

On the nature of the 4th family ν

(in collaboration with A. Aparici, N. Rius and A. Santamaría)

[JHEP 1207 (2012) 030, arXiv:1204.1021 [hep-ph]]

J. Herrero-García

IFIC, Universidad de Valencia - CSIC

Across the TeV frontier with the LHC

Cargese, 27 August 2012

The nature of neutrino mass

- DIRAC: Add ν_R (≥ 2) and impose a global symmetry like $B - L$. No explanation for the smallness m_ν , with tiny Yukawas, 6 (11) orders of magnitude smaller than the electron (top) one.
- MAJORANA, parametrized by the Weinberg oper.:

$$\mathcal{L}_5 = -\frac{1}{2} \frac{c_{\alpha\beta}}{\Lambda_W} (\overline{\ell_\alpha \tilde{\phi}}) (\phi^\dagger \tilde{\ell}_\beta) + \text{H.c.},$$

where $\tilde{\ell} = i\tau_2 \ell^c$ and $\Lambda_W \gg v_\phi$ is the scale of NP.

- Upon EW SSB, it leads to:

$$m_\nu = c \frac{v_\phi^2}{\Lambda_W},$$

with $\langle \phi \rangle = v_\phi = 174$ GeV. Example: SSI, ν_R with $M \gg m_D$:

$$m_\nu \simeq -m_D M^{-1} m_D^T.$$

Fourth generation neutrino masses

- Lower bounds on $m_{\nu 4} \equiv m_4$ are (in GeV):
 - 1 Unstable (LEP II): $m_4 > 80.5$ (M), 90.3 (D), 62.1 (both).
 - 2 Stable (inv. Γ_Z): $m_4 > 39.5$ (M), 45 (D), 33.5 (both).

Fourth generation neutrino masses

- Lower bounds on $m_{\nu 4} \equiv m_4$ are (in GeV):
 - 1 Unstable (LEP II): $m_4 > 80.5$ (M), 90.3 (D), 62.1 (both).
 - 2 Stable (inv. Γ_Z): $m_4 > 39.5$ (M), 45 (D), 33.5 (both).

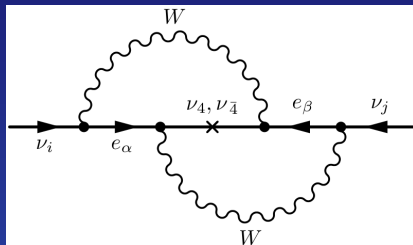
Conclusion:

- One needs at least one ν_R which has standard Yukawa couplings to the doublets to give mass to ν_4 .
- In general, a m_R for the 4th gen. ν_R is allowed by symmetry, and naturality arguments set a lower bound for it (unless some symmetry for the 4th gen. is invoked).

$$\mathcal{L}_Y = -\bar{\ell} Y_e \mathbf{e}_R \phi - \bar{\ell} y \nu_R \tilde{\phi} - \frac{1}{2} \overline{\nu_R^c} m_R \nu_R - \frac{1}{2\nu_\phi^2} (\bar{\ell} \tilde{\phi}) m_L (\phi^\dagger \tilde{\ell}) + \text{H.c.},$$

where ℓ and \mathbf{e}_R have 4 gen. comp., Y_e is 4×4 , y is a 4 comp. column vector, m_R is a number and m_L is complex symm. 4×4 .

Light neutrino masses induced by the extra family

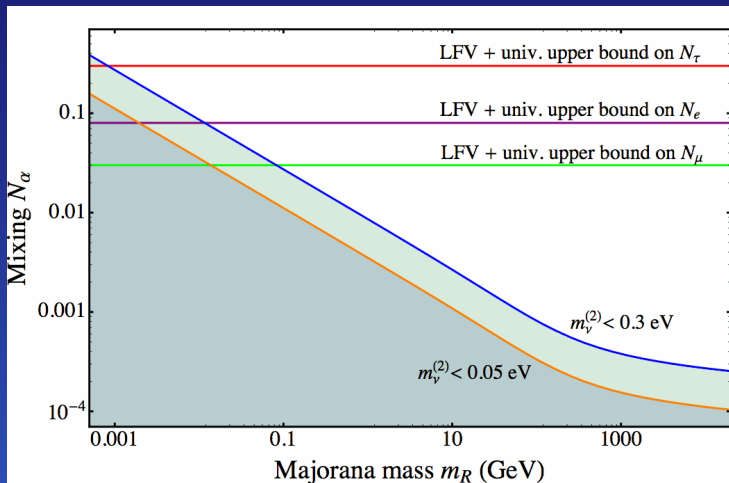


Two-loop corrections induced by the 4th gen. fermions generate light m_ν even if they were not present at tree level:

