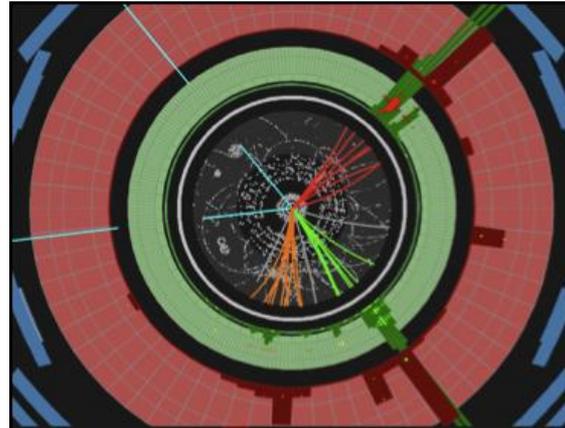


# QCD at Colliders

## Lecture 2

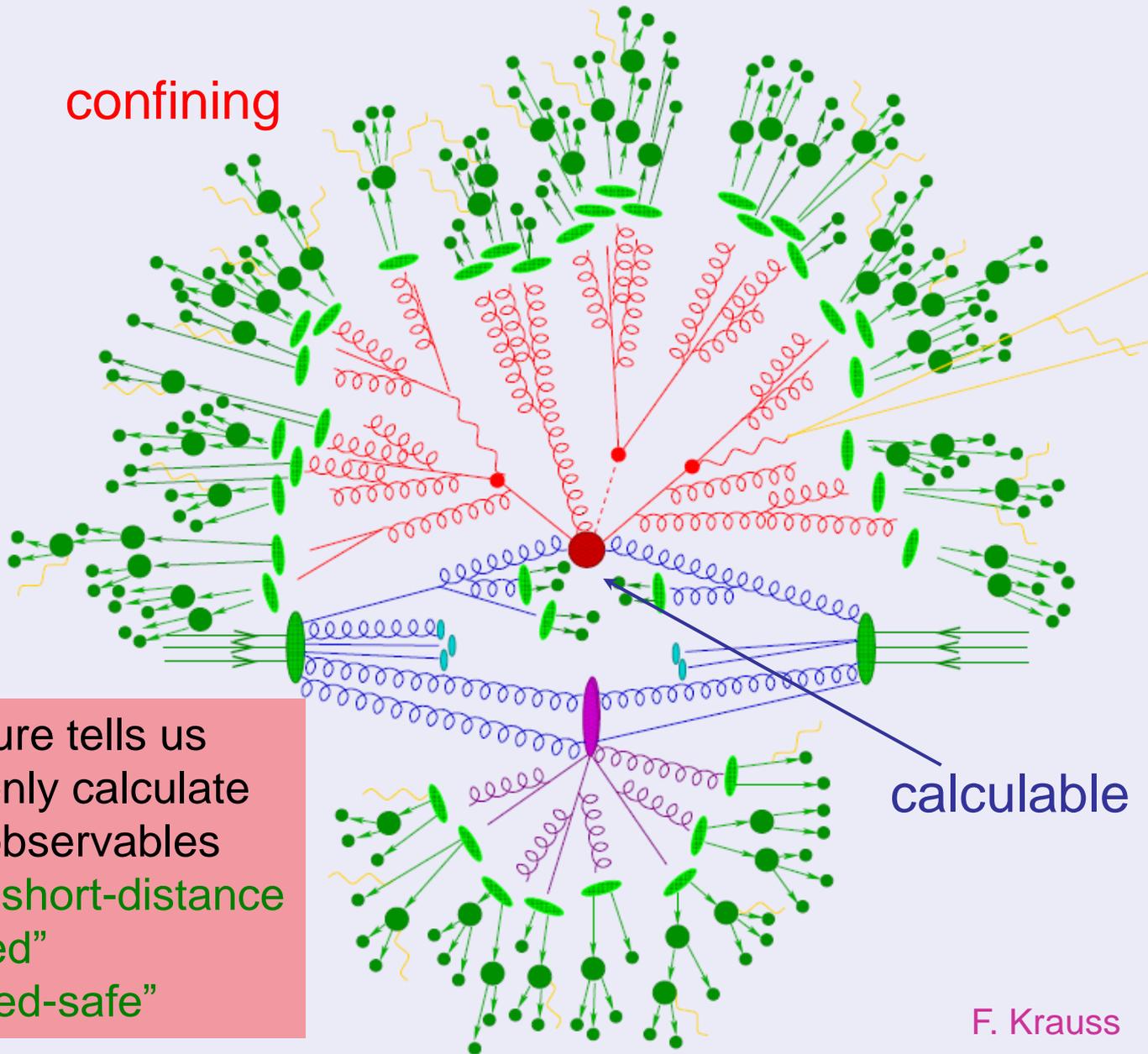
### Jets and parton showers



Lance Dixon

2012 European School  
of High Energy Physics

confining

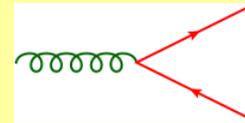


This picture tells us we can only calculate reliably observables that are “short-distance dominated” or “infrared-safe”

F. Krauss

# Two ways to be IR unsafe

1) Ask a question which is sensitive to **collinear splitting**, such as “how many quarks are there in the event?”



2) Ask a question which is sensitive to **soft gluon** radiation, such as “what is the probability of no hadrons in this region of the detector?”

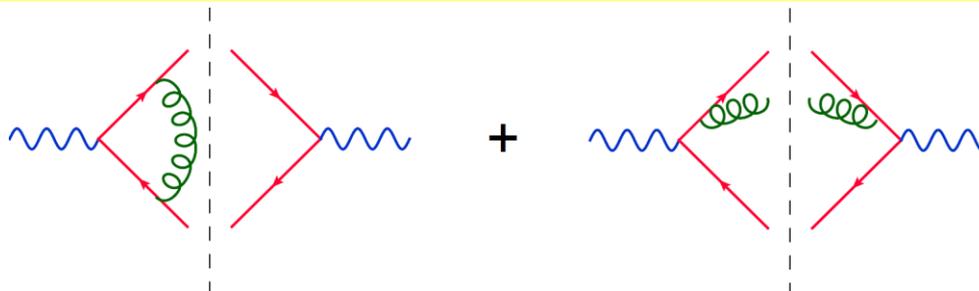
- Of course we could just look at the leptonic decay products of  $W$ 's,  $Z$ 's and Higgs bosons, but that would be rather restrictive
- **Jets** are a way to study hadronic energy flow, in a way that correlates pretty well with “the underlying partons”, and yet is **infrared safe** (for modern jet algorithms).

# Technical definition of infrared safety

**Infrared-safe** observables  $\mathcal{O}$  are defined for an arbitrary number of partons (or hadrons)  $n$ , and satisfy:

$$\begin{aligned} \mathcal{O}_{n+1}(\dots, k_s, \dots) &\rightarrow \mathcal{O}_n(\dots, \cancel{k_s}, \dots) & k_s \rightarrow 0 \\ \mathcal{O}_{n+1}(\dots, k_a, k_b, \dots) &\rightarrow \mathcal{O}_n(\dots, k_P, \dots) & k_a \parallel k_b \end{aligned}$$

- Physically, insensitive to soft gluon emission and general collinear splitting.
- In perturbative QCD, virtual corrections with  $n$  partons cancel singularities from real emission with  $n+1$  partons.



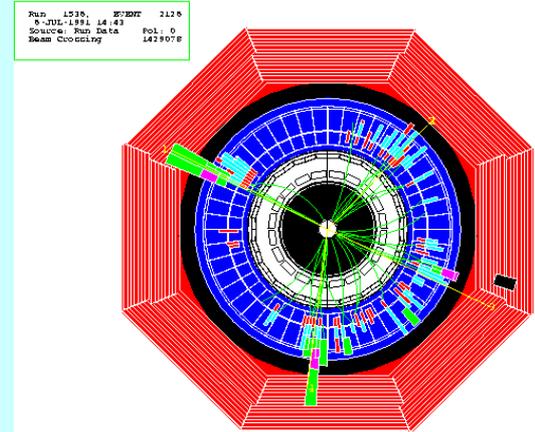
# Jets in $e^+e^-$ annihilation

Given a set of  $n$  particles  $\{i\}$  (or clusters of energy in a calorimeter) define a “distance” measure  $d_{ij}$ , which vanishes when  $i \parallel j$  or  $i$  or  $j$  becomes soft.

