

Susy SeeSaw: from EDM to Leptogenesis

Isabella Mazzini (CERN)

Meeting on Particle Physics Phenomenology, CERN, 29/06/07



Q: if observed, is d_e ss compatible with thermal leptogenesis?

[F.R.Joaquim, IM and A.Riotto, hep-ph/0701270]

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yes
A: no

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OUTLINE:

- γ_B vs d_e // th leptg // d_e ss // Method // **A:** yes no // Conclusions

$$\gamma_B = n_B/s$$

macroscopic cosmological observable
(n_B =baryon number asymm, s =entropy density)

Need 3 Sakharov's:

i) dev th eq, ii) BV, iii) CV, CPV

Need:

CPV, PV

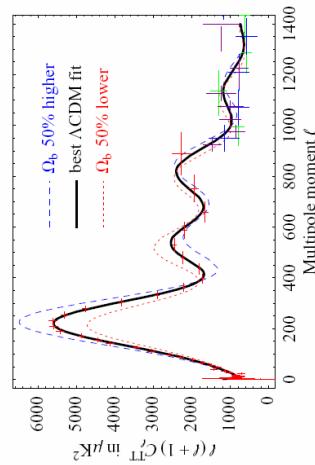
$$d_e$$

property of elementary particle
(like mass, spin, charge, MDM)



Norman Ramsey
Separated Oscillator Beam Resonance
Nobel Prize 1989 STANDARD OF TIME

Lab exp searches
in progress since
50's!



Determined by
WMAP-CMB
(& BBN)

$$\gamma_B = (8.7 \pm 0.3) \times 10^{-11}$$

$$d_e < 1.6 \times 10^{-27} \text{ e cm}$$

*A Permanent EDM Violates both
 T & P Symmetries:*

$$H = -d\vec{\sigma} \cdot \vec{E} \xrightarrow{T} H = -d(-\vec{\sigma}) \cdot \vec{E} = d\vec{\sigma} \cdot \vec{E}$$

$$H = -d\vec{\sigma} \cdot \vec{E} \xrightarrow{P} H = -d\vec{\sigma} \cdot (-\vec{E}) = d\vec{\sigma} \cdot \vec{E}$$

MDMs are Allowed...

$$H = -\mu\vec{\sigma} \cdot \vec{B} \xrightarrow{T} H = -\mu(-\vec{\sigma}) \cdot (-\vec{B}) = -\mu\vec{\sigma} \cdot \vec{B}$$

$$H = -\mu\vec{\sigma} \cdot \vec{B} \xrightarrow{P} H = -\mu(\vec{\sigma}) \cdot (\vec{B}) = -\mu\vec{\sigma} \cdot \vec{B}$$

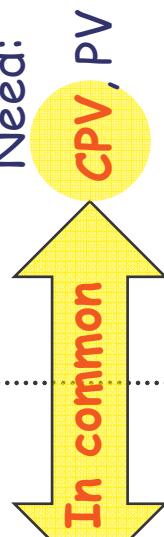
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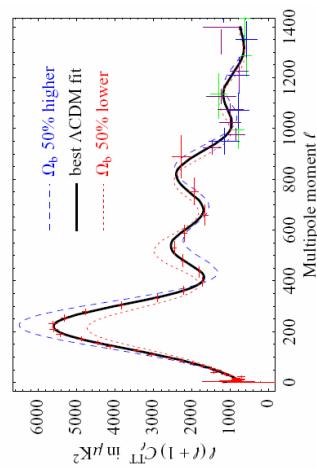
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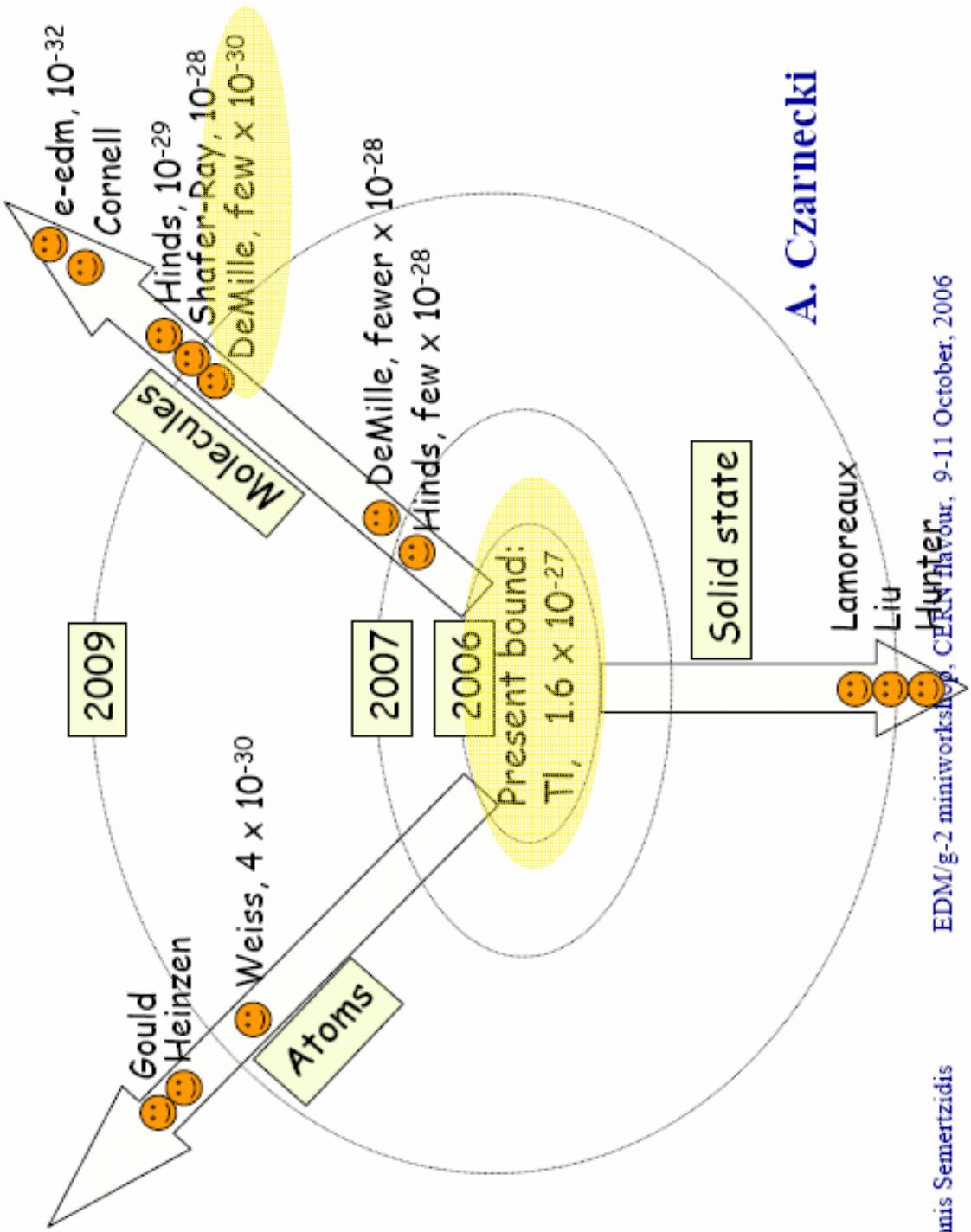


