



Wir schaffen Wissen – heute für morgen

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Basic powersupply control –

Digital implementation of analog controllers

Digital implementation of analog controllers

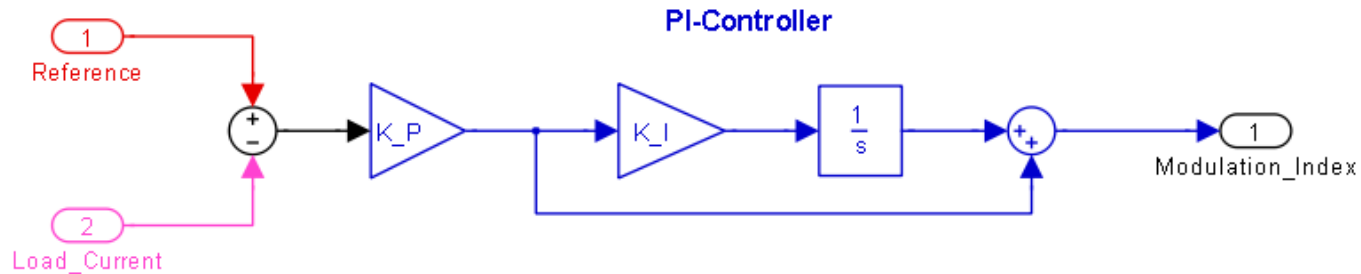
Part 1: Basic Powersupply Controller

- Essential Tasks of a basic powersupply controller and how to achieve them

Part 2: Discretization

- Paths to discrete controller
- Methods of discretization
- Effects of SamplingTime

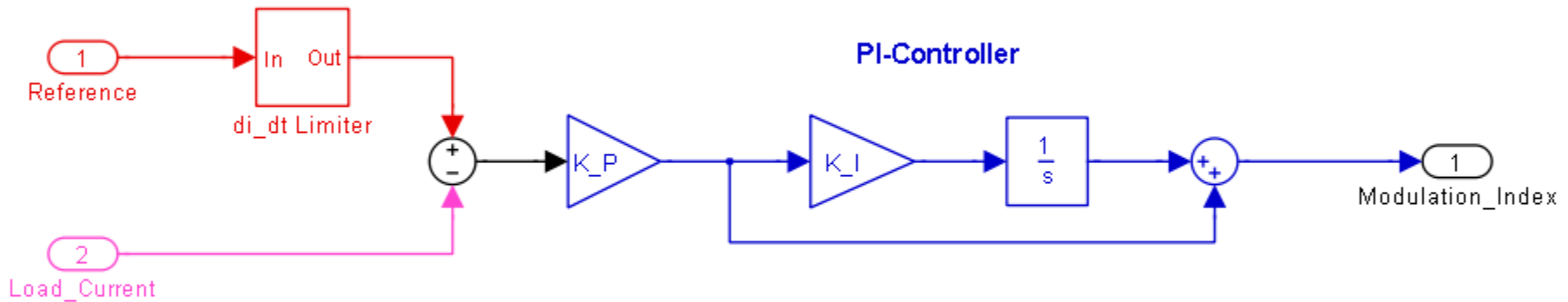
- Achieve zero steady-state error
-> Integral action



- $K_i = 1 / T_{\text{Magnet}}$
 - > experimentally (step response in open loop)
 - > $K_i = R_{\text{Magnet}} / L_{\text{Magnet}}$
- K_p can be found manually, starting value:

$$K_{p_init} = R_{\text{Magnet}} / U_{\text{DC_Link}} * \omega_{\text{CL}} / K_i$$

- Achieve zero steady-state error
 - > Integral action
- keep operation of controller linear (avoid limitations)
 - > Limit di_{Ref} / dt
 - > Anti-Windup