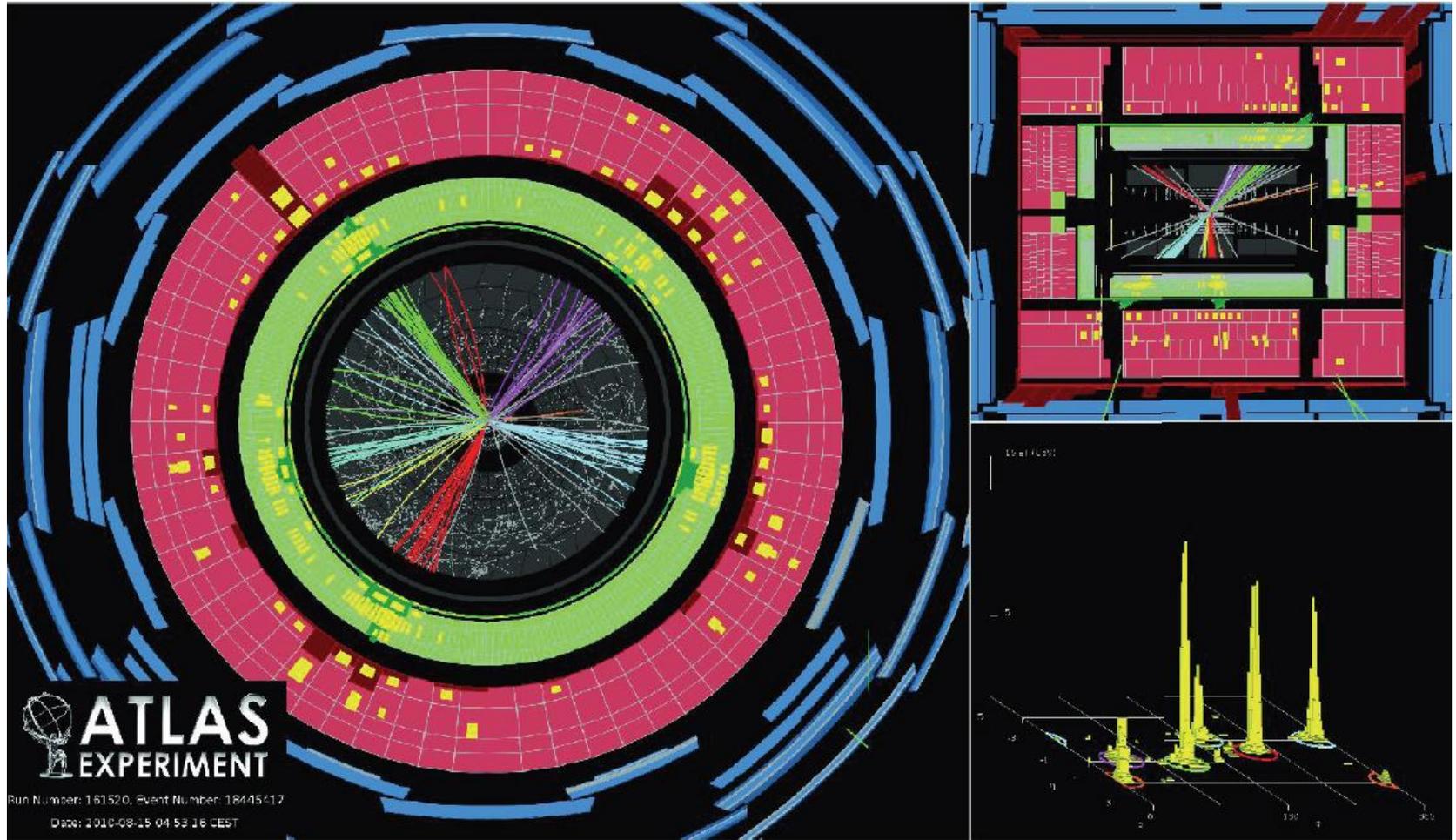
- For example (Durham/ $k_t$  algorithm)

$$d_{ij} \equiv y_{ij}^D = \frac{2 \min(E_i^2, E_j^2)(1 - \cos \theta_{ij})}{Q^2}$$

- Cluster the two “closest” partons into a single proto-jet, assigning momentum by (say)  $p_{ij} = p_i + p_j$
- Repeat procedure on the remaining  $n-1$  proto-jets.
- Iterate until all  $y_{ij} \gg y_{cut}$  (= jet resolution parameter)
- Remaining objects are jets.
- Properties depend on  $d_{ij}$
- Automatically IR safe because starts with most soft/collinear



# Jets at hadron colliders



# A word about kinematics

- At a hadron collider, we have no idea where the “rest of the proton” went (mostly down the beampipe)
- Since we have no idea about longitudinal momentum conservation, we would like variables that transform simply under

longitudinal Lorentz boosts:

$$\begin{pmatrix} E \\ p_z \end{pmatrix} \rightarrow \begin{pmatrix} \gamma & \beta\gamma \\ \beta\gamma & \gamma \end{pmatrix} \begin{pmatrix} E \\ p_z \end{pmatrix} \quad \Rightarrow \quad E \pm p_z \rightarrow \gamma(1 \pm \beta)(E \pm p_z)$$

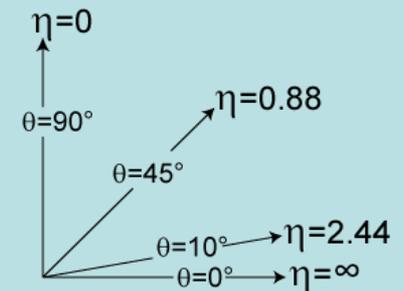
- **Rapidity**  $y \equiv \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) \quad y \rightarrow y + \frac{1}{2} \ln \left( \frac{1 + \beta}{1 - \beta} \right)$

- For massless particles, rapidity is equal to

pseudorapidity:

$$\eta \equiv -\ln \tan \left( \frac{\theta}{2} \right) = \frac{1}{2} \ln \left( \frac{1 + \cos \theta}{1 - \cos \theta} \right) = \frac{1}{2} \ln \left( \frac{|\mathbf{p}| + p_z}{|\mathbf{p}| - p_z} \right)$$

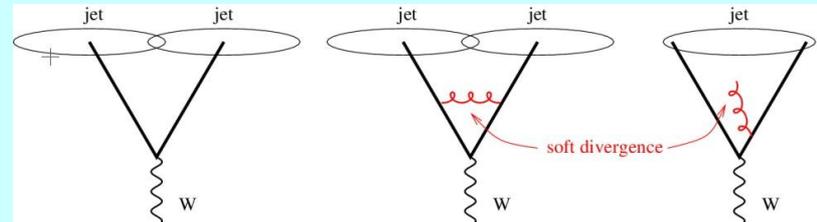
- Detector “coordinates”:  $(p_T, \eta, \phi)$



# Jets at hadron colliders

- Historically, “cone algorithms” were used, rather than  $e^+e^-$  style “cluster algorithms”.

- However, definitions of “seed” for early cone algorithms



Salam  
1011.5131

(where you start looking for a jet) were **not IR safe**.

- First cluster algorithm at hadron colliders was  $k_t$  algorithm (Catani et al., 1992; Ellis, Soper, 1993)

- “distance” measure  $d_{ij}$  modified to be invariant under longitudinal boosts:

$$d_{ij} = \min(p_{t,i}^2, p_{t,j}^2) \frac{\Delta R_{ij}^2}{R^2}$$

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

- Also need to define distance to beam:  $d_{iB} = p_{t,i}^2$
- If  $d_{iB}$  is smallest, proto-jet is removed and called a jet.
- IR safe, but **irregular shaped jets** were inconvenient for estimating effects of “underlying event”

# Anti- $k_t$ jet algorithm

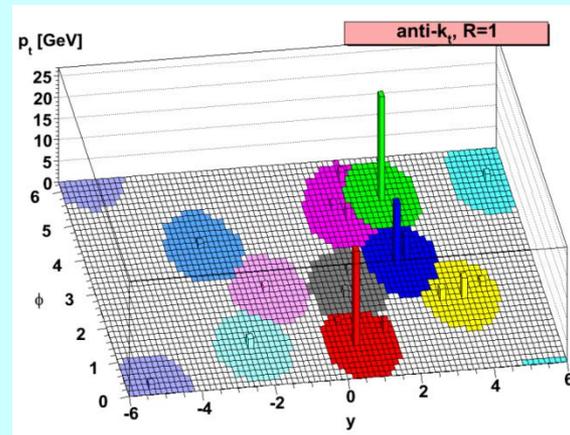
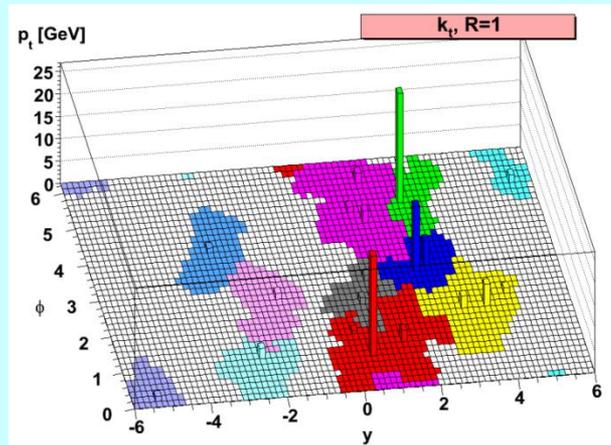
Cacciari, Salam, Soyez, 0802.1189

- Simply invert the  $p_t$  factors in  $k_t$  algorithm:

$$d_{ij} = \min(p_{t,i}^{-2}, p_{t,j}^{-2}) \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = p_{t,i}^{-2}$$

- Now the hardest (largest  $p_t$ ) particles tend to cluster first, soft wide angle ones last. (Still **IR safe** to add soft last) Now boundary of jet (catchment area for an additional soft particle) is **very circular**.