Determined by
WMAP-CMB
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$$\gamma_B = (8.7 \pm 0.3) \times 10^{-11}$$

$$d_e < 1.6 \times 10^{-27} e \text{ cm}$$

A forecast: electron EDM



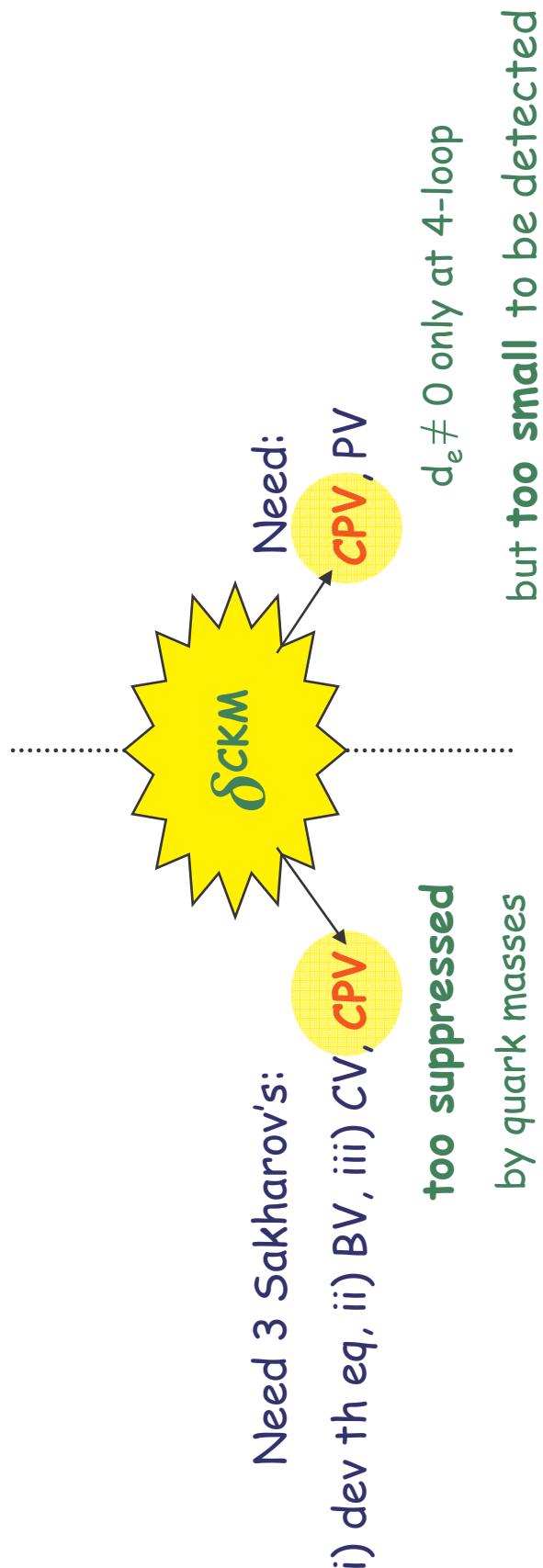
Yannis Semertzidis

EDM/g-2 miniworkshop, CERN Haïfa, 9-11 October, 2006

A. Czarnecki

$$\gamma_B = n_B/s$$

$$d_e$$

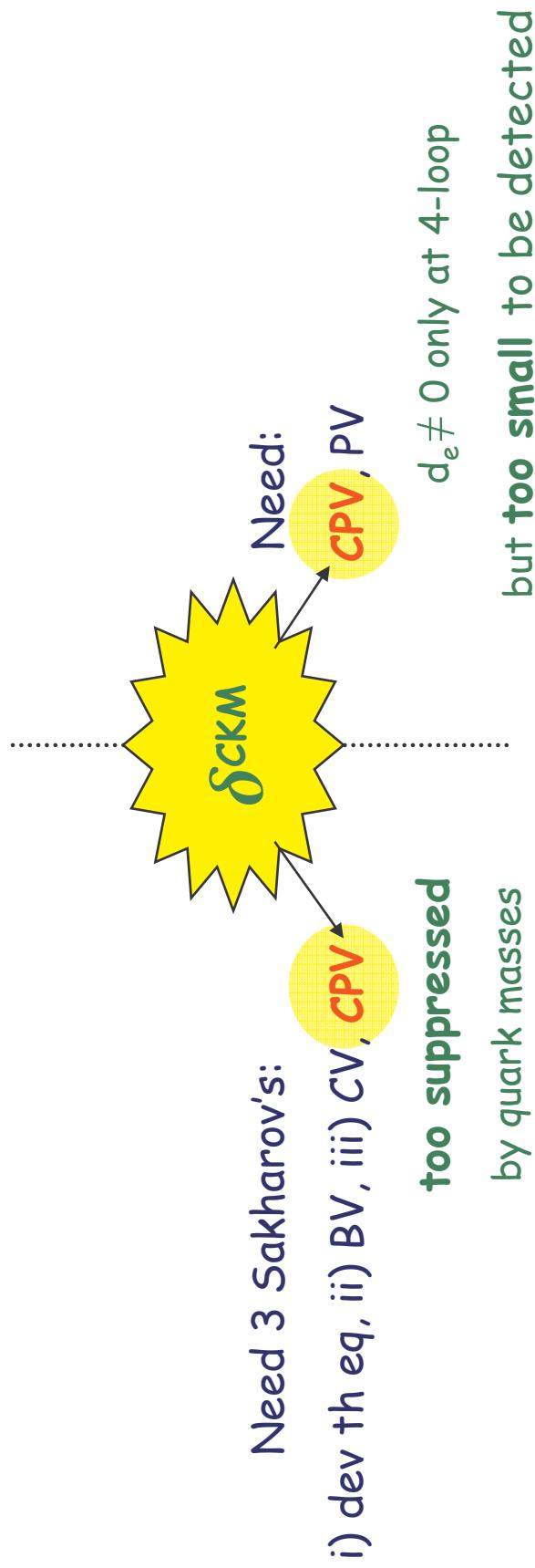


$d_e \neq 0$ only at 4-loop
but **too small** to be detected

**SM CANNOT DO
THE JOB**

$$\gamma_B = n_B/s$$

$$d_e$$



STRONG CP PROBLEM:

$$\mathcal{L}_{d \leq 4} \supset \bar{\theta} \frac{g_s^2}{32\pi^2} G^a \tilde{G}^a$$

($\theta = 0$ with PQ symm)

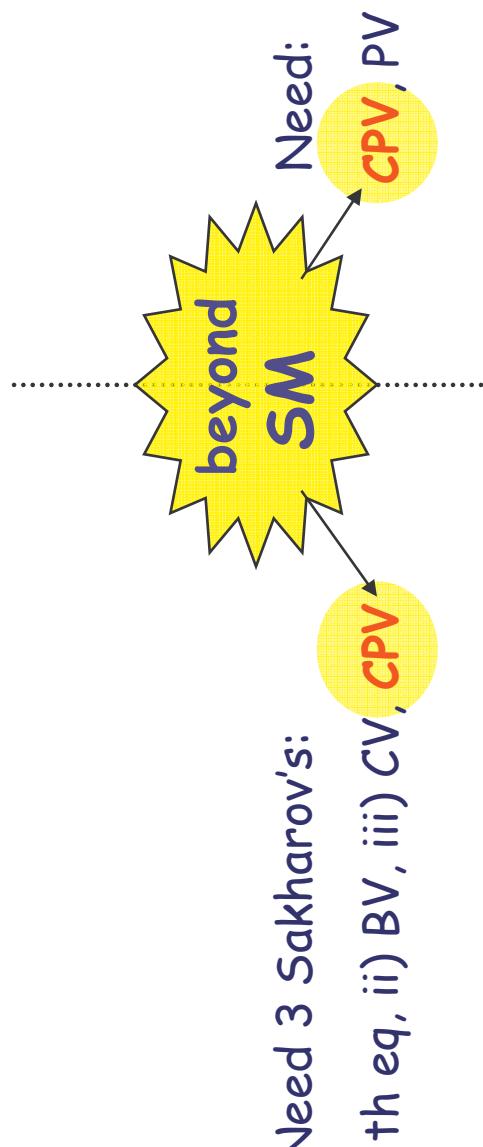
$$d_{\tau_l} < 1.5 \times 10^{-26} \text{ e cm} \rightarrow \theta < 10^{-10}, \text{ hence } d_{\tau_l} < 10^{-30} \text{ e cm}$$

$$d_{\tau_l} = -585 d_e + d(\theta)$$

If d_{τ_l} is measured, it is actually d_e !

$$\gamma_B = n_B/s$$

$$d_e$$



New physics is required to explain

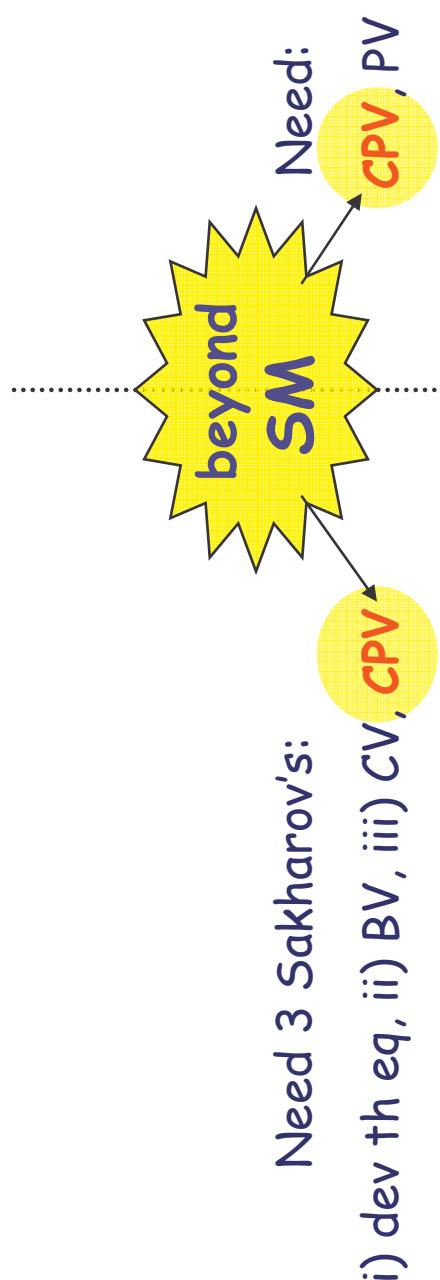
$$m_\nu = U^* m_\nu^d U^+$$

Spectrum:
NH or IH?

