

Plan of the lectures:

- ▶ An introduction to flavour physics
- ▶ Phenomenology of B and D decays
 - ▶ Time evolution and time-dependent asymmetries of $B_{d,s}$
 - ▶ CPV in B_s mixing
 - ▶ Time-dependent studies of “penguin modes”
 - ▶ CPV in charged B decays [measuring γ]
 - ▶ Rare B decays
 - ▶ Exclusive rare B decays
 - ▶ CP violation in the charm system
 - ▶ The puzzle of Δa_{CP}
- ▶ Flavour physics beyond the SM

► Time evolution and time-dependent asymmetries of $B_{d,s}$

$$B_{d,s} \text{ mass eigenstates: } |B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle \quad |B_H\rangle = p|\bar{B}^0\rangle + q|B^0\rangle$$

$$i \frac{d}{dt} \begin{bmatrix} B^0 \\ \bar{B}^0 \end{bmatrix} = [M - i\Gamma/2] \begin{bmatrix} B^0 \\ \bar{B}^0 \end{bmatrix}$$

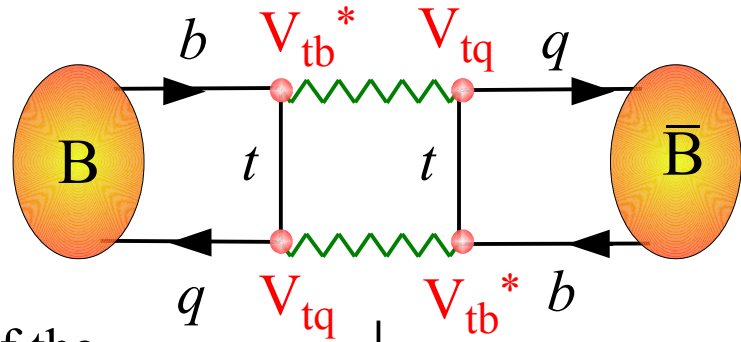
The time evolution can be described
in full generality by means of a
non-Hermitian Hamiltonian

► Time evolution and time-dependent asymmetries of $B_{d,s}$

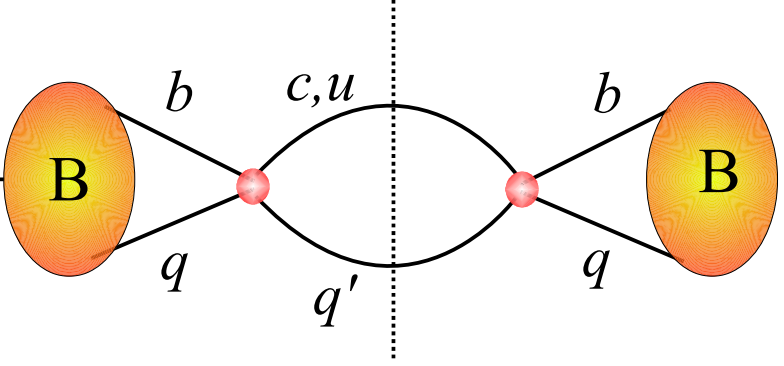
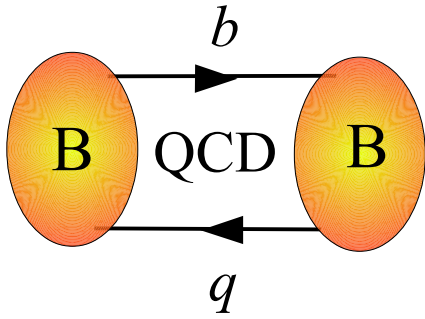
$B_{d,s}$ mass eigenstates: $|B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle$ $|B_H\rangle = p|\bar{B}^0\rangle + q|B^0\rangle$

$$i \frac{d}{dt} \begin{bmatrix} B^0 \\ \bar{B}^0 \end{bmatrix} = [M - i\Gamma/2] \begin{bmatrix} B^0 \\ \bar{B}^0 \end{bmatrix}$$

off-diagonal elements of the mass matrix

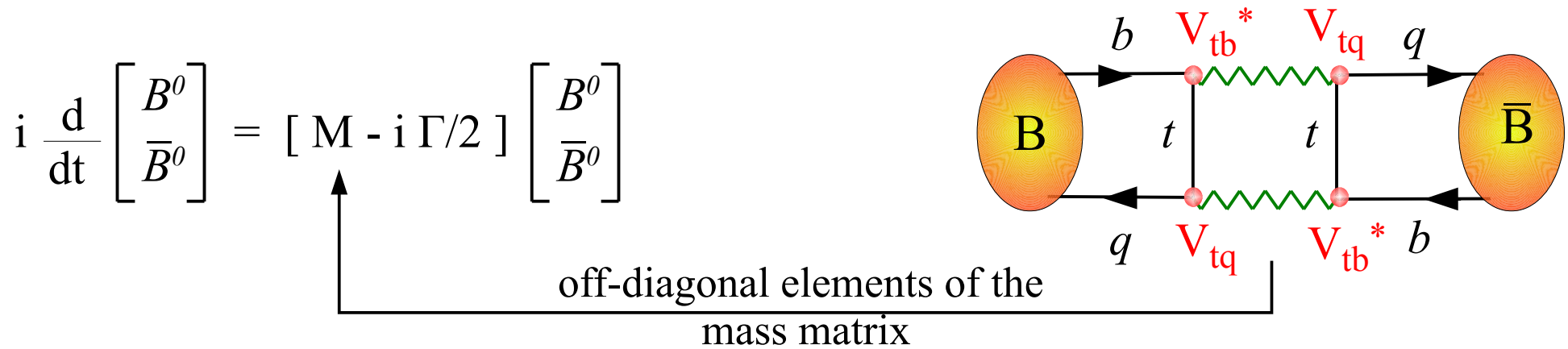


$M_{11} = M_{22}$



► Time evolution and time-dependent asymmetries of $B_{d,s}$

$$B_{d,s} \text{ mass eigenstates: } |B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle \quad |B_H\rangle = p|\bar{B}^0\rangle + q|B^0\rangle$$



$$\frac{q}{p} = \arg(A_{\text{box}}) + O(10^{-3} \text{ due to } \Gamma)$$

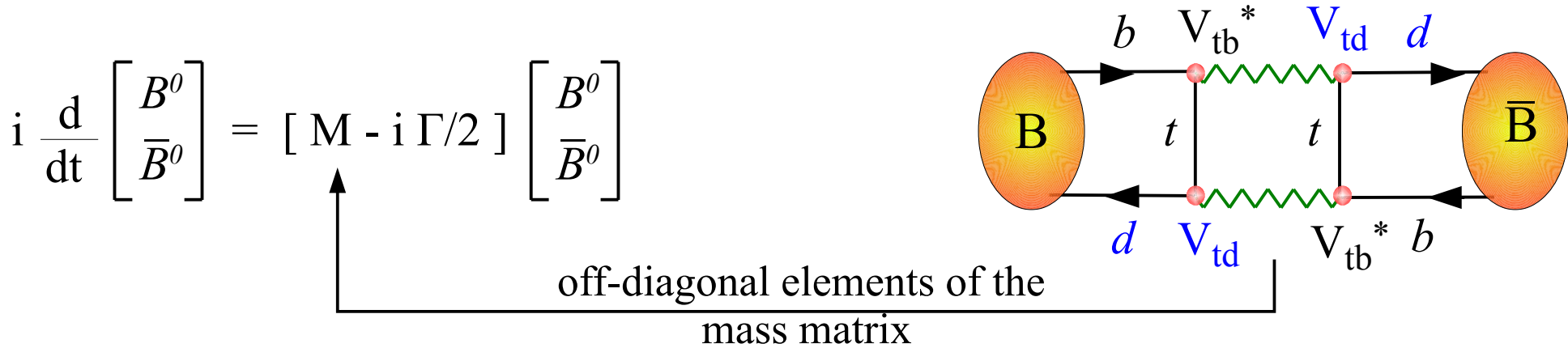
theoretically very clean

$$\Delta m_B \propto |A_{\text{box}}| \times |\langle \bar{B} | (\bar{b}_L \gamma_\mu q_L)^2 | B \rangle|$$

$O(10\%-30\%)$ theory error

► Time evolution and time-dependent asymmetries of $B_{d,s}$

$B_{d,s}$ mass eigenstates: $|B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle$ $|B_H\rangle = p|\bar{B}^0\rangle + q|B^0\rangle$



$$\frac{q}{p} = \frac{(V_{tb}^* V_{td})^2}{|(V_{tb} V_{td}^*)^2|} = e^{-2i\beta}$$

B_d

Large CPV phase
(in the standard CKM phase convention)

► Time evolution and time-dependent asymmetries of $B_{d,s}$

$$B_{d,s} \text{ mass eigenstates: } |B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle \quad |B_H\rangle = p|\bar{B}^0\rangle + q|B^0\rangle$$

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off-diagonal elements of the mass matrix

$$\frac{q}{p} = \frac{(V_{tb}^* V_{ts})^2}{|(V_{tb} V_{ts}^*)^2|} = \underbrace{1 + i \mathcal{O}(\lambda^2)}_{e^{-2i\beta_s}}$$

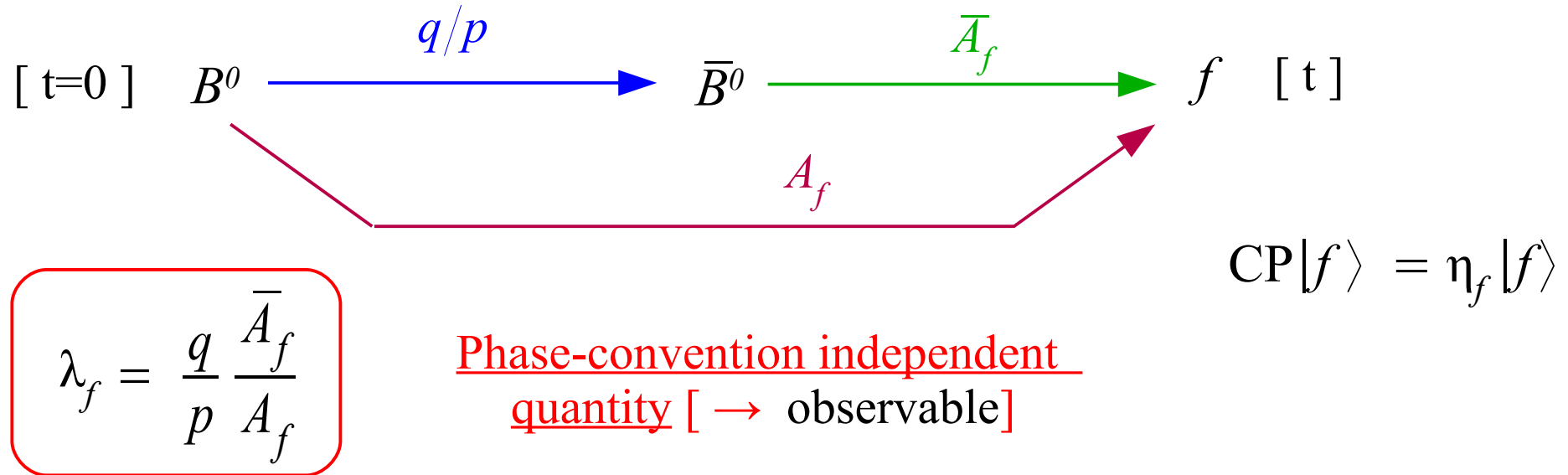
B_s

Negligible CPV phase
and large oscillation
frequency:

$$|\Delta m_{B_s}| \sim \lambda^{-2} |\Delta m_{B_d}|$$

$\sim 18 \text{ ps}^{-1}$ $\sim 0.5 \text{ ps}^{-1}$

The study of time-dependent decays of neutral B into CP eigenstates is a marvelous tool to extract CPV phases in a clean way:

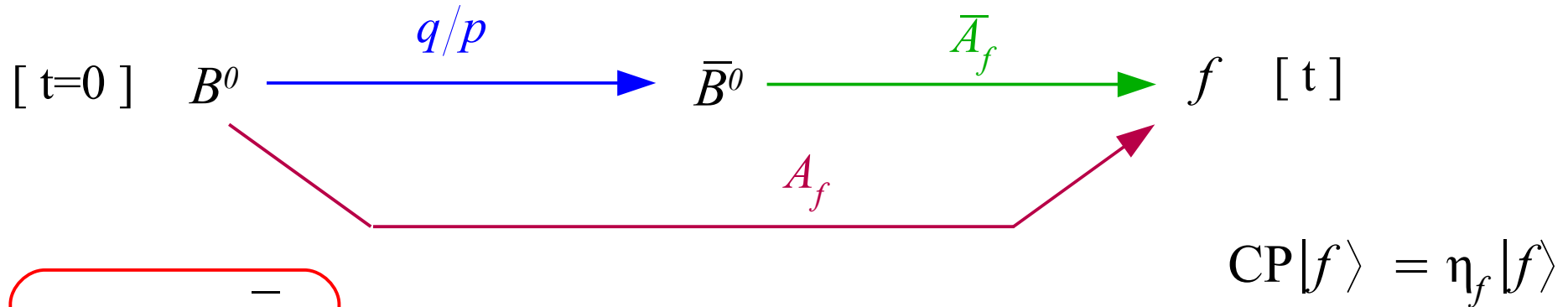


If $|\lambda_f| = 1$ (i.e. if A_f is dominated by a single weak phase) & $\Delta\Gamma = 0$ then :

$$\Gamma(B^0(t) \rightarrow f) \propto e^{-\Gamma_B t} \left[1 - \eta_f \text{Im}(\lambda_f) \sin(\Delta m_B t) \right]$$

$$\Gamma(\bar{B}^0(t) \rightarrow f) \propto e^{-\Gamma_B t} \left[1 + \eta_f \text{Im}(\lambda_f) \sin(\Delta m_B t) \right]$$

The study of time-dependent decays of neutral B into CP eigenstates is a marvelous tool to extract CPV phases in a clean way:



$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$$

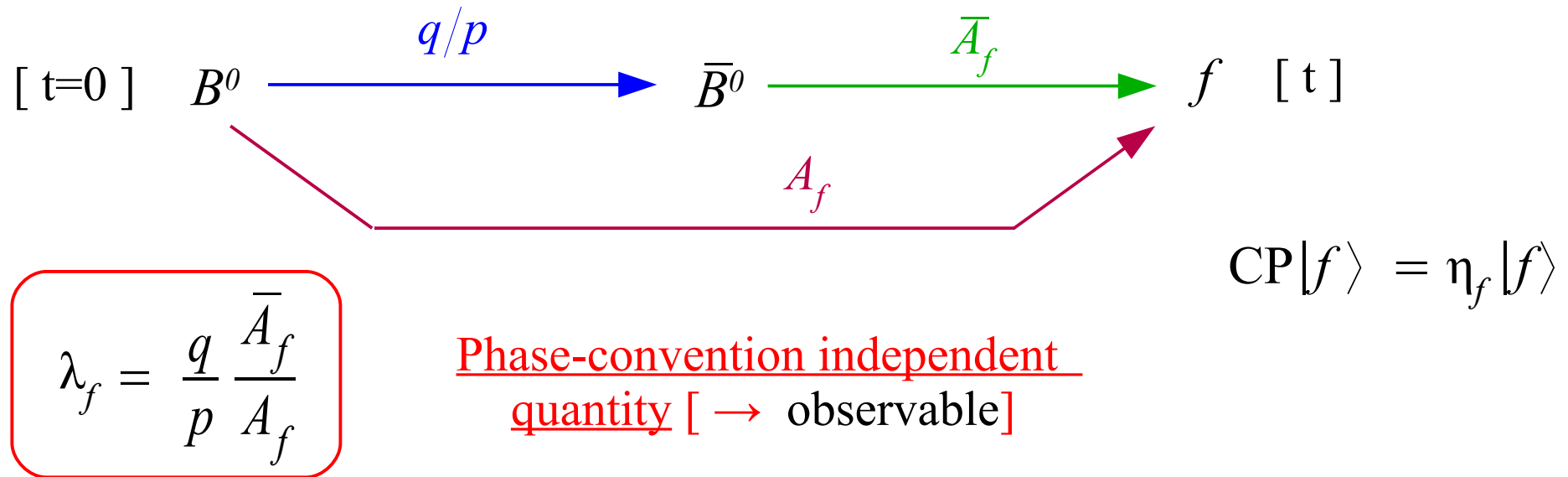
Phase-convention independent
quantity [\rightarrow observable]

If $|\lambda_f| = 1$ (i.e. if A_f is dominated by a single weak phase) & $\Delta\Gamma \neq 0$ then :

$$\Gamma(B^0(t) \rightarrow f) \propto e^{-\Gamma_B t} \left[e^{\Delta\Gamma t/2} (1 + c_f) + e^{-\Delta\Gamma t/2} (1 - c_f) - \eta_f s_f \sin(\Delta m_B t) \right]$$

$$s_f = \text{Im}(\lambda_f) \quad c_f = \text{Re}(\lambda_f)$$

The study of time-dependent decays of neutral B into CP eigenstates is a marvelous tool to extract CPV phases in a clean way:



If $|\lambda_f| = 1$ (i.e. if A_f is dominated by a single weak phase) & $\Delta\Gamma \neq 0$ then :

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Key points to successfully use this method:

$$s_f = \text{Im}(\lambda_f) \quad c_f = \text{Re}(\lambda_f)$$

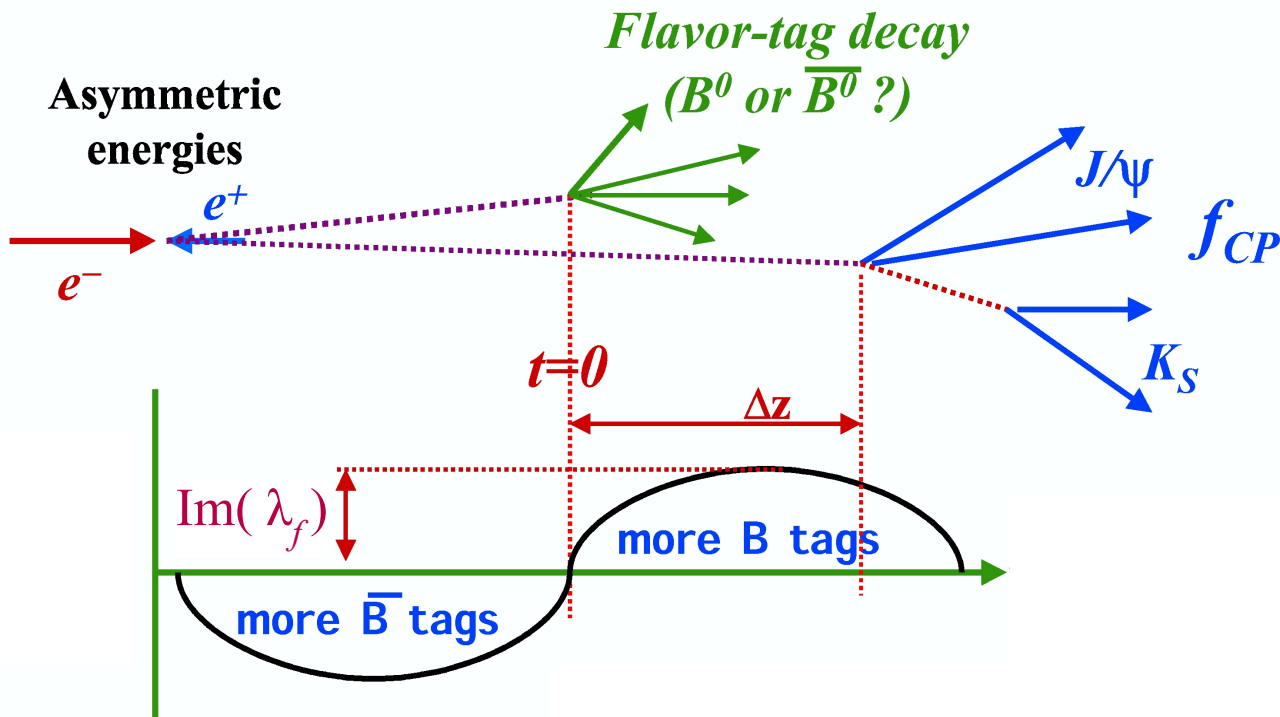
- [EXP]: flavour tagging and time-dependent resolution are essential ingredients
- [TH]: identify final states such that A_f is dominated by a single weak phase

A few words about flavour tagging: B factories vs. hadron colliders

B factories:



- clean environment [$\sigma(B) / \sigma(\text{bkg}) \sim 0.3$]
- coherent quantum state for neutral B
- low stat. [$\sim 10^8$ B pairs / 100 fb^{-1}]
- no B_s [unless running at higher energies with lower luminosity]



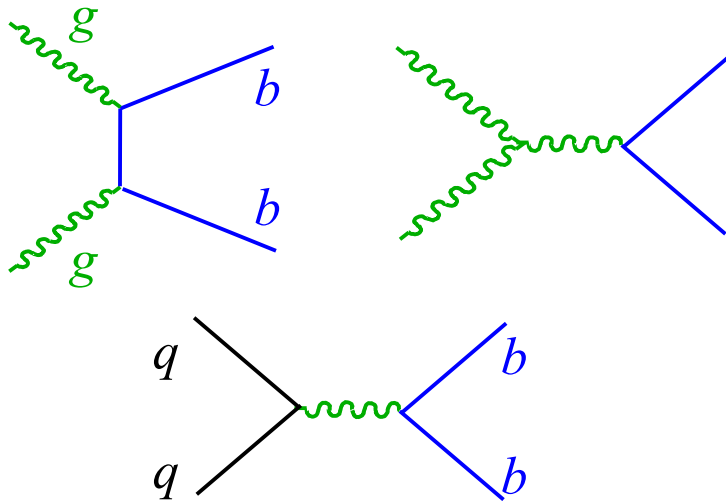
A few words about flavour tagging: B factories vs. hadron colliders

B factories:

$$e^+ + e^- \rightarrow \Psi(4S) \rightarrow B \bar{B}$$

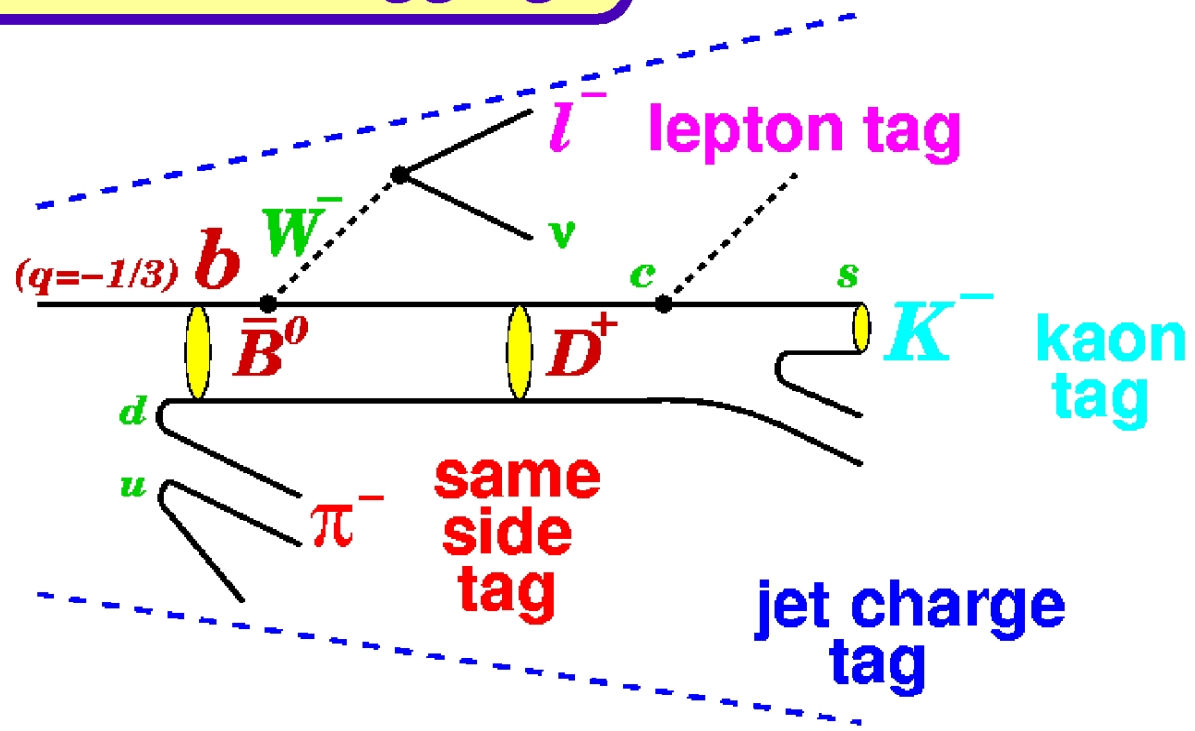
- clean environment [$\sigma(B) / \sigma(\text{bkg}) \sim 0.3$]
- coherent quantum state for neutral B
- low stat. [$\sim 10^8$ B pairs / 100 fb^{-1}]
- no B_s [unless running at higher energies with lower luminosity]

Hadron colliders:



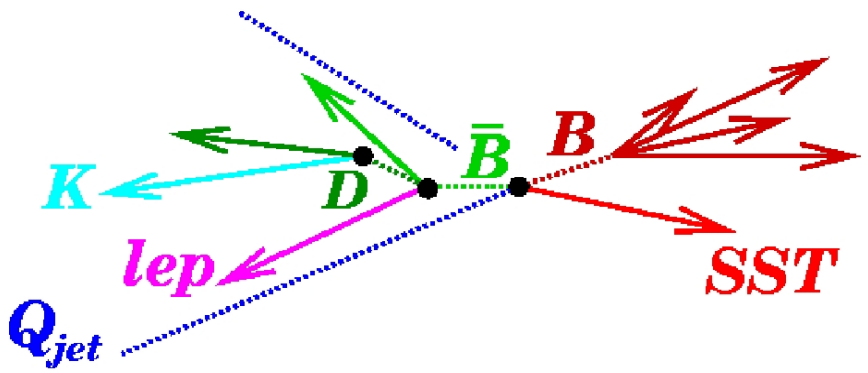
- dirty environment [$\sigma(B) / \sigma(\text{bkg}) < 0.01$]
- incoherent quantum state
- high stat. [$\sim 10^{12}$ B pairs / 1 fb^{-1}]
- all hadrons with b-quarks produced

B Flavour Tagging



B flavour tagging methods:

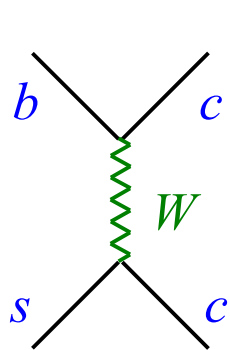
- Opposite side lepton tag
- Jet charge tag
- Same side tag
- Opposite side kaon tag



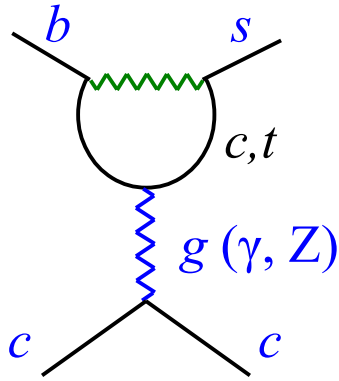
When is A_f dominated by a single weak phase?

