

**PECCEI-QUINN  
NMSSM IN THE  
LIGHT OF 125 GEV  
HIGGS**

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**WORK IN PROGRESS**

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# OUTLINE

- **MOTIVATION**
- **PQ-NMSSM AND PHENOMENOLOGY**
- **COLLIDER PERSPECTIVE**
- **SUMMARY**



# PECCEI-QUINN SYMMETRY

U(1) ANOMALOUS GLOBAL SYMMETRY THAT GIVES THE MOST PLAUSIBLE SOLUTION OF **STRONG CP PROBLEM**.

IN QCD

$$\mathcal{L}_\theta = \theta \frac{g^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{\mu\nu a} \longrightarrow |D_n| \lesssim 10^{-24} \text{ cm} \quad \Rightarrow \quad |\theta| \lesssim 10^{-9}$$

ANOMALY OF U(1)<sub>PQ</sub> GENERATES  $aG\tilde{G}$  TERM AND

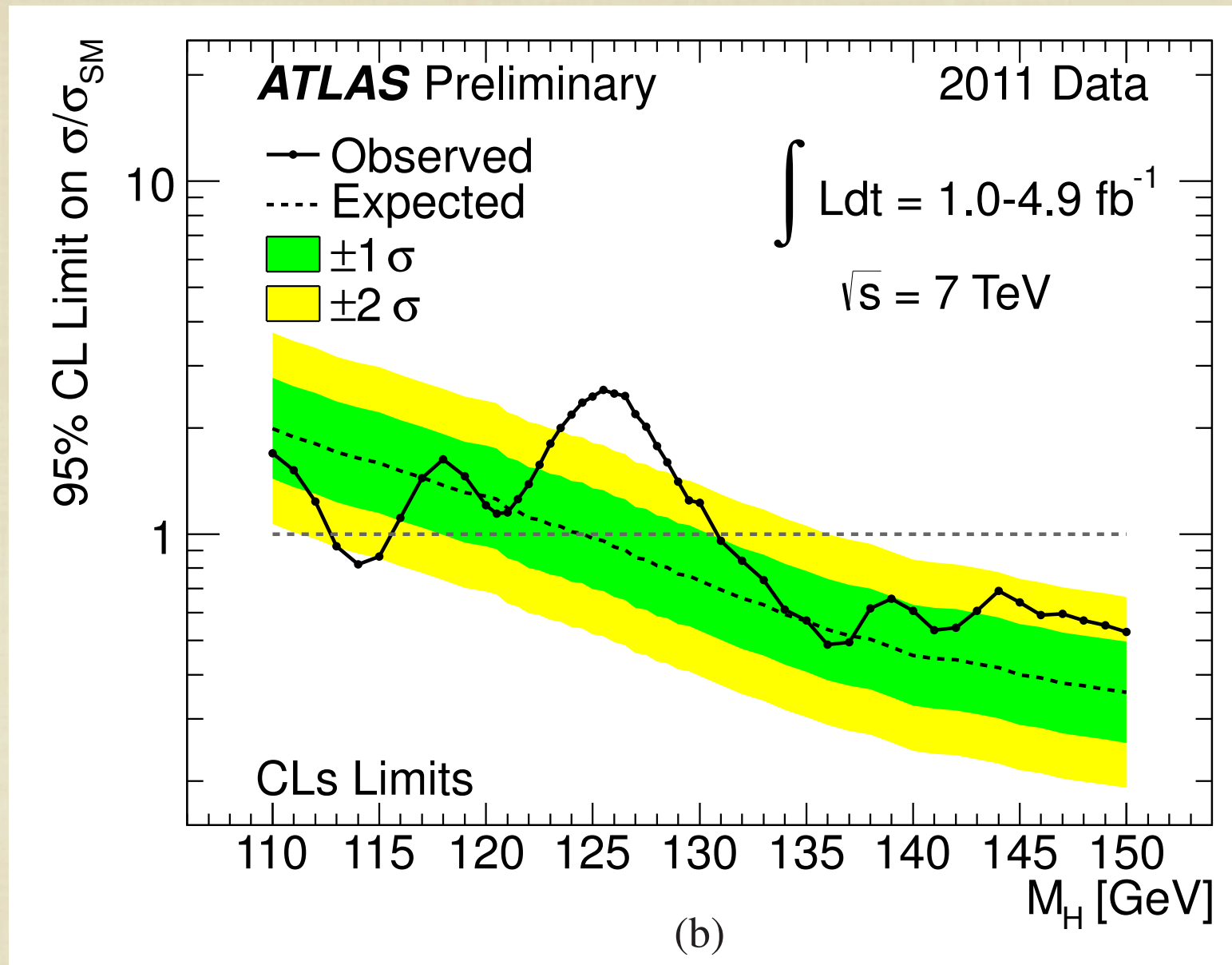
$$-\frac{g^2}{32\pi^2} \left( \theta - \frac{a}{f_a} \right) G\tilde{G} \longrightarrow \bar{\theta} \equiv \theta - \frac{a}{f_a}$$

$$E(\theta) = \langle \theta | H | \theta \rangle = -|K|^2 \cos \theta$$

VAFA-WITTEN SHOWED THAT ENERGY MINIMUM IS ALWAYS AT  $\langle \bar{\theta} \rangle = 0$ .