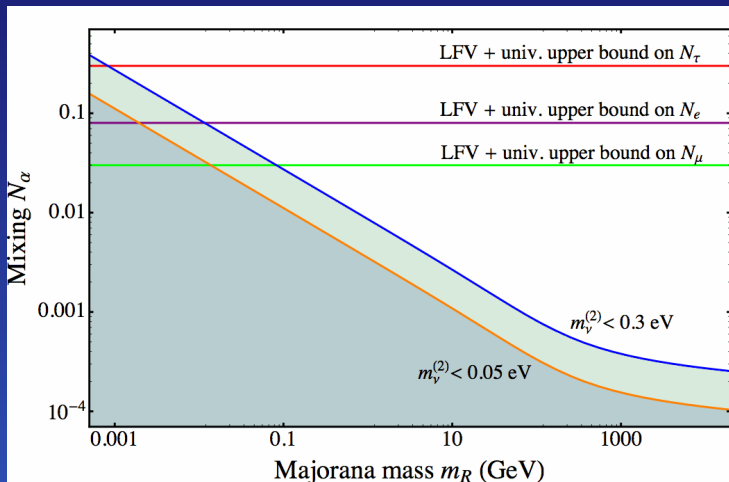
$$(m_\nu)_{ij}^{(2)} = -\frac{g^4}{m_W^4} m_R m_D^2 \sum_\alpha V_{\alpha i} V_{\alpha 4} m_\alpha^2 \sum_\beta V_{\beta j} V_{\beta 4} m_\beta^2 I_{\alpha\beta},$$

where the sums run over the charged leptons $\alpha, \beta = e, \mu, \tau, E$ while $i, j = 1, 2, 3$, and $I_{\alpha\beta}$ is a loop integral.

Light neutrino mass bound



Light neutrino mass bound



Conclusion:

Light neutrino masses give the strongest bound on the mixings.

- σ_H through gg fusion at LHC is enhanced by a factor of 9.
- Some Higgs decay channels behave very differently.
- To distinguish and discover/exclude one must look to $\sigma_H \cdot B_r$, for example, to the $\gamma\gamma$ and WW channels, which are very different for SM3 and SM4.
- If ν_4 's are light enough ($m_W/2 \lesssim m_{4,\bar{4}} \lesssim m_W$), the decay mode of the Higgs into ν_4 's can be dominant.
- However, with a SM-like Higgs, fourth generation is excluded: there may be ways out modifying the scalar sector, for instance, with an extra Higgs doublet.

Summary and conclusions

- 1 We have considered the case where light ν are Majorana, so their tiny mass is naturally understood.
- 2 If a 4th generation exists, at least one ν_R is needed.

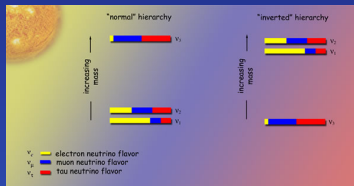
→ 1) + 2) imply that the ν_R should naturally have a Majorana mass m_R whose size ($\lesssim \text{TeV}$) depends on the LNV mechanism (if set $m_R = 0$ at tree level, it is generated at 2-loops).

- We have analyzed the phenomenology of the minimal 4G scenario: universality, charged LFV processes and $0\nu\beta\beta$.
- Strongest constraint: the 4th generation induces two-loop contributions to the light m_ν , which can easily exceed the atmospheric or the cosmological scale.
- Simplest 4th generation with SM Higgs now excluded.

BACK-UP SLIDES

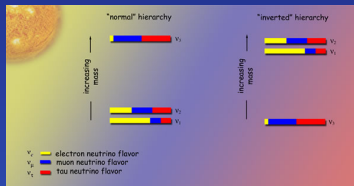
Introduction: light neutrino masses ask for new physics

- From cosmology $\sum m_\nu \lesssim 1$ eV, but scale is unknown.
- From oscillation experiments, the possible hierarchies are:
 - 1 NH (if $m_1 = 0$): $m_3 \approx 0.05$ eV & $m_2 \approx 0.01$ eV.
 - 2 IH (if $m_3 = 0$): $m_2 \approx 0.05$ eV & $m_1 \approx 0.04$ eV.
 - 3 Quasi-degenerate: $m_1 \simeq m_2 \simeq m_3 \lesssim 0.3$ eV $\sim 10^{-6} m_e$.



