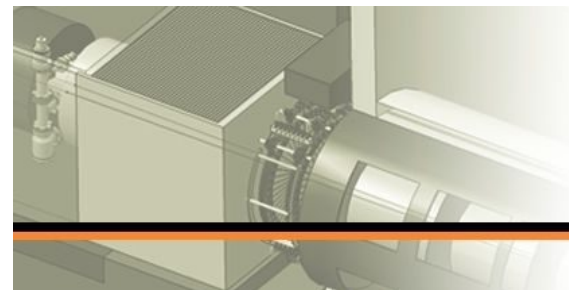
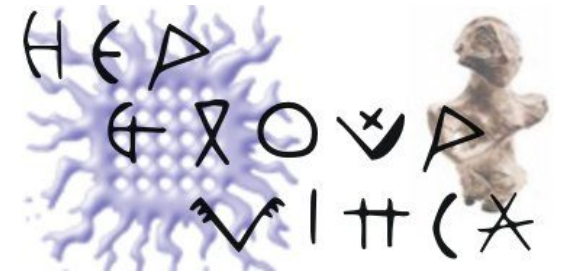


# CLIC and the BHSE

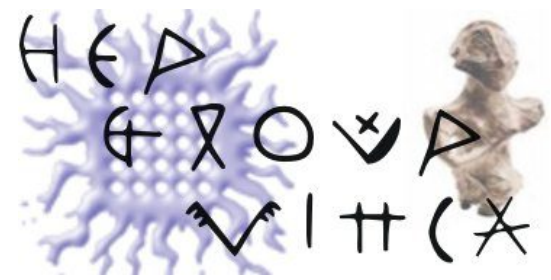
S. Lukić - HEP Group Vinča  
CERN meeting, November 2011



# Summary



- Method of analysis
- BHSE at CLIC, difficulties and possibilities



Guinea-PIG (v1.4.1)  
e<sup>-</sup>e<sup>+</sup> collision pairs –  
incoming momenta  $p_1, p_2$   
(collision axis,  $\sqrt{s'}$ , CM frame)

$\mathcal{R} < w f(s/s')$  ?  
no

yes

Calculate the collision axis  
in the CM frame

Rotate and scale the outgoing  
momenta in the CM frame, then  
boost back to the lab frame

output

Track...

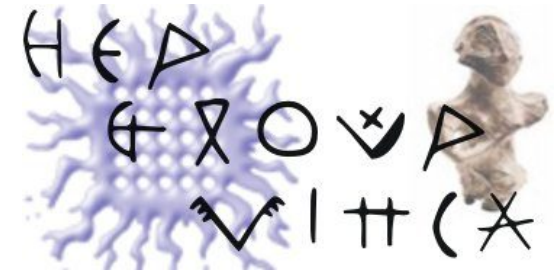
output

BHLUMI / BHWIDE  
Bhabha outgoing momenta  
fixed  $\sqrt{s}$ ,  
fixed collision axis

output



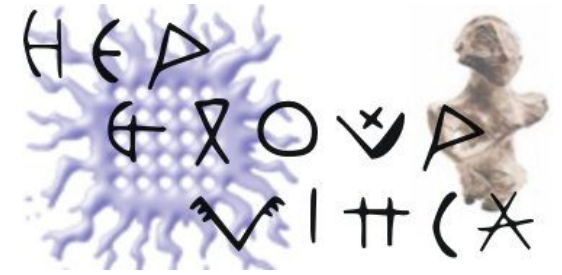
# Underlying assumptions



1.  $\sigma(\sqrt{s}) \sim f(\sqrt{s})$  (hopefully simple & analytical)
  2.  $\sigma(\sqrt{s}, \Omega) = \sigma(\sqrt{s}) g(\Omega)$
  3.  $\sigma(\sqrt{s}, E_{out}) = \sigma(\sqrt{s}) h(E_{out}/\sqrt{s})$
- ILC: All valid to a very good approximation  
(see I. Sadeh webpage: <http://alzt.tau.ac.il/~sadeh/bhabhaXs.html>)
  - CLIC: Tested by I. Smiljanić ([http://www.vin.bg.ac.rs/hep/Ivan/x-section\\_vs\\_energy\\_CLIC/Bh\\_Xsec\\_E\\_CLIC.htm](http://www.vin.bg.ac.rs/hep/Ivan/x-section_vs_energy_CLIC/Bh_Xsec_E_CLIC.htm))
    1.  $\sigma(\sqrt{s}) \sim s^{-0.9891}$  ;  $250 \text{ GeV} < \sqrt{s} \leq 3 \text{ TeV}$ ; excellent fit
    2. Agreement within statistical errors ( $5 \times 10^5$  events at each energy)
    3. Significant differences in  $h(E_{out}/\sqrt{s})$  at different  $\sqrt{s}$

