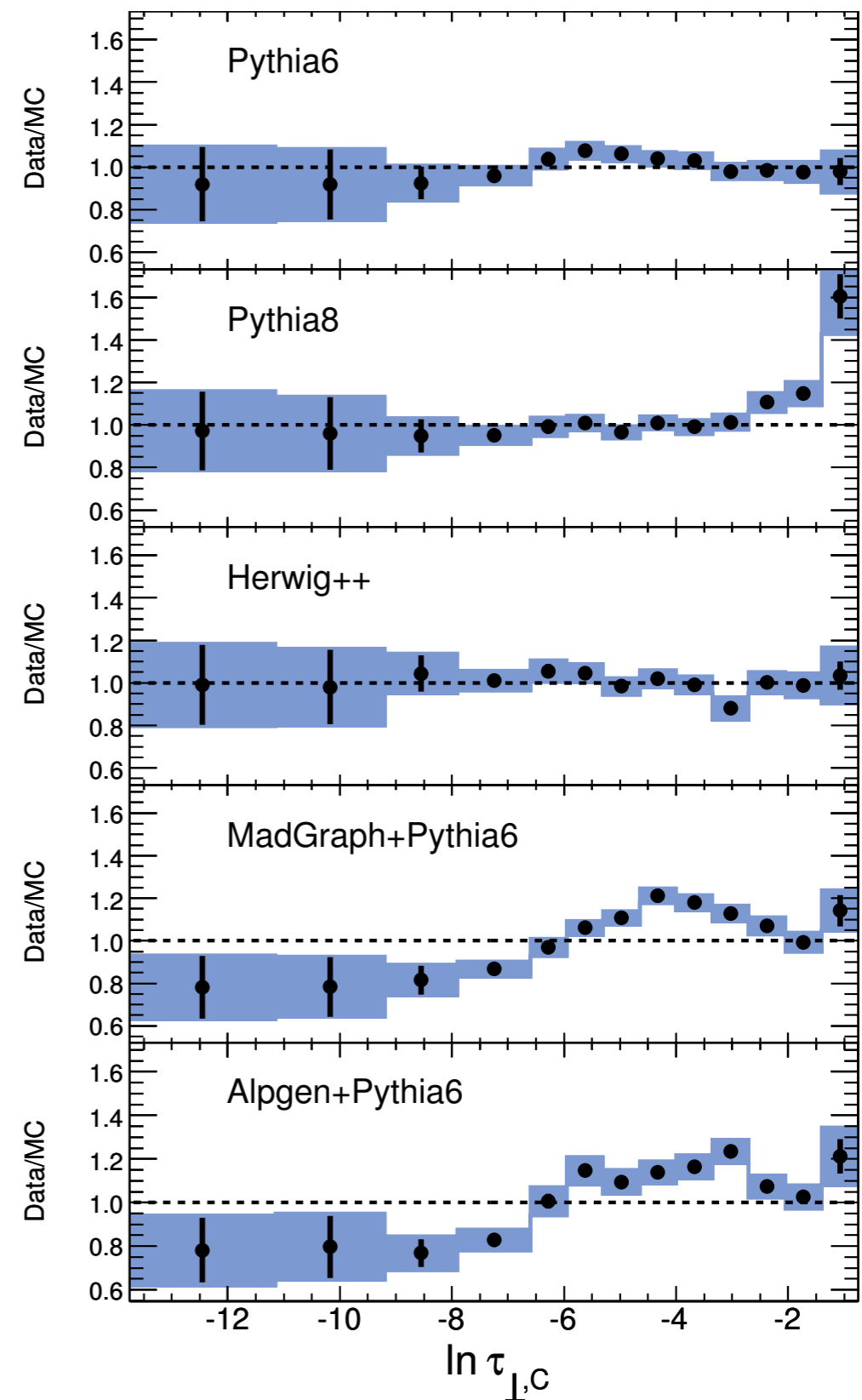
Central Transverse Thrust



◆ Event-shape variables

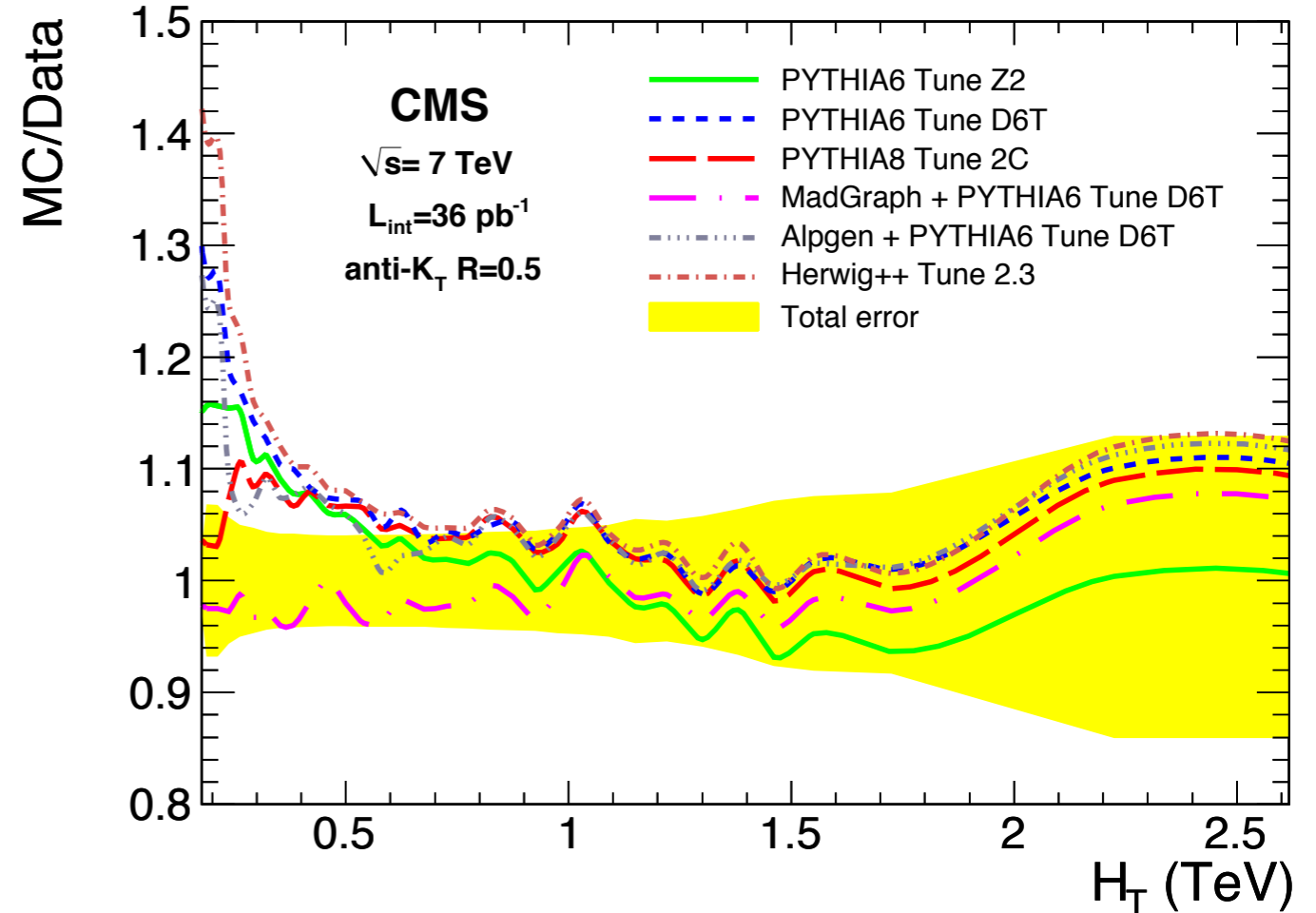
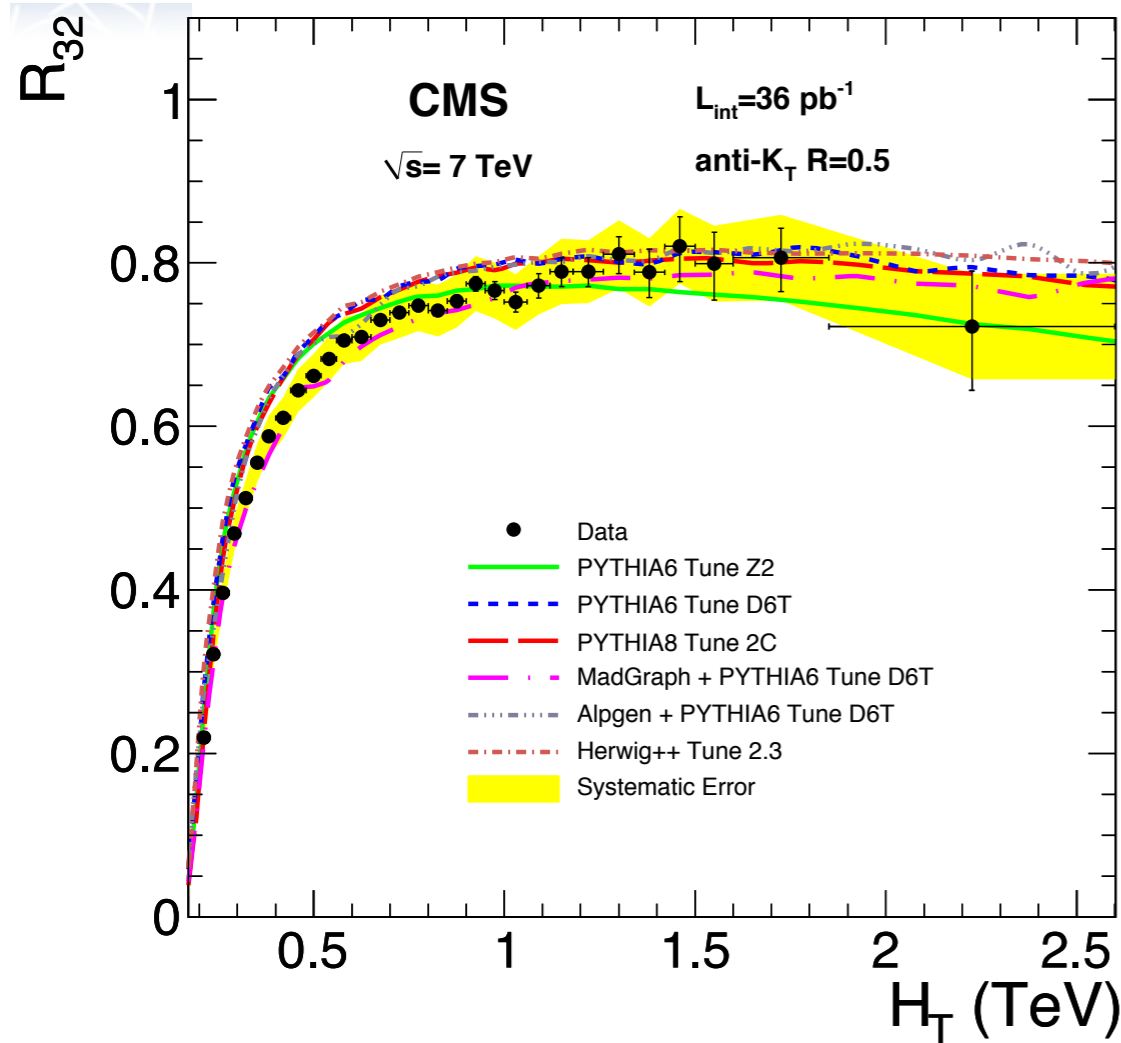
- central transverse thrust
- measured in bins of the leading jet p_T
- probe QCD radiative processes
- sensitive to 2j and 3j topologies

◆ Sensitive to the MC generator modeling



PLB 699 (2011) 48

3j/2j Cross-Section Ratio



$$R_{3/2} = \sigma_{3\text{-jet}} / \sigma_{2\text{-jet}} = \frac{\sum \text{3-jet diagrams} + \dots}{\sum \text{2-jet diagrams} + \dots}$$

◆ Ratio of cross sections (3j/2j), vs H_T

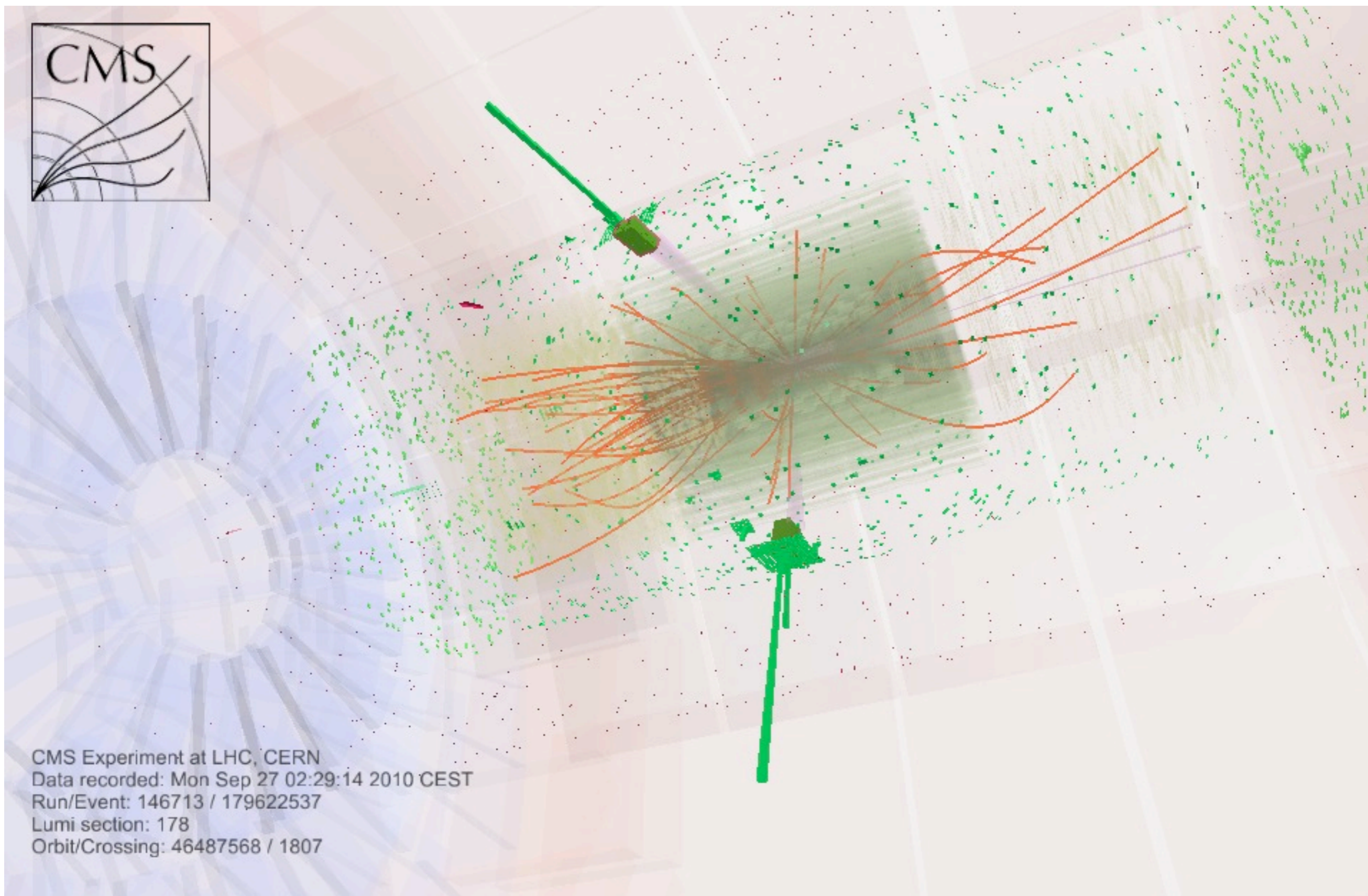
- insensitive to many experimental uncertainties
- the NLO calculation for the given setup is affected by large scale uncertainties
- can be used for the α_s measurement (in a different setup)

◆ Comparison to QCD MC generators

- all generators agree for $H_T > 0.7 \text{ TeV}$ with some deviation at low values
- the ME predictions are sensitive to the choice of the jet p_T matching threshold

PLB 702 (2011) 336

Measurements with Photons

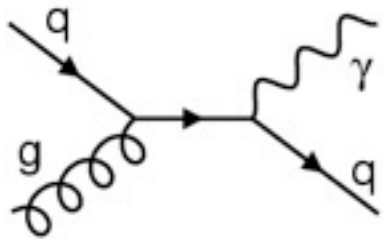


CMS Experiment at LHC, CERN
Data recorded: Mon Sep 27 02:29:14 2010 CEST
Run/Event: 146713 / 179622537
Lumi section: 178
Orbit/Crossing: 46487568 / 1807