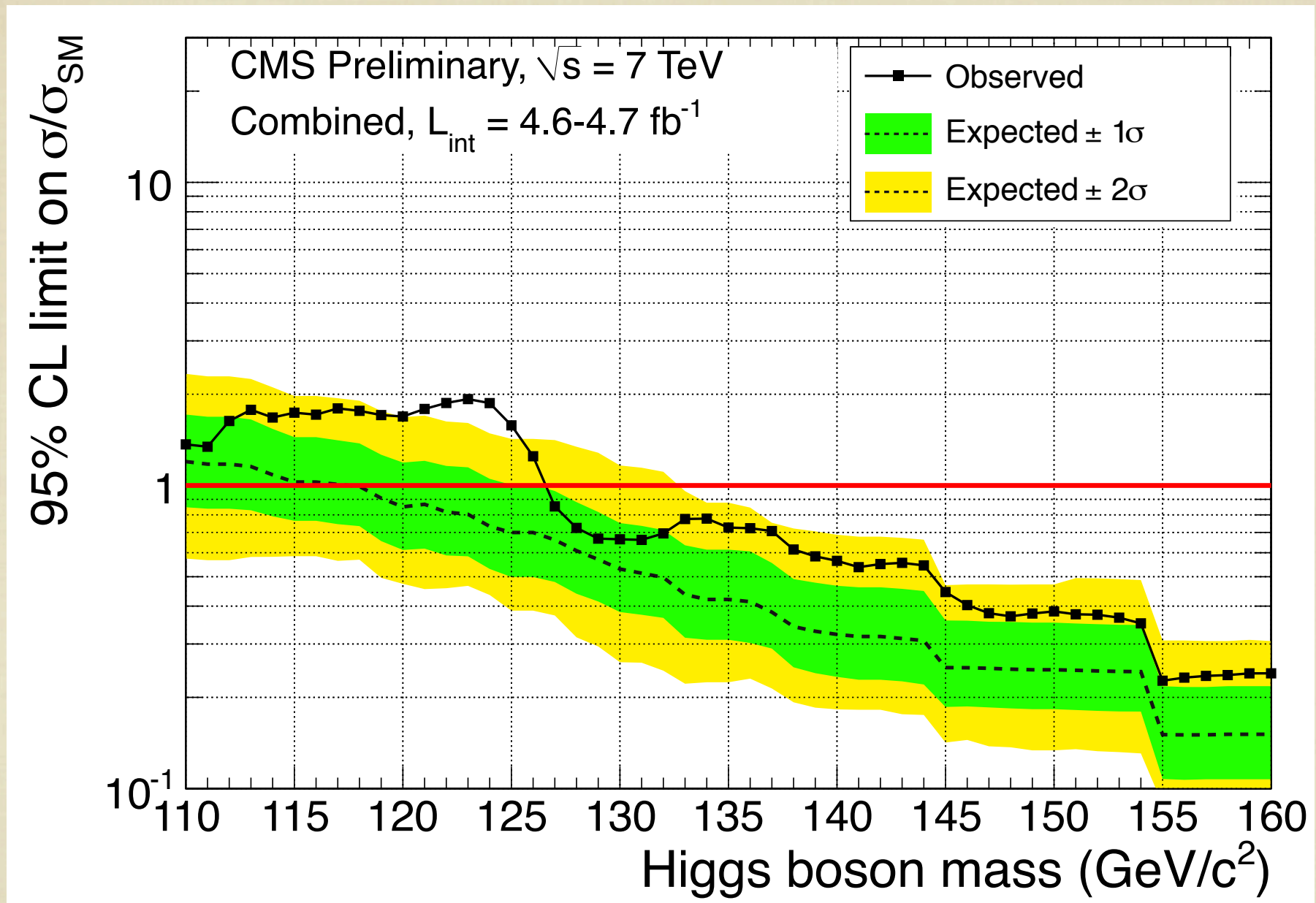
Phys.Rev.Lett. 53 (1984) 535

# 125 GEV HIGGS AT THE LHC





# 125 GEV HIGGS AT THE LHC



# 125 GEV HIGGS IN MSSM

IN MSSM, TREE-LEVEL HIGGS MASS IS BOUNDED FROM ABOVE BY  $M_Z$ . WE NEED RADIATIVE CORRECTIONS...

$$m_h^2 = M_Z^2 \cos 2\beta + \frac{3G_F m_t^4}{\sqrt{2}\pi^2} \left\{ \log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right\} + \dots$$

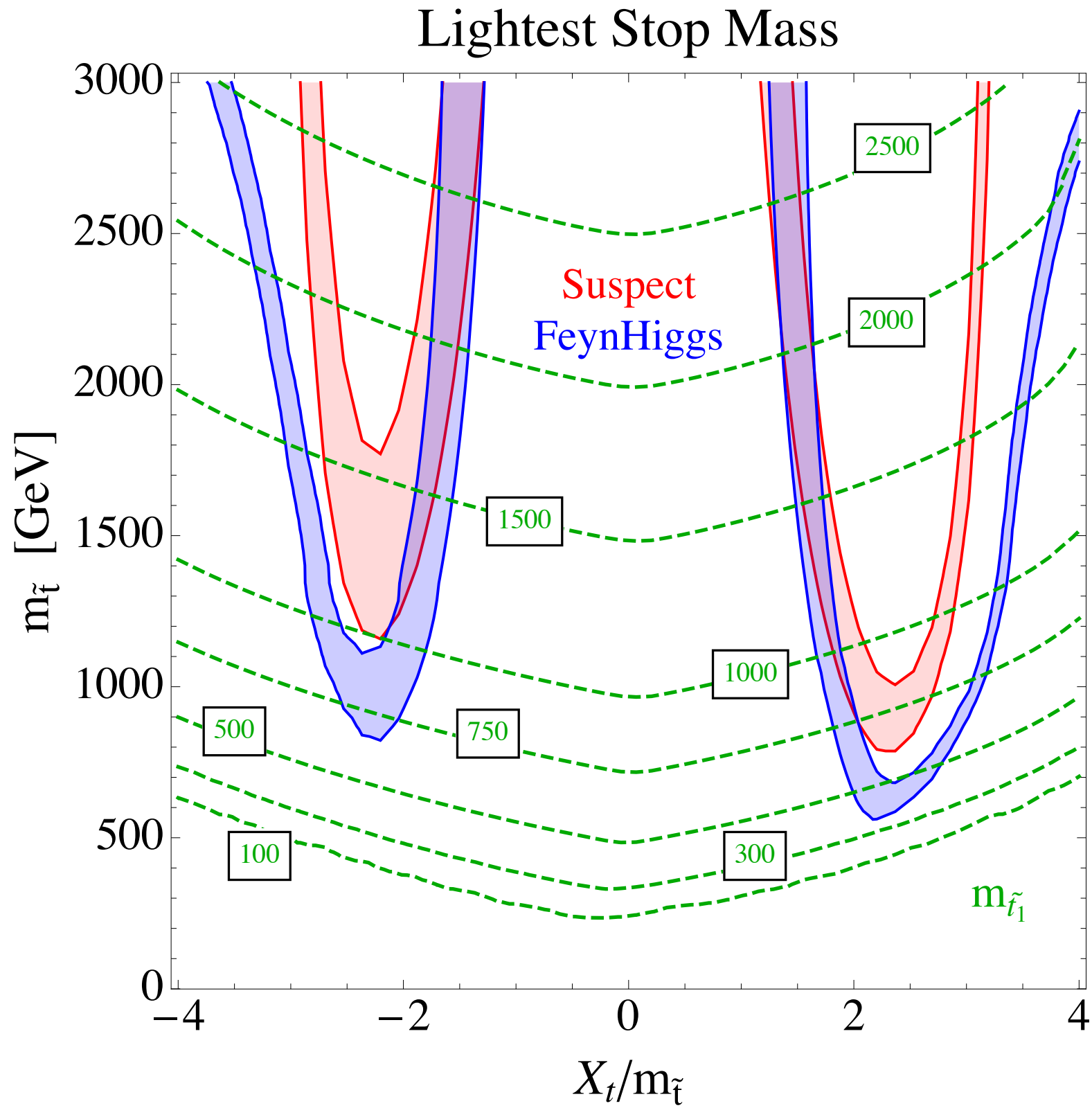
TO MAKE HIGGS MASS 125 GEV, LARGE STOP MASS IS NEEDED.



125

IN MSS  
ABOVE

TO MAINTAIN  
NEEDED



TAKEN FROM HALL, PINNER, RUDERMAN

OM

S

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TO MAKE HIGGS MASS 125 GEV, LARGE STOP MASS IS NEEDED.



**NATURALNESS** PROB. IS ON RISE TO OBTAIN WEAK SCALE.

NEED SOME EXTENSIONS TO MAKE MORE NATURAL MODEL FOR 125 GEV HIGGS



# RAISING THE HIGGS MASS

WE CAN ADD HIGGS QUARTIC COUPLINGS BY SOME WAYS...

- NEW GAUGE SYMMETRY THAT GIVES ADDITIONAL D-TERM QUARTIC POTENTIAL, E.G.  $U(1)_X$
- SINGLET EXTENSION THAT GIVES ADDITIONAL F-TERM POTENTIAL, E.G. NMSSM:  $\lambda S H_U H_D$



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WE FOCUS ON THIS POSSIBILITY



PQ-NMSSM AND  
PHENOMENOLOGY



# PQ-NMSSM: MODEL I

WE INTRODUCE AXION SUPERFIELD  $X$  OTHER THAN SINGLET SUPERFIELD  $S$ .

JEONG, SHOJI, YAMAGUCHI

$$\mathcal{L} = \int d^2\theta \lambda S H_u H_d + \int d^4\theta \kappa \frac{X^{*2}}{M_p} S + \text{h.c.}$$

WITH PQ-CHARGE  $(X, S, H_U, H_D) = (1, 2, -1, -1)$ .

