

Survey of edge-TCT measurements at CERN

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Outline

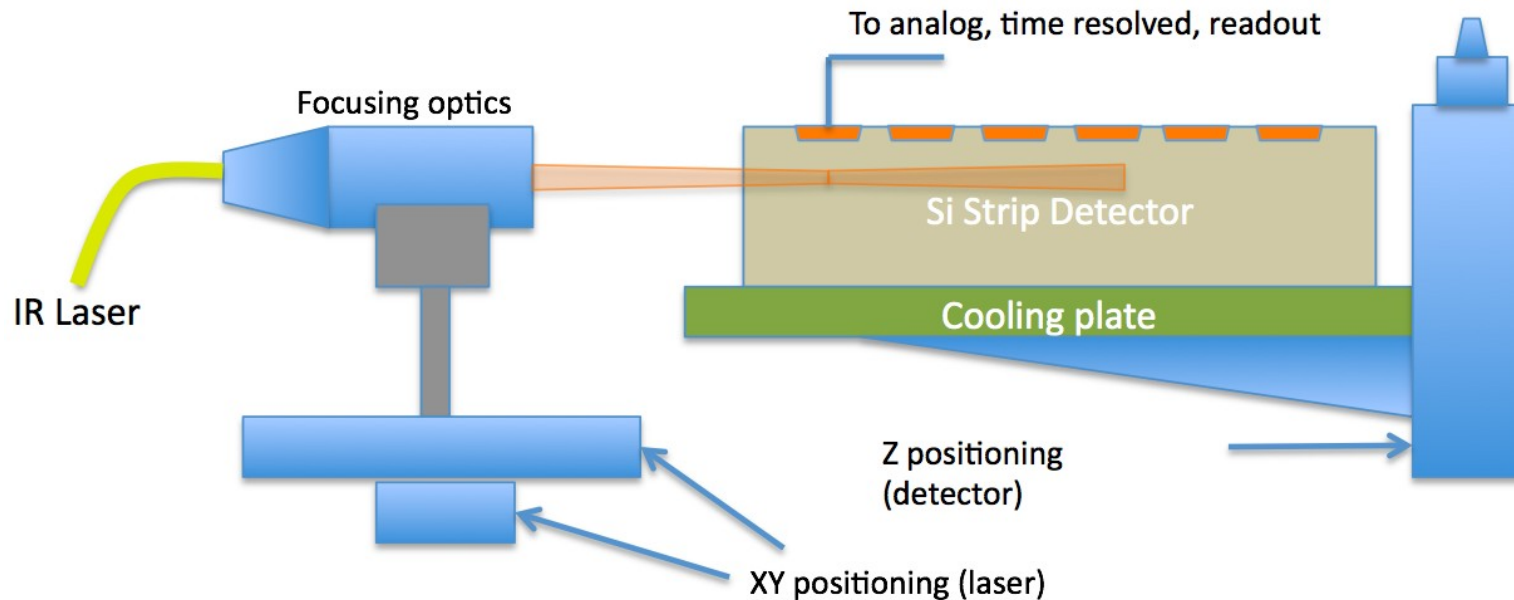
- ◆ Extraction of trapping time profiles from eTCT measurements
 - ◆ 2 methods proposed
 - ◆ Extraction of electric field profile from measured drift velocity profile (electric field profile required by both methods)
 - ◆ Determination of transfer function of the measurement system (required for 1. method)
 - ◆ An example of 2. method (1. method presented at 19th RD50 workshop)
- ◆ eTCT measurements with p-type strip detectors after proton irradiation (N. Pacifico's PhD, also presented at 19th RD50 workshop)
 - ◆ Study of annealing development of drift velocity and efficiency profile behavior in FZ and MCz p-type detectors
 - ◆ Study of effect of oxygen enrichment on drift velocity and efficiency profiles

Part 1:
**Trapping time extraction
from eTCT measurements**

τ extraction from eTCT measurements

- ◆ Classical TCT measurement with red laser:
 - ◆ Offers trapping time determination with the assumption:
 $\tau_{e,h}(E) = \text{const.}$
 - ◆ Difficulties with trapping time extraction for highly irradiated detectors $\rightarrow \tau_{e,h}(E) \neq \text{const.}$
- ◆ eTCT measurement:
 - ◆ Offers $v_{dr}(z)$ extraction $\rightarrow \tau_{e,h}(E)$
 - ◆ Investigating 2 different methods

eTCT technique



- ◆ For details on eTCT and related analysis see [1]
- ◆ Drift velocity profile:
 - ◆ Integration window of 0.5ns from beginning of signal
- ◆ Efficiency profile:
 - ◆ Integration window of 25ns around the signal

Drift velocity deconvolution (1/5)

- ◆ Extraction of point charge $v_{dr,t}(z)$ required → deconvolution of measured $v_{dr,m}(z)$

- ◆ General remarks on deconvolution:

$$g(z) = h(z) * f(z)$$

- ◆ Problem: deconvolution most often ill posed problem
 - ◆ In Fourier space $G(\omega) = H(\omega)F(\omega) \rightarrow F(\omega) = G(\omega)/H(\omega)$
 - ◆ $H(\omega)$ is typically a low pass filter, the inverse $1/H(\omega)$ is a high pass filter → amplifies noise and numerical errors!
- ◆ Methods
 - ◆ Regularization (filtering)
 - ◆ “Fitting”: take model function for f and vary parameters to fit the measured data, gives best results, if the model function is known...

Drift velocity deconvolution (2/5)

$$v_{dr,m}(z) = G(0, \sigma) * v_{dr,t}(z)$$

- ◆ Assuming Gaussian smearing function (laser beam, imperfection due to polishing)
- ◆ Tried several regularization methods
 - ◆ Problems: not edge preserving, can be time consuming, no reliable automatic algorithm for determination of regularization constants found ...
- ◆ Decided to use “fitting” strategy
- ◆ $v_{dr,t}(z)$ function is modeled with N parabolas/lines applied to different regions of detector
- ◆ Least squares minimization with TMinuit is performed: typically Simplex method is used to bring initial guess closer to solution, followed by Migrad minimization to improve the result
- ◆ Parameters
 - ◆ σ of Gaussian smearing function
 - ◆ Points (z, v_{dr}) determining the N regions with different parabolas/lines
 - ◆ Constant a or b ($v_{dr}(z) = az^2 + bz + c$) for each parabola
 - ◆ Depending on the problem, some can be fixed before Migrad and/or Simplex minimization

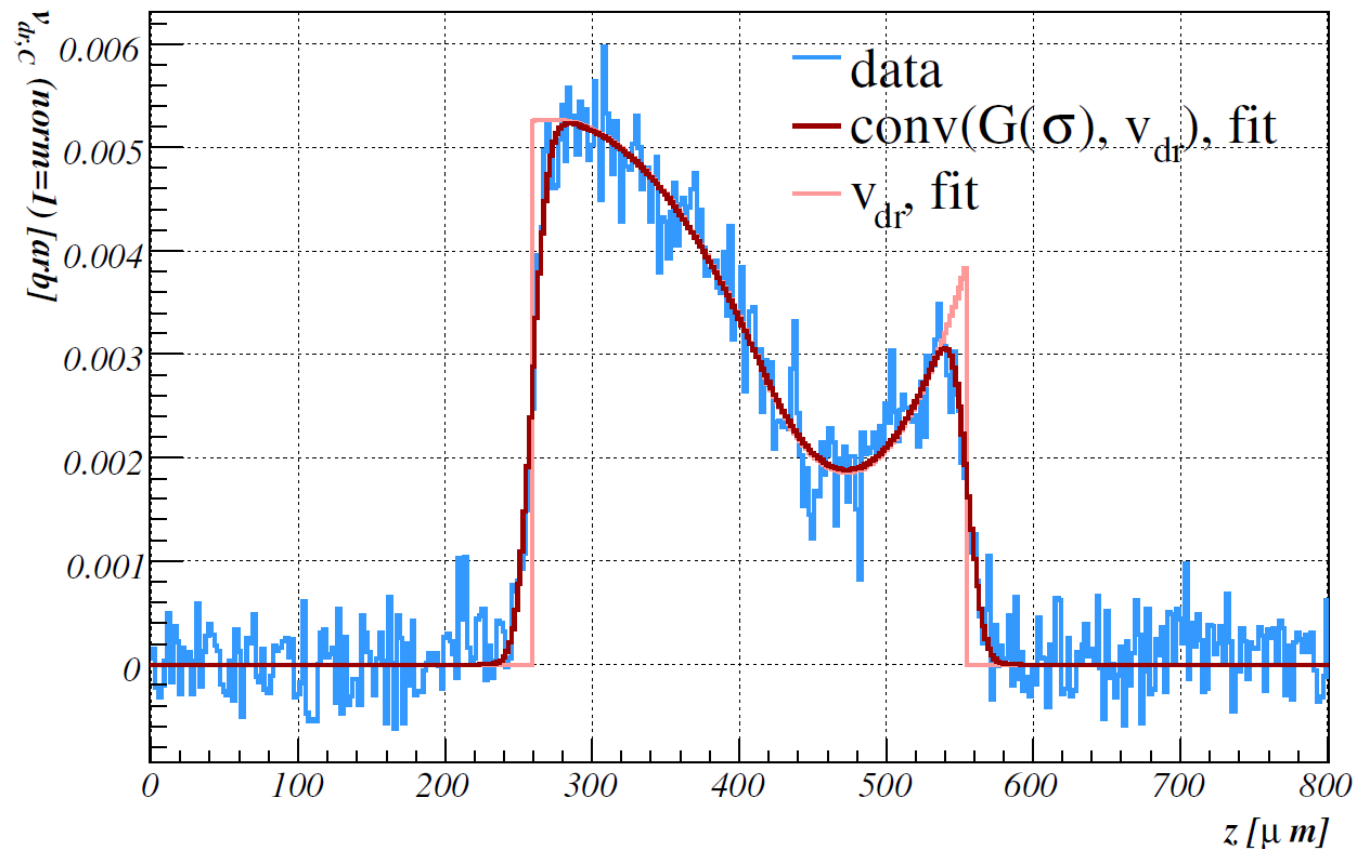
Drift velocity deconvolution (3/5)

- ◆ Use deconvoluted $v_{dr,t}(z)$ → calculate $v_{dr,t}^e(z)$, $v_{dr,t}^h(z)$, $E(z)$
- ◆ Extracted deconvoluted $v_{dr,t}(z)$ in arbitrary units
- ◆ Constraint $\int E(z)dz = U_{bias}$ to determine the absolute scale
 - ◆ Fix normalization A of $v_{dr,t}(z)$ and calculate $v_{dr,t}^e(z)$, $v_{dr,t}^h(z)$, $E(z)$
$$A \cdot v_{dr,t}(z) = (v_{dr,t}^e(z) + v_{dr,t}^h(z)) = E \cdot (\mu_e(E) + \mu_h(E))$$
→ requires “bisection” like method at each z due to nonlinear mobility dependence on field
 - ◆ “Bisection”: vary A until the constraint is $\int E(z)dz = U_{bias}$ is met
- ◆ Limitations: fails at very high fields where both electron and hole drift velocities are saturated

Drift velocity deconvolution (4/5)

Example:

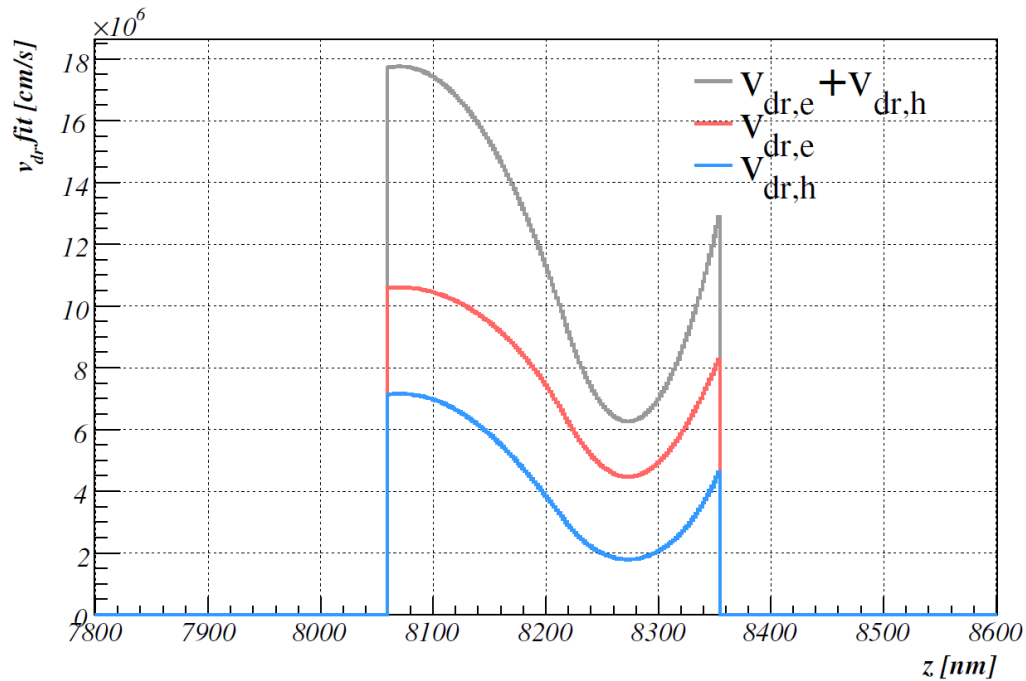
- ◆ Micron FZ-p strip detector, $\Phi = 2 \times 10^{15}$ protons/cm², in annealing minimum, $U_{bias} = 500$ V, measurement $T = -25^\circ\text{C}$
- ◆ Model function: 2 parabolas in 2 different regions
 - ◆ Gaussian smear: $\sigma_{best} = 8.6\mu\text{m}$ (laser $\sigma = 7.5\text{-}8\mu\text{m}$)
 - ◆ Active region: $d_{best} = 292\mu\text{m}$
- ◆ Calculated $E(z)$ and $v_{dr,t}^e(z)$, $v_{dr,t}^h(z)$ on next slide...