Introduction: light neutrino masses ask for new physics

- From cosmology $\sum m_\nu \lesssim 1$ eV, but scale is unknown.
- From oscillation experiments, the possible hierarchies are:
 - 1 NH (if $m_1 = 0$): $m_3 \approx 0.05$ eV & $m_2 \approx 0.01$ eV.
 - 2 IH (if $m_3 = 0$): $m_2 \approx 0.05$ eV & $m_1 \approx 0.04$ eV.
 - 3 Quasi-degenerate: $m_1 \simeq m_2 \simeq m_3 \lesssim 0.3$ eV $\sim 10^{-6} m_e$.



New physics is needed (in SM neutrinos are massless):

- Many models have been proposed (see later).
- Here we study the ν sector in the presence of a 4th family.

Seesaw type II (SS II)

- Add to the SM one scalar triplet with hypercharge $Y = 1$ and $L = -2$. In the doublet representation of $SU(2)_L$ the triplet is a 2×2 matrix:

$$\chi = \begin{pmatrix} \chi^+/\sqrt{2} & \chi^{++} \\ \chi_0 & -\chi^+/\sqrt{2} \end{pmatrix}$$

Gauge invariance allows a Yukawa coupling of the scalar triplet to 2 lepton doublets,

$$\mathcal{L}_\chi = - \left((Y_\chi)_{\alpha\beta} \tilde{\ell}_\alpha \chi \ell_\beta + \text{H.c.} \right) - V(\phi, \chi),$$

where Y_χ is a symmetric matrix and $\tilde{\ell} = i\tau_2 \ell^c$. The scalar potential has the following terms:

$$V(\phi, \chi) = m_\chi^2 \text{Tr}[\chi\chi^\dagger] + \left(\mu \tilde{\phi}^\dagger \chi^\dagger \phi + \text{H.c.} \right) + \dots$$

- The μ coupling violates L and induces a VEV for the triplet via v_ϕ , even if $m_\chi > 0$. In the limit $m_\chi \gg v_\phi$:

$$m_\nu = 2Y_\chi v_\chi = 2Y_\chi \frac{\mu v_\phi^2}{m_\chi^2}$$

- m_ν are thus proportional to both Y_χ and μ , since the breaking of L results from their simultaneous presence.
- If m_χ^2 is positive and large, v_χ will be small, in agreement with the ρ parameter, $v_\chi \lesssim 6$ GeV.
- Moreover, μ can be naturally small, because in its absence L is recovered, increasing the symmetry.

Seesaw type III (SS III)

- The SM is extended by fermion $SU(2)_L$ triplets Σ_i with $Y = 0$ (at least 2).

The new terms in the Lagrangian are given by:

$$\mathcal{L}_\Sigma = i \text{Tr} [\bar{\Sigma} \gamma^\mu D_\mu \Sigma] - \left(\frac{1}{2} \text{Tr} [\bar{\Sigma} M \Sigma^c] + \sqrt{2} Y_{\alpha\beta} \bar{\ell}_\alpha \Sigma_\beta \tilde{\phi} + \text{H.c.} \right),$$

where Y is the Yukawa coupling of the fermion triplets to the SM lepton doublets and the Higgs and M their Majorana mass matrix, which can be chosen to be diagonal and real.

After SSB the neutrino mass matrix can be written as

$$\mathcal{L}_{\nu \text{ mass}} = -\frac{1}{2} (\overline{\nu_L} \quad \overline{\Sigma_0^c}) \begin{pmatrix} 0 & m_D \\ m_D^T & M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \Sigma_0 \end{pmatrix} + \text{H.c.},$$

and leads to a light neutrino Majorana mass matrix

$$m_\nu \simeq -m_D M^{-1} m_D^T$$

However, since the triplet has also charged components with the same Majorana mass, there are stringent lower bounds:

$$M \gtrsim 100 \text{ GeV}$$

Other mechanisms

- Induced by radiative corrections. On top of loop factors $1/(4\pi)^2$, there can be extra suppressions due to couplings or ratios of masses, so Λ_{NP} can be EW scale.
- Supersymmetry by R-parity breaking. The SM doublet neutrinos mix with the neutralinos. Majorana masses for ν 's (generated at tree level and at one loop) are naturally small because they are proportional to the small R-parity-breaking parameters.