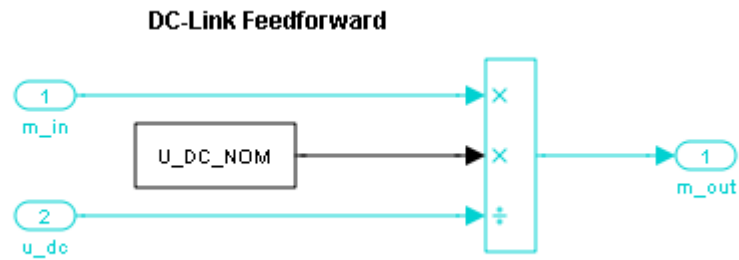
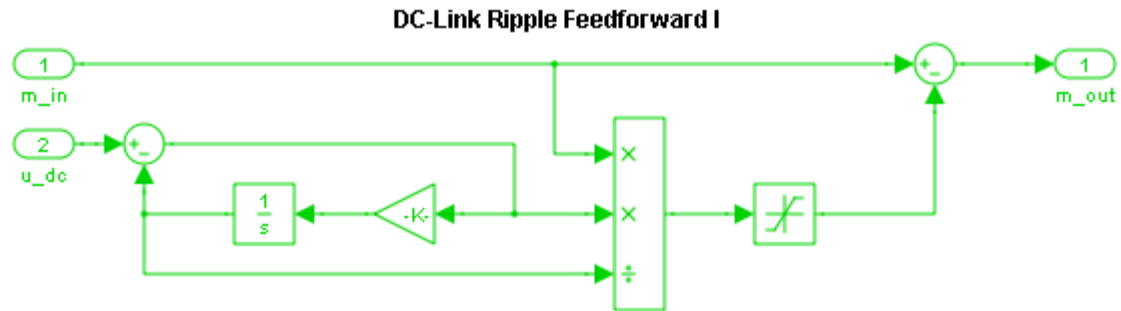


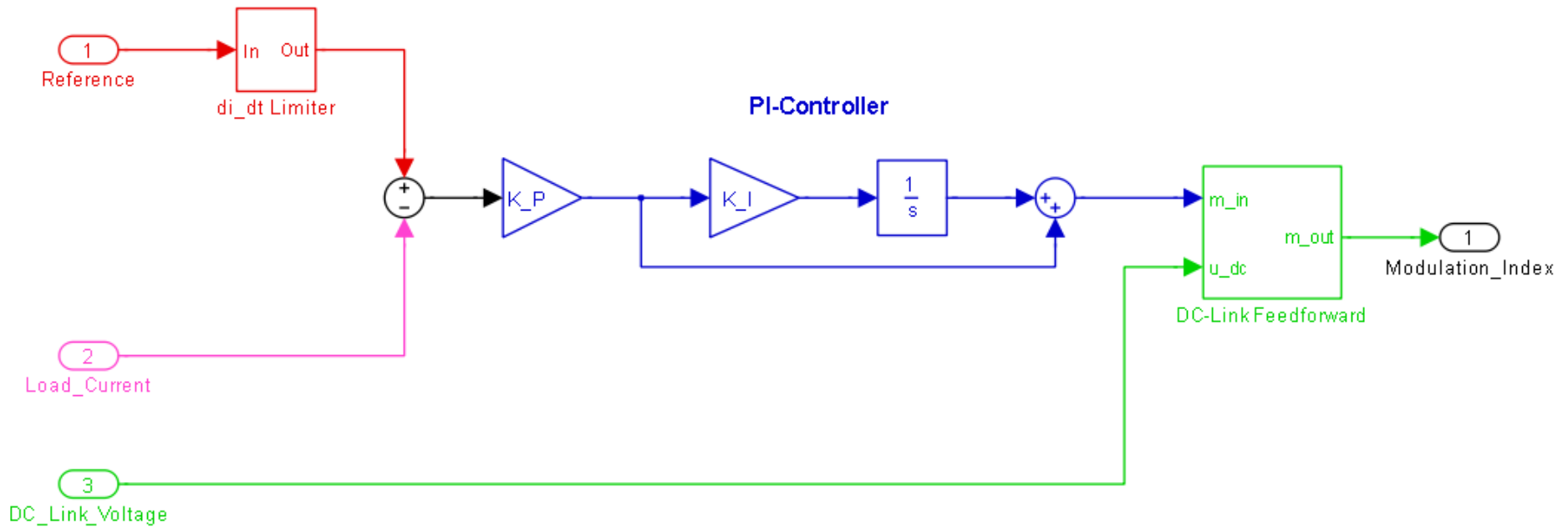
- Keeps the controller in the linear regime by preventing actuator saturation

