

# Peccei-Quinn NMSSM in the light of 125 GeV Higgs

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# Contents

- PQ NMSSM
  - Higgs mass
  - Neutralino sector
- Phenomenological constraints
  - Z invisible decay
  - $X_1^0, X_2^0$  production in LEP II
  - Higgs invisible decay
  - DM relic density, XENON100 bound on direct detection
- Small  $\tan\beta$  ( $1 < \tan\beta < 2$ ) region
- Large  $\tan\beta$  ( $\tan\beta > 2$ ) region

# PQ NMSSM

$$W_{\text{eff}} = (\mu_0 + \lambda S) H_u H_d + \mu_S^2 S + \frac{1}{2} \mu'_S S^2 + \frac{1}{3} \kappa S^3$$

- **NMSSM** : SM singlet superfield  $S$  coupled to the Higgs fields through the renormalizable term  $\lambda S H_u H_d$  which can give a solution to the "mu problem" in the MSSM by the VEV of  $S$ .
- **PQ** symmetry : Global  $U(1)$  symmetry that can give the axion solution to the "strong CP problem".
- Assume  $\lambda S H_u H_d$  is allowed in the PQ symmetric phase with  $q_S = -(q_{H_u} + q_{H_d})$ .
- The other terms are generated by spontaneous PQ symmetry breaking below the PQ scale  $v_{\text{PQ}}$  with the PQ sector like

$$W_{\text{PQ}} = \frac{\kappa_{\text{PQ}}}{M_{\text{Pl}}} X_1^n X_2^{4-n} \quad K = \frac{\kappa_{XS}}{M_{\text{Pl}}} X_1^{*2} S + \text{h.c.}$$

# PQ NMSSM

$$W_{\text{eff}} = (\mu_0 + \lambda S)H_u H_d + \mu_S^2 S + \frac{1}{2}\mu'_S S^2 + \frac{1}{3}\kappa S^3$$

- It can be shown that the dimensionful parameters can be given by the soft SUSY breaking scale and the  $S^3$  term is generally suppressed in the PQ NMSSM  
 $\mu_0 \sim \mu_S \sim \mu'_S \sim v_{\text{PQ}}^2/M_{\text{Pl}} \sim m_{\text{soft}}$
- The  $\mu_0$  term can be rotated away by the field redefinition  
 $S \rightarrow S - \mu_0/\lambda$
- The  $\mu'_S$  term needs more complex field contents and charge assignments to be obtained in the PQ sector.
- So the simplest and easiest possibility of PQ symmetric NMSSM realized in low energy scale is

$$W_{\text{eff}} = \lambda S H_u H_d + \mu_S^2 S.$$

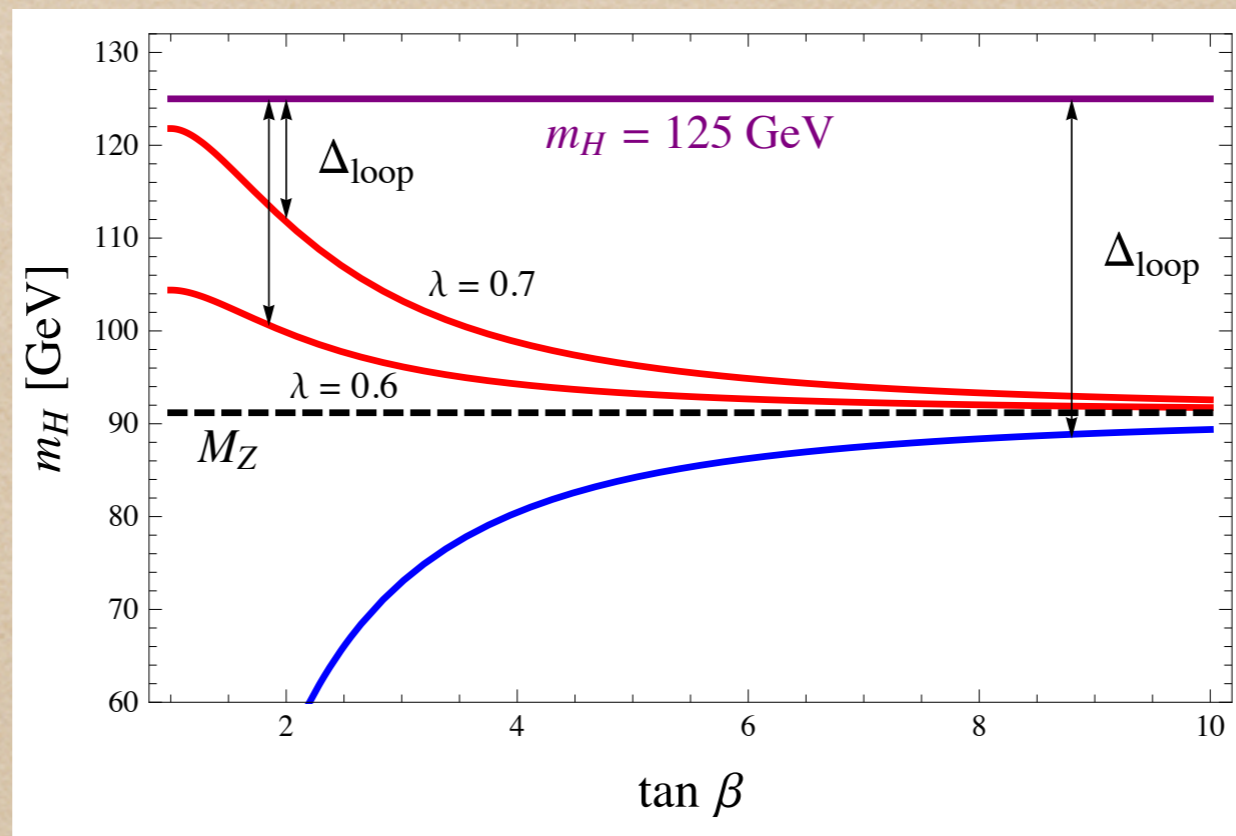
which we will call Minimal PQ NMSSM.

