

Rare decays and other future prospects in flavour physics

Nazila Mahmoudi
CERN TH & LPC Clermont-Ferrand (France)

Implications of LHC results for TeV-scale physics – WG3 meeting

CERN, December 9th, 2011



Motivations

Indirect searches for New Physics

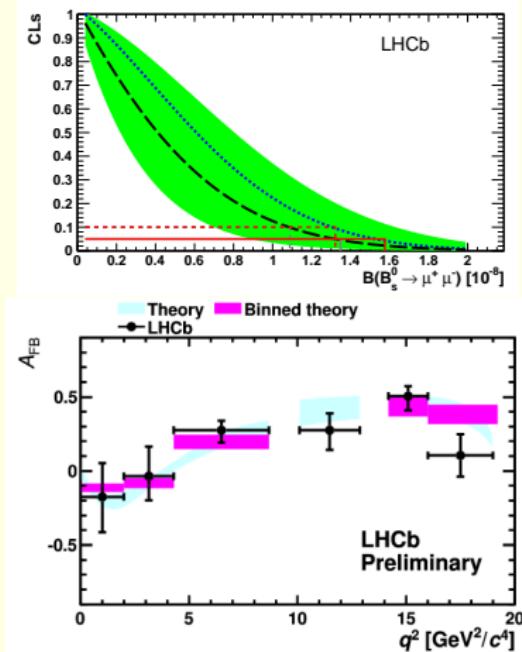
- ▶ sensitivity to new physics effects
- ▶ complementary to other searches
- ▶ probe sectors inaccessible to direct searches
- ▶ test quantum structure of the SM at loop level
- ▶ constrain parameter spaces of new physics scenarios
- ▶ valuable data already available
- ▶ promising experimental situation
- ▶ consistency checks with direct observations



LHCb and New Physics

Already, a lot of interesting results:

- ▶ CP violation
- ▶ Rare decays
 - ▶ $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$
 - ▶ $B \rightarrow K^* \mu^+ \mu^-$
 - ▶ $B \rightarrow K^* \gamma$



In this talk

- ▶ Constrained (Conventional) MSSM scenarios
 - ▶ implication of $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$ limit/measurement
 - ▶ implication of other rare decays
 - ▶ comparison with the direct SUSY limits
- ▶ More general MSSM scenarios
 - ▶ implications of flavour observables
 - ▶ constraints from $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$
- ▶ Beyond SUSY
- ▶ Model independent constraints
- ▶ Conclusions



BR($B_s \rightarrow \mu^+ \mu^-$)

Effective Hamiltonian:

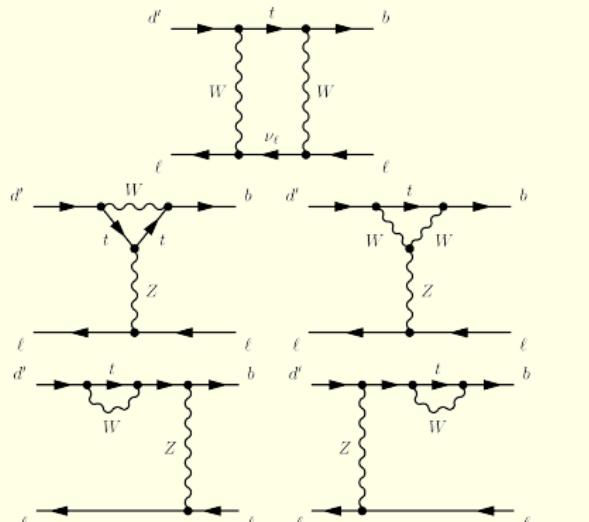
$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* (\sum C_i(\mu) \mathcal{O}_i(\mu) + \sum C_{Q_i}(\mu) Q_i(\mu))$$

Important operators:

$$\mathcal{O}_{10} = \frac{e^2}{(4\pi)^2} (\bar{s}\gamma^\mu b_L)(\bar{\ell}\gamma_\mu\gamma_5\ell)$$

$$Q_1 = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha)(\bar{\ell}\ell)$$

$$Q_2 = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha)(\bar{\ell}\gamma_5\ell)$$

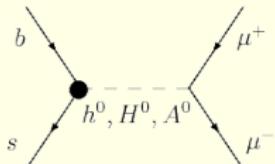


$$\begin{aligned} \text{BR}(B_s \rightarrow \mu^+ \mu^-) &= \frac{G_F^2 \alpha^2}{64\pi^3} f_{B_s}^2 \tau_{B_s} m_{B_s}^3 |V_{tb} V_{ts}^*|^2 \sqrt{1 - \frac{4m_\mu^2}{m_{B_s}^2}} \\ &\times \left\{ \left(1 - \frac{4m_\mu^2}{m_{B_s}^2}\right) \left| \left(\frac{m_{B_s}}{m_b + m_s}\right) (C_{Q_1} - C'_{Q_1}) \right|^2 + \left| \left(\frac{m_{B_s}}{m_b + m_s}\right) (C_{Q_2} - C'_{Q_2}) + 2(C_{10} - C'_{10}) \frac{m_\mu}{m_{B_s}} \right|^2 \right\} \end{aligned}$$



$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$

Very sensitive to SUSY, especially for large $\tan\beta$:



$$\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{MSSM} \sim \frac{m_b^2 m_\mu^2 \tan^6 \beta}{M_A^4}$$

SUSY contributions in $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$ can lead to an $\mathcal{O}(100)$ enhancement over the SM!

Large uncertainty from the decay constant (f_{B_s})!

