Introduction

to the EW STANDARD MODEL

CERN School

Angers, June 2012

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I. Summary of the Phenomenology

TABLE OF ELEMENTARY PARTICLES		
QUANTA OF RADIATION		
Strong Interactions		Eight gluons
Electromagnetic Interactions		Photon (γ)
Weak Interactions		Bosons W^+ , W^- , Z^0
Gravitational Interactions		Graviton (?)
MATTER PARTICLES		
	Leptons	Quarks
1st Family	$ u_{e}$, e^{-}	u_{a} , d_{a} , $a=1,2,3$
2nd Family	$ u_{\mu}$, μ^-	c_{a} , s_{a} , $a=1,2,3$
3rd Family	$ u_{ au}$, $ au^-$	t_{a} , b_{a} , $a=1,2,3$
HIGGS BOSON (?)		

Table: This Table shows our present ideas on the structure of matter. Quarks and gluons do not exist as free particles and the graviton and the Higgs boson have not yet been observed.

All interactions are produced by the exchange of virtual quanta. For the strong, e.m. and weak interactions they are vector (spin-one) fields, while the graviton is assumed to be a tensor, spin-two field.

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- Quarks and gluons do not appear as free particles. They form a large number of bound states, the hadrons.
- Quarks and leptons seem to fall into three distinct groups, or "families". Why?
- The sum of all electric charges inside any family is equal to zero.

Electromagnetic Interactions

$$\mathcal{L}_i \sim -eA_\mu(x)j^\mu(x)$$

For the matter fields the current is: (A bit more complicated for the charged vector fields)

$$j^{\mu}(x) = \sum_{i} q_{i} \overline{\psi}_{i}(x) \gamma^{\mu} \psi_{i}(x)$$

- Vector current
- Conservation of P, C, and T
- Absence of more complex terms, such as:

 $j^{\mu}(x)j_{\mu}(x), \quad \partial A(x)\overline{\psi}(x)...\psi(x),...$

- All these terms, as well as all others we can write, share one common property:
- In a four-dimensional space-time, their canonical dimension is larger than four.
- The resulting quantum field theory is *non-renormalisable*
- For some reason, Nature does not like Non-Renormalisable theories.

Weak Interactions

• Mediated by massive vector bosons

 ${\cal L}_i ~\sim~ V_\mu(x) j^\mu(x)$; V_μ : $W^+_\mu, ~W^-_\mu, ~Z^0_\mu$

For the matter part the current is again bi-linear in the fermion fields: $\bar{\psi}...\psi$

• The charged current (i) Contains only left-handed fermion fields:

$$j_{\mu}\simar{\psi}_{L}\gamma_{\mu}\psi_{L}\simar{\psi}\gamma_{\mu}(1+\gamma_{5})\psi$$

(ii) It is non-diagonal in the quark flavour space.

• The neutral current

(i) Contains both left- and right-handed fermion fields:

 $j_{\mu} \sim C_L \bar{\psi}_L \gamma_{\mu} \psi_L + C_R \bar{\psi}_R \gamma_{\mu} \psi_R$

(ii) It is diagonal in the quark flavour space.

• Violation of P, C, and T



 In Physics a Symmetry follows from the assumption that a certain quantity is not measurable.

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- Space-time Symmetries
 Translations, Rotations, Lorentz boosts, Inversions
- Internal Symmetries The phase of the wave function, Field redefinitions

Ex. SPACE TRANSLATIONS



If A is the trajectory of a free particle in the (x,y,z) system, its image, A', is also a possible trajectory of a free particle.

A first abstraction: Local Symmetries

Einstein 1918



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Local space translations

A" IS NOT a possible trajectory of a free particle. Are there forces for which A" is the trajectory?

Local space translations

The question is purely geometrical without any obvious physical meaning, so we expect a mathematical answer with no interest for Physics.

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 Surprise: The Dynamics which is invariant under local translations is

GENERAL RELATIVITY

The resulting force is Gravity One of the four fundamental forces.

• The phase of the wave function in Quantum Mechanics $\Psi(x) o e^{i heta} \Psi(x)$

Leaves the Scrödinger, or the Dirac, equation, as well as the normalisation condition, invariant

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Isospin Heisenberg 1932

$$N(x) = \left(egin{array}{c} p(x) \ n(x) \end{array}
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- With the discovery of new internal symmetries the idea was generalised to multi-dimensional internal spaces.
- The space of Physics became an abstract mathematical concept with non-trivial geometrical and topological properties.
- Only a part of it, the three-dimensional Euclidean space, is directly accessible to our senses.