# Higgs mass in the NMSSM

$$m_{h,\text{tree}}^2 \simeq \underbrace{m_Z^2 \cos^2 2\beta}_{\text{Usual MSSM contribution}} + \underbrace{\lambda^2 v^2 \left( \sin^2 2\beta - \frac{(2\mu_{\text{eff}} - A_\lambda \sin 2\beta)^2}{m_S^2} \right)}_{\text{NMSSM-specific contribution}}$$

Usual MSSM contribution

NMSSM-specific contribution



- The new Higgs quartic coupling induced by the  $F_S$  term raises the tree level Higgs mass which can ameliorate the fine-tuning for the 125 GeV Higgs mass with lower stop mass compared to the MSSM.
- Since it is proportional to  $\sin 2\beta \sim 2/\tan \beta$ , small  $\tan \beta$  is favored in the NMSSM for the naturalness purpose.

# Neutralino sector

$$\mathcal{M}_{\tilde{\chi}^0} = \begin{pmatrix} M_1 & 0 & -g_1 v_d / \sqrt{2} & g_1 v_u / \sqrt{2} & 0 \\ & M_2 & g_2 v_d / \sqrt{2} & -g_2 v_u / \sqrt{2} & 0 \\ & & 0 & -\mu_{\text{eff}} & -\lambda v_u \\ & & & 0 & -\lambda v_d \\ & & & & 0 \end{pmatrix} \quad \text{in the basis } (-i\tilde{\lambda}_1, -i\tilde{\lambda}_2, \tilde{H}_d^0, \tilde{H}_u^0, \tilde{S})$$

$$\longrightarrow m_{\tilde{\chi}_1^0} \simeq \frac{\lambda^2 v^2}{\mu_{\text{eff}}} \left[ \sin 2\beta - \frac{\lambda^2 v^2}{\mu_{\text{eff}}^2} \sin 2\beta - \left( \frac{g_1^2 v^2}{2\mu_{\text{eff}} M_1} + \frac{g_2^2 v^2}{2\mu_{\text{eff}} M_2} \right) \cos^2 2\beta + \mathcal{O}\left(\frac{v^4}{\mu_{\text{eff}}^4}\right) \right]$$

- The fermion component in the  $S$  superfield, called singlino, constitutes for the lightest neutralino, mixing with neutral Higgsinos and gauginos.
- Since there is no supersymmetric mass term ( $W_{\text{eff}} \not\propto \mu_S' S^2$ ) for the singlino in the minimal PQ NMSSM, it can obtain its mass only by mixing.
- So the mass of the lightest neutralino in the minimal PQ NMSSM turns out to be quite small in general parameter space.

# Phenomenological constraints

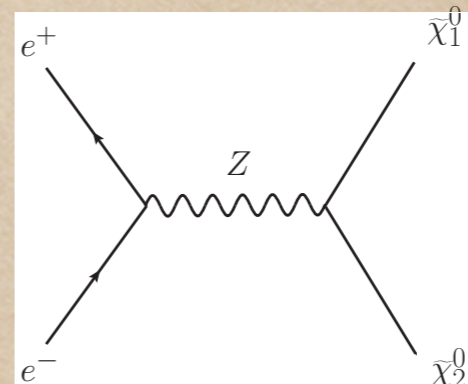
- Due to the light lightest neutralino, the minimal PQ NMSSM suffers several important phenomenological constraints.

- Z invisible decay in LEP II

$$\Gamma(Z \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0) = \frac{g_2^2}{4\pi} \frac{(N_{13}^2 - N_{14}^2)^2}{24 \cos^2 \theta_W} m_Z \left[ 1 - \left( \frac{2M_{\tilde{\chi}_1^0}}{m_Z} \right)^2 \right]^{3/2} < 3 \text{ MeV}$$