PQ SYMMETRY BREAKING CAN BE GENERATED BY SUSY BREAKING ( $f_a \sim \sqrt{m_{\text{soft}} M_p}$ ).

$$X = F_a(1 + m_{\text{soft}}\theta^2), \quad \kappa \rightarrow \kappa(1 + m_{\text{soft}}\theta^2 + m_{\text{soft}}\bar{\theta}^2 + m_{\text{soft}}^2\theta^4)$$

WE OBTAIN EFFECTIVE SUPERPOTENTIAL

$$W_{\text{eff}} = \lambda S H_u H_d + (\xi_F + \theta^2 \xi_S) S$$

$$\xi_F = \kappa m_{\text{soft}} \frac{f_a^2}{M_p}$$

$$\xi_S = \kappa m_{\text{soft}}^2 \frac{f_a^2}{M_p}$$

SIMILAR TO NMSSM

PANAGIOTAKOPOULOS, TAMVAKI;  
PANAGIOTAKOPOULOS, PILAFTSIS



# PQ-NMSSM: MODEL I

## HIGGS SECTOR

$$\mathcal{M}_{S,11}^2 = m_Z^2 \cos^2 \beta + m_A^2 \sin^2 \beta,$$

$$\mathcal{M}_{S,22}^2 = m_Z^2 \sin^2 \beta + m_A^2 \cos^2 \beta,$$

$$\mathcal{M}_{S,12}^2 = (2\lambda^2 v^2 - m_A^2 - m_Z^2) \sin \beta \cos \beta,$$

$$\mathcal{M}_{S,33}^2 = m_S^2 + \lambda^2 v^2,$$

$$\mathcal{M}_{S,13}^2 = 2\lambda\mu_{\text{eff}}v \cos \beta - \lambda A_\lambda v \sin \beta,$$

$$\mathcal{M}_{S,23}^2 = 2\lambda\mu_{\text{eff}}v \sin \beta - \lambda A_\lambda v \cos \beta,$$

$$m_A^2 = \frac{\mu_{\text{eff}} B_{\text{eff}} + \widehat{m}_3^2}{\sin \beta \cos \beta}$$

$$m_S^2 = \lambda^2 v^2 \left( \frac{A_\lambda \sin \beta \cos \beta}{\mu_{\text{eff}}} - 1 \right) - \frac{\lambda \xi_S}{\mu_{\text{eff}}}$$

$$\mu_{\text{eff}} = \lambda s$$

$$B_{\text{eff}} = A_\lambda$$

$$\widehat{m}_3^2 = \lambda \xi_F.$$



# PQ-NMSSM: MODEL I

## HIGGS SECTOR

2X2 DOUBLET PART  
ROTATED BY ANGLE  $\beta$

$$\begin{aligned}\mathcal{M}_{S,11}^2 &= m_Z^2 \cos^2 \beta + m_A^2 \sin^2 \beta, \\ \mathcal{M}_{S,22}^2 &= m_Z^2 \sin^2 \beta + m_A^2 \cos^2 \beta, \\ \mathcal{M}_{S,12}^2 &= (2\lambda^2 v^2 - m_A^2 - m_Z^2) \sin \beta \cos \beta,\end{aligned}$$

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$$\mathcal{M}_{S,23}^2 = 2\lambda\mu_{\text{eff}}v \sin \beta - \lambda A_\lambda v \cos \beta,$$

## TREE-LEVEL HIGGS MASS



$$m_h^2 \lesssim m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta$$

$$m_A^2 = \frac{\mu_{\text{eff}} B_{\text{eff}} + \widehat{m}_3^2}{\sin \beta \cos \beta}$$

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## TREE-LEVEL HIGGS MASS

$$m_h^2 \lesssim m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta$$

WE CAN HAVE **125 GEV HIGGS**  
FOR MODERATE  **$1 < \tan \beta < 3$**   
AND  **$O(100)$  GEV STOP**

WE TAKE  **$\lambda=0.7$**  BECAUSE IT IS MAXIMUM  
VALUE ALLOWED BY LANDAU POLE  
CONSTRAINT



## NEUTRALINO SECTOR

$$\mathcal{M}_0 = \begin{pmatrix} M_1 & 0 & -g_1 v_d / \sqrt{2} & g_1 v_u / \sqrt{2} & 0 \\ & M_2 & g_2 v_d / \sqrt{2} & -g_2 v_u / \sqrt{2} & 0 \\ & & 0 & -\mu_{\text{eff}} & -\lambda v_u \\ & & & 0 & -\lambda v_d \\ & & & & 0 \end{pmatrix} .$$



## NEUTRALINO SECTOR

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**ZERO MASS**  $\longrightarrow$  **GENERATED BY MIXING**

$$m_{\chi_1} = \frac{\lambda^2 v^2 \sin 2\beta}{\mu_{\text{eff}}} \left( 1 - \frac{\lambda^2 v^2}{\mu_{\text{eff}}^2} + \mathcal{O}\left(\frac{\lambda^4 v^4}{\mu_{\text{eff}}^4}\right) \right)$$



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RELATIVELY LIGHT (**SINGLINO-LIKE**) NEUTRALINO INDUCES **INVISIBLE DECAYS OF Z BOSON AND HIGGS BOSON,**

CONSTRAINS THE MODEL AND **REDUCES HIGGS SIGNALS AT COLLIDER.**

RELIC NEUTRALINOS ARE OVERPRODUCED BUT IT CAN BE DILUTED BY LATE-TIME ENTROPY PRODUCTION. OR IT CAN DECAY TO LIGHT AXINOS.



# LEP CONSTRAINTS

## Z BOSON INVISIBLE DECAY

$$\Gamma(Z \rightarrow \chi_1 \chi_1) \approx \frac{g_2^2}{4\pi} \frac{(N_{13}^2 - N_{14}^2)^2}{24 \cos^2 \theta_W} M_Z$$

FROM LEPI,  $\Gamma_{\text{INV}} < 3 \text{ MEV}$ ,

$$|N_{13}^2 - N_{14}^2| \approx \frac{\lambda^2 v^2}{\mu_{\text{eff}}^2} |\cos 2\beta| < 0.13$$

FROM LEPII ( $s = (208 \text{ GEV})^2$ ),

$$\sigma(e^+ e^- \rightarrow \chi_1 \chi_2) \approx \frac{1}{128\pi s} \frac{g_2^4}{\cos^4 \theta_W} (N_{13} N_{23} - N_{14} N_{24})^2 < 70 \text{ fb}$$

$$|N_{13} N_{23} - N_{14} N_{24}| \lesssim 0.2$$



# HIGGS INVISIBLE DECAY

## 2 POSSIBLE WAYS TO AVOID HIGGS INVISIBLE DECAY

LARGE SINGLINO-HIGGSINO MIXING CAN MAKE NEUTRALINO MASS ABOVE  $M_H/2$ .

HOWEVER,  $e^+e^- \rightarrow \chi_1\chi_2$  IN LEP II CONSTRAINS THIS SINCE  $\mu$  SHOULD BE SMALL ( $\sim 110$  GEV) FOR LARGE MIXING.

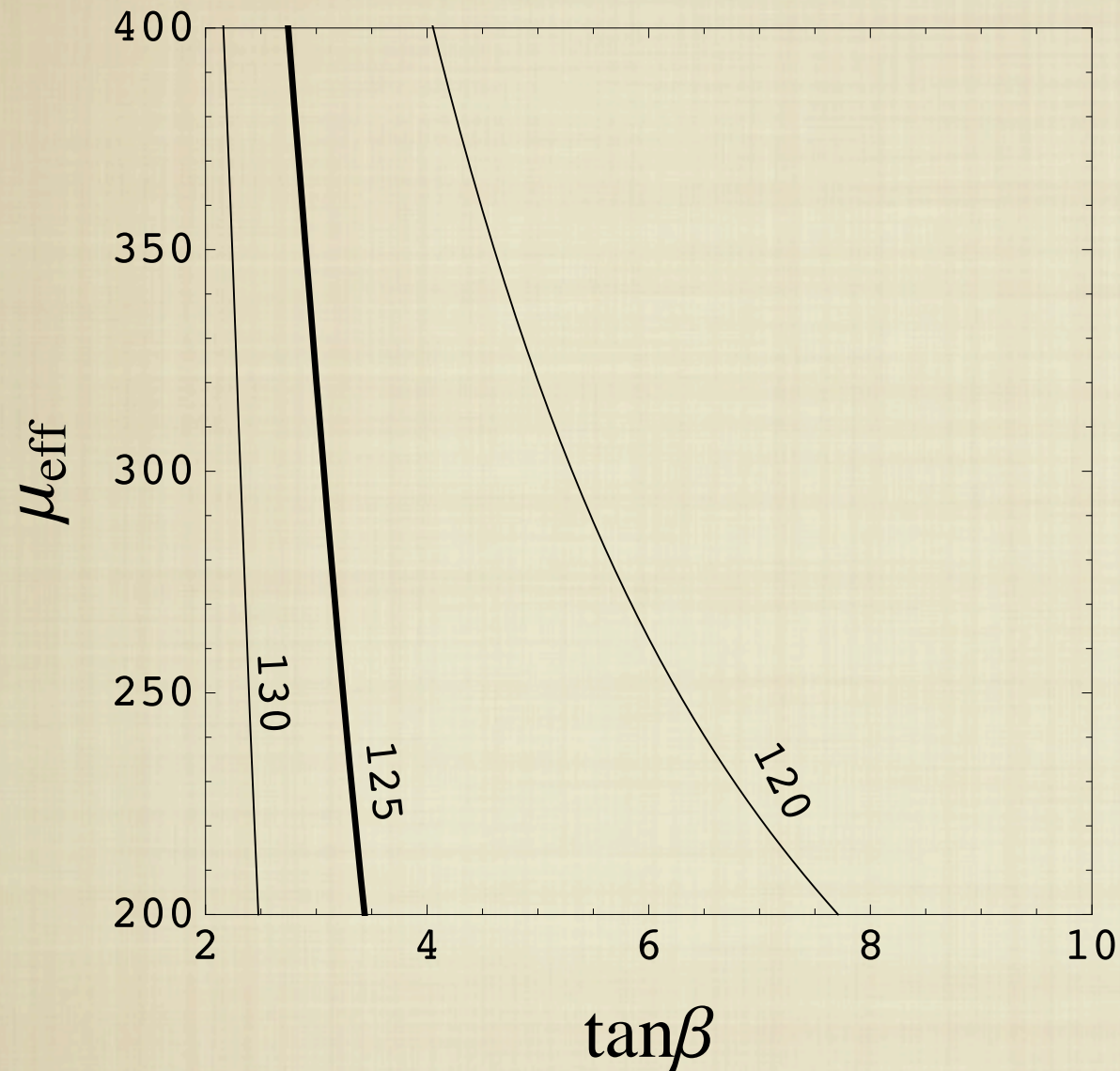
EVEN FOR LIGHT NEUTRALINO,  $g_{H\chi_1\chi_1}$  CAN **VANISH** IN THE PARAMETER REGION THAT **GAUGINO PART AND HIGGSINO PART CANCEL**.