MNS: 2 large
angles and 3
CPV phases

$$\gamma_B = n_B/s$$

$$d_e \quad vs$$



Simplest: try with seesaw yukawas ! [P.Minkowski '77]

The seesaw

[P.Minkowski '77]

In addition to SM: take 3 RH neutrinos N
 (nicely fit into 16 of $SO(10)$)

(like other ch fermions)
Dirac-Yukawa

(L_{tot} viol)
Majorana-mass

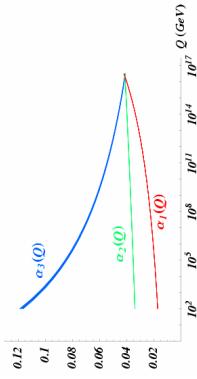


$$L_{SS} = N Y_\nu v H_u + N M_R N$$

$$\text{I.e. } L_{SS} = v \underbrace{Y_\nu^\top M_R^{-1} Y_\nu}_{M_\nu} v^2$$

$m_\nu \leftarrow \text{diag}'d$ by U_{MNS}

$m_\nu = O(eV) \rightarrow M_R = O(10^{15} \text{GeV})$, near SUSY g.c.u.!



$$\gamma_B = n_B/s$$

$$d_e \quad vs$$

Need 3 Sakharov's:
 i) dev th eq, ii) BV, iii) CV, CPV

beyond SM
 Need:
 CPV, PV

Simplest: try with seesaw yukawas ! [P.Minkowski '77]

$$\mathcal{L}_{ss} = N Y_\nu \nu H_u + N M_R N \rightarrow \nu Y_\nu^\top M_R^{-1} Y_\nu v^2 v$$

[Casas Ibarra '01]

$$R^\top R = 1$$

$$m_\nu = U^* m_\nu d^+ U^+$$

R as dominance matrix
 [Lavignac IM Savoy'02]

$$E.g. \quad R = \begin{pmatrix} m_1 & m_2 & m_3 \\ 0 & 0 & 1 \\ m_2 & 0 & 1 \\ m_3 & 1 & 0 \end{pmatrix}$$

$$M_1 \approx M_2 \approx M_3$$

$$\gamma_B = n_B/s$$

$$d_e \quad vs$$

Need 3 Sakharov's:
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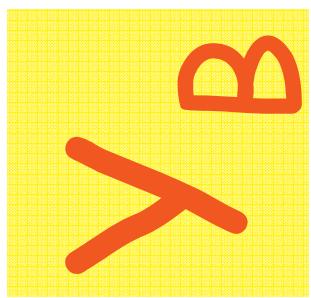
$$\mathcal{L}_{ss} = N Y_\nu v H_u + N M_R N \rightarrow v Y_\nu^\top \underbrace{M_R^{-1} Y_\nu}_{{R^\top R=1}} v$$

$$m_\nu = U^* m_\nu d U^+$$

[Casas Ibarra '01]

$$\epsilon_1^\ell \propto M_1 \frac{Im(\sum_{\beta\rho} m_\beta^{1/2} m_\rho^{3/2} U_{\ell\rho}^* U_{\ell\beta} R_{1\beta} R_{1\rho})}{\sum_\beta m_\beta |R_{1\beta}|^2}$$

$$C_{ij}^k = Y_\nu^* k_i Y_\nu k_j \ln \frac{M_{Pl}}{M_k}$$



γ_B

Flavored ($\ell = e, \mu, \tau$) + leptogenesis

[Fukugita Yanagida '86]

At $T \sim M_1$ decays of (the highest) $N_1 \rightarrow L_\ell H$

out of eq if $\Gamma_1 < H(M_1)$: CPV in γ generate $\Delta\ell$: later converted to ΔB by SM sphalerons

$$\epsilon_1^\ell \propto M_1 \frac{Im(\sum_{\beta\rho} m_\beta^{1/2} m_\rho^{3/2} U_{\ell\beta}^* U_{\ell\rho} R_{1\beta} R_{1\rho})}{\sum_\beta m_\beta |R_{1\beta}|^2}$$

efficiency factor (N_1 inverse decays tend to maintain the eq)

ℓ in eq. (susy case)

$$\frac{n_B}{n_\gamma} \approx \sum_\ell \frac{\epsilon_1^\ell \eta_\ell}{g_{\text{SM}}}$$

$$\left\{ \begin{array}{ll} \mu, \tau & (1+\tan^2\beta) 10^5 < M_1 [\text{GeV}] < (1+\tan^2\beta) 10^9 \\ \tau & (1+\tan^2\beta) 10^9 < M_1 [\text{GeV}] < (1+\tan^2\beta) 10^{12} \\ \text{none} & M_1 [\text{GeV}] > (1+\tan^2\beta) 10^{12} \\ & (\text{1-flav OK}) \end{array} \right.$$

γ_B

Flavored ($\ell = e, \mu, \tau$) RH leptogenesis

[Fukugita Yanagida '86]

$$\epsilon_1^\ell \propto M_1 \frac{Im(\sum_{\beta\rho} m_\beta^{1/2} m_\rho^{3/2} U_{\ell\beta}^* U_{\ell\rho} R_{1\beta} R_{1\rho})}{\sum_\beta m_\beta |R_{1\beta}|^2}$$

For hier RH N's and thermal initial abundance

$$\frac{n_B}{n_\gamma} \approx \frac{\epsilon_1^\ell \eta_\ell}{\sum_\ell g_{\text{SM}}}$$

including flavor - but very mod dep

Efficient generation of N_1 only if

$$T_{RH} > M_1$$

γ_B

Flavored ($\ell = e, \mu, \tau$) RH leptogenesis

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$$\epsilon_1^\ell \propto M_1 \frac{Im(\sum_{\beta\rho} m_\beta^{1/2} m_\rho^{3/2} U_{\ell\beta}^* U_{\ell\rho} R_{1\beta} R_{1\rho})}{\sum_\beta m_\beta |R_{1\beta}|^2}$$

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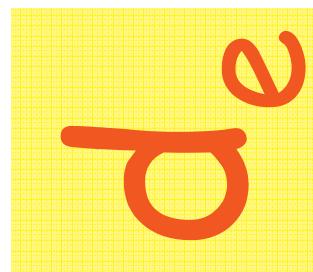
Efficient generation of N_1 only if

$$\textcolor{red}{“10^{10} GeV”} > T_{RH} > M_1$$

To avoid overproduction of gravitinos during reheating (their late decays destroy BBN)

including flavor: **milder tension** with T_{RH}

Introduction first....