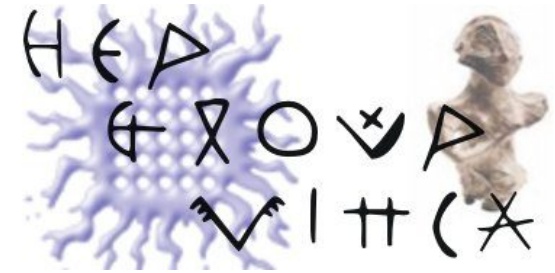


# Simulation

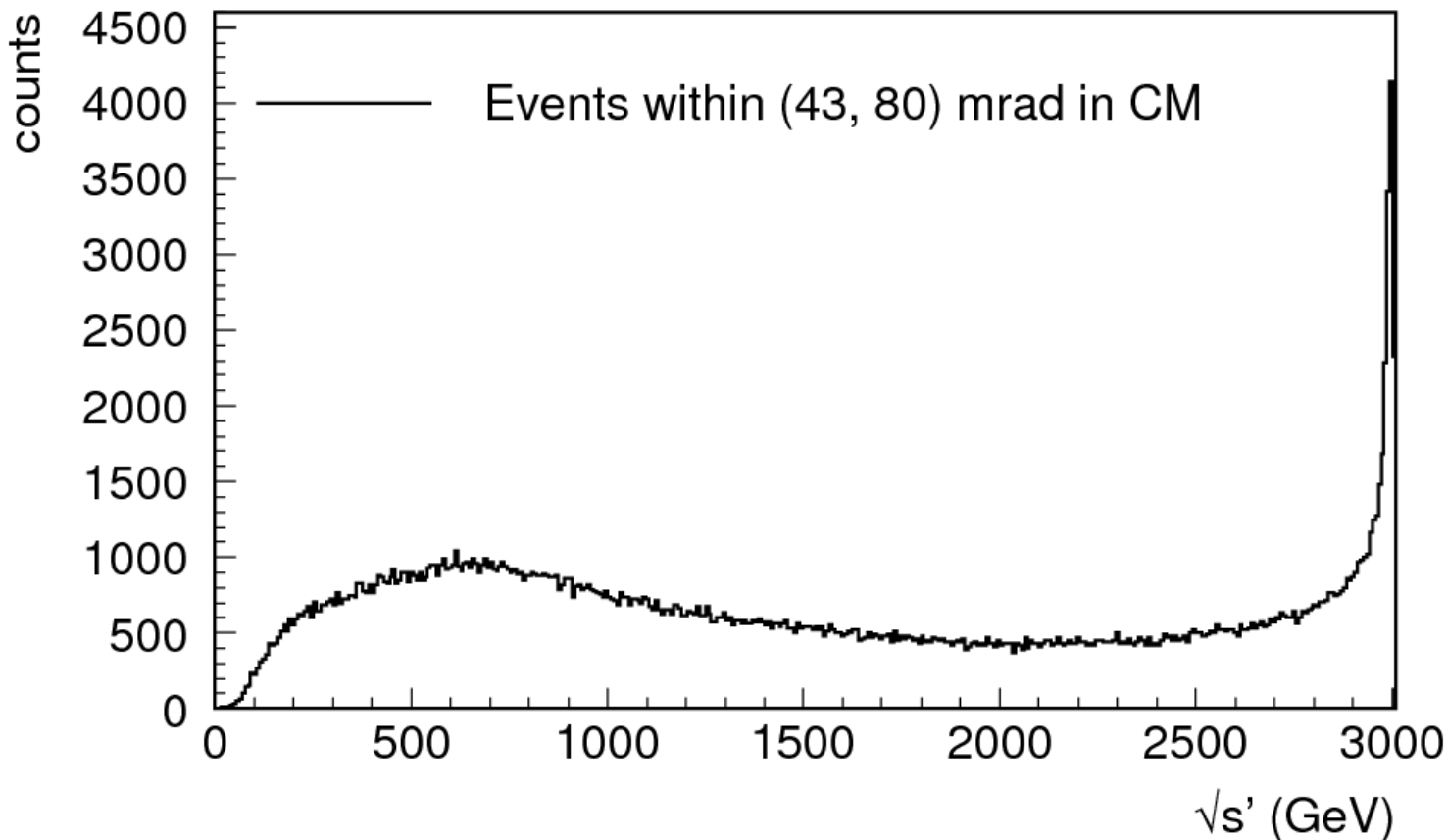


- Realistic beam profiles
- Individual bunches only!
- Scaling of the Bhabha cross section with  $(s/s')^{0.9891}$

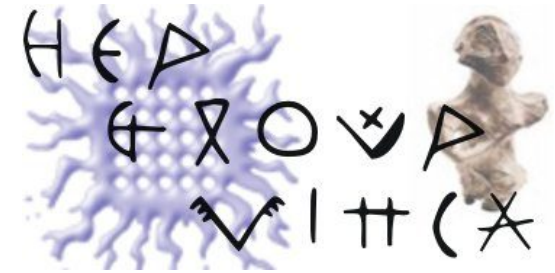
# Beamstrahlung



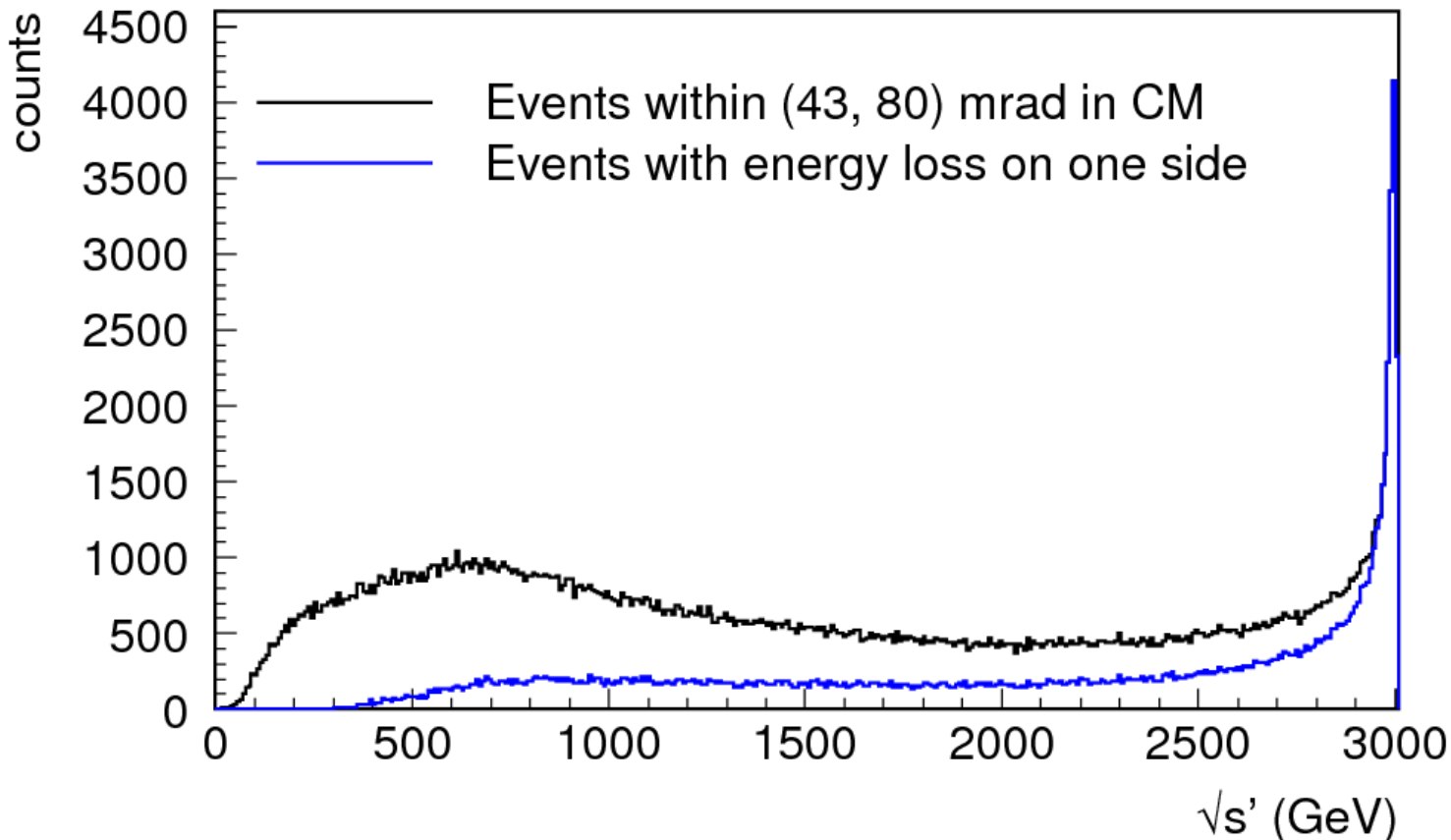
- $\sqrt{s'}$  spectrum of the Bhabha events (luminosity spectrum times  $s/s'$ )