IF  $H_U$ - $H_D$  MIXING VANISHES,  $H \rightarrow \gamma\gamma$  SIGNAL IS ENHANCED FOR SMALL INVISIBLE DECAY REGION.

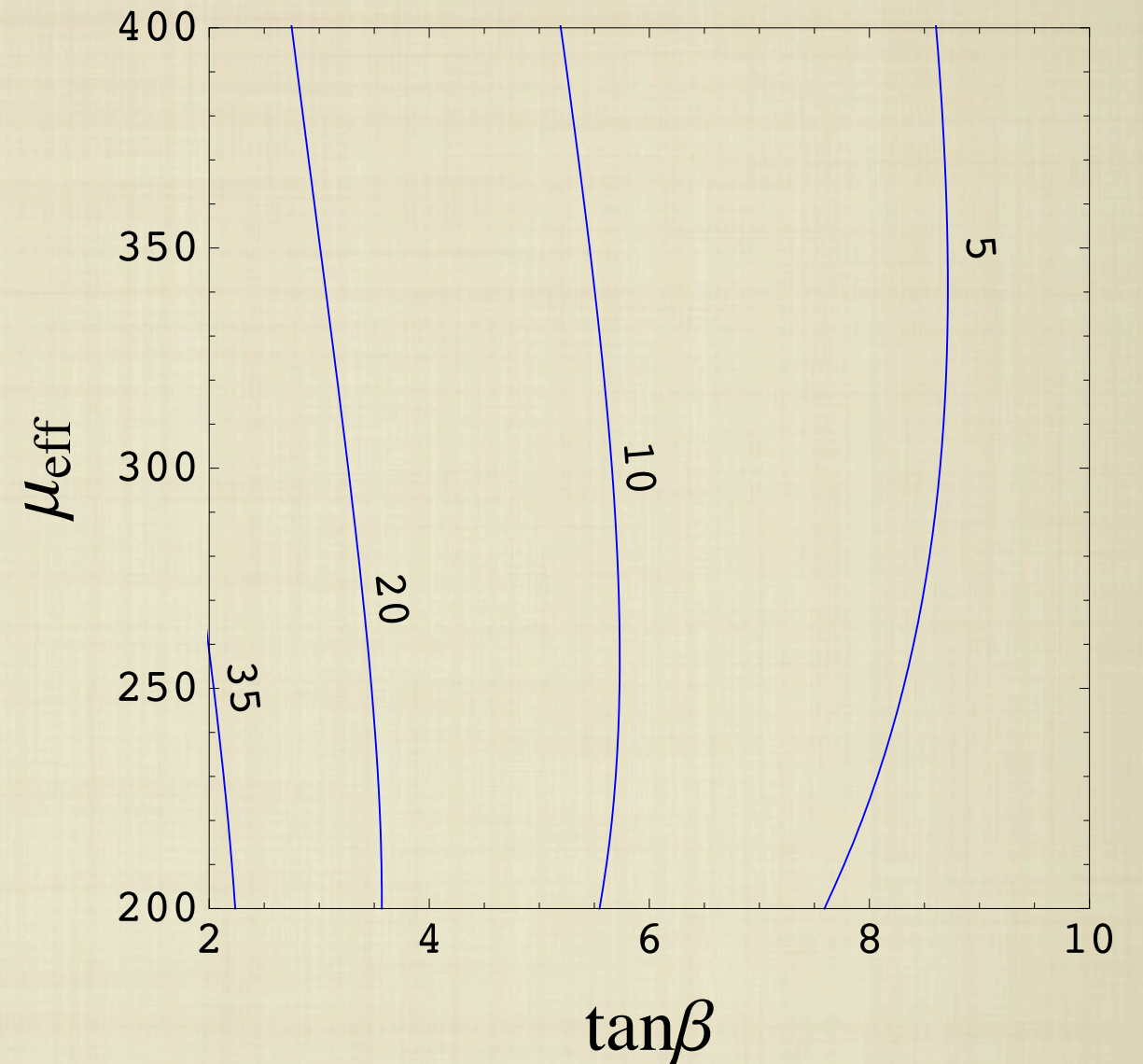
IF  $H_U$ - $H_D$  MIXING IS SIZABLE,  $H \rightarrow \gamma\gamma$  SIGNAL IS AT MOST SM ONE FOR VANISHING INVISIBLE DECAY REGION.