→ A way out: double ratios of leptonic decays:

$$R = \left(\frac{\text{BR}(B_s \rightarrow \mu^+ \mu^-)}{\text{BR}(B_u \rightarrow \tau \nu)} \right) / \left(\frac{\text{BR}(D_s \rightarrow \tau \nu)}{\text{BR}(D \rightarrow \mu \nu)} \right)$$

B. Grinstein, Phys. Rev. Lett. 71 (1993)

A.G. Akeroyd, JHEP 1010 (2010)

From the form factor and CKM matrix point of view:

$$R \propto \frac{|V_{ts} V_{tb}|^2}{|V_{ub}|^2} \frac{(f_{B_s}/f_B)^2}{(f_{D_s}/f_D)^2} \quad \text{with:} \quad \frac{(f_{B_s}/f_B)}{(f_{D_s}/f_D)} \approx 1$$

R has no dependence on the decay constants, contrary to each decay taken individually!

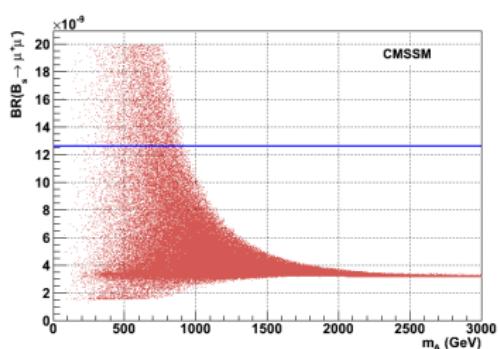


Results

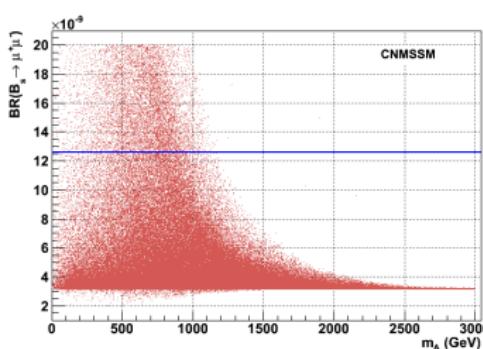
LHCb + CMS combined limit: $\text{BR}(B_s \rightarrow \mu^+ \mu^-) \lesssim 3 \times \text{SM value}$

At 95% C.L., including th uncert.: $\text{BR}(B_s \rightarrow \mu^+ \mu^-) < 1.26 \times 10^{-8}$

CMSSM



CNMSSM

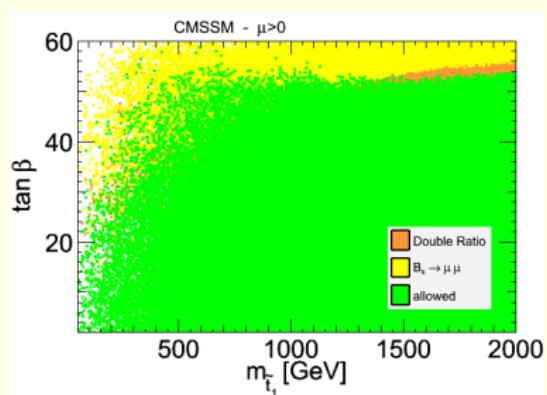


Results

The constraining power in the case of a SM like discovery:

Current limit

SM like branching ratio

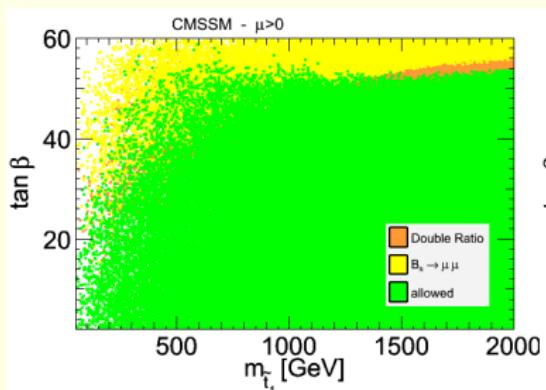


A.G. Akeroyd, F.M., D. Martinez Santos, arXiv:1108.3018
SuperIso v3.2

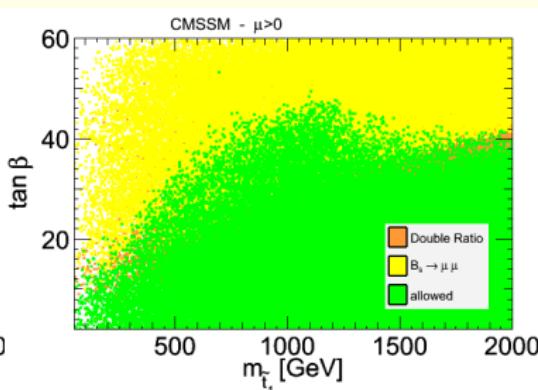
Results

The constraining power in the case of a SM like discovery:

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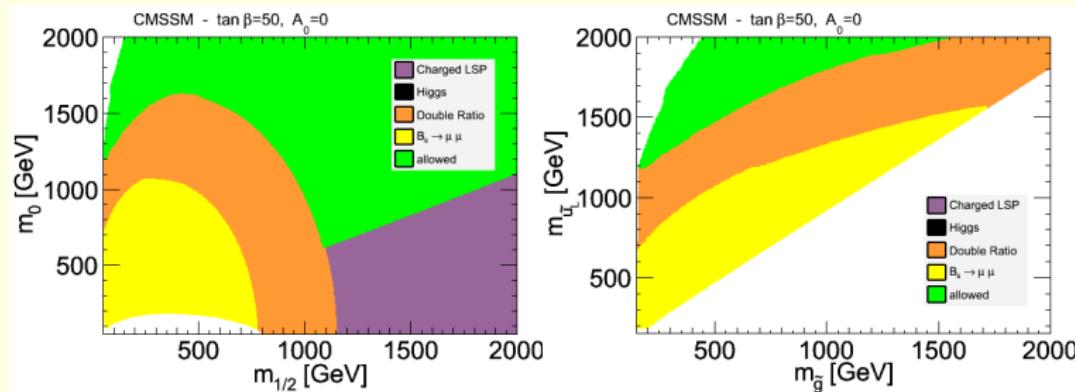
SM like branching ratio