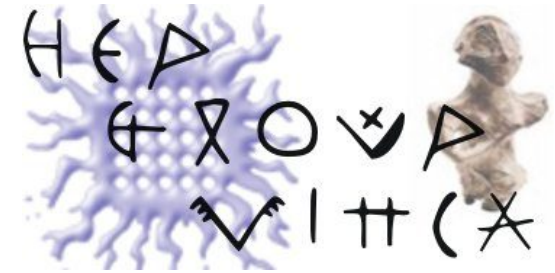
# Beamstrahlung



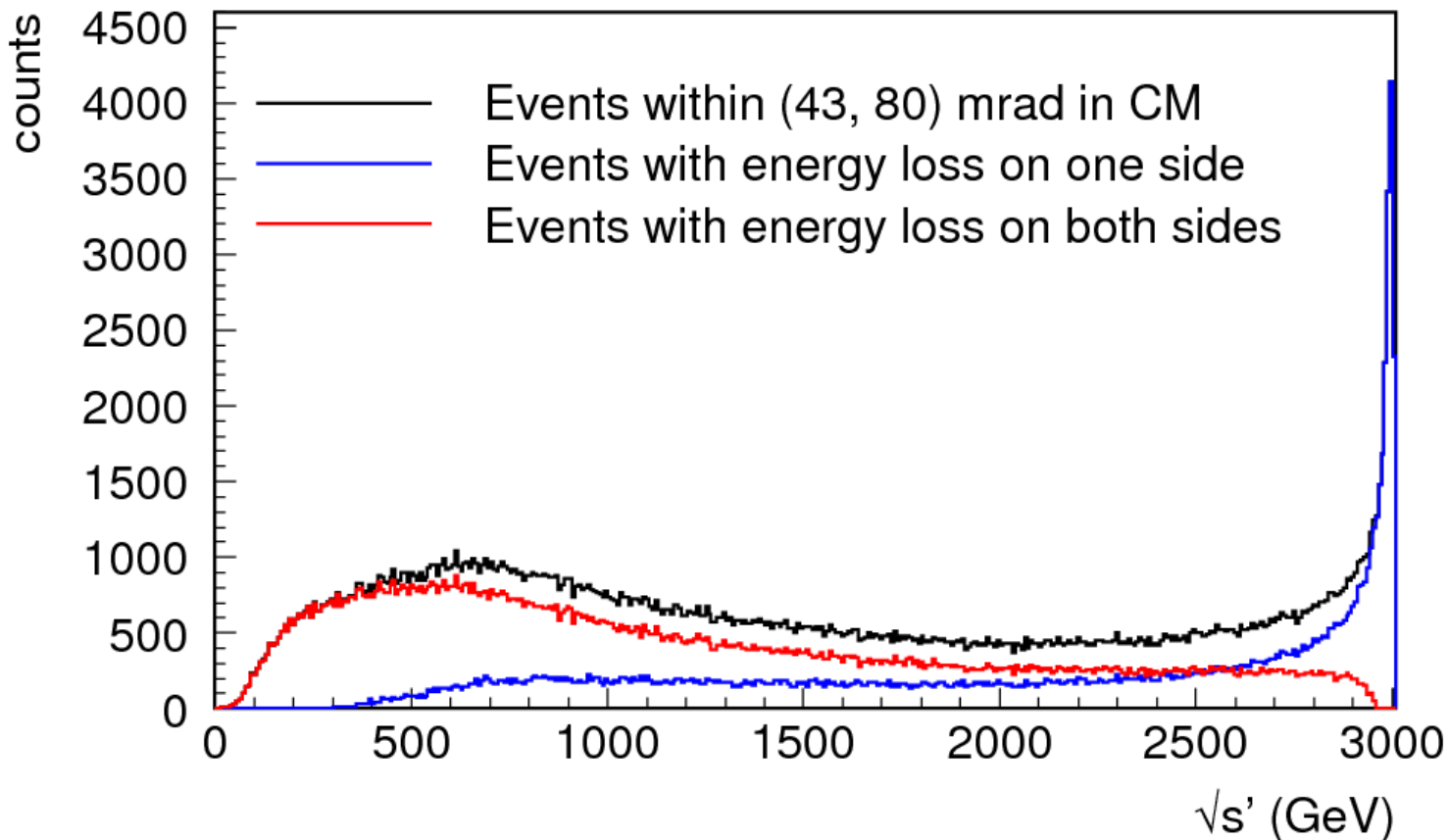
- $\sqrt{s'}$  spectrum of the Bhabha events (luminosity spectrum times  $s/s'$ )



# Beamstrahlung

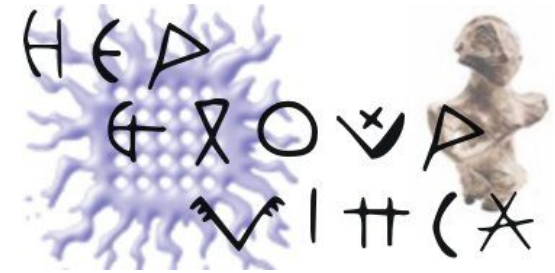


- $\sqrt{s'}$  can not be reconstructed from polar angles only – particle energy reconstruction in LumiCal important!