- $\tilde{\chi}_1^0, \tilde{\chi}_2^0$  pair production in LEP II

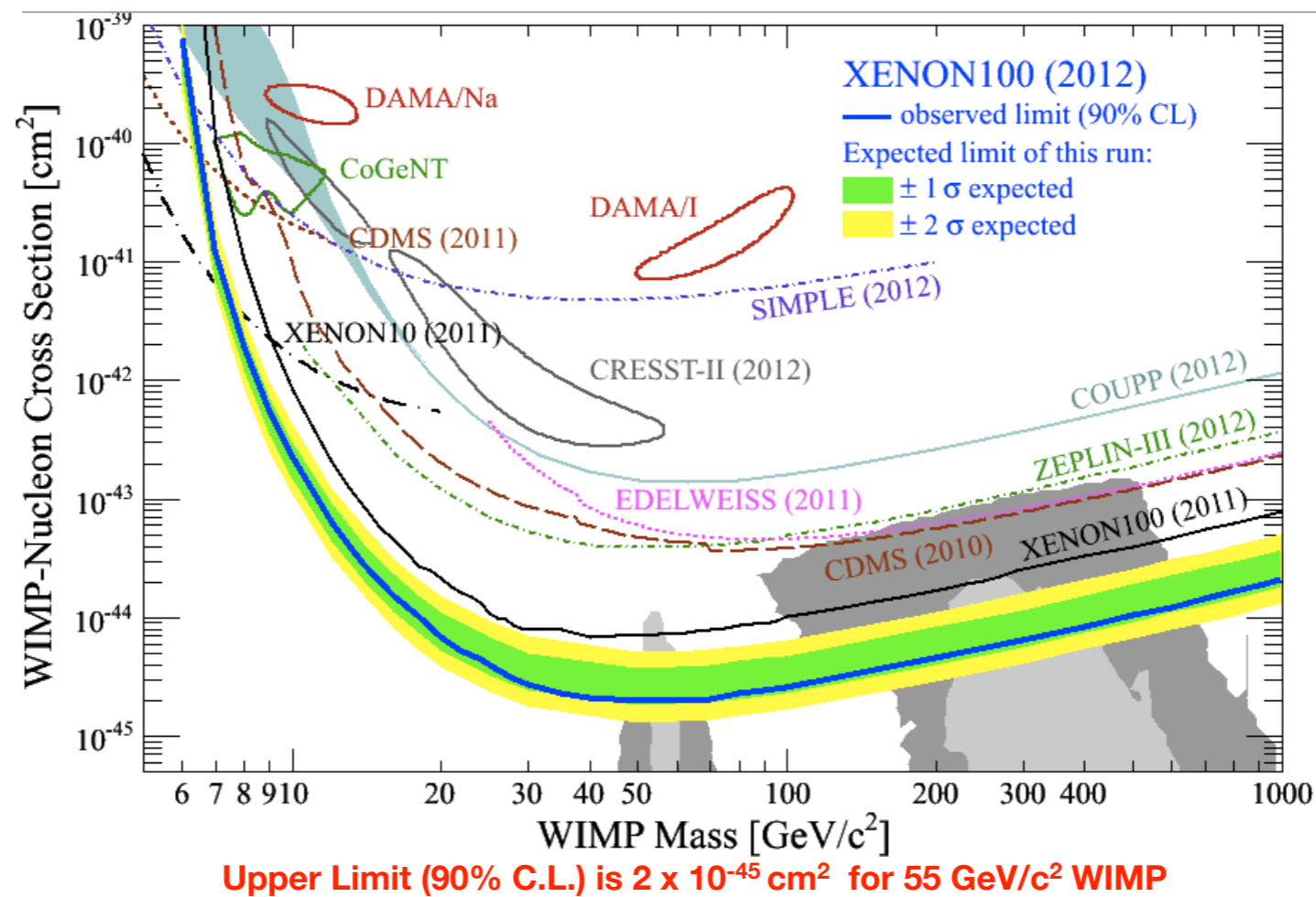
$$\sigma(e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0) < 10 \text{ fb}$$



- Higgs invisible decay : small  $\tan\beta$  (kinematically forbidden), large  $\tan\beta$  (nontrivial coupling suppression needed)

- Due to the enhanced Higgs-neutralino-neutralino coupling by  $\lambda S H_u H_d$ , the direct detection cross section of the lightest neutralino LSP is rather larger than MSSM.
- Recent XENON100 bound thus restricts the viable parameter space considerably.

### XENON100: New Spin-Independent Results





# Small $\tan\beta$ ( $1 < \tan\beta < 2$ ) region

- In small  $\tan\beta$  region, the lightest neutralino mass can be larger than the half of the Higgs mass.
- So the Higgs invisible decay as well as the Z invisible decay is kinematically forbidden.
- Also small  $\tan\beta$  gives large  $\lambda$ -proportional contribution to the tree level Higgs mass, which is favored by the naturalness perspective.