A.G. Akeroyd, F.M., D. Martinez Santos, arXiv:1108.3018
SuperIso v3.2



Results

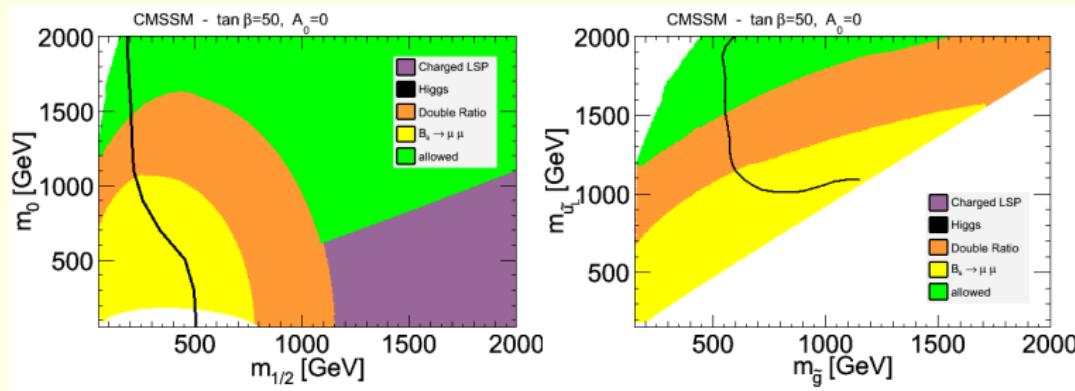


This goes far beyond ATLAS and CMS direct limits!

A.G. Akeroyd, F.M., D. Martinez Santos, arXiv:1108.3018
SuperIso v3.2



Results



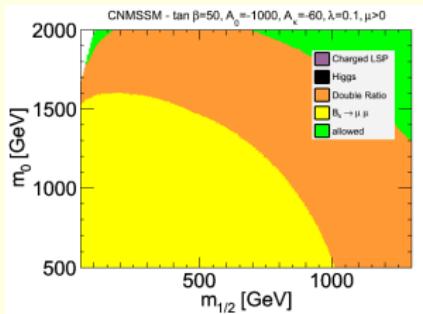
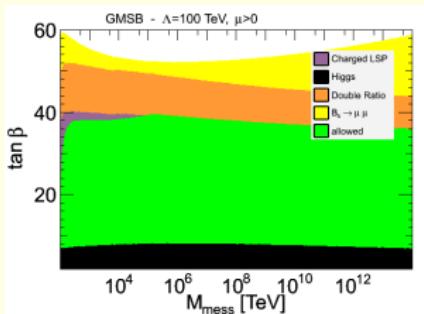
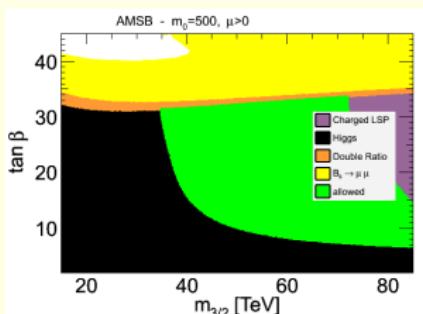
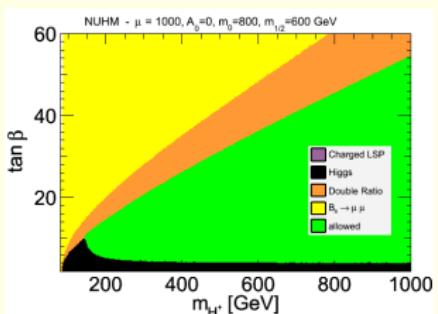
This goes far beyond ATLAS and CMS direct limits!

A.G. Akeroyd, F.M., D. Martinez Santos, arXiv:1108.3018
SuperIso v3.2



Results

Also very constraining for other constrained MSSM scenarios:



$$\text{BR}(B \rightarrow K^* \mu^+ \mu^-)$$

Effective Hamiltonian:

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* (\sum C_i(\mu) \mathcal{O}_i(\mu) + \sum C_{Q_i}(\mu) Q_i(\mu))$$

QCDF/SCET → 7 hadronic form factors

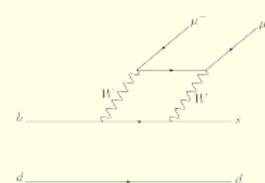
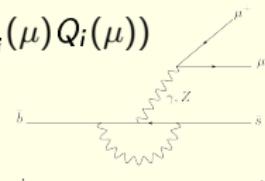
Main operators:

$$\mathcal{O}_9 = \frac{e^2}{(4\pi)^2} (\bar{s}\gamma^\mu b_L)(\bar{\ell}\gamma_\mu \ell)$$

$$\mathcal{O}_{10} = \frac{e^2}{(4\pi)^2} (\bar{s}\gamma^\mu b_L)(\bar{\ell}\gamma_\mu \gamma_5 \ell)$$

$$Q_1 = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha)(\bar{\ell}\ell)$$

$$Q_2 = \frac{e^2}{16\pi^2} (\bar{s}_L^\alpha b_R^\alpha)(\bar{\ell}\gamma_5 \ell)$$



→ explore full angular analysis, design observables with reduced hadronic uncertainties