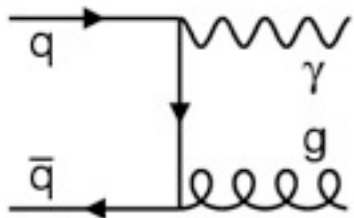


Direct Photon Production

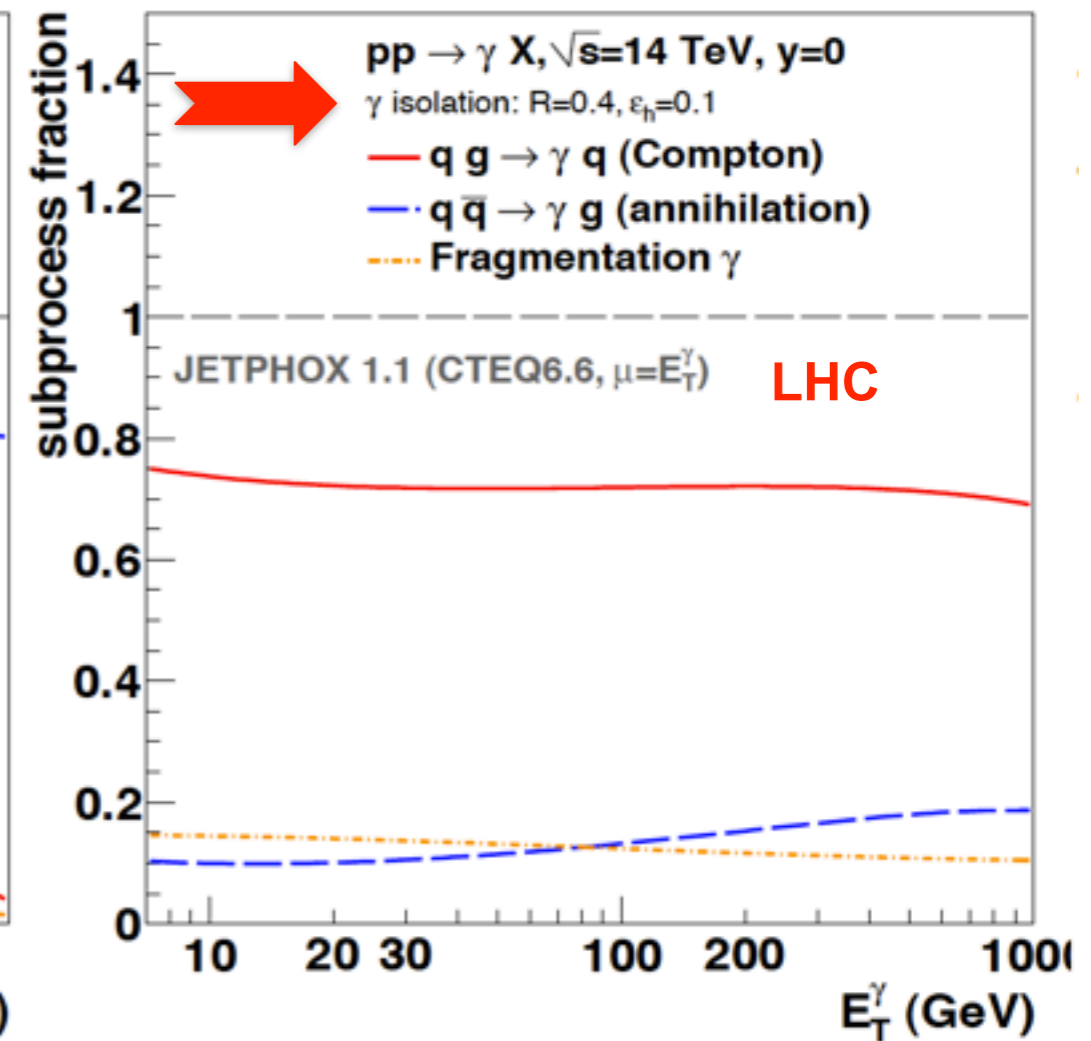
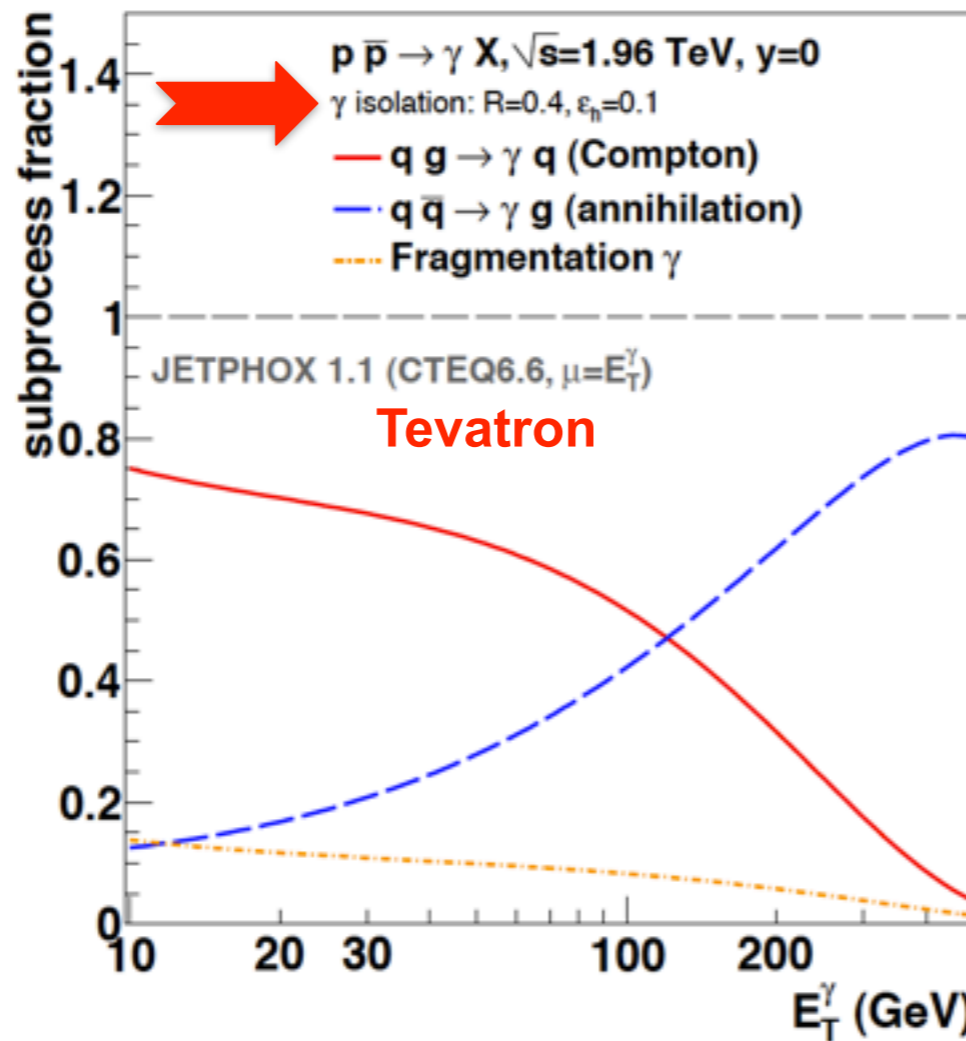
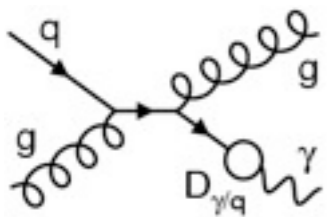
Compton



Annihilation



Fragmentation



◆ Production mechanisms

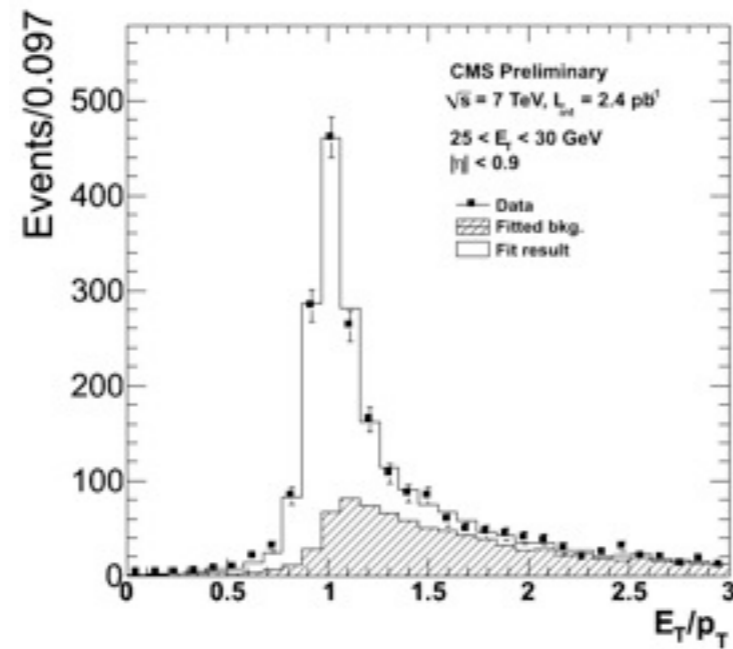
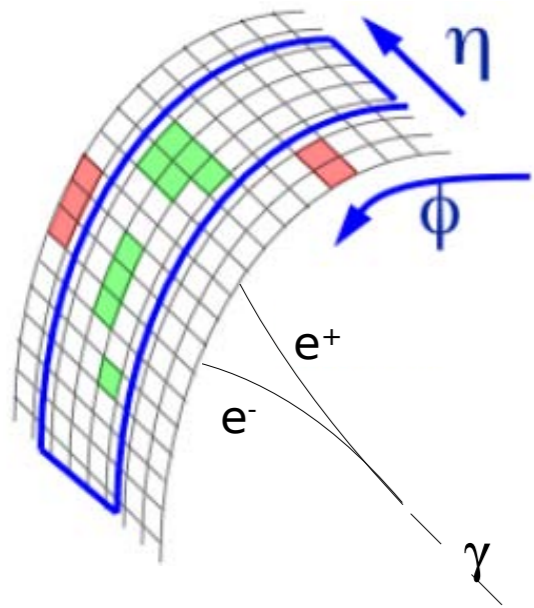
- quark-gluon Compton scattering (dominant at LHC)
- quark-antiquark annihilation
- fragmentation of colored partons (greatly suppressed by isolation requirements)

◆ Test of pQCD

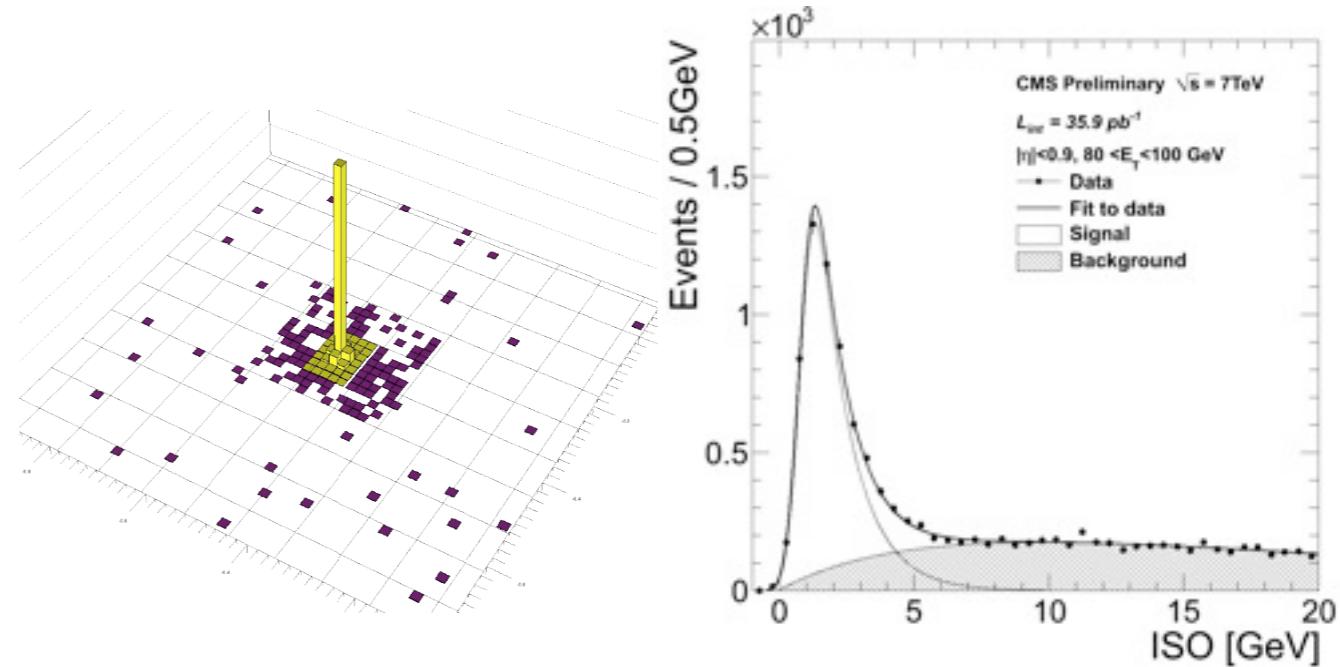
- NLO calculations
- sensitive to gluon PDF

Photon Signal Extraction

Conversion



Combined Isolation Template



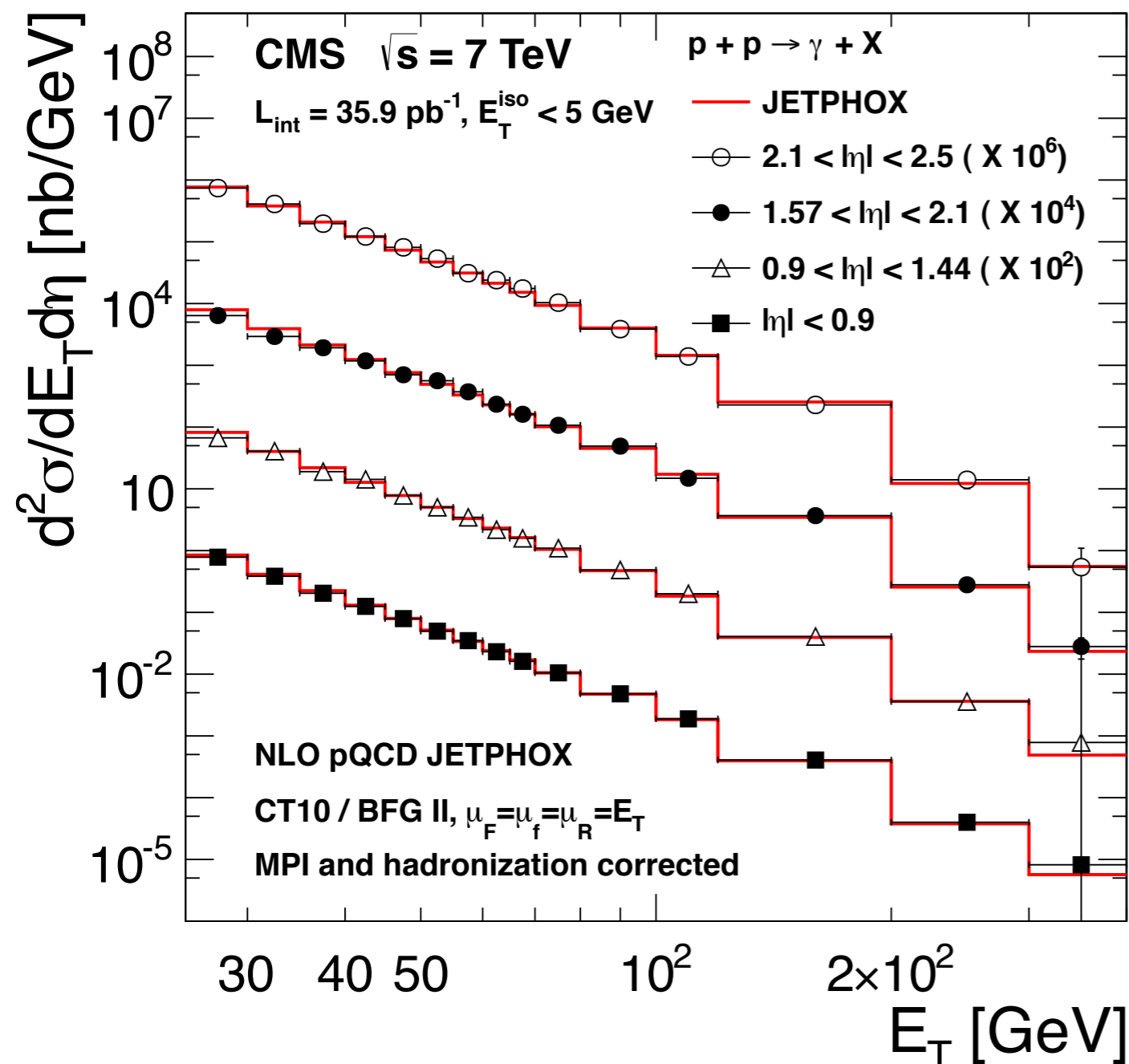
◆ Reconstruction

- photon candidates based on identification & isolation preselection criteria
- quality requirements on the converted photon candidates

◆ Signal yield

- photon candidates contaminated by decays of energetic neutral mesons
- signal extracted statistically
- conversion template ($E_{T,ECAL}/p_{T,trk}$ variable)
- isolation template ($ISO = ISO_{TRK} + ISO_{ECAL} + ISO_{HCAL}$ variable)