Cacciari, Salam,  
Soyez, 0802.1188;  
Salam, 0906.1833

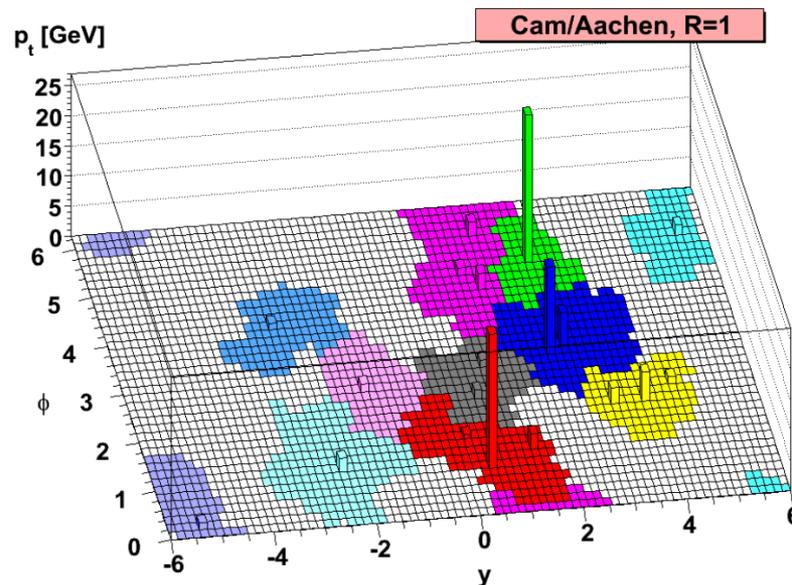
- Anti- $k_t$  is default for both ATLAS ( $R = 0.4, 0.6$ ) and CMS ( $R = 0.5, 0.7$ )

# Cambridge/Aachen (C/A) jet algorithm

- Intermediate between  $k_t$  and anti- $k_t$  algorithms, clustering depends only on angles:

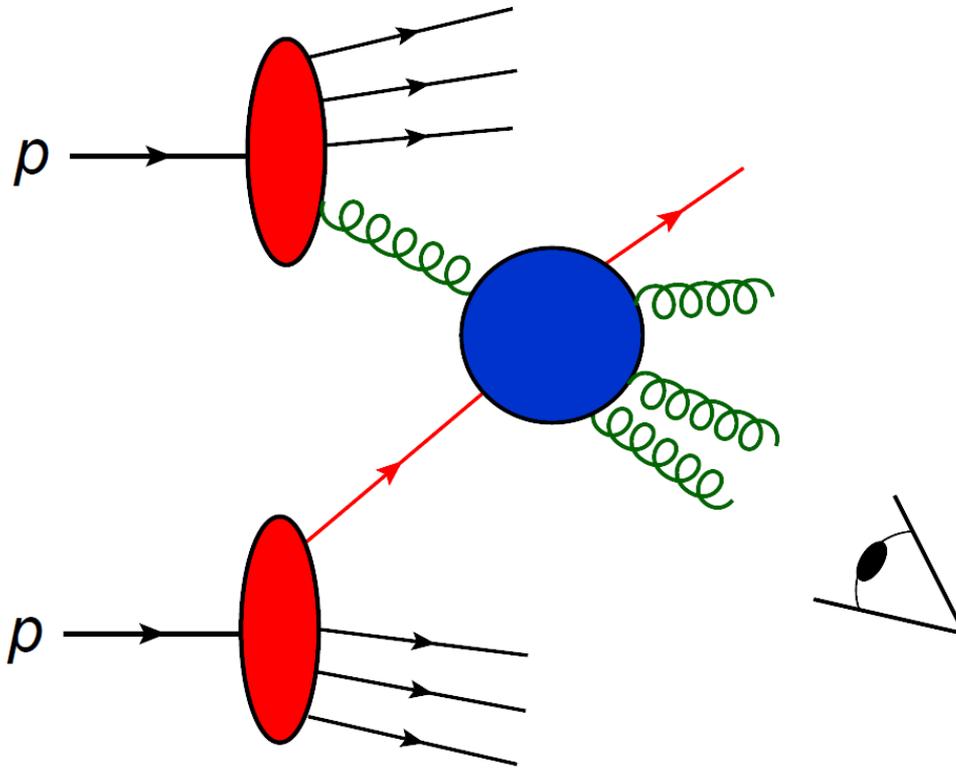
$$d_{ij} = \frac{\Delta R_{ij}^2}{R^2} \quad d_{iB} = 1$$

- Typically used with a large  $R$ , say  $R = 1.2$ , as the first step in **jet substructure** studies. (Anti- $k_t$  jets don't work well for this.)



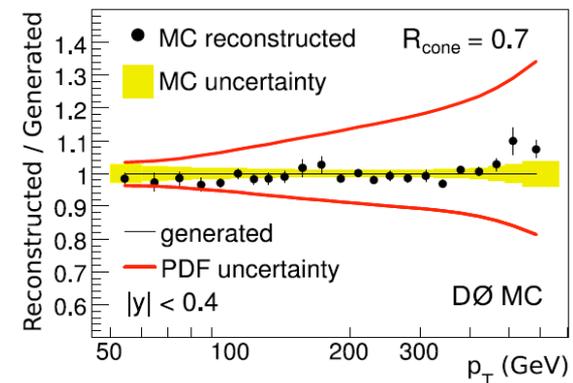
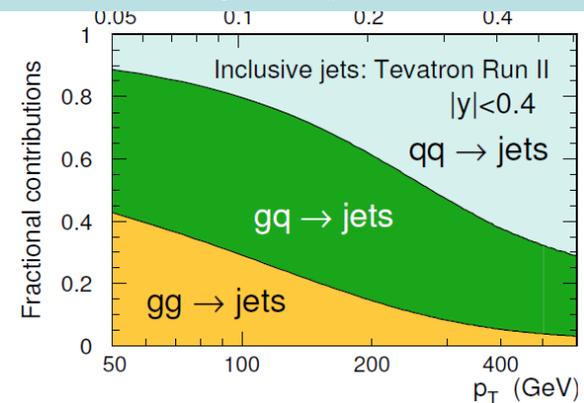
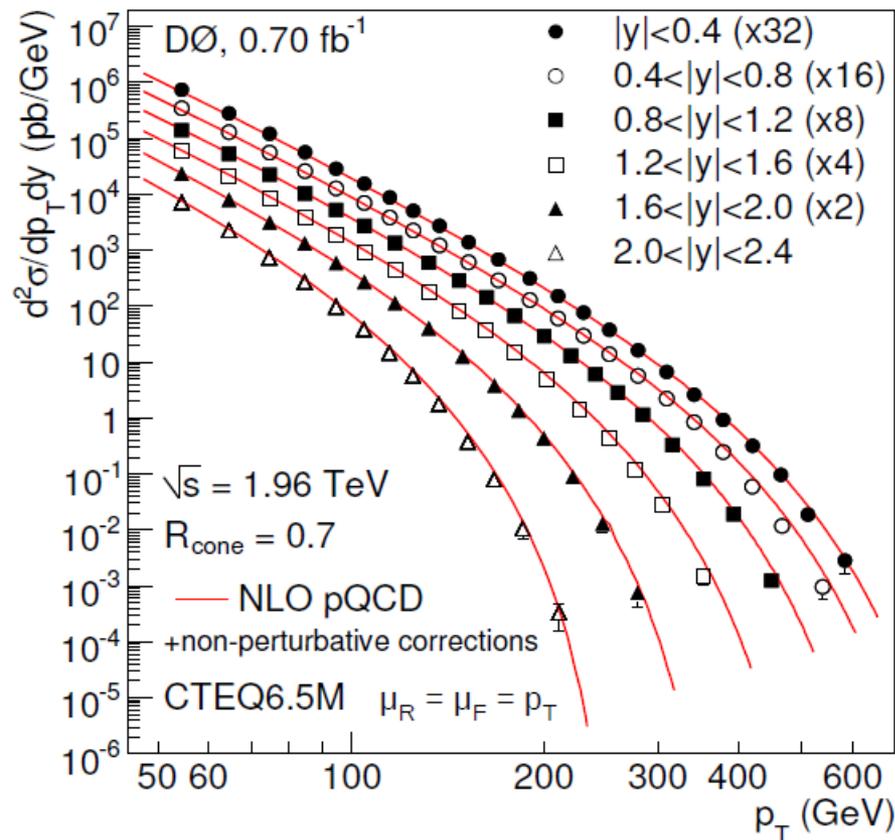
# Inclusive Jets