$|B_d\rangle \rightarrow |\psi K_S\rangle$

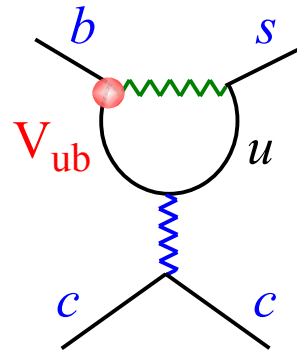
$[b+d \rightarrow c\bar{c}s+d]$



real $O(\lambda^2)$



real $O(\alpha_s \lambda^2)$



$O(\alpha_s \lambda^5)$

dominant amplitude

pollution $\lesssim 1\%$

$\text{Im}(\lambda_f) = \sin(2\beta)$

(from the mixing)

$V_{tb}^* V_{ts} = -V_{cb}^* V_{cs} - V_{ub}^* V_{us}$

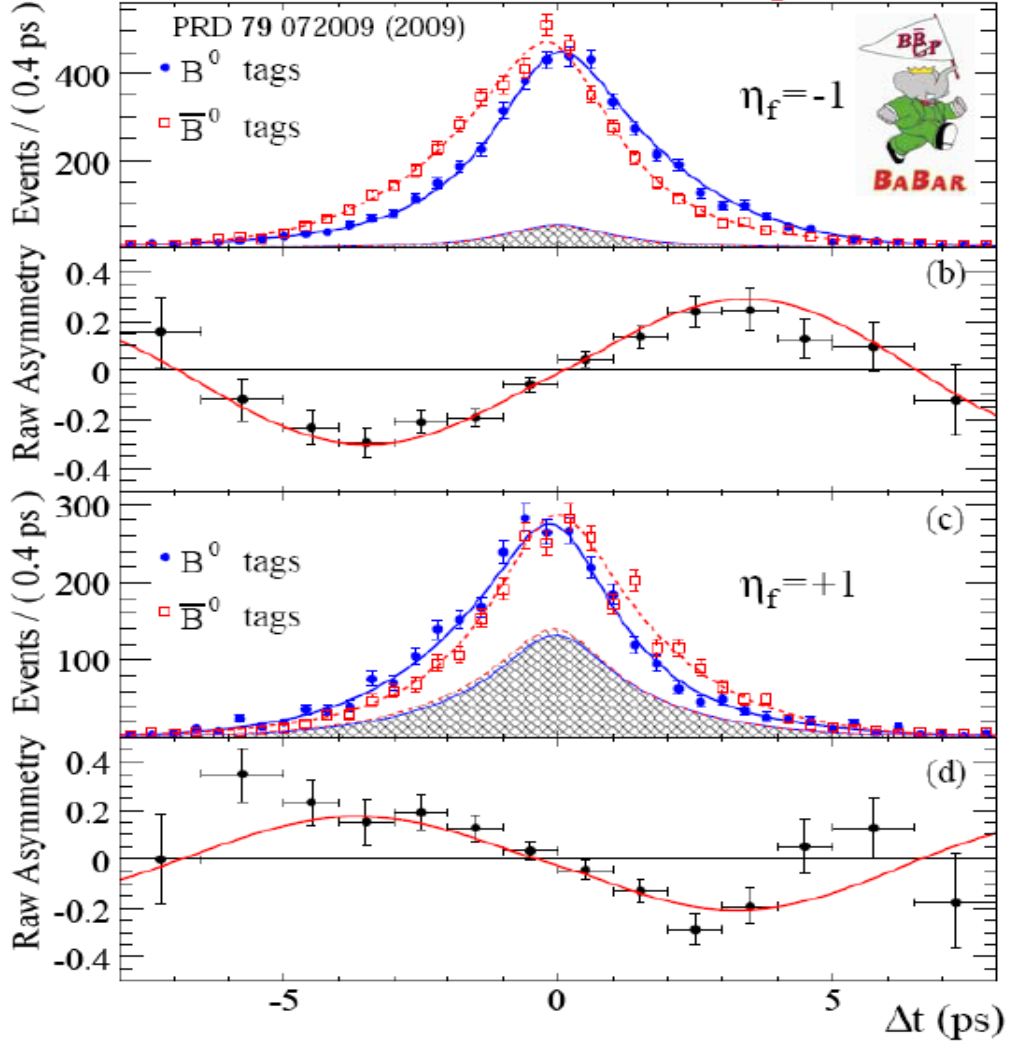
flat triangle

extremely precise constraint in the $\rho-\eta$ plane

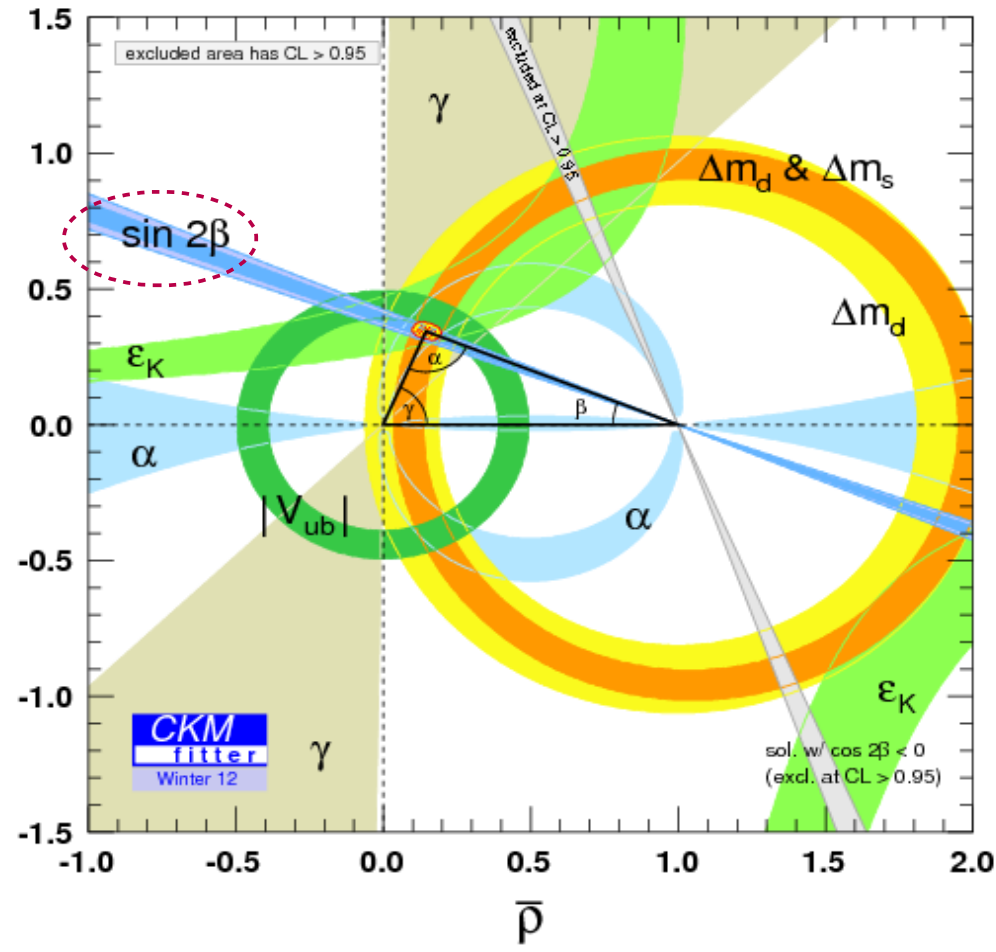


Golden channel for B factories

BaBar’s final result has been published:



A. Bevan, Lepton-Photon 2009

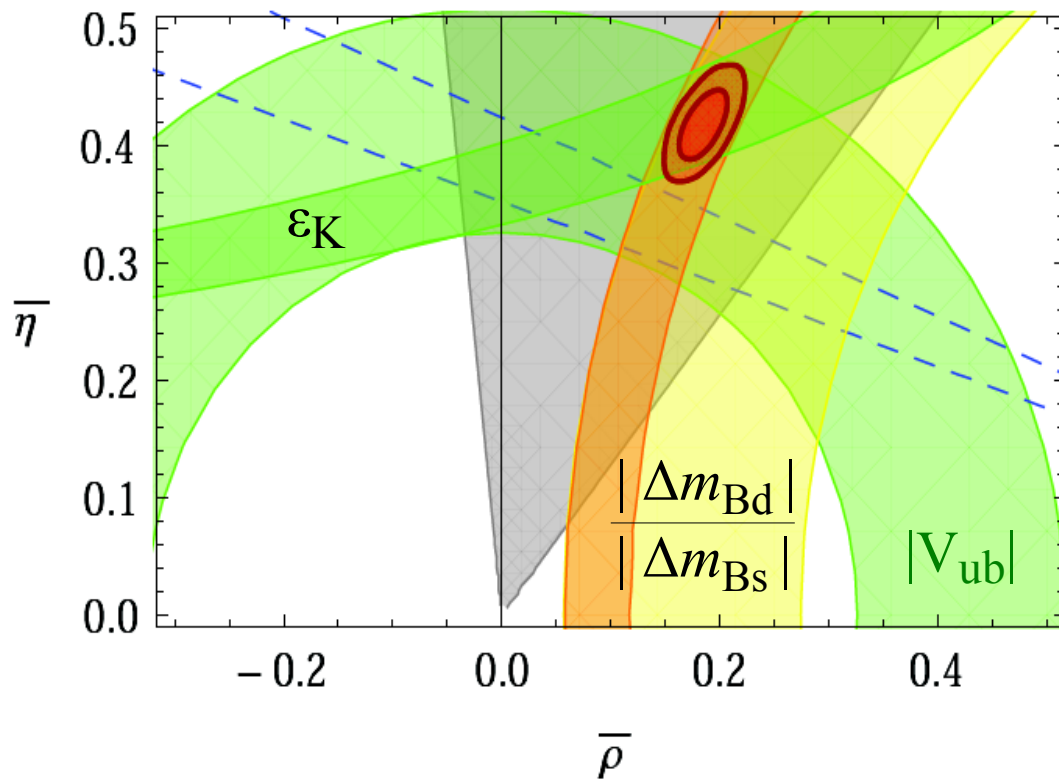


extremely precise constraint in the ρ - η plane

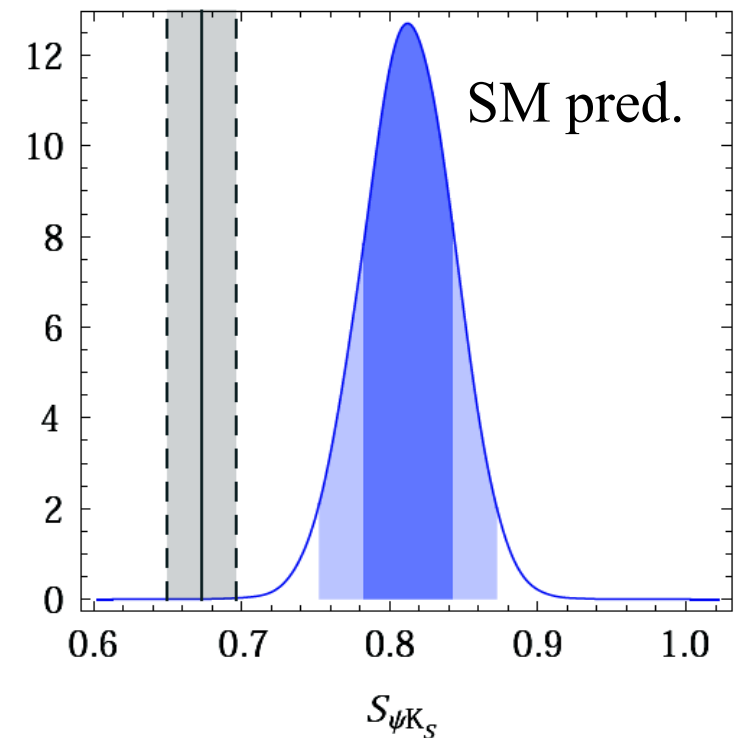
N.B.: Despite the overall consistency of the CKM picture, looking more closely the agreement of the various constraints is not so good. At present there is a $\sim 2\sigma$ tension between

- the value of ε_K (CPV in K^0 mixing) [or $|V_{ub}|$ extracted from $B \rightarrow \tau\nu$]
- the value of $\sin(2\beta)$ extracted from $B_d \rightarrow \psi K$

SM fit, no $S_{\psi K}$ (no B_d mixing phase):

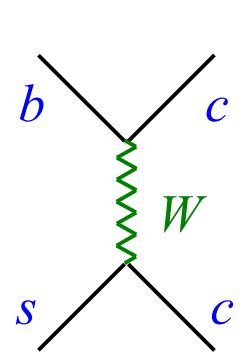


exp.