Isolated Prompt Photon Cross Section



◆ Differential isolated prompt photon cross section

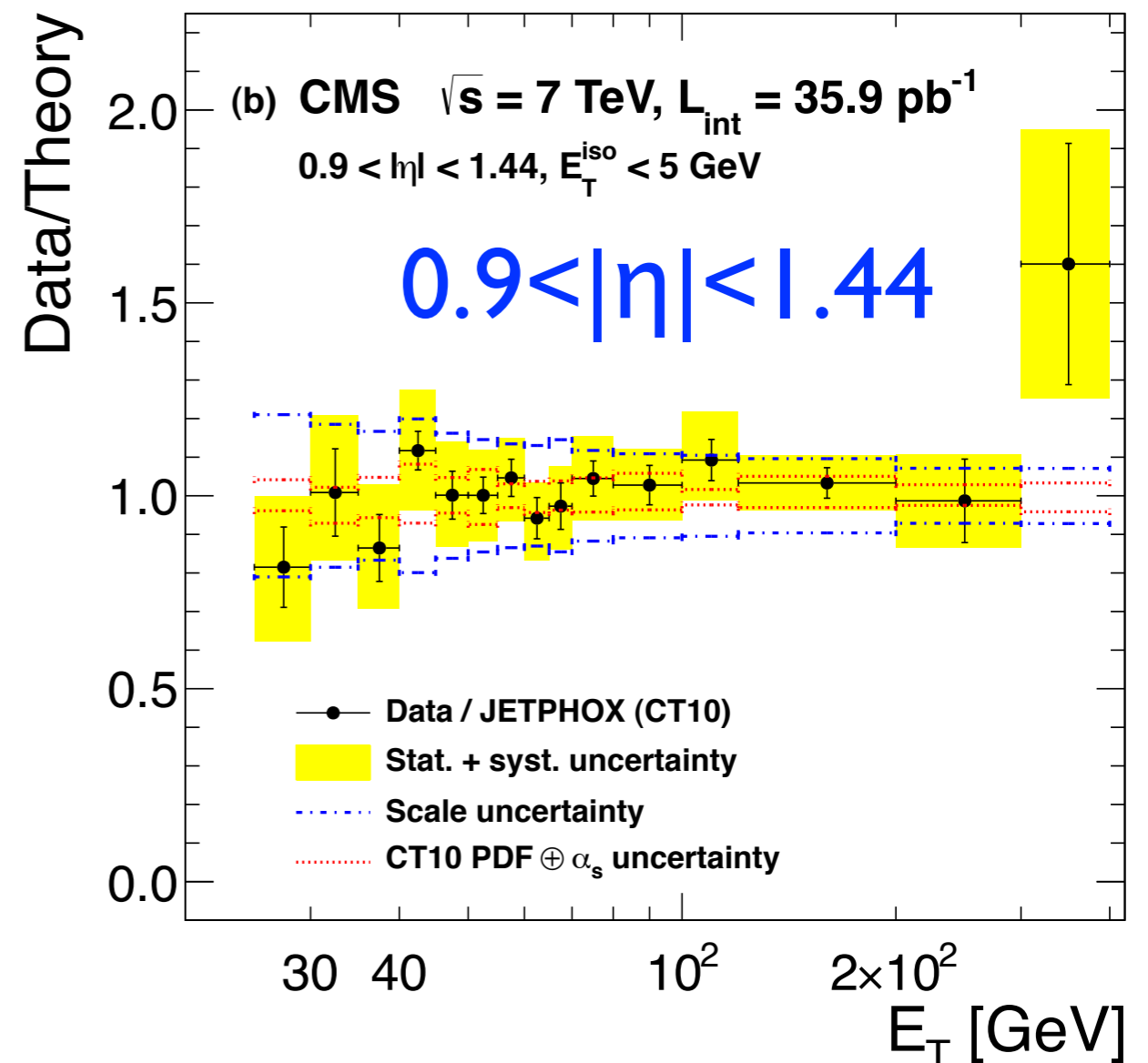
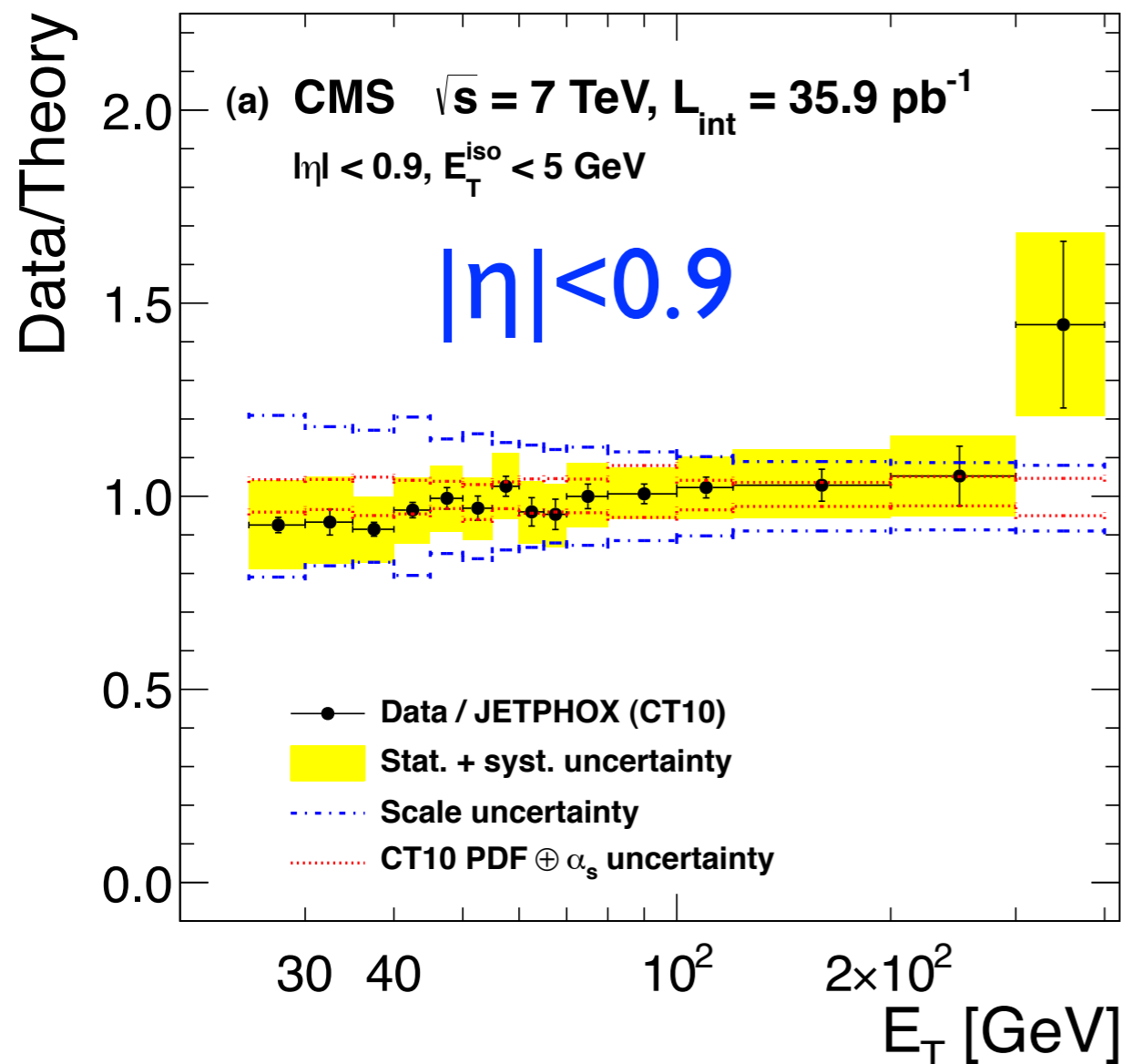
- combination of conversion and isolation template methods
- measurement from 25 GeV to 400 GeV in E_T and up to $|\eta| = 2.5$
- bin-by-bin unfolding

◆ Theory prediction

- isolation: $E_T < 5 \text{ GeV}$ in $R < 0.4$
- JETPHOX
- CT10 PDF & BFG II fragmentation functions
- $\mu_R = \mu_F = \mu_f = E_T$
- NP correction = 0.975

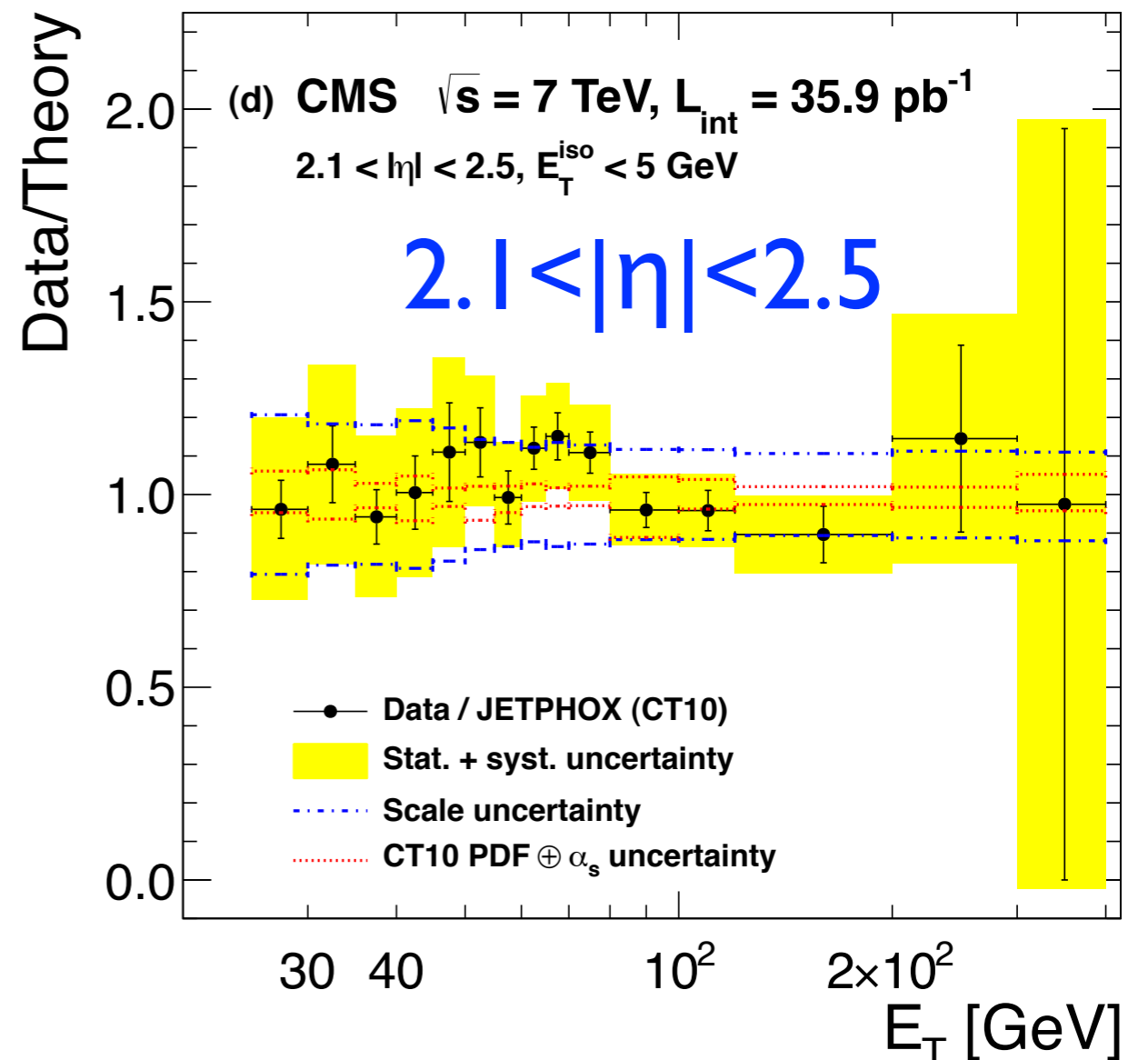
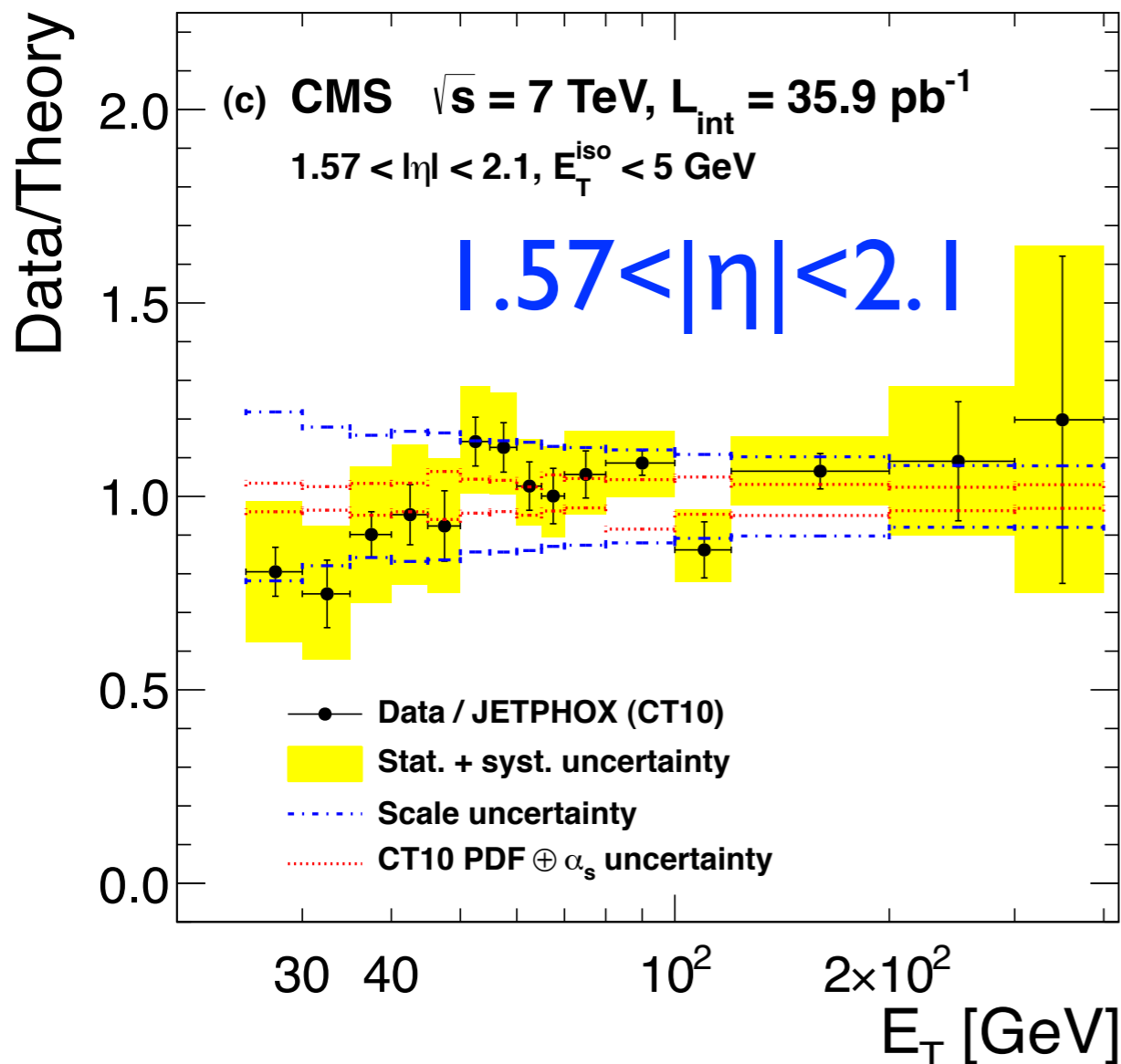
PRD 84 (2011) 052011

Comparison to Theory (I)