- Just ask for a single jet, in a given range of  $p_T$  and  $\eta$



# Inclusive jets at Tevatron

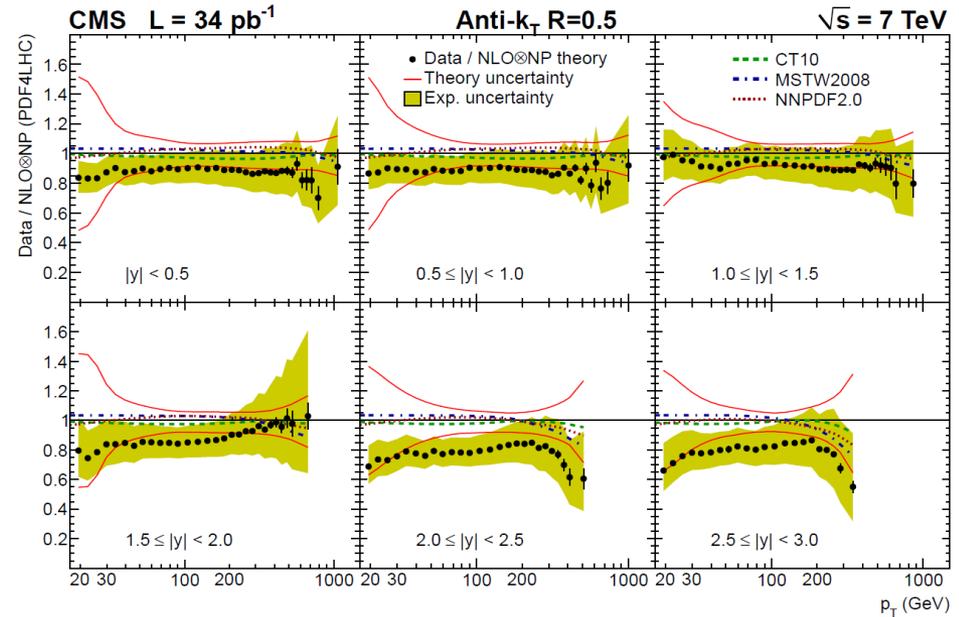
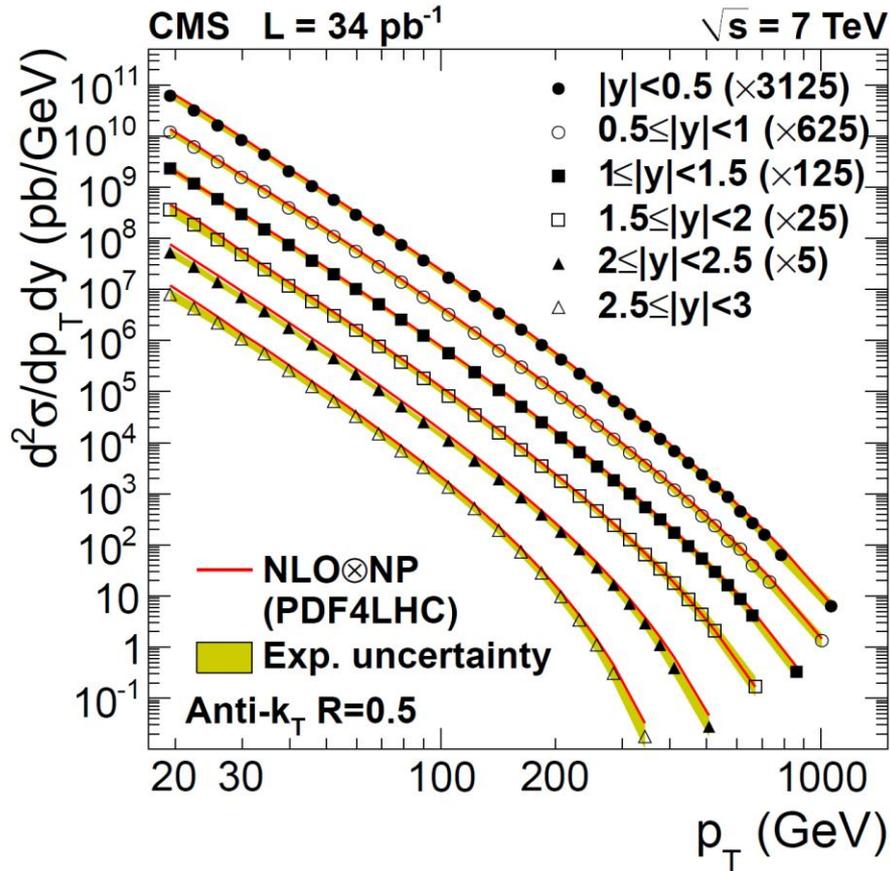
- “Midpoint” cone algorithm not IR safe in general but OK here (through NLO).
- Note sensitivity to pdfs, especially large  $x$  gluon, which is poorly constrained.



D0, 1110.3771

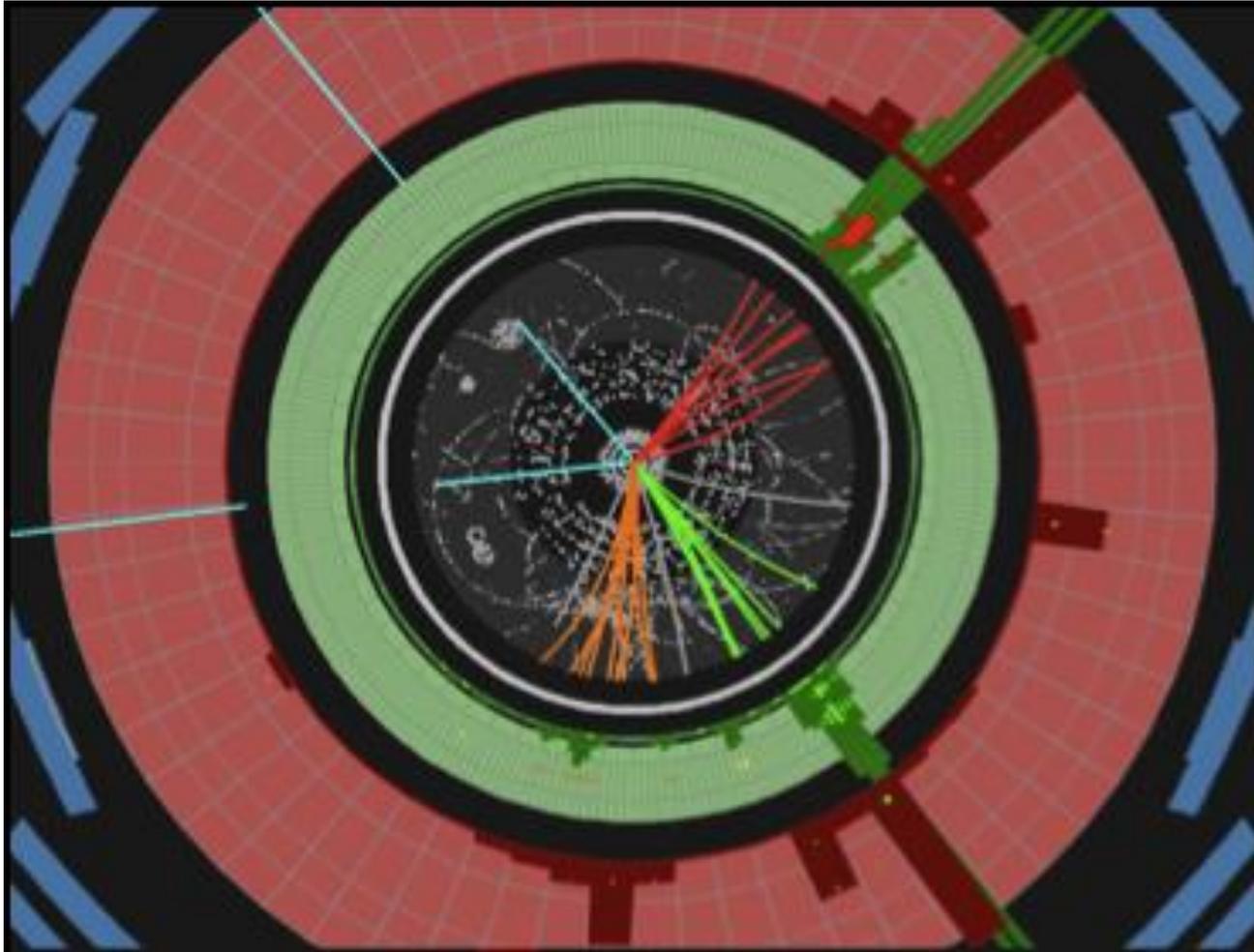
# Inclusive jets at LHC

- IR safe anti- $k_t$  jet algorithm, better coverage at forward rapidities (where NLO theory is not working quite as well)



CMS, 1106.0208

# More complicated final states

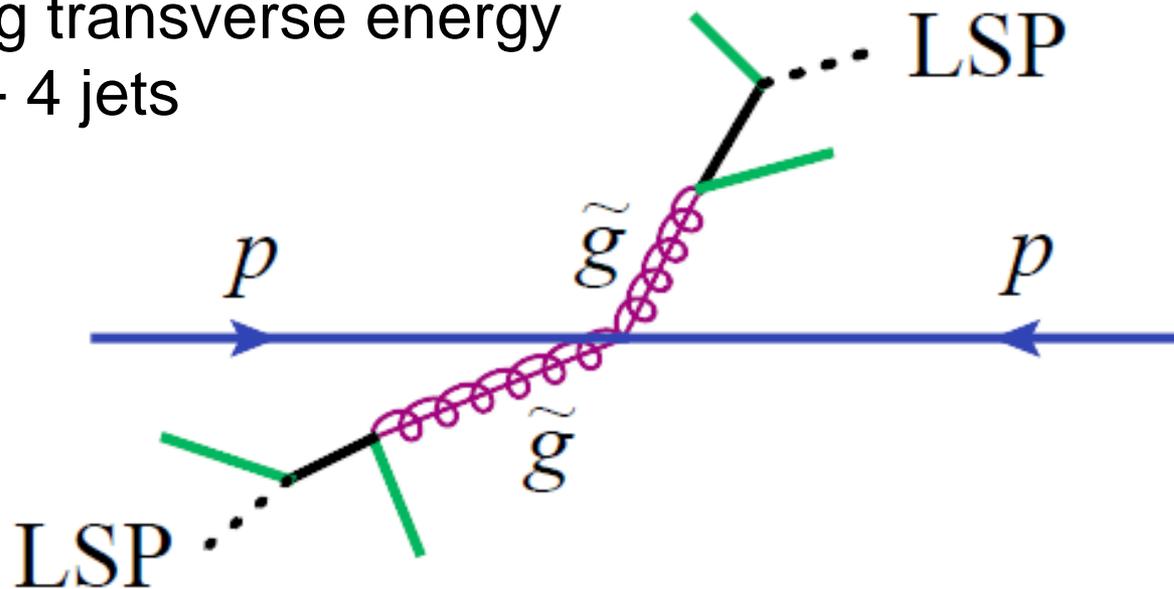


# Classic SUSY dark matter signature

→ Multiple jets + missing energy (+ lepton(s)?)