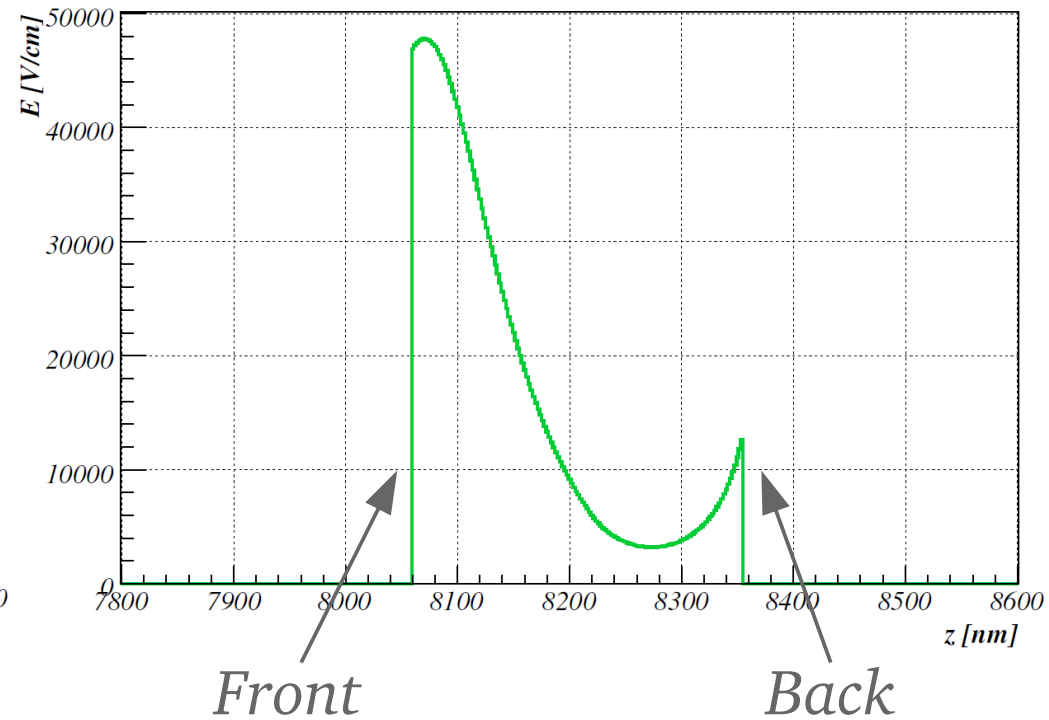
Drift velocity deconvolution (5/5)

- ◆ Calculated $v_{dr,t}^e(z)$, $v_{dr,t}^h(z)$, $E(z)$
- ◆ Mobility model: Jacoboni [2]

$$v_{dr,t}^e(z), v_{dr,t}^h(z)$$



$$E(z)$$



[2] C. Jacoboni et al., Solid State Electronics, 1977, Vol. 20, 77-89

τ extraction: method 1

◆ Procedure:

- ◆ Consider front/back injection (only one type of charge drifting)
- ◆ $E(z) \rightarrow$ calculate induced current, assume Gaussian laser beam profile with σ as extracted from the deconvolution of $v^e_{dr,t}(z)$
- ◆ Add trapping, convolve with transfer function and vary trapping model parameters to fit the result to measured waveform in the least squares sense (Minuit minimization)

◆ Fit parameters:

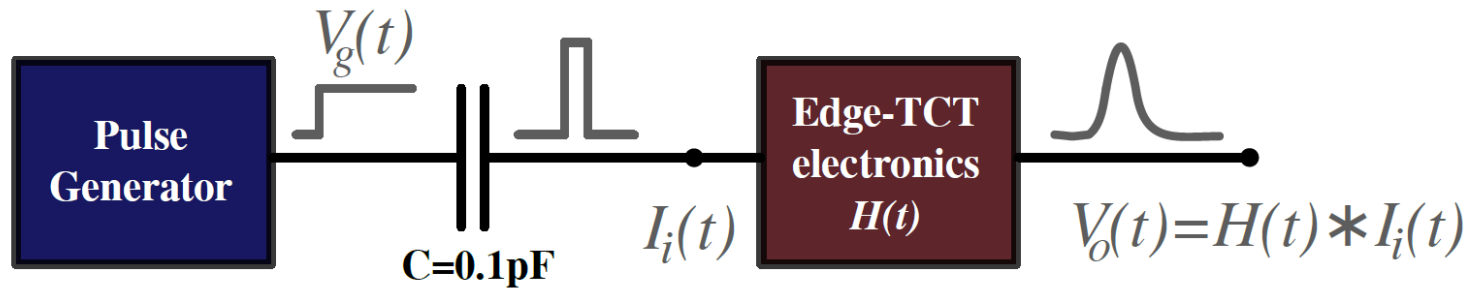
- ◆ Normalization constant (can be fixed, depending on the transfer function used)
- ◆ Parameters for $\tau_{e,h}$ modeling

◆ $\tau_{e,h}$ modeling:

- 1) Divided detector in n equidistant regions with different trapping time for each region
- 2) Assume some other dependence on electric field (linear, exp...)

Transfer function of the meas. system (1/5)

- ◆ Method 1) for trapping time extraction requires knowledge of transfer function of the measurement system
- ◆ Option: measured I_i and V_o (2.5GHz scope, Agilent DSO9254A):



I_i δ -like current spike

V_g : step-like voltage pulse

- ◆ H calculated in Fourier space (Riad-Parruck method [3]):

$$H(\omega) = \frac{V_o(\omega)}{I_i(\omega)} S(\omega)$$

- ◆ Filter (regularization):

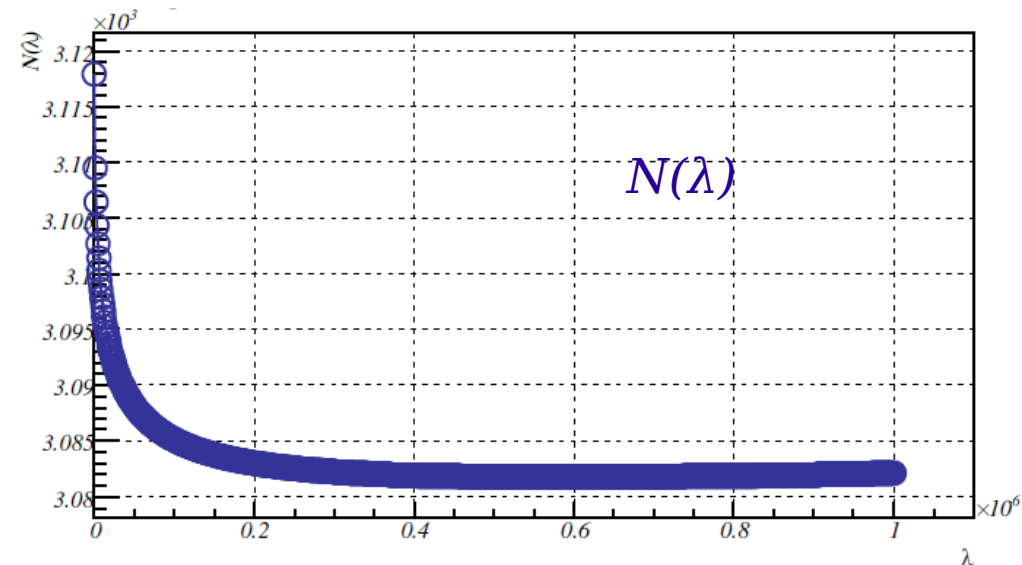
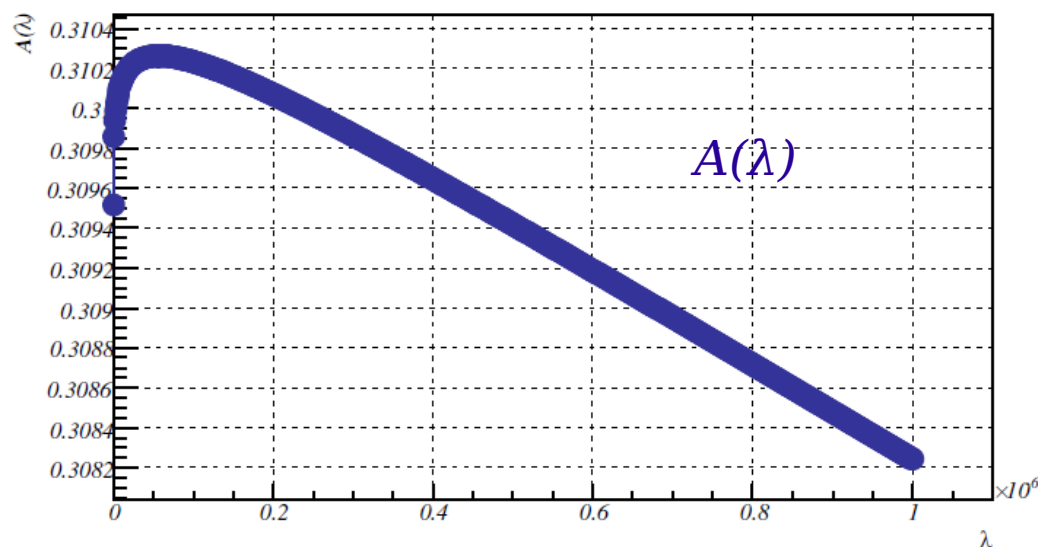
$$S(\omega) = \frac{|I_i(\omega)|^2}{|I_i(\omega)|^2 + \lambda}$$

Transfer function of the meas. system (2/5)

- ◆ Optimal regularization constant λ determination:
 - ◆ For each λ :
 - ◆ Check the integral of calculated $H(t)$ to get a smooth step-like waveform (less sensitive to noise), $\int H(t)dt$
 - ◆ check mean, $A(\lambda)$, and RMS, $N(\lambda)$, in the tail part of the step-like response $\int H(t)dt$
 - ◆ Optimum λ_{opt} :

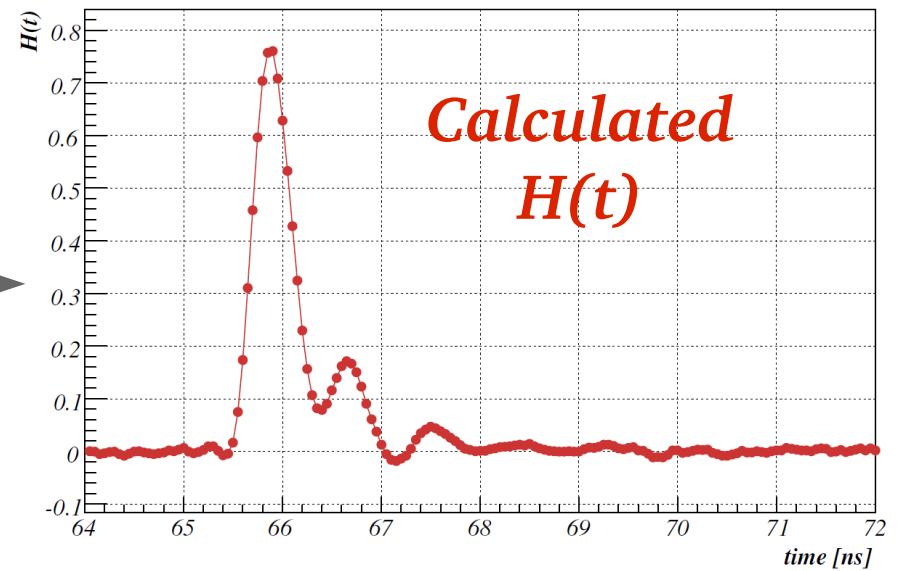
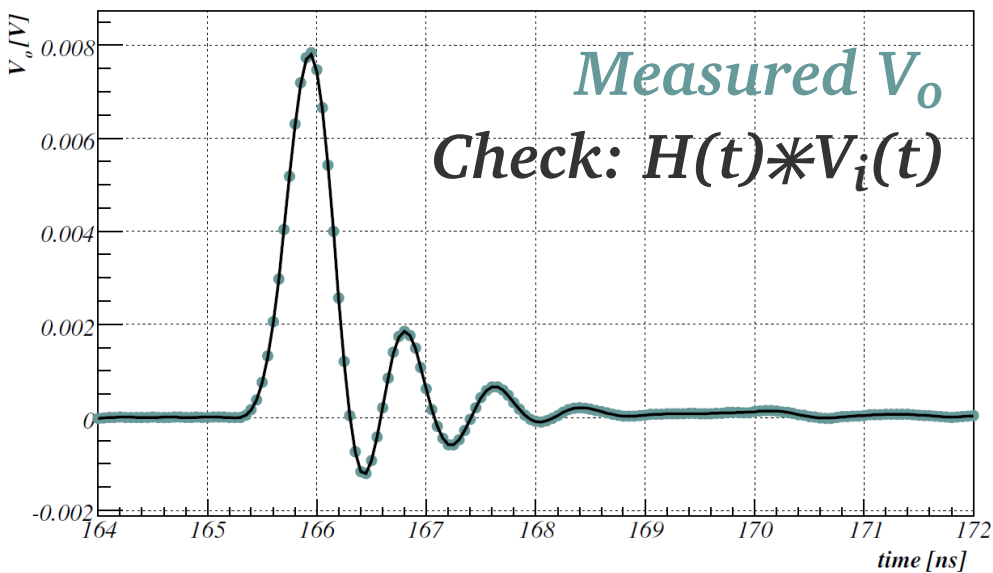
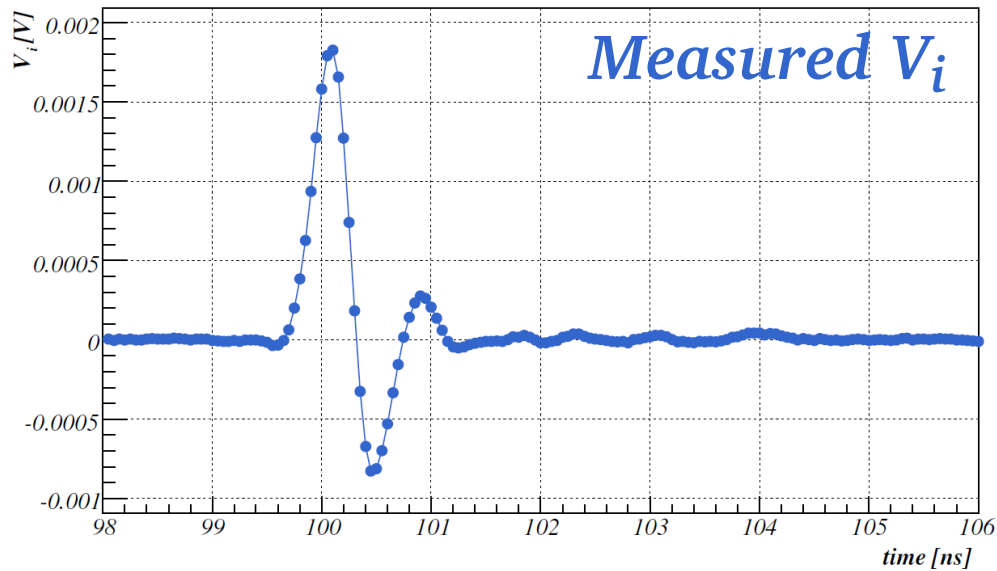
$$\frac{A(0) - A(\lambda_{opt})}{A(0)} \ll 1$$