All from DIPOLE OPERATOR bSM

Lfv decays

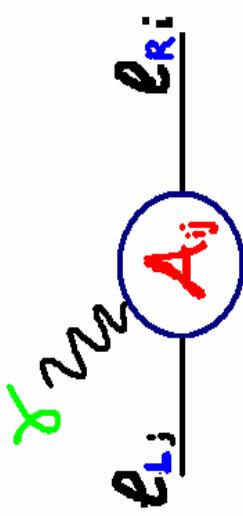
$$BR(\ell_i \rightarrow \ell_j \gamma) \propto |A_{ij}|^2$$

$$\mathcal{L}_{d=5} = \frac{1}{2} \bar{\psi}_{Ri} \overset{\text{newPhys}}{\circlearrowleft} A_{ij} \psi_{Lj} \sigma^{\mu\nu} F_{\mu\nu} + h.c.$$

$$\text{MDMs} \quad \delta a_{\ell_i} = Re A_{ii}$$

$$\text{EDMs} \quad d_{\ell_i} = Im A_{ii} \quad \text{P\&T V}$$

$$\begin{array}{c|ccc} & \left| \begin{array}{c} F^{\mu\nu}, \bar{\psi} \sigma^{\mu\nu} \psi \\ i \bar{\psi} \sigma^{\mu\nu} \gamma_5 \psi \end{array} \right. & & \\ \hline C & - & & - \\ P & + & & - \\ T & - & & - \end{array} +$$



$$BR(\ell_i \rightarrow \ell_j \gamma) \propto |A_{ij}|^2$$

$$\delta a_{\ell_i} = Re A_{ii}$$

$$d_{\ell_i} = Im A_{ii}$$



Which NP scales and couplings are to be probed?

	present	planned	at present $M_{NP} >$	planned
EDM	$d_e [e \text{ cm}]$ 1.6×10^{-27}	10^{-30}	$(\text{Im}\Gamma_{ee})^{1/2} \times 6 \text{ TeV}$	$\rightarrow 250 \text{ TeV}$
	$d_\mu [e \text{ cm}]$ 10^{-19}	10^{-24}	$(\text{Im}\Gamma_{\mu\mu})^{1/2} \times 10 \text{ GeV}$	$\rightarrow 3 \text{ TeV}$
MDM	δa_e	6×10^{-11}	$(\text{Re}\Gamma_{ee})^{1/2} \times 30 \text{ GeV}$	
	δa_μ	$\approx (1-3) \times 10^{-9}$	$\approx (\text{Re}\Gamma_{\mu\mu})^{1/2} \times 0.2 \text{ TeV}$	th?
LFV	$\text{BR}(\mu \rightarrow e \gamma)$	10^{-11}	10^{-14} (PSI)	$ \Gamma_{\mu e} ^{1/2} \times 4 \text{ TeV}$ $\rightarrow 20 \text{ TeV}$
	$\text{BR}(\tau \rightarrow \mu \gamma)$	10^{-6}	10^{-8} (LHC)	$ \Gamma_{\tau \mu} ^{1/2} \times 0.1 \text{ TeV}$ $\rightarrow 0.5 \text{ TeV}$

EDM

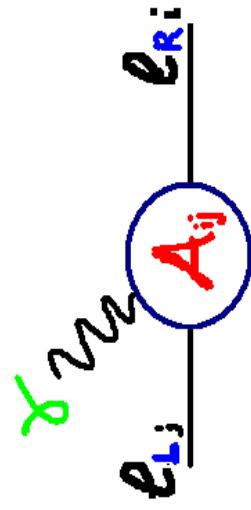
MDM

LFV

$$BR(\ell_i \rightarrow \ell_j \gamma) \propto |A_{ij}|^2$$

$$\delta a_{\ell_i} = Re A_{ii}$$

$$d_{\ell_i} = Im A_{ii}$$



adim coupl of NP with lept
 encodes F&CP violations

$$\Gamma \frac{ij}{M^2}$$

 NP mass scale

if $\Gamma^{\text{NP}} = O(1)$ \rightarrow probe now $M_{\text{NP}} = O(\text{TeV})$, in future $O(10 \text{ TeV})$

Relevant for l.e. susy

SUSY

$$BR(\ell_i \rightarrow \ell_j \gamma) \propto |A_{ij}|^2 = f_{LL} |\delta_{ji}^{LL}|^2 + f_{RR} |\delta_{ji}^{RR}|^2 + f_{LR} |\delta_{ji}^{LR}|^2 + f_{RL} |\delta_{ji}^{RL}|^2 + \dots$$

$$\delta a_{\ell_i} = Re A_{ii} = f_\mu m_{\ell_i}^2 Re \mu + \dots$$

$$d_{\ell_i} = Im A_{ii} = f_a m_{\ell_i} Im a_i + f_{LLR} Im (\delta^{LL} m_\ell \delta^{RR})_{ii} + \dots$$

lept-slept misalignment

$$\frac{\Gamma_{ij}}{M_{\text{susy}}^2} \approx \frac{e m_i}{(4\pi)^2}$$

Loops w/ Sleptons
& Gauginos

$$(L_e^* \tilde{L}_\mu^* \tilde{L}_\tau^*) \underbrace{M_L^2}_{\tilde{L}_e \tilde{L}_\mu \tilde{L}_\tau} + (\tilde{e}_R^* \tilde{\mu}_R^* \tilde{\tau}_R^*) \underbrace{M_R^2}_{\tilde{e}_R \tilde{\mu}_R \tilde{\tau}_R} + \left[(\tilde{e}_L^* \tilde{\mu}_L^* \tilde{\tau}_L^*) \underbrace{M_{LR}^2}_{\tilde{e}_L \tilde{\mu}_L \tilde{\tau}_L} + (\tilde{e}_R^* \tilde{\mu}_R^* \tilde{\tau}_R^*) \underbrace{M_{RL}^2}_{\tilde{e}_R \tilde{\mu}_R \tilde{\tau}_R} \right] + h.c.$$

