

An Effective Theory for Higgs Compositeness

Jay Hubisz
Syracuse University
2/27/2011



WIP - Bellazzini, Csáki, JH, Serra, Terning

Perspectives on Higgs physics

By G. L. Kane

Why I would be very sad if a Higgs boson were discovered*†

Howard Georgi

Lyman Laboratory of Physics

Harvard University

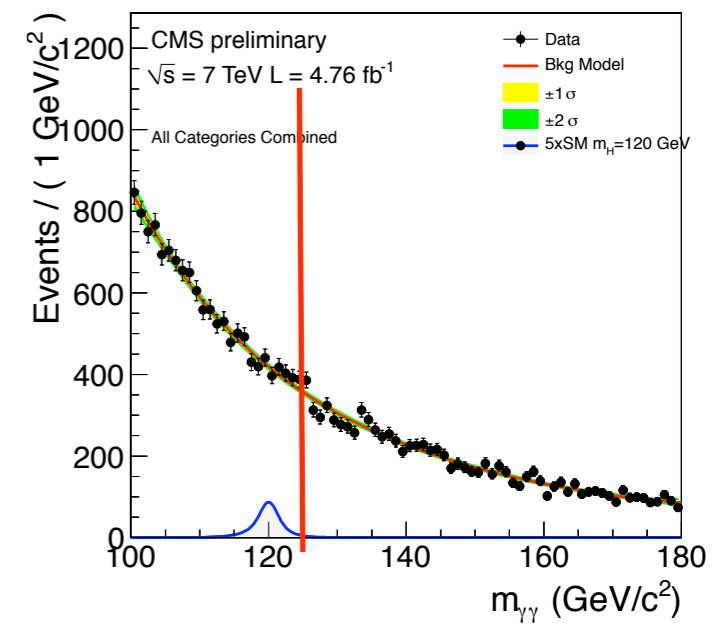
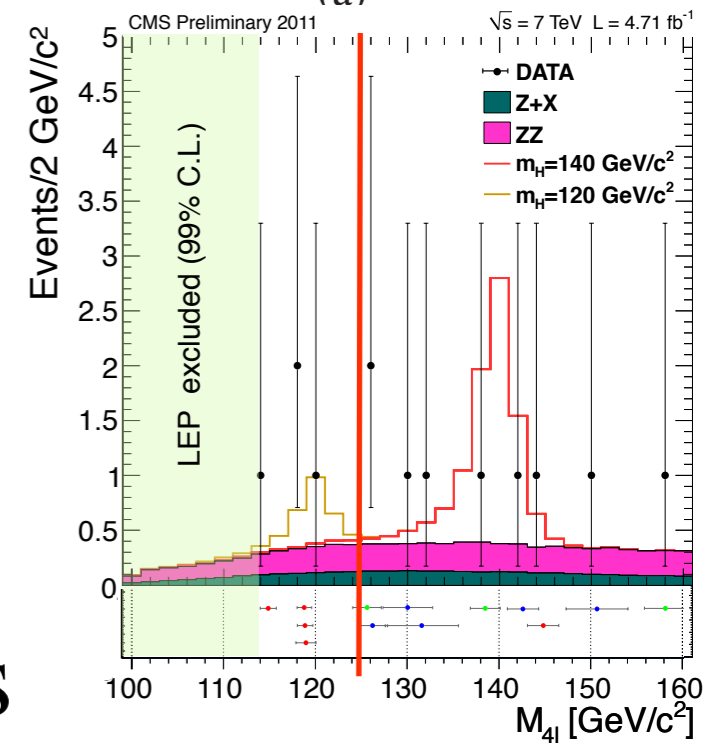
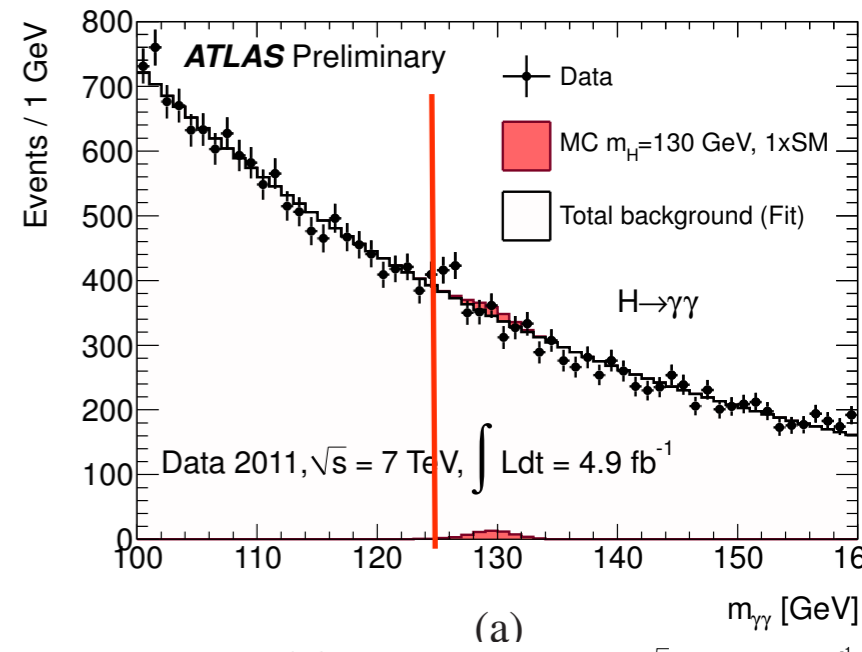
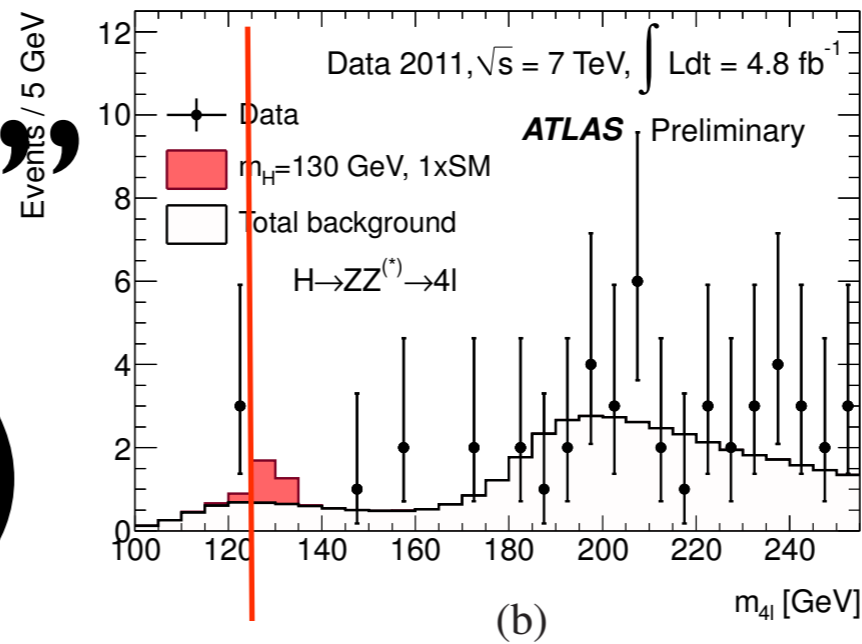
Cambridge, MA 02138

Abstract

I explain the difference between the Higgs mechanism and the Higgs, discuss various options for spontaneous $SU(2) \times U(1)$ symmetry breaking and quark and lepton mass generation, and speculate about chiral gauge theories.

The “Higgs” at 125(ish)

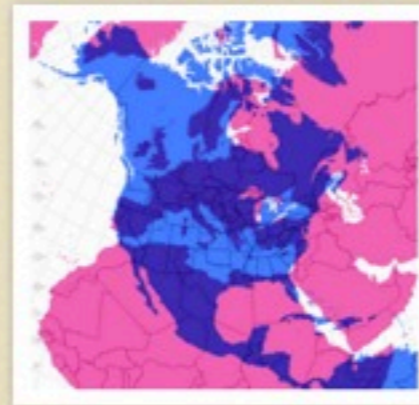
- ATLAS + CMS have excesses in $\gamma\gamma$
- Backed up by collections of 41 events
- Slight excesses in CMS low res. channels
- “Smells” right



Consistent with other fundamental laws:

Pauli's Other Exclusion Principle

As I am currently stretched between continents, I ponder over the differences between the US and Europe. Apart from the taste of food and the size of humans, there seems to be a fundamental difference at the level of particle physics. Let's have a closer look at the time and place of discoveries of elementary particles:



- Tau neutrino, 2000, Fermilab, United States
- Top quark, 1995, Fermilab, United States
- W and Z bosons, 1983, CERN, Switzerland
- Gluon, 1979, DESY, Germany
- Bottom quark, 1977, Fermilab, United States
- Tau, 1975, SLAC, United States
- Charm quark, 1974, SLAC/Brookhaven, United States
- Up, down, and strange quarks, 1968, SLAC, United States
- Muon neutrino, 1962, Brookhaven, United States
- Electron neutrino, 1956, Los Alamos, United States
- Muon, 1936, Caltech, United States
- Photon, 1905, Patent Office in Bern, Switzerland
- Electron...let's skip that one for simplicity...

This can be summarized as Pauli's other exclusion principle:

Fermions are discovered in the US, whereas bosons are discovered in Europe.

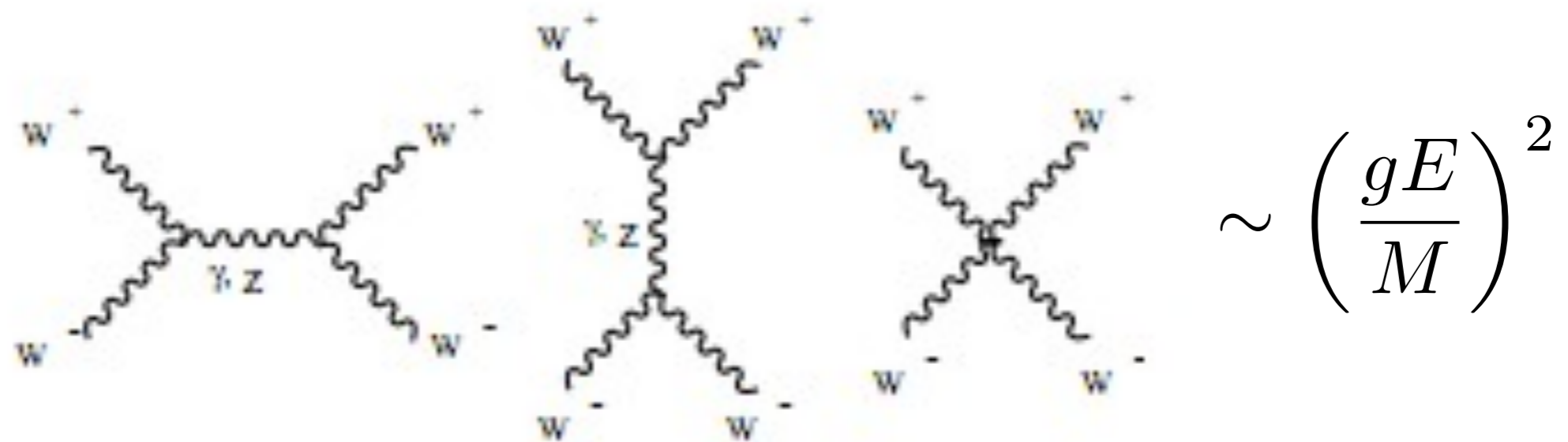
Resonaances - Falkowski

Naturalness and a Composite Higgs

- Higgs not necessarily a fundamental scalar
- composite at the TeV/few-TeV scale
- Composite models 'natural' in sense that the loops that correct the higgs mass are cut off at a much lower scale (little hierarchy often remains)
- models which combine these ideas address LH prob
 - Little Higgs, composite SUSY, ...
- motivates a simplified model approach to CH
 - what are generic signatures/constraints?