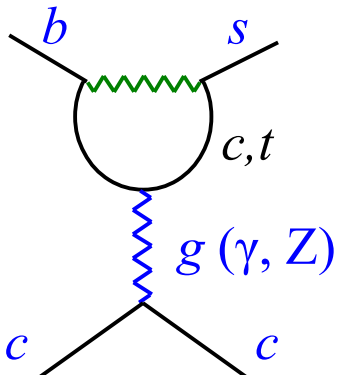


The golden channel for B_s mixing is

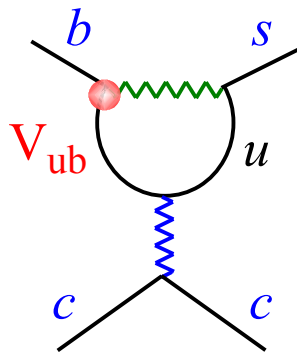
$|B_s\rangle \rightarrow |\psi\phi\rangle$ $[b+s \rightarrow c\bar{c}s+s]$



real $O(\lambda^2)$



real $O(\alpha_s \lambda^2)$



$O(\alpha_s \lambda^5)$

dominant amplitude

pollution $\lesssim 1\%$

$Im(\lambda_f) = \sin(2\beta_s) = 0 + O(\lambda^2) \approx 0.04$

It is not a constraint in the ρ - η plane but is a very significant test of the SM

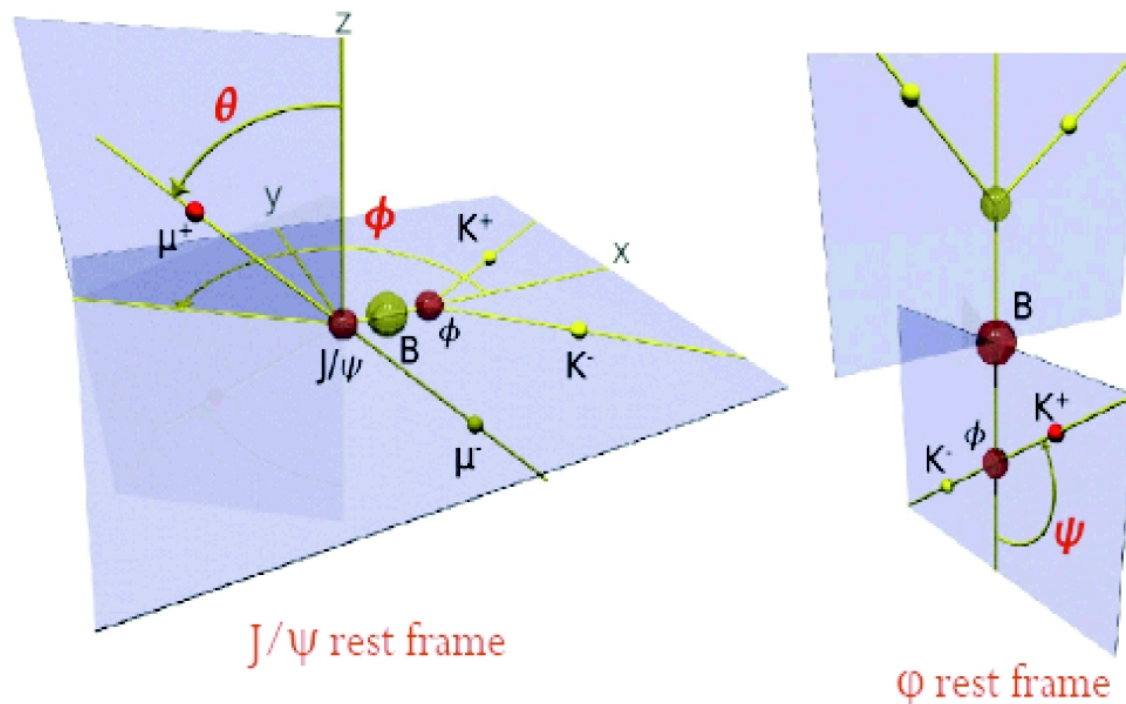


Golden channel for hadron machines

► Measuring CPV in B_s mixing

The extraction of the B_s mixing phase differs (and is somehow more challenging) with respect to the B_d case for three main reasons:

- $|\psi \phi\rangle$ is not a CP eigenstate and a complete angular analysis of the 4-body final state is needed in order to disentangle the amplitudes with different CP
- Since $\Delta\Gamma_s \neq 0$, a simultaneous fit of the width difference and the mixing phase is needed
- The flavour tag is much more involved at hadron machines



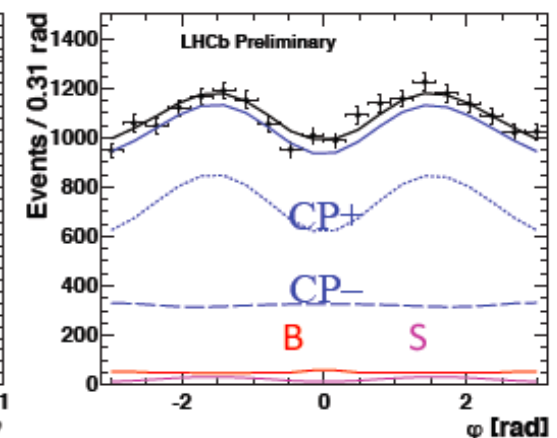
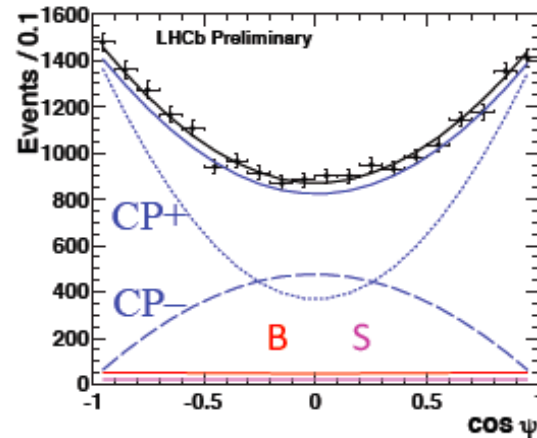
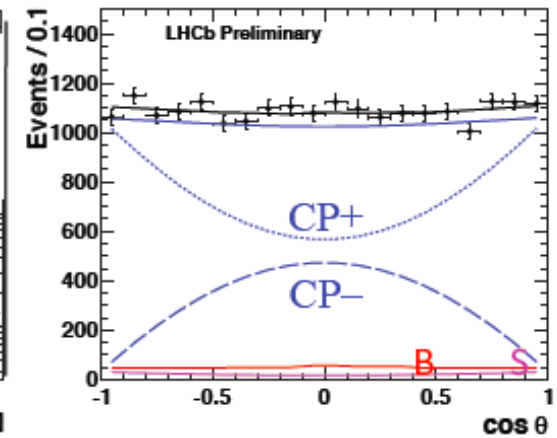
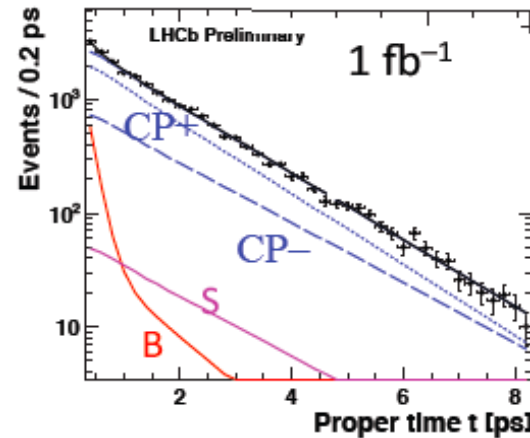
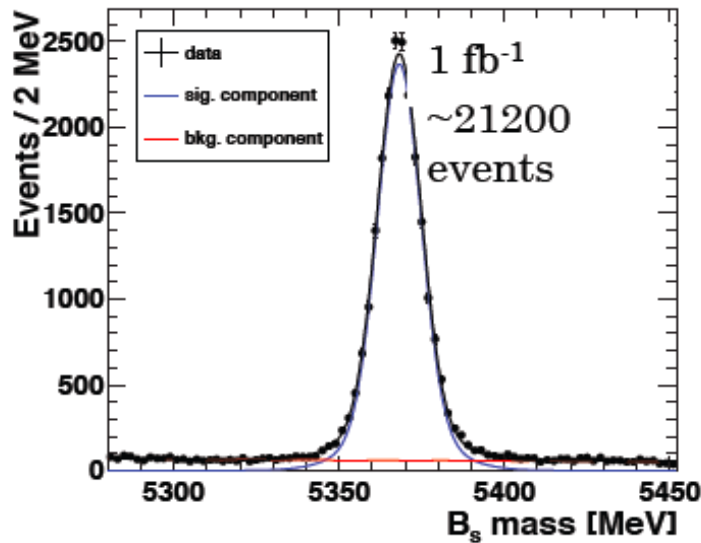


$B_s \rightarrow J/\psi\phi$: LHCb latest result [1 fb^{-1}]

Full fit of tagged and untagged rates as a function of B_s mass, proper time and transversity angles:

$B_s \rightarrow J/\psi KK$ final state is a mixture of CP-even and CP-odd eigenstates so angular analysis needed

LHCb-CONF-2012-002, $1/\text{fb}$



G. Lanfranchi, Blois 2012

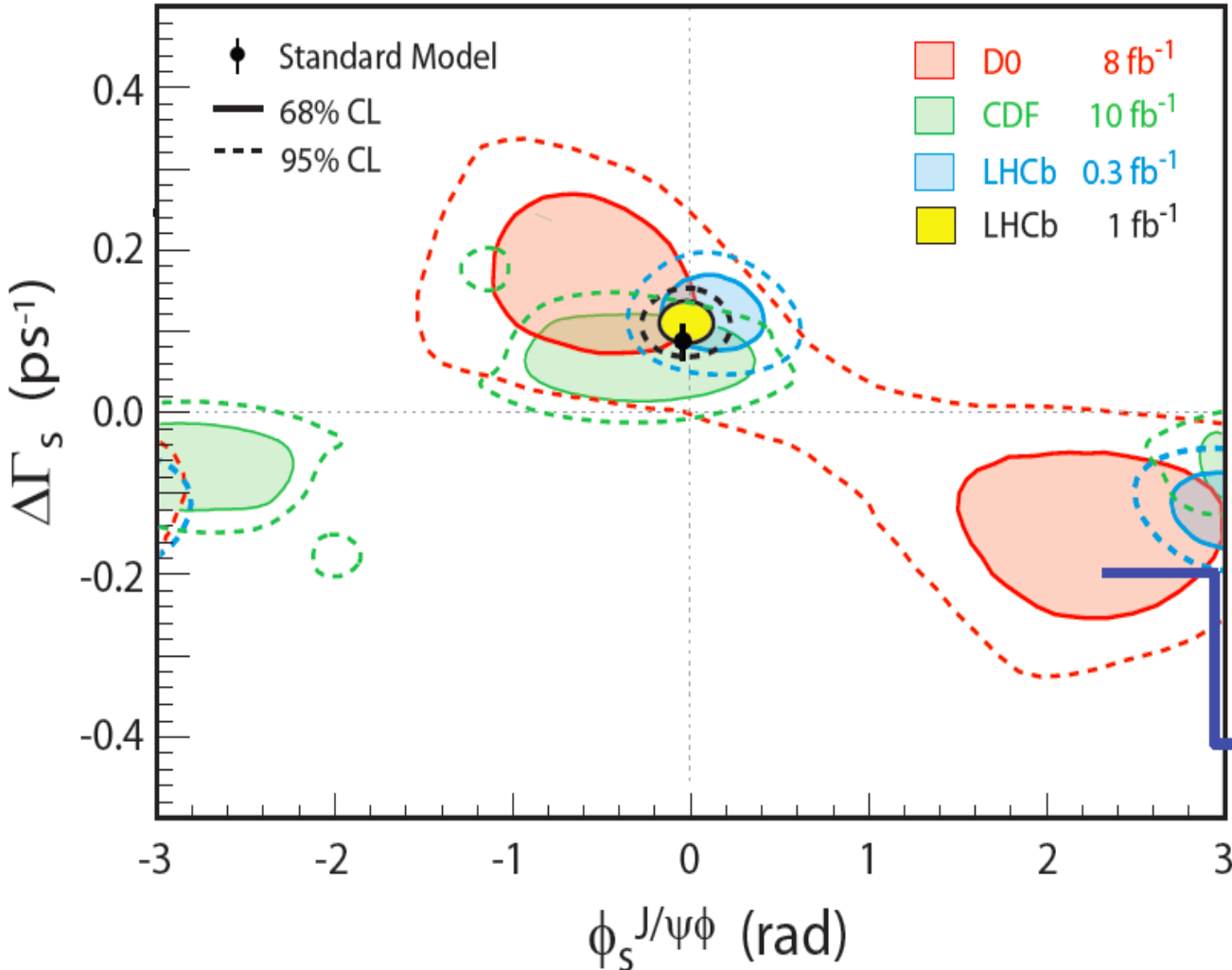
CP+ : $B_s \rightarrow J/\psi\phi$ signal with CP-even final state

S : $B_s \rightarrow J/\psi KK$ signal with $J_{KK}=0$ (S-wave, CP-odd)

CP- : $B_s \rightarrow J/\psi\phi$ signal with CP-odd final state

B : combinatorial background

So far there is an excellent agreement with the SM:

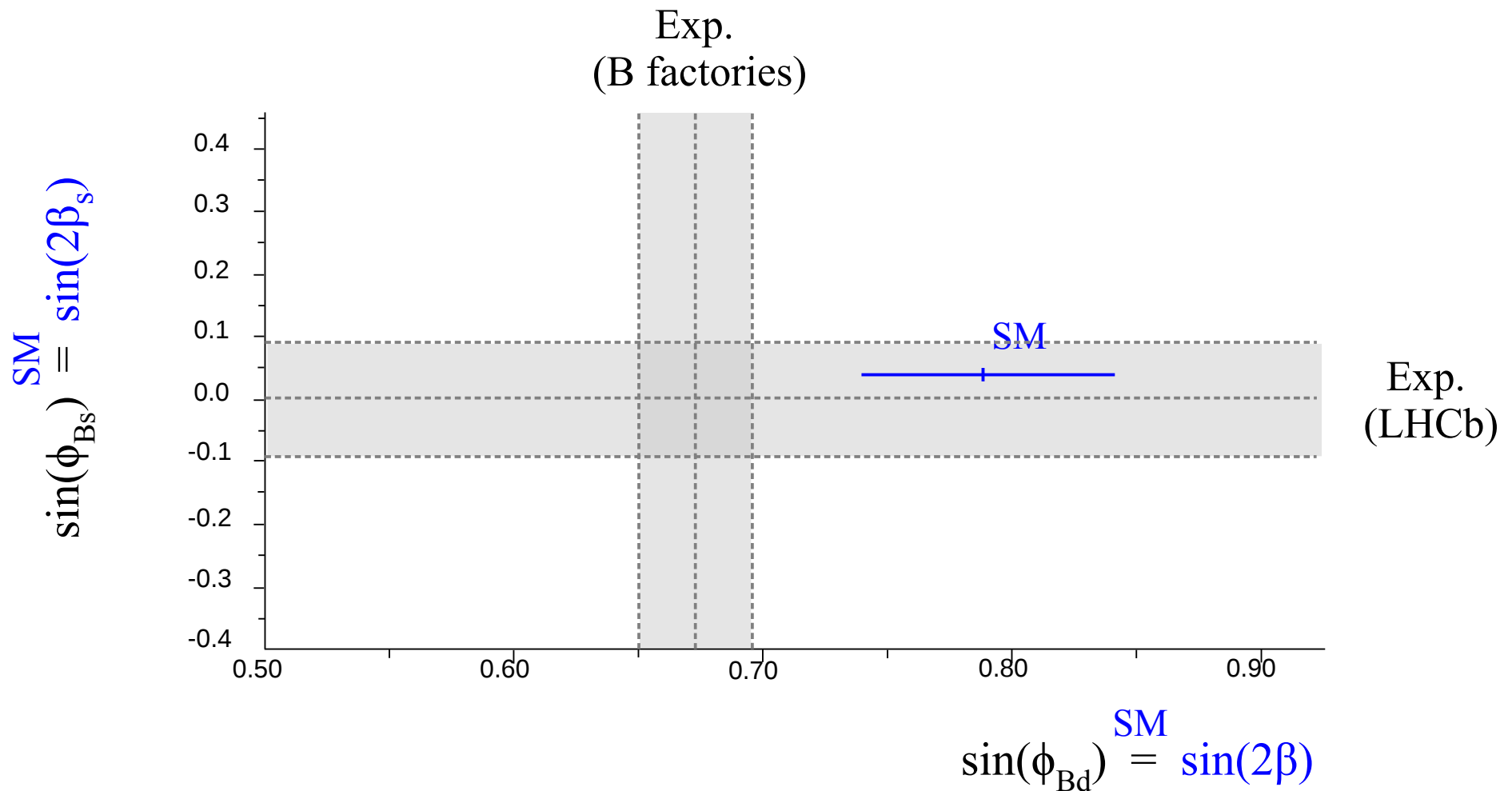


PRD 85 (2012) 032006
CDF note 10778
arXiv:1112.3183
LHCb-CONF-2012-002

Ambiguity removed by LHCb

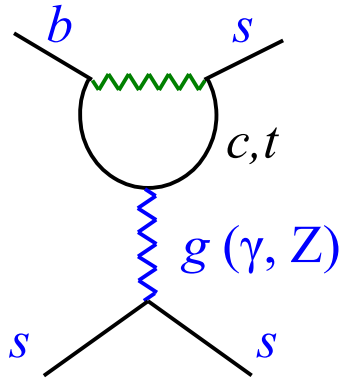
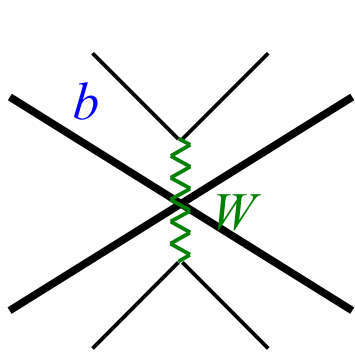
So far there is an excellent agreement with the SM.

But we cannot exclude surprises with more precise measurements, especially given the “tension” in the B_d case. *There is still a lot to learn...*

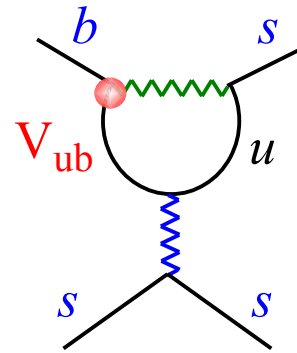


► Time-dependent studies in “penguin” modes

E.g.: $|B_d\rangle \rightarrow |\phi K\rangle$ [$b+d \rightarrow s\bar{s}s+s$]



real $O(\alpha_s \lambda^2)$
dominant



$O(\alpha_s \lambda^5)$
pollution < 10 %

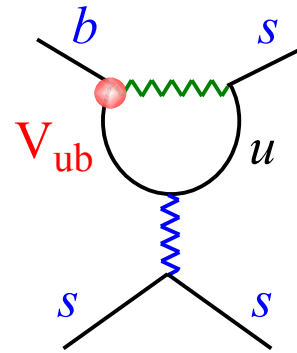
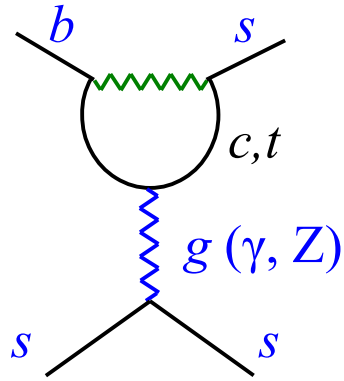
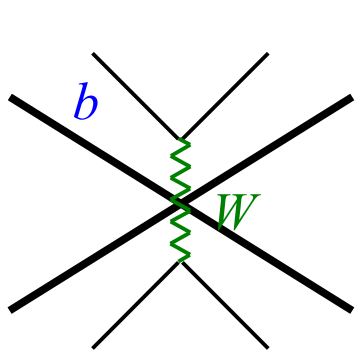
$$| \text{Im}(\lambda_{\psi K}) - \text{Im}(\lambda_{\phi K}) | < 0.1 \quad (\text{within SM})$$

These modes are not interesting for precise determinations of CKM elements, neither for very precise tests of the SM, but are potentially sensitive to NP:

$$| \text{Im}(\lambda_{\psi K}) - \text{Im}(\lambda_{\phi K}) | \gg 0.1 \quad \rightarrow \quad \text{New Physics !}$$

► Time-dependent studies in “penguin” modes

E.g.: $|B_d\rangle \rightarrow |\phi K\rangle$ [$b+d \rightarrow s\bar{s}s+s$]



real $O(\alpha_s \lambda^2)$
dominant

$O(\alpha_s \lambda^5)$
pollution < 10 %

$$| \text{Im}(\lambda_{\psi K}) - \text{Im}(\lambda_{\phi K}) | < 0.1 \quad (\text{within SM})$$

Unfortunately there are not many *pure penguin* channels of this type, moreover, even for pure penguin modes, it is very difficult to control the theory error below the $\sim 10\%$ level

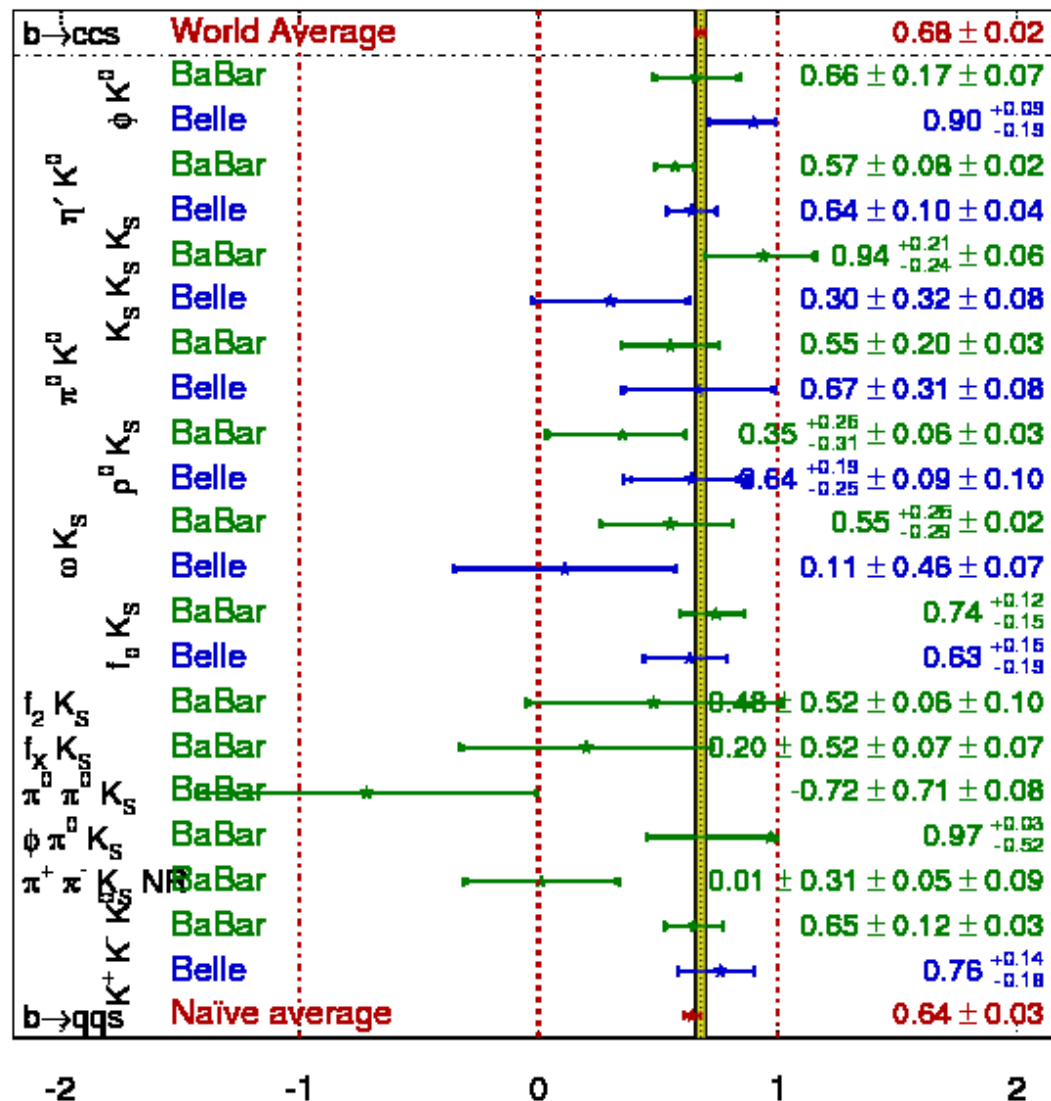
► Time-dependent studies in “penguin” modes

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

HFAG
Moriond 2012
PRELIMINARY

A few years ago there was a lot of (partly unjustified...), “excitement”. Right now:

- The most clean observables show no significant deviations.
- In most cases the exp. precision is already below the level of the irreducible th. errors.

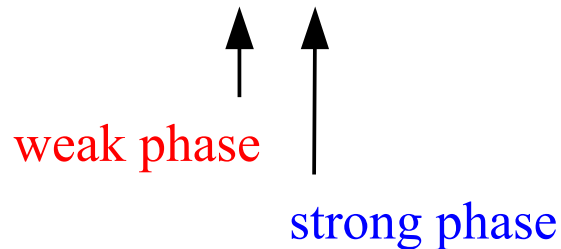


► CPV in charged B decays

CP violation in charged modes is usually easy from the experimental point of view, but it is hard to be predicted/interpreted from the theoretical point of view [no control on non-perturbative hadronic amplitudes]

$$\Gamma(B^+ \rightarrow f^+) = |A_1 + e^{i\gamma} e^{i\delta} A_2|^2$$

$$\Gamma(B^- \rightarrow f^-) = |A_1 + e^{-i\gamma} e^{i\delta} A_2|^2$$



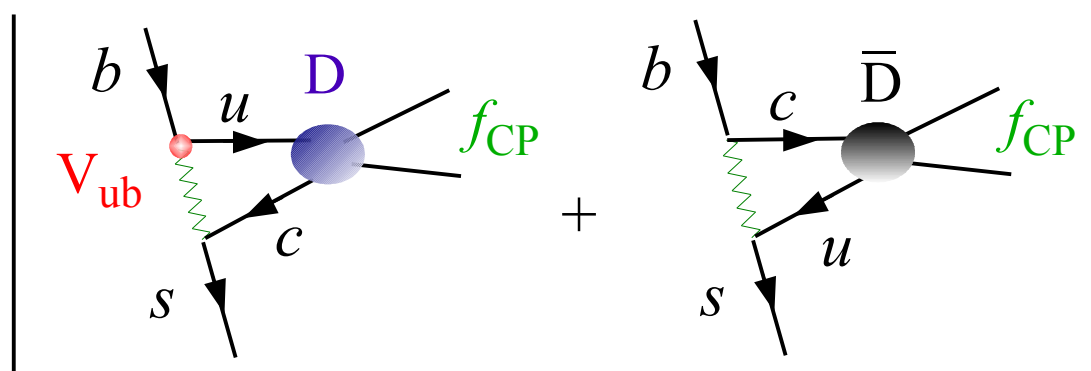
 ↑ ↑

 weak phase strong phase

► CPV in charged B decays

CP violation in charged modes is usually easy from the experimental point of view, but it is hard to be predicted/interpreted from the theoretical point of view [no control on non-perturbative hadronic amplitudes]

A notable exception are the $B^\pm \rightarrow D (\bar{D}) + K^\pm \rightarrow f_{\text{CP}} + K^\pm$ decays

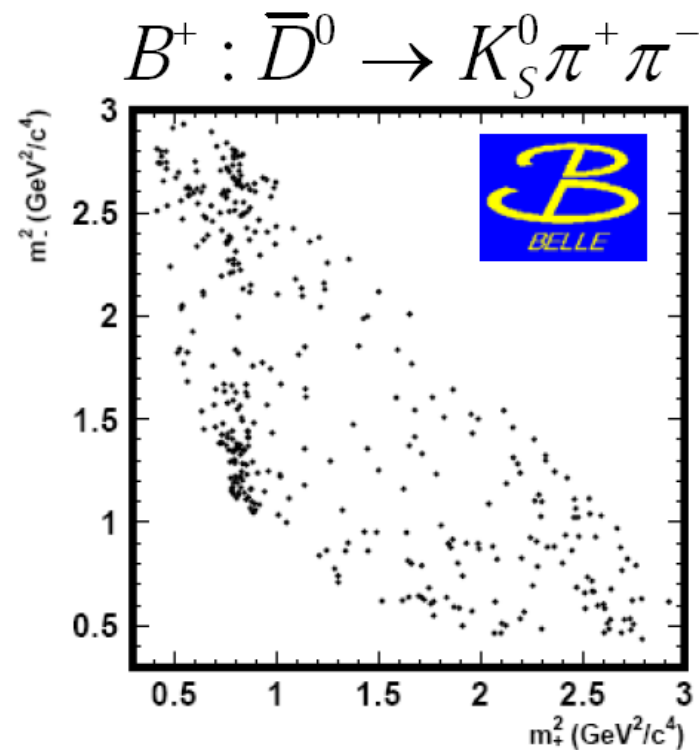
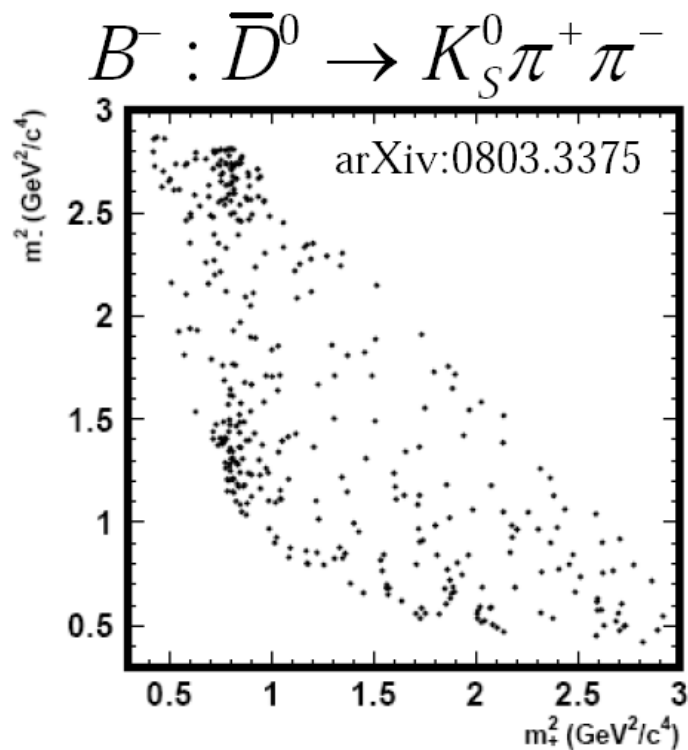