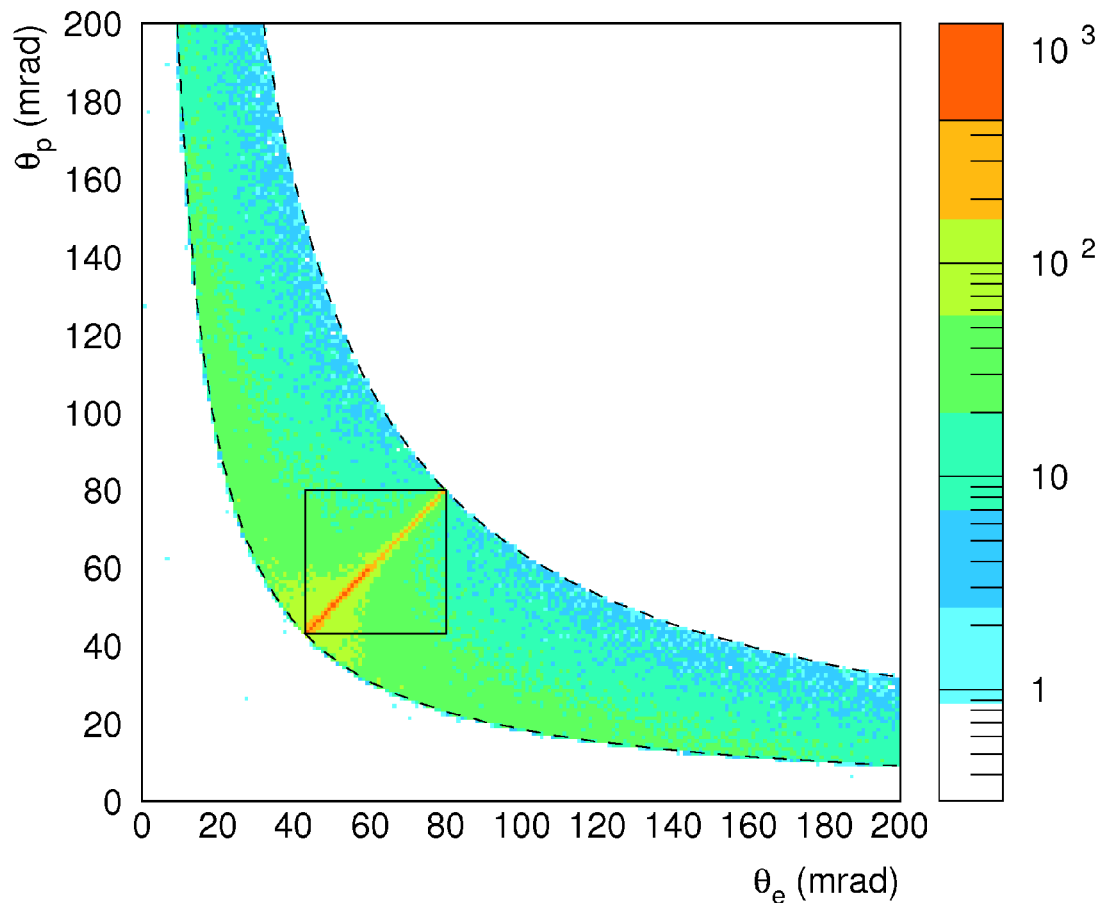




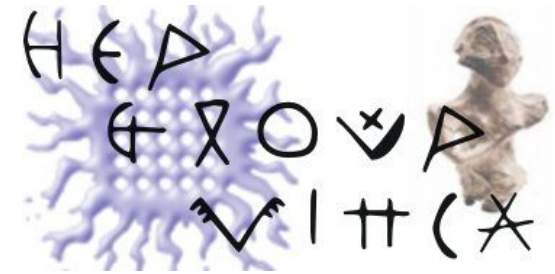
# Polar angles



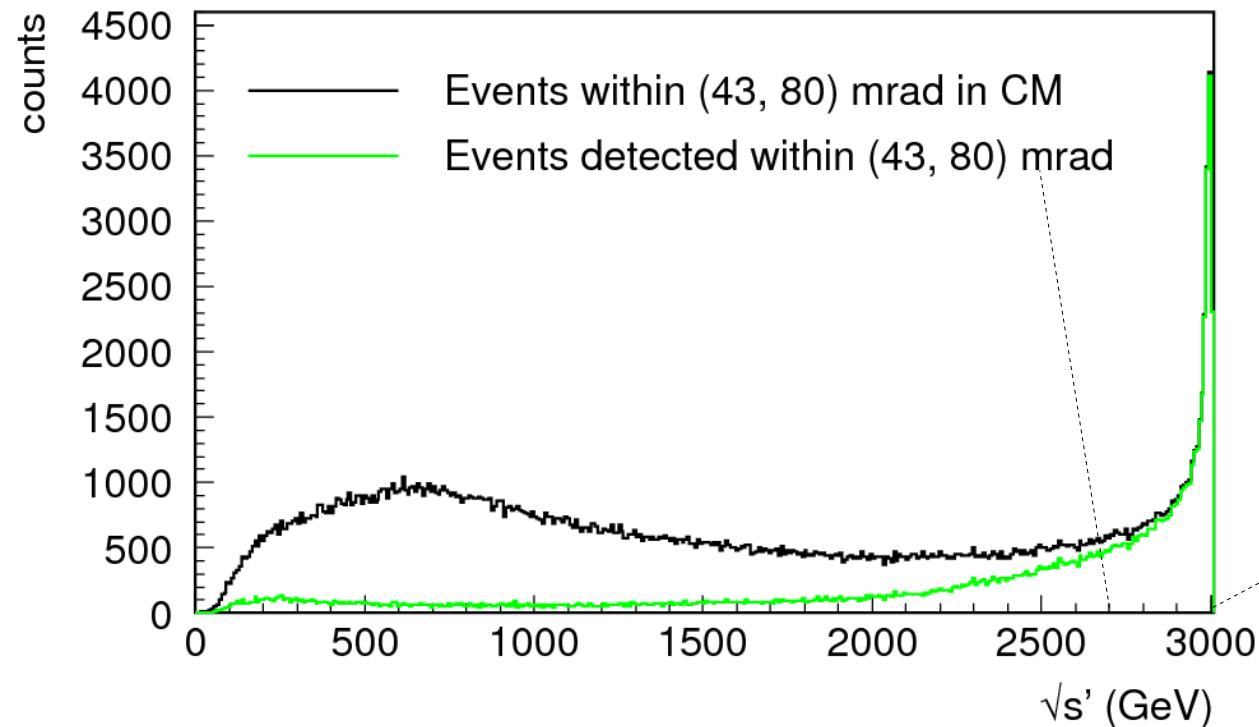
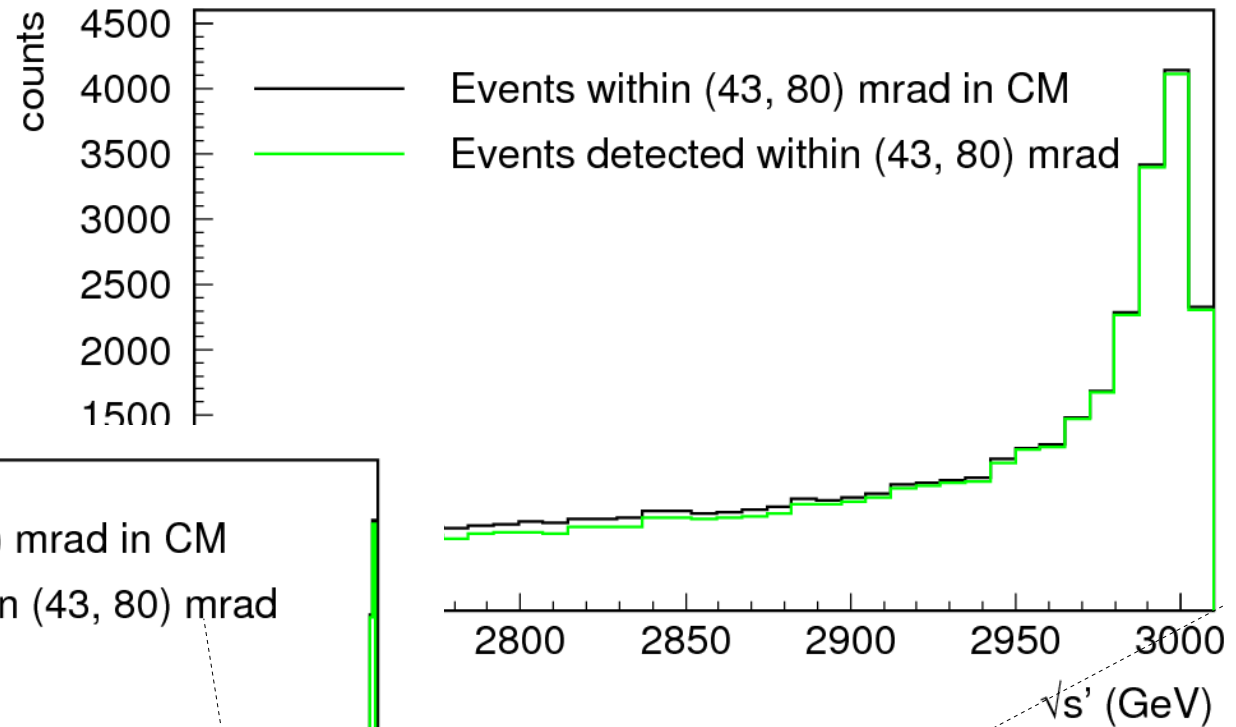
- BHSE 76.4 % ( $E_{rel}$  + fiducial volume)
- Needs to be more reliably estimated and corrected
- Energy-differential luminosity essential



