

# No-go Theorem for $R$ Symmetries in 4D GUTs

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in collaboration with Michael Ratz and Patrick K.S. Vaudrevange

MF, Ratz and Vaudrevange, *Phys. Lett. B* **705** (2011).



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August 2012

2012 Cargèse Summer School

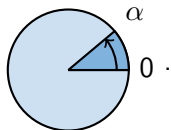
**Four-dimensional**  
supersymmetric **SU(5) GUT** Georgi and Glashow (1974).  
with an ***R* symmetry** and  
only a **finite number of multiplets**.

We would like to...

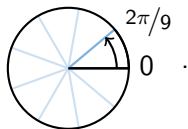
- ... break  $SU(5) \rightarrow G_{SM}$ .
- ... **keep the *R* symmetry unbroken.**
- ... arrive at the MSSM spectrum.

$R$  symmetries distinguish between superpartners.

■  $U(1)_R$ :



■  $\mathbb{Z}_M^R, M \geq 3$ :



**$\Rightarrow R$  parity is not a real  $R$  symmetry.**  
(it is equivalent to non- $R$  matter parity)

■ the superpotential is charged under an  $R$  symmetry:

$$q_R(W) \neq 0.$$

# The theorem

In supersymmetric SU(5) GUTs with a low-energy  $R$  symmetry and a finite number of multiplets. . .

. . . there are always  
**charged massless states**  
beyond the MSSM spectrum.

- underlying reason: mass term of GUT-breaking Higgs forbidden,

$$\cancel{m H_0 H_0}.$$

**$\Rightarrow$  no low-energy  $R$  symmetries in conventional SU(5) GUTs.**

Thank you!

- 1 M. Fallbacher, M. Ratz and P. K. S. Vaudrevange, 'No-go theorems for R symmetries in four-dimensional GUTs', *Phys. Lett. B* **705** (2011), 503–506, arXiv: 1109.4797 [hep-ph].
- 2 H. Georgi and S. L. Glashow, 'Unity of All Elementary-Particle Forces', *Phys. Rev. Lett.* **32** (1974), 438–441.
- 3 H. M. Lee, S. Raby, M. Ratz, G. G. Ross, R. Schieren, K. Schmidt-Hoberg and P. K. S. Vaudrevange, 'Discrete R symmetries for the MSSM and its singlet extensions', *Nucl. Phys. B* **850** (2011), 1–30, arXiv: 1102.3595 [hep-ph].

# An application: the $\mu$ problem

- Assume MSSM with SU(5) GUT relations for matter charges:

What **symmetries** are

**anomaly-free** and

**forbid** the  $\mu$  term  ~~$\mu H_u H_d$~~  ?

**$\Rightarrow$  only  $R$  symmetries!** Lee et al. (2011).

- in SU(5) GUTs:

$\Rightarrow$  no  $R$  symmetries at low energies.

$\Rightarrow$  no symmetry that forbids the  $\mu$  term.

**$\Rightarrow$  no natural solution to the  $\mu$  problem.**