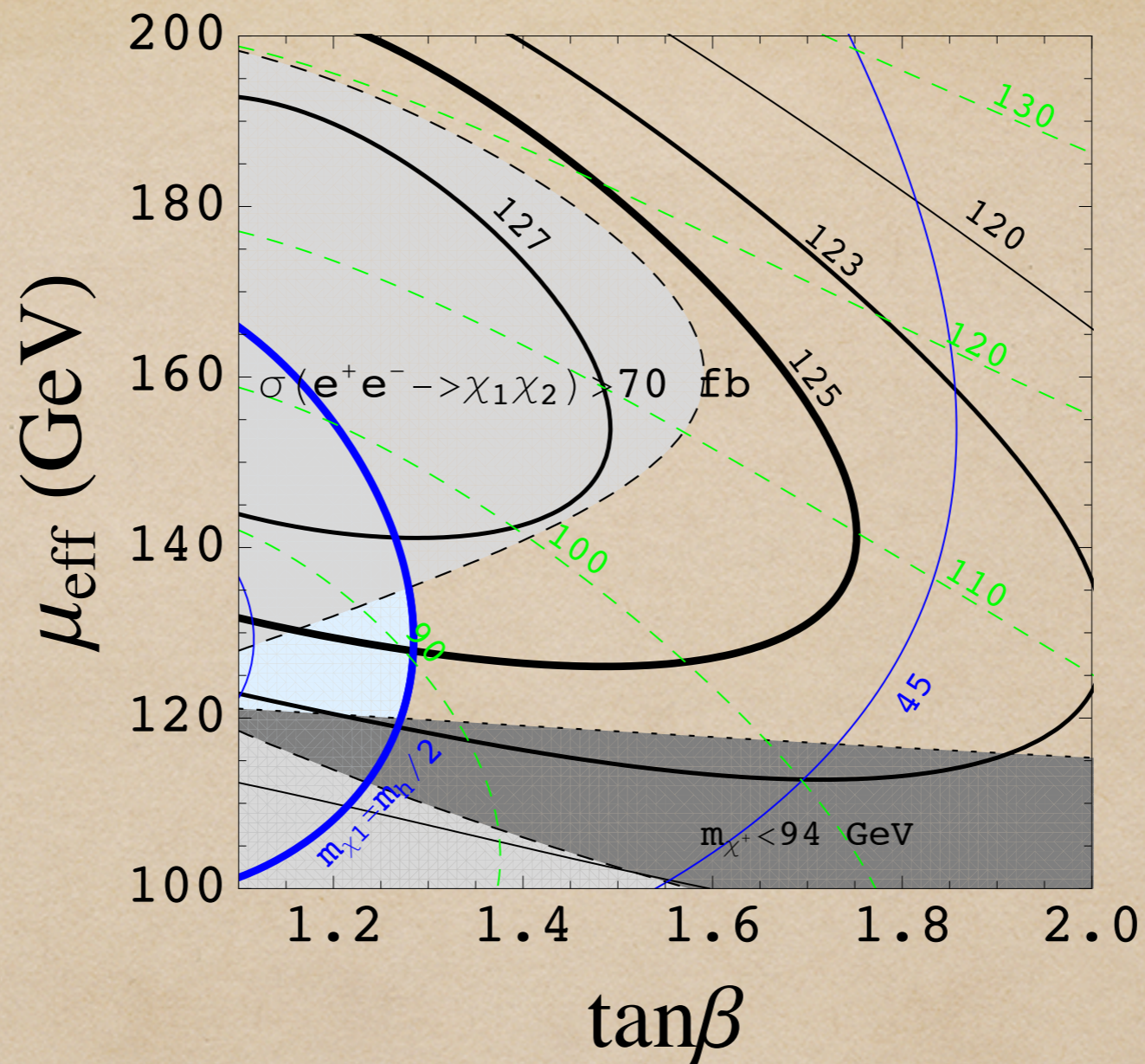
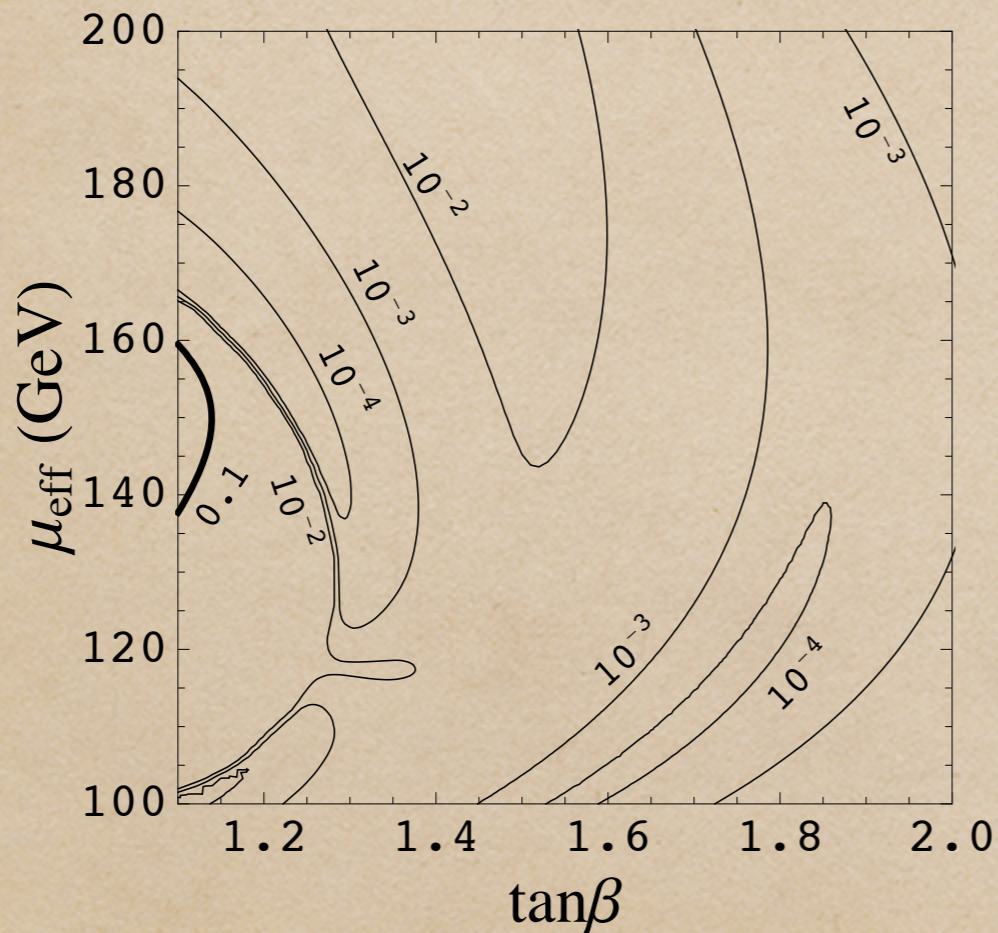