- Neutral D mixing weak phase measured to be small
- Relative weight and phase of the two strong amplitudes measured by looking at different CP eigenstates

Clean way to extract phase $\gamma = \arg(V_{ub})$:

- Gronau-London-Wyler/Atwood-Dunietz-Soni methods: $B^\pm \rightarrow (K\pi, \pi\pi) + K^\pm$
- Giri-Grossman-Soffer-Zupan method: $B^\pm \rightarrow (K_S \pi^+ \pi^-) + K^\pm$

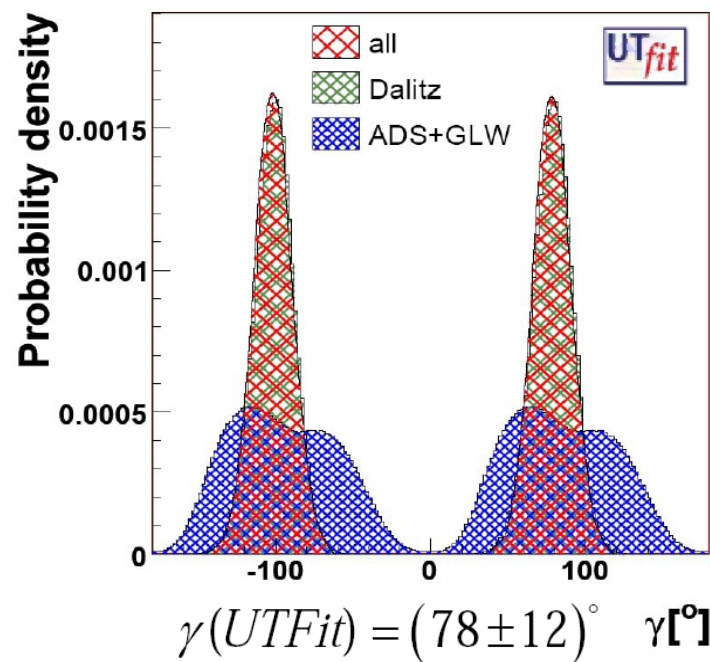
full Dalitz-Plot analysis



Method shown to work at B factories:
no theoretical limitations,
only statistically limited



Substantial room for improvements
at LHCb

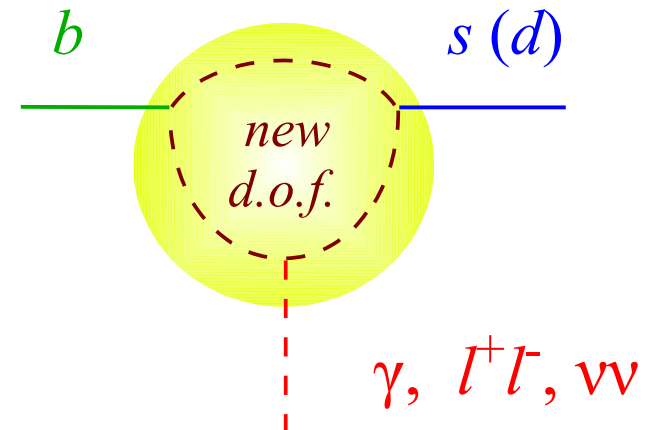


► Rare B decays

Similarly to $\Delta F=2$ mixings, rare decays mediated by *Flavour Changing Neutral Current* (FCNC) amplitudes are useful probes for *precision* tests of flavor dynamics beyond the SM



- No SM tree-level contribution
- Strong suppression within the SM because of CKM hierarchy
- Predicted with high precision within the SM at the partonic level: **NNLO** pert. calculations available for all the main B modes ($m_b \gg \Lambda_{\text{QCD}}$)



The $\Delta F=1$ sector is, in principle, much more reach:

FLAVOUR COUPLING:

ELECTROWEAK STRUCTURE

	$b \rightarrow s (\sim\lambda^2)$	$b \rightarrow d (\sim\lambda^3)$	$s \rightarrow d (\sim\lambda^5)$
$\Delta F=2$ box	$(Q_L^b \Gamma Q_L^s)^2$...	
$\Delta F=1$ 4-quark box	⋮		
gluon penguin			
γ penguin			
Z^0 penguin			
H^0 penguin			

The FCNC matrix:

each box correspond to an independent combination of dimension-6 $SU(3) \times SU(2) \times U(1)$ -invariant operators

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d \geq 5} \frac{c_n}{\Lambda^{d-4}} \mathcal{O}_n^d$$

...although not all observables
are theoretically very clean

FLAVOUR COUPLING:

ELECTROWEAK STRUCTURE

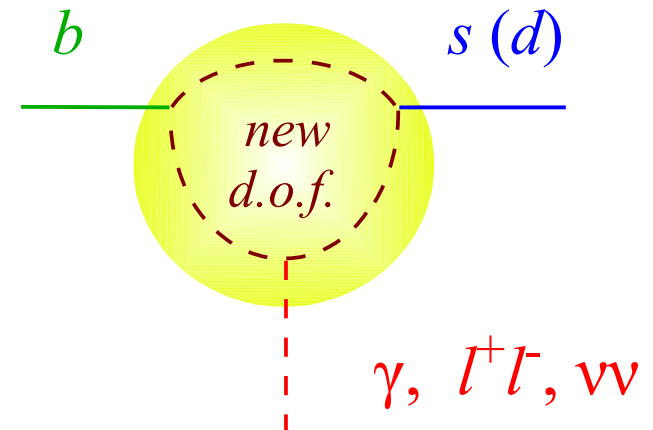
	$b \rightarrow s (\sim\lambda^2)$	$b \rightarrow d (\sim\lambda^3)$	$s \rightarrow d (\sim\lambda^5)$
$\Delta F=2$ box	ΔM_{B_s} $A_{CP}(B_s \rightarrow \psi\phi)$	ΔM_{B_d} $A_{CP}(B_d \rightarrow \psi K)$	$\Delta M_K, \epsilon_K$
$\Delta F=1$ 4-quark box	$B_d \rightarrow \phi K, B_d \rightarrow K\pi, \dots$	$B_d \rightarrow \pi\pi, B_d \rightarrow \rho\pi, \dots$	$\epsilon'/\epsilon, K \rightarrow 3\pi, \dots$
gluon penguin	$B_d \rightarrow X_s \gamma, B_d \rightarrow \phi K,$ $B_d \rightarrow K\pi, \dots$	$B_d \rightarrow X_d \gamma, B_d \rightarrow \pi\pi, \dots$	$\epsilon'/\epsilon, K_L \rightarrow \pi^0 l^+ l^-, \dots$
γ penguin	$B_d \rightarrow X_s l^+ l^-, B_d \rightarrow X_s \gamma$ $B_d \rightarrow \phi K, B_d \rightarrow K\pi, \dots$	$B_d \rightarrow X_d l^+ l^-, B_d \rightarrow X_d \gamma$ $B_d \rightarrow \pi\pi, \dots$	$\epsilon'/\epsilon, K_L \rightarrow \pi^0 l^+ l^-, \dots$
Z^0 penguin	$B_d \rightarrow X_s l^+ l^-, B_s \rightarrow \mu\mu$ $B_d \rightarrow \phi K, B_d \rightarrow K\pi, \dots$	$B_d \rightarrow X_d l^+ l^-, B_d \rightarrow \mu\mu$ $B_d \rightarrow \pi\pi, \dots$	$\epsilon'/\epsilon, K_L \rightarrow \pi^0 l^+ l^-,$ $K \rightarrow \pi\nu\nu, K \rightarrow \mu\mu, \dots$
H^0 penguin	$B_s \rightarrow \mu\mu$	$B_d \rightarrow \mu\mu$	$K_{L,S} \rightarrow \mu\mu$

► Rare B decays

Similarly to $\Delta F=2$ mixings, rare decays mediated by *Flavour Changing Neutral Current* (FCNC) amplitudes are useful probes for *precision* tests of flavor dynamics beyond the SM



- No SM tree-level contribution
- Strong suppression within the SM because of CKM hierarchy
- Predicted with high precision within the SM at the partonic level: **NNLO** pert. calculations available for all the main B modes ($m_b \gg \Lambda_{\text{QCD}}$)
- The key point is the relation between partonic & hadronic worlds



Fully inclusive decays
usually good precision thanks
to heavy-quark symmetry

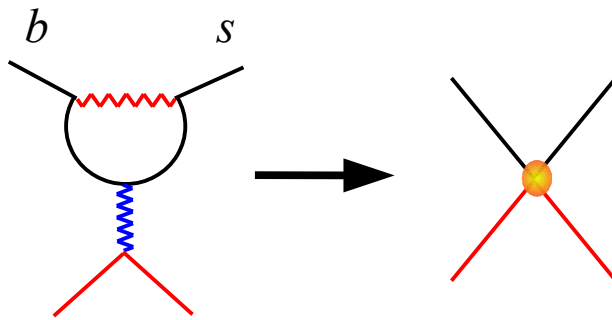
$$\Gamma(b \rightarrow s\gamma) \xrightarrow{m_b \rightarrow \infty} \Gamma(B \rightarrow X_s \gamma)$$

Exclusive decays
generally more difficult than inclusive,
with some notable exceptions:

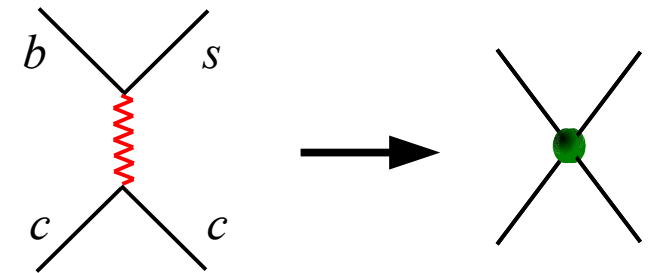
$$B \rightarrow (0, K, K^*) + \mu^-\mu^+$$

Three-step procedure to deal with the various scales of the problem:

1st step: Construction of a local eff. Hamiltonian at the electroweak scale integrating out all the heavy fields around m_W (including the heavy SM fields)



$$H_{\text{eff}} = \sum_i C_i(M_W) Q_i$$



FCNC operators:

$$Q_6 = (bs)_{V-A} (qq)_V \quad [\text{Gluon penguins}]$$

$$\vdots$$

$$Q_{9V} = Q_f (bs)_{V-A} (ff)_V \quad [\text{E.W. penguins}]$$

$$Q_{10A} = Q_f (bs)_{V-A} (ff)_A$$

Four-quark (tree-level) ops.:

$$Q_1 = (bs)_{V-A} (cc)_{V-A}$$

$$Q_2 = (bc)_{V-A} (cs)_{V-A}$$

$$\vdots$$

The interesting short-distance info is encoded in the $C_i(M_W)$ (*initial conditions*) of the Wilson coefficients of the FCNC operators

2nd step: Evolution of H_{eff} down to low scales using RGE

Penguin operators:

$$Q_6 = (bs)_{V-A}(qq)_V$$

$$\vdots$$

$$Q_{9V} = Q_f (bs)_{V-A}(ff)_V$$

$$Q_{10A} = Q_f (bs)_{V-A}(ff)_A$$

$$H_{\text{eff}} = \sum_i C_i(M_W) Q_i$$



$$H_{\text{eff}} = \sum_i C_i(\mu \sim m_b) Q_i$$

Four-quark (tree-level) ops.:

$$Q_1 = (bs)_{V-A}(cc)_{V-A}$$

$$Q_2 = (bc)_{V-A}(cs)_{V-A}$$

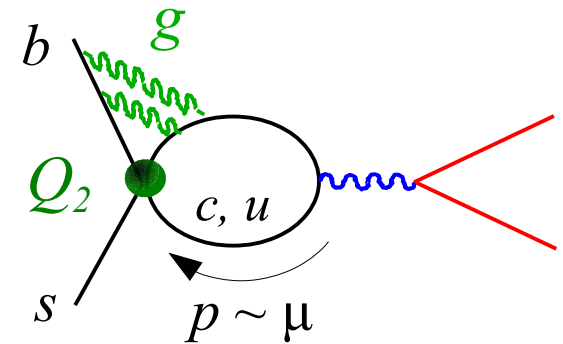
$$\vdots$$

Sources of long-distance effects:

[dilution of the interesting short-distance info]:

- Mixing of the **four-quark** Q_i into the **FCNC** Q_i
[perturbative long-distance contribution]

e.g.:



- Small in the case of electroweak penguins (Q_{10A}) because of the power-like GIM mechanism [mixing parametrically suppressed by $O(m_c^2/m_t^2)$]
- Large for gluon penguins

3rd step: Evaluation of the hadronic matrix elements

$$A(B \rightarrow f) = \sum_i C_i(\mu) \langle f | Q_i | B \rangle (\mu) \quad [\mu \sim m_b]$$

- sensitivity to long-distances (*cc* threshold, m_c dependence,...)
- distinction between inclusive (OPE + $1/m_{b,c}$ expansion) and exclusive modes (hadronic form factors)
- irreducible large theory errors in the case of exclusive non-leptonic final states

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Putting all the ingredients together in the case of $B \rightarrow X_s \gamma$

[best inclusive mode so far]:

NNLO SM th. estimate:

$$B(B \rightarrow X_s \gamma) = (3.15 \pm 0.23) \times 10^{-4}$$

[Misiak *et al.* '07]

To be compared with:

$$B(B \rightarrow X_s \gamma) = (3.57 \pm 0.24) \times 10^{-4}$$

[present exp. W.A.]