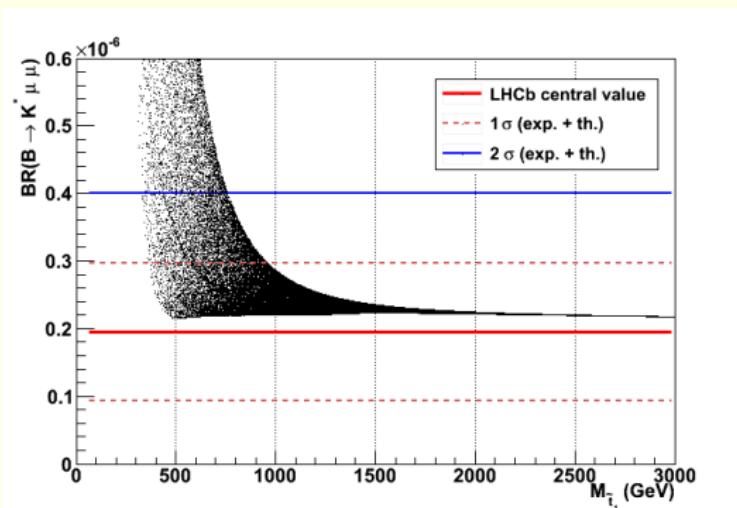
In particular, the forward-backward asymmetry is of interest:

$$A_{FB}(\hat{s}) = \frac{1}{d\Gamma/d\hat{s}} \left[\int_0^1 d(\cos\theta) \frac{d^2\Gamma}{d\hat{s}d(\cos\theta)} - \int_{-1}^0 d(\cos\theta) \frac{d^2\Gamma}{d\hat{s}d(\cos\theta)} \right]$$

θ : angle between B^0 and μ^+ momenta in the dilepton system center of mass

$$\hat{s} = s/M_B^2, \text{ with } s = (p_{\mu^+} + p_{\mu^-})^2$$



$B \rightarrow K^* \mu^+ \mu^-$
 $\text{BR}(B \rightarrow K^* \mu^+ \mu^-)$ in the low q^2 region:


For $m_{\tilde{q}} > 750$ GeV, SUSY spread is within the th+exp error

Look at other observables (A_{FB} , F_L , ...)

Reduce both theory and experimental errors.



Isospin asymmetry of $B \rightarrow K^* \gamma$

Based on $b \rightarrow s\gamma$ transitions.

SUSY contributions from charged Higgs and chargino loops

Isospin asymmetry: very interesting when the interference is destructive

$$\Delta_{0-} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0}\gamma) - \Gamma(B^- \rightarrow K^{*-}\gamma)}{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0}\gamma) + \Gamma(B^- \rightarrow K^{*-}\gamma)}$$

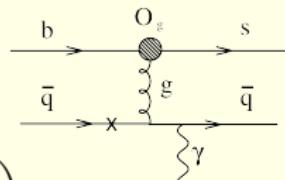
$$\Delta_{0-} = \text{Re}(b_d - b_u), \quad b_q = \frac{12\pi^2 f_B Q_q}{m_b T_1^{B \rightarrow K^*} a_7^c} \left(\frac{f_{K^*}}{m_b} K_1 + \frac{f_{K^*} m_{K^*}}{6\lambda_B m_B} K_2 \right)$$

$$a_7^c = C_7 + \frac{\alpha_s(\mu) C_F}{4\pi} \left(C_1(\mu) G_1(s_p) + C_8(\mu) G_8 \right) + \frac{\alpha_s(\mu_h) C_F}{4\pi} \left(C_1(\mu_h) H_1(s_p) + C_8(\mu_h) H_8 \right)$$

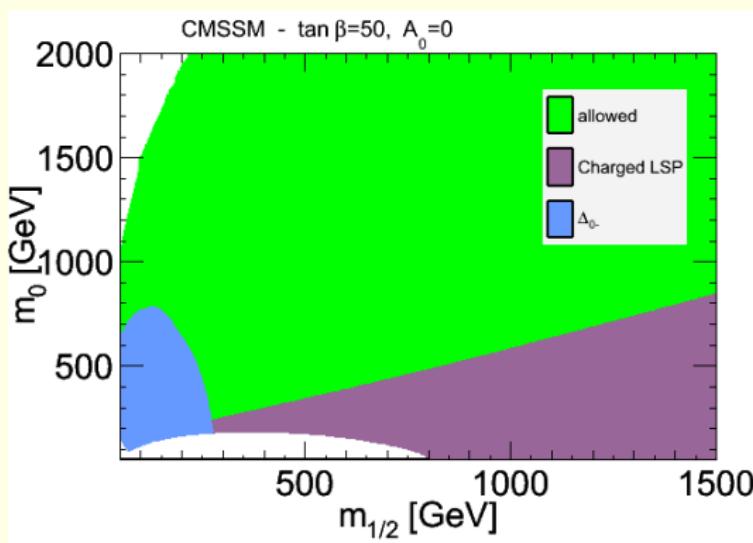
In the Standard Model: $\Delta_{0-} \simeq 8\%$

Kagan and Neubert, Phys. Lett. B539, 227 (2002)