Unitarity

- The principle of unitarity in EWSB provides the strongest justification for the LHC program
- The Higgs (or cousins) had to be there



Amplitude grows with energy - non-perturbative for $E \gg M$

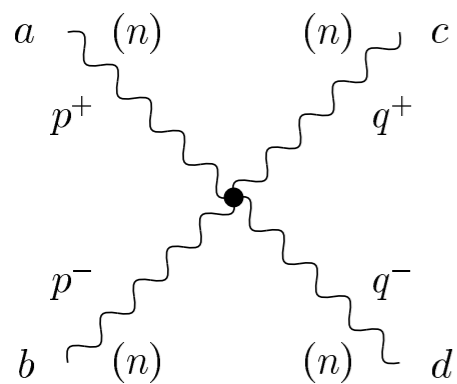
SM: Fixed by including higgs contributions
(gauge invariance forces a 'sum-rule')

Gaugephobic Higgs

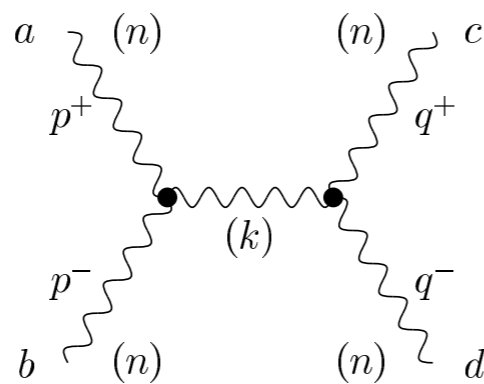
Limit of decoupled Higgs

gauge resonances terminate
growth of amplitudes via
KK-mode sum rule

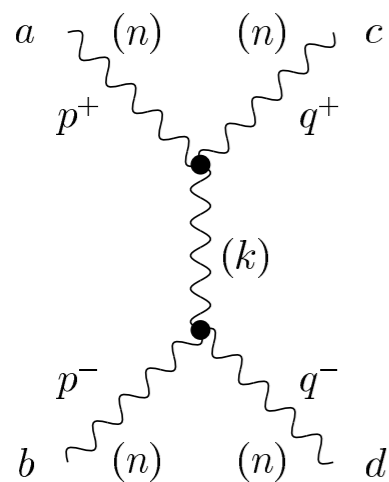
Unitarity with only vectors:



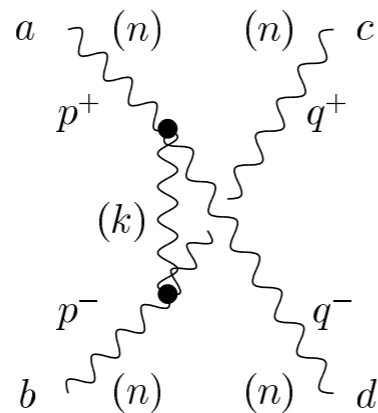
contact interaction



s channel exchange



t channel exchange



u channel exchange

$$\mathcal{A} = A^{(4)} \frac{E^4}{M_n^4} + A^{(2)} \frac{E^2}{M_n^2} + A^{(0)} + \mathcal{O}\left(\frac{M_n^2}{E^2}\right)$$

$$A^{(2)} = \frac{i}{M_n^2} \left(4g_{nnnn}M_n^2 - 3 \sum_k g_{nnk}^2 M_k^2 \right) (f^{ace} f^{bde} - \sin^2 \frac{\theta}{2} f^{abe} f^{cde})$$

$$g_{nnnn}M_n^2 = \frac{3}{4} \sum_k g_{nnk}^2 M_k^2$$

sum rule automatic
(5D gauge invariance)

review: Csaki, JH, Meade

Simplified model for LHC unitarity

WIP: Bellazzini, Csáki, JH, Serra, Terning

- Unitarity sum-rule only partially saturated by Higgs exchange diagrams - suppressed couplings
- one set of vector resonances (ρ 's) - completes saturation of the electroweak GB sum-rules
- non-linear realization of custodial coset:
 - $SU(2)_L \times SU(2)_R / SU(2)_C$ a-la hidden local symmetry
Cassalbuoni, Curtis, Dominici, Gatto '87
Falkowski, Grojean, Kaminska, Pokorski, Weiler '11
 - ρ 's come as triplet of $SU(2)_C$

The Goldstones

Symmetry spontaneously broken at $f = v_{ew}$

Element of coset G/H : $U(\Pi) = e^{i\Pi^{\hat{a}}T^{\hat{a}}}$

$$-iU^{-1}\partial_{\mu}U = \Pi_{\mu}^{\hat{a}}T^{\hat{a}} + E_{\mu}^aT^a \equiv \Pi_{\mu} + E_{\mu}$$

Under transformation g_0 in G :

$$\Pi_{\mu} \rightarrow h(\Pi, g_0)\Pi_{\mu}h^{-1}(\Pi, g_0)$$

$$E_{\mu} \rightarrow h(\Pi, g_0)E_{\mu}h^{-1}(\Pi, g_0) - ih(\Pi, g_0)\partial h^{-1}(\Pi, g_0)$$

Π_{μ} transforms linearly

E_{μ} transforms like gauge field

The Goldstones

Build action that is invariant under G:

$$\mathcal{L}_{\Pi}^{(2)} = \frac{f^2}{2} \text{Tr}[\Pi_{\mu}\Pi^{\mu}]$$

Goldstone kinetic terms

Add Higgs interactions (singlet couplings):

$$\mathcal{L}^{(h)} = \frac{1}{2}(\partial h)^2 + V(h) + \frac{f^2}{2} \left(2a_h \frac{h}{f} + b_h \frac{h^2}{f^2} \right) \text{Tr}[\Pi_{\mu}\Pi^{\mu}]$$

free parameters

a_h sets $h\Pi\Pi$ coupling - unitarity saturated for $a_h=1$

The ρ 's

With E_μ , can write down invariant action that includes additional gauge fields transforming under $SU(2)_c$

$$\mathcal{L}_\rho^{(2)} = -\frac{1}{4g_\rho^2} \rho_{\mu\nu}^a \rho_{\mu\nu}^a + \frac{a_\rho^2 f^2}{2} (\rho_\mu^a - E_\mu^a(\Pi))^2$$

free parameter

Generates a ρ mass: $m_\rho = a_\rho g_\rho f$

g_ρ sets self-interactions of ρ 's

a_ρ sets mass, interactions with goldstones, and adds goldstone self-interactions

Higgs couplings to ρ 's:

$$\mathcal{L}_{h\rho} = \frac{f^2}{2} \left(2c_h \frac{h}{f} + d_h \frac{h^2}{f^2} \right) (\rho_\mu^a - E_\mu^a)^2$$

SM Gauge Bosons

Gauging $SU(2)_L \times U(1)_Y$: gauge fields in Π_μ and E_μ .

ρ 's mix with SM gauge bosons:

$$W^\pm \longrightarrow W^\pm - \frac{g_2}{2g_\rho} \rho^\pm$$

$$Z \longrightarrow Z + \frac{g_1^2 - g_2^2}{2g_\rho \sqrt{g_1^2 + g_2^2}} \rho^0$$

$$A \longrightarrow A - \frac{e}{g_\rho} \rho^0$$

$$\rho^3 \longrightarrow \rho^0 + \frac{e}{g_\rho} A - \frac{g_1^2 - g_2^2}{2g_\rho \sqrt{g_1^2 + g_2^2}} Z$$

$SU(2)_c$ insures against large T-parameter

after diagonalization, have explicit ρVV couplings:

$$g_{WW\rho^0} = -\frac{g_2^2}{4g_\rho} = -\left(\frac{\sqrt{g_1^2 + g_2^2}}{4g_\rho}\right) g_{WWZ}^{SM}$$

$$g_{\rho WZ} = -\left(\frac{g_2}{4g_\rho}\right) \sqrt{g_1^2 + g_2^2} = -\left(\frac{g_1^2 + g_2^2}{4g_2 g_\rho}\right) g_{WWZ}^{SM}$$

participates in unitarization of VBS

Couplings to light fermions

mixing also generates couplings to non-composite fermions:

$$\mathcal{L}_{\rho\text{-currents}}^{(\text{element.})} = -\frac{g_2^2}{2\sqrt{2}g_\rho} \rho_\mu^\pm \bar{\psi} \gamma^\mu T^\mp \psi + \rho_\mu^0 \bar{\psi} \left[\frac{(g_1^2 - g_2^2)}{2g_\rho} T^3 - \frac{g_1^2}{2g_\rho} Q \right] \gamma^\mu \psi$$

light quark coupling - **Drell Yan production**

Couple with strength $g_{\rho f \bar{f}} = g_{\text{SM}} \left(a_\rho \frac{m_W}{m_\rho} \right)$

Heavy fermions may be composite

carry charge under $SU(2)_c$

couple strongly

The Model - Summary

We gauge unbroken global $SU(2)_c$

g_ρ is ρ 'gauge coupling' a_ρ fixes ρ mass

a_h controls suppression of higgs couplings

$$\begin{aligned}\mathcal{L} = & \frac{v^2}{2} (\Pi_\mu^{\hat{a}})^2 - \frac{1}{4} (\rho_{\mu\nu}^a)^2 + a_\rho^2 \frac{v^2}{2} (g_\rho \rho_\mu^a - E_\mu^a)^2 \\ & + \frac{1}{2} (\partial_\mu h)^2 + V(h) + \frac{v^2}{2} \left(2a_h \frac{h}{v} + b_h \frac{h^2}{v^2} \right) (\Pi_\mu^{\hat{a}})^2 + \frac{v^2}{2} \left(2c_h \frac{h}{v} + d_h \frac{h^2}{v^2} \right) (g_\rho \rho_\mu^a - E_\mu^a)^2 \\ & + O(p^4)\end{aligned}$$

Sufficient to consider Π scattering for unitarity
(goldstones eaten by W, Z)

Electroweak bosons mix with ρ 's
couple to SM gauge fields/fermions

Specific models predict values for some/all parameters

Unitarization

Couplings and masses must satisfy sum rules
to ensure perturbative W/Z scattering

$$\mathcal{M}(\pi^+\pi^- \rightarrow \pi^+\pi^-) = \frac{1}{32\pi} \frac{s}{f^2} (1 - a_h^2 - \hat{a}_\rho^2) - \frac{1}{48\pi f^2} [m_\rho^2 \hat{a}_\rho^2 (1 - 2 \log[s/m_\rho^2]) + 3m_h a_h^2 (2m_h - i\Gamma_h)]$$

$$\hat{a}_\rho^2 \equiv \frac{3}{4} a_\rho^2 \quad \text{Sum Rule: } a_h^2 + \frac{3}{4} a_\rho^2 = 1$$