Fourth generation neutrino masses

- Lower bounds on $m_{\nu_4} \equiv m_4$ are (in GeV):
 - 1 Unstable (LEP II): $m_4 > 80.5$ (M), 90.3 (D), 62.1 (both).
 - 2 Stable (inv. Γ_Z): $m_4 > 39.5$ (M), 45 (D), 33.5 (both).

Possible mechanisms:

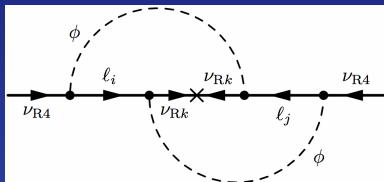
- 1) **Dirac**: quite natural for ν_4 as long as L is conserved. However, this is not the case if the light ν are Majorana (as in most of models) where they can mix with the 4th family.
- 2) **Weinberg Operator**: masses $\mathcal{O}(v_\phi^2/\Lambda_W)$ which should be $\gtrsim m_Z/2$, so Λ_W can not be $\gg v_\phi$ and the effective theory does not provide a useful parametrization.

Fourth generation neutrino masses

- 3) **Seesaw type I:** if $m_R \gg m_D$, $m_4 \sim m_D^2/m_R$, which must be heavier than $\sim m_Z/2$. Therefore $m_R < m_D^2/m_Z$, so m_R cannot be \gg EW scale. If $m_R \ll m_D$ there are 2 almost degenerate ν (PD limit), which is OK.
- 4) **Seesaw type II:** $v_\chi \lesssim 6$ GeV will yield ν_4 masses too small. Not viable.
- 5) **Seesaw type III:** the charged fermions must be > 100 GeV, so the PD limit is not possible. These new fermions have to be \lesssim few TeV, so it is viable but much more constrained than type I.
- 6) **Others:** radiative mechanisms and SUSY with broken R parity. m_ν in these models are strongly suppressed with respect to the EW scale by either loop factors, couplings and/or ratios of masses. Not viable.

Natural fourth generation neutrino masses in SS I

- Suppose SS I for light neutrino masses, and we have ν_{R4} .
- Is it stable under radiative corrections to set $m_{R4} = 0$, given that m_{R4} does not increase the symmetry?



Above the m_{Rk} scale, m_{R4} and m_{Rk} mix under renormalization. Even if $m_{R4} = 0$ at some scale $\Lambda_C > m_{Rk}$, m_{R4} will be generated by running from Λ_C to m_{Rk} . Barring accidental cancellations, one should require:

$$m_{R4} \gtrsim \frac{1}{(4\pi)^4} \sum_{ijk} Y_{i4} Y_{ik}^* m_{Rk} Y_{jk}^* Y_{j4} \ln(\Lambda_C/m_{Rk})$$

where $i, j = 1, 2, 3, 4, k = 1, 2, 3$.

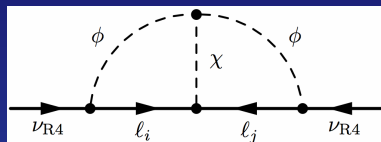
Natural fourth generation neutrino masses in SSI

As $(m_\nu)_{ij} \sim \sum_k Y_{ik} Y_{jk} v_\phi^2 / m_{Rk}$, by taking all m_{Rk} of the same order we can rewrite the bound as (taking $\ln(\Lambda_C / m_{Rk}) \gtrsim 1$):

$$m_{R4} \gtrsim \sum_{ij} \frac{Y_{i4} (m_\nu)_{ij} Y_{j4}}{(4\pi)^4} \frac{m_{Rk}^2}{v_\phi^2}$$

- The same result is obtained for SS III.
- For $m_\nu = 0.01$ eV and $Y_{k4} = 0.01$ (suppressed due to universality and LFV constraints) we obtain that m_{R4} is of order keV, GeV, PeV for $m_{Rk} = 10^9, 10^{12}, 10^{15}$ GeV resp.