In models such as supersymmetry, heavy produced particles (colored) decay rapidly to stable Weakly Interacting Massive Particle (WIMP) plus jets

→ Missing transverse energy  
MET + 4 jets



# Happens in Standard Model too

- **MET + 4 jets from**  
 $pp \rightarrow Z + 4 \text{ jets},$   
 $Z \rightarrow \nu\nu$

Neutrinos also weakly interacting,  
escape detector.

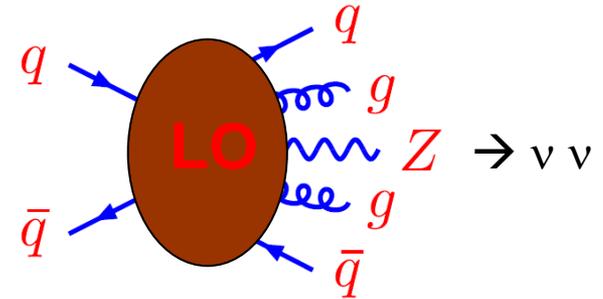
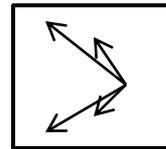
Irreducible background.

Also a large background from

$$pp \rightarrow W + 4 \text{ jets},$$
$$W \rightarrow l\nu$$

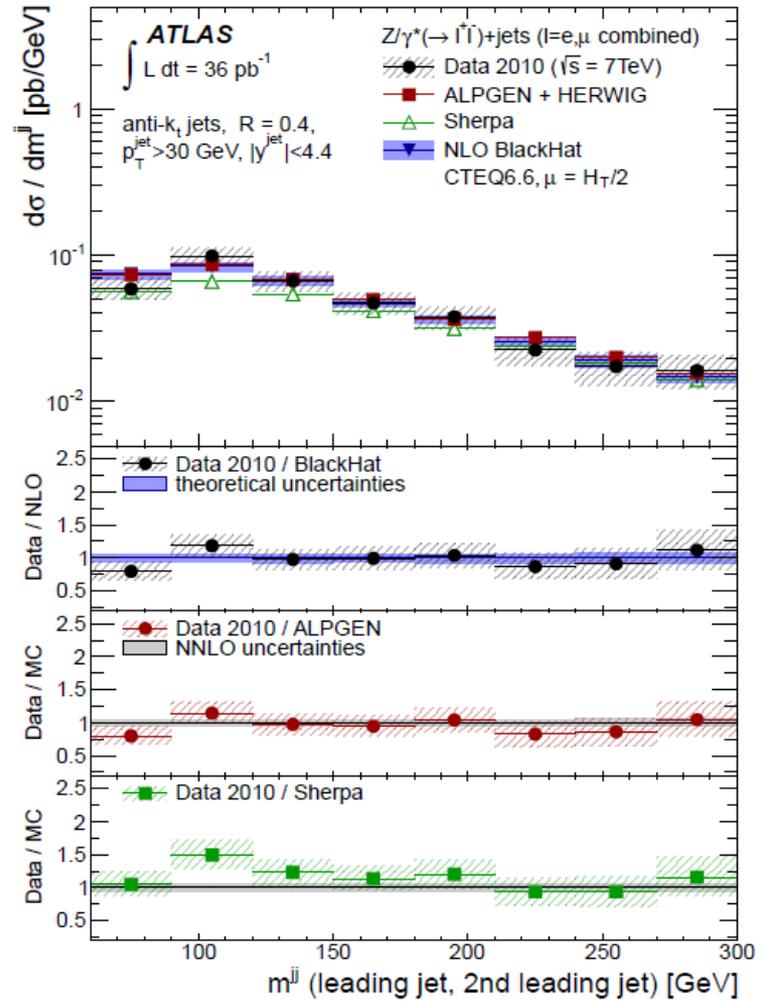
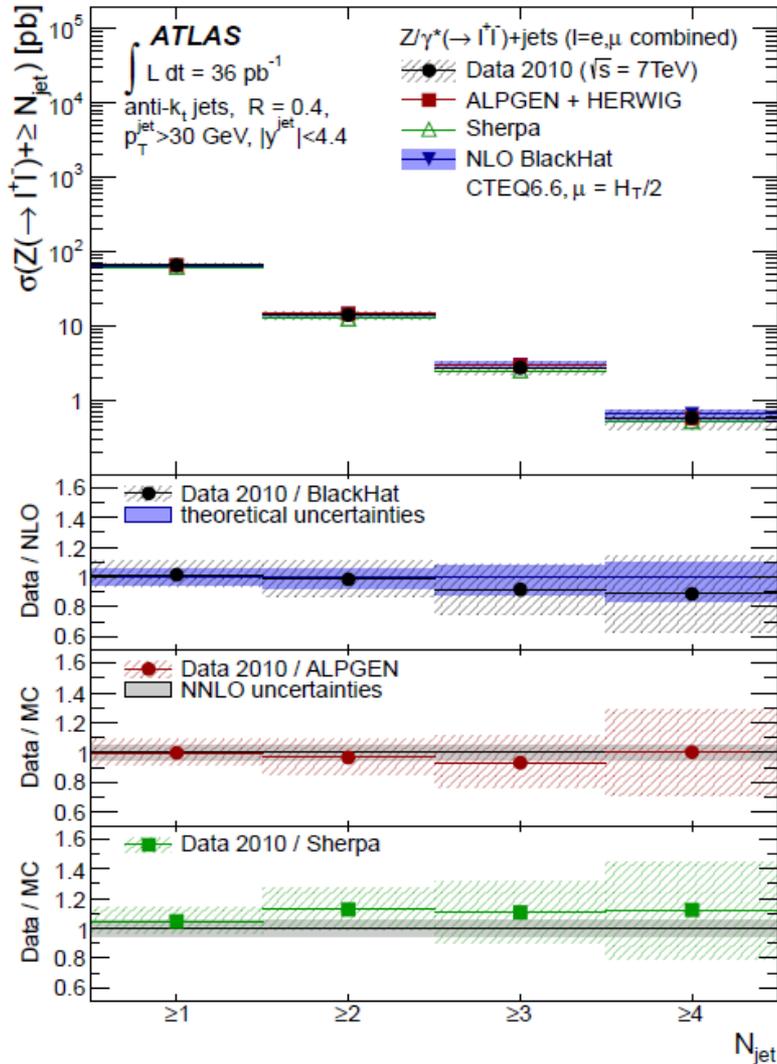
(~ 10x  $Z \rightarrow \nu\nu$  rate)

if you lose the charged lepton  
(or if you **want** a lepton)

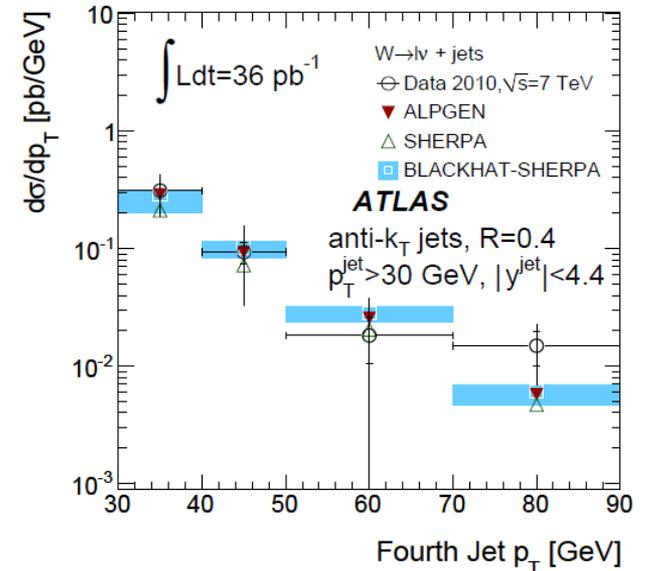
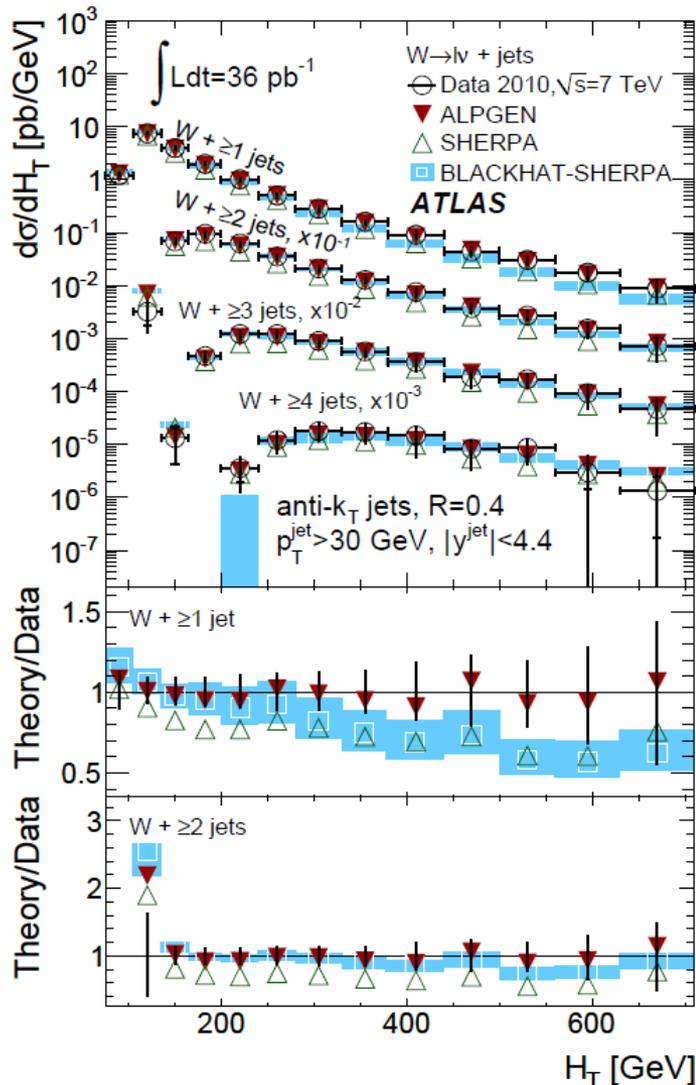