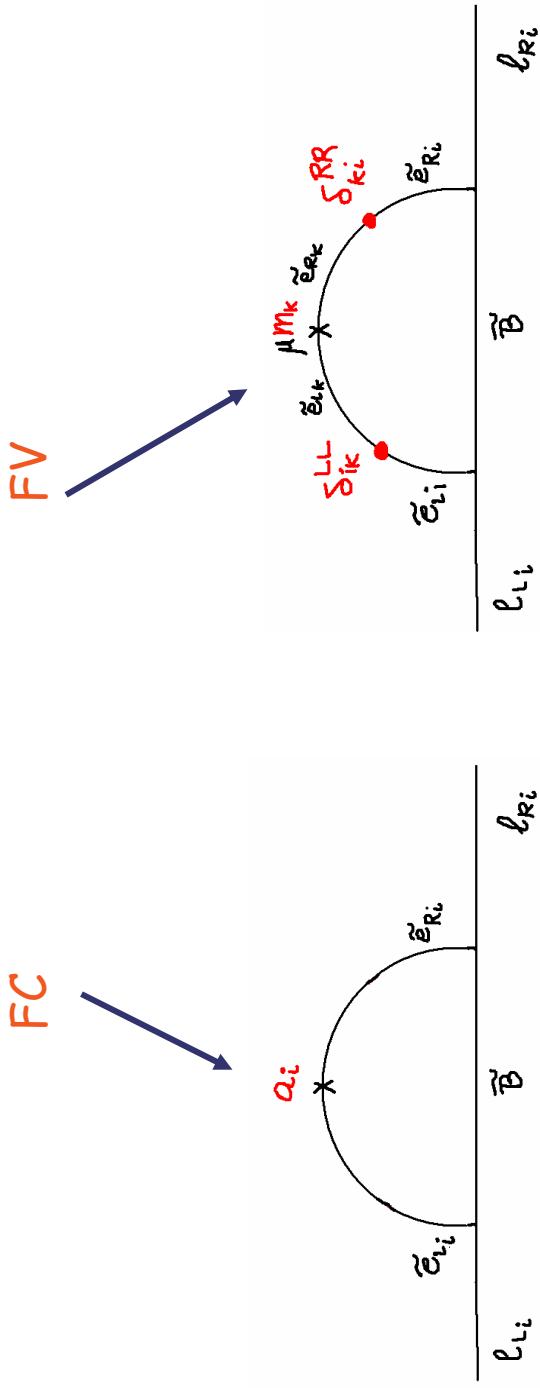
Mass Insertion:
assume real μ -term

$$\tilde{m}_L^2 (\mathbb{1} + \delta^{LL}) \quad \tilde{m}_R^2 (\mathbb{1} + \delta^{RR}) \quad \hat{m}_e (\hat{a}_e^* - \mu \dagger \beta) + \tilde{m}_L \tilde{m}_R \delta^{LR}$$

$$BR(\ell_i \rightarrow \ell_j \gamma) \propto |A_{ij}|^2 = f_{LL} |\delta_{ji}^{LL}|^2 + f_{RR} |\delta_{ji}^{RR}|^2 + f_{LR} |\delta_{ji}^{LR}|^2 + f_{RL} |\delta_{ji}^{RL}|^2 + \dots$$

$$\delta a_{\ell_i} = Re A_{ii} = f_\mu m_{\ell_i}^2 Re \mu + \dots$$

$$d_{\ell_i} = Im A_{ii} = \underbrace{f_a m_{\ell_i} Im a_i}_{FC} + \underbrace{f_{LLRR} Im (\delta^{LL} m_\ell \delta^{RR})_{ii}}_{FV} + \dots$$



d_e

From **mSUGRA** at M_{Pl} , **susy seesaw**
induce **FV** and **CPV** at l.e. via **RGE**

$$C_{ij}^{\textcolor{violet}{k}} = Y_{\nu}^{*}{}_{ki} Y_{\nu}{}_{kj} \ln \frac{M_{Pl}}{\textcolor{violet}{M}_k}$$

[BorzumatiMassiero '86]

$$\xrightarrow{-\frac{1}{(4\pi)^2} \frac{6m_0^2 + 2a_0^2}{\bar{m}_L^2} \sum_k C_{ij}^k}$$

$$BR(\ell_i \rightarrow \ell_j \gamma) \propto |A_{ij}|^2 = f_{LL} |\delta_{ji}^{LL}|^2 + f_{RR} |\delta_{ji}^{RR}|^2 + f_{LR} |\delta_{ji}^{LR}|^2 + f_{RL} |\delta_{ji}^{RL}|^2 + \dots$$

$$d_{\ell_i} = Im A_{ii} = f_a m_{\ell_i} Im a_i + f_{LLR} Im (\delta^{LL} m_{\ell} \delta^{RR})_{ii} + \dots$$

$$\xrightarrow{\frac{8a_0}{(4\pi)^4} \sum_{k>k'} \frac{\ln_{k'}^k}{\ln_{k'}^{\text{Pl}}} \text{Im}(C^k C^{k'})_{ii}}$$

FC

$$\xrightarrow{\frac{8m_{\ell_i}}{(4\pi)^6} \frac{(6m_0^2 + 2a_0^2)(6m_0^2 + 3a_0^2)}{\bar{m}_L^2 \bar{m}_R^2} \frac{m_{\tau}^2 \tan^2 \beta}{v^2} \sum_{k>k'} \frac{\ln_{k'}^k}{\ln_{k'}^{\text{Pl}}} \text{Im} \left(C^k \frac{m_{\ell}^2}{m_{\tau}^2} C^{k'} \right)_{ii}}$$

FV

[EllisHisanoLolaRaidalShimizu '01]