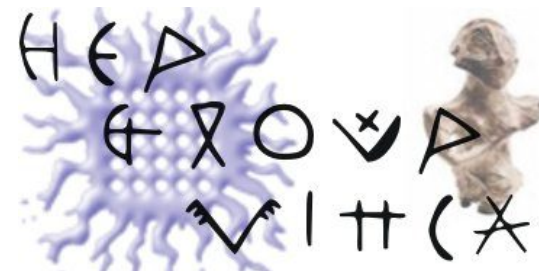
# Energy differential BHSE



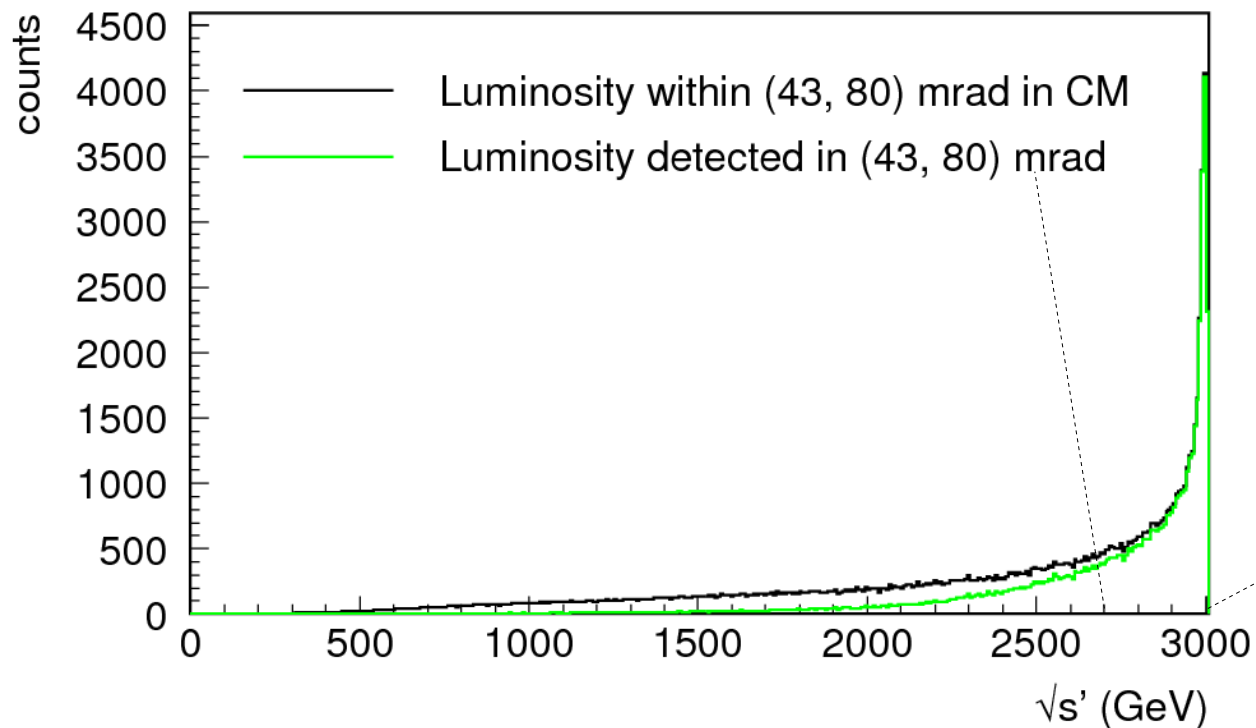
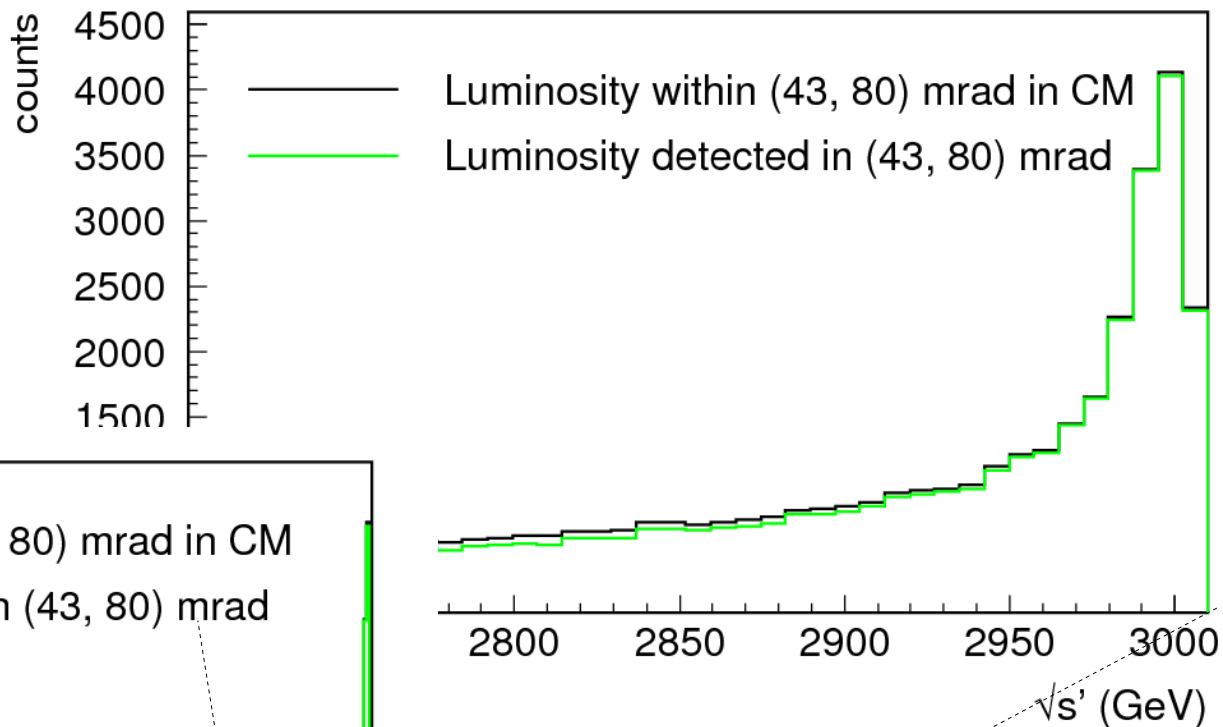
- Large losses only at lower CM energies