The gravitational forces are not the only ones which have a geometrical origin

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The example of the quantum mechanical phase:

 $\Psi(x)
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The example of the quantum mechanical phase:

 $\Psi(x) \to e^{i\theta}\Psi(x) \quad \text{with} \quad \theta \to \theta(x)$ $\bullet \ \partial_{\mu}e^{i\theta(x)}\Psi(x) = e^{i\theta(x)}\partial_{\mu}\Psi(x) + ie^{i\theta(x)}\Psi(x)\partial_{\mu}\theta(x)$

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- $\bullet \ \partial_{\mu}e^{i\theta(x)}\Psi(x) = e^{i\theta(x)}\partial_{\mu}\Psi(x) + ie^{i\theta(x)}\Psi(x)\partial_{\mu}\theta(x)$

• Introduce $A_{\mu}(x)$ such that $A_{\mu}(x) \rightarrow A_{\mu}(x) - \frac{1}{e} \partial_{\mu} \theta(x)$

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$$A_{\mu}(x) \rightarrow A_{\mu}(x) - \frac{1}{e}\partial_{\mu}\theta(x)$$

Then

 $\partial_\mu o D_\mu = \partial_\mu - i e A_\mu(x)$; $D_\mu e^{i heta(x)} \Psi(x) = e^{i heta(x)} D_\mu \Psi(x)$

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 Replacing ∂_μ by D_μ turns any equation which was invariant under the global phase transformation, invariant under the local (gauge) one.
 Fock 1926

► The introduction of the covariant derivative: The free Scrödinger, or Dirac, equation ⇒ The same equation in the presence of an external

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electromagnetic field

The introduction of the covariant derivative:

The free Scrödinger, or Dirac, equation \Rightarrow

The same equation in the presence of an external electromagnetic field

To obtain the fully interacting theory:

Add the energy of the new vector field:

 $\sim F_{\mu
u}^2 = (\partial_\mu A_
u - \partial_
u A_\mu)^2$

The resulting interaction is:

QUANTUM ELECTRODYNAMICS

Think of a field theory formulated on a space-time lattice:

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- $egin{aligned} \Psi(x) &\Rightarrow \Psi_i \ ; & \partial \Psi(x) &\Rightarrow (\Psi_i \Psi_{i+1}) \ \Psi(x) &\Rightarrow e^{i heta} \Psi(x) &\Rightarrow \Psi_i &\Rightarrow e^{i heta} \Psi_i \end{aligned}$
 - For global transformations, *i.e.* constant θ : $\bar{\Psi}_i \Psi_i$ as well as $\bar{\Psi}_i \Psi_{i+1}$ remain invariant

Think of a field theory formulated on a space-time lattice:

- $\Psi(x) \Rightarrow \Psi_i$; $\partial \Psi(x) \Rightarrow (\Psi_i \Psi_{i+1})$ $\Psi(x) \rightarrow e^{i\theta}\Psi(x) \Rightarrow \Psi_i \rightarrow e^{i\theta}\Psi_i$
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 - ► For gauge transformations, *i.e.* $\theta(x) \Rightarrow \theta_i$, the term: $\bar{\Psi}_i \Psi_{i+1}$ transforms into $e^{-i\theta_i} \bar{\Psi}_i \Psi_{i+1} e^{i\theta_{i+1}}$

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- We need a field to *connect* the points i and i + 1.

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- We need a field to connect the points i and i + 1.
 U_{i,i+1} which transforms as U_{i,i+1} → e^{iθ_i}U_{i,i+1}e^{-iθ_{i+1}}
 The term Ψ_iU_{i,i+1}Ψ_{i+1} is now invariant. In the continuum limit the field U becomes the gauge potential A
- The matter fields live on the lattice points.

Think of a field theory formulated on a space-time lattice:

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The term $\overline{\Psi}_i U_{i,i+1} \Psi_{i+1}$ is now invariant. In the continuum limit the field U becomes the gauge potential A

- The matter fields live on the lattice points.
- The gauge potentials live on the oriented lattice links

$$\bullet \ \Psi = \left(\begin{array}{c} \psi^1 \\ \vdots \\ \psi^r \end{array}\right) \quad ; \quad \Psi(x) \to U(\omega)\Psi(x) \quad ; \quad \omega \in G$$

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For infinitesimal transformations:

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 ; $\Theta = \sum_{a=1}^{m} \theta^{a} T^{a}$; $[T^{a}, T^{b}] = i f^{abc} T^{c}$

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- ► L(Ψ, ∂Ψ) is assumed to be invariant under these global transformations
- As was done for the Abelian case, we wish to find a new L, invariant under the corresponding gauge transformations in which the θ^a's are arbitrary functions of x.
- In a qualitative sense, we look for a theory invariant under G^∞

▶ We need a gauge field, the analogue of the electromagnetic field, to transport the information from one point to the next. Since we can perform *m* independent transformations, the number of generators in the Lie algebra of *G*, we need *m* gauge fields $A^a_{\mu}(x)$, a = 1, ..., m. It is easy to show that they belong to the adjoint representation of *G*.

$$\mathcal{A}_{\mu}(x) = \sum_{a=1}^{m} A^{a}_{\mu}(x) T^{a}$$

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- ► It satisfies $\mathcal{D}_{\mu}e^{i\Theta(x)}\Psi(x) = e^{i\Theta(x)}\mathcal{D}_{\mu}\Psi(x)$ provided $\mathcal{A}_{\mu}(x) \rightarrow e^{i\Theta(x)}\mathcal{A}_{\mu}(x)e^{-i\Theta(x)} + \frac{i}{g}\left(\partial_{\mu}e^{i\Theta(x)}\right)e^{-i\Theta(x)}$

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- If L(Ψ, ∂Ψ) is invariant under the global G
 L(Ψ, DΨ) is invariant under the gauge G

• $\mathcal{L}(\Psi, \mathcal{D}\Psi)$ describes the interaction of the fields Ψ in an external Yang-Mills field