$$N(\lambda_{opt}) \ll N(0)$$



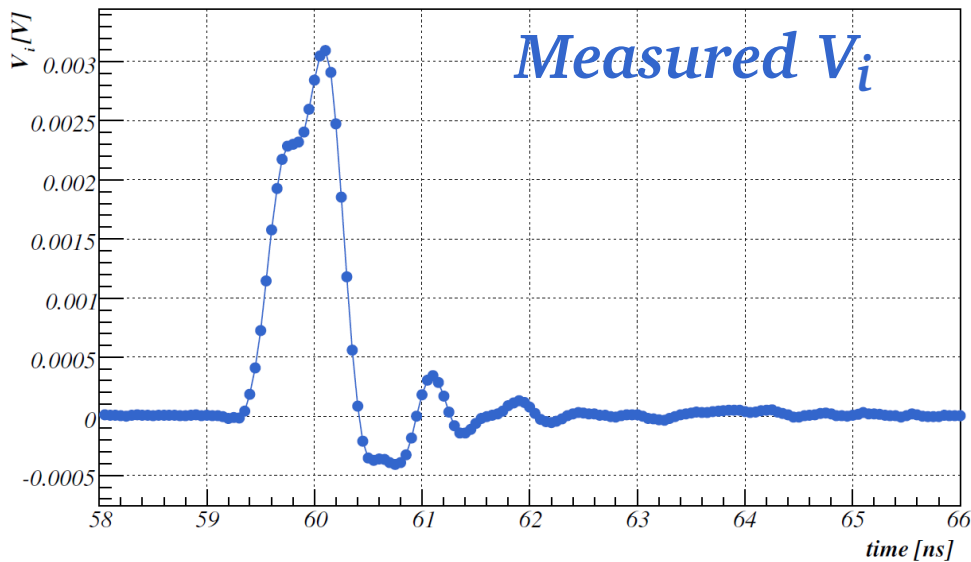
Transfer function of the meas. system (3/5)

Result



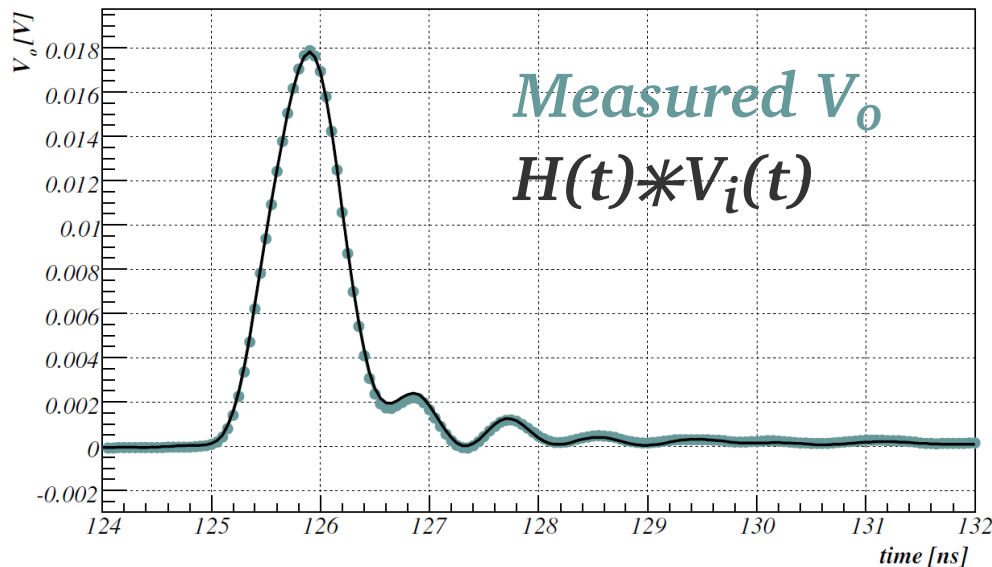
Transfer function of the meas. system (4/5)

Check: how calculated $H(t)$ transforms a different V_i ?



Looks good

- ◆ Extra check: for detector irradiated to 2×10^{14} pions/cm² compared calculated signal with measured ones, shapes matched well
- ◆ Different strategy for transfer function extraction presented on the next slide...



Transfer function of the meas. system (4/5)

- ◆ Unirradiated sensor: take calculated signal as input and measured signal as output to calculate the transfer function
- ◆ Problem: measured signals were too noisy... high value for regularization constant needed for Riad-Parruck method to work, but this alters the calculated transfer function too much for our needs...
- ◆ Tried with no filtering and average over the transfer functions calculated at different positions z in the detector
 - ◆ Still not good enough results...
 - ◆ Noticed that while transfer functions calculated from the central regions of detector match well, the ones from the edges look different... problems with model of the laser beam?

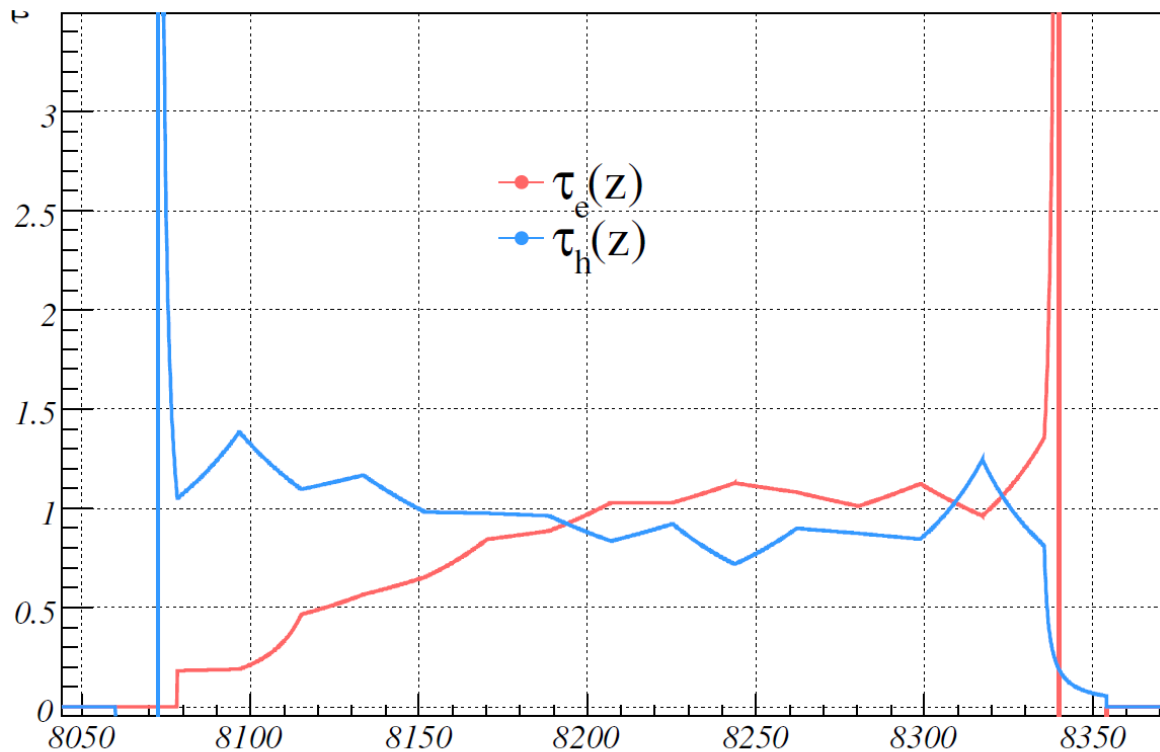
τ extraction: method 2

- ◆ Procedure: iterative process
 - ◆ Calculate the efficiency profile and compare it to the measured one
 - ◆ Divide the detector width in N equidistant regions with linear $1/\tau_{e,h}$
 - ◆ $E(z) \rightarrow$ calculate induced current at each point z inside the detector
 - ◆ assume Gaussian laser beam profile with σ as extracted from the deconvolution of $v_{dr,t}^e(z)$
 - ◆ Apply some initial values of $1/\tau_{e,h}$ for each of the points bounding the regions
 - ◆ Extract the integral of this signal (charge) \rightarrow efficiency profile
 - ◆ Apply same normalization factor on the calculated efficiency profile as extracted from measured one
 - ◆ Vary $1/\tau_{e,h}$ for each of the points bounding the regions (and each of the charge type) separately (while keeping others constant) to minimize the χ^2
 - ◆ Repeat until desired accuracy is reached
- ◆ No need for transfer function 😊
- ◆ No model function for $\tau_{e,h}(E)$ needed 😊
- ◆ Much more time consuming than method 1... 😞

τ extraction: method 2

Example (not final result)

- ◆ FZ-p strip detector $\Phi = 2 \times 10^{15}$ protons/cm², $U_{bias} = 500$ V, (electric field on p10):
 - ◆ Detector divided in 16 regions
 - ◆ Expected from [4]: $\tau_e \sim 0.5$ ns, $\tau_h \sim 0.4$ ns
- ◆ Observations:
 - ◆ Tried with different initial conditions and get approximately same result (in the central part)
 - ◆ Less trapping close to front/back edges (higher el. Field) for holes/electrons?
 - ◆ Holes: shape follows the electric field ϵ (apart from points at the back...) and seams as one would expected intuitively
 - ◆ Electrons: opposite behavior than with holes
 - ◆ Problems with edge points...
 - ◆ Wrong laser beam shape modeling?
 - ◆ More investigation needed to see if this makes sense and if the method can work...