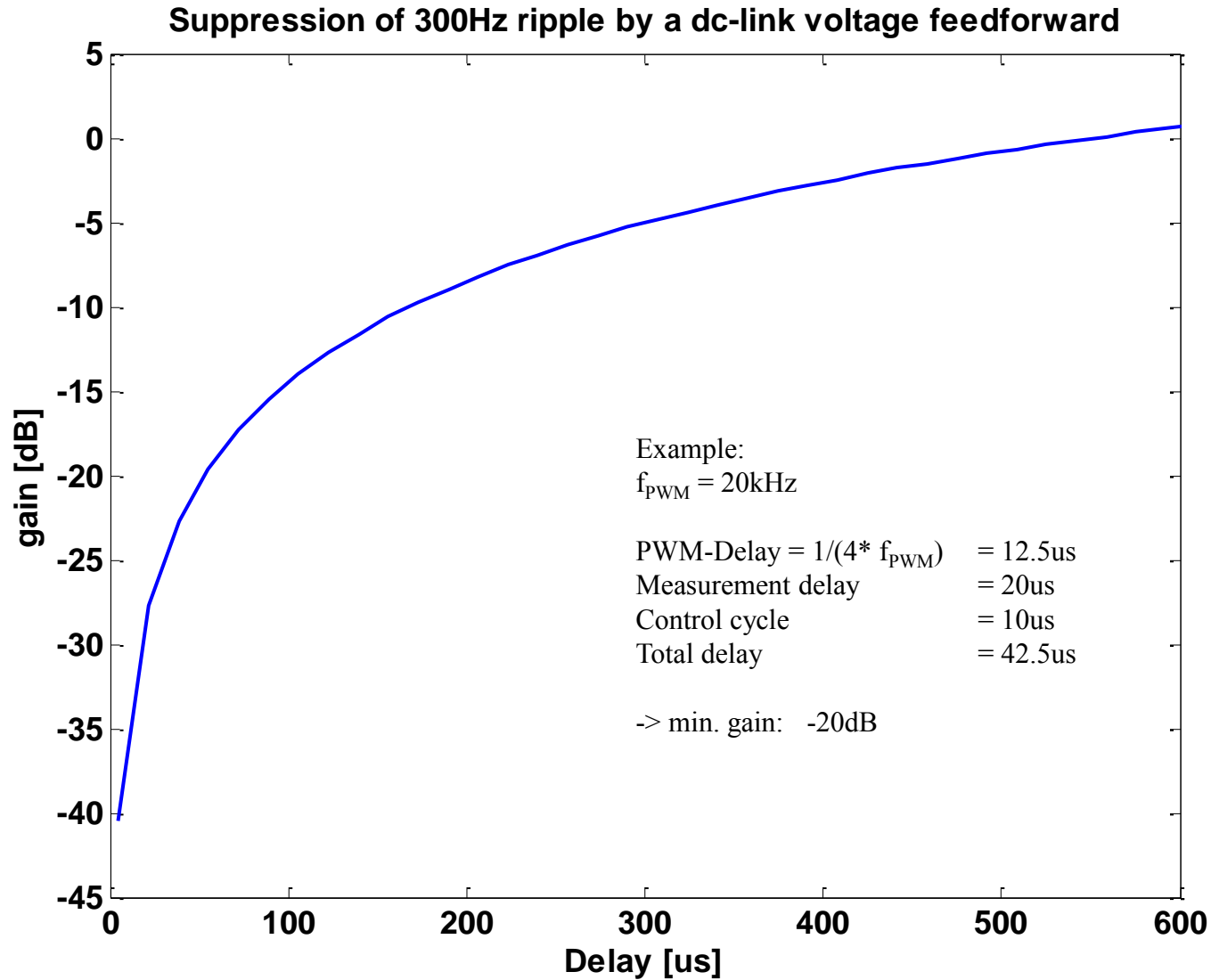
$$\left(\frac{dI}{dt}\right)_{MAX} = \frac{U_{DC_MIN} - U_{CONV} - I_{NOM} * R_{MAGNET_MAX}}{L_{MAGNET}}$$