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- ► L(Ψ, DΨ) describes the interaction of the fields Ψ in an external Yang-Mills field
- In order to obtain the fully interacting theory, we must include the degrees of freedom of the gauge fields by adding to the Lagrangian density a gauge invariant kinetic term.

$$\begin{split} \mathcal{L}_{inv} &= -\frac{1}{2} \operatorname{Tr} \mathcal{G}_{\mu\nu} \mathcal{G}^{\mu\nu} + \mathcal{L}(\Psi, \mathcal{D}\Psi) \\ \mathcal{G}_{\mu\nu} &= \partial_{\mu} \mathcal{A}_{\nu} - \partial_{\nu} \mathcal{A}_{\mu} - ig \left[\mathcal{A}_{\mu}, \mathcal{A}_{\nu} \right] \\ \mathcal{G}_{\mu\nu}(x) &\to e^{i\theta^{a}(x)t^{a}} \ \mathcal{G}_{\mu\nu}(x) \ e^{-i\theta^{a}(x)t^{a}} \end{split}$$

Remarks:

No terms proportional to A_µA^µ. ⇒ the gauge fields describe massless particles. Useless for Physics??

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- The coupling constant g appears in the covariant derivative of the fields Ψ. They are all coupled with the same strength.

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- Extension to $G = G_1 \times ... \times G_n$ semi-simple. $\Rightarrow n$ independent coupling constants.

Gell-Mann and Glashow, 1960

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- ► Extension to G = G₁ × ... × G_n semi-simple. ⇒ n independent coupling constants. Gell-Mann and Glashow, 1960

• If one of the factors is Abelian \Rightarrow no charge quantisation.

Spontaneous Symmetry Breaking (SSB)

An infinite system may exhibit the phenomenon of phase transitions. It often implies a reduction in the symmetry of the ground state.

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- An infinite system may exhibit the phenomenon of phase transitions. It often implies a reduction in the symmetry of the ground state.
- For a field theory, in many cases, we encounter at least two phases:

(i) The unbroken, or, the Wigner phase: A symmetry is manifest in the spectrum of the theory whose excitations form irreducible representations of the symmetry group. For a gauge theory the vector gauge bosons are massless and belong to the adjoint representation.

(ii) *The spontaneously broken phase*: Part of the symmetry is hidden from the spectrum. For a gauge theory, some of the gauge bosons become massive.

An example from Classical Mechanics



$$IE\frac{d^{4}X}{dz^{4}} + F\frac{d^{2}X}{dz^{2}} = 0 \quad ; \quad IE\frac{d^{4}Y}{dz^{4}} + F\frac{d^{2}Y}{dz^{2}} = 0$$
$$X = X'' = Y = Y'' = 0 \text{ for } z = 0 \text{ and } z = I$$

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An example from Classical Mechanics

• A symmetric solution always exists: X = Y = 0

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$$F \ge F_{cr} = \frac{\pi^2 El}{l^2}$$
 asymmetric solutions appear:
 $X = C \sin kz$; $kl = n\pi$; $n = 1,...$; $k^2 = F/El$
They correspond to lower energy.

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What happened to the original symmetry?

An example from Classical Mechanics

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They correspond to lower energy.

- What happened to the original symmetry?
- The ground state is degenerate.

A field theory example

•
$$\mathcal{L}_1 = (\partial_\mu \phi)(\partial^\mu \phi^*) - M^2 \phi \phi^* - \lambda (\phi \phi^*)^2$$

Invariant under U(1) global transformations: $\phi(x) \rightarrow e^{i\theta}\phi(x)$

• The Hamiltonian is given by:

$$\begin{aligned} \mathcal{H}_1 &= (\partial_0 \phi)(\partial_0 \phi^*) + (\partial_i \phi)(\partial_i \phi^*) + V(\phi) \\ V(\phi) &= M^2 \phi \phi^* + \lambda (\phi \phi^*)^2 \end{aligned}$$

- The symmetric solution is $\phi(x) = 0$.
- The minimum energy configuration corresponds to:

 $\phi(x) = {
m constant} = \phi$ such that $V(\phi)$ is minimum, solution of: V' = 0

A field theory example



The potential $V(\phi)$ with $\lambda > 0$ and $M^2 \ge 0$. The only solution is the symmetric one $\phi = 0$.

A field theory example



The potential $V(\phi)$ with $\lambda > 0$ and $M^2 < 0$.

 $\phi = 0$ is a local maximum. An entire circle of minima at the complex ϕ -plane with radius $v = (-M^2/2\lambda)^{1/2}$. Any point on it corresponds to a spontaneous breaking of the U(1) symmetry.

A field theory example

• Conclusion: $M^2 = 0$ is a critical point.

For $M^2 > 0$ the symmetric solution is stable.

For $M^2 < 0$ spontaneous symmetry breaking occurs.

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► In order to reach the stable solution we translate the field ϕ . $\phi(x) = \frac{1}{\sqrt{2}} [v + \psi(x) + i\chi(x)]$ $\mathcal{L}_1(\phi) \rightarrow \mathcal{L}_2(\psi, \chi) = \frac{1}{2} (\partial_\mu \psi)^2 + \frac{1}{2} (\partial_\mu \chi)^2 - \frac{1}{2} (2\lambda v^2) \psi^2$ $-\lambda v \psi (\psi^2 + \chi^2) - \frac{\lambda}{4} (\psi^2 + \chi^2)^2$

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• χ is massless (*Goldstone mode*).

