

# Probing models of neutrino mass and neutrino interactions with cosmology and colliders

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# Cosmology and Colliders



Low energy



High energy

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Low energy

High energy



*Dark matter*

# Cosmology and Colliders



Low energy

High energy



*Dark matter*

Completely stable

TeV mass

# Cosmology and Colliders



Low energy

High energy

*Higher dimension  
operator*

# Cosmology and Colliders



Low energy

High energy

*Higher dimension  
operator*

Sensitive to very low rates  
(small couplings)

Produce directly

# Models of Neutrino Mass

- Generate higher dimension operator with see-saw mechanism

$$L_{mass} = \frac{y^2 LHLH}{M}$$

( $m_\nu \sim \frac{(100 \text{ GeV})^2}{M}$ )

$$L_{mass} = yHLe_R + yHL\nu_R + M\nu_R\nu_R$$

$$m = \begin{pmatrix} \nu_L & \nu_R \\ 0 & m_D \\ m_D & M \end{pmatrix} \quad m_{light} \sim \frac{m_D^2}{M} \quad \longleftrightarrow \quad L_{mass} = \frac{y^2 LHLH}{M}$$



# Models of Neutrino Mass

- Right handed neutrino mass generated by additional scalar

$$L_{mass} = yHLe_R + yHL\nu_R + M\nu_R\nu_R$$

$$L_{mass} = \frac{y^2 LHLH}{M}$$

$$L_{mass} = yHLe_R + yHL\nu_R + \lambda\Phi\nu_R\nu_R$$

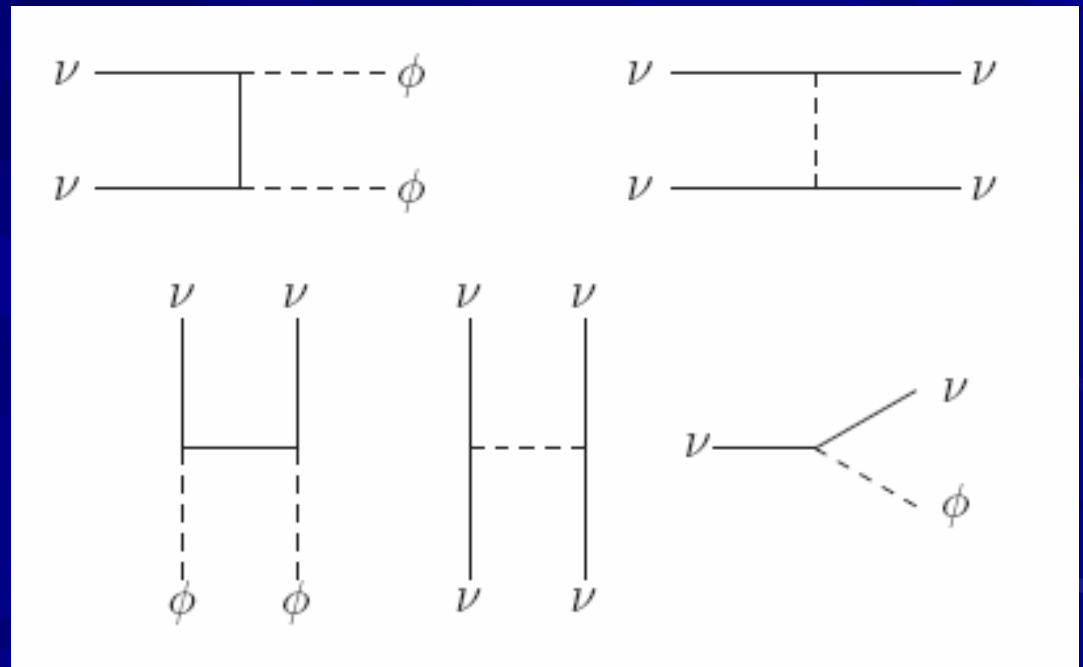
$$L_{mass} = \frac{y^2 LHLH}{M} \frac{\lambda\Phi}{M}$$