- Anti-Windup is a remedy in case of actuator saturation

- Achieve zero error
 - > Integral action
- Stay in linear region
 - > Limit di_{Ref} / dt
 - > Anti-Windup
- Suppress dc-link voltage disturbances (e.g. 300Hz Ripple)
 - > feedforward the dc-link disturbances







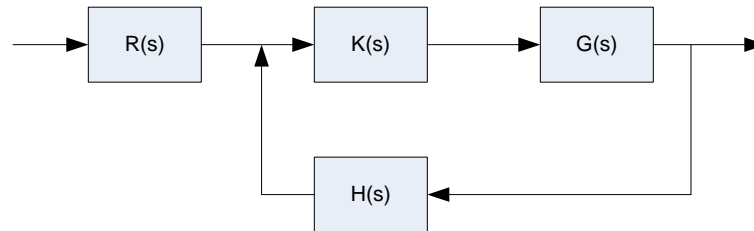
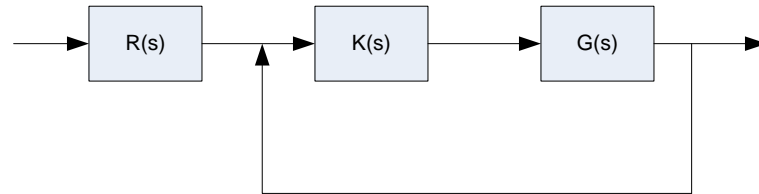
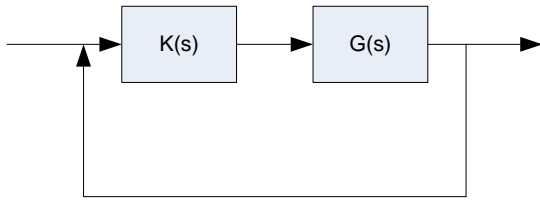
- Achieve zero error
 - > Integral action
- Stay in linear region
 - > Limit di_{Ref} / dt
 - > Anti-Windup
- Suppress dc-link voltage disturbances
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Protect Output Filter Resistor

-> Output limiter

- Reduce measurement noise
 - > Lowpass-filter for the measured value
- Reduce overshoot
 - > Lowpass-filter for the reference value