[IM '03]

d_e

From mSUGRA at M_{Pl} , susy seesaw
induce FV and CPV at l.e. via RGE

$$C_{ij}^k = Y_\nu^{*k} Y_\nu^{kj} \ln \frac{M_{Pl}}{\bar{M}_k}$$

[BorzumatiMassiero '86]

$$-\frac{1}{(4\pi)^2} \frac{6m_0^2 + 2a_0^2}{\bar{m}_L^2} \sum_k C_{ij}^k$$

$$BR(\ell_i \rightarrow \ell_j \gamma) \propto |A_{ij}|^2 = f_{LL} |\delta_{ji}^{LL}|^2 + f_{RR} |\delta_{ji}^{RR}|^2 + f_{LR} |\delta_{ji}^{LR}|^2 + f_{RL} |\delta_{ji}^{RL}|^2 + \dots$$

$$d_{\ell_i} = Im A_{ii} = f_a m_{\ell_i} Im a_i + f_{LLR} Im (\delta^{LL} m_{\ell} \delta^{RR})_{ii} + \dots$$

$$\frac{8a_0}{(4\pi)^4} \sum_{k>k'} \frac{\ln_{k'}^k}{\ln_{k'}^{Pl}} \text{Im}(C^k C^{k'})_{ii}$$

$$\frac{8m_{\ell_i}}{(4\pi)^6} \frac{(6m_0^2 + 2a_0^2)(6m_0^2 + 3a_0^2)}{\bar{m}_L^2 \bar{m}_R^2} \frac{m_{\tau}^2 \tan^2 \beta}{v^2} \sum_{k>k'} \frac{\ln_{k'}^k}{\ln_{k'}^{Pl}} \text{Im} \left(C^k \frac{m_{\ell}^2}{m_{\tau}^2} C^{k'} \right)_{ii}$$

[EllisHisanoLolaRaidalShimizu '01]

[IM '03]

FC & FV

FC&FV vanish if RH N's are deg

With O(1) yuk & hier RH, (only) d_e ss is significant for experiments
FV generically dominant for tanβ > 10

Q: if observed, is d_e compatible with thermal leptogenesis?

Work it out ...

...by exploiting the fact that

$$Y_\nu = N_1 \left(\begin{array}{c} v_e \\ \approx 10^{-2} \\ v_\mu \\ \approx 10^{-2} \\ v_\tau \\ \approx 10^{-2} \end{array} \right) \quad \text{For } M_1 \text{ to be in the interesting range for leptogenesis}$$



C¹ negligible, only **C^{2,3} matter**
for LFV and d_e



the splitting M_2/M_3 is crucial for d_e

#1 : Largeness of d_e^{ss}

Taking here for definiteness $P = (\tilde{M}_1, \bar{m}_R) = (200, 500) \text{ GeV}$, the limit on $\ell_i \rightarrow \ell_j \gamma$ constrains:

$$(k=2,3) \quad \sum_k C_{21}^k < 5 \times 10^{-3} \frac{50}{\tan \beta} \quad \sum_k C_{32}^k < 0.8 \frac{50}{\tan \beta} \quad \sum_k C_{31}^k < \frac{50}{\tan \beta} = C$$

very small

$$d_e^{\text{SS}} \approx (f_{FC} + f_{FV}) \underbrace{\text{Im}(C_{31}^{2*} C_{31}^3)}_{< |CC|} \ln \frac{M_3}{M_2} < d_e^{\tau \rightarrow e\gamma} \approx (10^{-2} - 10^{-1}) d_e^{\text{exp}}$$

barring canc's

But even allowing for cancellations in
 $|C^{2*}C^3|_{13}$ the bound is safe

#1 : Largeness of d_e^{ss}

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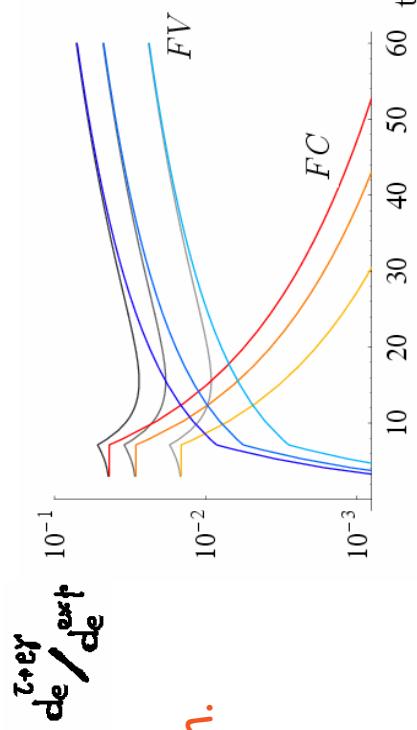
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very small

$$d_e^{SS} \approx (f_{FC} + f_{FV}) \underbrace{\text{Im}(C_{31}^{2*} C_{31}^3)}_{\text{↔ CCL}} \ln \frac{M_3}{M_2} < d_e^{\tau \rightarrow e\gamma} \approx (10^{-2} - 10^{-1}) d_e^{exp}$$

barring canc's

But even allowing for cancellations in
 $|C^{2*}C^3|_{13}$ the bound is safe



**Exp improvement by 2 o.o.m.
needed to test d_e^{ss}**

; $M_2 = 5 \times 10^{14}$ GeV and, from top to bottom lines, $M_3/M_2 = 10^3, 10^2, 10$.

#2. The class of textures maximizing d_e ss

$$M_3 \gg M_2$$

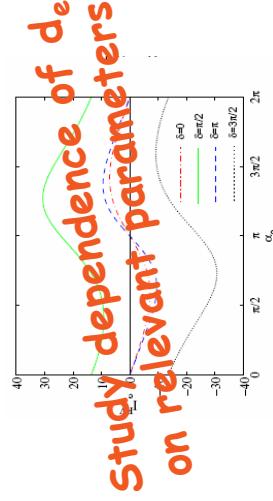
&

$$Y_\nu = \begin{pmatrix} \lesssim 10^{-2} & \lesssim 10^{-2} & \lesssim 10^{-2} \\ \mathcal{O}(1) & \approx 0 & \mathcal{O}(1) \\ \mathcal{O}(1) & \approx 0 & \mathcal{O}(1) \end{pmatrix}$$

For M_1 in the interesting range for leptogenesis

Only possible structure allowing large d_e
and enough suppressed $\mu \rightarrow e\gamma$
(clearly, $\tau \rightarrow e\gamma$ is close to its bound)

→ explore parameter space



$$M_2 \approx \frac{v_\omega^2}{m_h} \quad m_\ell \approx \frac{v_\omega^2}{M_3}$$

cannot vanish!