# RESULTS: NO $H_U$ - $H_D$ MIXING



**HIGGS MASS**

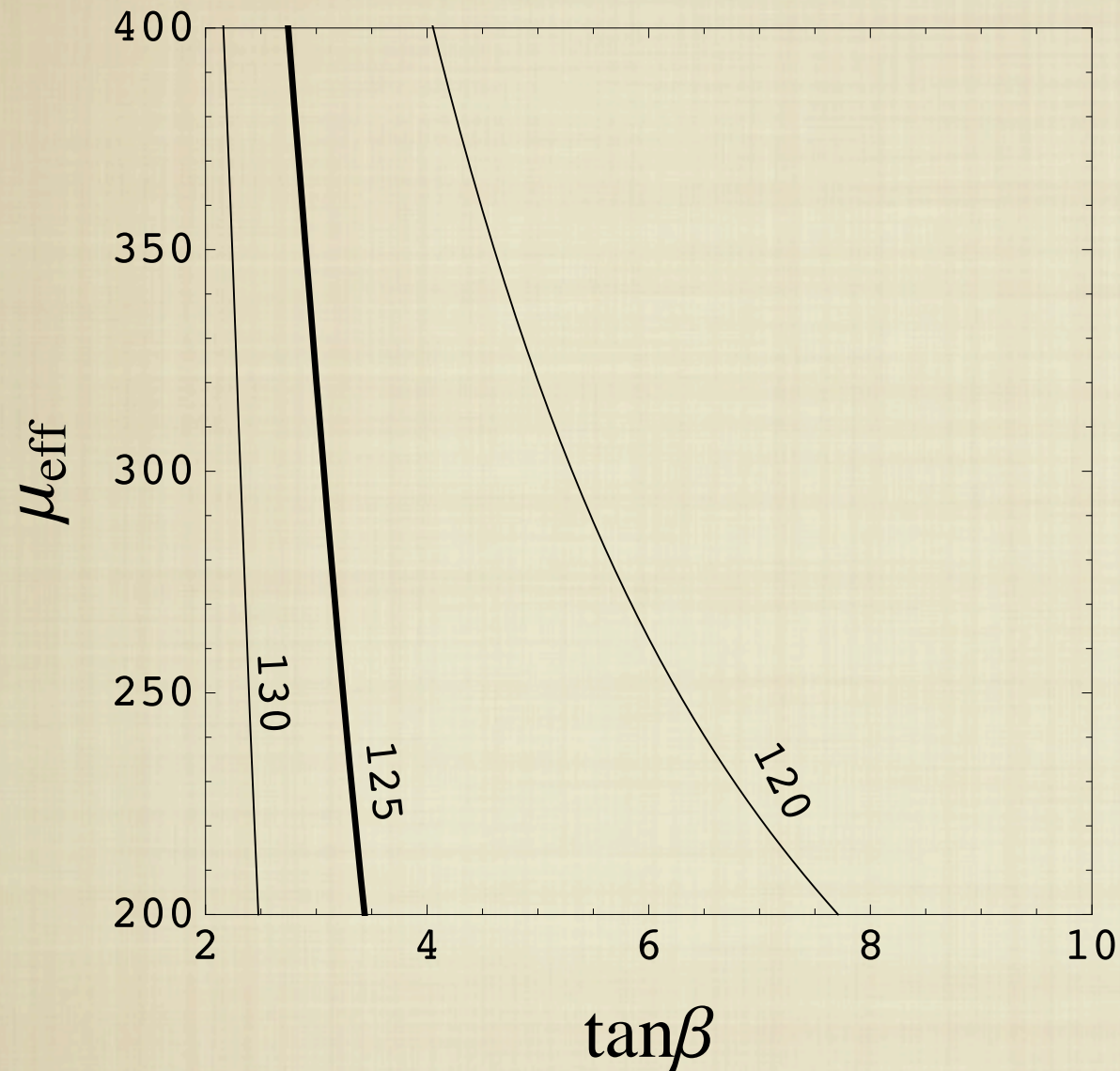


**NEUTRALINO MASS**

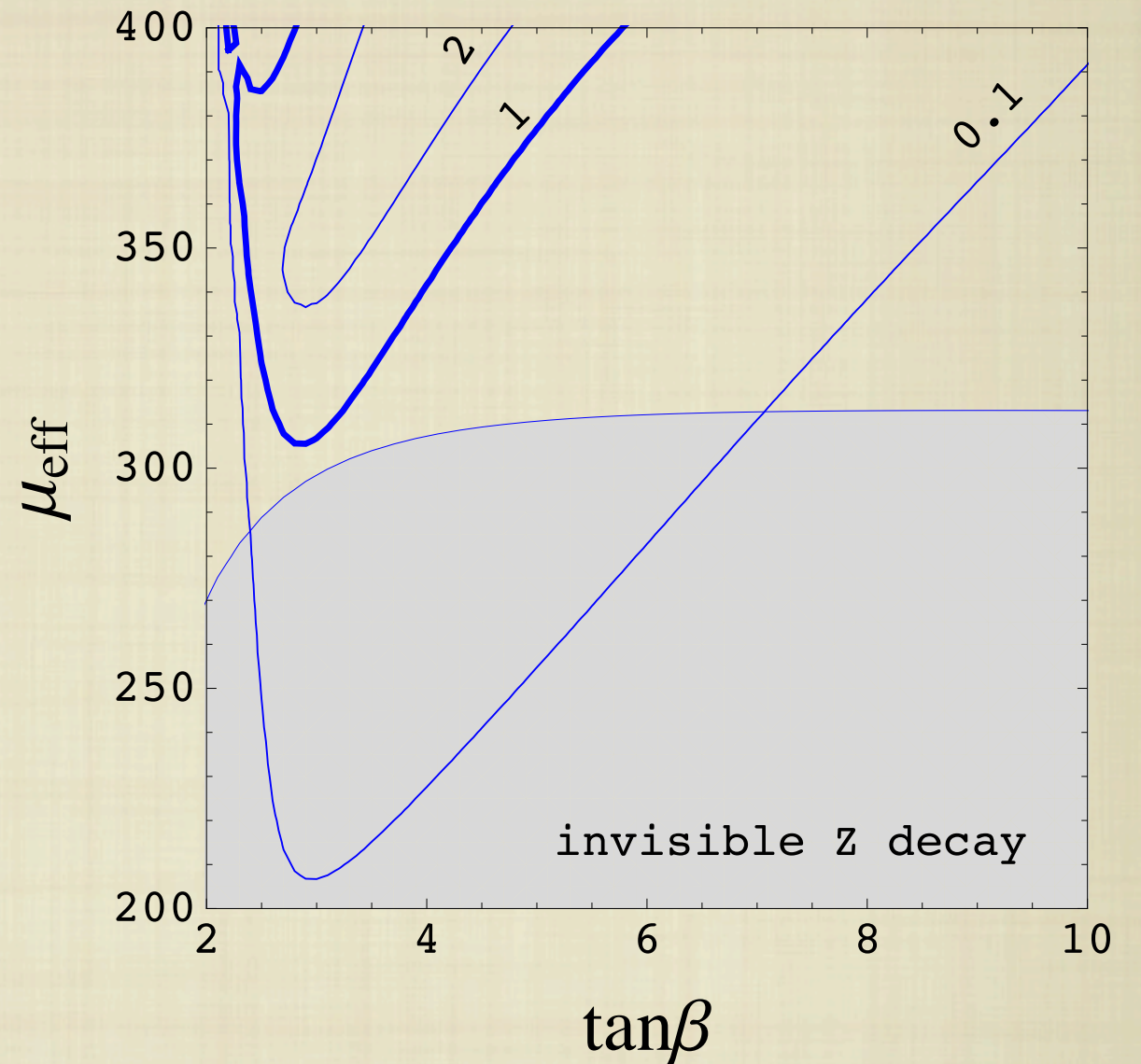
$$m_A = 146 \text{ GeV}, \quad M_3 = 3M_2 = 6M_1 = 900 \text{ GeV},$$
$$m_{\tilde{Q}_3} = m_{\tilde{u}_3} = 500 \text{ GeV}, \quad X_t = -1 \text{ TeV}$$