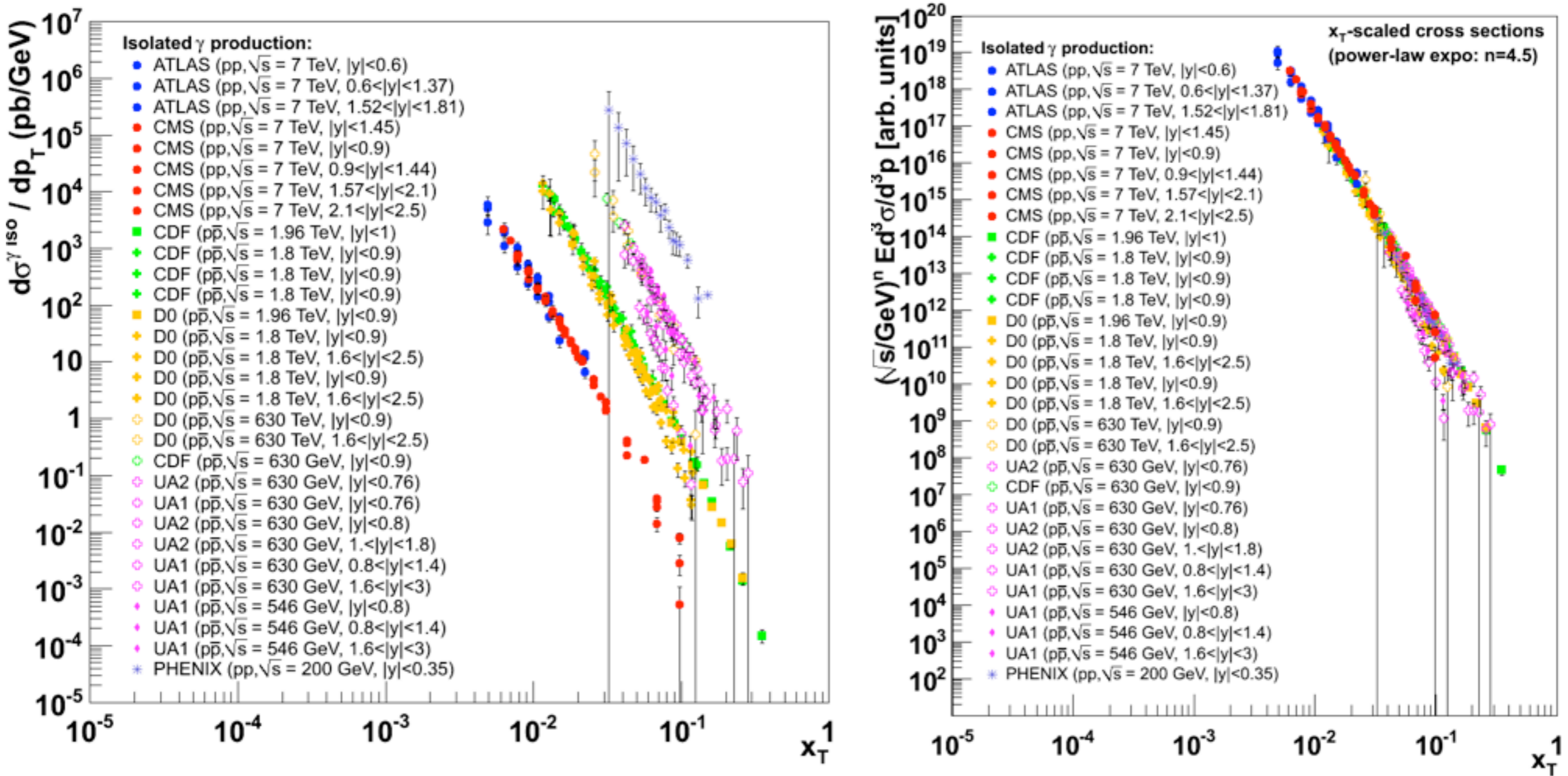
- ◆ **Good agreement with the theory**
 - scale uncertainty dominates the theoretical prediction
- ◆ **Overestimated cross section at low E_T**
 - different trend than the one observed at Tevatron

Comparison to Theory (II)



- ◆ **Good agreement with the theory**
 - scale uncertainty dominates the theoretical prediction
- ◆ **Overestimated cross section at low E_T**
 - different trend than the one observed at Tevatron

Isolated Prompt Photons: the Big Picture



There exists a large number of photon measurements that could be used to constrain directly the gluon PDF

Di-photon Production

Direct Born

26 pb @ NLO

One Fragmentation

$\mu_{\text{frag}} = m_{\gamma\gamma}$

10 pb @ NLO

DIPHOX

Two Fragmentation

0.5 pb @ NLO

Direct Box

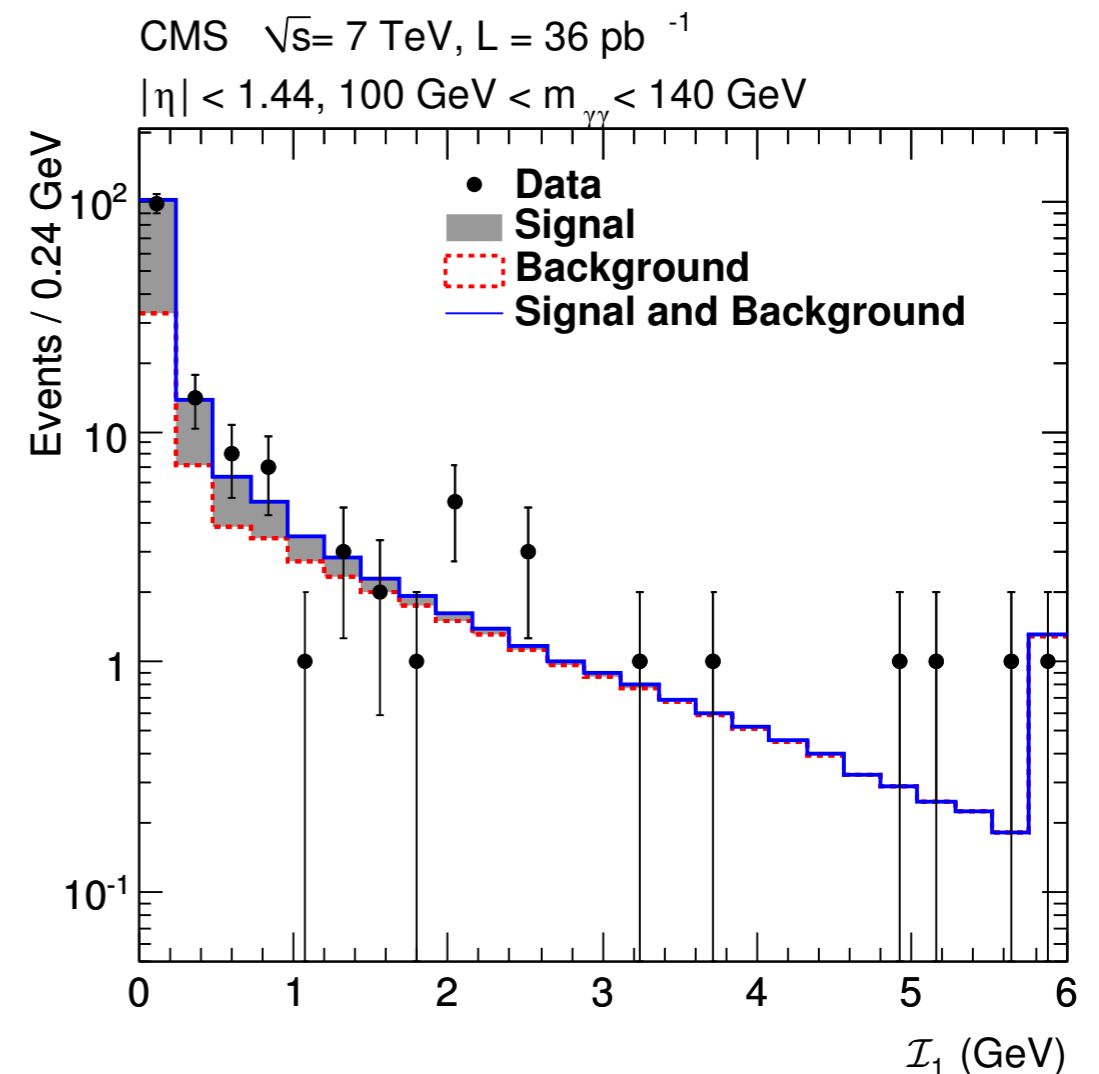
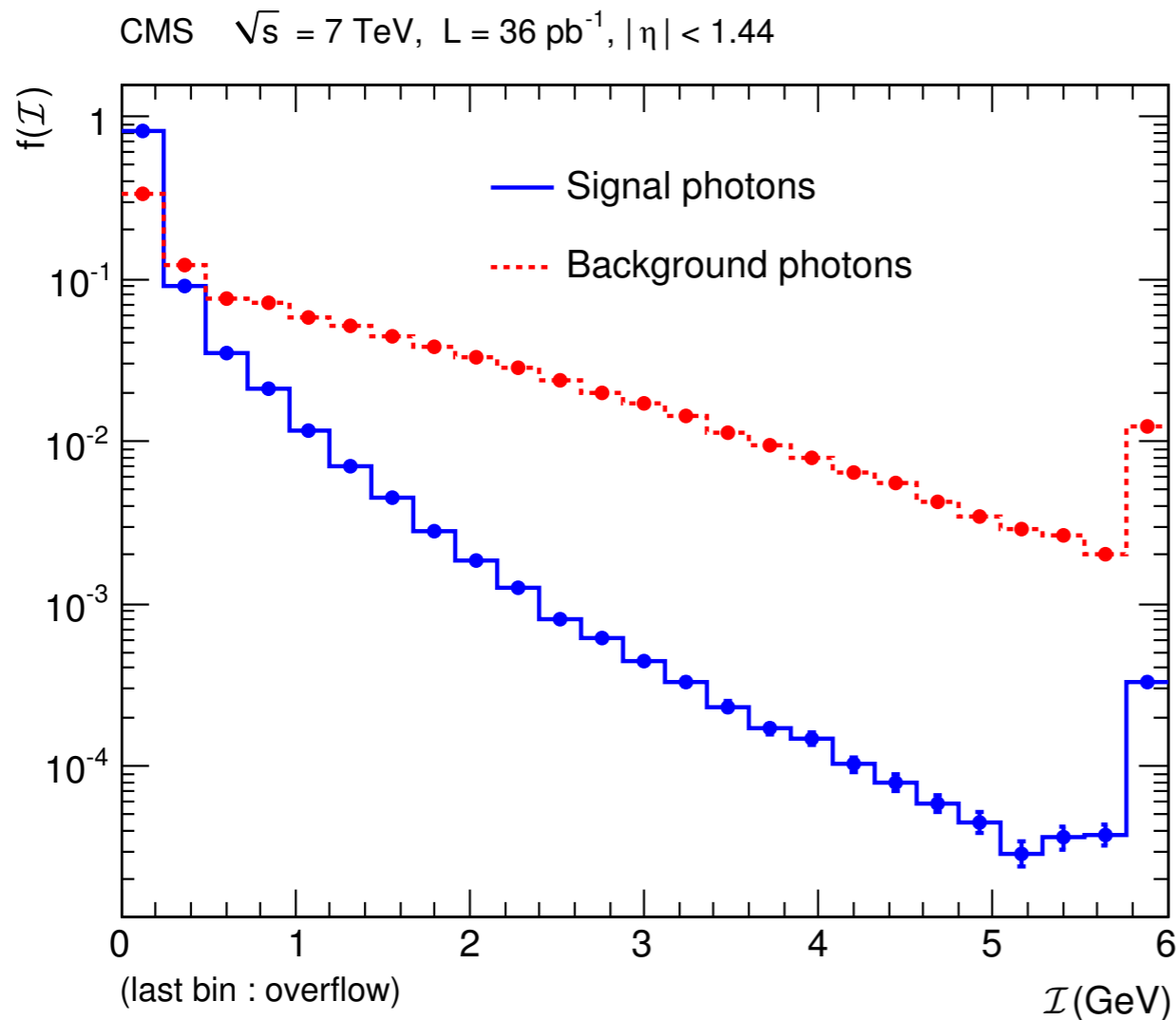
15 pb @ NLO

GAMMA2MC

The sub-process cross sections refer to the CMS measurement acceptance

- ◆ **Probing pQCD**
 - NLO calculations
 - PDF
- ◆ **Irreducible background for the $H \rightarrow \gamma\gamma$ search**

Di-photon Signal Extraction



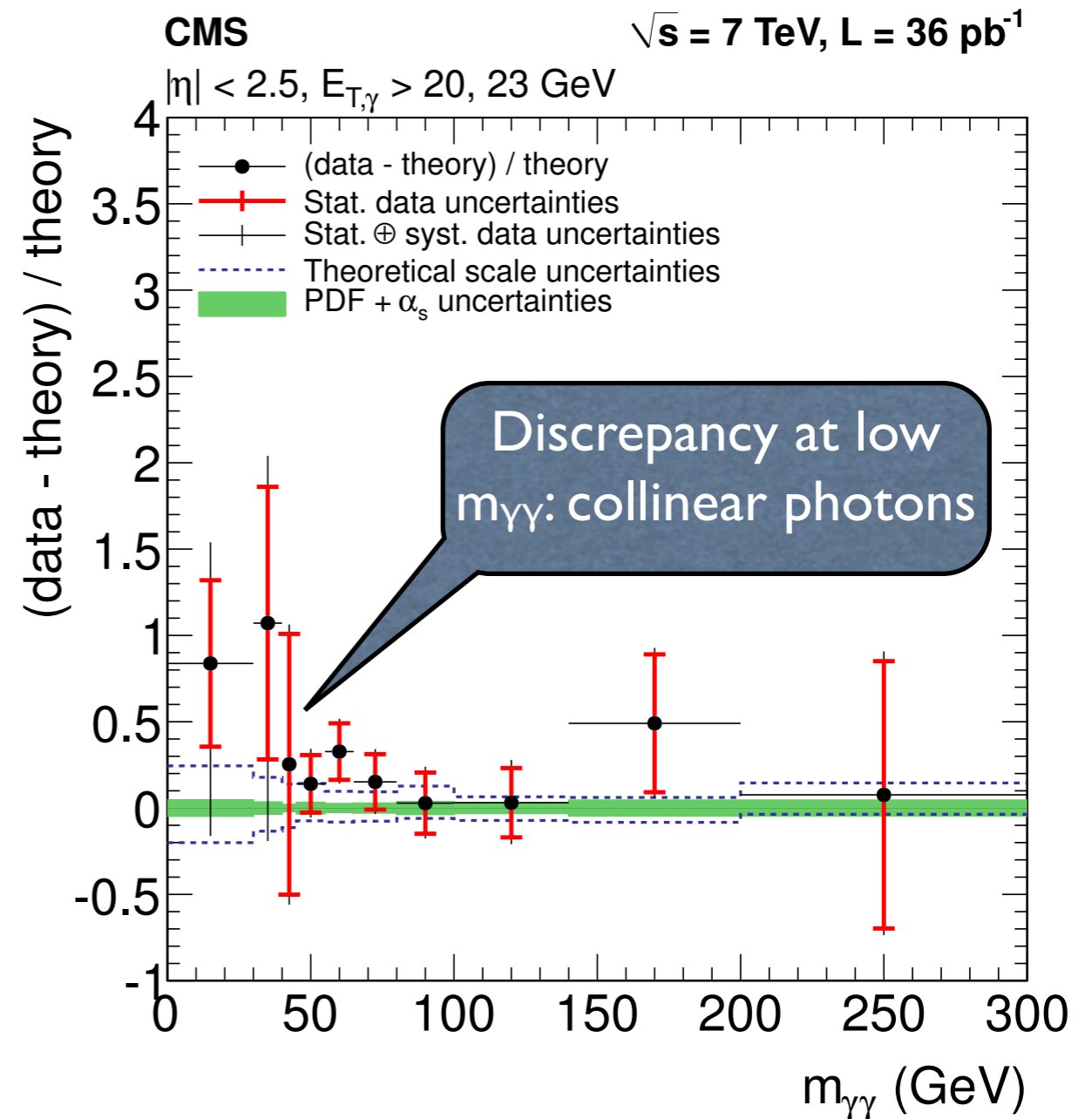
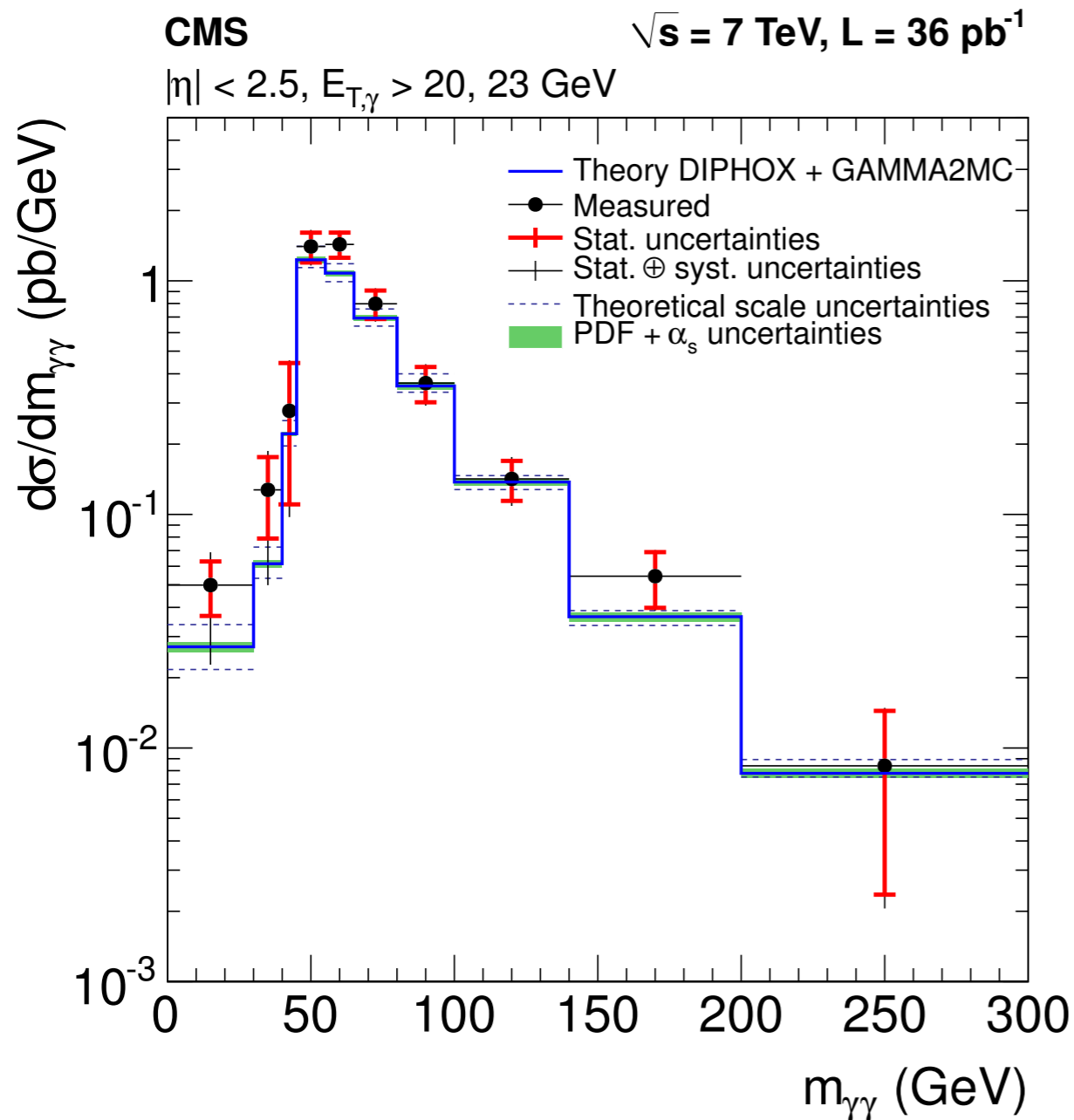
◆ Reconstruction