**Part 2:
Annealing study**

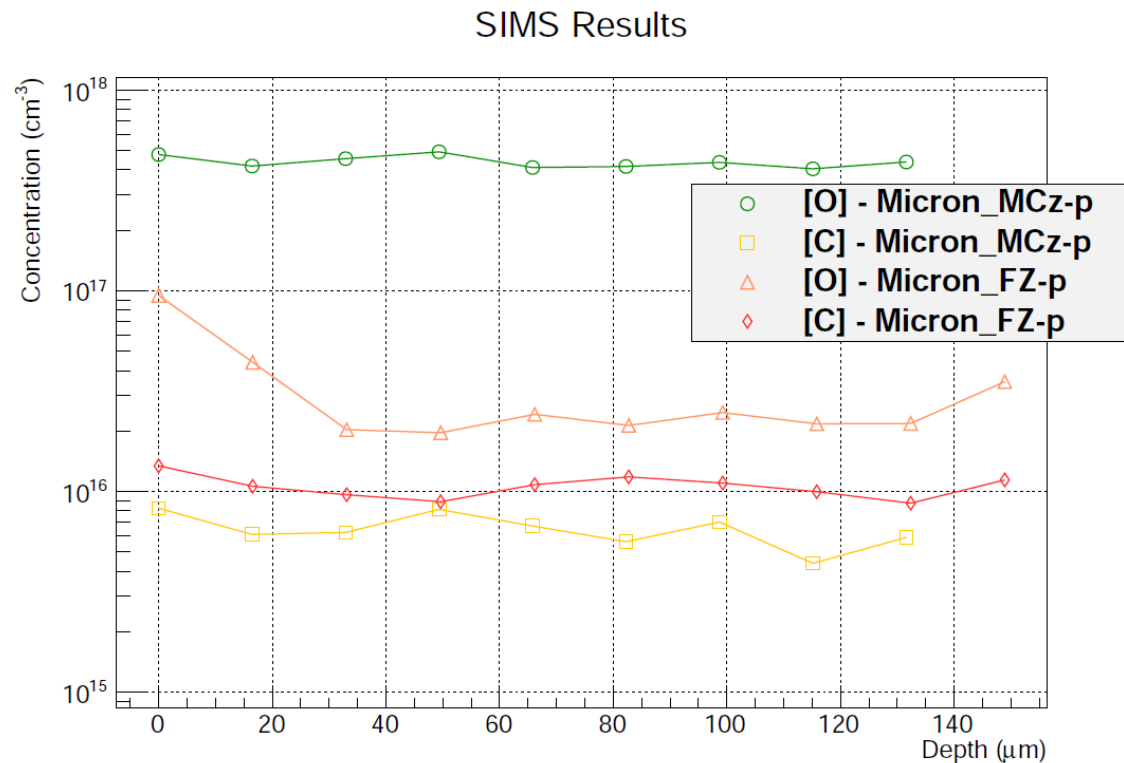
Annealing study: samples & irradiations

◆ Detectors:

- ◆ 2010 Micron RD50 production
- ◆ FZ-p and MCz-p strip detectors
- ◆ 300 μm thick
- ◆ Strips: 80 μm pitch, 20 μm width
- ◆ SIMS measurements
 - ◆ MCz: uniform oxygen concentration
 - ◆ FZ: higher oxygen concentration close to the implant, but still order of magnitude lower than in MCz

◆ Irradiations

- ◆ Irradiated with 24GeV/c protons (CERN PS)
- ◆ $\Phi = 10^{16} \text{p/cm}^2$ ($\Phi_{\text{eq}} = 6.2 \times 10^{15} \text{n}_{\text{eq}}/\text{cm}^2$)

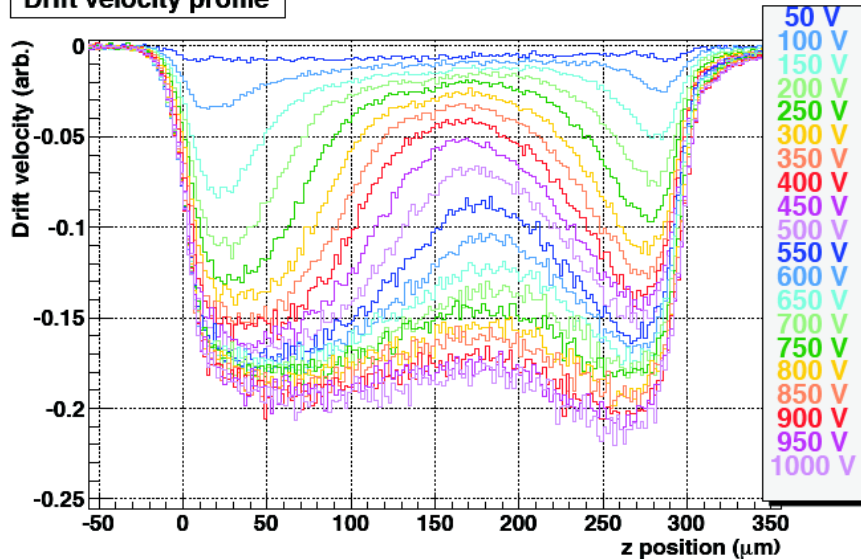


Annealing study: procedure

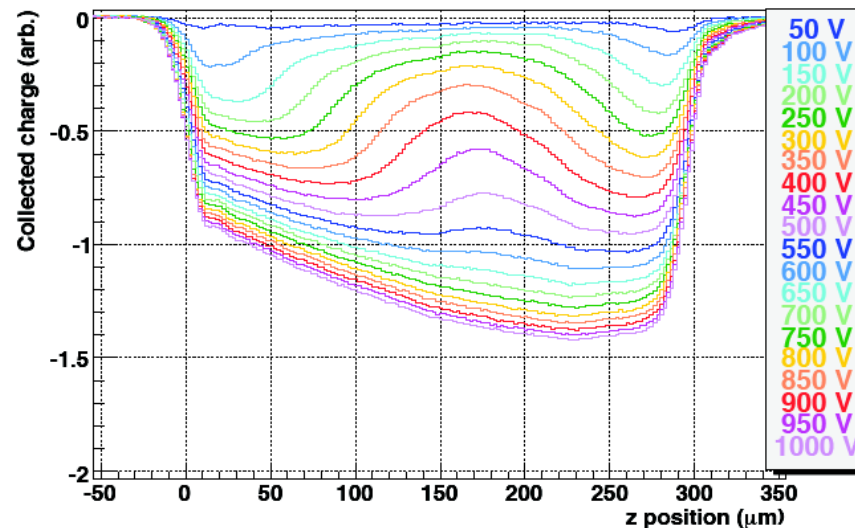
- ◆ After each annealing step devices were characterized with eTCT, for details on eTCT and related analysis see [1]
- ◆ Measurement temperature -25°C
- ◆ Drift velocity profile:
 - ◆ Integration window of 0.6ns from beginning of signal
- ◆ Efficiency profile:
 - ◆ Integration window of 25ns around the signal
- ◆ Annealing:
 - ◆ @ temperature 60°C
 - ◆ Up to maximum annealing time of 10^4min
 - ◆ On-board, without changing laser parameters (focusing distance, power, etc) → possible comparison between measurements on same detector