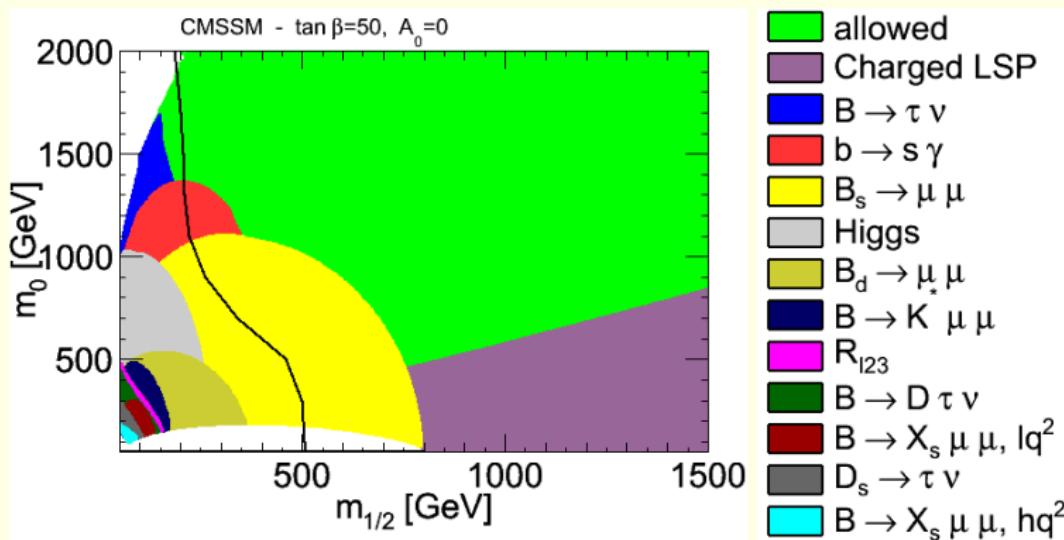
Experimental value (HFAG): $\Delta_0 = (5.2 \pm 2.6) \times 10^{-2}$



Isospin asymmetry of $B \rightarrow K^* \gamma$



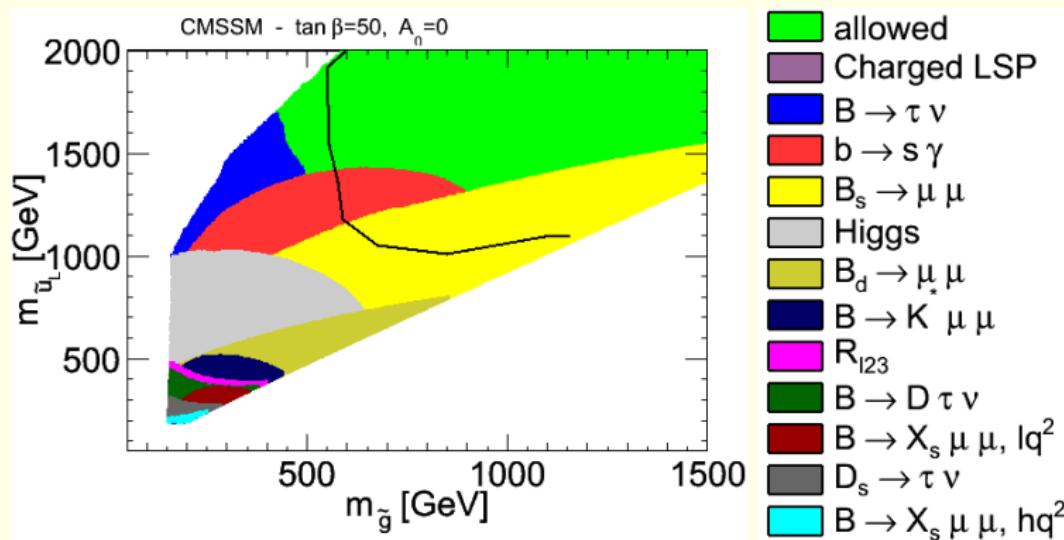
Other rare decays



SuperIso v3.2+



Other rare decays



SuperIso v3.2+



pMSSM

Going beyond constrained scenarios

- ▶ CMSSM useful for benchmarking,...
- ▶ However the mass patterns could be more complicated
- ▶ How do the conclusions change when moving to the MSSM?

Phenomenological MSSM (pMSSM)

- ▶ The most general CP/R parity-conserving MSSM
- ▶ Minimal Flavour Violation at the TeV scale
- ▶ The first two sfermion generations are degenerate
- ▶ The three trilinear couplings are general for the 3 generations
 → 19 free parameters

10 sfermion masses, 3 gaugino masses, 3 trilinear couplings, 3 Higgs/Higgsino

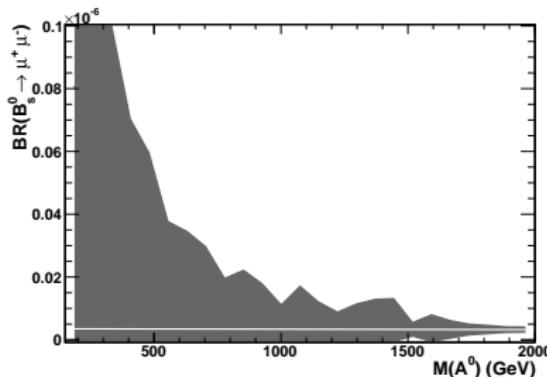
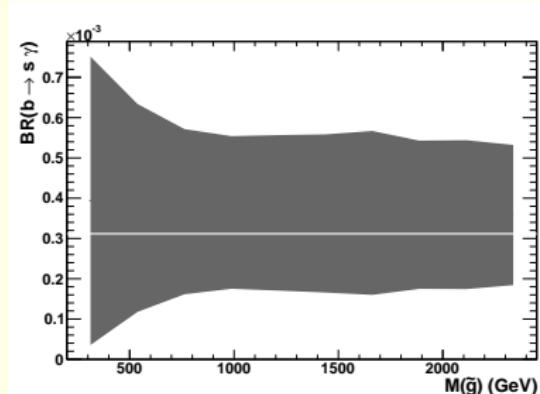
A. Djouadi, J.-L. Kneur, G. Moutata, [hep-ph/0211331](#)
 C.F. Berger et al., JHEP 0902 (2009) 023
 S. AbdusSalam et al., Phys. Rev. D81 (2010) 095012
 S. Sekmen et al., [arXiv:1109.5119](#)
 A. Arbey, M. Battaglia, F.M., [arXiv:1110.3726](#)