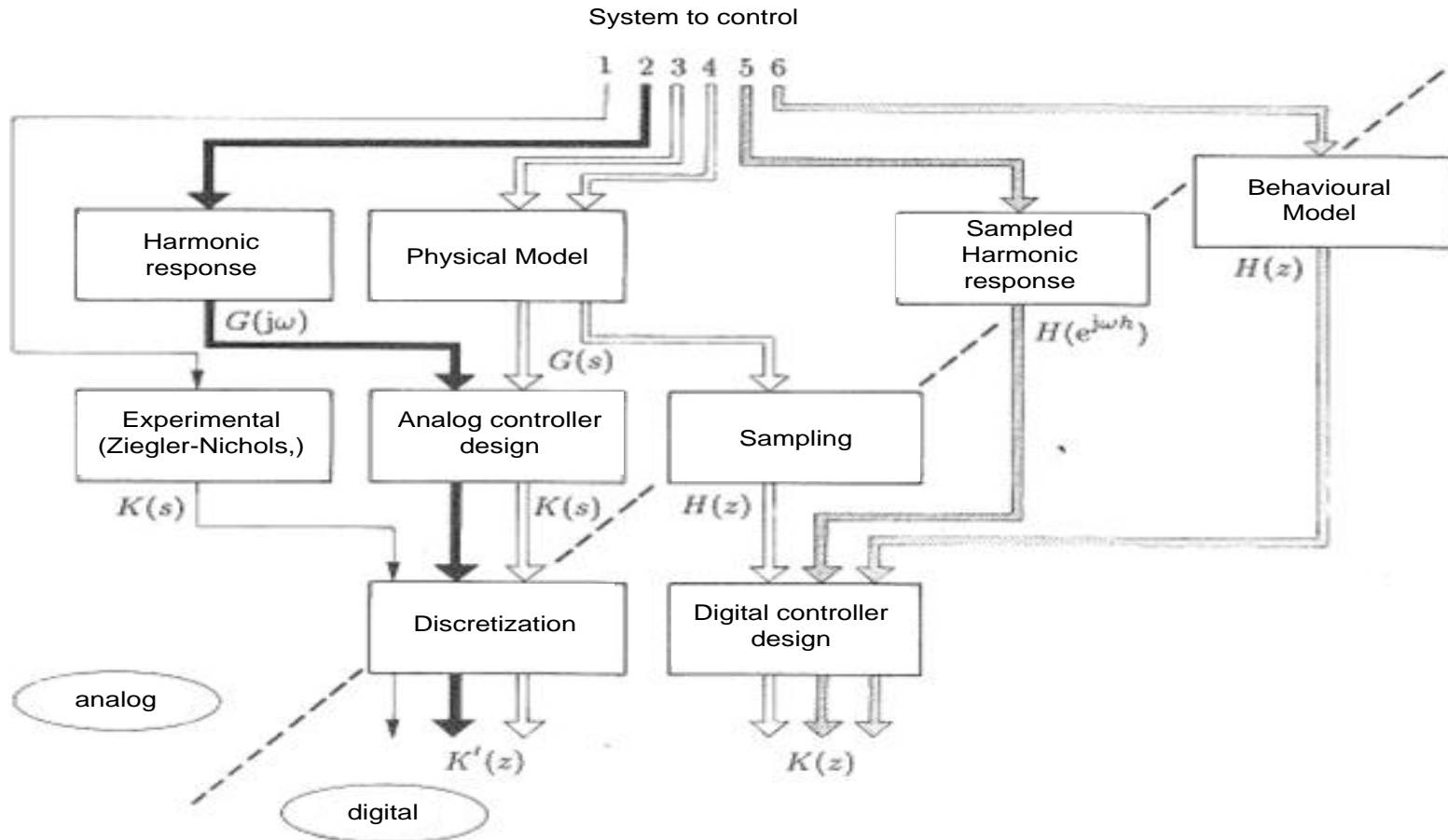
- Compensation of higher order plant dynamics e.g. the output filter
- 2-DOF structure to separately tune reference tracking and disturbance rejection



Analog:

$$u(t) = K_p * (e(t) + K_i * \int e(t) dt) \quad \leftrightarrow \quad K(s) = \frac{U(s)}{E(s)} = K_p * \left(1 + \frac{K_i}{s}\right)$$