- photon candidates based on identification & isolation preselection criteria
- $E_{T,1} > 23 \text{ GeV}$, $E_{T,2} > 20 \text{ GeV}$, $R_{\gamma\gamma} > 0.45$ in η - ϕ ,

◆ Signal yield

- signal extracted statistically
- ECAL isolation template

Di-photon Cross Section (vs $m_{\gamma\gamma}$)



◆ Differential isolated prompt photon cross section

- response matrix inversion unfolding

◆ Theory prediction

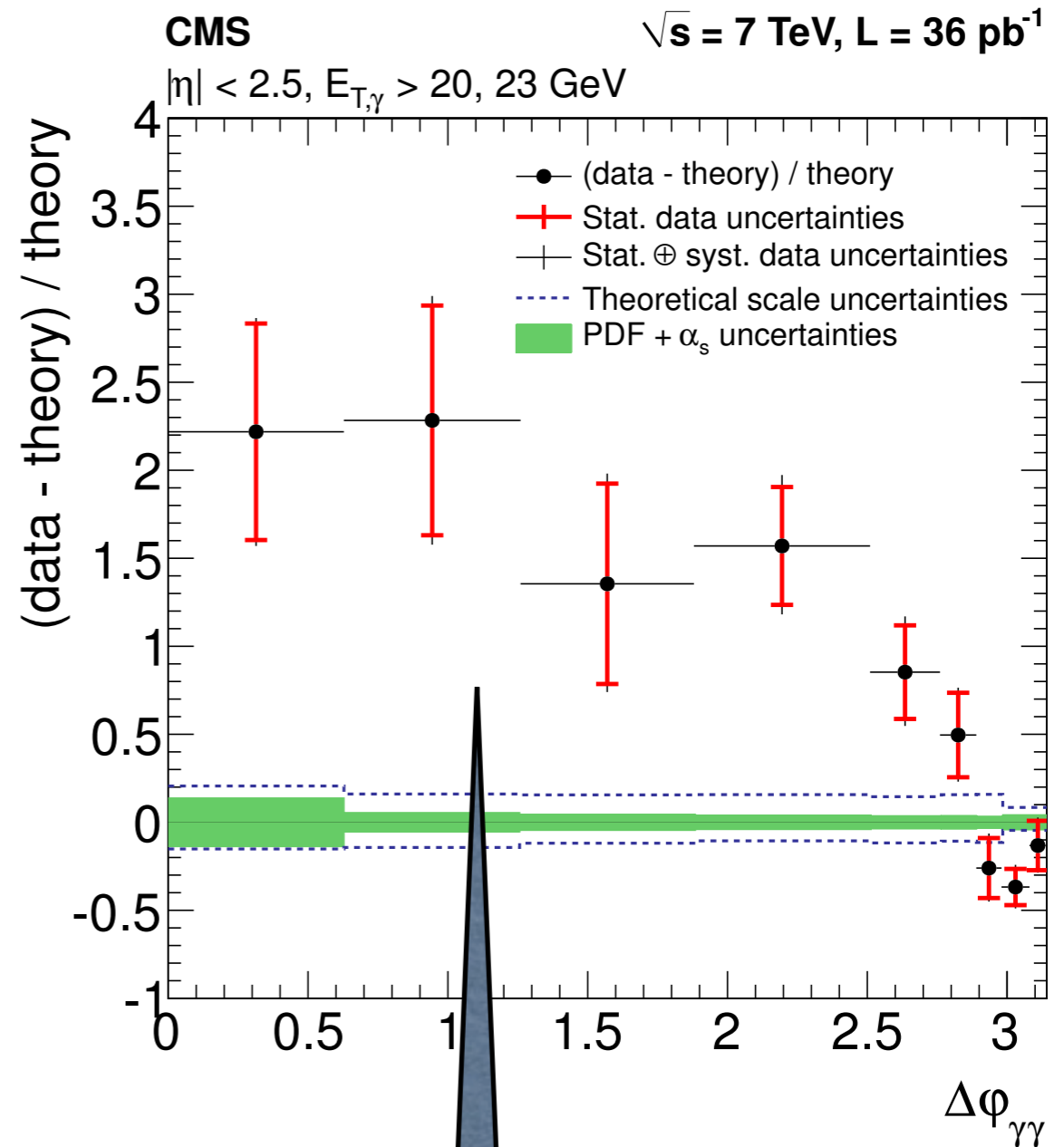
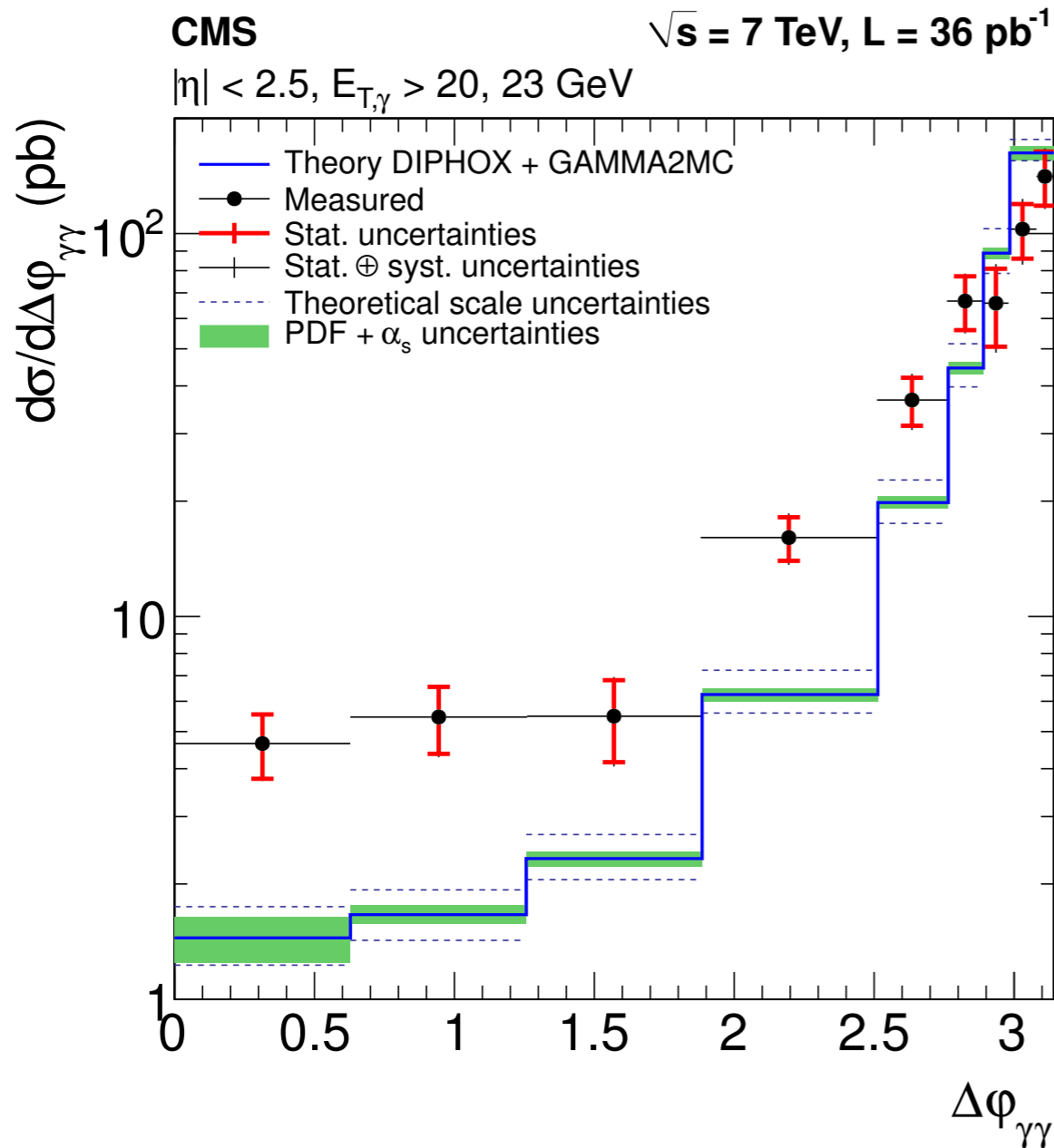
- isolation: $E_T < 5 \text{ GeV}$ in $R < 0.4$

- NP correction = 0.953

PDF4LHC
 $\mu_R = \mu_F = \mu_f = m_{\gamma\gamma}$

arXiv:1110.6461

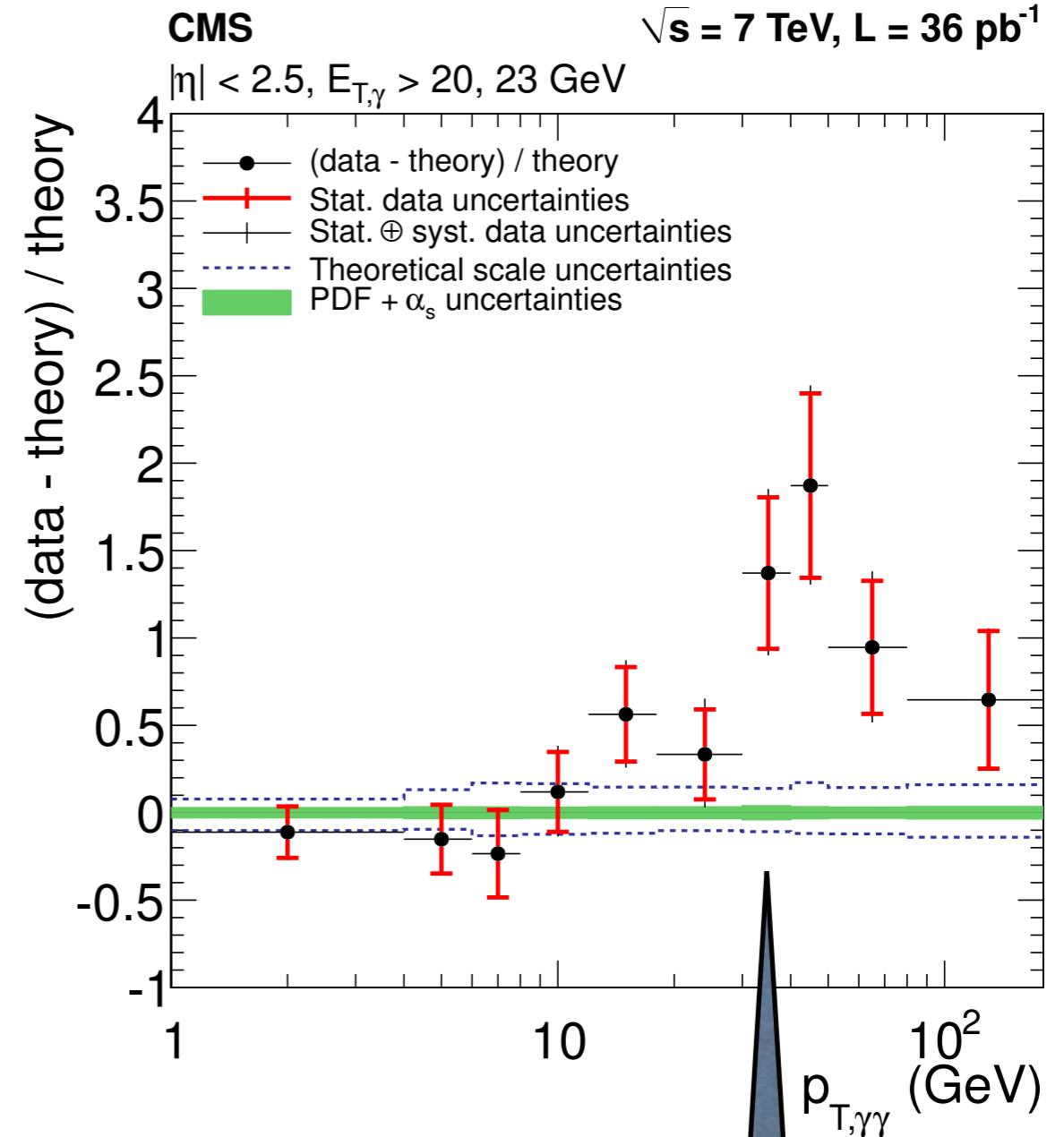
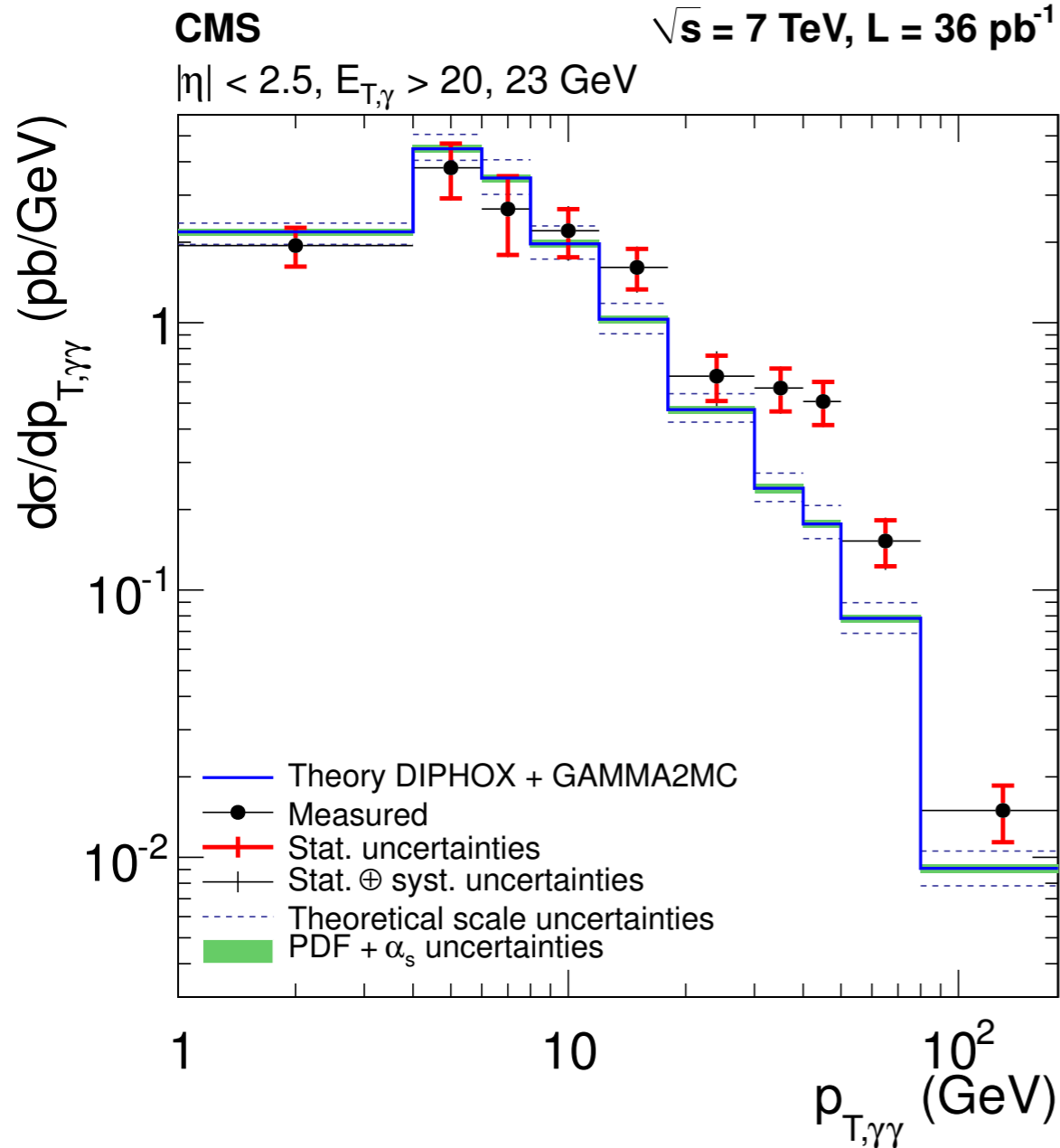
Di-photon Cross Section (vs $\Delta\phi_{\gamma\gamma}$)