Log growth remains

We limit m_ρ by requiring perturbative scattering up
to a few TeV (LHC unitarity)

include inelastic channels

Parameters

Unitarity sum-rule fixes a_ρ in terms of a_h

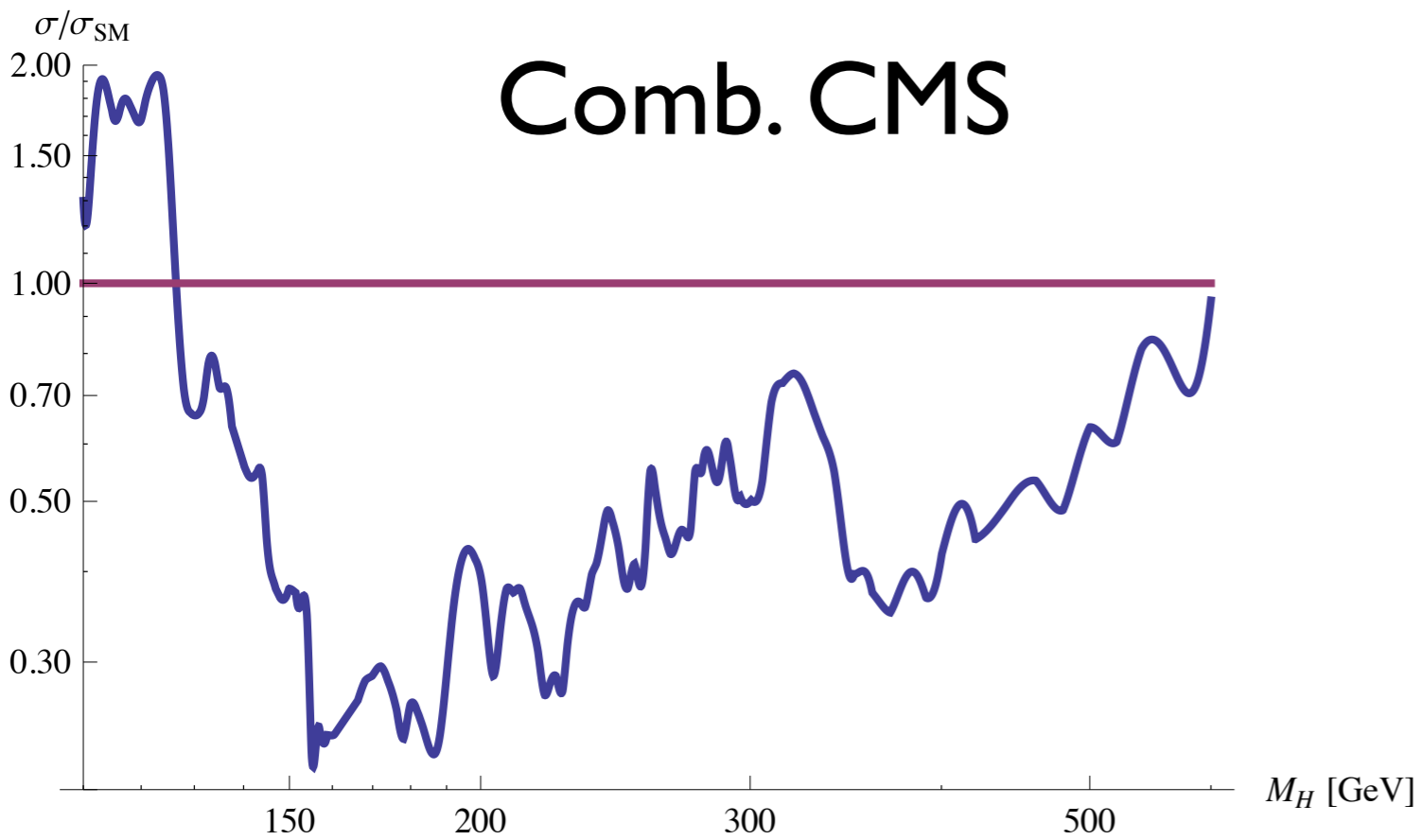
VB Mass matrix set by g_ρ , a_ρ , and $f=246$ GeV

Mixing with SM gauge fields determines most interesting
phenomenology

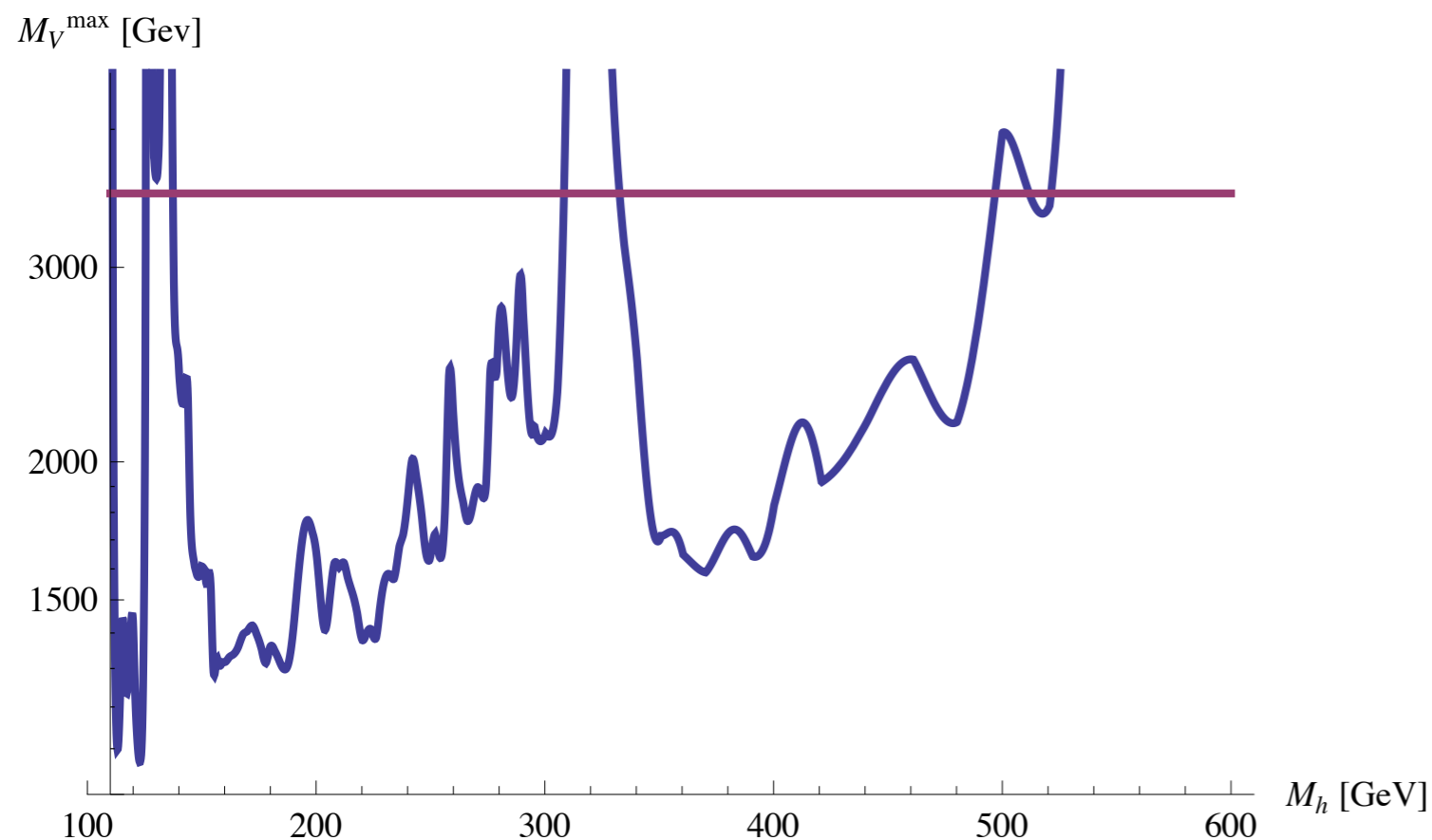
effectively have a 2-parameter model

We parameterize in terms of a_h and m_ρ

Turn that Higgs bound up-side down!



Exercise:
Higgs is at mass m_H , but
with suppressed overall
couplings



Saturate s-growth
sum-rule

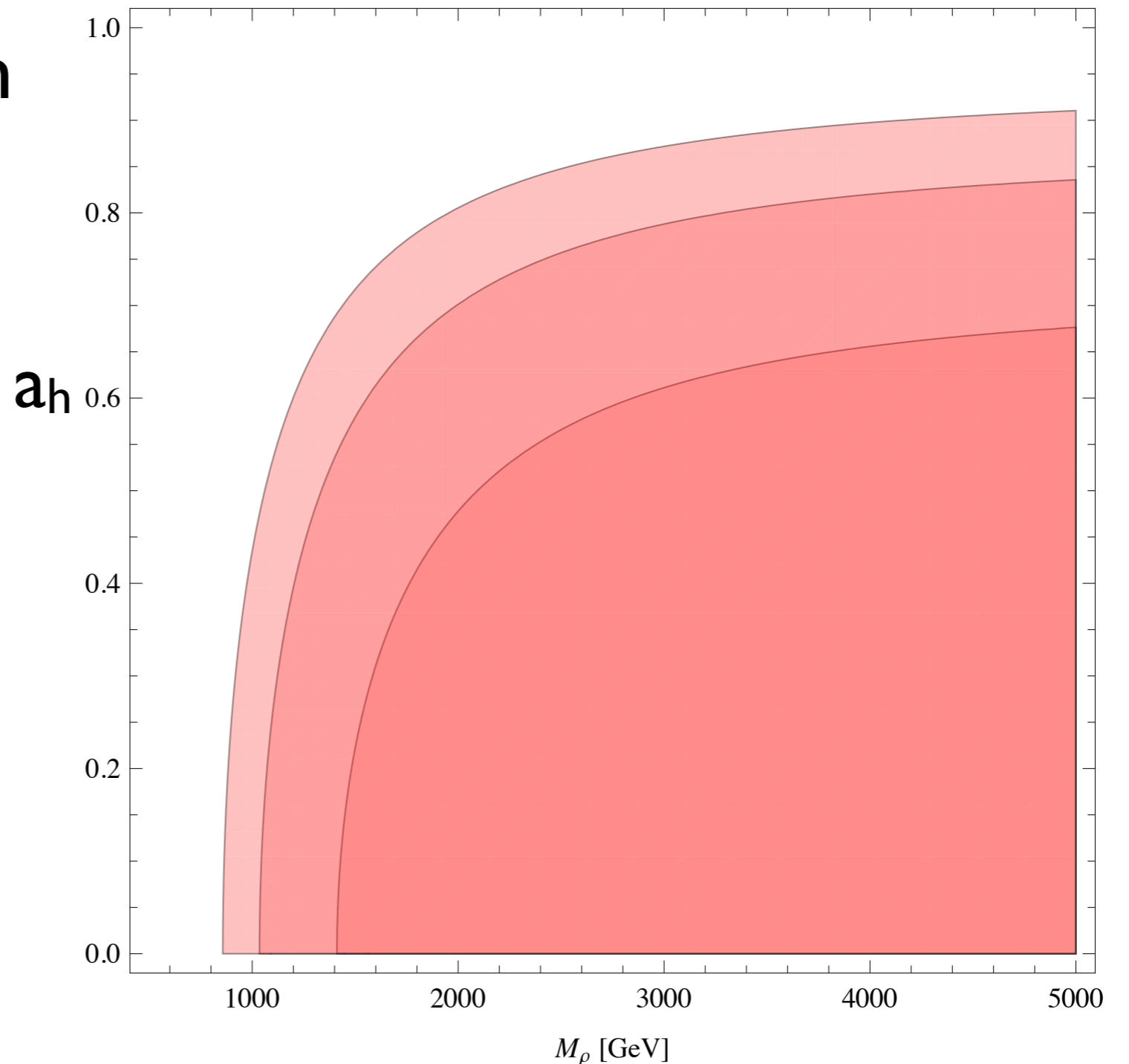
What is max allowed ρ
mass?