Implication of flavour observables on the pMSSM models

$\text{BR}(B \rightarrow X_s \gamma)$

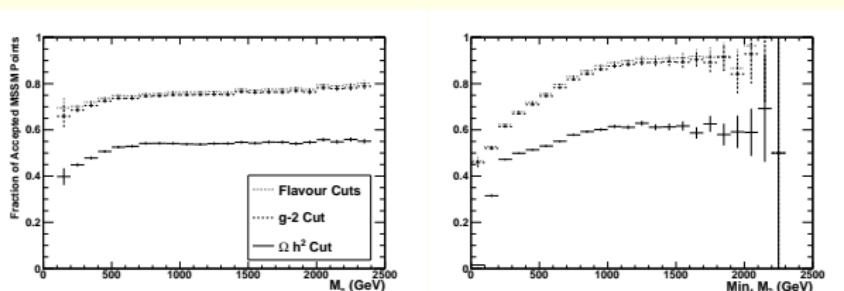
$\text{BR}(B_s \rightarrow \mu^+ \mu^-)$



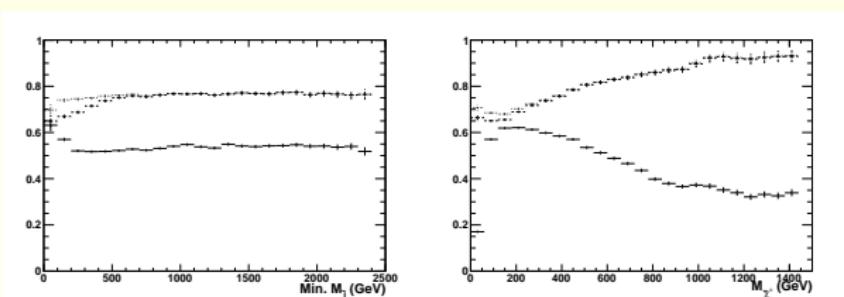
A. Arbey, M. Battaglia, F.M., arXiv:1110.3726



Implication of flavour observables on the pMSSM models



Flavour cuts disfavour masses below ~ 500 GeV for the gluino and the lightest scalar quark



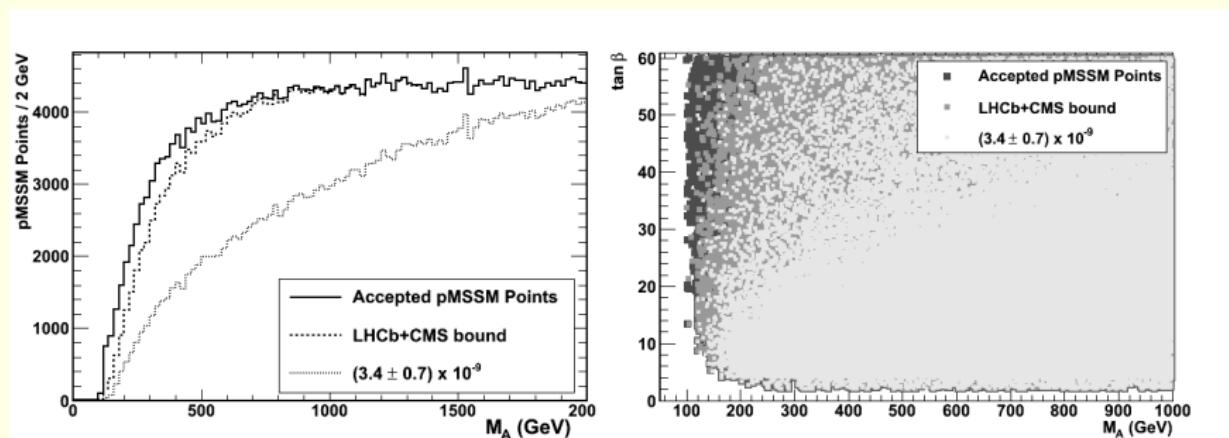
Sensitivity to M_A from $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$

Considering 2 scenarios:

- ▶ Current bound from LHCb+CMS + estimated th syst:

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) < 1.26 \times 10^{-8}$$

- ▶ SM like branching ratio with estimated 20% total uncertainty



Light M_A strongly constrained!



Beyond SUSY

An example: Warped extra dimensions (RS)

- ▶ A slice of anti-de Sitter spacetime in five dimensions (AdS_5)
- ▶ Fifth dimension ϕ compactified on a S^1/Z^2 orbifold
- ▶ Two branes : at orbifold fixed points $\phi = 0$ and $\phi = \pi$
- ▶ The warp factor acts as a conformal factor for the fields localized on the brane
→ Mass factors get rescaled by this factor
- ▶ Solves the hierarchy!
- ▶ Only the Higgs field is localized on the TeV brane while the rest of the SM fields are in the bulk
- ▶ Localization of fermions close to the TeV brane (overlap with the Higgs)
→ large Yukawa couplings
- ▶ Localization of fermions close to the Planck brane → small Yukawa couplings