A field theory example

L₂ is still invariant.

$$\delta\psi = -\theta\chi$$
 ; $\delta\chi = \theta\psi + \theta\mathbf{v}$

We still have a conserved current:

$$j_{\mu} \sim \psi \partial_{\mu} \chi - \chi \partial_{\mu} \psi + \mathbf{v} \partial_{\mu} \chi$$

 $\partial^{\mu} j_{\mu}(\mathbf{x}) = \mathbf{0}$

It is the minimum energy configuration which is not invariant.

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It is the minimum energy configuration which is not invariant.

 Goldstone Theorem: Spontaneous breaking of a continuous symmetry ⇒ A massless particle (Needs Lorentz invariance and positivity)

SSB: Gauge Symmetries: I. Abelian

Consider the gauge theory extension of the previous model:

$$\mathcal{L}_1=-rac{1}{4} {F}^2_{\mu
u}+|(\partial_\mu+{\it ie} A_\mu)\phi|^2-M^2\phi\phi^*-\lambda(\phi\phi^*)^2$$

 \mathcal{L}_1 is invariant under the gauge transformation:

$$\phi(x) \rightarrow e^{i\theta(x)}\phi(x)$$
 ; $A_{\mu} \rightarrow A_{\mu} - \frac{1}{e}\partial_{\mu}\theta(x)$

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Consider the gauge theory extension of the previous model:

 *L*₁ = -¹/₄*F*²_{µν} + |(∂_µ + ieA_µ)φ|² - M²φφ^{*} - λ(φφ^{*})²

 *L*₁ is invariant under the gauge transformation:
 φ(x) → e^{iθ(x)}φ(x) ; A_µ → A_µ - ¹/_e∂_µθ(x)

 Same analysis for λ > 0 and M² < 0 yields:

$$\mathcal{L}_1 \rightarrow \mathcal{L}_2 = -\frac{1}{4} F_{\mu\nu}^2 + \frac{e^2 v^2}{2} A_{\mu}^2 + e v A_{\mu} \partial^{\mu} \chi + \frac{1}{2} (\partial_{\mu} \psi)^2 + \frac{1}{2} (\partial_{\mu} \chi)^2 - \frac{1}{2} (2\lambda v^2) \psi^2 + \dots$$

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SSB: Gauge Symmetries: I. Abelian

► L₂ is invariant under the gauge transformation:

$$\begin{split} \psi(x) &\to \cos\theta(x)[\psi(x) + v] - \sin\theta(x)\chi(x) - v \\ \chi(x) &\to \cos\theta(x)\chi(x) + \sin\theta(x)[\psi(x) + v] \\ A_{\mu} &\to A_{\mu} - \frac{1}{e}\partial_{\mu}\theta(x) \end{split}$$

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- \mathcal{L}_2 contains a term proportional to A^2 . A massive photon??
- Degrees of freedom:

 $L_1: 2+2=4$

 \mathcal{L}_2 : 2+3=5 ??

Notice the term $evA_{\mu}\partial^{\mu}\chi$

In order to make this counting easier, let us choose a different parametrisation:

 $\phi(x) = \frac{1}{\sqrt{2}} [v + \rho(x)] e^{i\zeta(x)/v} \quad ; \quad A_{\mu}(x) = B_{\mu}(x) - \frac{1}{ev} \partial_{\mu}\zeta(x)$ A gauge transformation: $\zeta(x) \to \zeta(x) + v\theta(x)$

$$\begin{aligned} \mathcal{L}_1 \ \to \ \mathcal{L}_3 &= -\frac{1}{4} B_{\mu\nu}^2 + \frac{e^2 v^2}{2} B_{\mu}^2 + \frac{1}{2} (\partial_{\mu} \rho)^2 - \frac{1}{2} (2\lambda v^2) \rho^2 \\ &- \frac{\lambda}{4} \rho^4 + \frac{1}{2} e^2 B_{\mu}^2 (2v\rho + \rho^2) \\ &B_{\mu\nu} &= \partial_{\mu} B_{\nu} \partial_{\nu} B_{\mu} \end{aligned}$$

The ζ field has disappeared!!

• \mathcal{L}_3 describes the interaction of:

- A massive spin-one field : $B_\mu(x) \rightarrow 3$ degrees of freedom
- ullet A massive, real, scalar field : ho(x) $\,
 ightarrow\,$ 1 degree of freedom

There is no more any gauge invariance left. No massless particles. The ζ degree of freedom gave rise to the longitudinal component of the vector boson.

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► Conclusion: We obtained three different Lagrangian densities: L₁, L₂, L₃.

L₃ describes the interaction of:

- A massive spin-one field : $B_\mu(x) \rightarrow 3$ degrees of freedom
- ullet A massive, real, scalar field : $ho(x) \ o \ 1$ degree of freedom

There is no more any gauge invariance left. No massless particles. The ζ degree of freedom gave rise to the longitudinal component of the vector boson.

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- They all describe the same Physics.

• \mathcal{L}_3 describes the interaction of:

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- ullet A massive, real, scalar field : $ho(x) \ o \ 1$ degree of freedom

There is no more any gauge invariance left. No massless particles. The ζ degree of freedom gave rise to the longitudinal component of the vector boson.