The unitarity constraint

$m_H = 125 \text{ GeV}$ $\Lambda = 2.5\text{-}5 \text{ TeV}$

Pink regions forbidden
for different values of
effective cutoff

As Higgs couplings
reduced, ρ 's must
come in earlier to
unitarize scattering



Vector Production

- Vector Boson Fusion
 - Pro: model independent (unitarity)
 - Con: cross section small, signal challenging
- Drell-Yan
 - most models have mixing with SM W 's, Z
 - coupling to light quarks (but small)
 - Pro: potentially large (enough) σ
 - Con: model dependent production

Vector decays

- The ρ 's are composite strongly interacting states
- prefer to decay to other composites
- massive degrees of freedom typically have larger degrees of compositeness

$$\begin{array}{ll} \rho^0 & \rightarrow W^+W^- \\ & \rightarrow \bar{t}t \\ & \rightarrow \bar{b}b \end{array} \quad \begin{array}{ll} \rho^\pm & \rightarrow W^\pm Z \\ & \rightarrow \bar{b}t(\bar{t}b) \end{array}$$

decays to light fermions typically suppressed

decays to 3rd gen fermions present challenging final states

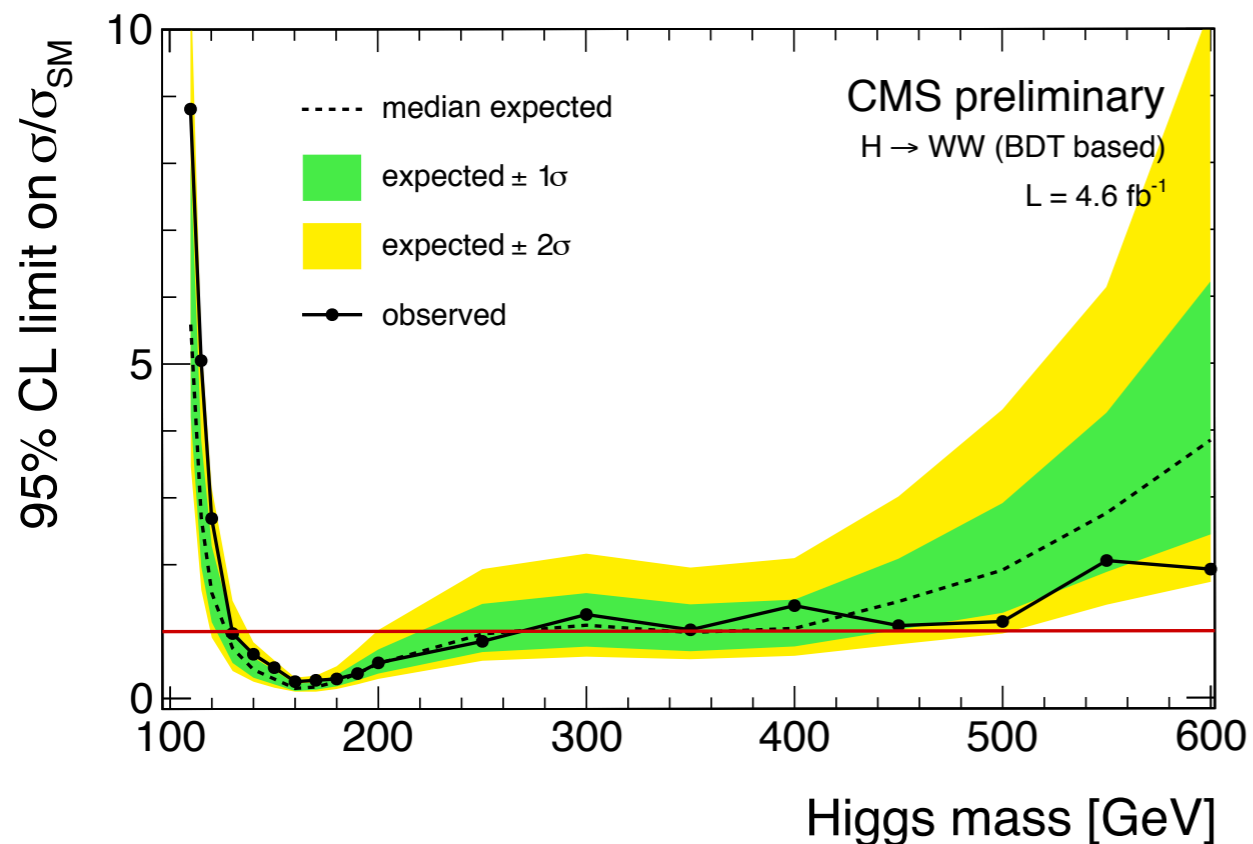
resonances in di-boson spectrum (leptonic) best bet