Natural fourth generation neutrino masses in SSII



In SS II (for light ν 's) plus one ν_R for the 4th gen., m_{R4} and the trilinear coupling of the triplet μ , mix under renormalization, so, as before (taking $\ln(\Lambda_C/m_\chi) \gtrsim 1$):

$$m_{R4} \gtrsim \frac{\mu}{(4\pi)^4} \sum_{ij} Y_{i4}(Y_\chi)_{ij} Y_{j4},$$

where Y_χ are the Yukawa couplings of the triplet to the lepton doublets. Expressed in terms of $(m_\nu)_{ij} \sim (Y_\chi)_{ij} \mu v_\phi^2 / m_\chi^2$:

$$m_{R4} \gtrsim \sum_{ij} \frac{Y_{i4}(m_\nu)_{ij} Y_{j4}}{(4\pi)^4} \frac{m_\chi^2}{v_\phi^2},$$

which is very similar to that obtained for SS I.

Natural fourth generation mass

Fourth generation naturally Majorana:

One expects that $m_R \neq 0$ (using NDA):

$$m_{R4} \sim \frac{\Lambda_W}{(4\pi)^4} \sum_{ij} Y_{i4} c_{ij} Y_{j4} \sim \frac{Y_{i4} (m_\nu)_{ij} Y_{j4}}{(4\pi)^4} \frac{\Lambda_W^2}{v_\phi^2},$$

which is the result obtained in the see-saw models if one identifies $\Lambda_W \sim m_{Rk}, m_\chi$.

The heavy ν sector consists of two Majorana ν 's:

$$\nu_4 = i \cos \theta (-\nu'_4 + \nu_4^c) + i \sin \theta (\nu_R - \nu_R^c)$$

$$\nu_{\bar{4}} = -\sin \theta (\nu'_4 + \nu_4^c) + \cos \theta (\nu_R + \nu_R^c)$$

with masses:

$$m_{4,\bar{4}} = \frac{1}{2} \left(\sqrt{m_R^2 + 4m_D^2} \mp m_R \right),$$

and mixing angle $\tan^2 \theta = m_4/m_{\bar{4}}$.

New families are a natural SM extension

- New families are allowed and testable at LHC.
- Theoretically: $\beta_{QCD} < 0 \implies n_{gen} \leq 8$.
- Baryogenesis: more CPV.
- DM: hadrons, heavy neutrinos/singlets if stable.
- Composite Higgs & dynamical EW symm. breaking: no hierarchy problem!
- Might help to solve flavor discrepancies.

Light neutrino masses induced by the extra family

Defining

$$N_\alpha \equiv V_{\alpha 4} = \frac{y_\alpha}{\sqrt{\sum_\beta y_\beta^2}},$$

for $m_E \gg m_{4,\bar{4}} \gg m_W$, the largest contribution is approximately:

$$(m_\nu)_{33}^{(2)} \approx \frac{g^4}{2(4\pi)^4} (N_e^2 + N_\mu^2 + N_\tau^2) m_R \frac{m_D^2 m_E^2}{m_W^4} \ln \frac{m_E}{m_{\bar{4}}}$$

Light neutrino masses induced by the extra family

Defining

$$N_\alpha \equiv V_{\alpha 4} = \frac{y_\alpha}{\sqrt{\sum_\beta y_\beta^2}},$$

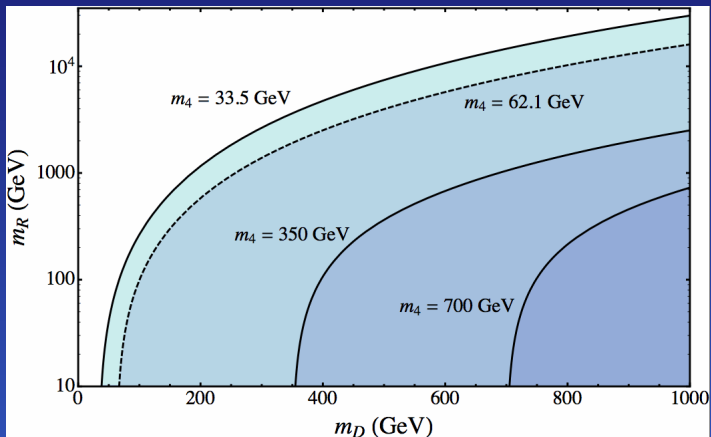
for $m_E \gg m_{4,\bar{4}} \gg m_W$, the largest contribution is approximately:

$$(m_\nu)_{33}^{(2)} \approx \frac{g^4}{2(4\pi)^4} (N_e^2 + N_\mu^2 + N_\tau^2) m_R \frac{m_D^2 m_E^2}{m_W^4} \ln \frac{m_E}{m_{\bar{4}}}$$

Could these radiative corrections explain by themselves the observed spectrum of masses and mixings?