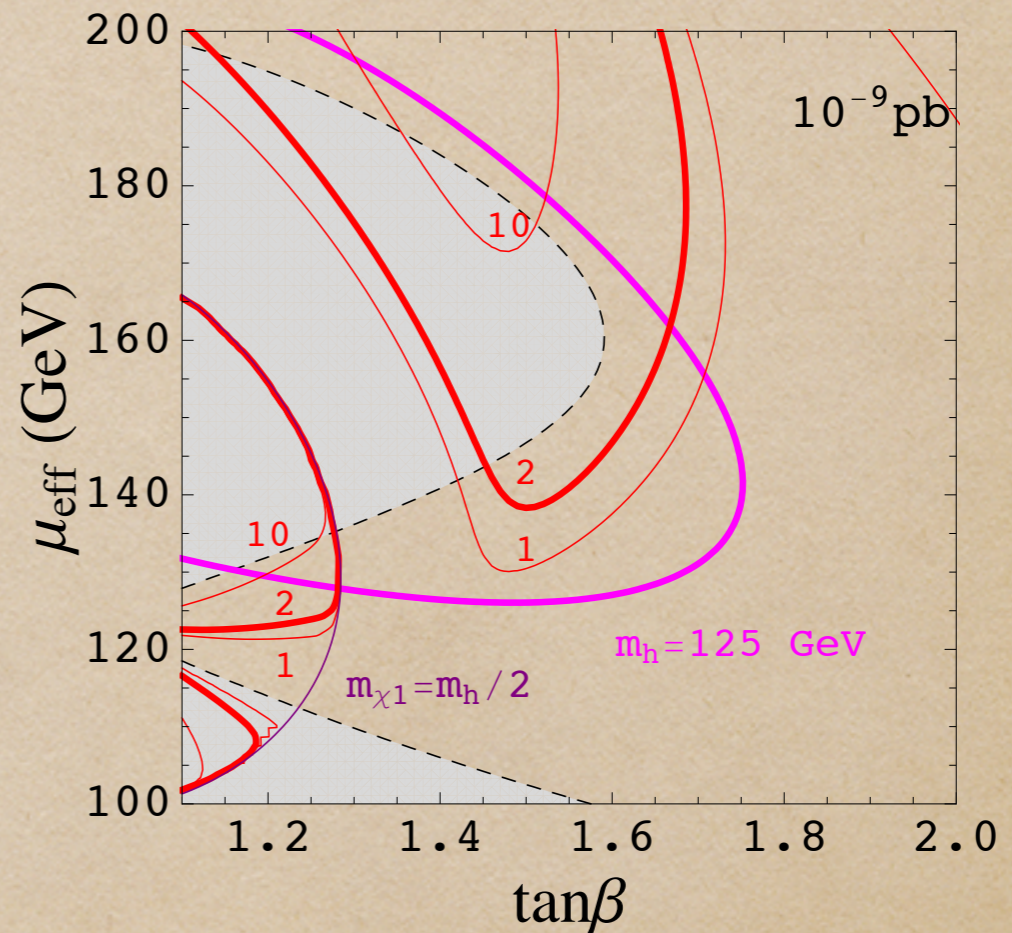
Figure 2: Plot for small  $\tan\beta$ . Here we set  $6M_1 = 3M_2 = M_3 = 1$  TeV,  $m_A = 350$  GeV,  $m_{\tilde{Q}_3} = m_{\tilde{t}^c} = 500$  GeV,  $A_t = 0$ , and  $\xi_S = -7 \times 10^7$  GeV<sup>3</sup>. Black curves denote Higgs mass in GeV, blue curves denote  $m_{\tilde{\chi}_1^0}$  in GeV, and green dashed curves denote  $m_{\tilde{\chi}_2^0}$ . The gray-shaded region is excluded by the OPAL [17].

- However, the small  $\tan\beta$  region is severely constrained by the recent XENON100 bound on the direct detection cross section of DM
- We find that the lightest neutralino LSP heavier than the half of the Higgs mass cannot satisfy the XENON100 bound without fine-tuning of the LSP mass to give resonant cross section.

$$m_{\tilde{\chi}_1^0} - \frac{m_h}{2} \lesssim 0.1 \text{ GeV}$$



(a)  $\Omega_{\tilde{\chi}_1^0}^{\text{TH}} h^2$



(b)  $(\Omega_{\tilde{\chi}_1^0}^{\text{TH}} / \Omega_{\text{DM}}) \sigma_{\text{SI}, \tilde{\chi}_1^0}$

- However, the PQ sector can cure this problem.
- The entropy dumping by late saxion decay with lower reheating temperature than the LSP freeze-out temperature can dilute the thermal LSP relic density enough.

$$\begin{aligned} \Delta &= \frac{S(T_{\text{RH}})}{S(T_f)} \simeq \frac{g_*(T_f)}{g_*(T_{\text{RH}})} \left( \frac{T_f}{T_{\text{RH}}} \right)^5 \\ &\simeq 0.9 \times 10^5 \left( \frac{g_*(T_f)}{80} \right) \left( \frac{70}{g_*(T_{\text{RH}})} \right) \left( \frac{T_f}{3 \text{ GeV}} \right)^5 \left( \frac{500 \text{ MeV}}{T_{\text{RH}}} \right)^5 \end{aligned}$$

- Then the DM relic density can be explained by the axion CDM.

$$\Omega_a h^2 \simeq 0.23 \left( \frac{v_{\text{PQ}}}{10^{12} \text{ GeV}} \right)^{7/6} \langle \theta^2 \rangle$$

# Large $\tan\beta$ ( $\tan\beta > 2$ ) region

- In large  $\tan\beta$  region, the LSP mass becomes smaller than the half of the Higgs mass, and the Higgs invisible decay channel opens.
- However, suppressing the  $h\text{-}X_1^0\text{-}X_1^0$  coupling turns out to be difficult.