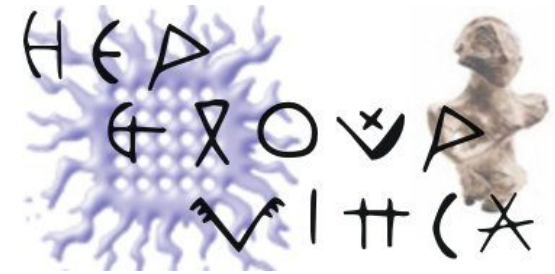
# Energy differential BHSE



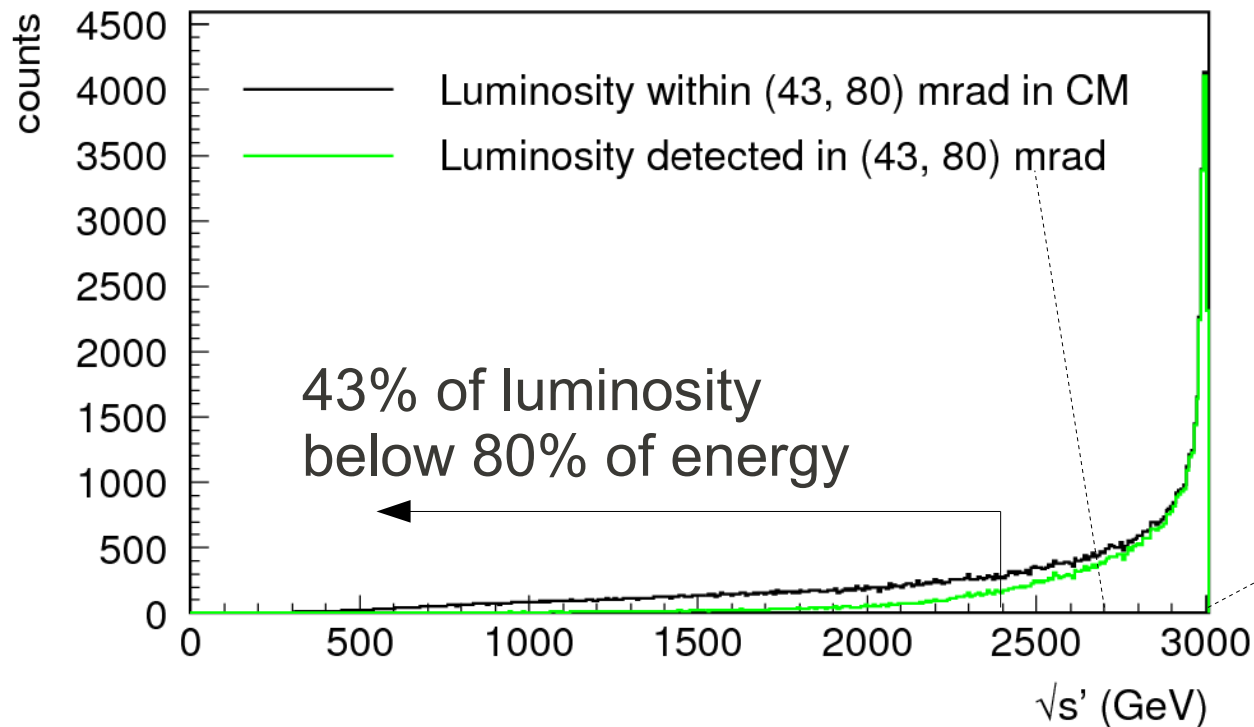
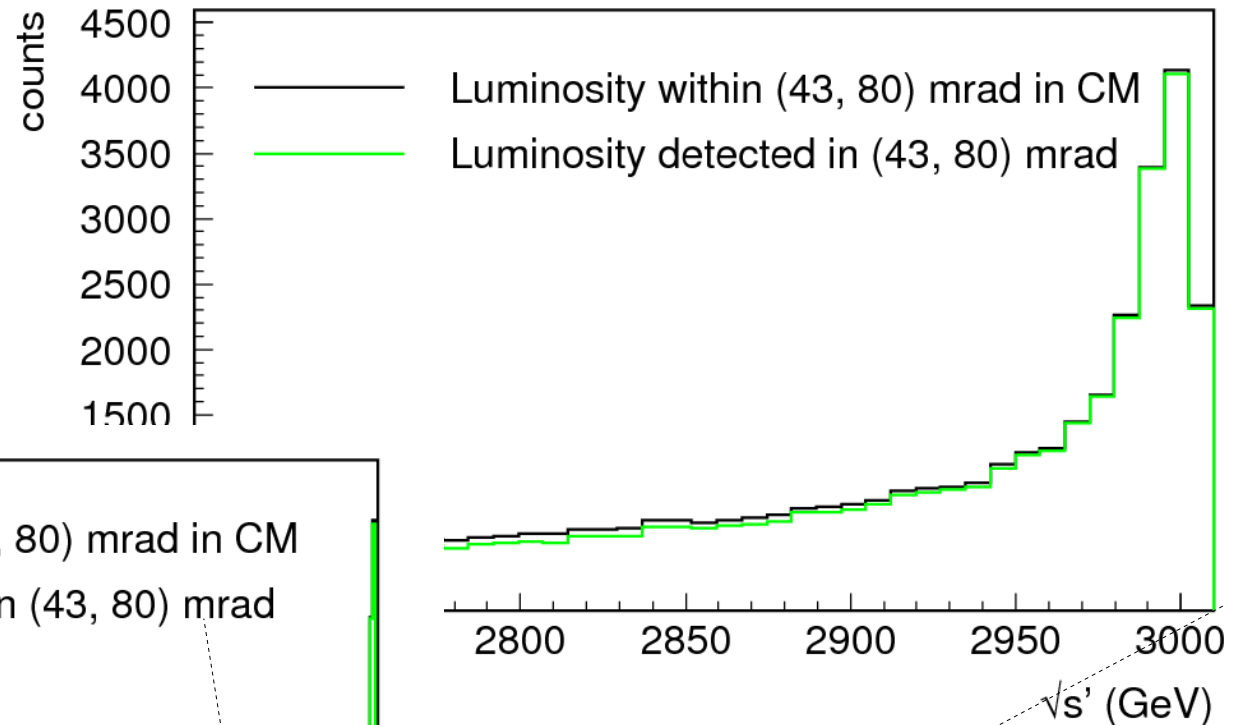
- Luminosity spectrum as reconstructed from the Bhabha particles (not corrected for the ISR)