Annealing study: no annealing

Drift velocity profile

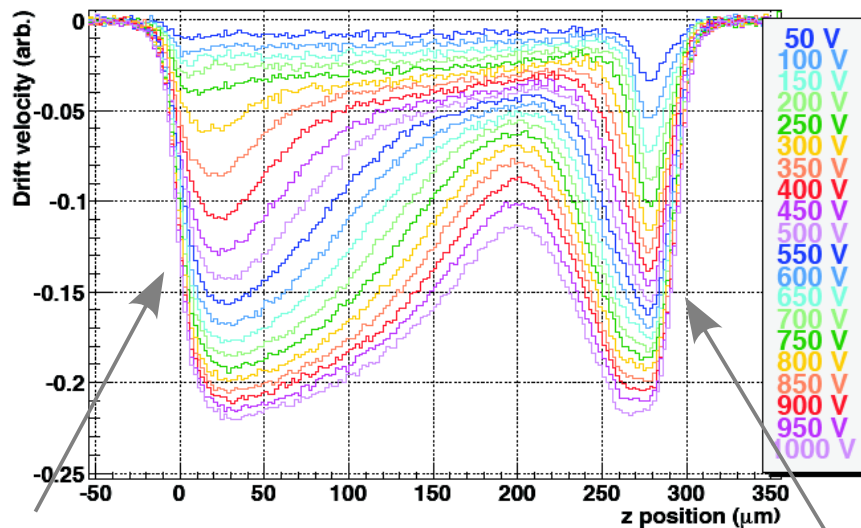


Efficiency scan of the detector

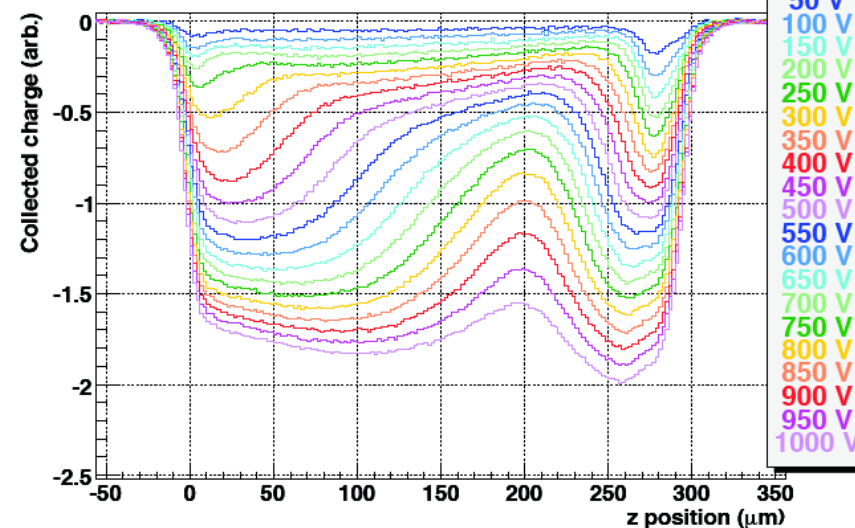


FZ

Drift velocity profile



Efficiency scan of the detector



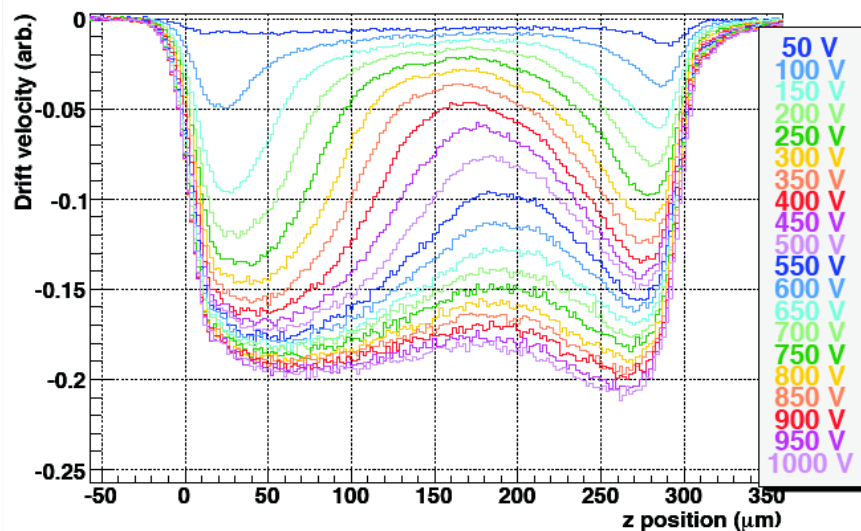
MCz

front

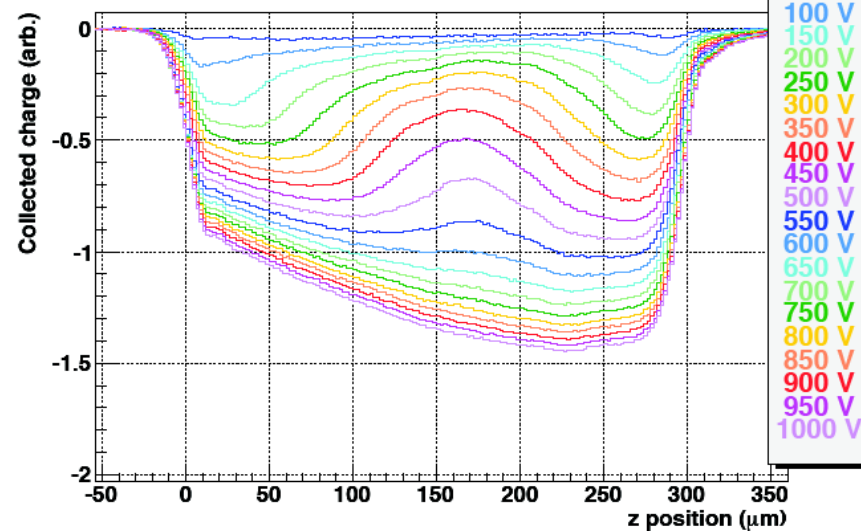
back

Annealing study: 80 min annealing

Drift velocity profile

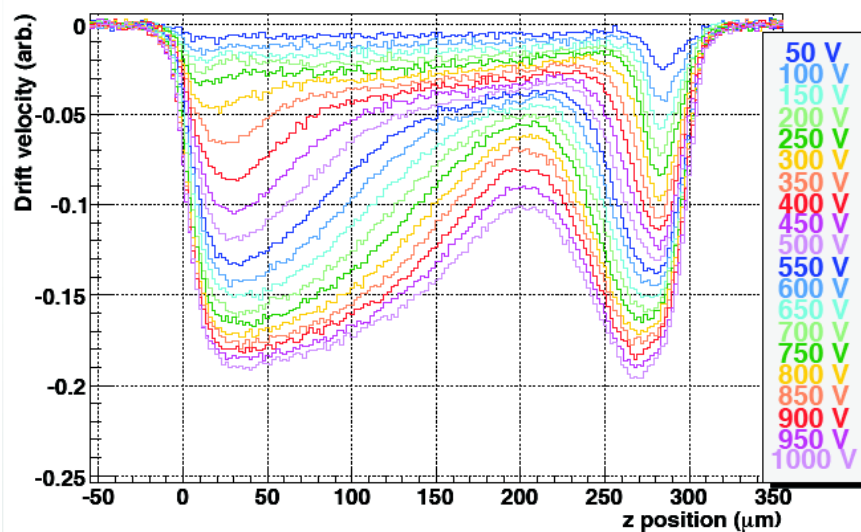


Efficiency scan of the detector

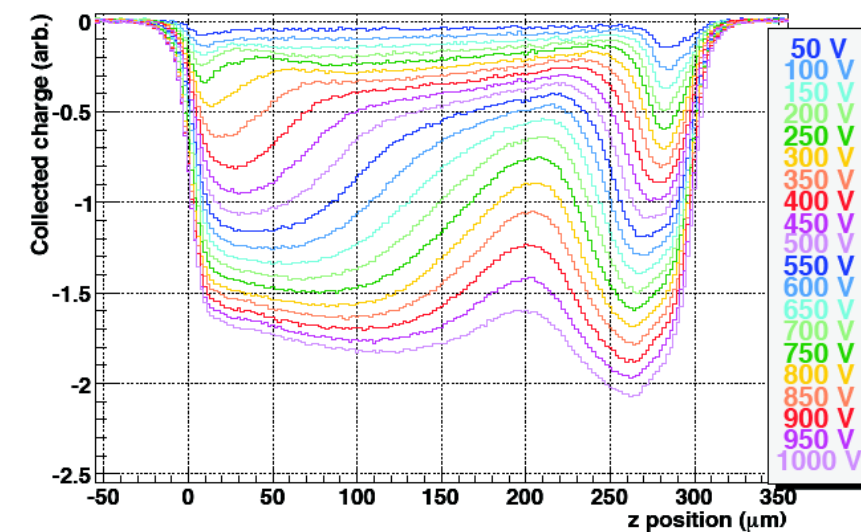


FZ

Drift velocity profile



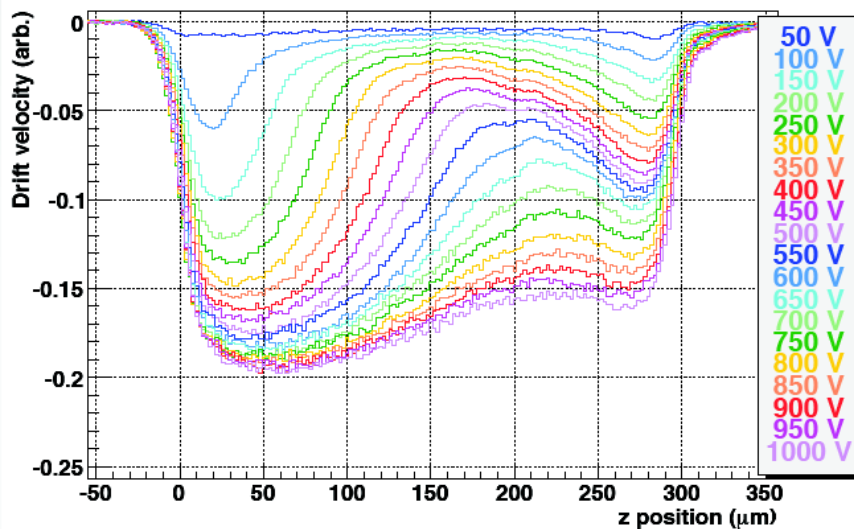
Efficiency scan of the detector



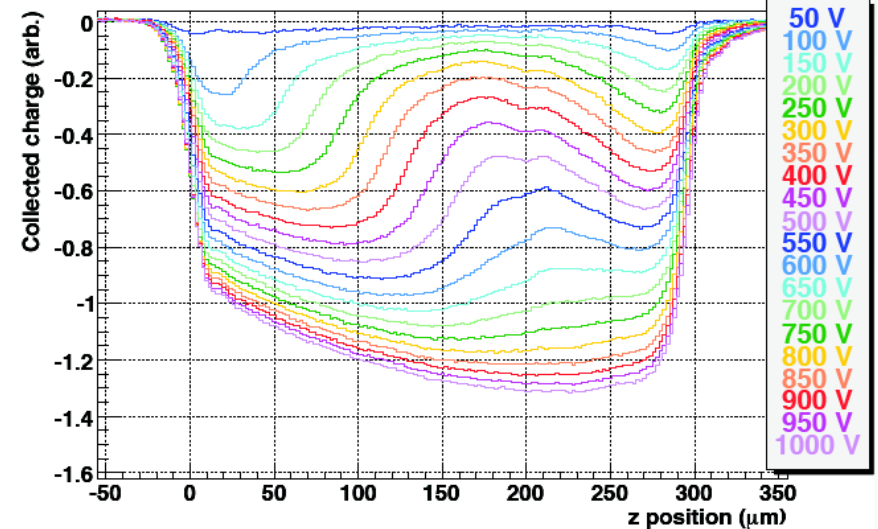
MCz

Annealing study: 240 min annealing

Drift velocity profile

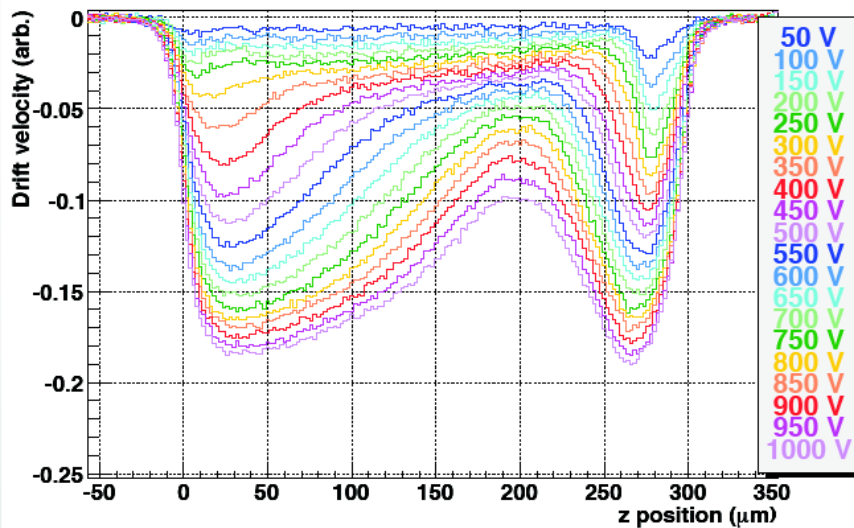


Efficiency scan of the detector

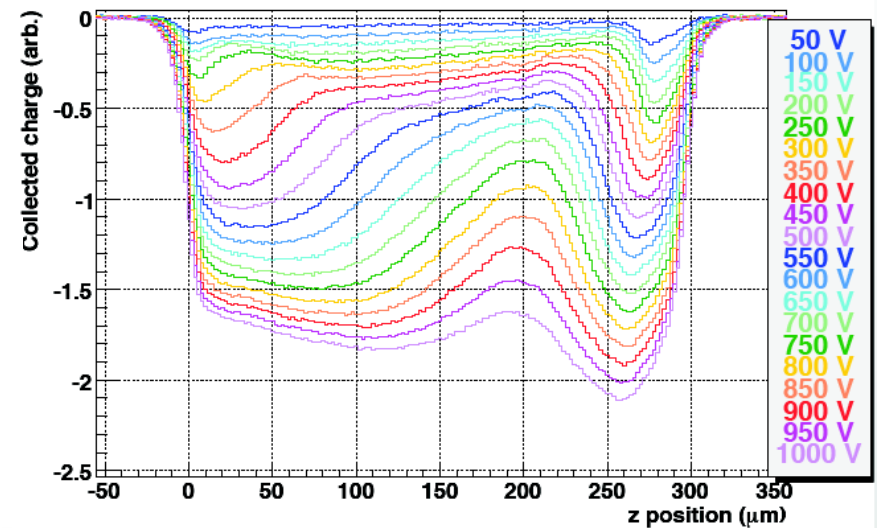


FZ

Drift velocity profile



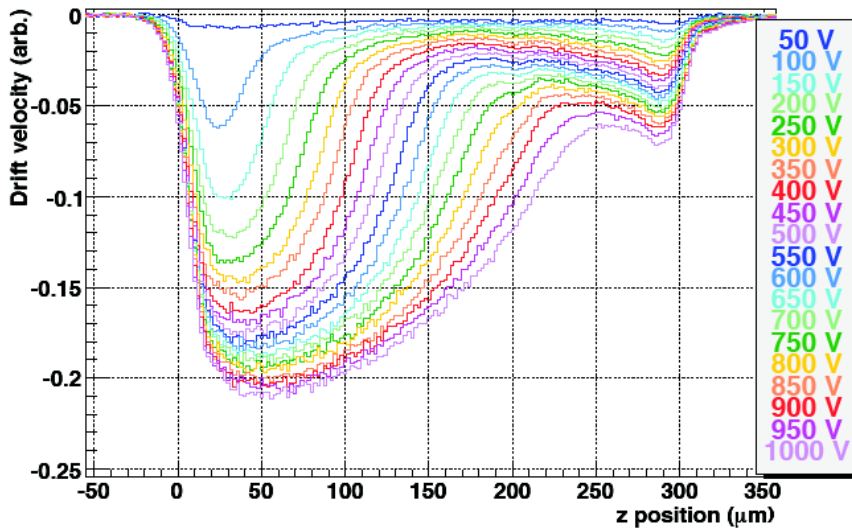
Efficiency scan of the detector



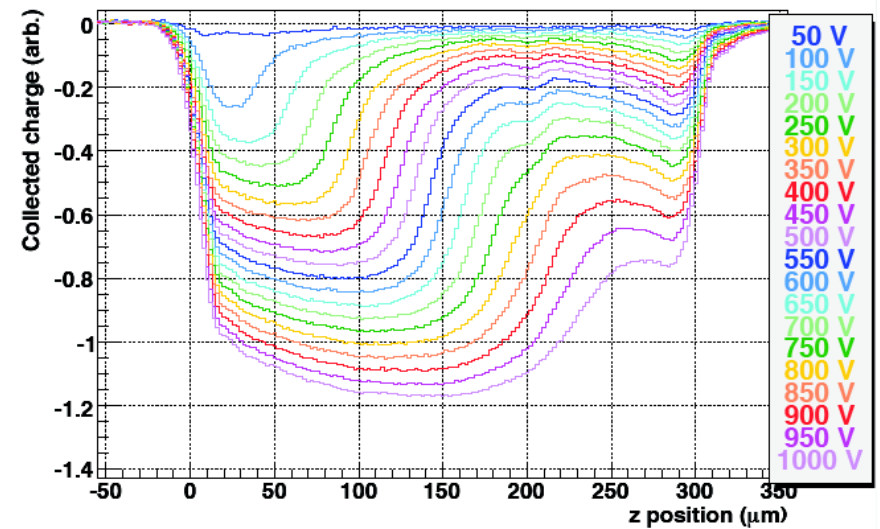
MCz

Annealing study: 560 min annealing

Drift velocity profile

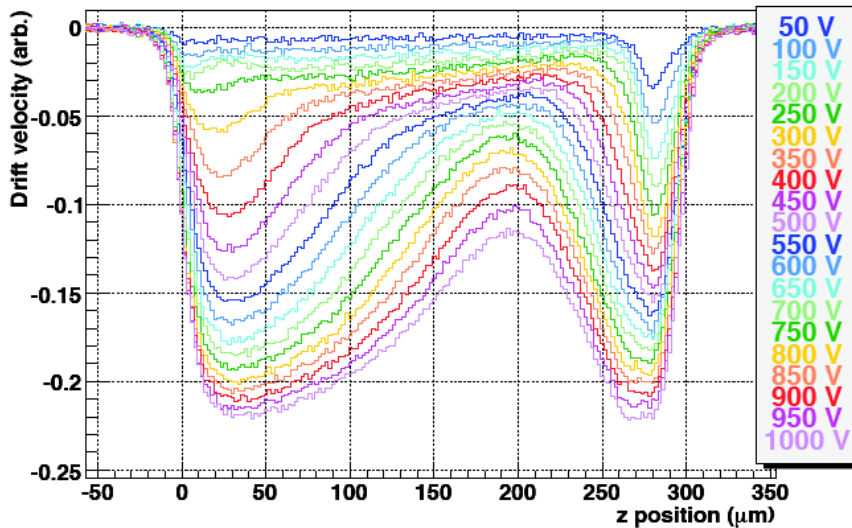