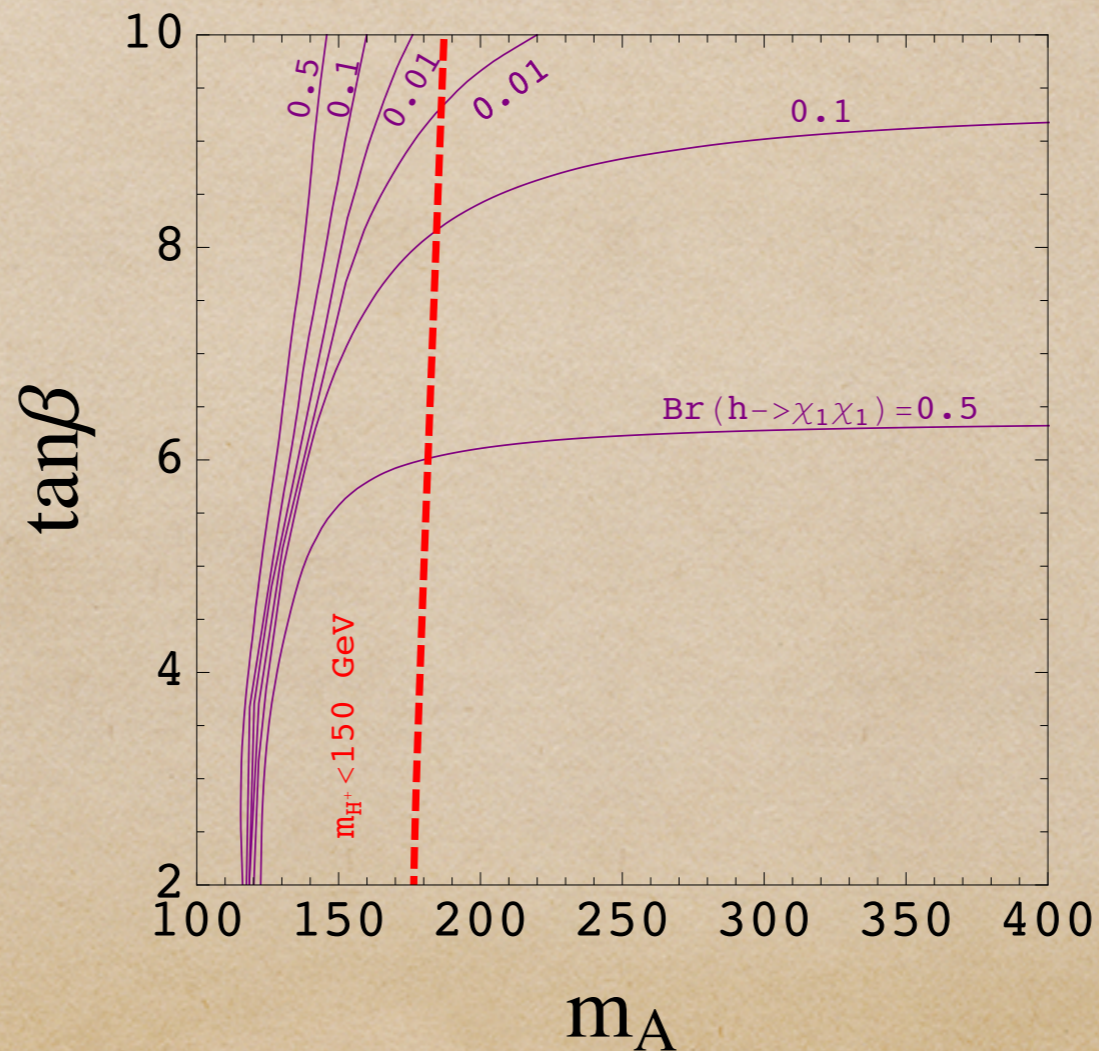
$$g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} = -g_2 \left( N_{12} - \tan\theta_W N_{11} \right) \left( S_{11}N_{13} - S_{12}N_{14} \right) \\ + \sqrt{2}\lambda \left( S_{13}N_{13}N_{14} + N_{15}(S_{12}N_{13} + S_{11}N_{14}) \right)$$

$$\downarrow \quad g_{hXX} = 0$$

$$\frac{1}{\tan\beta} \simeq - \left( c - c \frac{9m_W^4}{4M_2^2\mu_{\text{eff}}^2} - \frac{3m_W^2}{M_2\mu_{\text{eff}}} \right) \left( 1 - c \frac{3m_W^2}{2M_2\mu_{\text{eff}}} \right) \left( 1 + \frac{3\sqrt{2}\lambda^2 v^2}{\mu_{\text{eff}}^2} \right) \\ = \left[ \frac{3m_W^2}{M_2\mu_{\text{eff}}} - c \left( 1 + \frac{9m_W^4}{4M_2^2\mu_{\text{eff}}^2} \right) - c^2 \frac{3m_W^2}{2M_2\mu_{\text{eff}}} \left( 1 - \frac{9m_W^4}{4M_2^2\mu_{\text{eff}}^2} \right) \right] \left( 1 + \frac{3\sqrt{2}\lambda^2 v^2}{\mu_{\text{eff}}^2} \right)$$

where  $c \equiv S_{11}/S_{12}$ ,  $g_2 \simeq 2g_1$

- With  $M_A^2 \equiv 2b_{\text{eff}}/\sin 2\beta$  (Not physical CP-odd Higgs mass in the NMSSM),
- For small  $M_A \lesssim 170$  GeV, the parameter space is ruled out by the ATLAS bound on the charged Higgs mass (for  $\tan\beta < 4$ ), or disfavored by non SM-like Higgs due to the CP-even Higgs mixing.
- For large  $M_A \gtrsim 170$  GeV, the parameter space is disfavored by the large  $\tan\beta$  needed to suppress the coupling. It requires  $\tan\beta \gtrsim 10$  where the NMSSM specific contribution to the Higgs mass is negligible.