- ► Conclusion: We obtained three different Lagrangian densities: L₁, L₂, L₃.
- They all describe the same Physics.
- But not necessarily in perturbation theory!

- \mathcal{L}_1 :
 - It is gauge invariant.

 \bullet In the quadratic part it has an imaginary mass \rightarrow not suitable for perturbation expansion.

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 $\blacktriangleright \mathcal{L}_2$:

- It is gauge invariant.
- It has redundant degrees of freedom.
- It has a correct quadratic part for a perturbation expansion.

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► L₃ :

- No gauge invariance. Only physical degrees of freedom.
- Non-renormalisable by power counting.
- \bullet It can be obtained from \mathcal{L}_2 by a suitable choice of gauge.

• Assume a gauge Lie-group G with m generators $\rightarrow m$ massless gauge bosons.

• Add a multiplet of scalar fields ϕ_i belonging to an *n*-dim. repr.

$$\mathcal{L} = -\frac{1}{4} Tr(F_{\mu\nu}F^{\mu\nu}) + (D_{\mu}\Phi)^{\dagger}D^{\mu}\Phi - V(\Phi)$$
$$D_{\mu}\phi_{i} = \partial_{\mu}\phi_{i} - ig^{(a)}T^{a}_{ij}A^{a}_{\mu}\phi_{j}$$

• Choose the parameters in V such that the minimum is not at $\Phi = 0$ but rather at $\Phi = v$.

• The *m* generators of *G* can be separated into two classes: *h* generators which annihilate *v* and form the Lie algebra of a subgroup *H* and the m - h others represented, in the representation of Φ , by matrices T^a , such that $T^a v \neq 0$.

• Any vector in the orbit of v, *i.e.* of the form $e^{iw^aT^a}v$, is an equivalent minimum of the potential.

• $\Phi \rightarrow \Phi + v$

• Decompose Φ into components along the orbit of v and orthogonal to it:

$$\Phi(x) = i \sum_{a=1}^{m-h} \frac{\chi^{a}(x) T^{a} v}{|T^{a} v|} + \sum_{b=1}^{n-m+h} \psi^{b}(x) u^{b} + v$$

The u^b 's are orthogonal to all the T^av 's. The corresponding generators span the coset space G/H.

• The fields χ^a will give the longitudinal components of the m-h gauge bosons.

- The fields ψ^b will remain physical.
- There is always at least one field $\psi.$

SSB: Gauge Symmetries. Conclusions:

The Brout-Englert-Higgs Mechanism

• The vector bosons corresponding to spontaneously broken generators of a gauge group become massive.

• The corresponding Goldstone bosons decouple and disappear from the physical spectrum.

• Their degrees of freedom become the longitudinal components of the vector bosons.

• Gauge bosons corresponding to unbroken generators remain massless.

• There is always at least one physical, massive, scalar particle.

Model Building: A five step programme

1) Choose a gauge group G.

2) Choose the fields of the "elementary" particles and assign them to representations of G. Include scalar fields to allow for the Higgs mechanism.

3) Write the most general renormalisable Lagrangian invariant under G. At this stage gauge invariance is still exact and all gauge vector bosons are massless.

4) Choose the parameters of the Higgs potential so that spontaneous symmetry breaking occurs.

5) Translate the scalars and rewrite the Lagrangian in terms of the translated fields. Choose a suitable gauge and quantise the theory.

A remark: Gauge theories provide only the general framework, not a detailed model. The latter will depend on the particular choices made in steps 1) and 2).

A. The lepton world

Step 1. We have four vector bosons: W⁺, W⁻, Z⁰ and γ ⇒ We need a group with four generators. ⇒
 G = U(2) ~ SU(2) × U(1)

Quantum number assignment: $Q = T_3 + \frac{1}{2}Y$

A. The lepton world

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▶ Step 2. Three families \Rightarrow Simplest solution: Three copies

$$\Psi_L^i(x) = \frac{1}{2}(1+\gamma_5) \begin{pmatrix} \nu_i(x) \\ \ell_i^-(x) \end{pmatrix} \quad ; \quad i = 1, 2, 3$$

$$\nu_{iR}(x) = \frac{1}{2}(1-\gamma_5)\nu_i(x)$$
 (?); $\ell_{iR}^-(x) = \frac{1}{2}(1-\gamma_5)\ell_i^-(x)$

 $\Psi_L^i(x) \to e^{i\vec{\tau}\vec{ heta}(x)}\Psi_L^i(x) \quad ; \quad R_i(x) \to R_i(x)$ $Y(\Psi_L^i) = -1 \quad ; \quad Y(R_i) = -2$

Higgs choice:

$$\Phi = \left(egin{array}{c} \phi^+ \ \phi^0 \end{array}
ight) \quad ; \quad \Phi(x) o e^{i ec heta ec heta}(x) \Phi(x) \quad ; \quad Y(\Phi) = 1$$