Efficiency scan of the detector

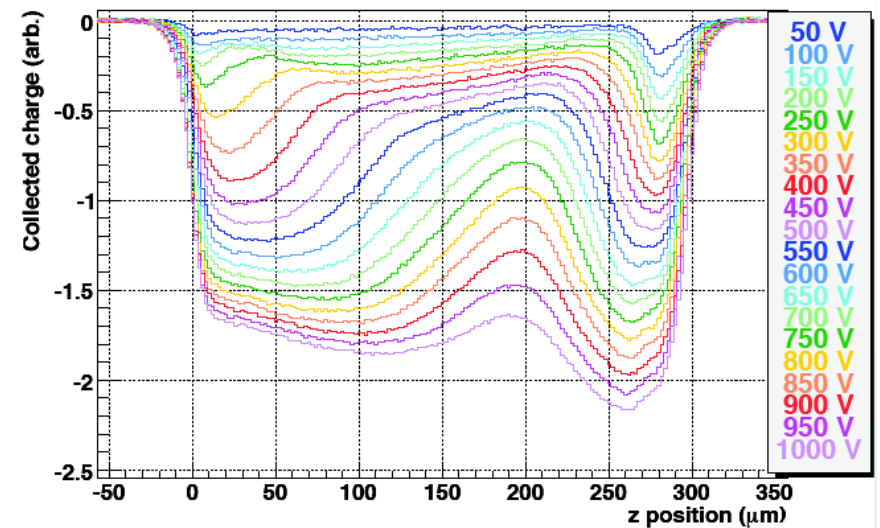


FZ

Drift velocity profile



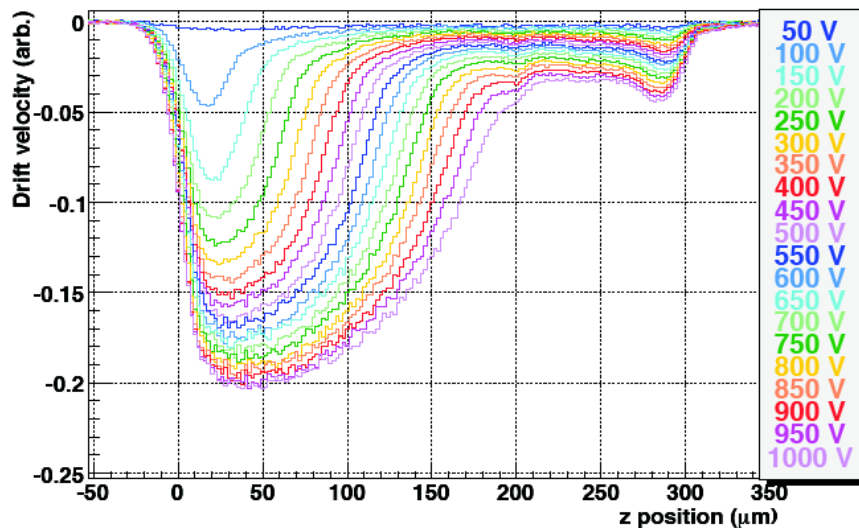
Efficiency scan of the detector



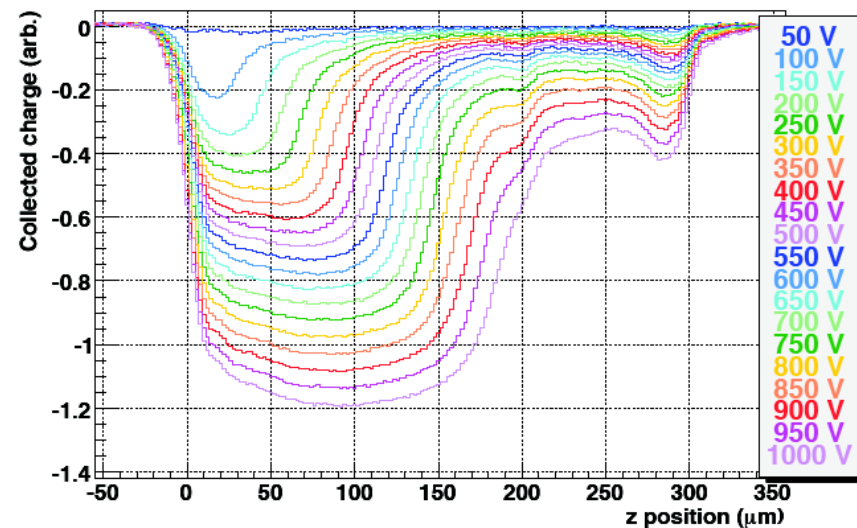
MCz

Annealing study: 1200 min annealing

Drift velocity profile

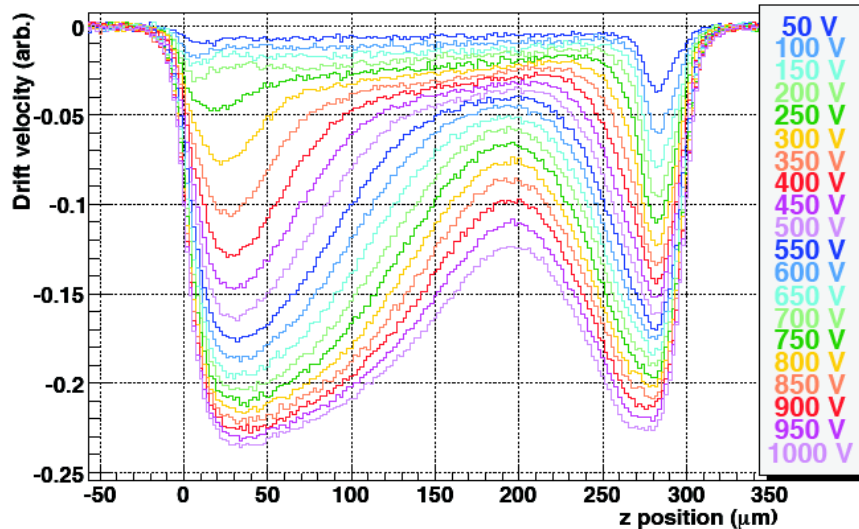


Efficiency scan of the detector

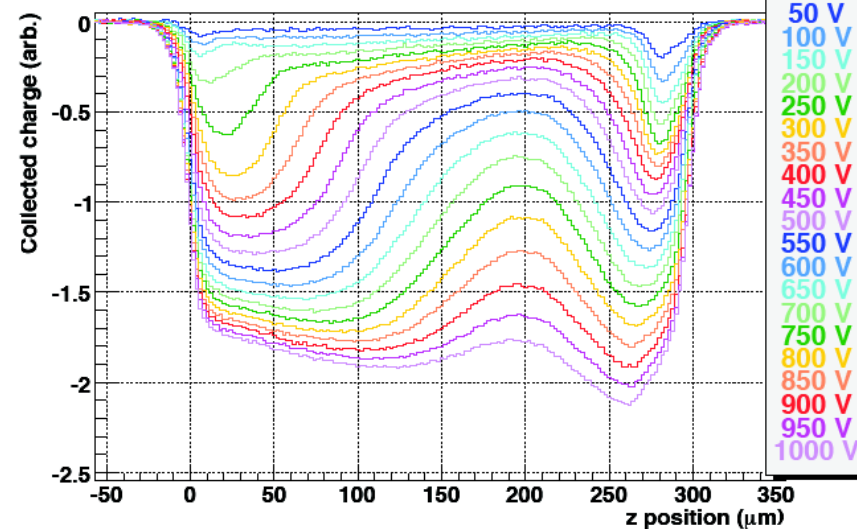


FZ

Drift velocity profile



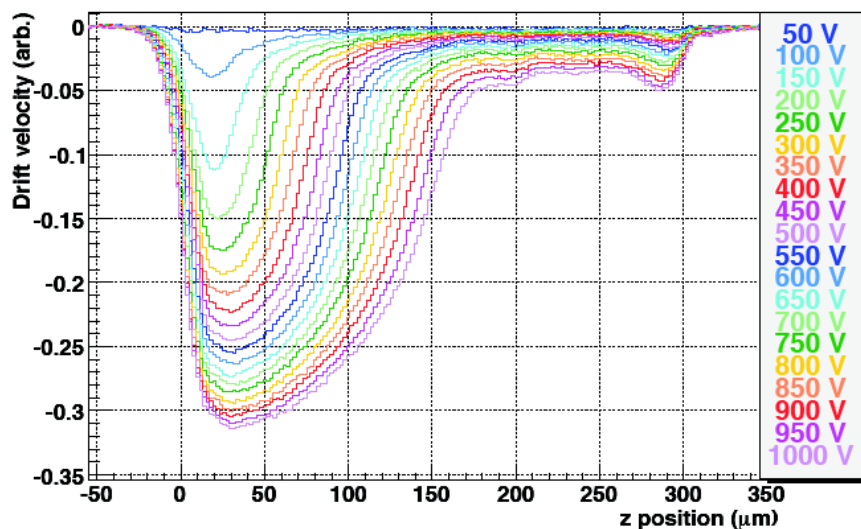
Efficiency scan of the detector



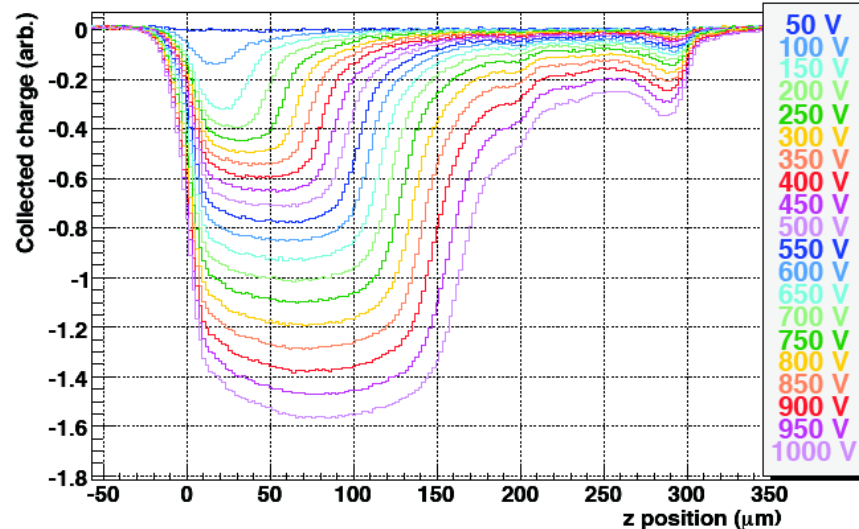
MCz

Annealing study: 2480 min annealing

Drift velocity profile

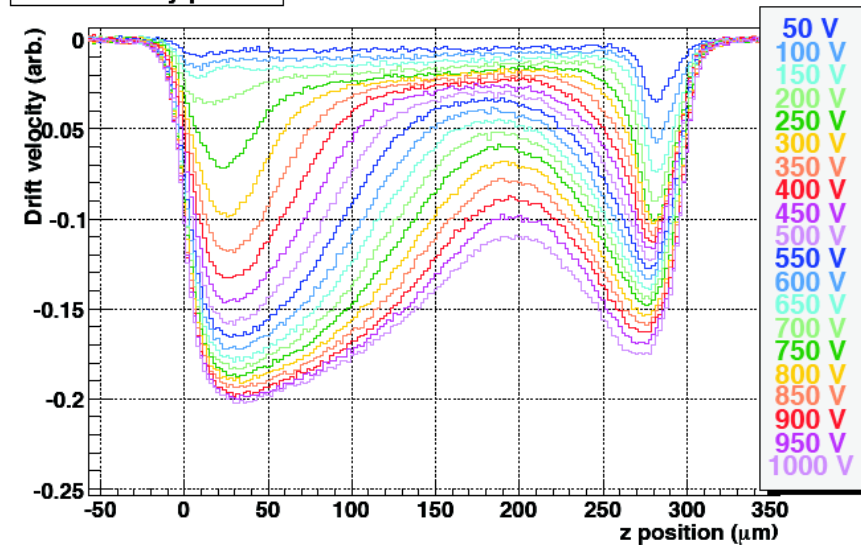


Efficiency scan of the detector

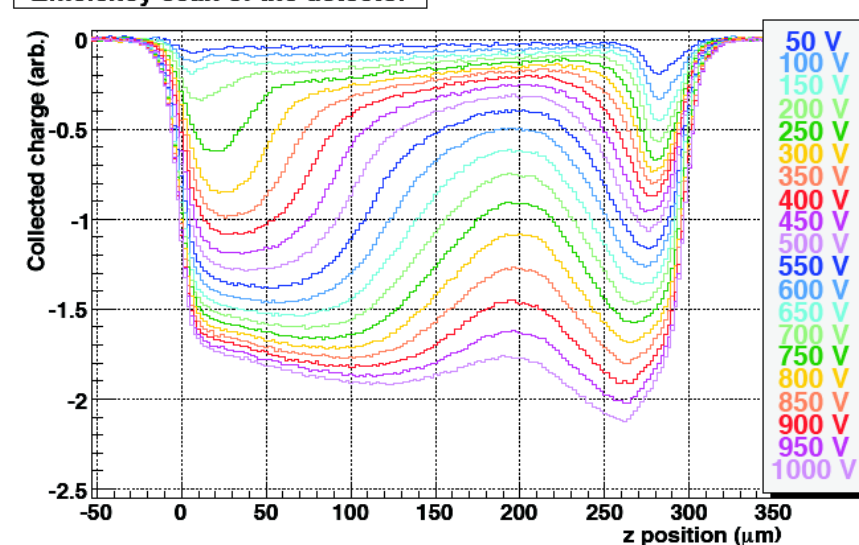


FZ

Drift velocity profile



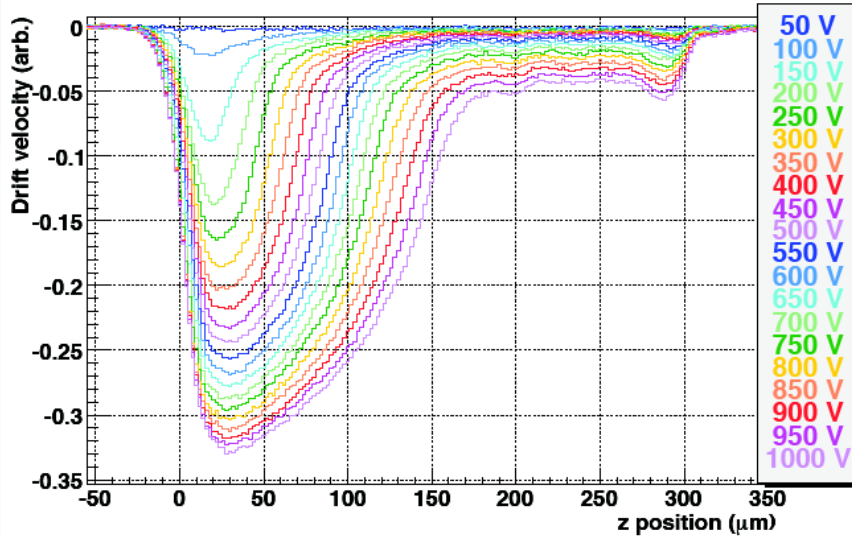
Efficiency scan of the detector



MCz

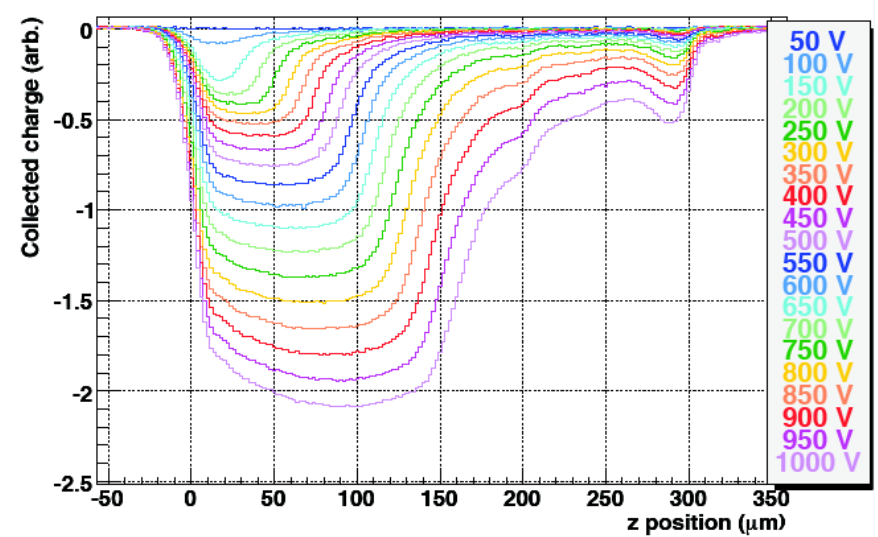
Annealing study: 5040 min annealing

Drift velocity profile

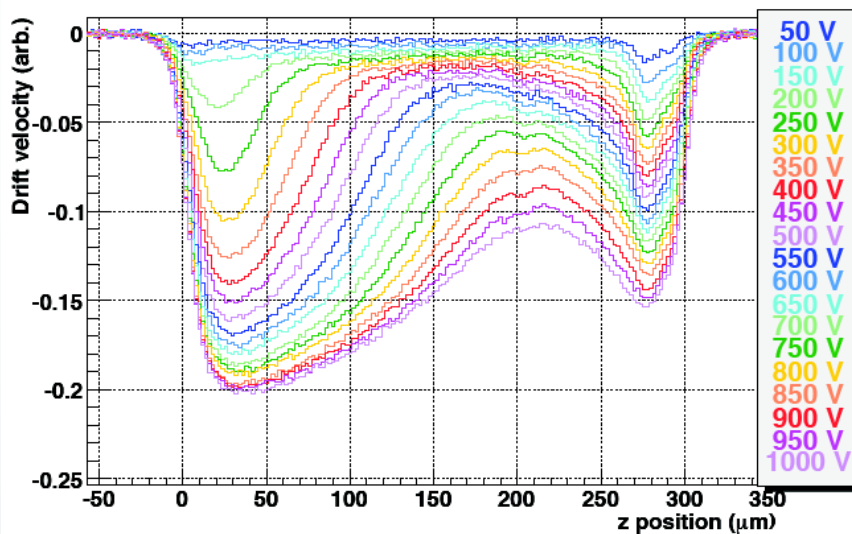


FZ

Efficiency scan of the detector

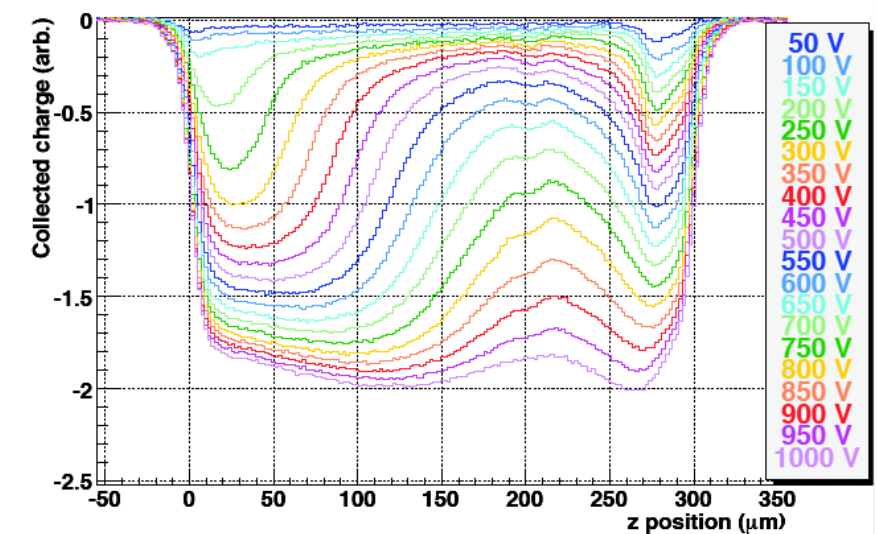