# Conclusions

- The minimal PQ NMSSM is the simplest low energy consequence of the PQ symmetrized NMSSM which incorporates solutions to the  $\mu$  problem and strong CP problem.
- This model is strongly disfavored by the Higgs invisible decay induced by the light lightest neutralino and the recent XENON100 bound on the DM direct detection cross section.
- Still, the thermal LSP dilution by the saxion decay in the PQ sector leaves the space for this model to be viable.

back-up

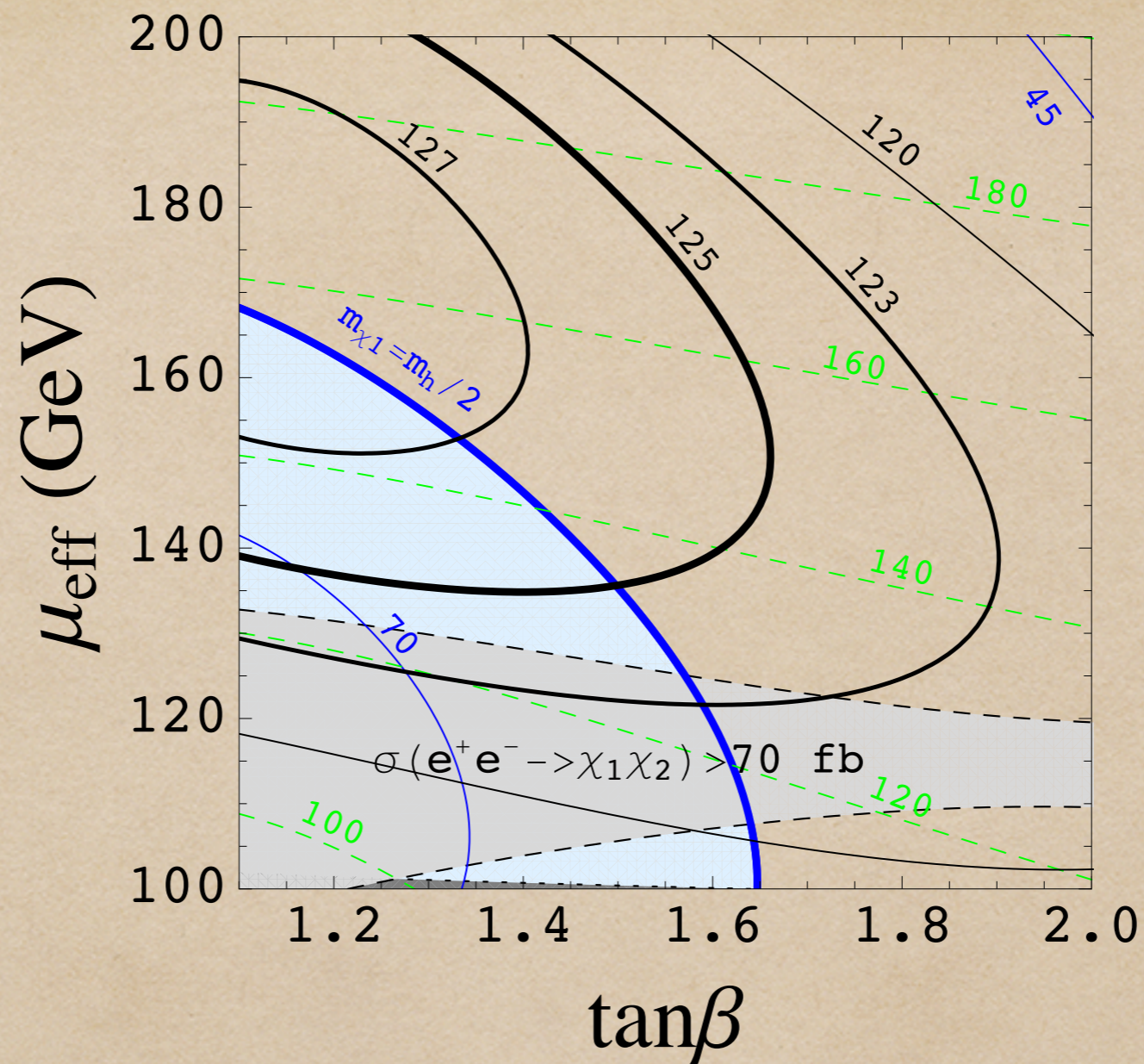
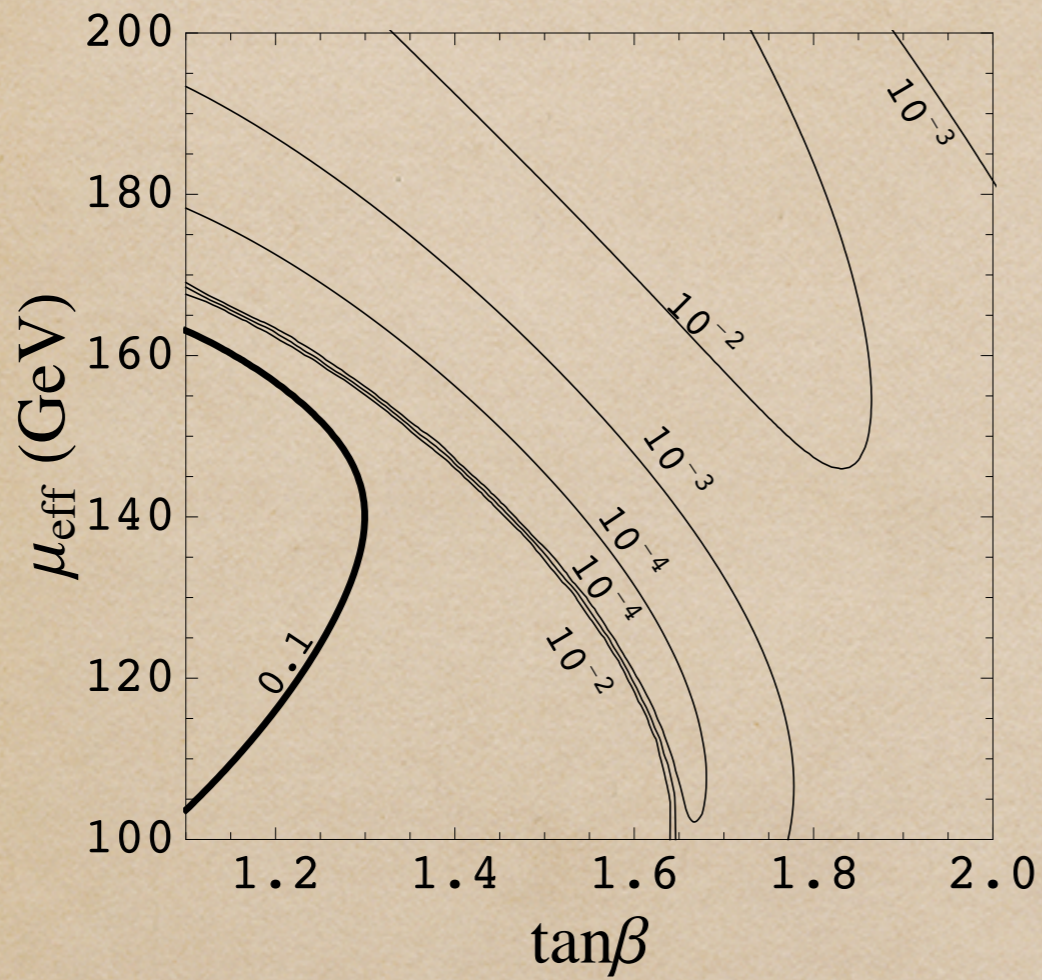