Direct Bounds on new resonances

Higgs search

$$\rho^0 \rightarrow W^+ W^-$$

$l\nu l\nu$

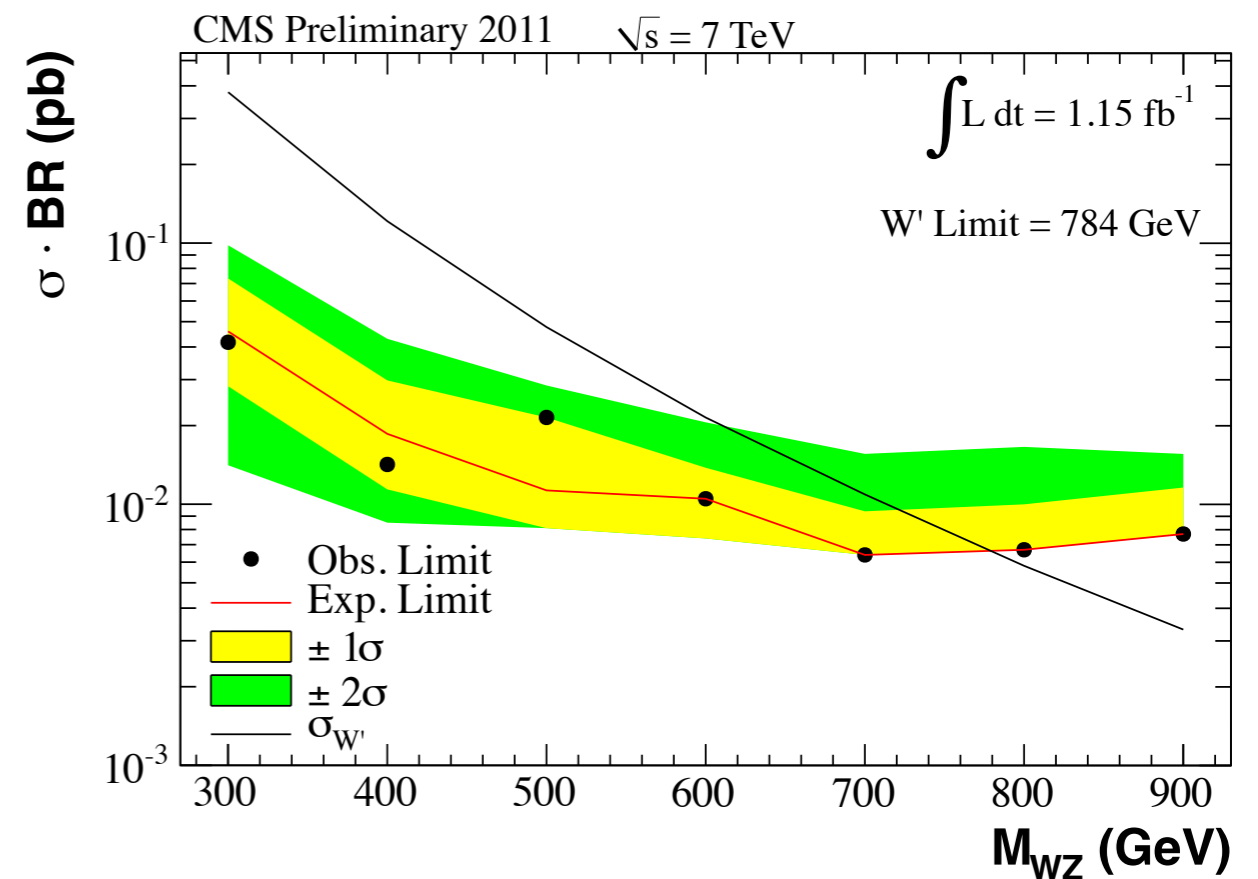


CMS-PAS-HIG-11-024

Dedicated di-boson

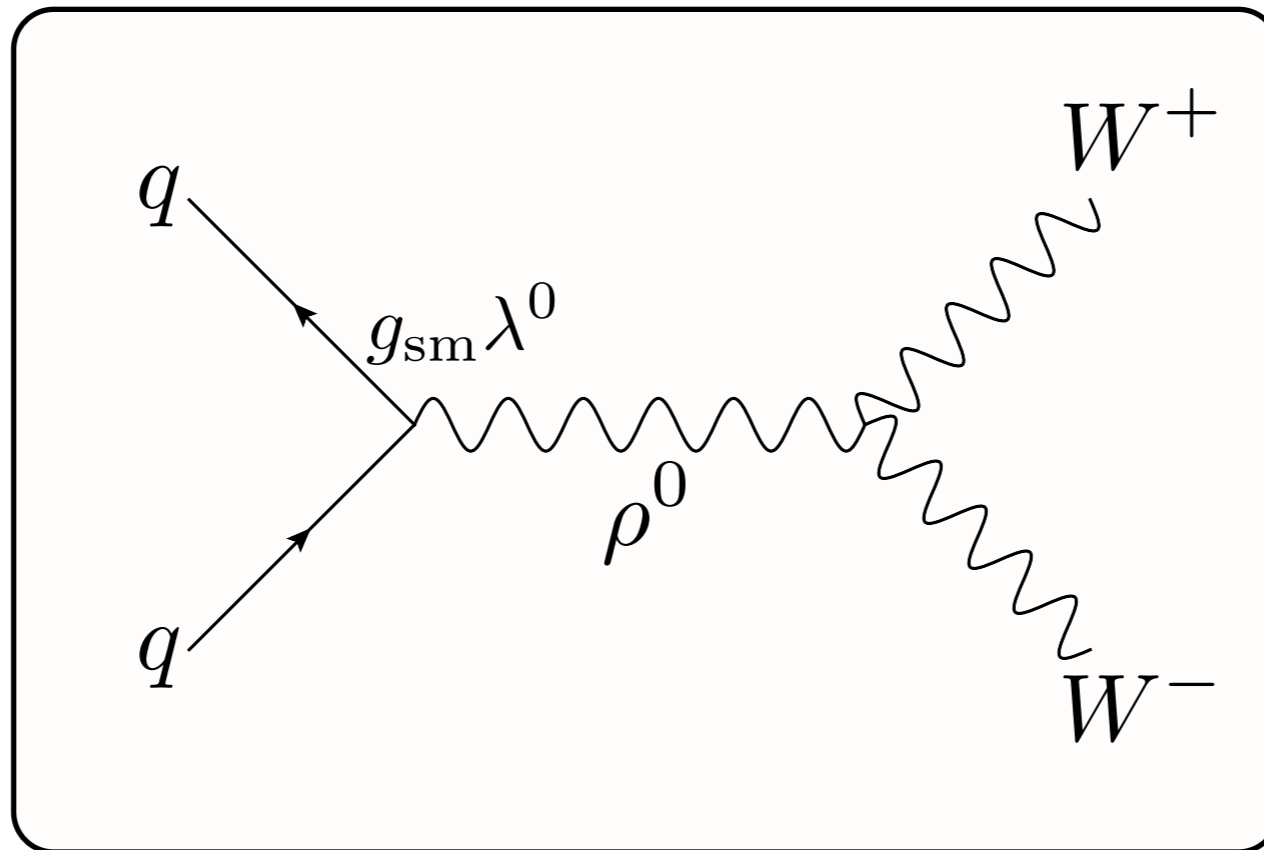
$$\rho^\pm \rightarrow W^\pm Z$$

$3l+\nu$



EXO-11-041-pas

Modeling the ρ^0

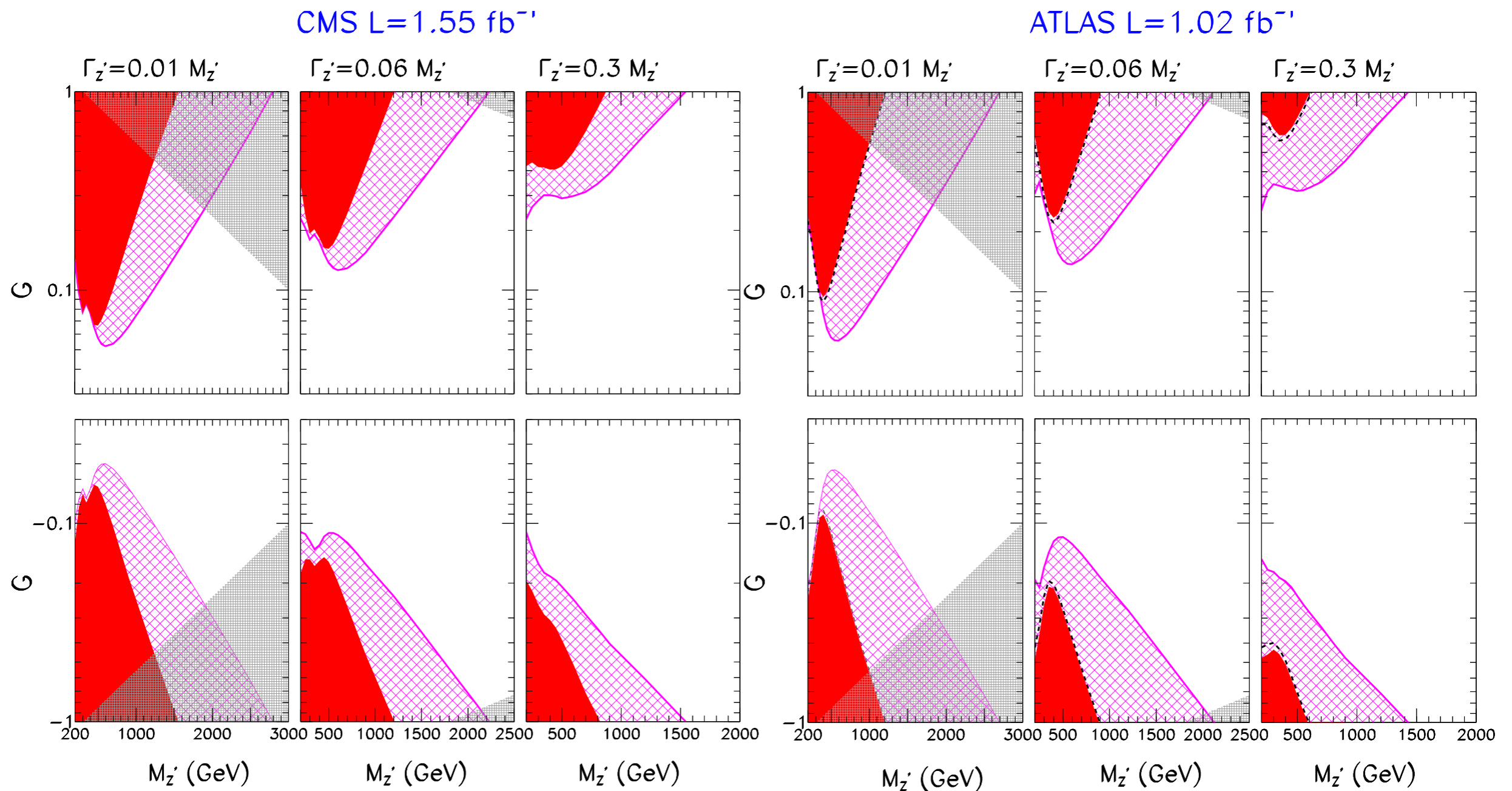


Z' with suppressed coupling to light quarks

High mass Higgs search restricts values of $\lambda^2 \text{Br}(\rho^0 \rightarrow WW)$

Seems hard - Higgs search is very optimized for SM

Recent Bounds on Z' bosons

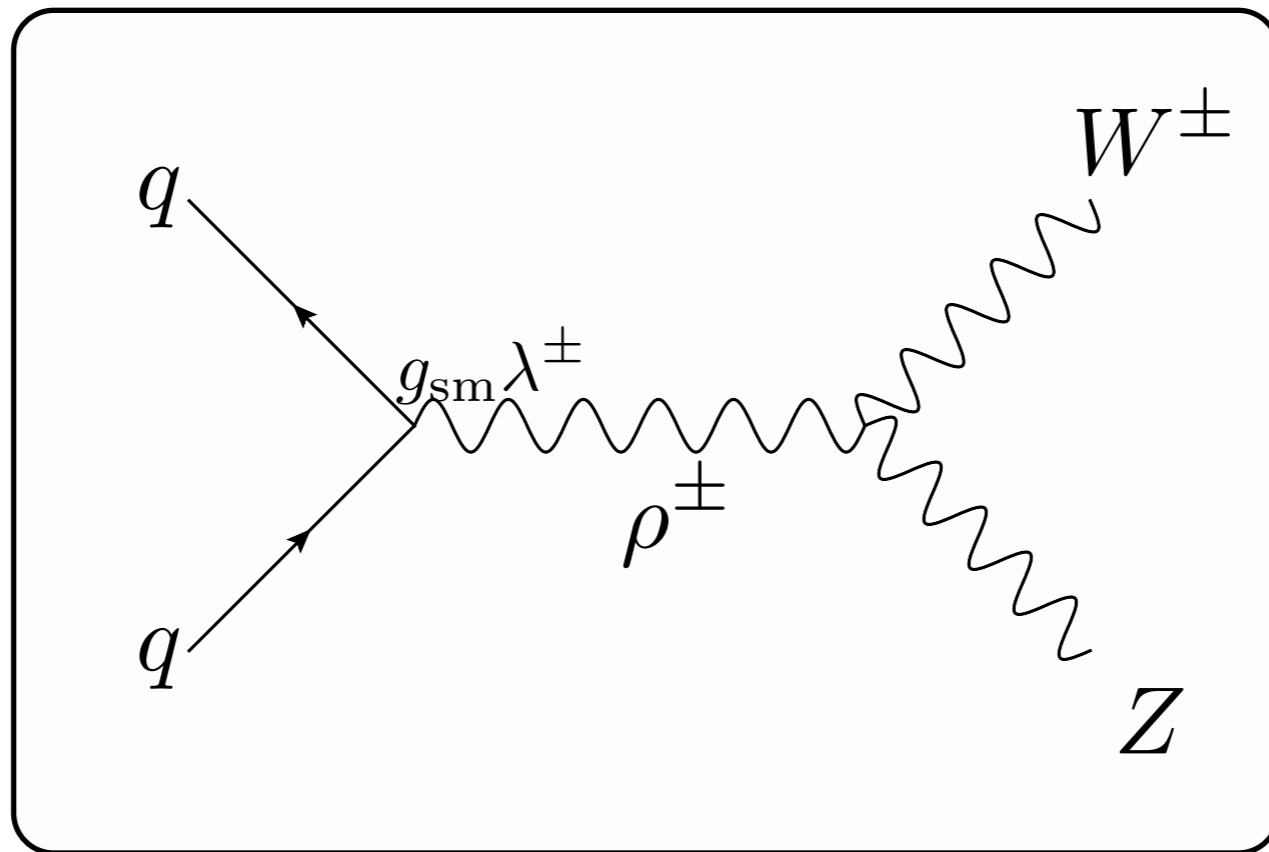


$$G = \left(\frac{g_{Z'q\bar{q}}}{g_{Zq\bar{q}}} \right) \left(\frac{g_{Z'WW}}{g_{Z'WW_{max}}} \right)$$

O.J.P. Eboli, J. Gonzalez-Fraile, M.C. Gonzalez-Garcia.