Drift velocity profile



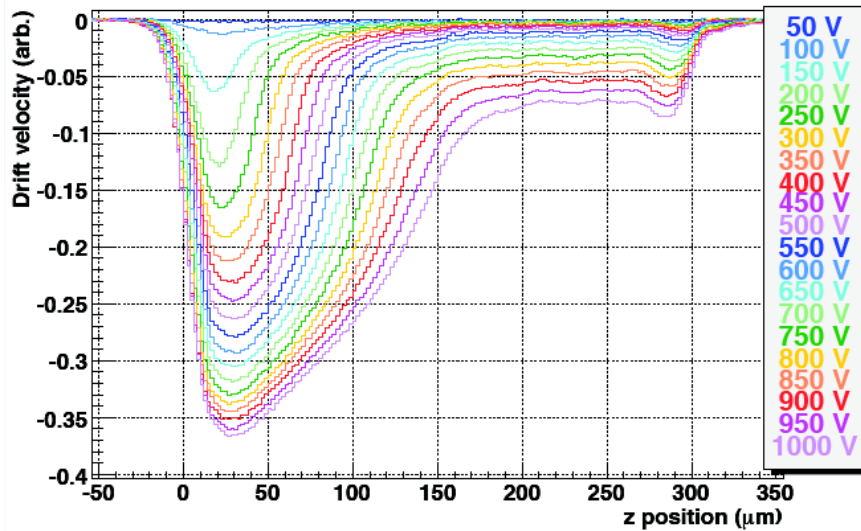
MCz

Efficiency scan of the detector

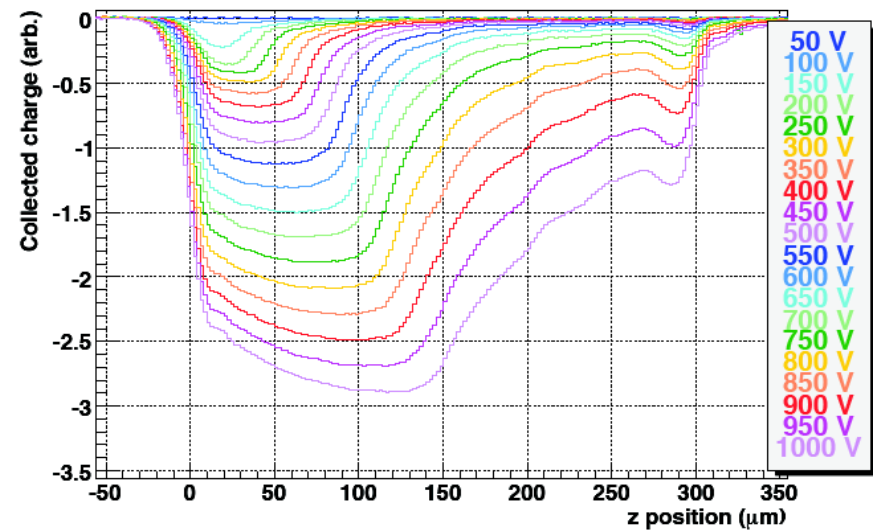


Annealing study: 10200 min annealing

Drift velocity profile

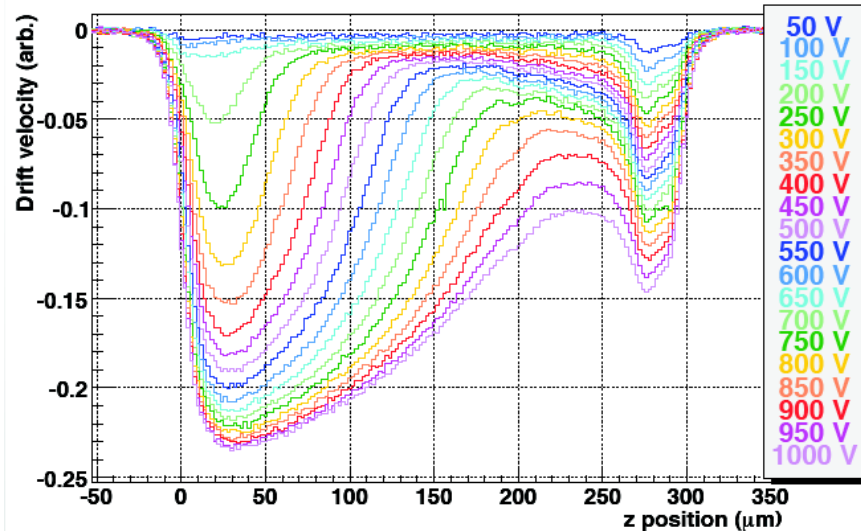


Efficiency scan of the detector

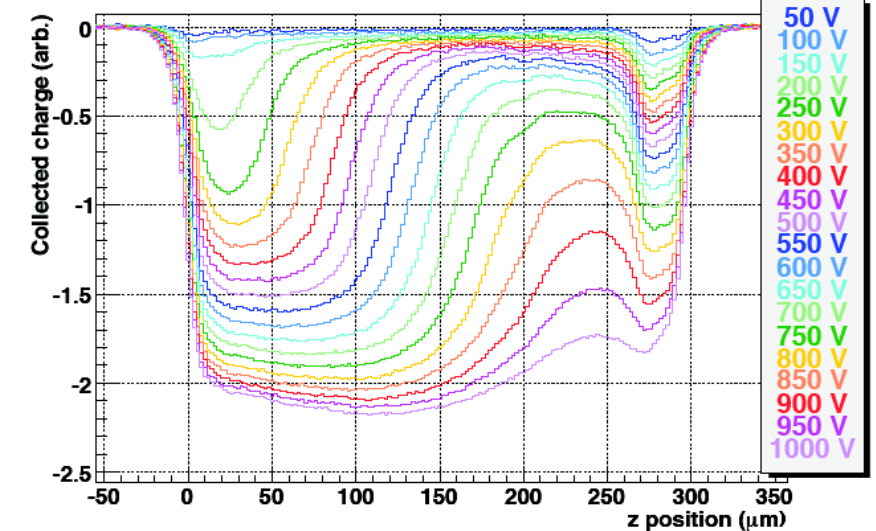


FZ

Drift velocity profile



Efficiency scan of the detector



MCz

Annealing study: comments

- ◆ Drift velocity profiles
 - ◆ Immediately after the irradiation for both FZ and MCz: double peak configuration with higher peak on the back → indication of introduction of donor like defects
 - ◆ Decrease of the field strength on the back with annealing, field concentrated on the front → introduction of acceptor like defects with annealing
 - ◆ Shapes for FZ and MCz comparable at end of annealing
 - ◆ Before annealing lower field in the central more pronounced for MCz than for FZ → lower introduction rate of space charge with irradiation in FZ, which is then compensated with annealing when the net acceptor introduction rate appears to be higher