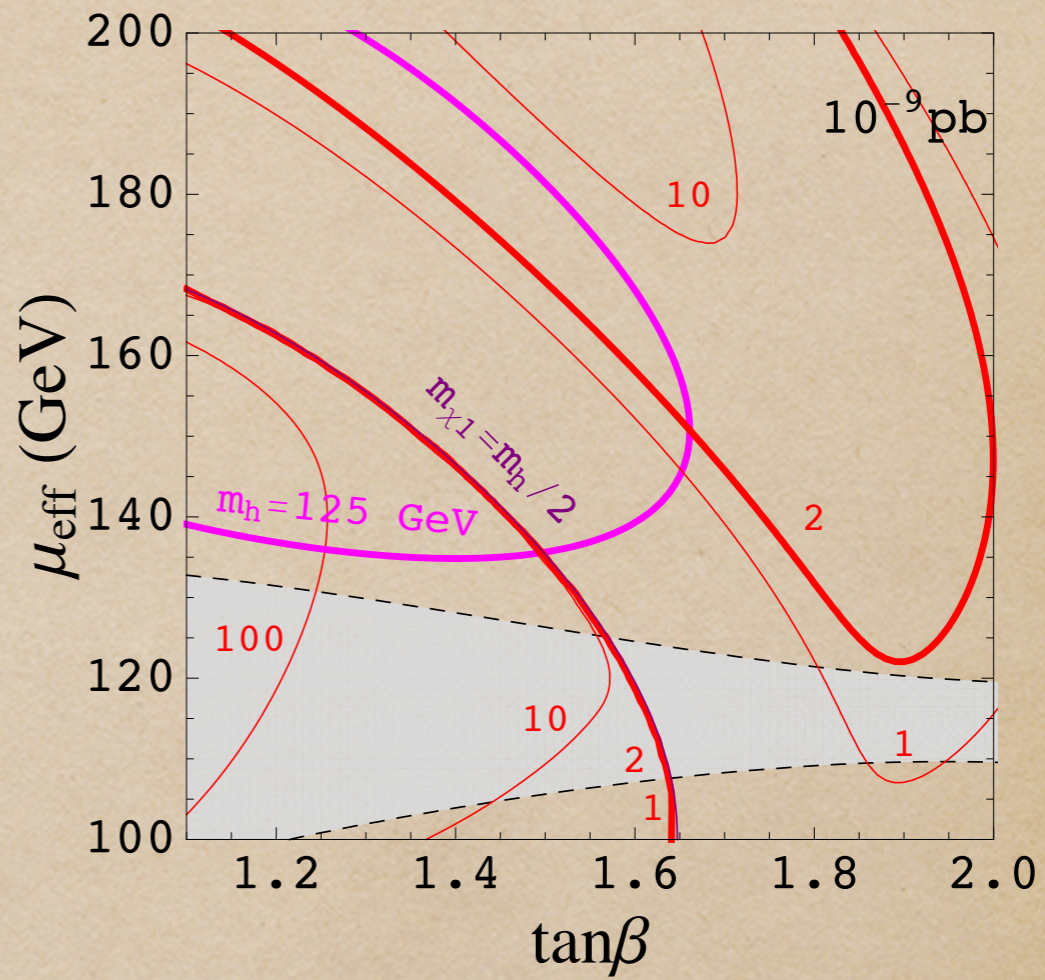


Figure 3: Plot for small  $\tan\beta$ . Here we set  $M_1 = M_2 = M_3 = 1 \text{ TeV}$ ,  $m_A = 350 \text{ GeV}$ ,  $m_{\tilde{Q}_3} = m_{\tilde{t}_c} = 500 \text{ GeV}$ ,  $A_t = 0$ , and  $\xi_S = -7 \times 10^7 \text{ GeV}^3$ . Black curves denote Higgs mass in GeV, blue curves denote  $m_{\tilde{\chi}_1^0}$  in GeV, and green dashed curves denote  $m_{\tilde{\chi}_2^0}$ . The gray-shaded region is excluded by the OPAL [17].





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