Really requires dedicated di-boson resonance search

Modeling charged ρ 's

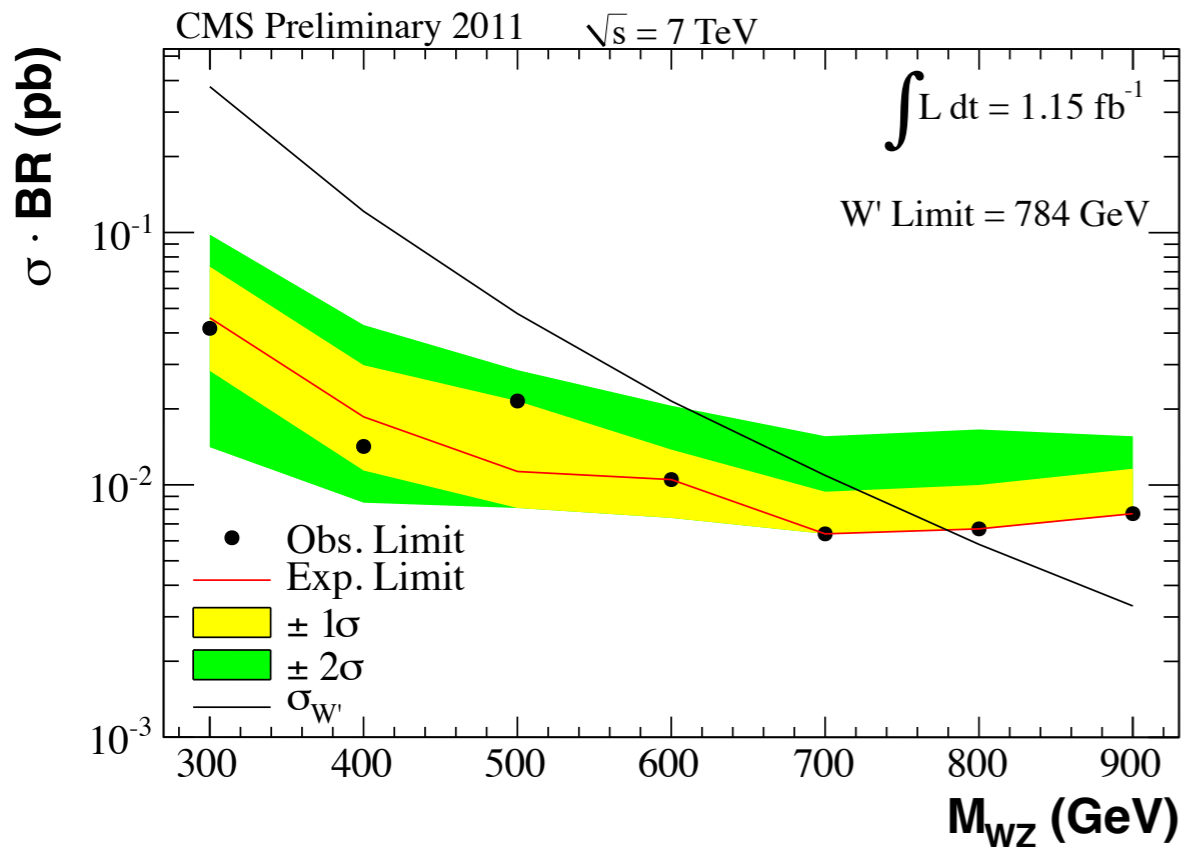


W' with suppressed coupling to fermions

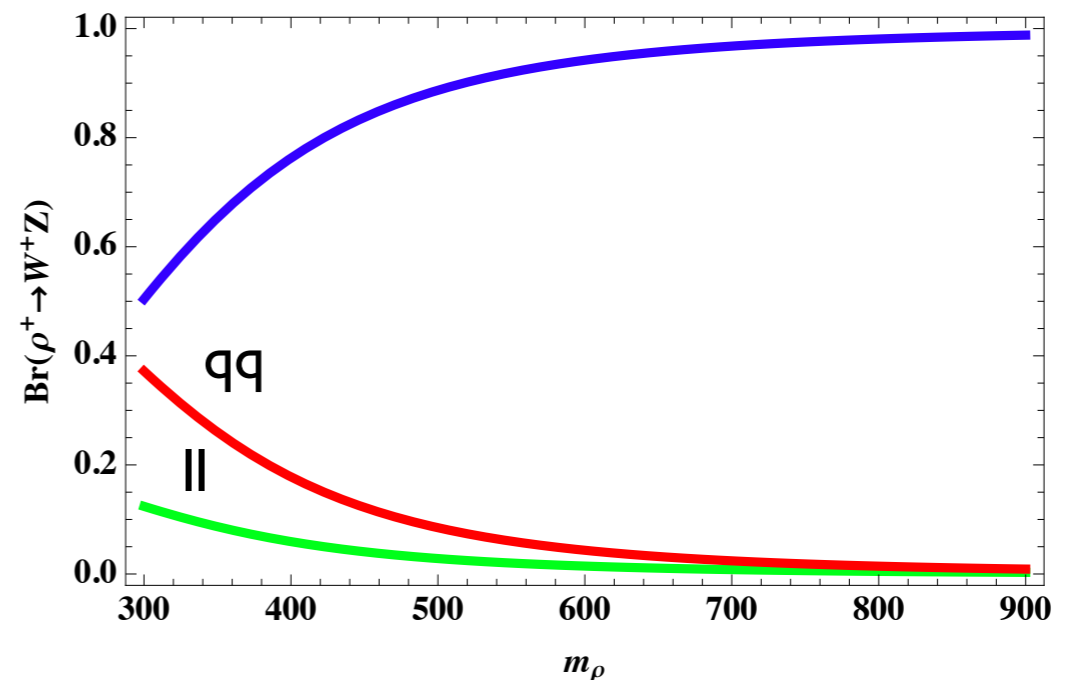
Search for W' /techni-rho limits $\lambda^2 \text{Br}(\rho^0 \rightarrow WW)$