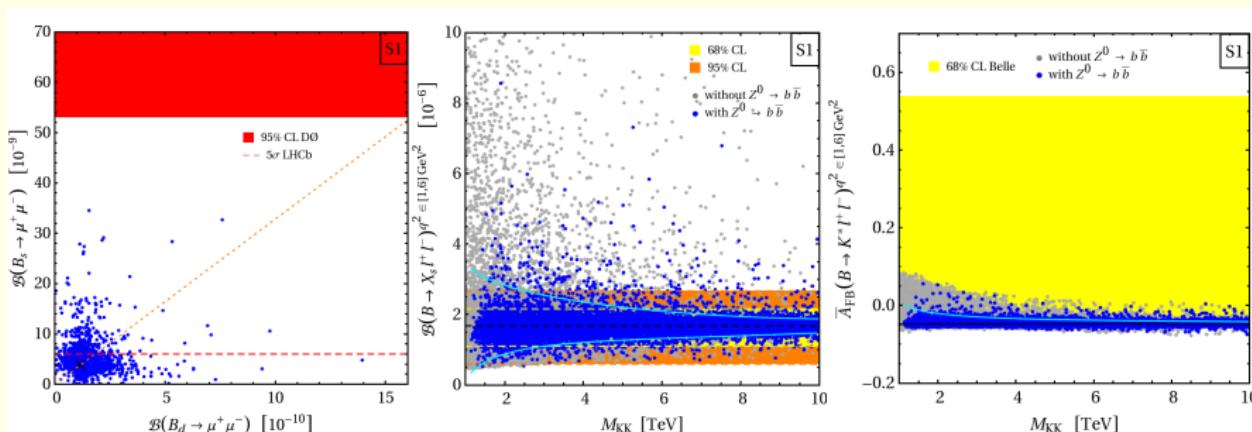
**Explains the hierarchies in fermion spectrum!
→ very attractive theory of flavour!**

Y. Grossman & M. Neubert, Phys.Lett. B474 (2000) 361; T. Gherghetta & A. Pomarol, Nucl.Phys. B586 (2000) 141
 S. Huber & Q. Shafi, Phys.Rev. D63 (2001) 045010; G. Burdman, Phys.Lett. B590 (2004) 86
 K. Agashe et al., Phys.Rev.Lett. 93 (2004) 201804; M. Bauer et al., JHEP 1009 (2010) 017



Warped extra dimensions (RS): benchmark scenario S1

Modified Wilson coefficients



Horizontal lines: SM values

Horizontal coloured bands: excluded ($B_s \rightarrow \mu^+ \mu^-$) / favoured (other decays) regions

Gray points: inconsistent with measured $Z^0 \rightarrow b\bar{b}$ at 99% C.L.

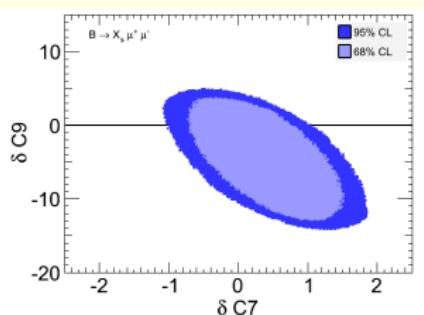
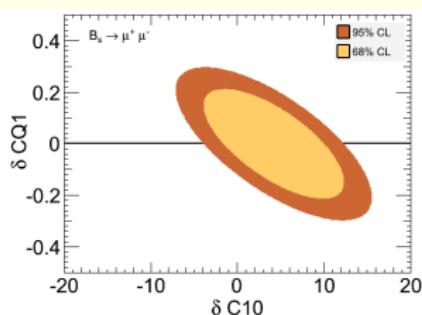
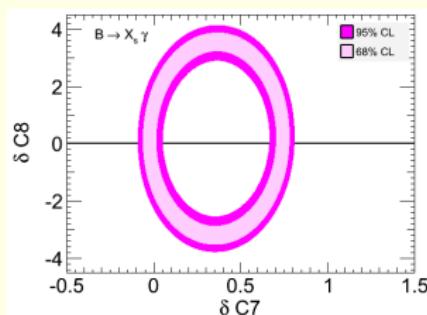
Blue points: consistent with measured $Z^0 \rightarrow b\bar{b}$ at 99% C.L.



Constraints on Wilson Coefficients

Use the existing limits/measurements to find the allowed intervals for the Wilson coefficients

Make predictions for other observables!



Guideline for model building!

T. Hurth, F.M., work in progress



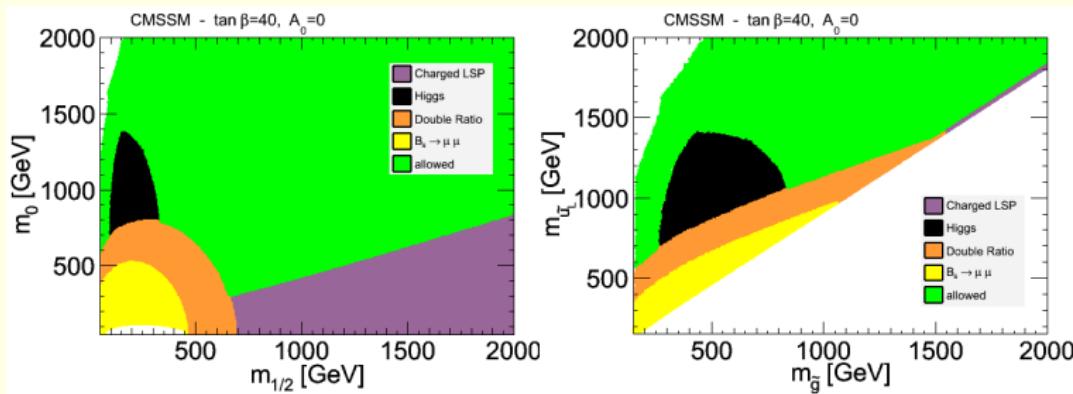
Conclusion

- ▶ Flavour physics plays a very important role in constraining BSM scenarios
- ▶ Brings valuable information when combined with the direct search data
- ▶ The constrained SUSY scenarios are highly constrained
- ▶ General MSSM: A lot of viable model points survive, but combining with other sectors, one can squeeze the parameter space
- ▶ Room for a lot of work in non-SUSY and/or model independent analyses