Motivates study of  $V + n \text{ jets}$  at Tevatron and LHC

# NLO $pp \rightarrow Z + 1,2,3,4$ jets vs. ATLAS 2010 data



# NLO $pp \rightarrow W + 1,2,3,4$ jets vs. ATLAS 2010 data

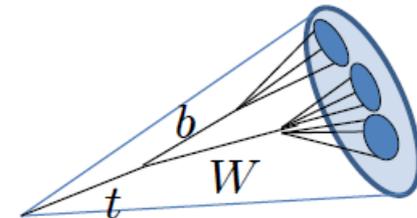
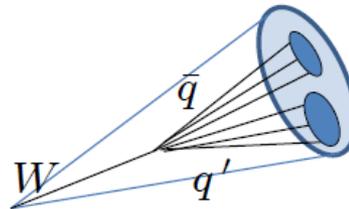
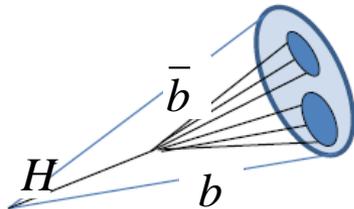
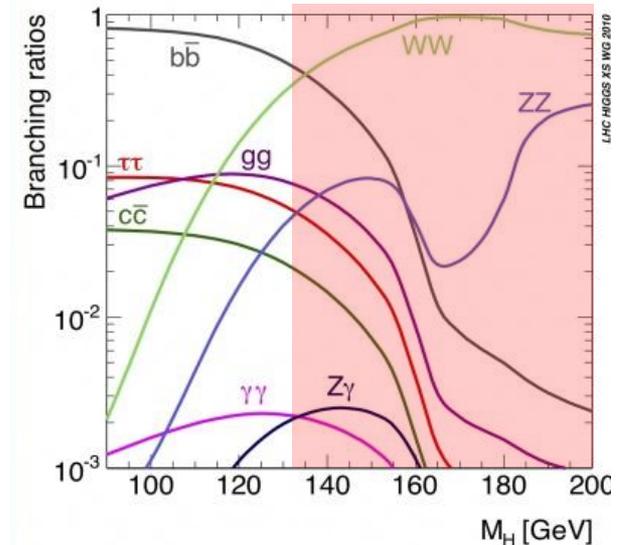


NLO undershoots badly for  $W + 1$  jet  
 – production dominated by  $W + 2$  parton configurations. Theory can be improved here:  
 Rubin, Salam, Sapeta 1006.2144

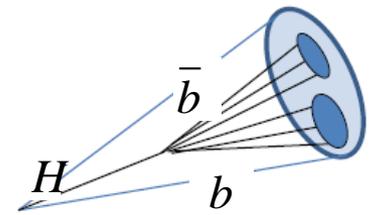
$$H_T = p_T^l + p_T^\nu + \sum_j p_T^j$$

# Boosted jets & jet substructure

- Decays of heavy particles can produce multiple jets:
- A light SM Higgs boson  $\rightarrow bb$  *most of the time*
- Top quark  $\rightarrow Wb \rightarrow q\bar{q}b$  *most of the time*
- How to find if parent particle is boosted, so jets merge?
- How to distinguish from jets from direct QCD production?



$$pp \rightarrow WH \rightarrow l\nu b\bar{b}$$



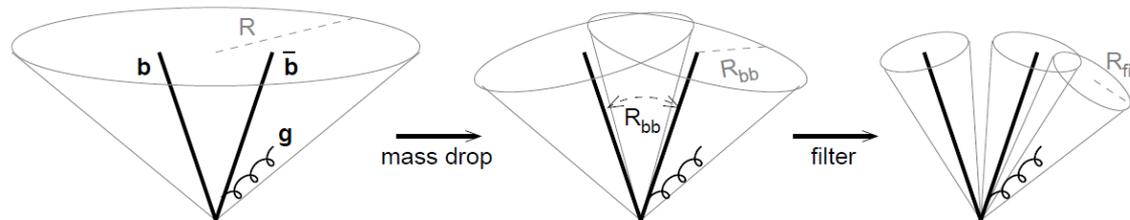
Butterworth, Davison, Rubin, Salam, 0802.2470

- For  $WH$  near production threshold, backgrounds from top ( $t\bar{t} \rightarrow l\nu b\bar{b}jj$ ) made search for  $H \rightarrow b\bar{b}$  at LHC look very difficult.
- Background suppressed well above threshold,  $p_T^H \sim 200\text{-}300$  GeV, because the  $b$  quarks are boosted, moving in same direction.
- Start with C/A  $R = 1.2$  “fat jet”. Break jet  $j$  into 2 subjets,  $j_1$  and  $j_2$ , by undoing last C/A clustering. Look for a large “mass drop”,

$$\mu m_j > m_{j_1} > m_{j_2}$$

and a splitting that is “not too asymmetric” (to suppress QCD soft radiation)

- Another “filtering” stage looks for 3 hardest subjets on a finer angular scale, to keep perturbative QCD radiation while suppressing the underlying event.



# $pp \rightarrow WH \rightarrow l\nu b\bar{b}$ , and more

Butterworth, Davison, Rubin, Salam, 0802.2470

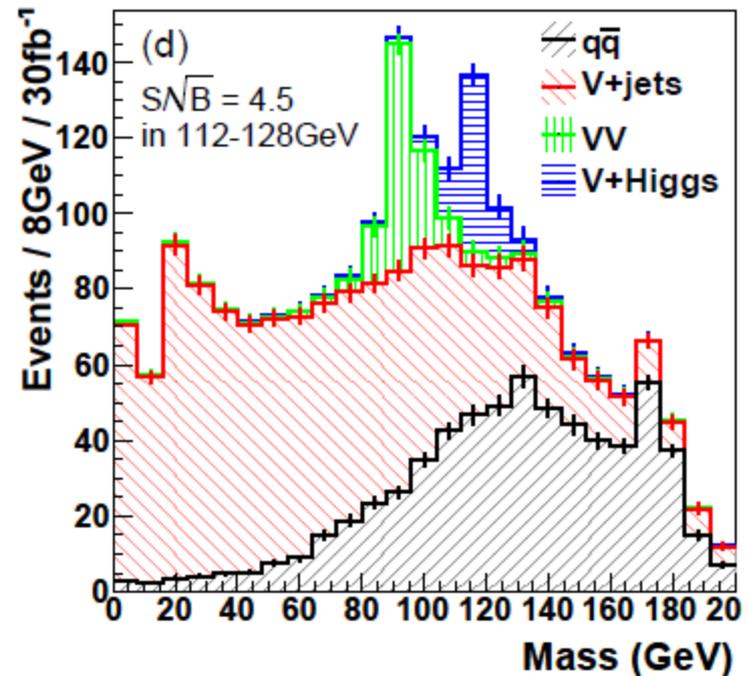
- Result is a greatly boosted  $S/\sqrt{B}$

- Also heavy  $H \rightarrow WW \rightarrow l\nu jj$

Seymour (1994)

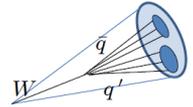
- Many subsequent variations on boosted jets and jet substructure techniques: [trimming](#), [pruning](#), [angular correlation functions](#), ...