- No, because the eigenvalues are $\propto m_\mu^4, m_\tau^4, m_D^2 m_E^2$, which gives a huge hierarchy between neutrino masses.
- However, they lead to a strong constraint for a 4th family.

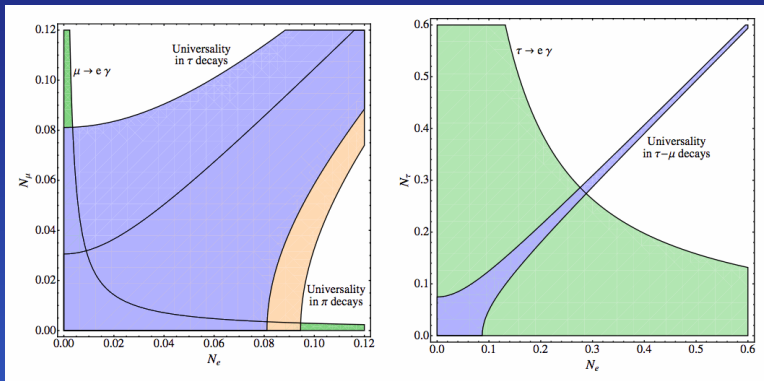
m_D versus m_R plane



Universality and LFV constraints

The bounds on the mixings of the light families are, at 90% C.L.:

$$N_e < 0.08, N_\mu < 0.03, N_\tau < 0.3$$



$$A \approx A_L + A_4 ,$$

where A_L is the light ν contribution (i.e., $m_k \ll p_{\text{eff}} \sim 100$ MeV):

$$A_L \propto \sum_k^{\text{light}} m_k U_{ek}^2 M^{0\nu 2\beta}(m_k) \simeq m_{ee} M^{0\nu 2\beta}(0) ,$$

with $M^{0\nu 2\beta}(0) \propto 1/p_{\text{eff}}^2$ the nuclear matrix element.

$$\begin{aligned} A_4 &\propto N_e^2 \left(m_4 \cos^2 \theta M^{0\nu 2\beta}(m_4) - m_{\bar{4}} \sin^2 \theta M^{0\nu 2\beta}(m_{\bar{4}}) \right) \\ &\propto N_e^2 \left(\frac{\cos^2 \theta}{m_4} - \frac{\sin^2 \theta}{m_{\bar{4}}} \right) = N_e^2 \frac{m_R}{m_D^2} \end{aligned}$$

- The largest contributions to A_4 correspond to small m_D .

The contribution of ν_4 's to the $0\nu 2\beta$ amplitude is dominant if:

$$N_e^2 m_R / m_D^2 > m_{ee} / (100 \text{ MeV})^2.$$

One can use the dependence on $N_e^2 m_R$ of both A_4 and $(m_\nu)_{33}^{(2)}$ to constrain the ν_4 contribution to the $0\nu 2\beta$ decay amplitude:

$$A_4 \leq \left(\frac{4\pi m_W}{g m_D} \right)^4 \frac{2(m_\nu)_{33}^{(2)}}{m_E^2 \ln \frac{m_E}{m_4}} \lesssim 190 (m_\nu)_{33}^{(2)} \left(\frac{50 \text{ GeV}}{m_D} \right)^4 \text{ GeV}^{-1},$$

where we have used the LEP limit, $m_E \gtrsim 100 \text{ GeV}$.