- ◆ **Differential isolated prompt photon cross section**
 - response matrix inversion unfolding
- ◆ **Theory prediction**
 - isolation: $E_T < 5 \text{ GeV}$ in $R < 0.4$
 - NP correction = 0.953

Discrepancy at low $\Delta\phi_{\gamma\gamma}$: collinear photons

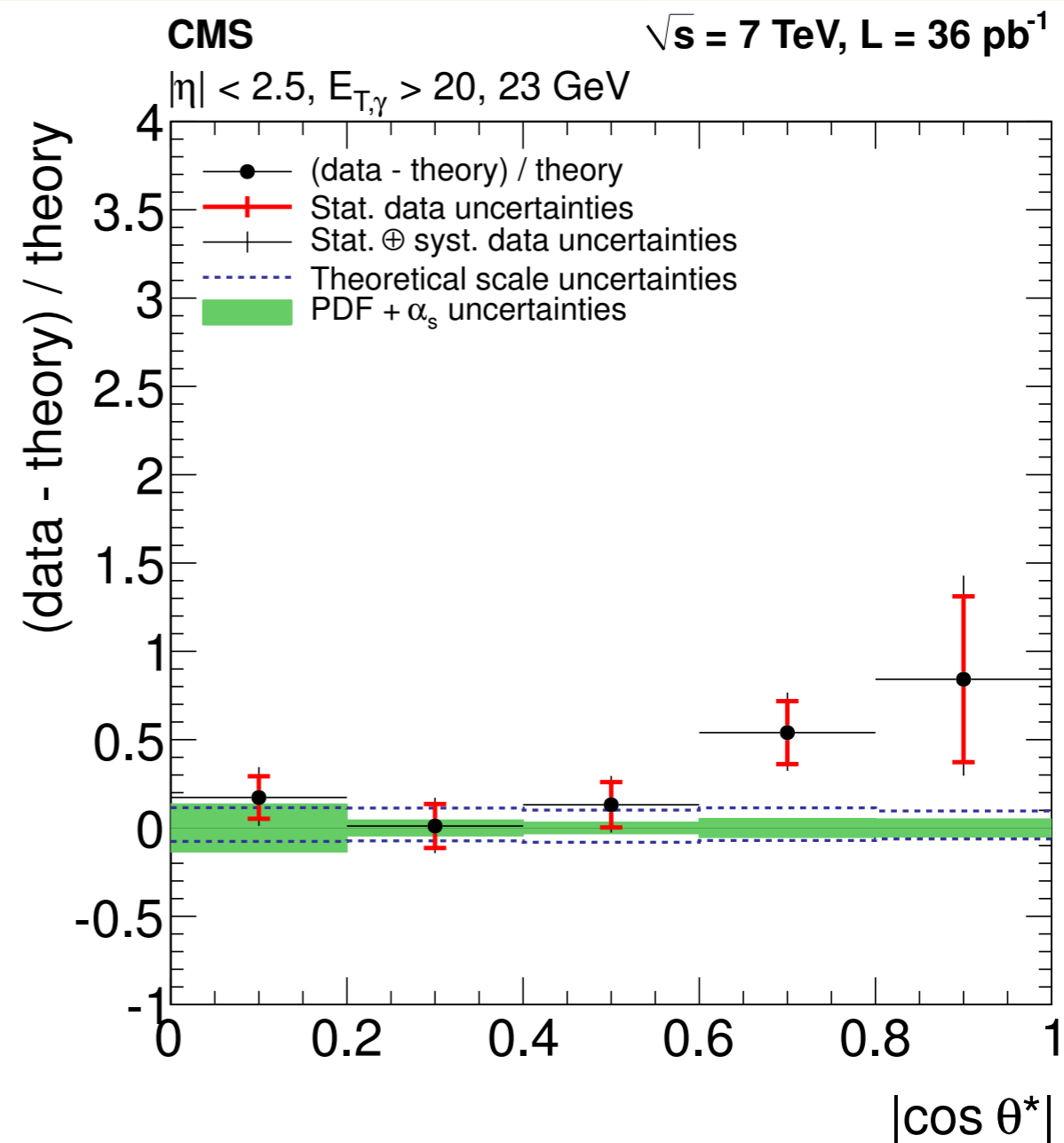
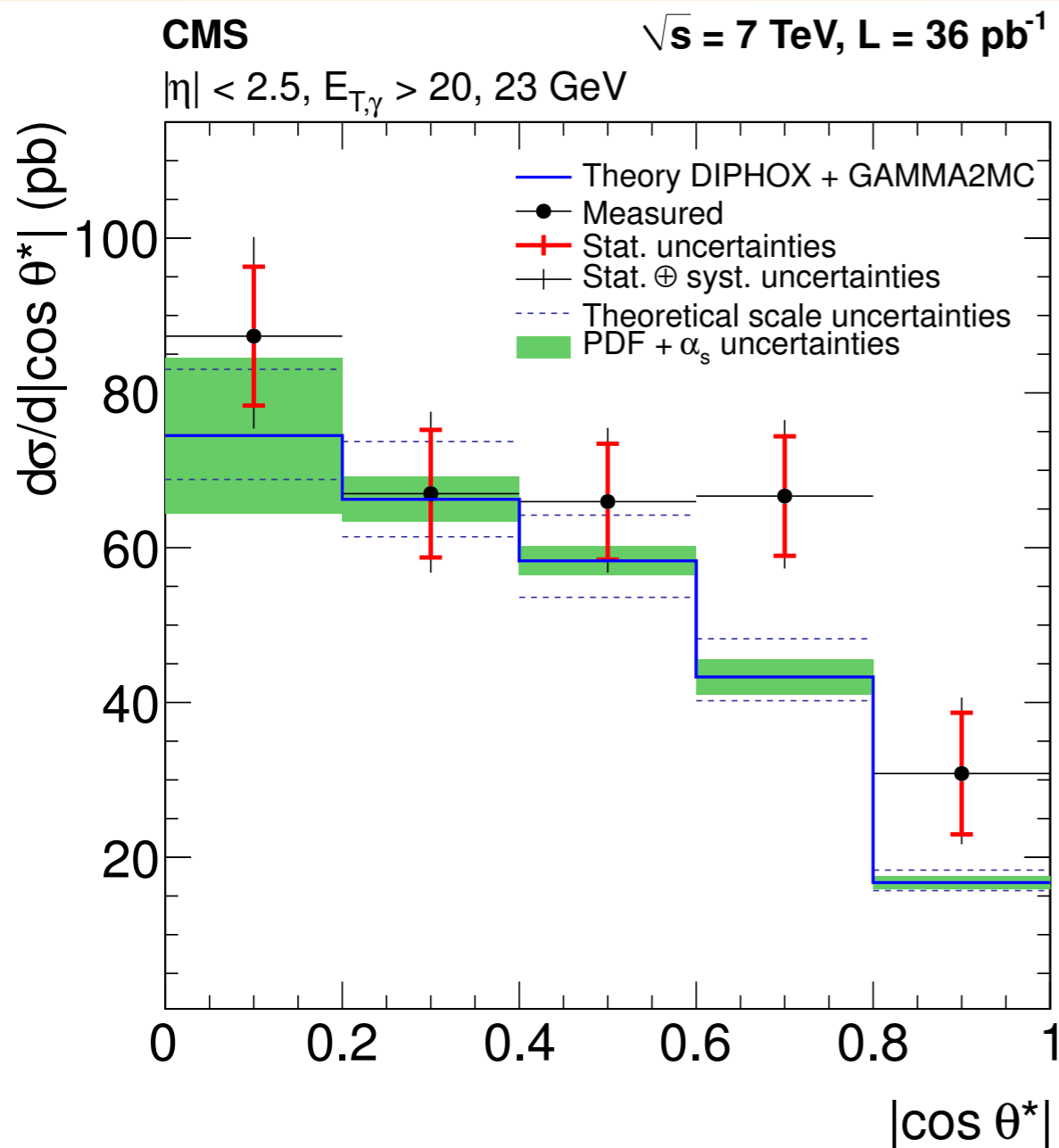
Di-photon Cross Section (vs $p_{T,\gamma\gamma}$)



- ◆ **Differential isolated prompt photon cross section**
 - response matrix inversion unfolding
- ◆ **Theory prediction**
 - isolation: $E_T < 5 \text{ GeV}$ in $R < 0.4$
 - NP correction = 0.953

Discrepancy at high $p_{T,\gamma\gamma}$:
collinear photons

Di-photon Cross Section (vs $\cos\theta^*$)



◆ Differential isolated prompt photon cross section

- response matrix inversion unfolding

◆ Theory prediction

- isolation: $E_T < 5 \text{ GeV}$ in $R < 0.4$

- NP correction = 0.953



Ongoing Measurements

- (1) Photon + jets differential cross sections
- (2) Photon + jet angular distribution
- (3) Di-photon + jets
- (4) Jet cross-sections, reaching jet $p_T > 2 \text{ TeV}$ ($x_T \sim 0.6$)
- (5) Three-jet production rate vs invariant mass
- (6) Measurement (?) of α_s with the R_{32}
- (7) Three-jet and Four-jet properties
- (8) Jet structure and substructure
- (9) Color coherence

.....

And many others, which are not classified as “QCD”
in the CMS organization:

- Z,W + jets production
- Z + jet angular distributions
- heavy flavor production
- forward physics





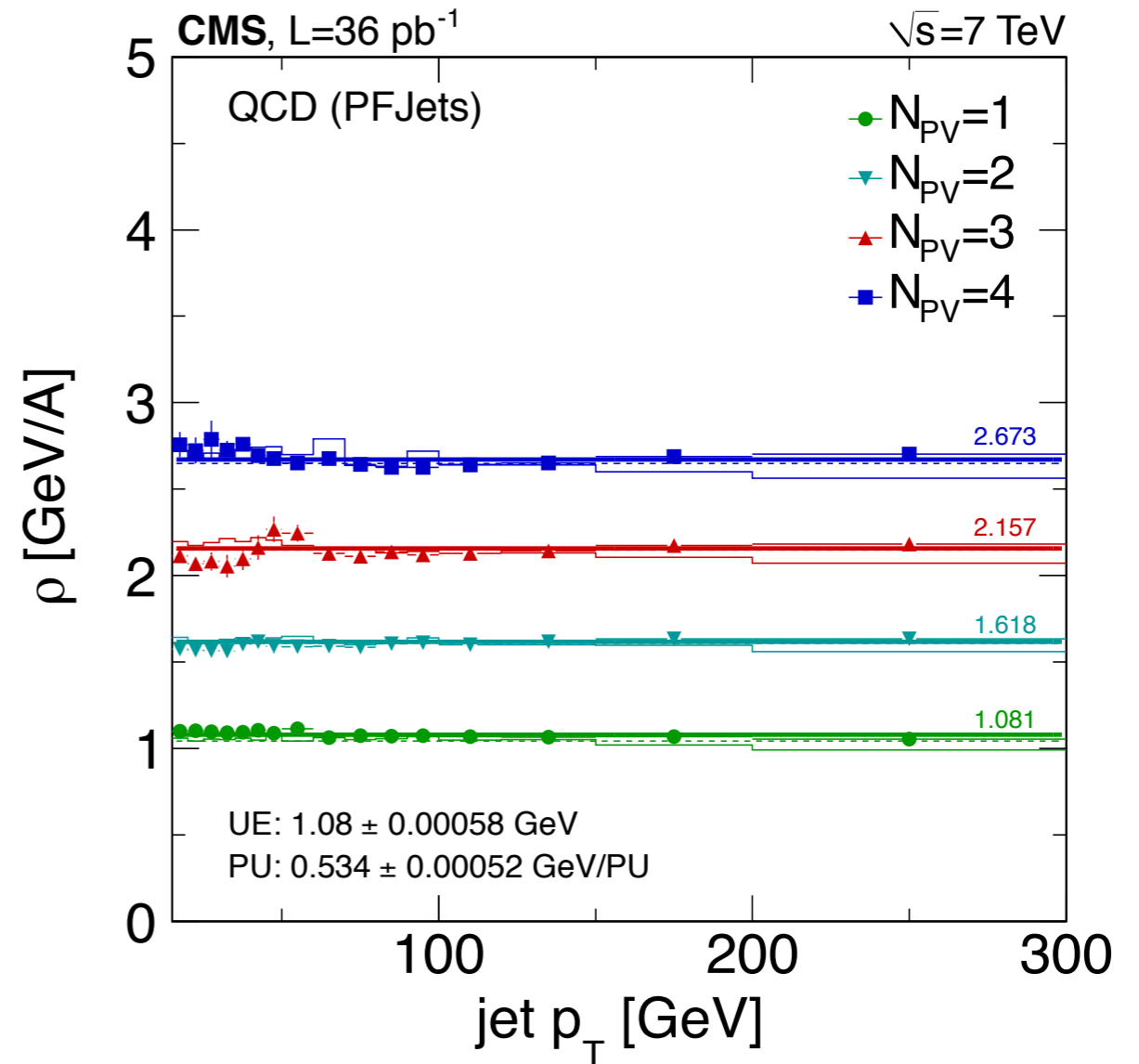
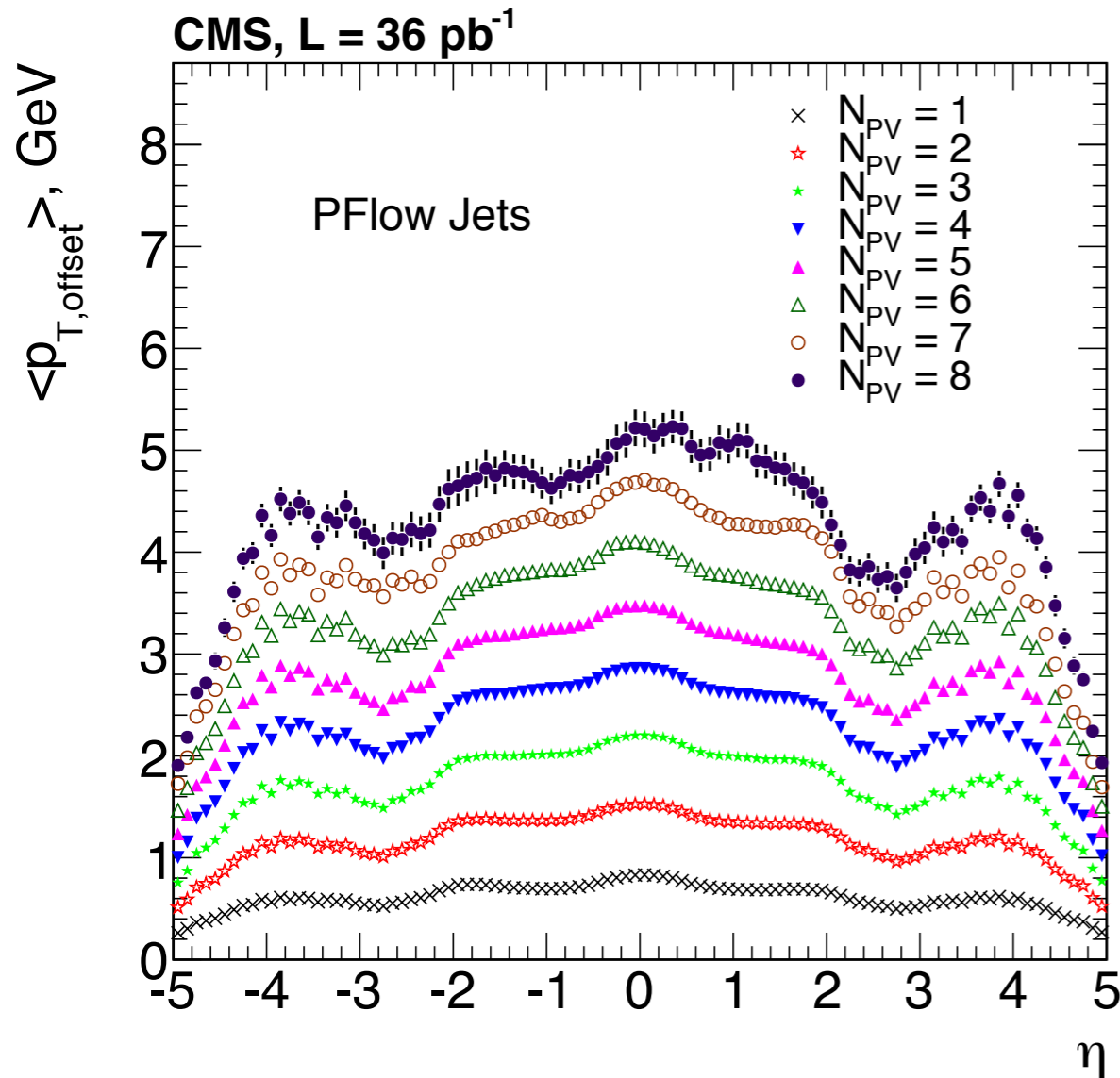
Summary