Paths to discrete controller



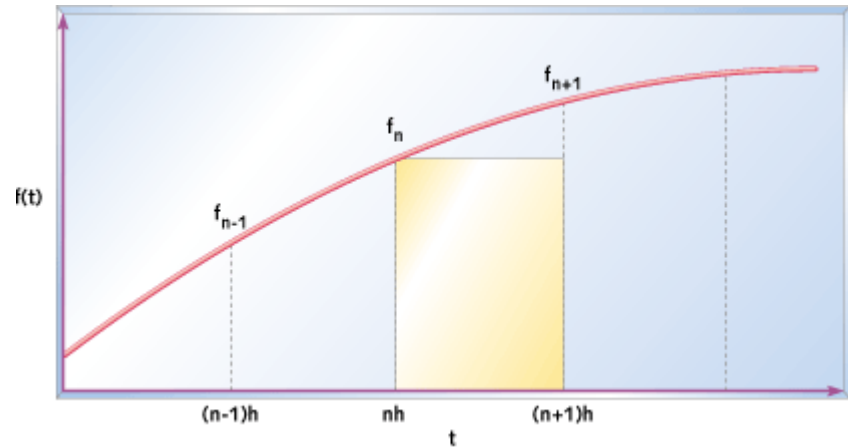
Source:
 Commande numérique de systèmes dynamiques, R. Longchamp

Area based approximations:

- Forward difference
- Backward difference
- Trapezoidal (Tustin, bilinear)

Response Invariant transforms:

- Step response (zero-order hold)
- Ramp response
- Impulse response

Pole-zero mapping

$$G(z) = \frac{z-1}{z} \mathcal{Z} \left\{ \frac{G(s)}{s} \right\}$$

Forward Euler:

$$y(n) = y(n-1) + T_s * u(n-1)$$

$$K(z) = \frac{T_s}{z-1}$$

Backward Euler:

$$y(n) = y(n-1) + T_s * u(n)$$

$$K(z) = \frac{zT_s}{z-1}$$

Trapezoidal:

$$y(n) = y(n-1) + \frac{T_s}{2} * (u(n-1) + u(n))$$

$$K(z) = \frac{T_s}{2} \frac{z+1}{z-1}$$

Analog:

$$u(t) = K_p * (e(t) + K_i * \int e(t) dt)$$

$$\leftrightarrow K(s) = \frac{U(s)}{E(s)} = K_p * \left(1 + \frac{K_i}{s}\right)$$

Discrete:

$$u(k) = K_p * (e(k) + e(k-1) * (K_i * T_s - 1) + u(k-1))$$

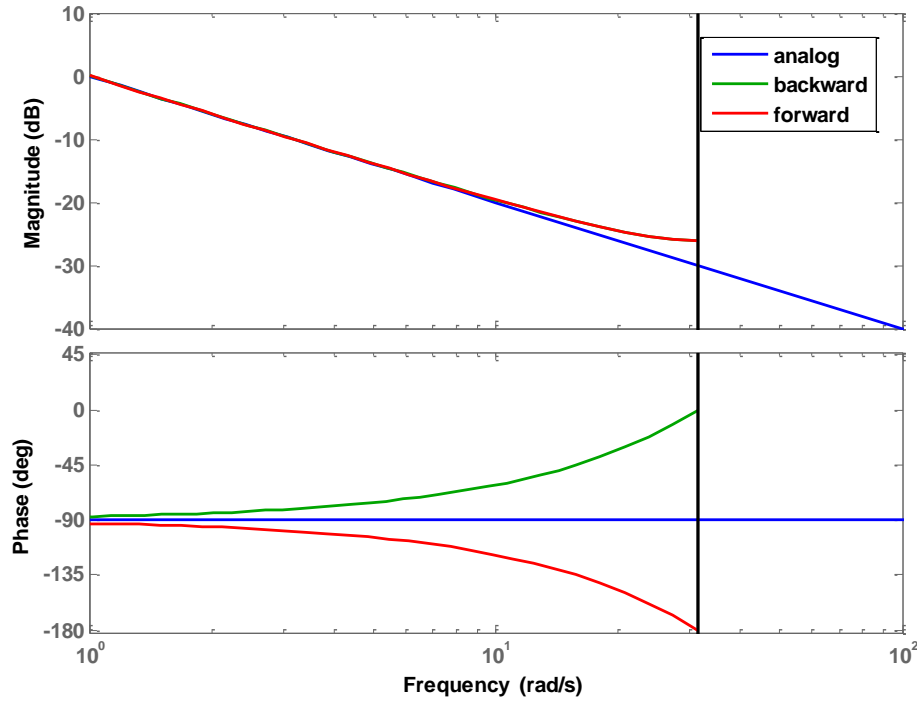
$$\leftrightarrow K(z) = \frac{U(z)}{E(z)} = K_p * \left(1 + \frac{K_i * T_s}{z-1}\right)$$