Step 3. Assume conservation of lepton numbers:

$$\mathcal{L} = -\frac{1}{4} \vec{W}_{\mu\nu} \cdot \vec{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + |D_{\mu}\Phi|^{2} - V(\Phi) + \sum_{i=1}^{3} \left[\bar{\Psi}_{L}^{i} i \vec{D} \Psi_{L}^{i} + \bar{R}_{i} i \vec{D} R_{i} - G_{i} (\bar{\Psi}_{L}^{i} R_{i} \Phi + h.c.) \right]$$

$$\begin{split} \vec{W}_{\mu\nu} &= \partial_{\mu}\vec{W}_{\nu} - \partial_{\nu}\vec{W}_{\mu} + g\vec{W}_{\mu} \times \vec{W}_{\nu} \qquad B_{\mu\nu} = \partial_{\mu}B_{\nu} - \partial_{\nu}B_{\mu} \\ D_{\mu}\Psi_{L}^{i} &= \left(\partial_{\mu} - ig\frac{\vec{\tau}}{2}\cdot\vec{W}_{\mu} + i\frac{g'}{2}B_{\mu}\right)\Psi_{L}^{i} \quad ; \quad D_{\mu}R_{i} = \left(\partial_{\mu} + ig'B_{\mu}\right)R_{i} \\ D_{\mu}\Phi &= \left(\partial_{\mu} - ig\frac{\vec{\tau}}{2}\cdot\vec{W}_{\mu} - i\frac{g'}{2}B_{\mu}\right)\Phi \end{split}$$

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$$V(\Phi) = \mu^2 \Phi^{\dagger} \Phi + \lambda (\Phi^{\dagger} \Phi)^2$$

Gauge bosons and leptons are massless

• Step 4. We choose
$$\mu^2 < 0 \rightarrow v^2 = -\mu^2/\lambda$$

We put the breaking along the real part of ϕ^0

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Gauge bosons and leptons are massless

- Step 4. We choose μ² < 0 → v² = −μ²/λ
 We put the breaking along the real part of φ⁰
- Step 5. Translate the Higgs field:

$$\Phi
ightarrow \Phi + rac{1}{\sqrt{2}} \left(egin{array}{c} 0 \ v \end{array}
ight) \qquad v^2 = -rac{\mu^2}{\lambda}$$

This transforms the Lagrangian and generates new terms. Some of them:

► Fermion mass terms:

$$m_e = rac{1}{\sqrt{2}} G_e v$$
 $m_\mu = rac{1}{\sqrt{2}} G_\mu v$ $m_\tau = rac{1}{\sqrt{2}} G_\tau v$

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Gauge boson mass terms:

$$\frac{1}{8}v^2[g^2(W^1_{\mu}W^{1\mu} + W^2_{\mu}W^{2\mu}) + (g'B_{\mu} - gW^3_{\mu})^2]$$
$$W^{\pm}_{\mu} = \frac{W^1_{\mu} \mp iW^2_{\mu}}{\sqrt{2}} \quad ; \quad m_W = \frac{vg}{2}$$

After diagonalisation, we obtain the neutral bosons:

$$Z_{\mu} = sin\theta_{W}B_{\mu} - cos\theta_{W}W_{\mu}^{3} ; m_{Z} = \frac{v(g^{2} + {g'}^{2})^{1/2}}{2} = \frac{m_{W}}{cos\theta_{W}}$$
$$A_{\mu} = cos\theta_{W}B_{\mu} + sin\theta_{W}W_{\mu}^{3} ; m_{A} = 0$$
$$g'/g = tan\theta_{W}$$

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$$A_{\mu} = \cos\theta_{W}B_{\mu} + \sin\theta_{W}W_{\mu}^{3} ; \quad m_{A} = 0$$
$$g'/g = \tan\theta_{W}$$

► Physical Higgs mass: $m_H = \sqrt{-2\mu^2} = \sqrt{2\lambda v^2}$

Extension to hadrons

- The lepton-hadron universality suggests to use also doublets for the left-handed quarks and singlets for the right-handed ones.
- New features: Individual quantum numbers are not separately conserved. All quarks have non-vanishing masses.
- A naïve assignment:

$$Q_{L}^{i}(x) = \frac{1}{2}(1 + \gamma_{5}) \begin{pmatrix} U^{i}(x) \\ D^{i}(x) \end{pmatrix} ; \quad U_{R}^{i}(x) ; \quad D_{R}^{i}(x)$$
$$U^{i} = u, c, t ; \quad D^{i} = d, s, b \quad i = 1, 2, 3$$
$$Y(Q_{L}^{i}) = \frac{1}{3} ; \quad Y(U_{R}^{i}) = \frac{4}{3} ; \quad Y(D_{R}^{i}) = -\frac{2}{3}$$

• The presence of the second right-hand singlet implies a second Yukawa term:

$$\mathcal{L}_{Yuk} = \mathcal{G}_d(\bar{Q}_L D_R \Phi + h.c.) + \mathcal{G}_u(\bar{Q}_L U_R \tilde{\Phi} + h.c.)$$

Extension to hadrons

- Had we only one family, this would have been the end of the story! BUT...
- The correct Yukawa term is:

$$\mathcal{L}_{Yuk} = \sum_{i,j} \left[(\bar{Q}_L^i G_d^{ij} D_R^j \Phi + h.c.) \right] + \sum_i \left[G_u^i (\bar{Q}_L^i U_R^i \tilde{\Phi} + h.c.) \right]$$