Imposing that $(m_\nu)_{33}^{(2)} \leq 0.05$ eV:

$$A_4 < 10^{-8} \left(\frac{50 \text{ GeV}}{m_D} \right)^4 \text{ GeV}^{-1}.$$

The non-observation of $0\nu 2\beta$ implies that:

$$A_4^{\text{non-obs}} < 10^{-8} \text{ GeV}^{-1}.$$

Imposing that $(m_\nu)_{33}^{(2)} \leq 0.05$ eV:

$$A_4 < 10^{-8} \left(\frac{50 \text{ GeV}}{m_D} \right)^4 \text{ GeV}^{-1}.$$

The non-observation of $0\nu 2\beta$ implies that:

$$A_4^{\text{non-obs}} < 10^{-8} \text{ GeV}^{-1}.$$

So the constraint from light neutrino masses implies that:

- the contribution of ν'_4 s to $0\nu 2\beta$ can reach observable values only if $m_D \lesssim 100$ GeV (although it can be the dominant one for other values of masses and mixings).

Two-loop integral

$$I_{kn} = \int \frac{d^4 p}{(2\pi)^4} \int \frac{d^4 q}{(2\pi)^4} \frac{p \cdot q}{(p^2 - m_k^2)(q^2 - m_n^2)((p+q)^2 - m_1^2)((p+q)^2 - m_2^2)} \times$$
$$\times \left[\frac{1}{p^2 q^2} - \frac{3}{4} \frac{1}{(p^2 - M_W^2)(q^2 - M_W^2)} \right]$$

If we take $m_E \gg m_{4,\bar{4}} > m_W$, we obtain:

$$I_0 \approx -\frac{1}{2^{10} \pi^4 m_4^2} \ln \frac{m_4^2}{m_4^2}, \quad k, n = e, \mu, \tau$$

$$I_E \approx -\frac{1}{2^{10} \pi^4 m_E^2} \ln \frac{m_E^2}{m_4^2}, \quad k \text{ and/or } n = E$$

A renormalizable model

- We build a model in the context of the 4G SM in which m_{R4} is generated radiatively and finite.
- $4G + 4\nu_{Ri}$ ($i = 1, \dots, 4$): 3 of them very heavy while one of them should be much lighter in order to avoid a too light ν_4 .
- So let the 4th ν_R be massless at tree level and let its mass be generated by radiative corrections.
- We add 3 extra chiral singlets s_{La} ($a = 1, \dots, 3$), and in order to break L , also a complex scalar singlet σ .

We assign L :

$$\ell_j \rightarrow e^{i\alpha} \ell_j, \quad e_{Rj} \rightarrow e^{i\alpha} e_{Rj}, \quad \nu_{Rj} \rightarrow e^{i\alpha} \nu_{Rj}, \quad \sigma \rightarrow e^{i\alpha} \sigma$$

The s_{La} do not carry L .

A renormalizable model

We have:

$$\mathcal{L}_Y = -\bar{\ell} Y_e e_R \phi - \bar{\ell} Y_\nu \nu_R \tilde{\phi} - \sigma \bar{\nu}_R y s_L - \frac{1}{2} \bar{s}_L^c M s_L + \text{H.c.},$$

where y_{ia} is a general 4×3 matrix while M is a symmetric 3×3 matrix, diagonal and positive.

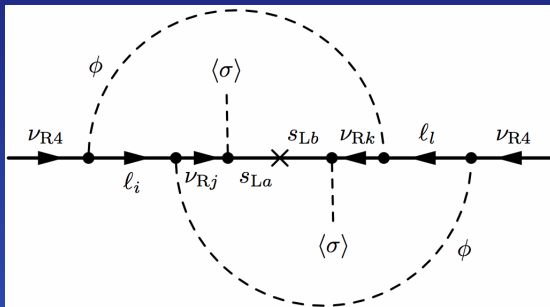
- Before SSB only s_{La} are massive.
- After σ gets a VEV, if $y v_\sigma \ll M$ the 4 ν_R 's will get a 4×4 Majorana mass matrix:

$$M_R^{(0)} \simeq v_\sigma^2 y M^{-1} y^T$$

- This is basically the see-saw formula but applied to ν_R 's with $v_\phi \rightarrow v_\sigma$. This matrix has rank 3 and, therefore, only 3 ν_R 's will obtain a tree-level mass.

A renormalizable model

- The other neutrino will remain massless at tree level. However, at two loops, also ν_{R4} will acquire a Majorana mass, via the following 2-loop diagram:



The diagram is obviously finite by power counting, so:

$$M_R^{(2)} \sim \frac{v_\sigma^2}{(4\pi)^4} Y_\nu Y_\nu^\dagger y M^{-1} y^T (Y_\nu Y_\nu^\dagger)^T \ln \left(\frac{M}{y v_\sigma} \right)$$