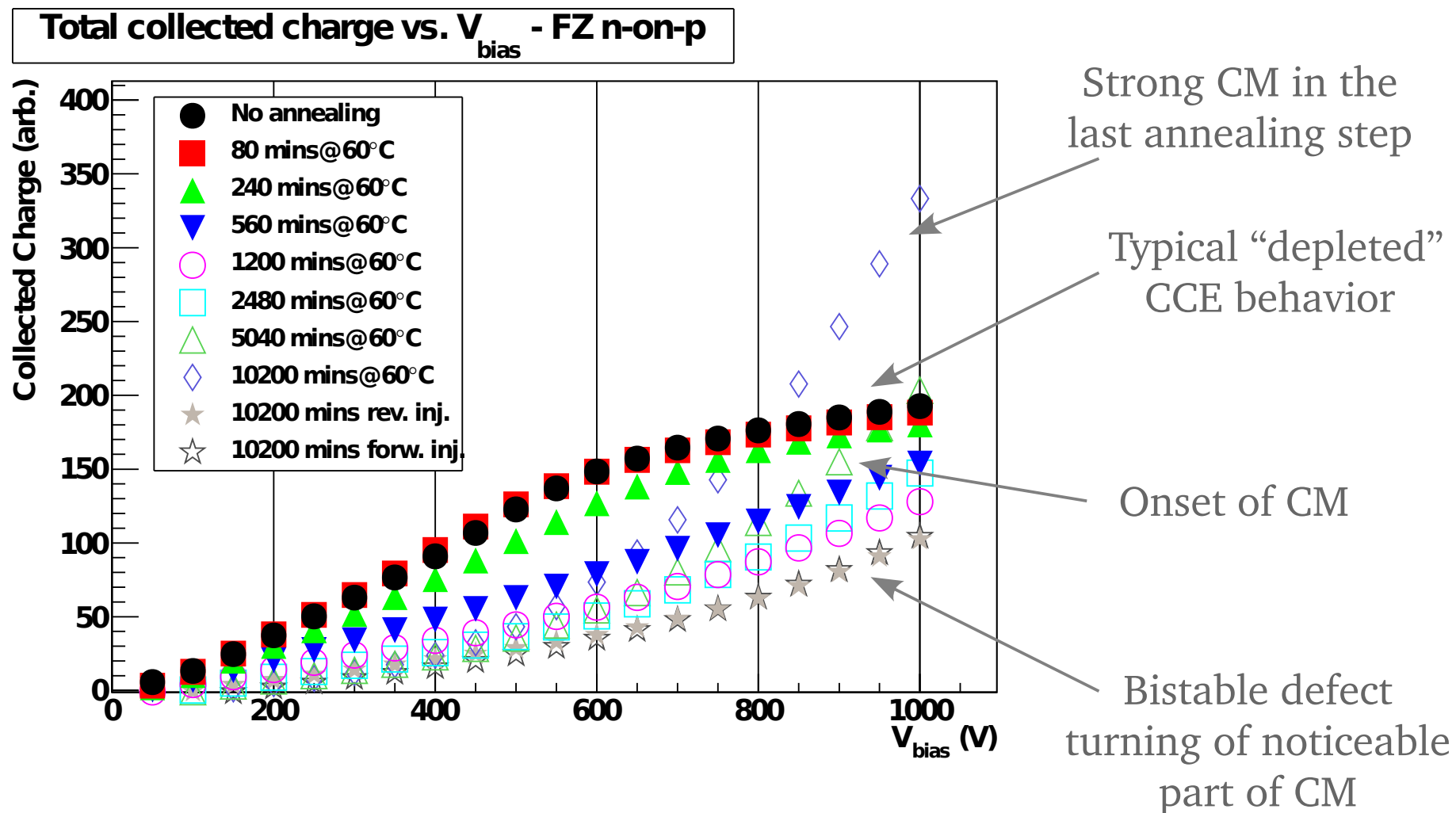
- ◆ Efficiency profiles:
 - ◆ Prior to annealing: region with maximum efficiency close to back side for both FZ and MCz (slightly higher field on the back)
 - ◆ FZ
 - ◆ Decrease of active region width with annealing up to annealing 5040min annealing step
 - ◆ After 5200 min step: increase of collected charge value, more prominent close to the back → onset of charge multiplication of electrons traveling towards front
 - ◆ Mcz
 - ◆ Almost no change up to to the last annealing step where detector starts to be more efficient in front

Annealing study: CM “quenching” in FZ

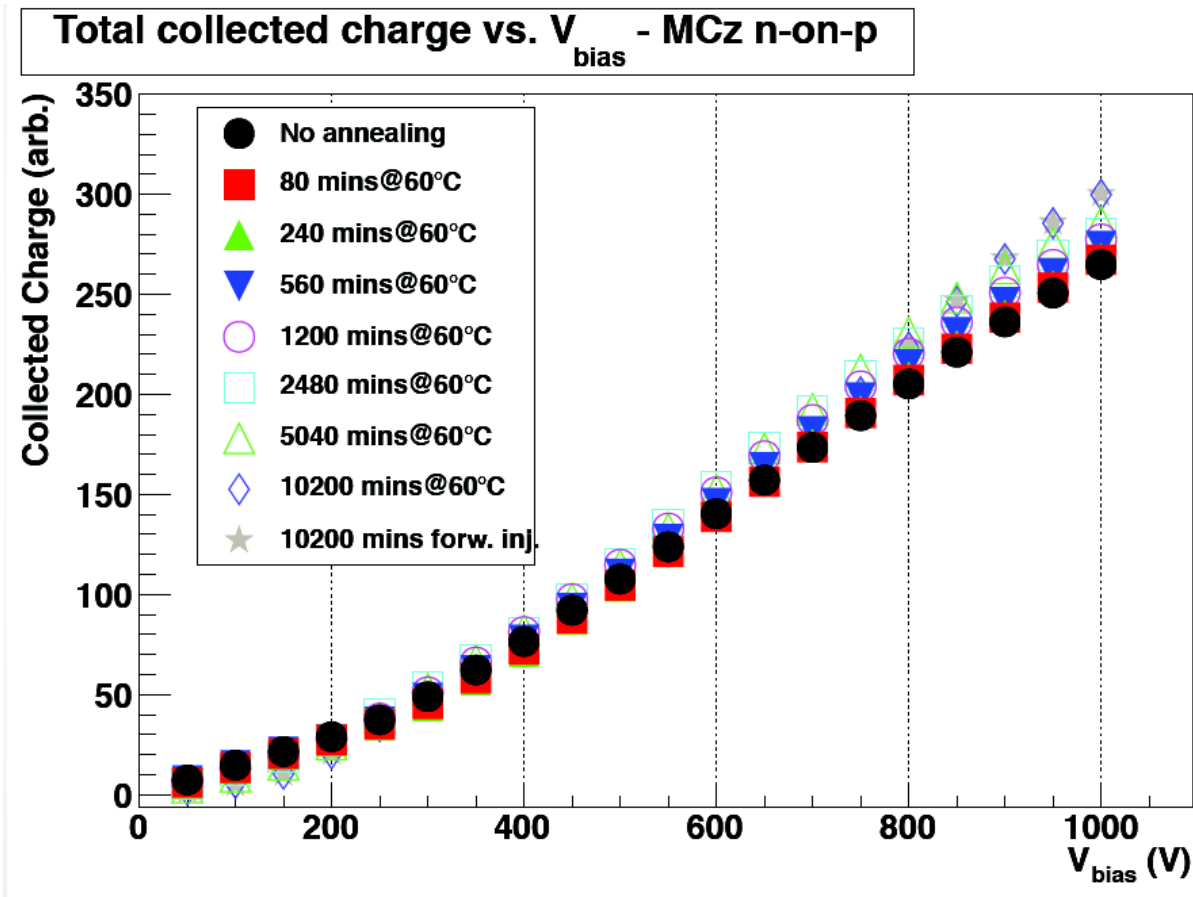
- ◆ After 10200min of annealing, FZ was observed to develop “memory”...
- ◆ Charge multiplication “turned off” by high current injection, performed either with forward injection at low temperature or reverse at high temperature ($\sim 700\mu\text{A}$), plots on the next slide
- ◆ The effect can be reversed by leaving the detector at room temperature over night
- ◆ The defect(s) can stay in its active state for more than 2 days at -25C ...
- ◆ An explanation for slow de-excitation rate could lie in the change of chemical configuration of defect (bistable behavior)

Annealing study: Total charge collected, FZ

Total collected charge (integral of efficiency profile over z) as function of bias



Annealing study: Total charge collected, MCz



- ◆ Annealing seems to have little influence
- ◆ No evidence of CM
- ◆ No evidence of bistable defect

Summary (part 1)

Trapping time extraction from eTCT measurements

- ◆ 2 methods proposed
 - 1) Comparison of measured and calculated signals at the edges of detector
 - 2) Comparison of measured and calculated efficiency profiles
- ◆ Both seem to have troubles close to the detector edges...

- ◆ Future plans:
 - ◆ Check modeling of laser beam
 - ◆ Try method 1) for number of positions in the middle of detector
 - ◆ Try method 2) but exclude regions close to edges when comparing measured/calc. Signal

Summary (part 2)

eTCT measurements at several annealing steps of FZ and MCz p-type strip detectors irradiated to $\Phi = 10^{16} \text{p/cm}^2$

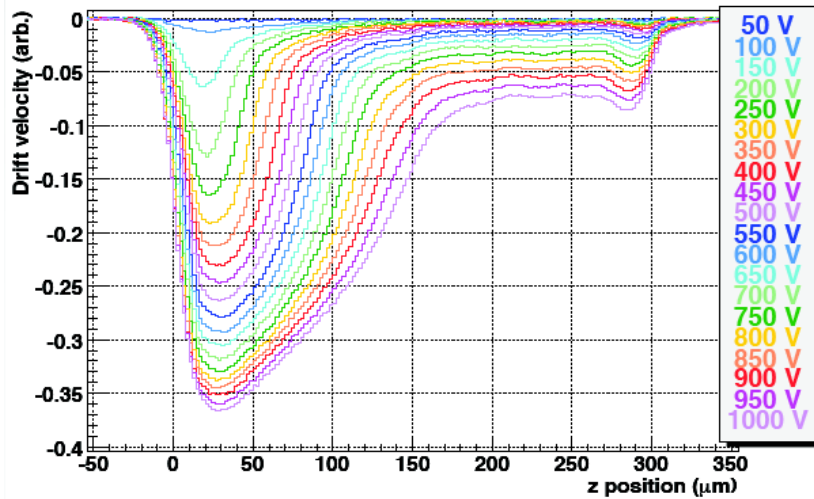
- ◆ FZ:
 - ◆ Devices show double junction field configuration
 - ◆ Acceptor introduction with annealing, at higher annealing times virtually all the field is concentrated in the front
 - ◆ Onset of charge multiplication
 - ◆ Bistable defect observed, decreasing both charge multiplication

- ◆ MCz by far less sensitive to annealing:
 - ◆ Collected charge almost unaffected even at higher annealing times
 - ◆ No evidence of charge multiplication
 - ◆ No bistable defect observed – most probably high O concentrations are gettering the defect observed in FZ

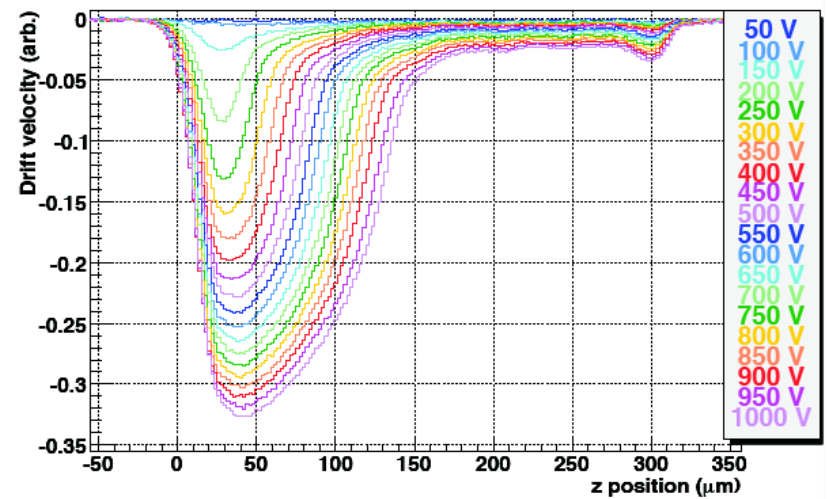
Back up
slides

eTCT measurements: CM “quenching” in FZ

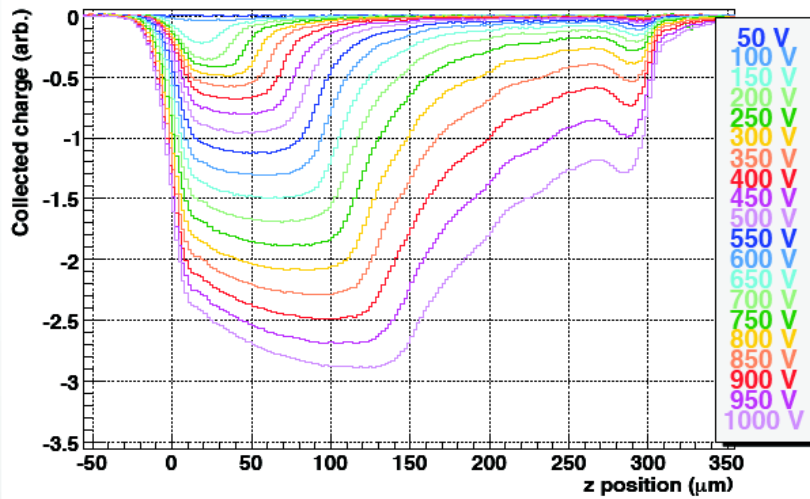
Drift velocity profile



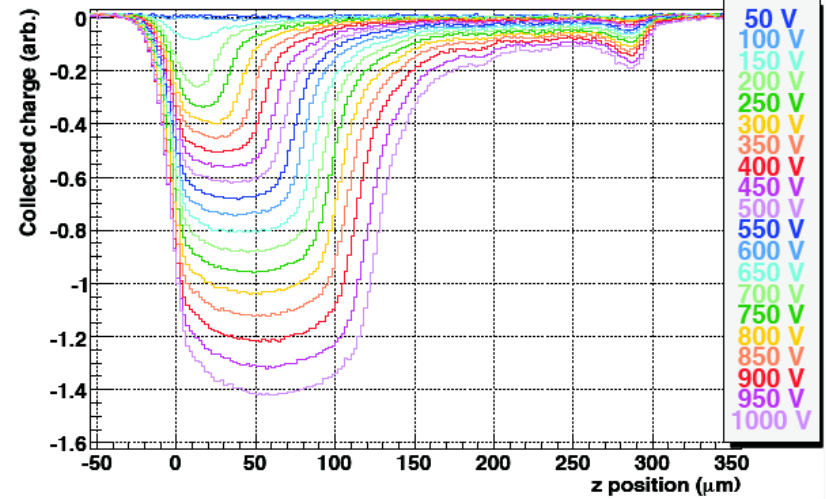
Drift velocity profile



Efficiency scan of the detector



Efficiency scan of the detector



Immediately
after annealing

After $\sim 700 \mu\text{A}$
forward injection

Collected Charge vs. Annealing time