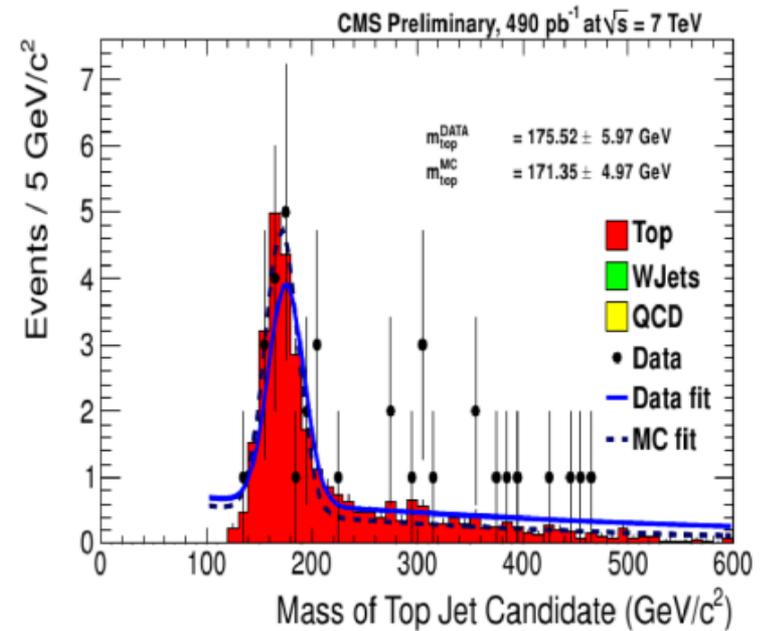
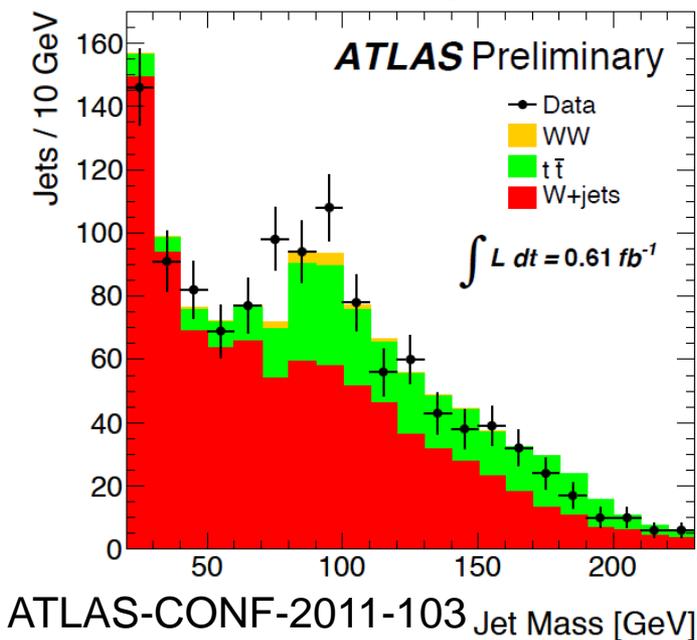
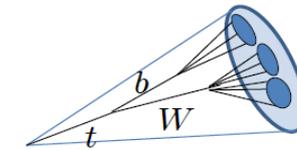
- Also applied to beyond-SM scenarios such as  $\sim$  TeV scale resonances decaying to top quark pairs.



$$pp \rightarrow t\bar{t} \rightarrow l\nu b\bar{b}jj$$

- Large cross section makes it ideal place to test these techniques experimentally


 $p_T^{W \rightarrow l\nu} > 200 \text{ GeV}, \quad p_T^{\text{C/A jet}} > 180 \text{ GeV}$



# Levels of Approximation

- Monte Carlos (PYTHIA, HERWIG,...)
- LO, fixed-order matrix elements (ALPGEN, SHERPA, MADGRAPH)
- LO MEs matched to parton showers (DITTO)
- NLO MEs (parton level; multiple programs)
- NLO MEs + shower (MC@NLO, POWHEG)
- NNLO MEs (FEHiP, FEWZ; HNNLO, DYNNLO)
- MC@NNLO?

# Parton Shower Monte Carlos

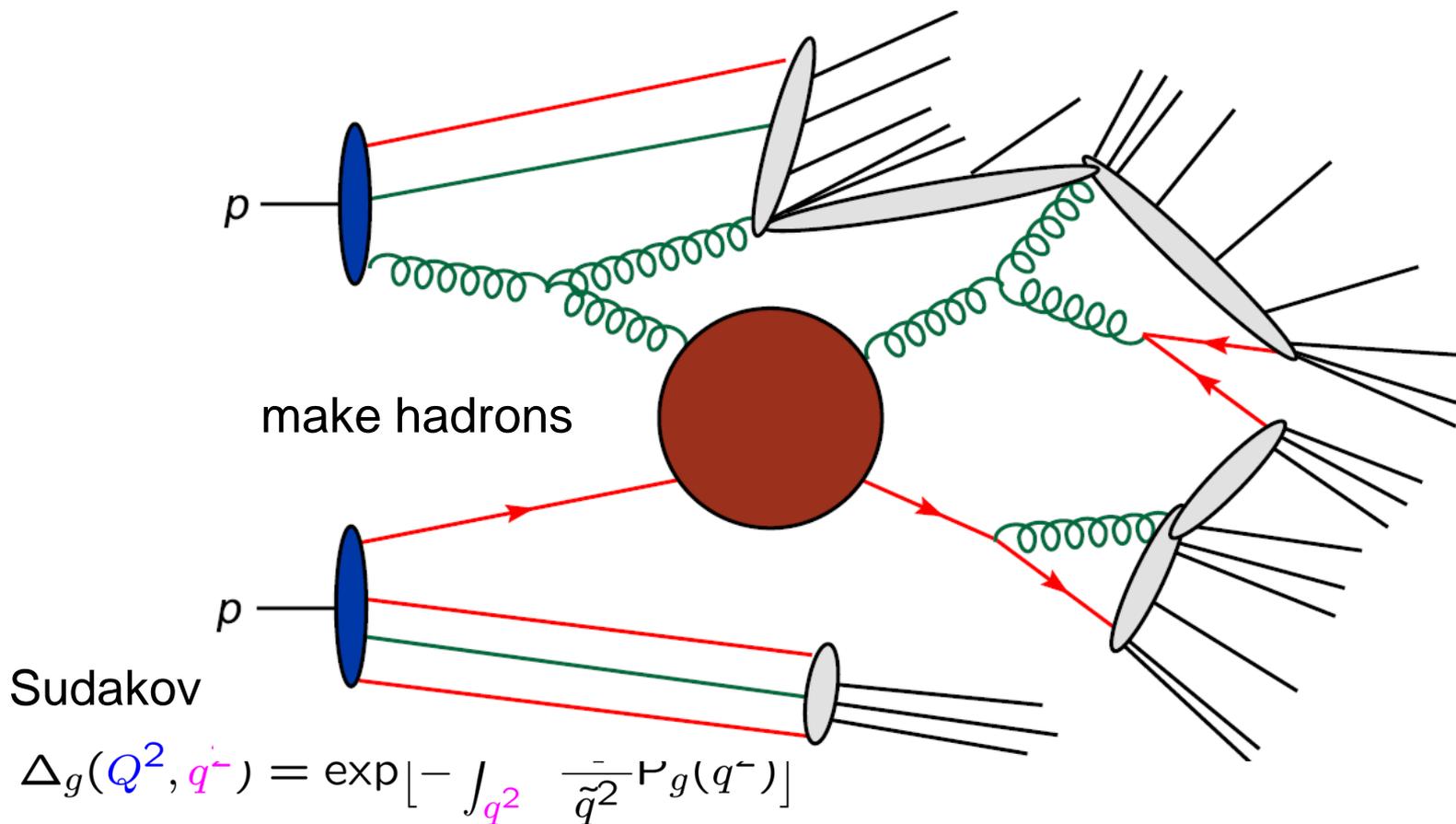
- Allow exclusive description of individual events at hadron level
- Can apply models for hadronization, the underlying event
- Indispensable to experimental analyses
- Overall normalization accuracy sacrificed a bit – but this is improving rapidly as NLO+MC programs expand their reach

# Monte Carlos

- Based on properties of **soft and collinear radiation** in QCD
- Partons surrounded by “cloud” of soft and collinear partons
- Leading double logs of  $Q_{\text{hard}}/Q_{\text{soft}}$  **exponentiate**, can be generated **probabilistically**
- Shower starts with **basic 2 → 2 parton scattering**
  - or **basic production process** for  $W, Z, tt$ , etc.
- Further radiation **approximate**, based on LO Altarelli-Parisi kernel + soft behavior.
- Requires infrared cutoff
- Shower can be evolved down to very low  $Q_{\text{soft}}$ , where models for **hadronization** and **spectator interactions (underlying event)** can be applied
- **Complete hadron-level event description attained**
- Normalization of event rates **unreliable**
- Event “shapes” **sometimes unreliable**

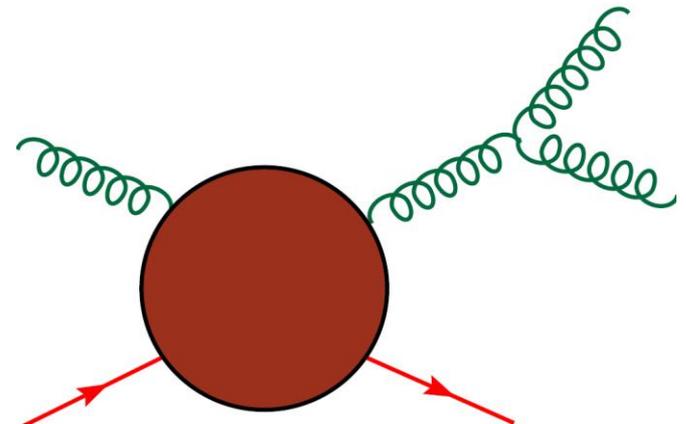
# Monte Carlos in pictures

Splitting probability:  $P_g(q^2) = \int_0^1 dz \frac{\alpha_s(q^2)}{2\pi} \hat{P}_{gg}(z) \Theta(q^2 - q_0^2)$