A great success for the SM...

...and a great challenge for many of its extensions !

► Exclusive rare B decays

The accuracy on *exclusive* FCNC B decays of the type $B \rightarrow H+(\gamma, l^+l^-)$ depends on the th. control of $B \rightarrow H$ *hadronic form factors* :

$$A(B \rightarrow f) = \sum_i C_i(\mu) \langle f | Q_i | B \rangle(\mu) \quad \mu \sim m_b$$

- Several progress in the last few years [[Light-cone sum rules](#), [Heavy-quark expansion](#), [Lattice](#)] but typical errors still $\sim 30\%$

The most difficult exclusive observables are the total branching ratios however, *f.f.* uncertainties can be considerably reduced in appropriate ratios or differential distributions, or considering very peculiar final states.

- Notable examples:

I. $B(B_{s,d} \rightarrow \mu^+\mu^-)$

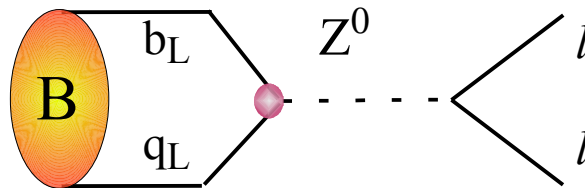
II. Differential distributions in $B \rightarrow K^* \mu^+\mu^-$

$$B_{s,d} \rightarrow \mu^+ \mu^-$$

A special case among exclusive B decays:

- No vector-current contribution [th. error of the short-distance calculation $\sim 1\%$]
- Hadronic matrix element relatively simple [f_B within the SM]

$$\langle 0 | \bar{b} \gamma_\mu \gamma_5 u | B(p) \rangle = i f_B p_\mu$$



$$B_{s,d} \rightarrow \mu^+ \mu^-$$

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$$\langle 0 | \bar{b} \gamma_\mu \gamma_5 u | B(p) \rangle = i f_B p_\mu$$

- Very clean signature
- Strong sensitivity to scalar currents beyond the SM [*Higgs penguin*]

Sizable deviations possible in multi-Higgs models,
even without new flavor structures [**SUSY @ large $\tan\beta$**]

SM expectations:

$$B(B_s \rightarrow \mu\mu)_{\text{SM}} = 3.2(2) \times 10^{-9}$$

$$B(B_s \rightarrow \mu\mu)_{\text{SM}} = 1.0(1) \times 10^{-10}$$

□
 e channels suppressed by $(m_e/m_\mu)^2$

τ channels enhanced by $(m_\tau/m_\mu)^2$

$$B_{s,d} \rightarrow \mu^+ \mu^-$$

A special case among exclusive B decays:

- No vector-current contribution [th. error of the short-distance calculation $\sim 1\%$]
- Hadronic matrix element relatively simple [f_B within the SM]

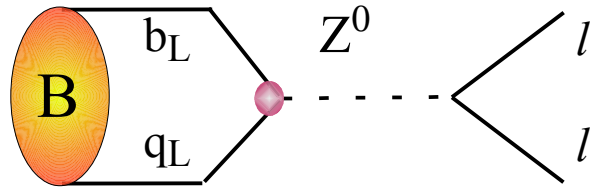
$$\langle 0 | \bar{b} \gamma_\mu \gamma_5 u | B(p) \rangle = i f_B p_\mu$$

- Very clean signature
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Exercise [to understand why $B_{s,d} \rightarrow ll$ is interesting]:

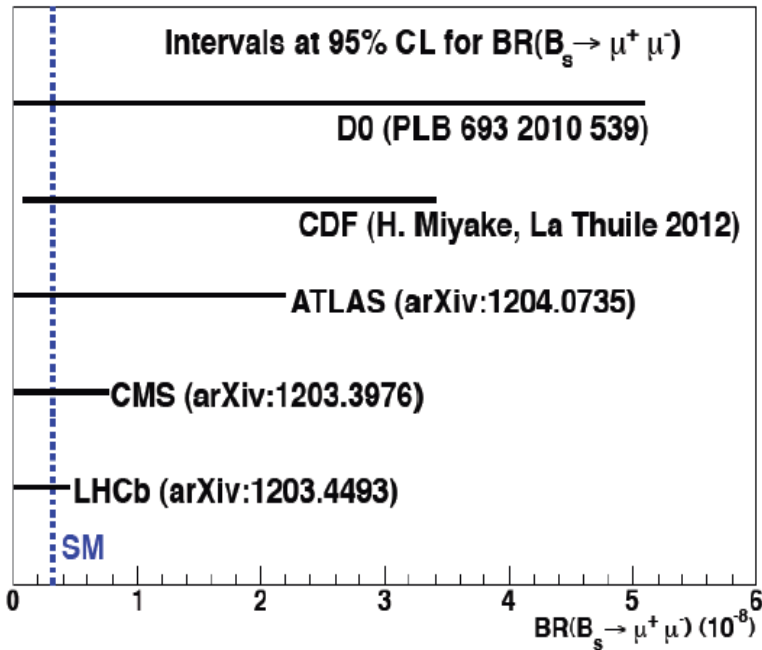
- Compute $B_u \rightarrow l\nu$ at the tree-level and compare it with the result obtained in the *gauge-less* limit
- Help: $\langle 0 | \bar{b} \gamma_\mu \gamma_5 u | B(p) \rangle = i f_B m_B^2 / m_b$ & neglect m_B / M_W

$$B_{s,d} \rightarrow \mu^+ \mu^-$$



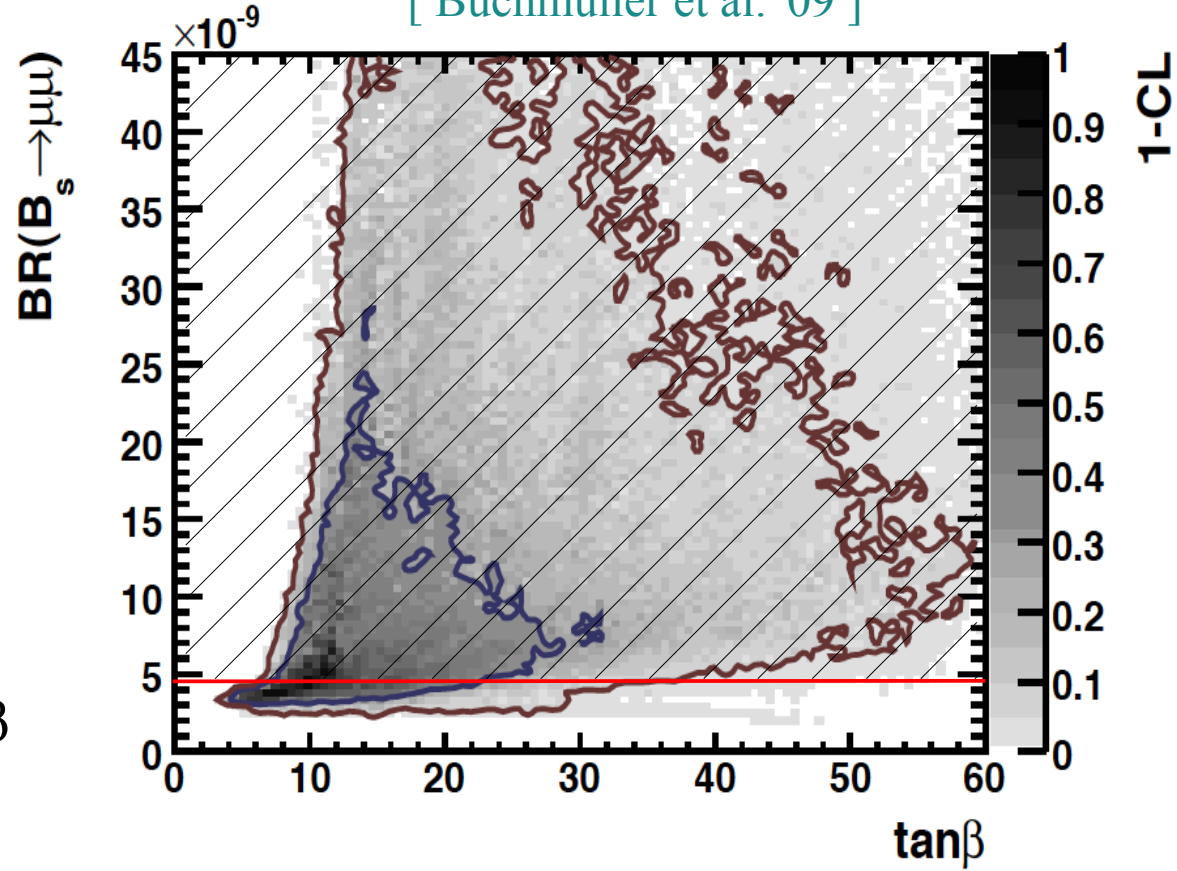
The amplitude is dominated by the **longitudinal component of the Z** (or the contribution of the Goldstone bosons) → particularly sensitive to possible modifications of the Higgs sector.

The recent exp. bounds:



Have strongly restricted the large $\tan\beta$ scenario of minimal SUSY models

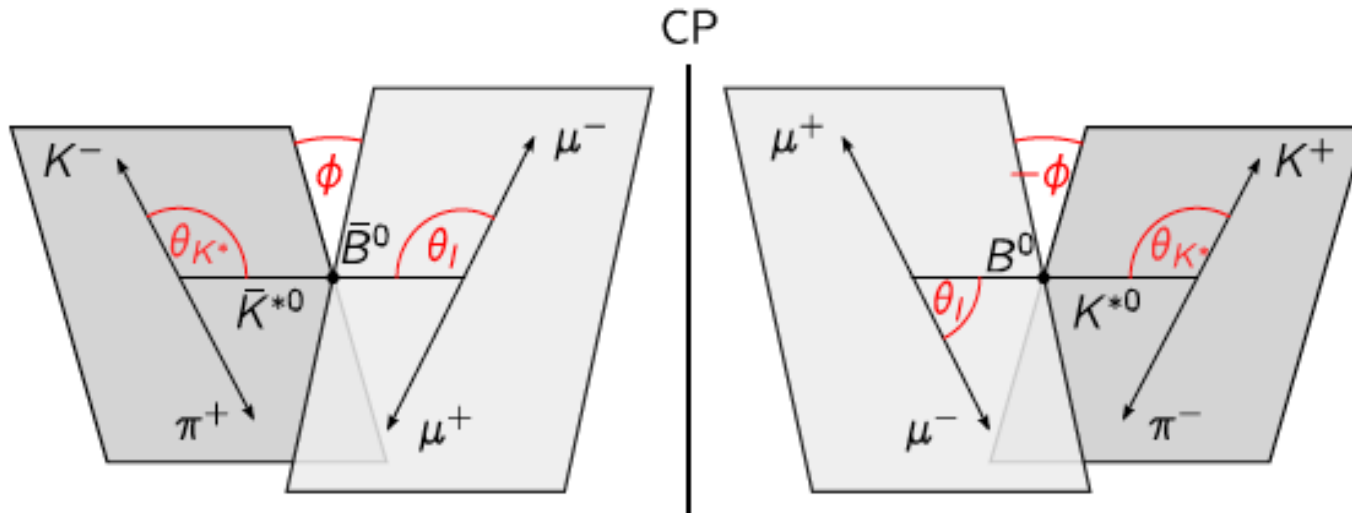
E.g.: MSSM with NUHM
[Buchmuller et al. '09]



Differential distributions in $B \rightarrow K^* \mu^+ \mu^-$

$$B^0 \rightarrow K^{0*} (\rightarrow K^+ \pi^-) \mu^+ \mu^-$$

$$\bar{B}^0 \rightarrow \bar{K}^{0*} (\rightarrow K^- \pi^+) \mu^+ \mu^-$$



$$\frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_K d\phi} = \frac{9}{32\pi} J(q^2, \theta_l, \theta_K, \phi)$$

$$\begin{aligned} & J_{1s} \sin^2 \theta_K + J_{1c} \cos^2 \theta_K + (J_{2s} \sin^2 \theta_K + J_{2c} \cos^2 \theta_K) \cos 2\theta_l + J_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \\ & + J_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + J_5 \sin 2\theta_K \sin \theta_l \cos \phi + (J_{6s} \sin^2 \theta_K + J_{6c} \cos^2 \theta_K) \cos \theta_l \\ & + J_7 \sin 2\theta_K \sin \theta_l \sin \phi + J_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + J_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \end{aligned}$$

- The angular distribution give access to several observables (12 indep. terms !)
- Self-tagging mode: easy to measure CP asymmetries

E.g.: The FB asymmetry

$$A_{FB} = \int \frac{d^2 B(B \rightarrow K^* \mu^+ \mu^-)}{ds d \cos \theta} \text{sgn}(\cos \theta) \propto \Re \left\{ C_{10}^* [s C_9 + r(s) C_7] \right\}$$