Limits on charged ρ 's

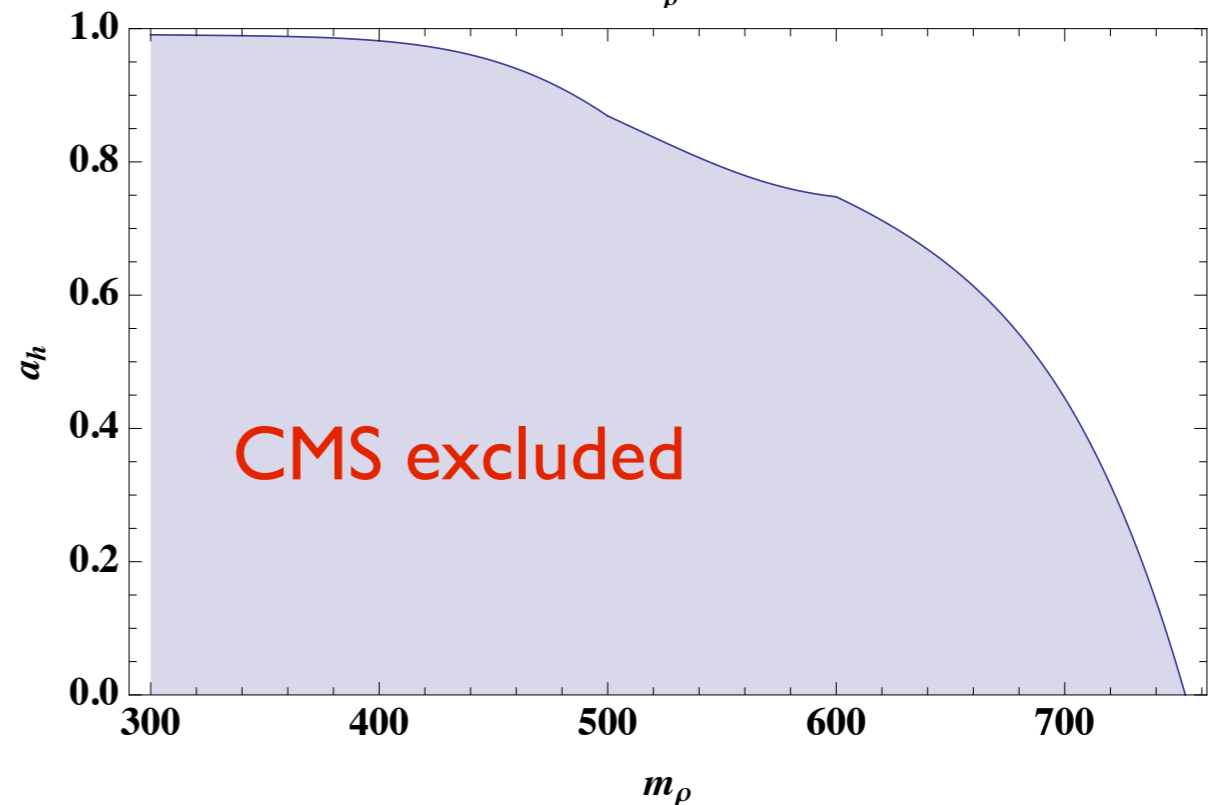
Implemented model in Madgraph



Calculate $\sigma^* \text{Br}$ in terms of a_h and m_ρ



mixing (coupling to quarks)
increases with a_ρ

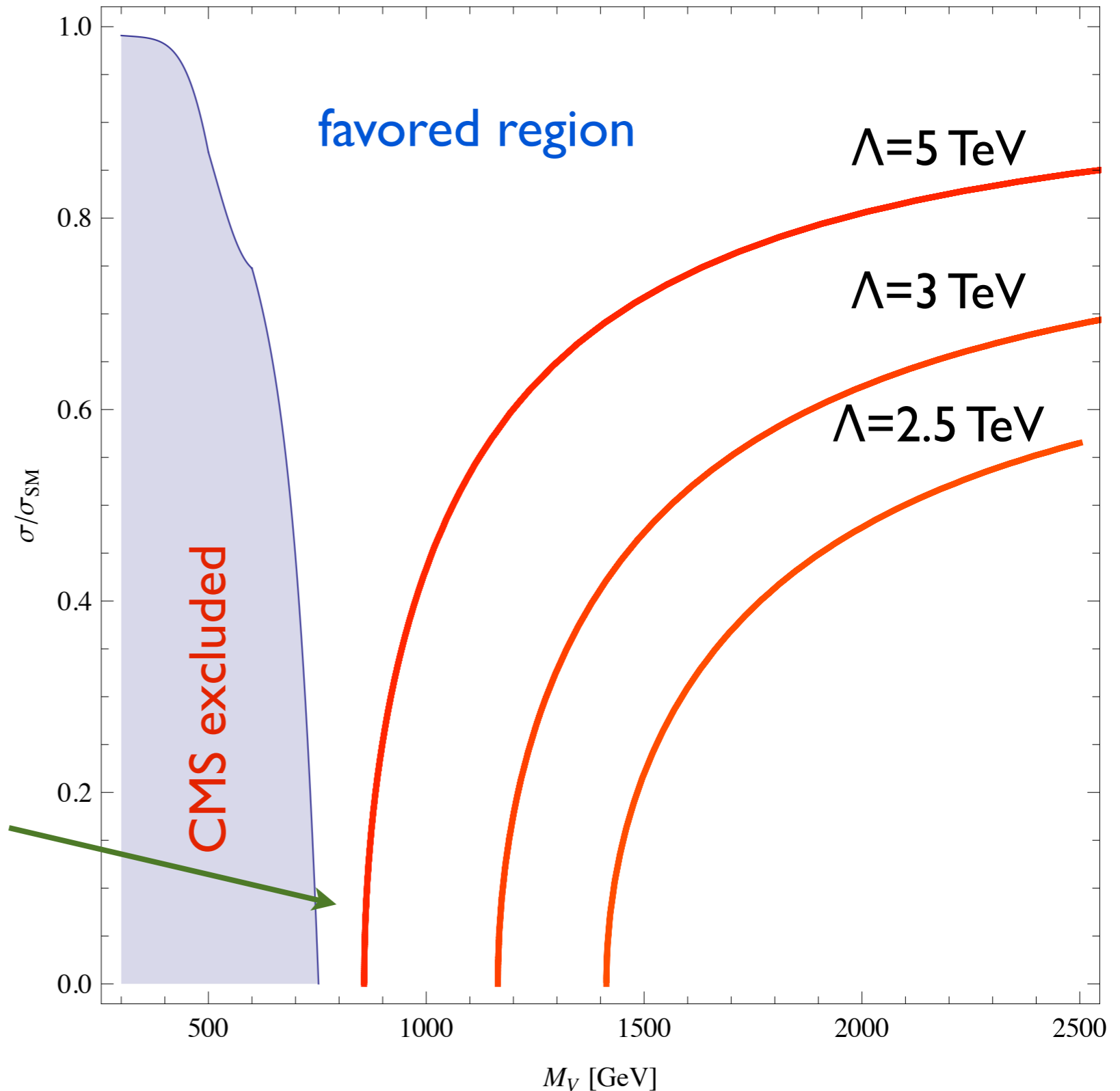


Combining limits

Sum rule enforced: $a_h^2 + 3/4 a_\rho^2 = 1$ $m_h = 125$ GeV

Direct limits from below
Theory limits from above

Rather tight for
gaugephobic scenarios



Higgs to $\gamma\gamma$ in composite models

- Higgs couplings in composite models are modified

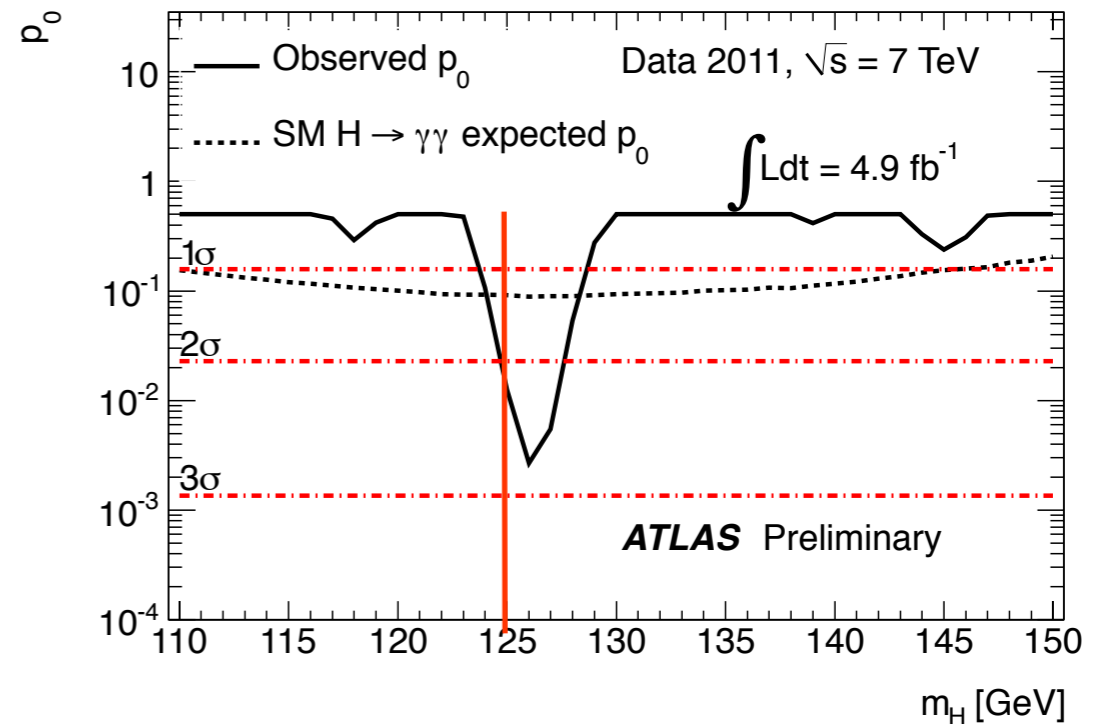
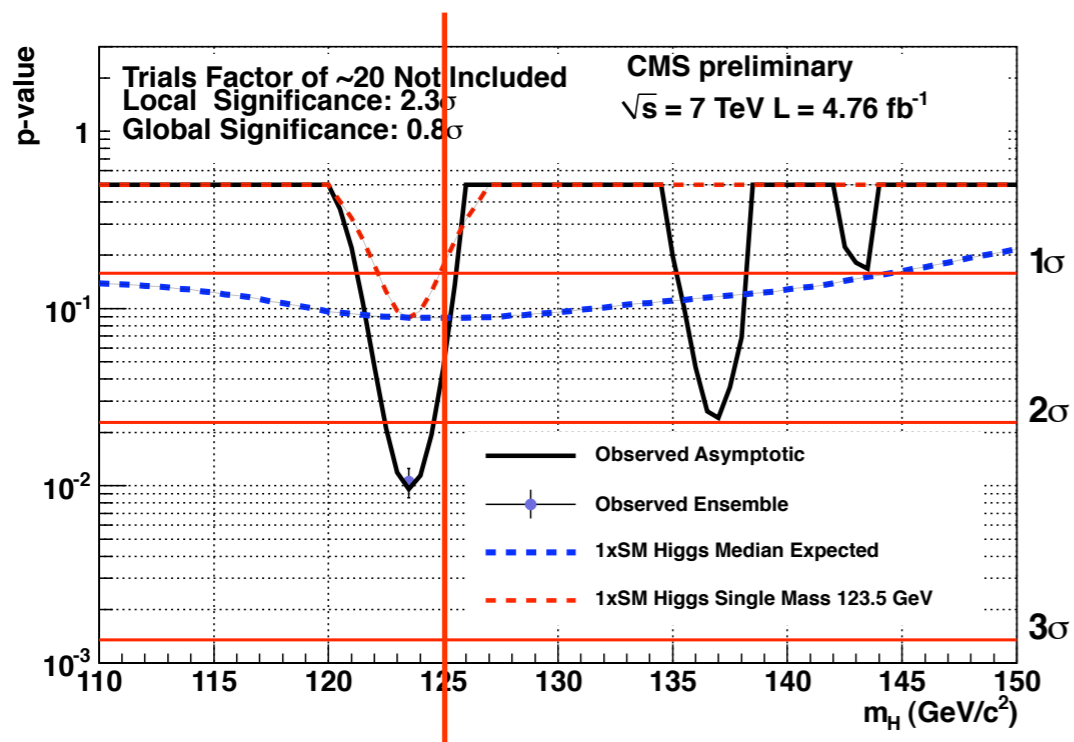
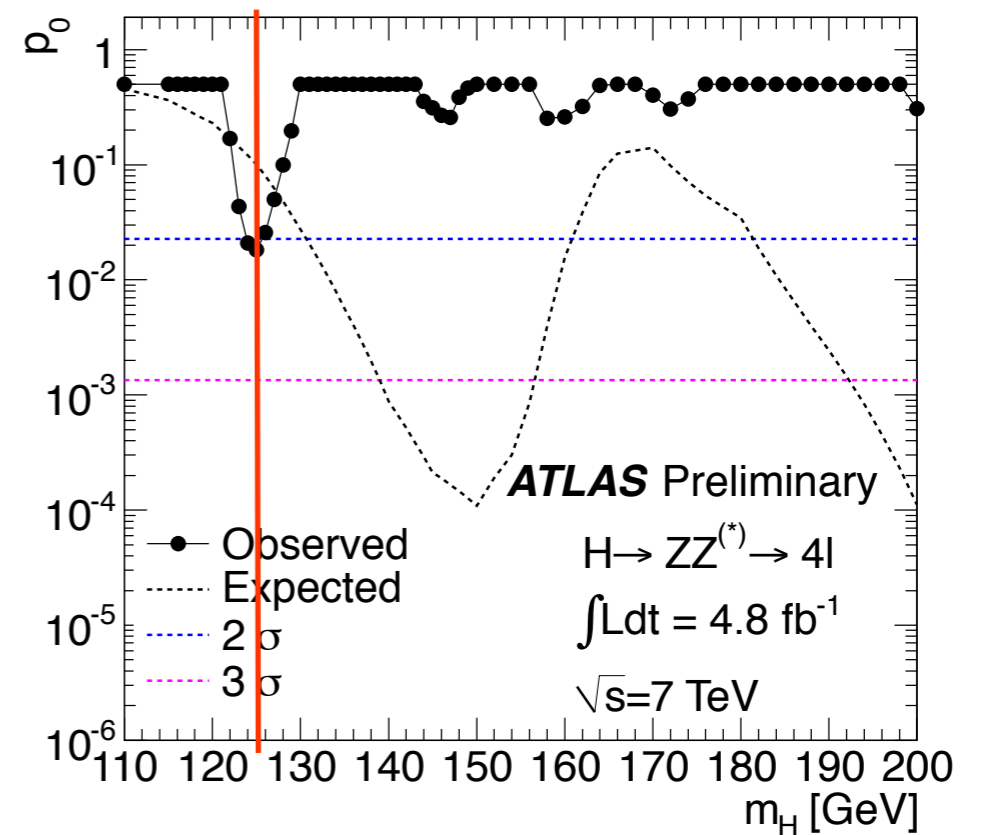
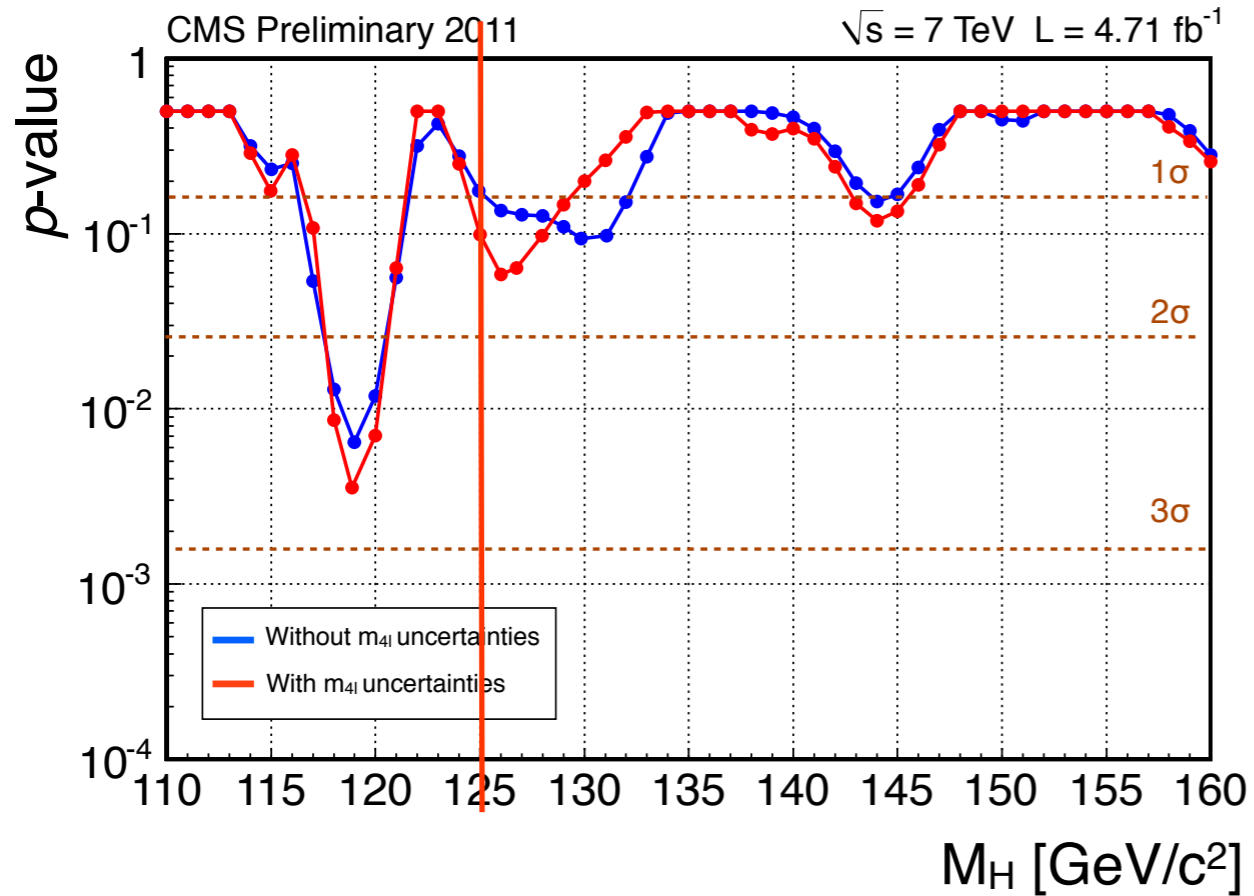
$$\lambda_i = \lambda_i^{\text{SM}} \left(1 + c \left(\frac{v}{f} \right)^2 \right)$$

- f is related to scale of compositeness
 - decay constant in higgs as PGB
- Of primary interest are hWW , htt , hbb couplings

Unitarity arguments

- in composite models, higgs couplings are generally suppressed
- otherwise sum rules supersaturated
- hard to get negative contribution
 - exception: Falkowski, Rychkov, Urbano (2012)
- best bet for increase in signal is decrease in hbb coupling, or new charged fields