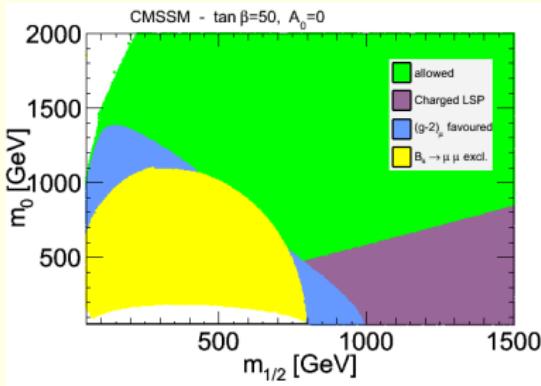
Backup

Backup

Constrained MSSM



Constrained MSSM



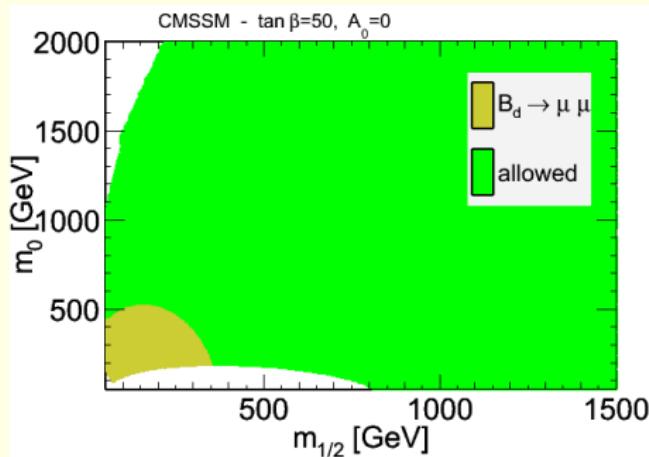
$\text{BR}(B_d \rightarrow \mu^+ \mu^-)$

Process similar to $B_s \rightarrow \mu^+ \mu^-$

CKM suppressed

SM prediction: $\text{BR}(B_d \rightarrow \mu^+ \mu^-) = (1.1 \pm 0.1) \times 10^{-10}$

LHCb limit: $\text{BR}(B_d \rightarrow \mu^+ \mu^-) < 5.1 \times 10^{-9}$ at 95% C.L.



pMSSM scans

Flat scans over the pMSSM 19 parameters.

- ▶ Spectrum generation (SoftSusy)
- ▶ Low energy observables (**SuperIso**)
- ▶ Dark matter (**SuperIso Relic**, Micromegas)
- ▶ SUSY and Higgs mass limits (SuperIso, HiggsBounds)
- ▶ Higgs and SUSY decays (HDECAY, Higlu, FeynHiggs, SDECAY)
- ▶ Event generation and cross sections (PYTHIA, Prospino)
- ▶ Detector simulation (Delphes)

$2.16 \times 10^{-4} < \text{BR}(B \rightarrow X_s \gamma) < 4.93 \times 10^{-4}$
$\text{BR}(B_s \rightarrow \mu^+ \mu^-) < 1.26 \times 10^{-8}$
$0.56 < R(B \rightarrow \tau \nu) < 2.70$
$4.7 \times 10^{-2} < \text{BR}(D_s \rightarrow \tau \nu) < 6.1 \times 10^{-2}$
$2.9 \times 10^{-3} < \text{BR}(B \rightarrow D^0 \tau \nu) < 14.2 \times 10^{-3}$
$0.985 < R_{\mu 23}(K \rightarrow \mu \nu) < 1.013$
$-2.4 \times 10^{-9} < \delta a_\mu < 4.5 \times 10^{-9}$
$10^{-4} < \Omega_\chi h^2 < 0.135$
+ sparticle mass upper bounds
+ Higgs search limits

pMSSM scans

Parameter	Range
$\tan \beta$	[1, 60]
M_A	[50, 2000]
M_1	[-2500, 2500]
M_2	[-2500, 2500]
M_3	[50, 2500]
$A_d = A_s = A_b$	[-2000, 2000]
$A_u = A_c = A_t$	[-2000, 2000]
$A_e = A_\mu = A_\tau$	[-2000, 2000]
μ	[-1000, 2000]
$M_{\tilde{e}_L} = M_{\tilde{\mu}_L}$	[50, 2500]
$M_{\tilde{e}_R} = M_{\tilde{\mu}_R}$	[50, 2500]
$M_{\tilde{\tau}_L}$	[50, 2500]
$M_{\tilde{\tau}_R}$	[50, 2500]
$M_{\tilde{q}_{1L}} = M_{\tilde{q}_{2L}}$	[50, 2500]
$M_{\tilde{q}_{3L}}$	[50, 2500]
$M_{\tilde{u}_R} = M_{\tilde{c}_R}$	[50, 2500]
$M_{\tilde{t}_R}$	[50, 2500]
$M_{\tilde{d}_R} = M_{\tilde{s}_R}$	[50, 2500]
$M_{\tilde{b}_R}$	[50, 2500]

Selection	pMSSM points	Selection Efficiency	Cumulative Efficiency
Generated Points	24.57M	1	1
Valid Spectra	9.41M	0.383	0.383
$\tilde{\chi}_1^0$ LSP and Mass Limits	2.62M	0.278	0.107
Higgs Limits	1.81M	0.691	0.074
Flavour and $g_\mu - 2$	1.34M	0.743	0.055
$\Omega_\chi h^2$	897k	0.668	0.037
Successfull Simulation	835k	0.931	0.034