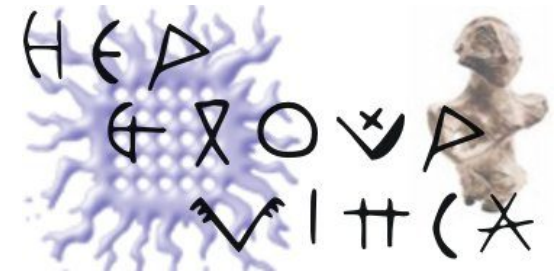
# Energy differential BHSE



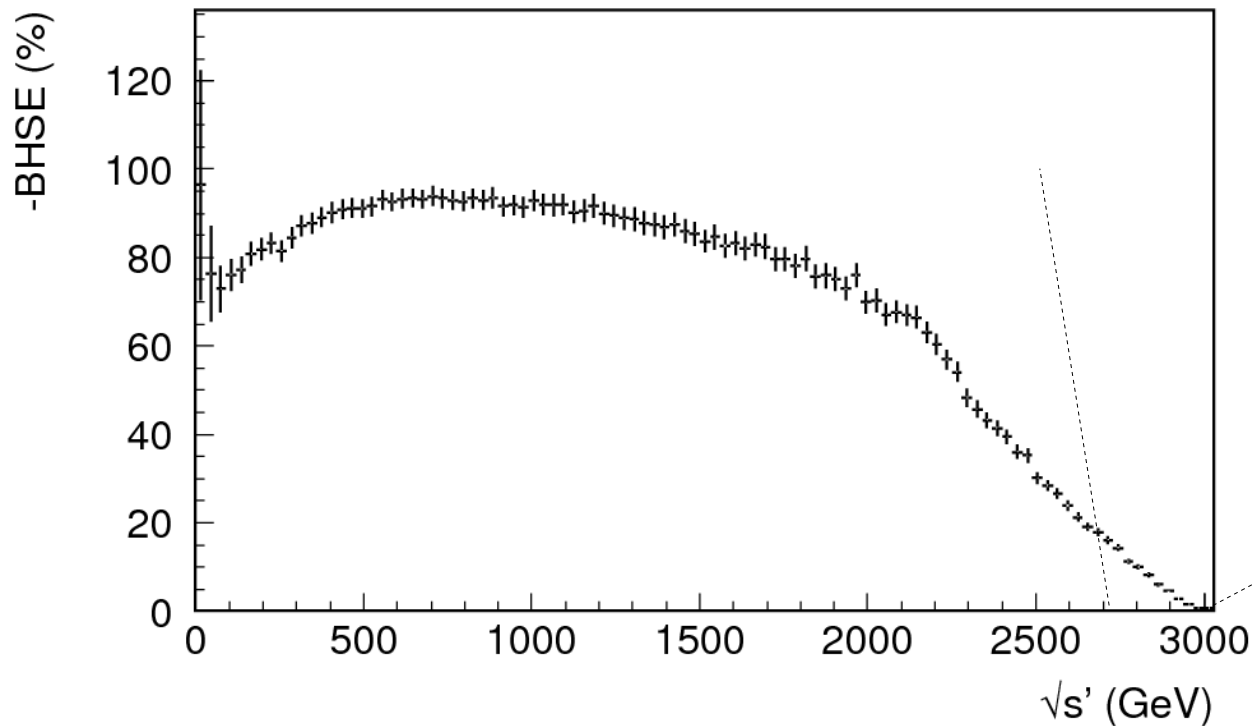
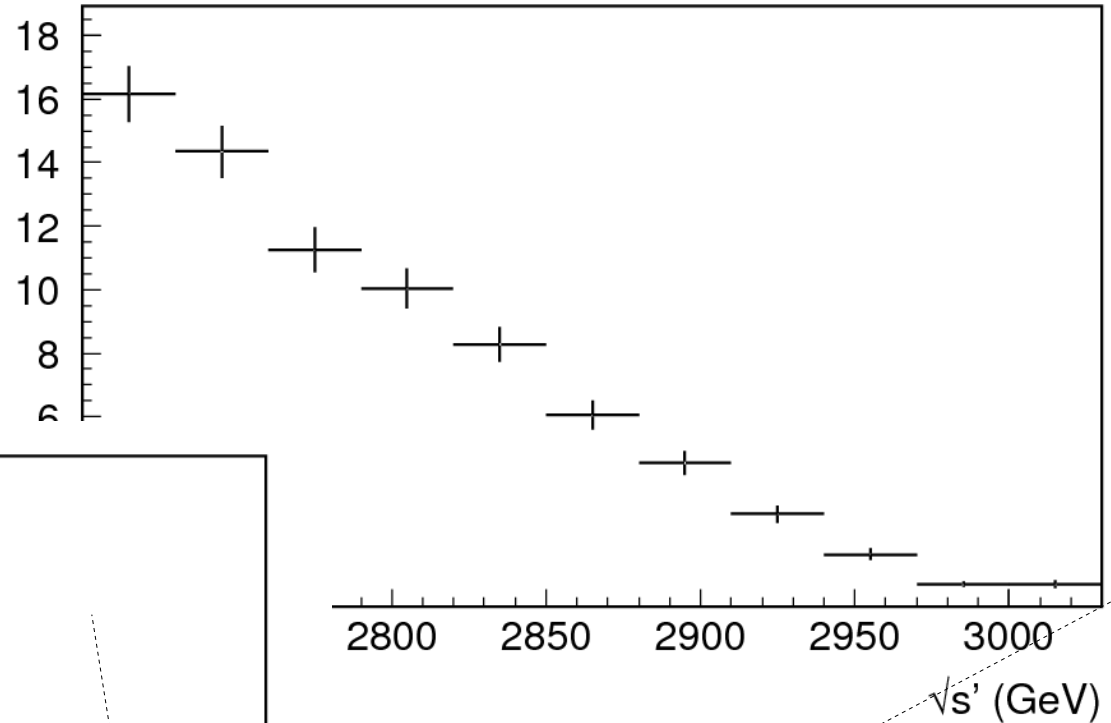
- Luminosity spectrum as reconstructed from the Bhabha particles (not corrected for the ISR)