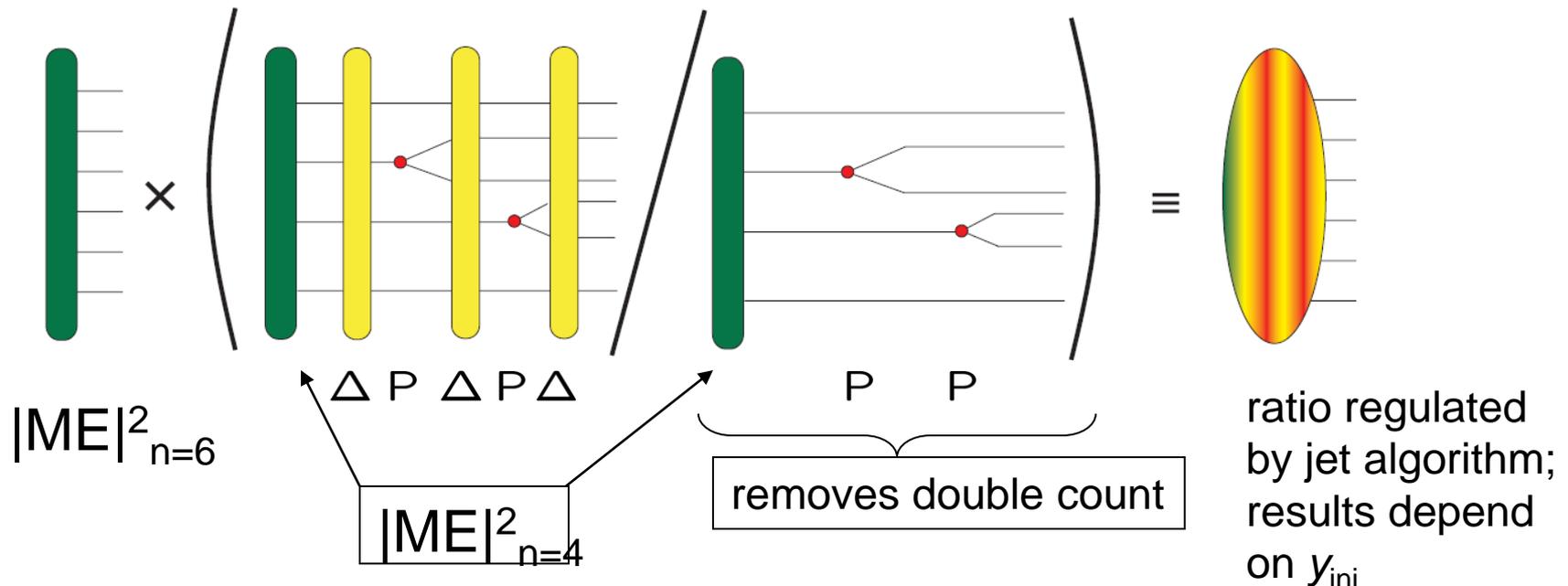
# Matching MEs to showers

- Would like to have both:
  - accurate hard radiation pattern of MEs
  - hadron-level event description of parton-shower MCs
- Why not just use  $2 \rightarrow 3, 4, \dots$  parton processes as starting point for the shower?
- Problem of **double-counting**:  
When does radiation “belong” to the shower, and when to the hard matrix element?



# ME/shower matching

- CKKW matching: [Catani, Kuhn, Krauss, Webber, hep-ph/0109231](#)
  - separate ME and shower domains using a common jet cluster algorithm variable ( $k_T$  algorithm with  $y = y_{ini}$ )
- an example in pictures: [Nagy, Soper, hep-ph/0607046](#)



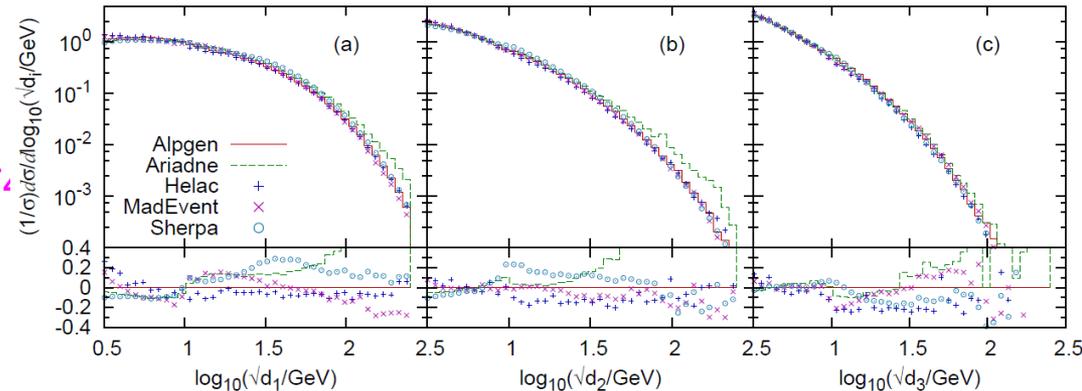
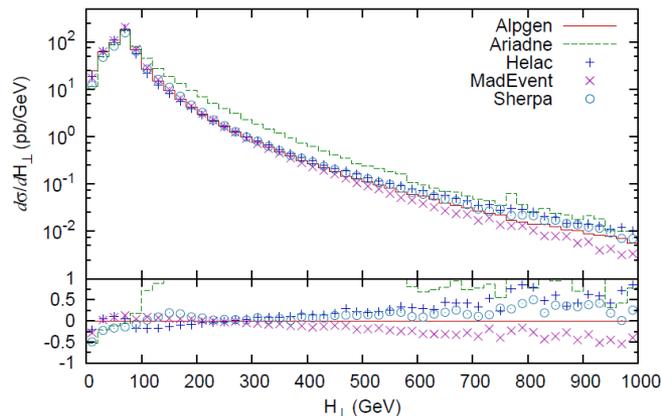
# ME/shower matching (cont.)

Several other general matching schemes available or in the works, e.g.:

- MLM scheme (ALPGEN)
- Lonnblad, hep-ph/0112284 (Ariadne)
- CKKW (Sherpa)
- Mrenna, Richardson, hep-ph/0312274
- Nagy, Soper, hep-ph/0601021
- VINCIA (Skands, Giele, Kosower)

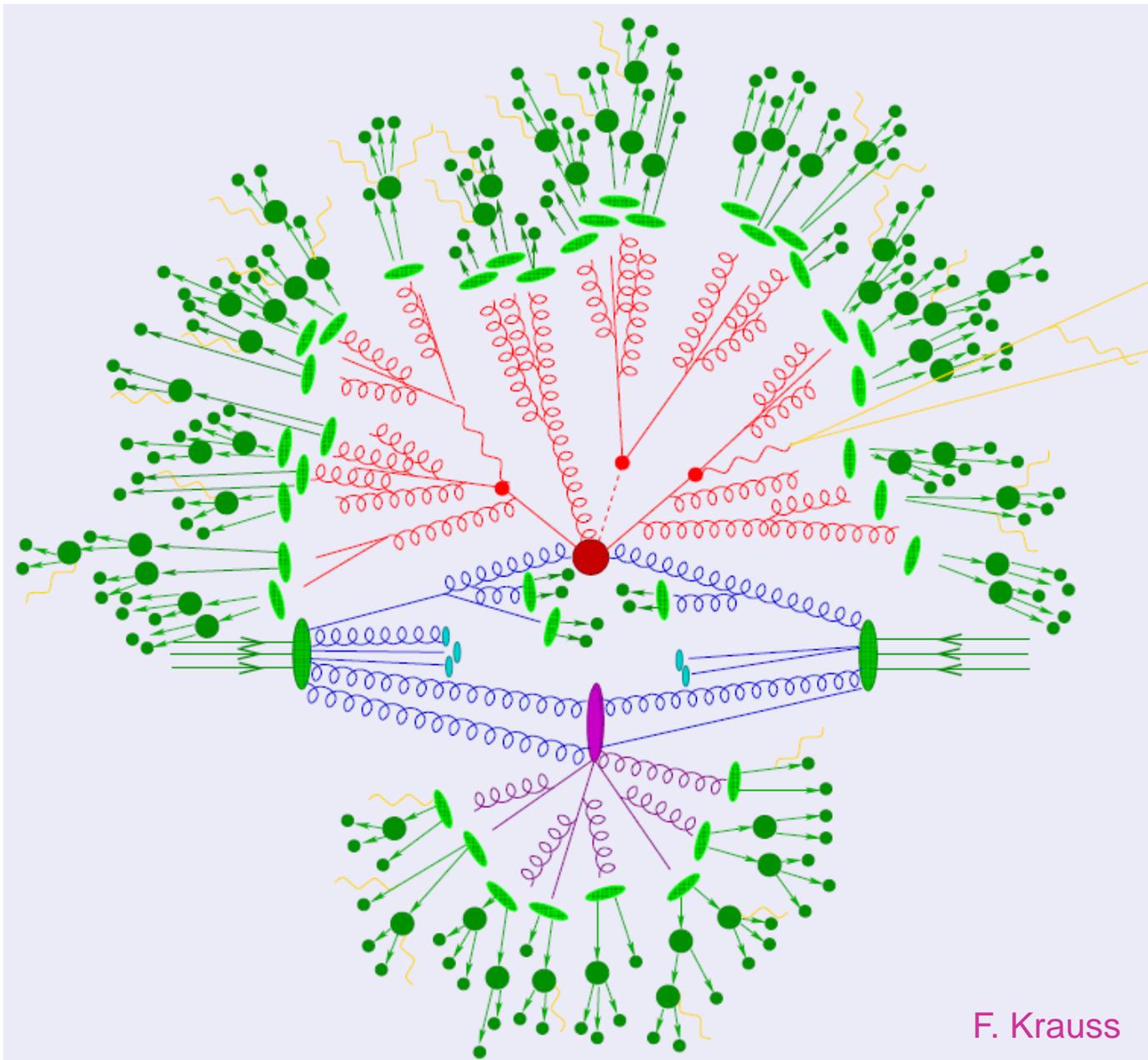
reasonable agreement between different schemes [0706.2569]

$p\bar{p} \rightarrow W + n \text{ jets at Tevatron}$



$d_i$  indicates transition between  $i$  and  $i-1$  jets in  $k_T$  algorithm

$$H_T = p_T^l + p_T^\nu + \sum_j p_T^j$$



F. Krauss