- After translation of the Higgs field: Masses for the up quarks $m_u = G_u^1 v$, $m_c = G_u^2 v$ and $m_t = G_u^3 v$. A mass matrix for the down quarks $G_d^{ij} v$.
- We prefer to work in a field space with diagonal masses: $\tilde{D}^i = U^{ij}D^j$ such that $U^{\dagger}G_dU = \text{diag}(m_d, m_s, m_b)$.
- For two families, with θ =The Cabibbo angle:

$$\mathcal{C} = \left(egin{array}{cc} \cos heta & \sin heta \ -\sin heta & \cos heta \end{array}
ight)$$

Extension to hadrons

• For three families:

$$KM = \begin{pmatrix} c_1 & s_1c_3 & s_1s_3 \\ -s_1c_3 & c_1c_2c_3 - s_2s_3e^{i\delta} & c_1c_2s_3 + s_2c_3e^{i\delta} \\ -s_1s_2 & c_1s_2c_3 + c_2s_3e^{i\delta} & c_1s_2s_3 - c_2c_3e^{i\delta} \end{pmatrix}$$

The Standard Model: The full Lagrangian

$$\mathcal{L} = -\frac{1}{4} \vec{W}_{\mu\nu} \cdot \vec{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + |D_{\mu}\Phi|^{2} - V(\Phi)$$

$$+ \sum_{i=1}^{3} \left[\bar{\Psi}_{L}^{i} i \vec{D} \Psi_{L}^{i} + \bar{R}_{i} i \vec{D} R_{i} - G_{i} (\bar{\Psi}_{L}^{i} R_{i} \Phi + h.c.) \right]$$

$$+ \bar{Q}_{L}^{i} i \vec{D} Q_{L}^{i} + \bar{U}_{R}^{i} i \vec{D} U_{R}^{i} + \bar{D}_{R}^{i} i \vec{D} D_{R}^{i} + G_{u}^{i} (\bar{Q}_{L}^{i} U_{R}^{i} \tilde{\Phi} + h.c.) \right]$$

$$+ \sum_{i,j=1}^{3} \left[(\bar{Q}_{L}^{i} G_{d}^{ij} D_{R}^{j} \Phi + h.c.) \right]$$

$$D_{\mu}Q_{L}^{i} = \left(\partial_{\mu} - ig\frac{\vec{\tau}}{2} \cdot \vec{W}_{\mu} - i\frac{g'}{6}B_{\mu}\right)Q_{L}^{i}$$

$$D_{\mu}U_{R}^{i} = \left(\partial_{\mu} - i\frac{2g'}{3}B_{\mu}\right)U_{R}^{i}$$

$$D_{\mu}D_{R}^{i} = \left(\partial_{\mu} + i\frac{g'}{3}B_{\mu}\right)D_{R}^{i}$$

The Standard Model: Arbitrary parameters

- The two gauge coupling constants g and g'.
- The two parameters of the Higgs potential λ and μ^2 .

• Three Yukawa coupling constants for the three lepton families, $G_{e,\mu, au}$. $(m_{
u}=0)$.

- Six Yukawa coupling constants for the three quark families, $G_u^{u,c,t}$, and $G_d^{d,s,b}$.
- Four parameters of the KM matrix, the three angles and the phase $\delta.$

• All but two come from the Higgs system.

- The gauge boson-fermion couplings.
 - The photon couplings

$$\frac{gg'}{(g^2+g'^2)^{1/2}}\left[\bar{e}\gamma^{\mu}e+\sum_{a=1}^3\left(\frac{2}{3}\bar{u}^a\gamma^{\mu}u^a-\frac{1}{3}\bar{d}^a\gamma^{\mu}d^a\right)+\ldots\right]A_{\mu}$$

$$e = \frac{gg'}{(g^2 + {g'}^2)^{1/2}} = gsin\theta_W = g'cos\theta_W$$

• The charged W couplings

$$\frac{g}{2\sqrt{2}} \left(\bar{\nu}_e \gamma^\mu (1+\gamma_5) e + \sum_{a=1}^3 \bar{u}^a \gamma^\mu (1+\gamma_5) d^a_{KM} + \dots \right) W^+_\mu + h.c.$$
$$\frac{G}{\sqrt{2}} = \frac{g^2}{8m_W^2} = \frac{1}{2v^2}$$

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• The Z^0 couplings

$$-\frac{e}{2}\frac{1}{\sin\theta_W\cos\theta_W}\left[\bar{\nu}_L\gamma^\mu\nu_L + (\sin^2\theta_W - \cos^2\theta_W)\bar{e}_L\gamma^\mu e_L + 2\sin^2\theta_W\bar{e}_R\gamma^\mu e_R + \ldots\right]Z_\mu$$

$$\frac{e}{2} \sum_{a=1}^{3} \left[\left(\frac{1}{3} tan\theta_{W} - cot\theta_{W} \right) \bar{u}_{L}^{a} \gamma^{\mu} u_{L}^{a} + \left(\frac{1}{3} tan\theta_{W} + cot\theta_{W} \right) \bar{d}_{L}^{a} \gamma^{\mu} d_{L}^{a} \right. \\ \left. + \frac{2}{3} tan\theta_{W} \left(2 \bar{u}_{R}^{a} \gamma^{\mu} u_{R}^{a} - \bar{d}_{R}^{a} \gamma^{\mu} d_{R}^{a} \right) \right. + \left. \ldots \right] Z_{\mu}$$