# RESULTS: NO $H_U$ - $H_D$ MIXING



**HIGGS MASS**

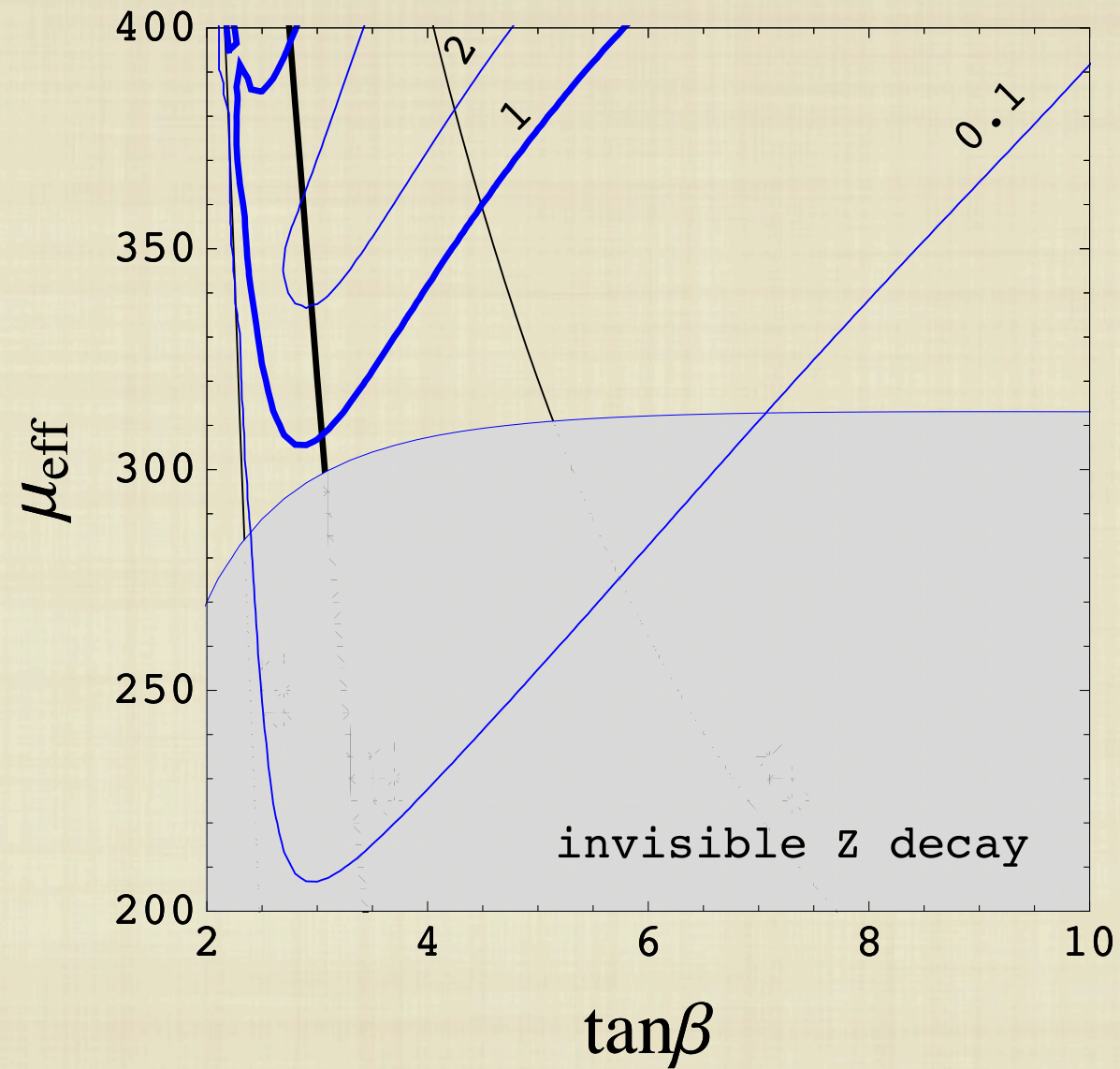


**$\sigma(\text{GG} \rightarrow \text{H} \rightarrow \gamma\gamma) / \sigma_{\text{SM}}$**

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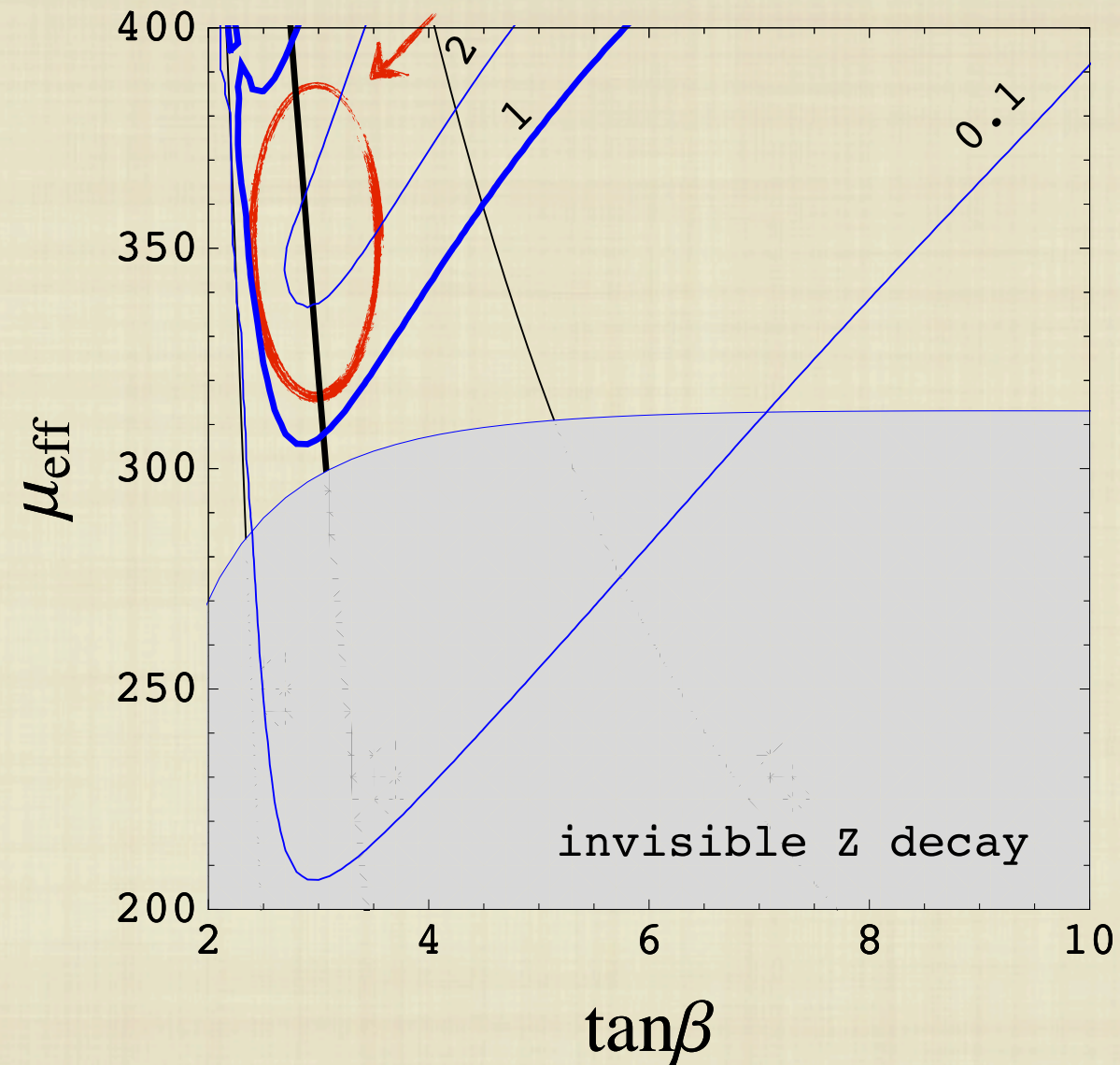


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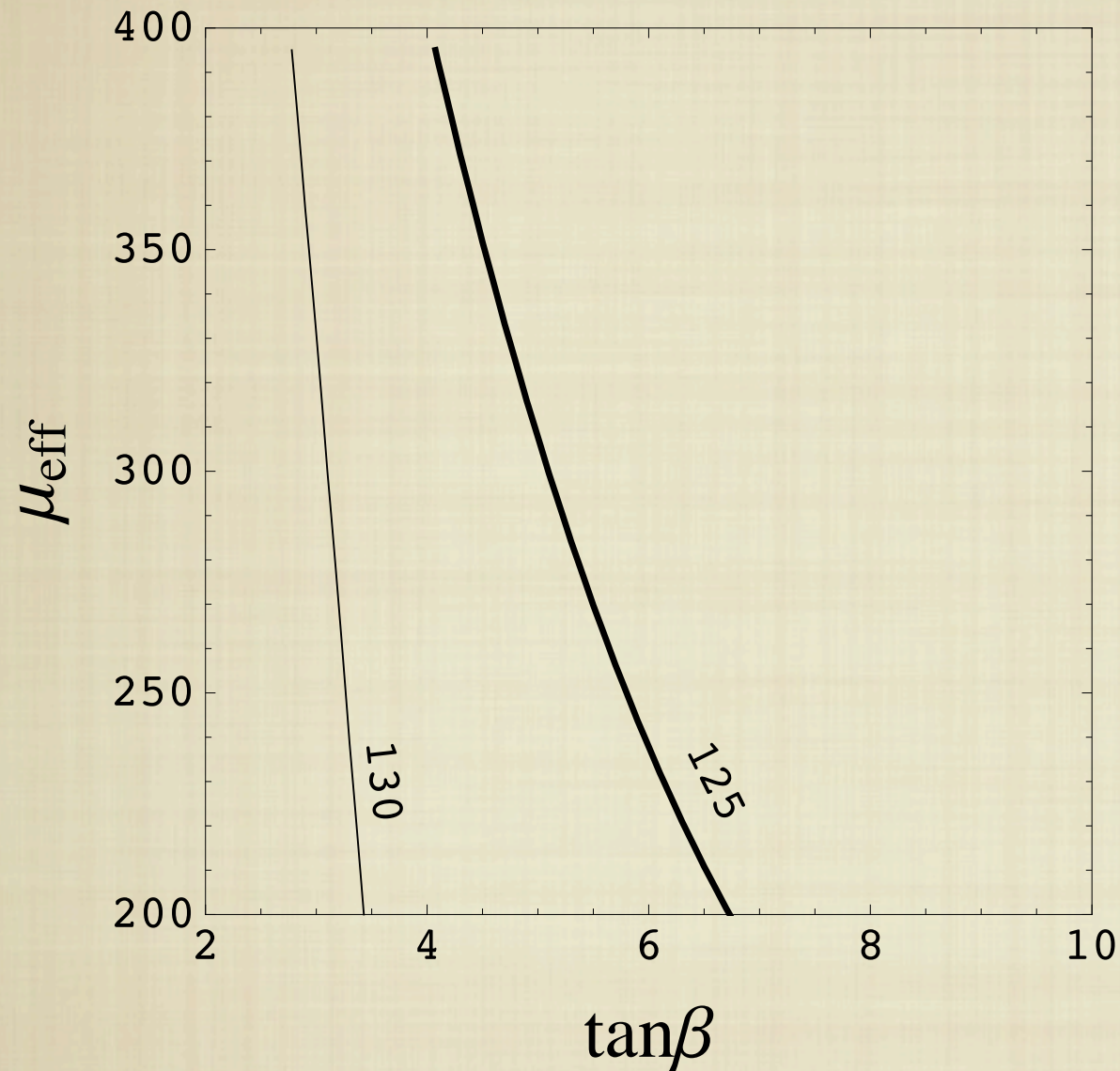
WE PREFER THIS REGION!