Big Higgs



getting lucky, or $\sigma \times \text{Br}$ is about $2 \times \text{SM}$

Enhancement in $\gamma\gamma$

- Charged ρ 's may contribute in $h\gamma\gamma$ triangle

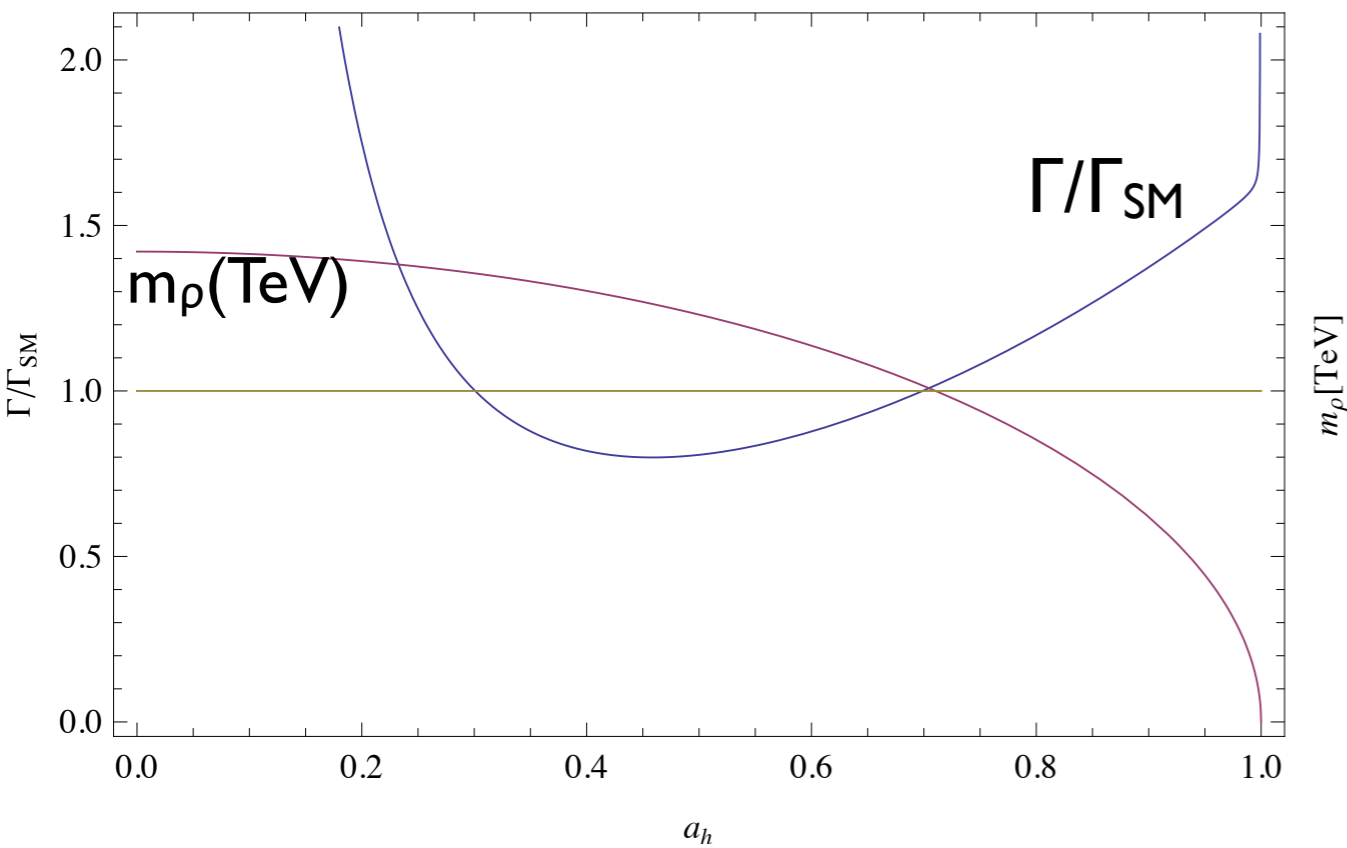
$$\begin{aligned}\mathcal{L} &= \frac{v^2}{2}(\Pi_{\mu}^{\hat{a}})^2 - \frac{1}{4}(\rho_{\mu\nu}^a)^2 + a_{\rho}^2 \frac{v^2}{2} (g_{\rho}\rho_{\mu}^a - E_{\mu}^a)^2 \\ &+ \frac{1}{2}(\partial_{\mu}h)^2 + V(h) + \frac{v^2}{2} \left(2a_h \frac{h}{v} + b_h \frac{h^2}{v^2} \right) (\Pi_{\mu}^{\hat{a}})^2 + \frac{v^2}{2} \left(2c_h \frac{h}{v} + d_h \frac{h^2}{v^2} \right) (g_{\rho}\rho_{\mu}^a - E_{\mu}^a)^2 \\ &+ O(p^4)\end{aligned}$$

This coupling is arb. from perspective of low energy EFT

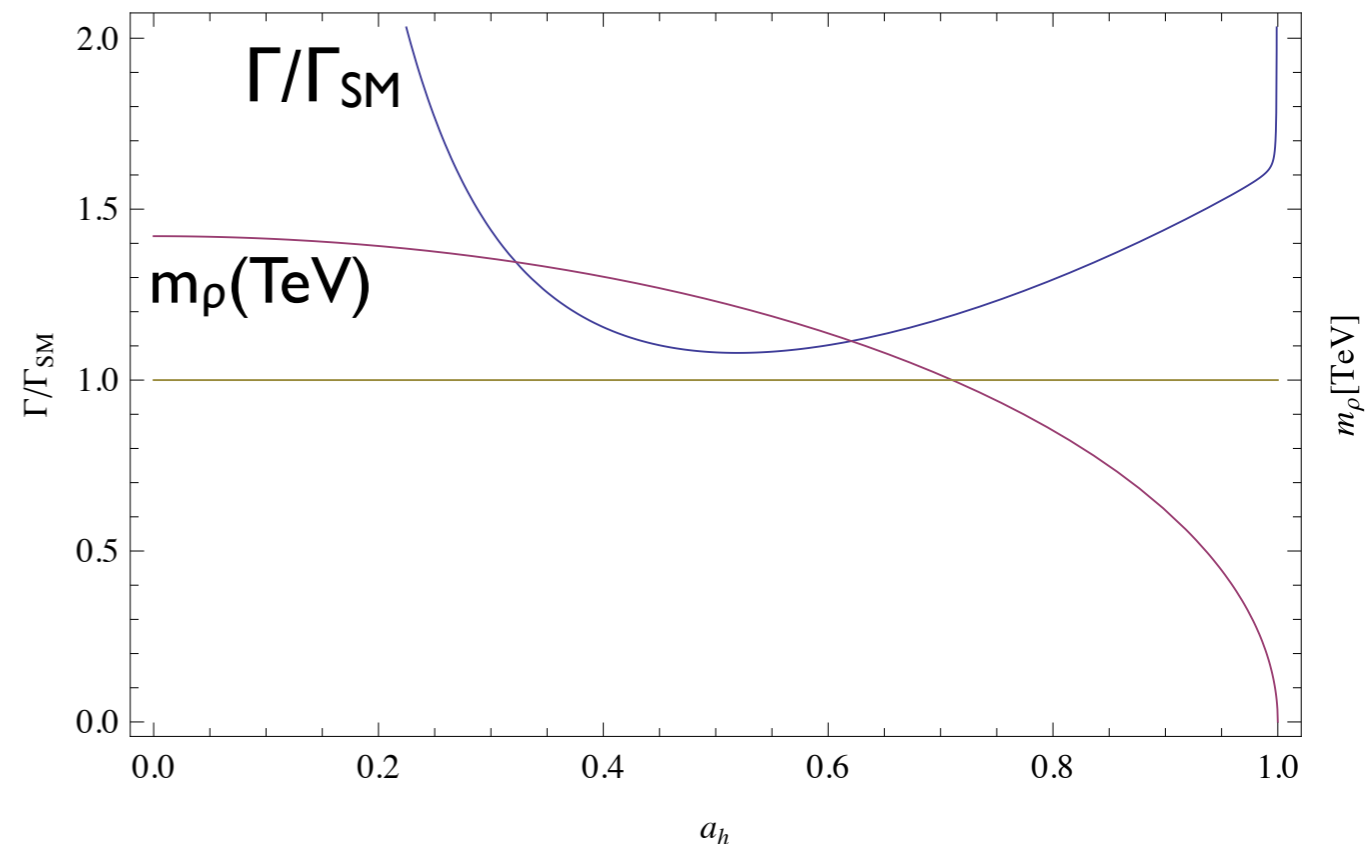
Vanishes in Higgs as PGB

Can compensate for reduction in gg coupling common in composite models

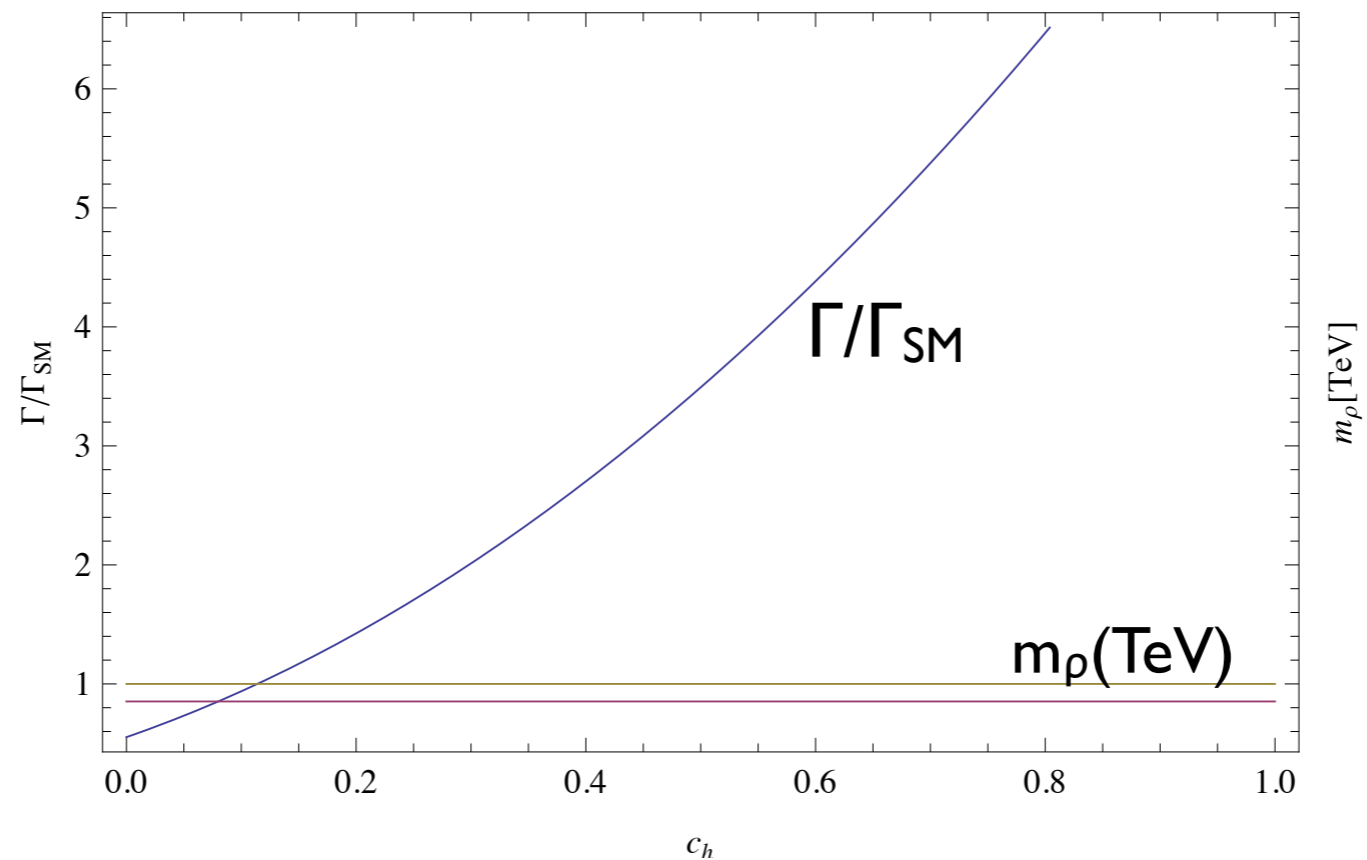
$$3/4 a_\rho^2 + a_h^2 = 1; \quad a_\rho^2 = 4 a_h c_h$$



$$a_t = a_h; \quad 3/4 a_\rho^2 + a_h^2 = 1; \quad a_\rho^2 = 4 a_h c_h$$



$$3/4 a_\rho^2 + a_h^2 = 1;$$



Can obtain enhancements in the $h \rightarrow \gamma\gamma$ signal

Conclusions

- A simplified model approach to Higgs compositeness
 - new VB's in representation of $SU(2)_c$
- new vector masses bounded from above (unitarity) and below (LHC)
- Can manage increase in h signal, even with suppressed couplings (new triangle diagrams)
- Upcoming experimental searches for di-boson resonances will be extremely valuable