#3. Estimate of γ_L

This class of textures corresponds to very specific \mathbf{R} structures, which depend on light ν-spectrum, \mathbf{U} and $\chi \ll 1$

$$R_{\text{NH}} = \begin{pmatrix} \chi & \bar{c} & \bar{s} \\ 0 & \bar{s} & -\bar{c} \\ -1 & \chi\bar{c} & \chi\bar{s} \end{pmatrix} \quad \text{where} \quad \bar{t} = \sqrt{\frac{m_3}{m_2}} \frac{U_{23}^*}{U_{22}^*}; \quad R^{\text{IH}} = \begin{pmatrix} \bar{s} & \bar{c} & \chi \\ -\bar{c} & \bar{s} & 0 \\ \bar{s}\chi & \chi\bar{c} & -1 \end{pmatrix} \quad \text{where} \quad \bar{t} = \sqrt{\frac{m_1}{m_2}} \frac{U_{21}^*}{U_{22}^*}$$

In terms of [S.F.King's] "dominance": $M_1 - m_{\text{heavy}}$ $M_3 - m_{\text{light}}$

Due to the particular form of R_{1j} , a sufficiently large $\epsilon_1^\ell \propto M_1 \frac{\text{Im}(\sum_{\beta\rho} m_\beta^{1/2} m_\rho^{3/2} U_{\ell\beta}^* U_{\ell\rho} R_{1\beta} R_{1\rho})}{\sum_\beta m_\beta |R_{1\beta}|^2}$ requires for both NH and IH

$M_1 > 10^{11} \text{ GeV}$

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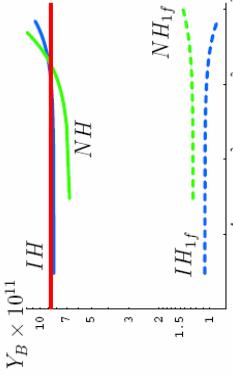
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2 examples with successful γ_B

#3. Estimate of γ_L

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$M_1 > 10^{11} \text{ GeV}$

definitely too large w.r.t. "bound on T_{RH} " → th prod of N_1 unlikely

Conclusions

Observing $d_{e\bar{e}}$ is possible BUT REQUIRES
specific class of textures and some relations to hold →
 $m_\ell \approx \frac{v_\omega^2}{M_3}$

This determines $R_{1j} \rightarrow M_1 > 10^{11} \text{GeV}$ for th lept (even with flavor effects)
strong tension with gravitino bound on $T_{RH} < "10^{10} \text{GeV}"$

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Observing d_e^{ss} is possible BUT REQUIRES
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THEN... in case d_e^{ss} were measured:

keep $d_e^{ss} \rightarrow$ non-thermal production of N_1 OR abandon leptogenesis

keep th leptog $\rightarrow d_e$ from a different source of CPV bSM than susy-ss
many candidates, e.g. GUT's triplet Yukawas

CPV-related observables are useful guides
for theories beyond the SM

$p \rightarrow K^+ \nu$

VS

d_e

From d=5 op generated by TRIPLET exchange
['82: Weinberg, Sakai, Yanagida, ...]

τ_p depends A LOT on M_T -structure

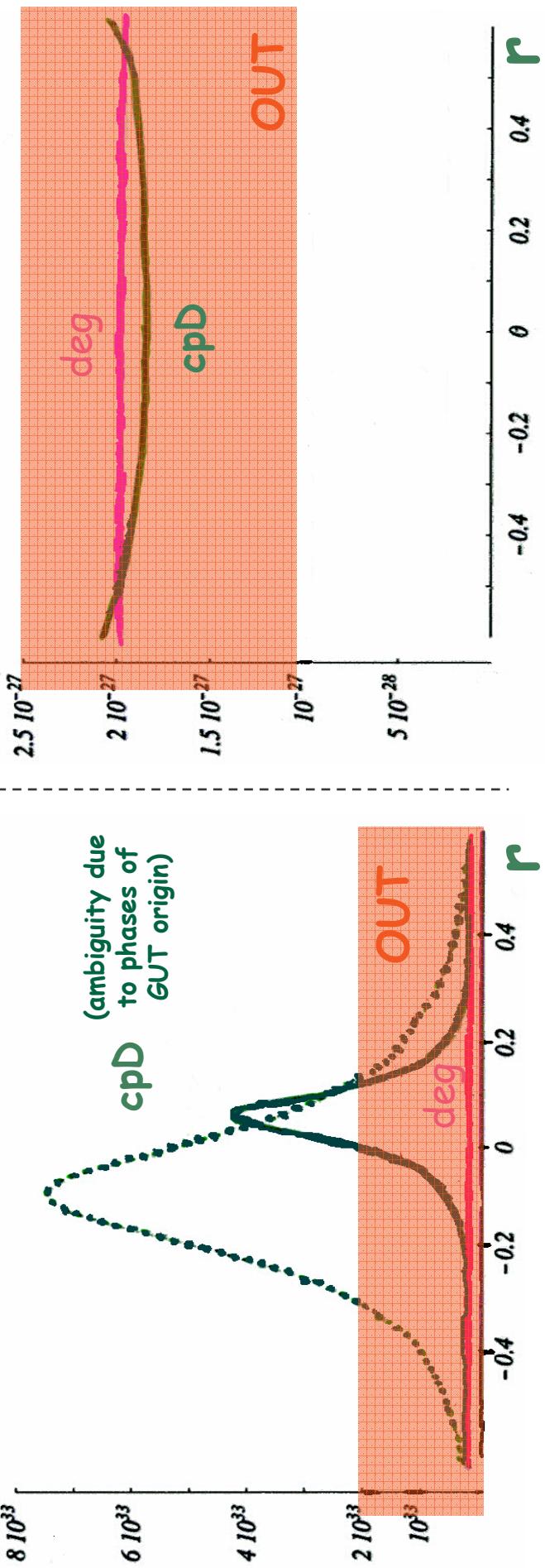
deg: KO cpD: SAFE

g_μ region & $\tan\beta = 3$

τ_p [yrs]

d_e [ecm]

With (naturally)
 $O(1)$ phase:



Complementary in constraining SUSY GUTs

Susy Seesaw & dipole operator

Basic idea:

- seesaw yukawas induce via RGE flavor & CP V in slepton masses
- coeff of dipole op is linked to seesaw
- & turns out to be exp relevant!

Caveat:

- to isolate just the seesaw contribution to dipole operator,
better to suppress other potential flavor & CP V sources
- assume real and universal soft masses at M_{Planck} : mSugra