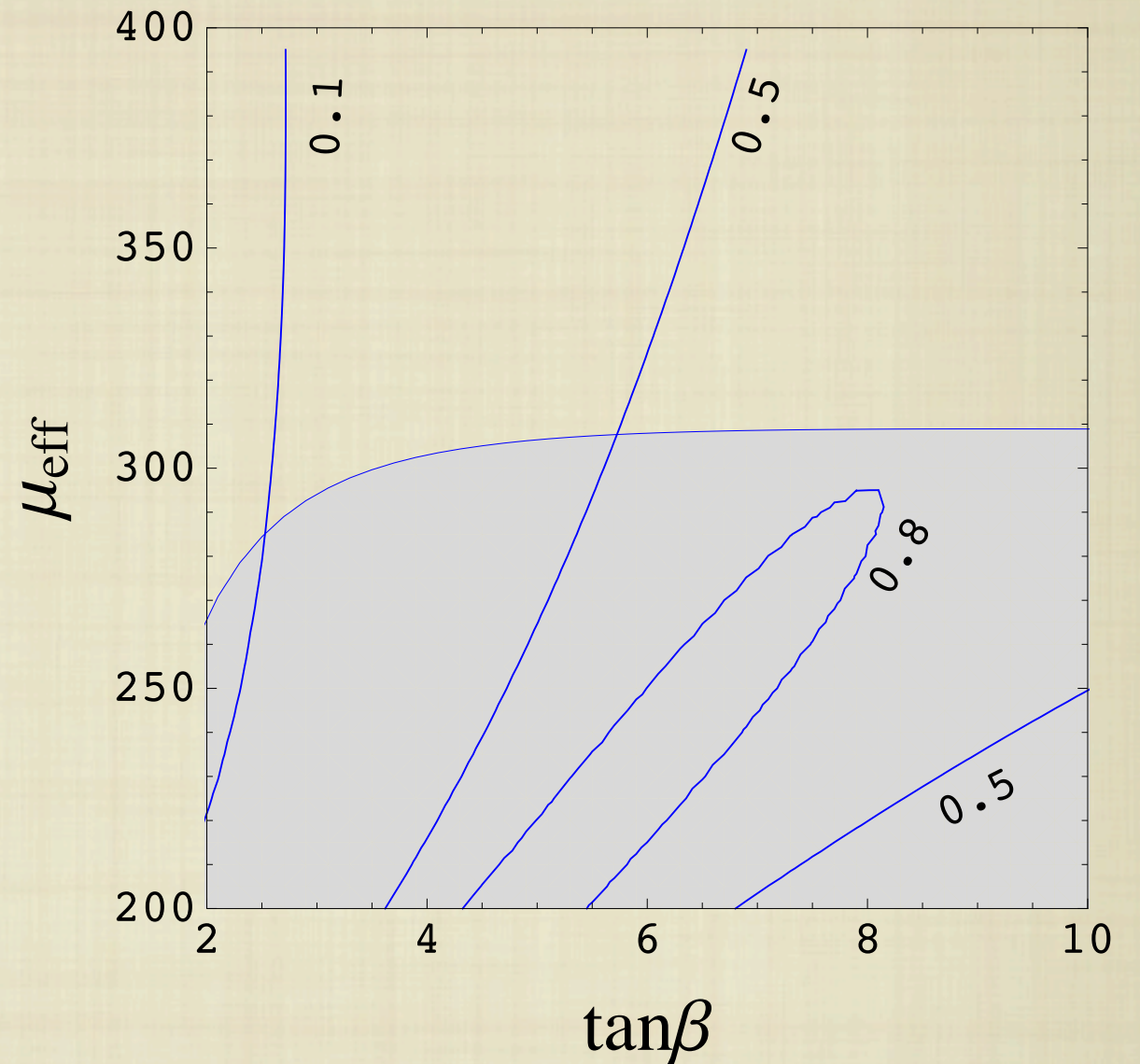
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# RESULTS: $H_U$ - $H_D$ MIXING



**HIGGS MASS**



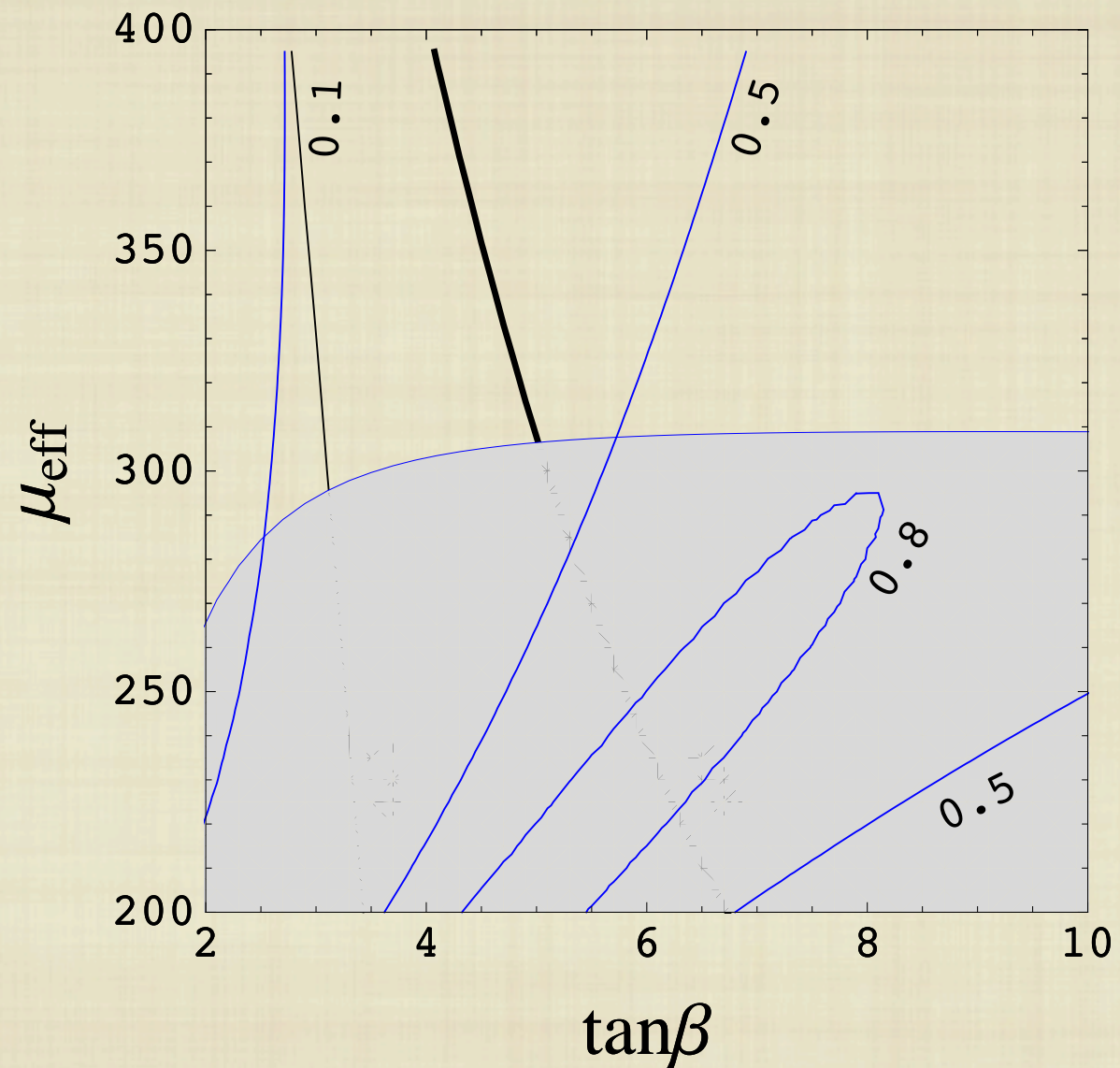
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# RESULTS: $H_U$ - $H_D$ MIXING