- ◆ Understanding QCD is essential for the LHC physics
- ◆ CMS has performed a large number of competing QCD measurements with the 2010 data (19 journal publications and several preliminary results)
- ◆ **Overall, data and theoretical predictions are compatible**
 - data are described well by pQCD @ NLO in the TeV scale
 - but still limited by the experimental systematic uncertainties
- ◆ QCD Monte-Carlo generators are in satisfactory agreement with the data
 - pre-LHC tunes clearly fail to describe the data
 - first LHC tunes in the right direction but there is room for improvement
 - MC tuning requires a global fit of as many measurements as possible
- ◆ Further QCD studies are being pursued with the 2011 data
 - the 2010 studies were only the prelude to the precision measurements to follow



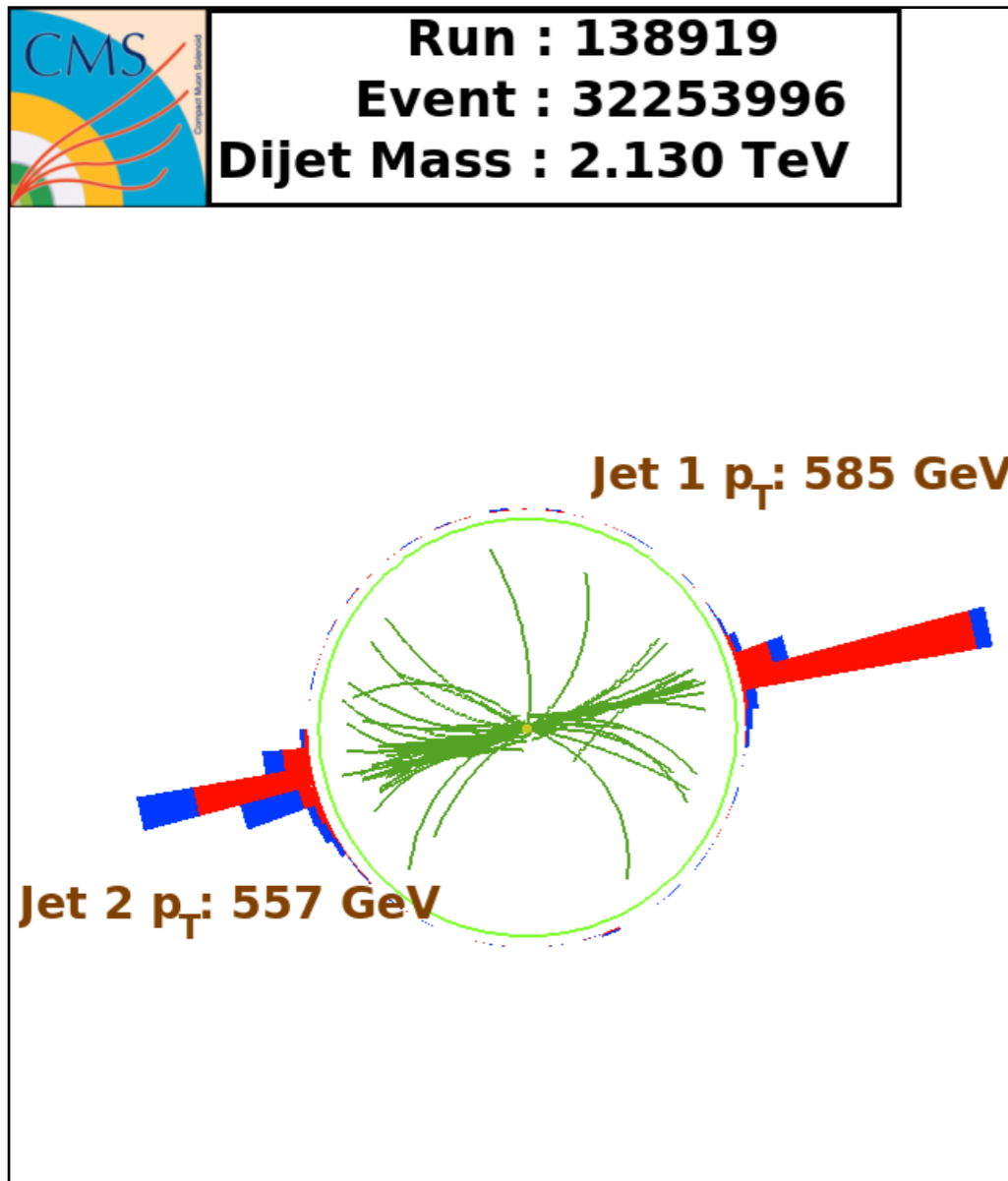
Backup

Jet Energy Calibration (offset)

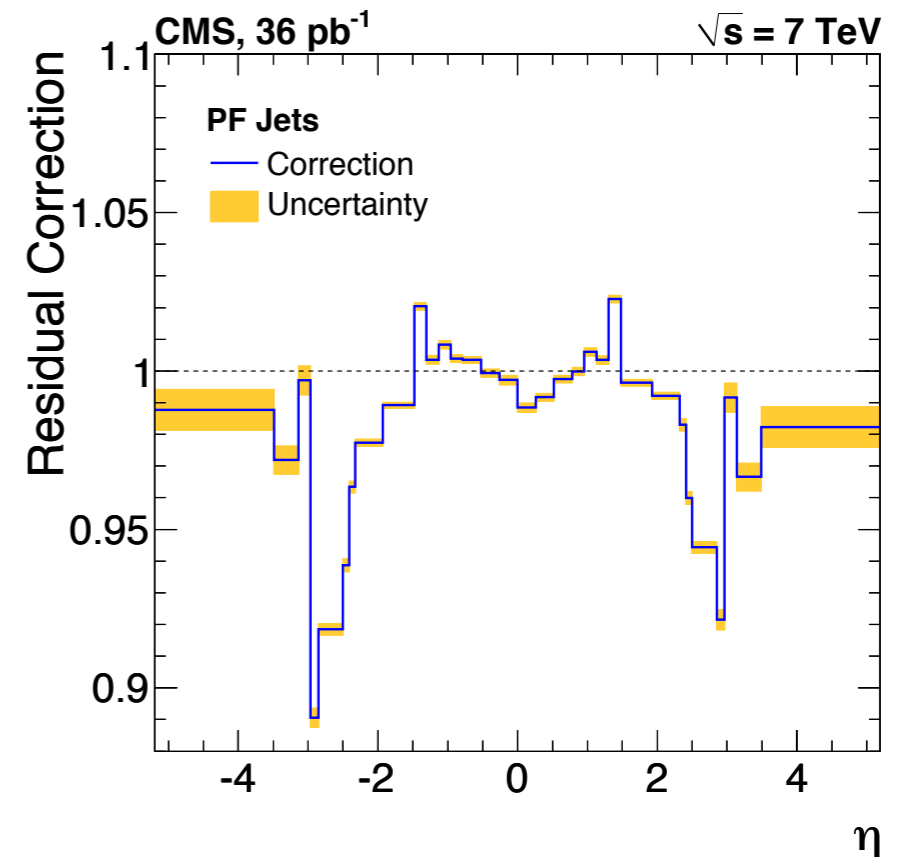
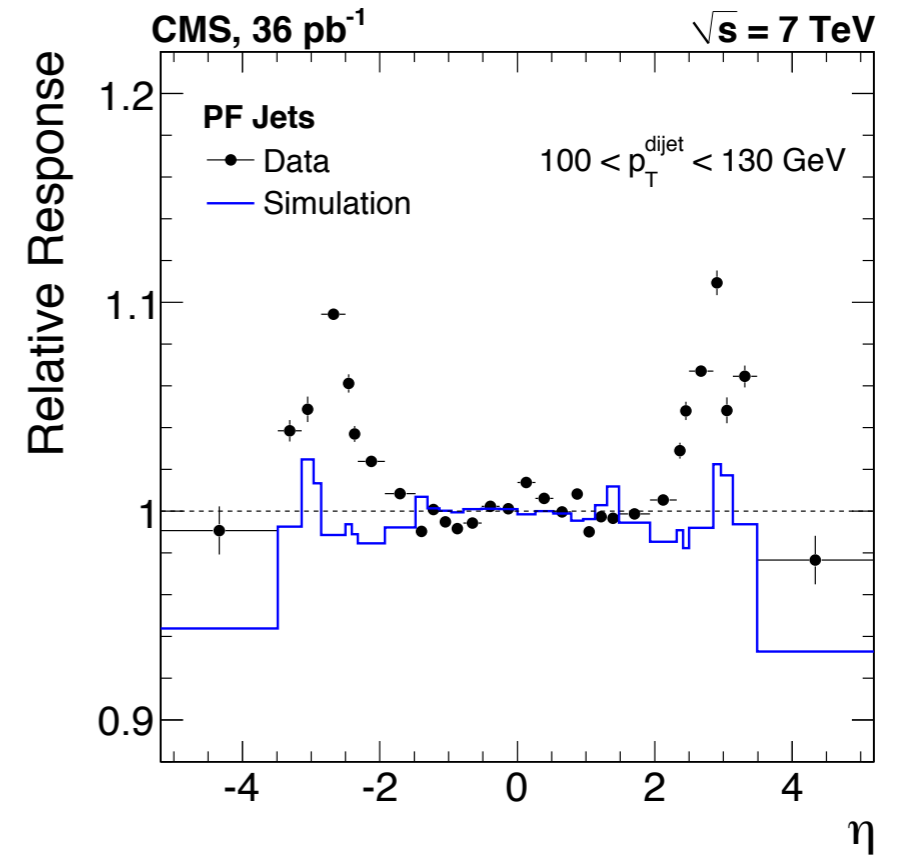


$$C_{\text{hybrid}}(p_T^{\text{raw}}, \eta, A_j, \rho) = 1 - \frac{(\rho - \langle \rho_{\text{UE}} \rangle) \cdot \beta(\eta) \cdot A_j}{p_T^{\text{raw}}}$$

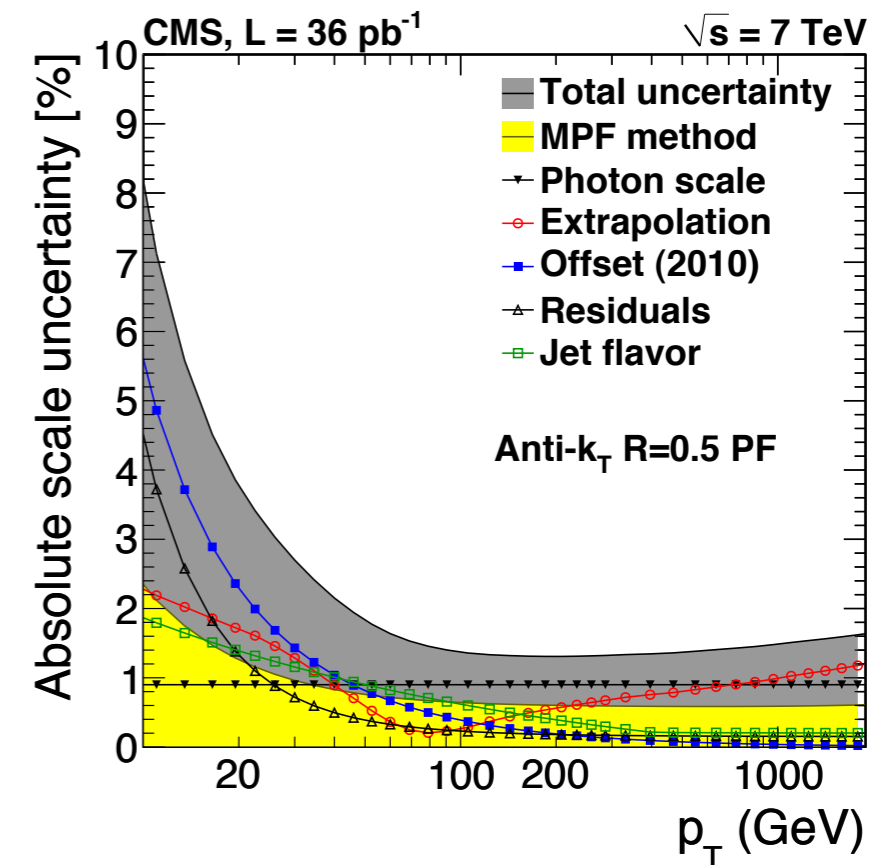
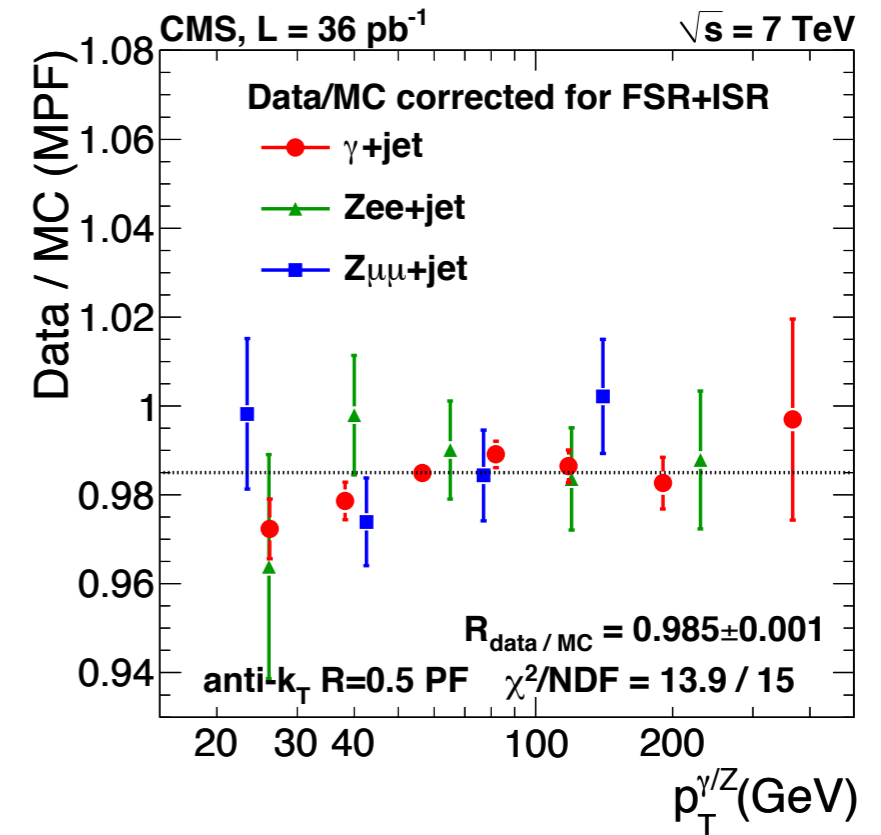
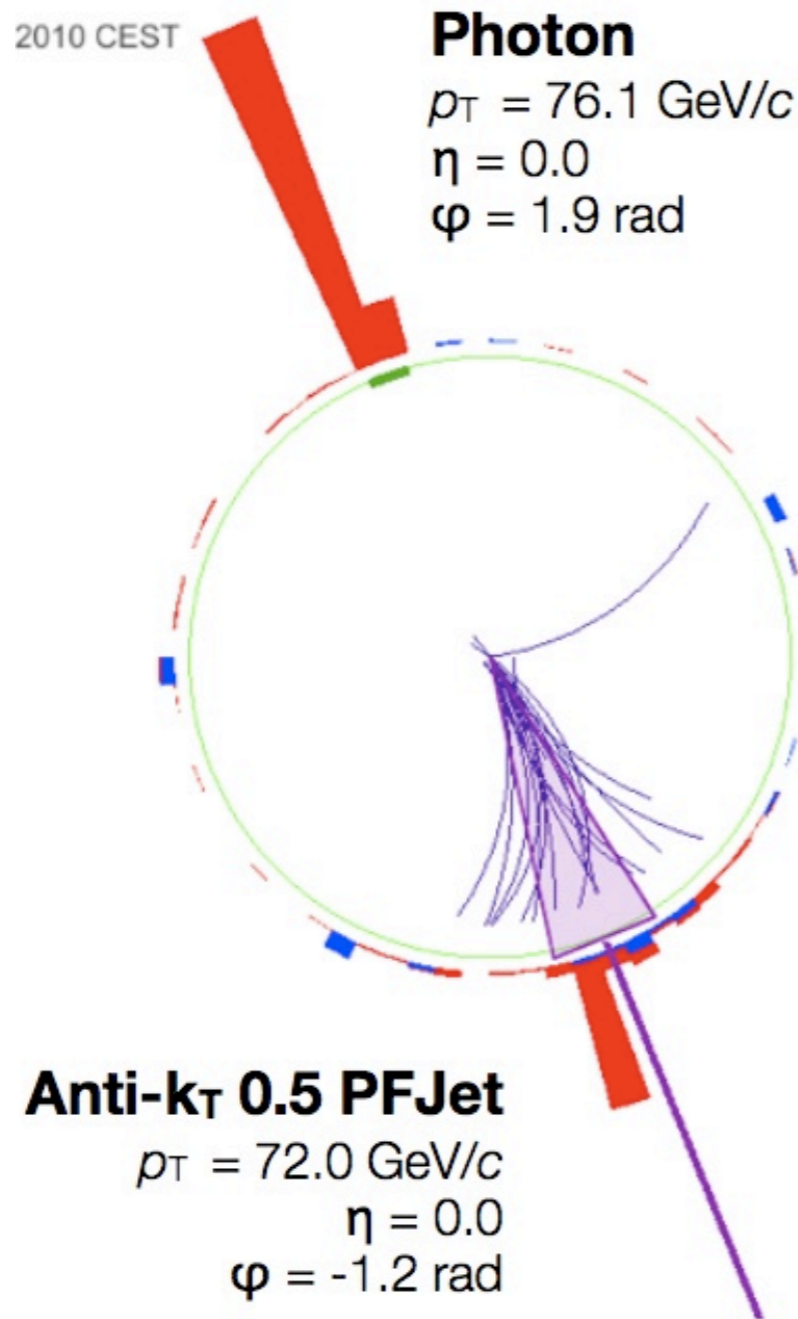
Jet Energy Calibration (vs η)