θ = angle between μ^+ & B momenta
in the dilepton rest frame

th. error $\sim 5\%$

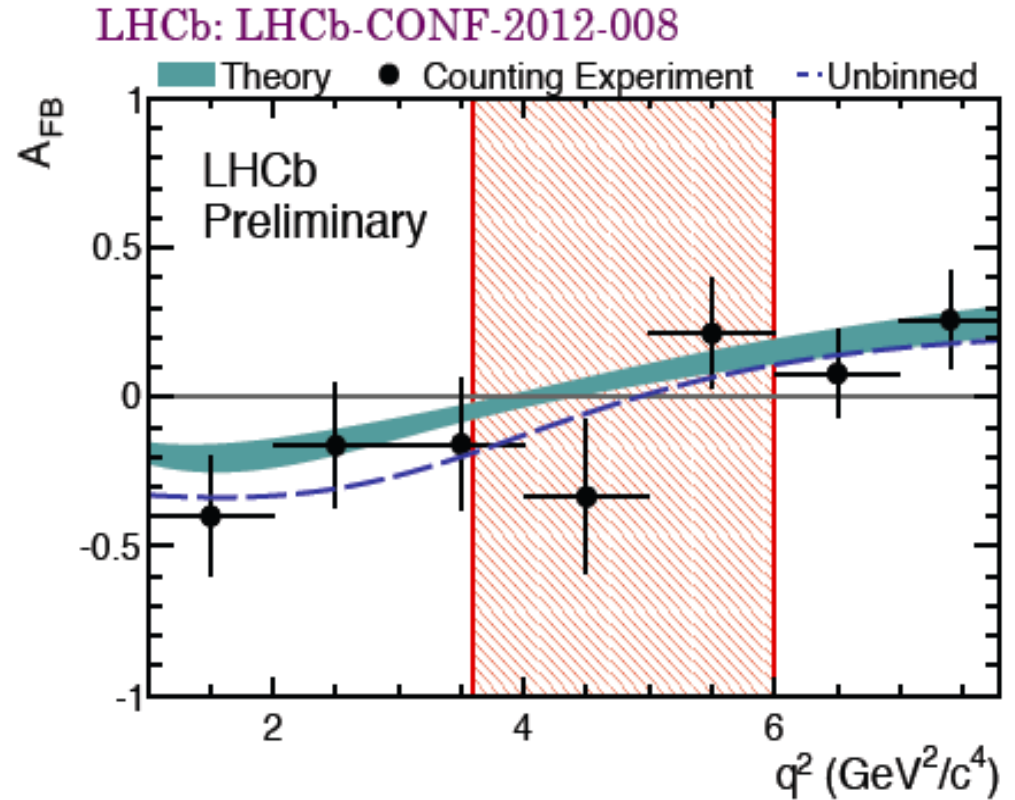
- Direct access to the *relative phases* of the C_i
- Proportional to C_{10} (\rightarrow interference of axial & vector currents \rightarrow small QCD corrections)
- Particularly clean prediction: $A_{FB}(s) = 0$ for $s = q^2/m_b^2 \sim C_7/C_9$
- Hadronic uncertainties substantially decreased with a proper normalization.

E.g.: The FB asymmetry

The clean prediction:

$$A_{FB}(s) = 0 \quad \text{for} \quad s = q^2/m_b^2 \sim C_7/C_9$$

Has recently been tested with good precision by LHCb, but there are many more observables that could be studied in this mode.



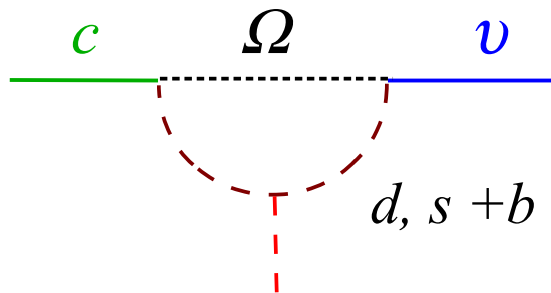
► CP violation in the charm system

The physics of charm mixing and charm decays ($c \rightarrow u$ transitions) is quite different with respect to the $B_{s,d}$ ($b \rightarrow s,d$) and K ($s \rightarrow d$) systems.

No top-enhancement of FCNC amplitudes (both $\Delta F=2$ & $\Delta F=1$):

$$V_{CKM} = \begin{array}{c} \left[\begin{array}{cc|c} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ \hline V_{td} & V_{ts} & V_{tb} \end{array} \right] \end{array}$$

- ♦ In all **CP-conserving** amplitudes we can safely approximate the CKM matrix to a 2x2 real mixing matrix, and **long-distance contributions are largely dominant**



- **CP-violating** amplitudes are not calculable with high-accuracy within the SM, but are expected to be very small because of the CKM hierarchy \Rightarrow possible interesting **null-tests of the SM**

► CP violation in the charm system

The *news of the year* in flavour physics is the evidence of CP violation in two-body Cabibbo-suppressed charm decays $D \rightarrow KK, \pi\pi$ ($c \rightarrow u+ss, dd$) observed by LHCb & CDF:

$$\Delta a_{\text{CP}} = a_{\text{CP}}(K^+K^-) - a_{\text{CP}}(\pi^+\pi^-) = (0.67 \pm 0.16)\%$$

- Unambiguous evidence of direct CP violation:

$$a_{\text{CP}}^{(\text{dir})} = \frac{\Gamma(D \rightarrow PP) - \Gamma(\bar{D} \rightarrow PP)}{\Gamma(D \rightarrow PP) + \Gamma(\bar{D} \rightarrow PP)}$$

- Totally unexpected, at least according to all the pre-LHCb predictions of the last 20 years: direct CPV in charm above 0.1% quoted as “clear signal of physics beyond the SM”...

► The puzzle of Δa_{CP}

Let's consider the relevant SM effective Hamiltonian ($|\Delta c|=1, |\Delta s|=0$) renormalized at a scale $m_c < \mu < m_b$

$$\mathcal{H}_{|\Delta c|=1}^{\text{eff}} = \lambda_d \mathcal{H}_{|\Delta c|=1}^{(d)} + \lambda_s \mathcal{H}_{|\Delta c|=1}^{(s)} + \lambda_b \mathcal{H}_{|\Delta c|=1}^{\text{peng}}$$

$$\mathcal{H}_{|\Delta c|=1}^q = \frac{G_F}{\sqrt{2}} \sum_{i=1,2} C_i^q Q_i^s + \text{H.c.},$$

$$Q_1^q = (\bar{u}q)_{V-A} (\bar{q}c)_{V-A}$$

$$Q_2^q = (\bar{u}_\alpha q_\beta)_{V-A} (\bar{q}_\beta c_\alpha)_{V-A}$$

Standard basis of QCD penguin operators

Tiny coefficients for μ in the perturbative regime: $C_i \sim \alpha_s(\mu)/\pi$

O(1) Wilson coeff.

$$\lambda_q = V_{cq}^* V_{uq} = \begin{cases} +\lambda + \dots & (q=d) \\ -\lambda + \dots & (q=s) \\ A^2 \lambda^5 e^{-i\gamma} & (q=b) \end{cases} \quad \lambda_d + \lambda_s + \lambda_b = 0$$

► The puzzle of Δa_{CP}

To a good approximation, for sufficiently heavy μ :

$$\mathcal{H}_{|\Delta c|=1}^{\text{eff}} \approx \lambda_d \mathcal{H}_{|\Delta c|=1}^{(d)} + \lambda_s \mathcal{H}_{|\Delta c|=1}^{(s)}$$

► The puzzle of Δa_{CP}

To a good approximation, for sufficiently heavy μ :

$$\mathcal{H}_{|\Delta c|=1}^{\text{eff}} \approx \lambda_d \mathcal{H}_{|\Delta c|=1}^d + \lambda_s \mathcal{H}_{|\Delta c|=1}^s$$

$$= + \lambda_d (\mathcal{H}_{|\Delta c|=1}^d - \mathcal{H}_{|\Delta c|=1}^s) - \lambda_b \mathcal{H}_{|\Delta c|=1}^s$$

$$= - \lambda_s (\mathcal{H}_{|\Delta c|=1}^d - \mathcal{H}_{|\Delta c|=1}^s) - \lambda_b \mathcal{H}_{|\Delta c|=1}^d$$

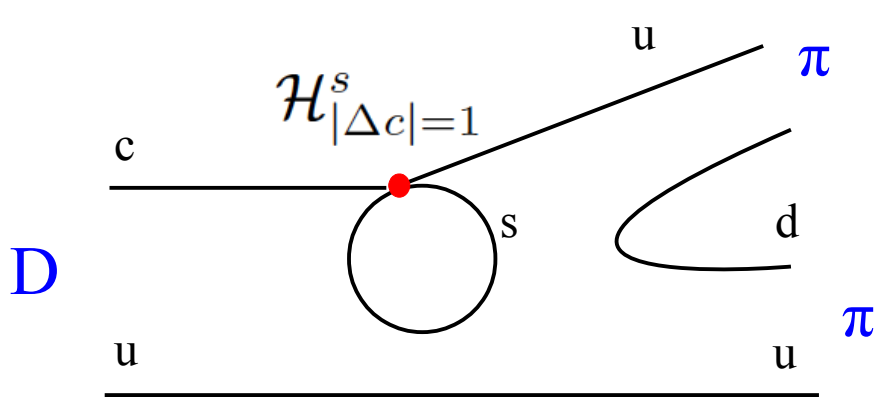
- Cabibbo-leading structure
- Tree-level amplitude in both K^+K^- and $\pi^+\pi^-$
- No penguin contractions in the SU(3) limit

- CKM-suppressed
- No tree-level in K^+K^- or $\pi^+\pi^-$
- Penguin contractions allowed

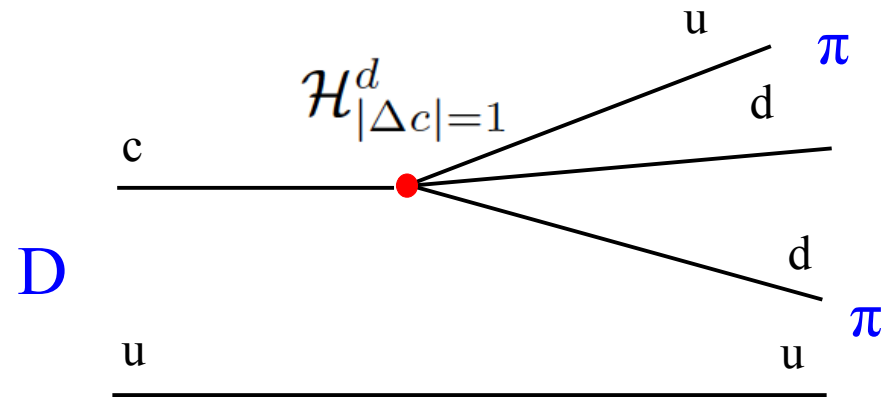
► The puzzle of Δa_{CP}

To a good approximation, for sufficiently heavy μ :

$$\begin{aligned} \mathcal{H}_{|\Delta c|=1}^{\text{eff}} &\approx \lambda_d \mathcal{H}_{|\Delta c|=1}^{(d)} + \lambda_s \mathcal{H}_{|\Delta c|=1}^{(s)} \\ &= +\lambda_d (\mathcal{H}_{|\Delta c|=1}^d - \mathcal{H}_{|\Delta c|=1}^s) - \lambda_b \mathcal{H}_{|\Delta c|=1}^s \\ &= -\lambda_s (\mathcal{H}_{|\Delta c|=1}^d - \mathcal{H}_{|\Delta c|=1}^s) - \lambda_b \mathcal{H}_{|\Delta c|=1}^d \end{aligned}$$



“Penguin contractions”



“Tree-level topologies”

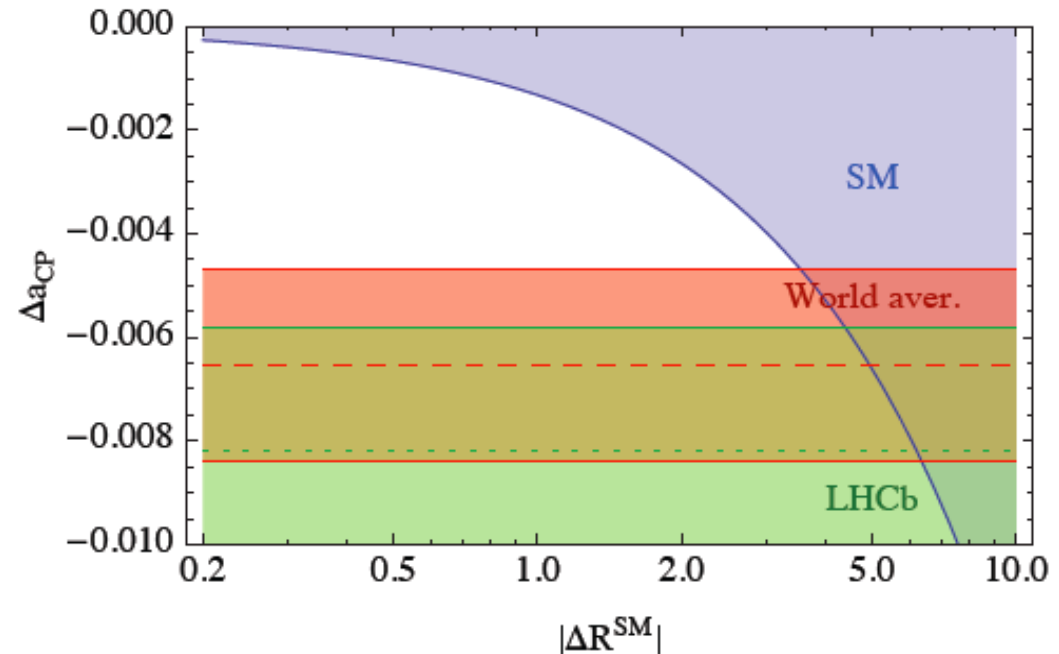
► The puzzle of Δa_{CP}

The observed Δa_{CP} is large compared to its “natural” SM expectation, but is not large enough, compared to SM uncertainties, to be considered a clear signal of NP:

$$\Delta a_{\text{CP}} \approx (0.13\%) \text{Im}(\Delta R^{\text{SM}})$$

CKM suppression: $\arg\left(\frac{V_{cs}^* V_{us}}{V_{cd}^* V_{ud}}\right) = \mathcal{O}(\lambda^4)$

matrix-element ratio:
 “penguin”
 “tree”



$\Delta R > 1$ is not what we expect for $m_c \gg \Lambda_{\text{QCD}}$, but is not impossible treating the charm as a light quark (*possible connection with the $\Delta I=1/2$ rule in Kaons*)

More works (and especially more observables) needed in order to clarify the situation.