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# PQ-NMSSM: MODEL II

TO AVOID SUCH PARAMETER CHOICE, WE CAN EXTEND THE MODEL.

$$W = \lambda S H_u H_d + Y T_1 T_2 + T_2 S^2 + \frac{X^3 T_1}{M_p} + \frac{X T_1 T_2 + Y^2 T_2}{M_p} S,$$
$$K = \frac{(X^\dagger)^2 + Y^\dagger T_1 + Y^2}{M_p} S^\dagger + \text{h.c.}$$

WITH CHARGE ASSIGNMENT

fields	$X$	$Y$	$T_1$	$T_2$	$S$	$H_u H_d$
$U(1)_{\text{PQ}}$	-1	1	3	-4	2	-2
$\mathbb{Z}_2$	0	$\pi$	$\pi$	0	$\pi$	$\pi$

$$\langle X \rangle, \langle Y \rangle \gg \langle T_1 \rangle, \langle T_2 \rangle, \langle S \rangle$$

INTEGRATING OUT HEAVY FIELD  $T_1$  AND  $T_2$ ,


$$W_{\text{eff}} = \lambda S H_u H_d - \frac{X^3 Y}{M_p^2} S - \frac{X^3}{M_p Y} S^2$$
$$= \lambda S H_u H_d + \xi_F S + \frac{1}{2} \mu' S^2$$



# PQ-NMSSM: MODEL II

HIGGS SECTOR IS SIMILAR TO MODEL I.

NEUTRALINO SECTOR IS

$$\mathcal{M}_0 = \begin{pmatrix} M_1 & 0 & -g_1 v_d / \sqrt{2} & g_1 v_u / \sqrt{2} & 0 \\ & M_2 & g_2 v_d / \sqrt{2} & -g_2 v_u / \sqrt{2} & 0 \\ & & 0 & -\mu_{\text{eff}} & -\lambda v_u \\ & & & 0 & -\lambda v_d \\ & & & & \mu' \end{pmatrix}$$


**NON-ZERO SINGLINO MASS**

THE  $\chi_1$  CAN BE **BOTH SINGLINO-LIKE OR HIGGSINO-LIKE**  
(ALSO GAUGINO-LIKE).

INVISIBLE DECAY OF Z AND HIGGS CAN BE KINEMATICALLY  
FORBIDDEN FOR SIZABLE  $\mu'$ .



COLLIDER  
PERSPECTIVE

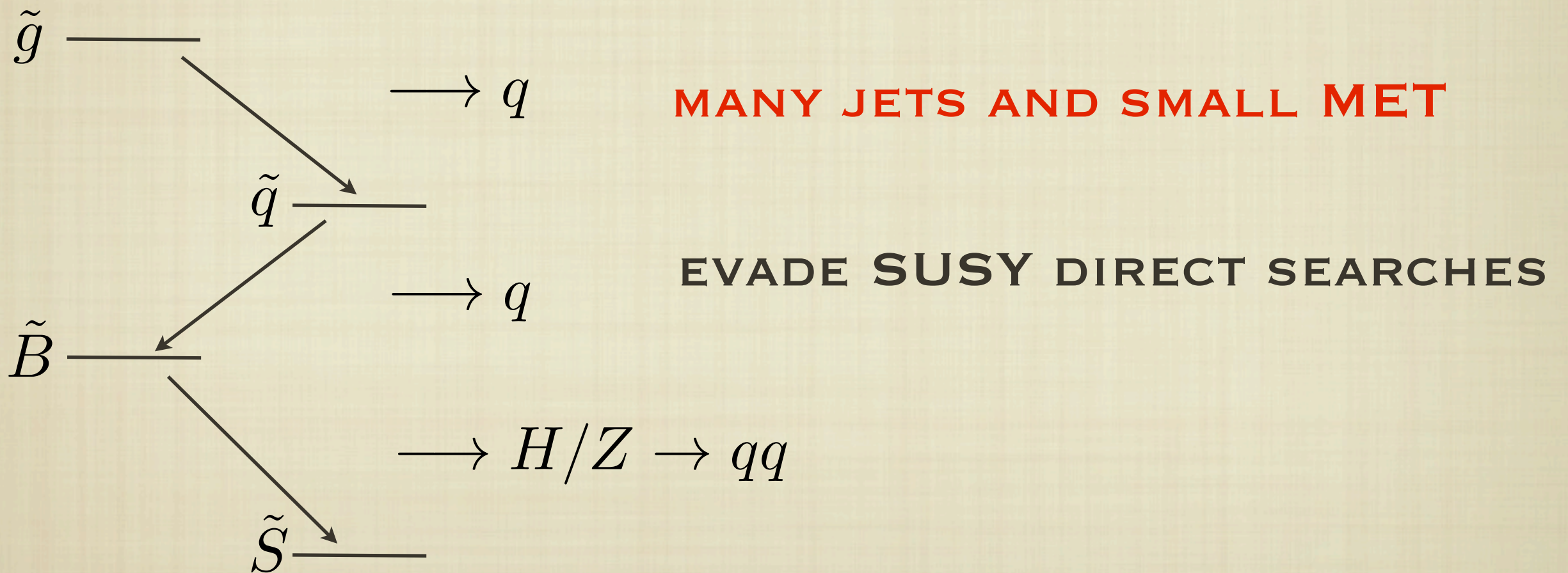


# PQ-NMSSM: MODEL I

LIGHT **SINGLINO-LIKE** NEUTRALINO ( $\sim 20$  GEV)



HEAVY PARTICLES MAKE LONG DECAY CHAIN.





# PQ-NMSSM: MODEL II

DEPENDENDING ON THE PARAMETER SPACE (SIZE OF  $\mu'$ ),

**SINGLINO-LIKE** ( $\mu' < M_1, M_2, \mu$ )

**HEAVY SINGLINO (~70 GEV)  
IS POSSIBLE.**

**MET IS NOT MUCH  
REDUCED.**



**MANY JETS FROM LONG  
CASCADE.**

**MSSM-LIKE** ( $\mu' > M_1$  or  $M_2$  or  $\mu$ )

**HIGGSINO-LIKE OR  
GAUGINO-LIKE.**

**2,3,4 JETS AND MET CAN  
CONSTRAIN THE MODEL.**



**SIMILAR TO MSSM.**

**NOW IN PROGRESS...**



# SUMMARY

- PQ SYMMETRY CAN SOLVE STRONG CP PROBLEM.
- TO MAKE 125 GEV HIGGS IN SUSY, SINGLET EXTENSION IS NEEDED.
- SIMPLE PQ-NMSSM CAN SATISFY ALL CONSTRAINTS ONLY IN SPECIAL PARAMETER SPACE (DOUBLET MIXING VANISHES).
- INCLUDING SINGLINO MASS TERM IS NEEDED TO AVOID SPECIAL PARAMETER CHOICE.
- LIGHT SINGLET OF PQ-NMSSM CAN MAKE MANY JETS AND SMALL MET.