Approximations $z \leftrightarrow s$

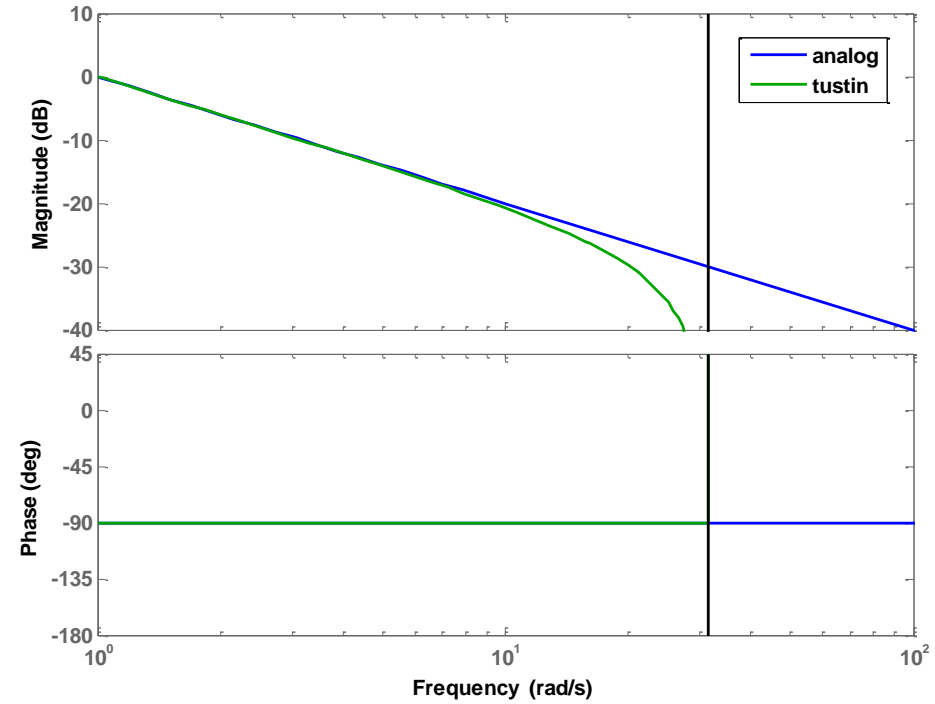
Näherung	Substitution T konstant	Abbildung $G(s) \rightarrow G(z)$ s-Ebene	z-Ebene
Rechteckregel vorwärts (Euler)	$s = \frac{z-1}{T}$ $z = 1 + sT$		
Rechteckregel rückwärts	$s = \frac{1}{T} \frac{z-1}{z}$ $z = \frac{1}{1-sT}$		
Trapezregel (Bilinear-Form, Tustin-Form)	$s = \frac{2}{T} \frac{z-1}{z+1}$ $z = \frac{1 + \frac{sT}{2}}{1 - \frac{sT}{2}}$		

Bode plot of integrators

Bode plot of discretized integrators



Bode plot of discretized integrators



How to choose sampling time

- too large -> loss of information
- too small -> loss of precision (numerical issues) / computational overload

- No absolute truth -> rules of thumb:
 - 10x faster than Shannons sampling theorem
 - $F_s = 10 - 30x$ system bandwidth
 - Loss of phase margin not more than $5^\circ - 15^\circ$ compared to the continuous system

- PI controller for magnet powersupplies is a good choice:
 - can be manually tuned (only two parameters K_p & K_i)
 - good static performance (zero error)
 - reasonable dynamic performance
- Fast enough sampling rate allows to regard the discrete PI controller as a (quasi-)continuous controller.
- High frequency behaviour not compensated (output filter resonance)