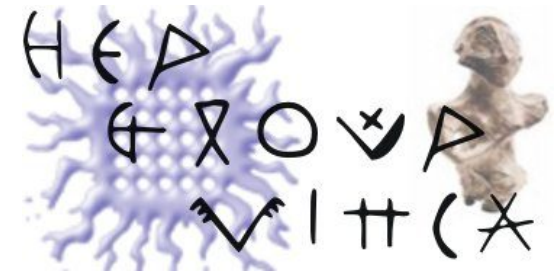
# Energy differential BHSE



- 0.71 % in the “last 1% of energy” (2970-3000 GeV bin) <sup>-BHSE (%)</sup>
- Over 90% at 500 GeV

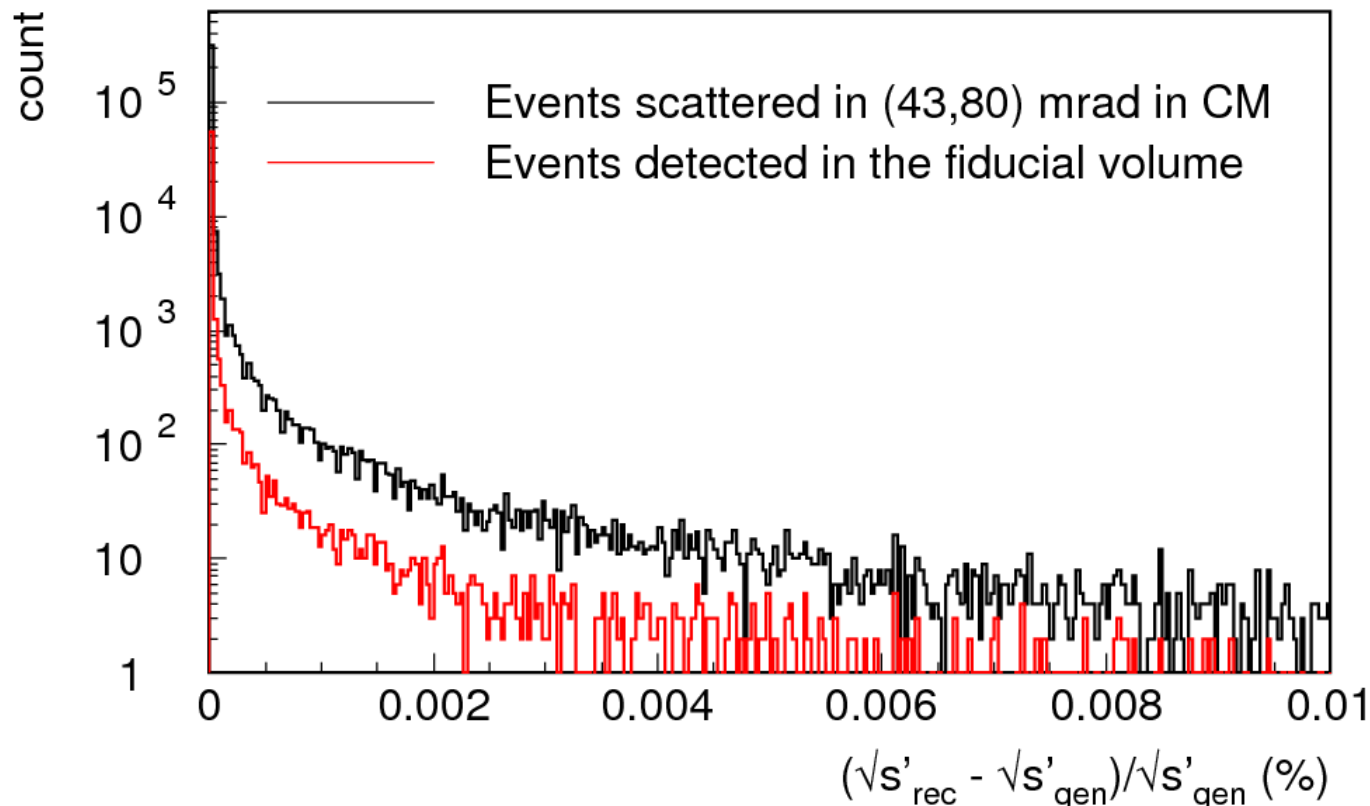


# Reconstruction of $s'$

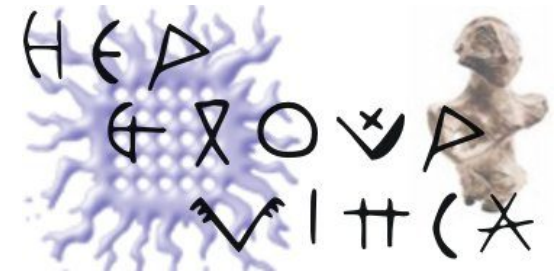


- $$s' = (E_1 + E_2)^2 - (p_1 + p_2)^2 \approx 2E_1E_2(1 - \cos\alpha_{1,2})$$
$$= 2E_1E_2(1 + \cos(\varphi_1 - \varphi_2) \sin\theta_1 \sin\theta_2 + \cos\theta_1 \cos\theta_2)$$
$$\approx 2E_1E_2(1 + \cos(\theta_1 - \theta_2))$$

( $\theta_2, \varphi_2$  defined in the mirror-inverted frame)



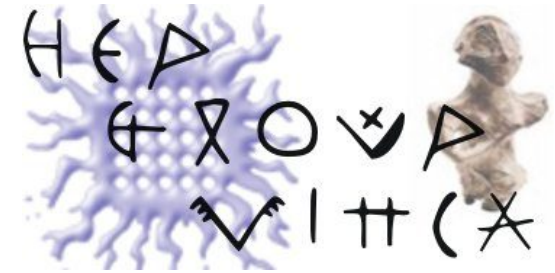
# Reconstruction of $s$



- Precise information on  $\varphi_{1,2}$  inaccessible to the measurement, but with  $\cos(\varphi_1 - \varphi_2) = 1$  the approximation error is negligible
- Influence of  $\theta$  resolution negligible
- $\sqrt{s}$  uncertainty is of the order of the resolution of the final particle energy (1% - 1.5%, depending on the energy - see talk by **J. Aguilar at TIPP 2011**)
- $\sqrt{s}$  spectrum distortion by the ISR in the Bhabha scattering
- Which level of detail in the description of the luminosity spectrum do we need (energy binning)?



# Conclusions



- The luminosity spectrum at CLIC extends down to almost zero CM energy
- The differential luminosity at lower energies difficult to precisely measure because of the high BHSE (and the background spectrum)
- BHSE at energies close to  $2E_{beam}$  is rather low
- Energy reconstruction capability of the LumiCal is crucial for the  $\sqrt{s}$  reconstruction at CLIC
- Integration of BHWIDE or BHLUMI necessary in order to make Guinea-PIG a precision tool for the analysis of Luminosity measurement at CLIC
- CLIC train structure should be simulated