Exploiting the dijet p_T balancing

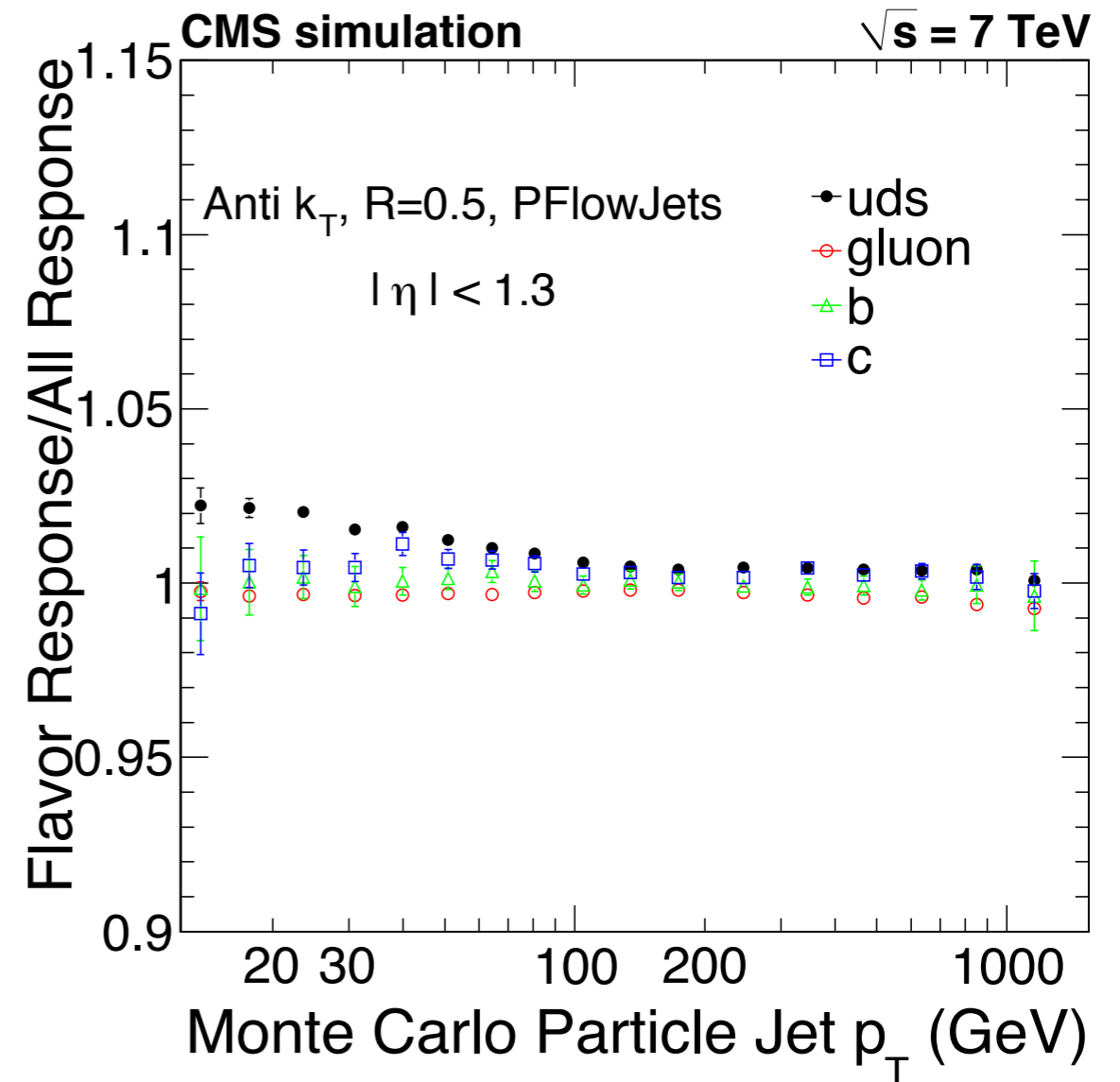
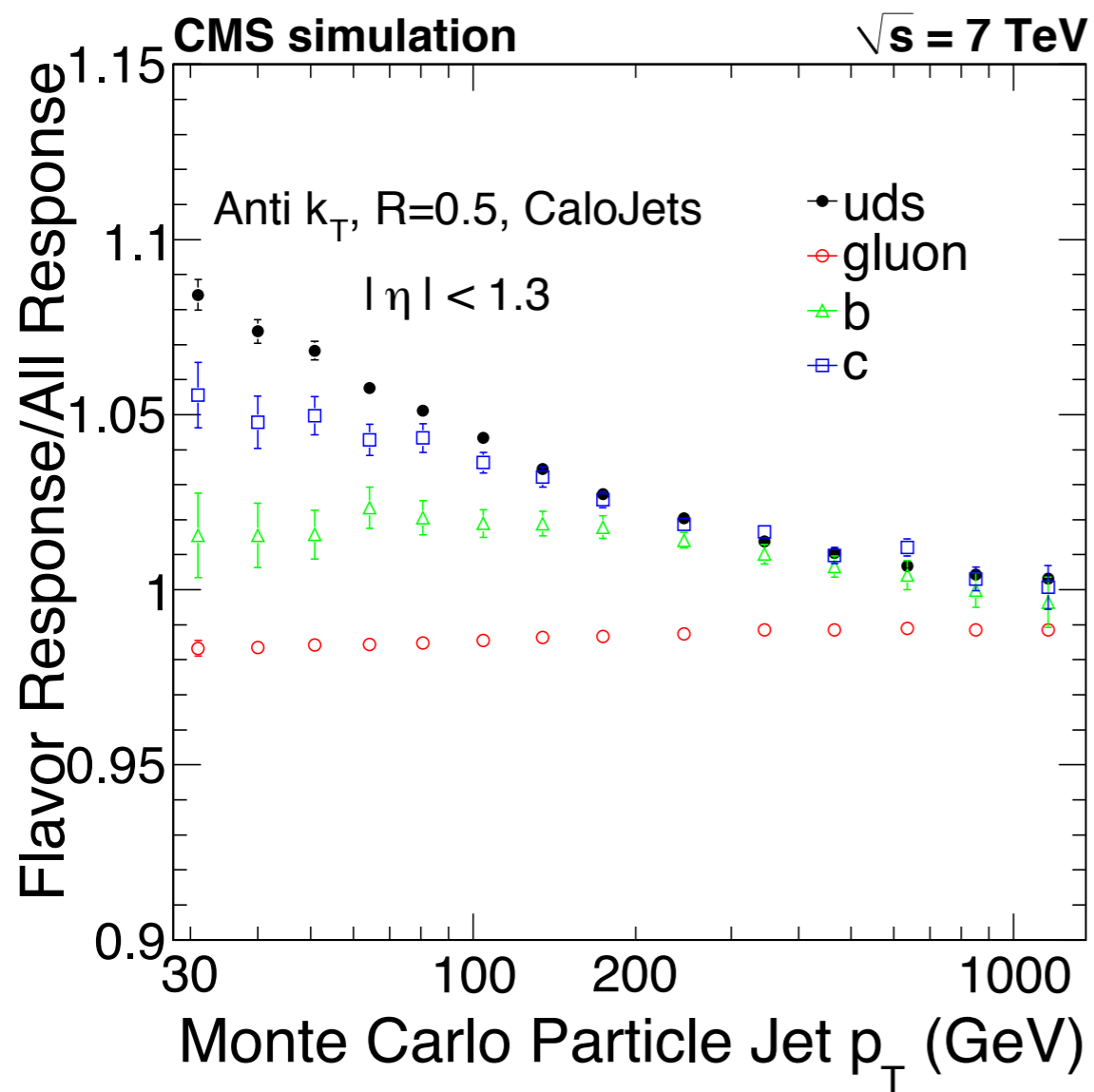


Jet Energy Calibration (vs p_T)



Exploiting the photon/Z+jet
 p_T balancing

Jet Energy Calibration (flavor dependence)



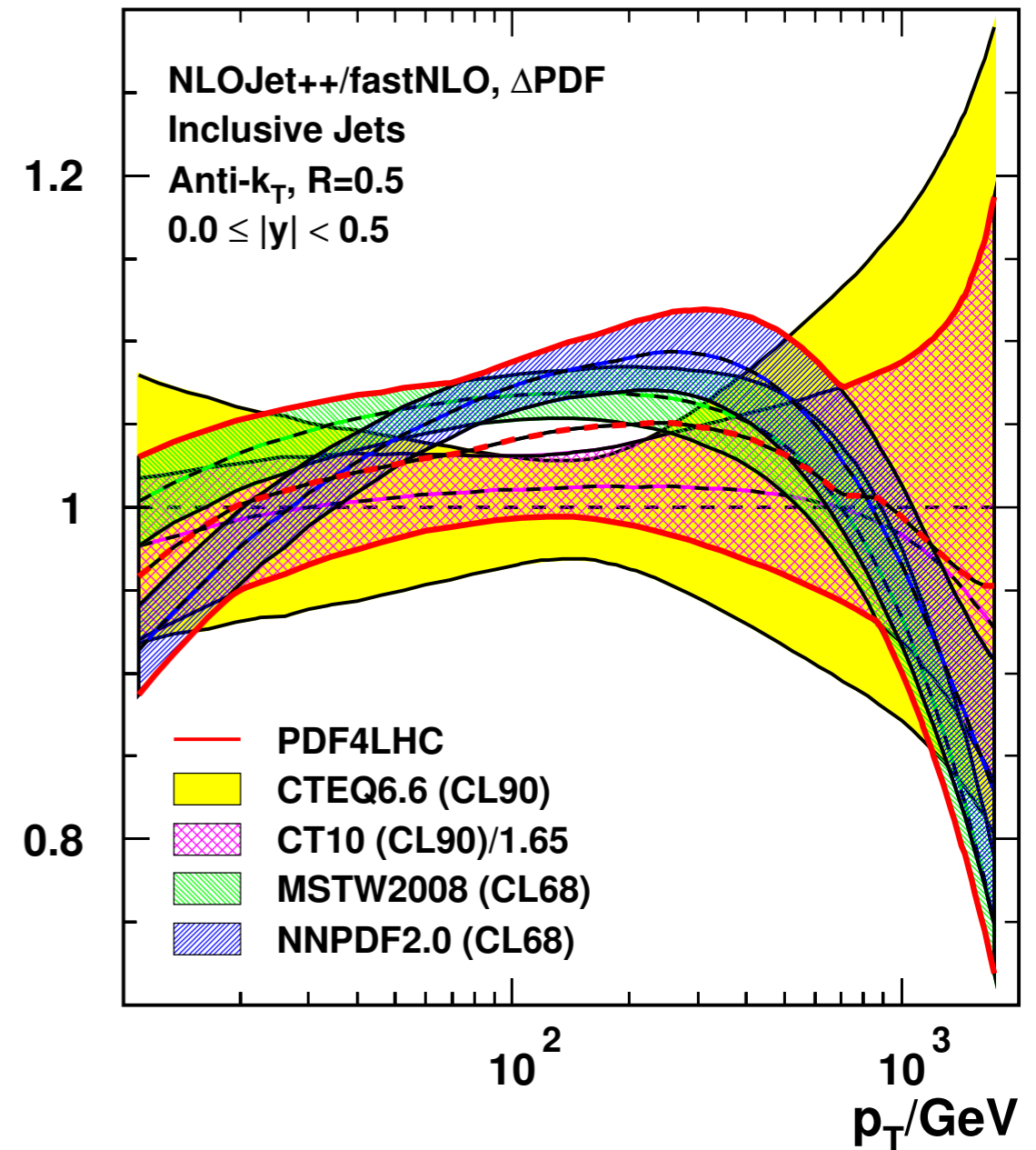
The PF jet reconstruction has reduced the flavor dependence to less than 2% for $p_T > 30 \text{ GeV}$

◆ **The PDF4LHC prescription describes the way to combine the various PDFs:**

- compute the observable of interest (e.g. inclusive jet cross section) with each PDF set
- construct the 1-sigma (68% CL) band from each PDF set
- at every point, define the global envelope from the 1-sigma bands
- the PDF4LHC prediction is the center of the global envelope

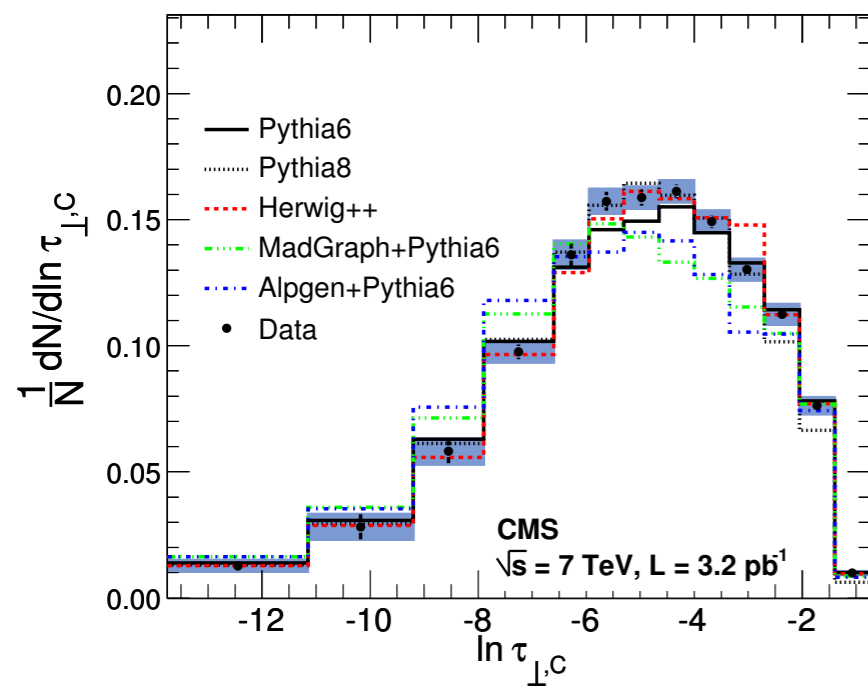
◆ **The PDF4LHC prescription is meant for a check of the overall compatibility between data and theory predictions**

$$\frac{d^2\sigma/dp_T dy_{PDF}}{d^2\sigma/dp_T dy_{CTEQ6.6}}$$

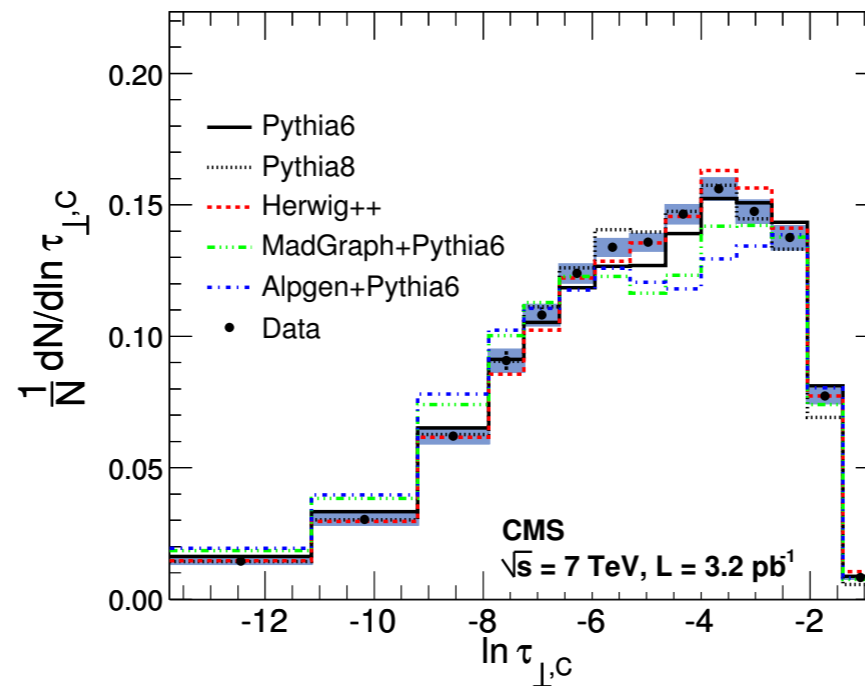


Hadronic Event Shapes

$90 < p_{T,max} < 125$ GeV



$125 < p_{T,max} < 200$ GeV



$p_{T,max} > 200$ GeV