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Remarks :

(i) The neutral current is diagonal in flavour space. (ii) The axial part is $\sim [\bar{u}\gamma_{\mu}\gamma_{5}u - \bar{d}\gamma_{\mu}\gamma_{5}d]$

The gauge boson self-couplings

•
$$-\frac{1}{4}\vec{W}_{\mu
u}\cdot\vec{W}^{\mu
u}$$
 \Rightarrow

$$- ig(sin\theta_{W}A^{\mu} - cos\theta_{W}Z^{\mu})(W^{\nu-}W^{+}_{\mu\nu} - W^{\nu+}W^{-}_{\mu\nu})
- ig(sin\theta_{W}F^{\mu\nu} - cos\theta_{W}Z^{\mu\nu})W^{-}_{\mu}W^{+}_{\nu}
- g^{2}(sin\theta_{W}A^{\mu} - cos\theta_{W}Z^{\mu})^{2}W^{+}_{\nu}W^{\nu-}
+ g^{2}(sin\theta_{W}A^{\mu} - cos\theta_{W}Z^{\mu})(sin\theta_{W}A^{\nu} - cos\theta_{W}Z^{\nu})W^{+}_{\mu}W^{-}_{\nu}
- \frac{g^{2}}{2}(W^{+}_{\mu}W^{\mu-})^{2} + \frac{g^{2}}{2}(W^{+}_{\mu}W^{-}_{\nu})^{2}
(- 2) V = 2 V$$

$$V_{\mu\nu} = \partial_{\mu} V_{\nu} - \partial_{\nu} V_{\mu},$$

• For a charged, massive W, the magnetic moment μ and the quadrupole moment Q are given by:

$$\mu = \frac{(1+\kappa)e}{2m_W} \qquad Q = -\frac{e\kappa}{m_W^2}$$

• An *SU*(2) prediction: $\kappa = 1$

• The Higgs fermion couplings

Proportional to the fermion mass!

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$$rac{1}{4}(v+\phi)^2 \left[g^2 W^+_\mu W^{-\mu} + (g^2+g'^2) Z_\mu Z^\mu\right]$$

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The five-step programme is complete

The Standard Model and experiment

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The Standard Model and experiment

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They are related to masses and coupling constants and should be determined experimentally.

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Observable	Mesure	Ajustement	O _{mes} -O _{ajust.}
$\Delta \alpha_{had}^{(5)}(m_Z)$	0.02761 ± 0.00036	6 0.02768	
m _z [GeV]	91.1875 ± 0.0021	91.1873	
Γ _z [GeV]	2.4952 ± 0.0023	2.4965	
$\sigma_{\sf had}^0$ [nb]	41.540 ± 0.037	41.481	
R	20.767 ± 0.025	20.739	
A ^{0,I} _{fb}	0.01714 ± 0.00095	5 0.01642	
Α _I (Ρ _τ)	0.1465 ± 0.0032	0.1480	
R _b	0.21638 ± 0.00066	6 0.21566	
R _c	0.1720 ± 0.0030	0.1723	•
A ^{0,b} _{fb}	0.0997 ± 0.0016	0.1037	
A ^{0,c} _{fb}	0.0706 ± 0.0035	0.0742	
A _b	0.925 ± 0.020	0.935	
A _c	0.670 ± 0.026	0.668	
A _I (SLD)	0.1513 ± 0.0021	0.1480	
$sin^2 \theta_{eff}^{lept}(Q_{fb})$	0.2324 ± 0.0012	0.2314	
m _w [GeV]	80.425 ± 0.034	80.398	
Г _w [GeV]	$\textbf{2.133} \pm \textbf{0.069}$	2.094	
m _t [GeV]	178.0 ± 4.3	178.1	
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Figure 6: Data vs theory in the ϵ_3 - ϵ_1 plane (notations as in fig.5)

$$\epsilon_1 = \frac{3G_F m_t^2}{8\sqrt{2}\pi^2} - \frac{3G_F m_W^2}{4\sqrt{2}\pi^2} \tan^2 \theta_W \ln \frac{m_H}{m_Z} + \dots$$
(1)

$$\epsilon_3 = \frac{G_F m_W^2}{12\sqrt{2}\pi^2} \ln \frac{m_H}{m_Z} - \frac{G_F m_W^2}{6\sqrt{2}\pi^2} \ln \frac{m_t}{m_Z} + \dots$$
(2)

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▶ The discovery of weak neutral currents by Gargamelle in 1972

$$u_{\mu} + e^- \rightarrow \nu_{\mu} + e^-$$
; $u_{\mu} + N \rightarrow \nu_{\mu} + X$

Both, their strength and their properties were predicted by the Model.

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A necessary condition for the consistency of the Model is that ∑_i Q_i = 0 inside each family.

When the τ lepton was discovered the *b* and *t* quarks were predicted with the right electric charges.

▶ The discovery of the *W* and *Z* bosons at CERN in 1983

The characteristic relation of the Standard Model with an isodoublet Higgs mechanism $m_Z = m_W/\cos\theta_W$ is checked with very high accuracy (including radiative corrections).

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- ► WHY?

IF THIS SUCCESS PERSISTS, NEW PHYSICS IS PREDICTED FOR LHC