- Effective interaction

$$L_{maj} = g\Phi\nu\nu \quad g = \lambda \frac{m_D^2}{M^2}$$

# Coupled neutrinos

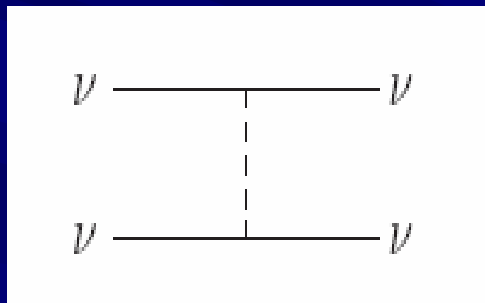
- Behaves like a fluid when  $\Gamma_{\text{scatt}} > H$
- Turns off free-streaming and effects CMB spectrum



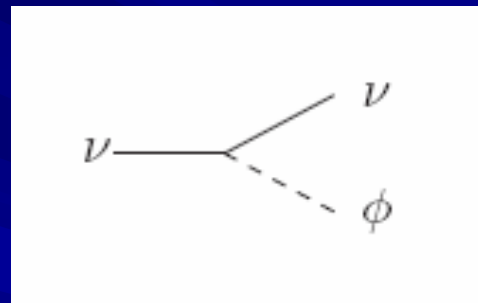
# Implications for models

- CMB very sensitive to  $g$  through neutrino non-free-streaming

$$L_{maj} = g\Phi\nu\nu$$



$$\Gamma \sim g^4 T$$



$$\Gamma \sim g^2 T$$

- Compare  $H$  at  $T \sim 1$  eV

– If neutrinos free-streaming  $\rightarrow g < 10^{-7} - 10^{-13}$

# Sensitive to TeV scale neutrino mass generation

■ Effective operator  $L_{mass} = \frac{y^2 LHLH}{M} \frac{\lambda\Phi}{M}$

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– Fix to experimental value  $m_\nu = \lambda \frac{y^2 \langle H \rangle^2}{M} \sim 10^{-1} \text{ eV}$

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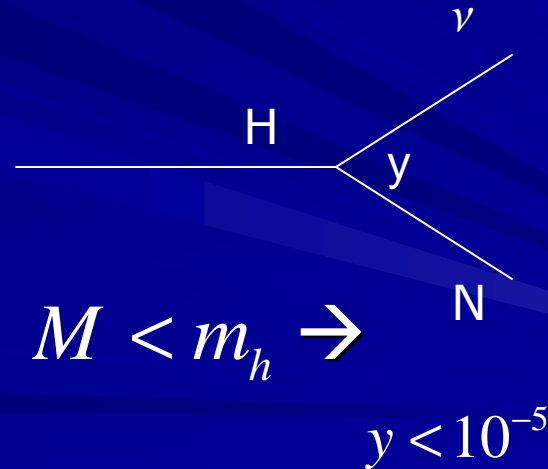
■ CMB sensitive to  $g \sim 10^{-13}$  OR  $M \sim 1\text{TeV}$   $g \sim \frac{m_\nu}{M}$

# For collider physics

- TeV or lighter sterile neutrinos
- Higgs decays to heavier steriles?
- Too small Yukawas?

$$m = \begin{pmatrix} \nu_L & N \\ 0 & y \langle v \rangle \\ y \langle v \rangle & M \end{pmatrix}$$

– Satisfy  $m_\nu \sim \frac{y^2 \langle v \rangle^2}{M} \sim 0.1 \text{ eV}$   $M < m_h \rightarrow y < 10^{-5}$





# For collider physics

- Too naïve (de Gouvea 0706.1732)

$$m_\nu = \frac{y^2 \langle \mathbf{v} \rangle^2}{M \cos \zeta^* \sin \zeta^*}$$

- $\zeta$  (parameter in matrix diagonalizing  $\nu$  masses) imaginary  $\rightarrow$  exponential suppression of neutrino mass
- Can maintain large mixing

# A toy example

From A. Nelson

See also Kersten and Smirnov,  
arXiv:0705.3221

$$M = \begin{matrix} & \nu & N_1 & N_2 \\ \begin{pmatrix} \varepsilon & m_D & 0 \\ m_D & M_1 & M_2 \\ 0 & M_2 & 0 \end{pmatrix} \end{matrix}$$

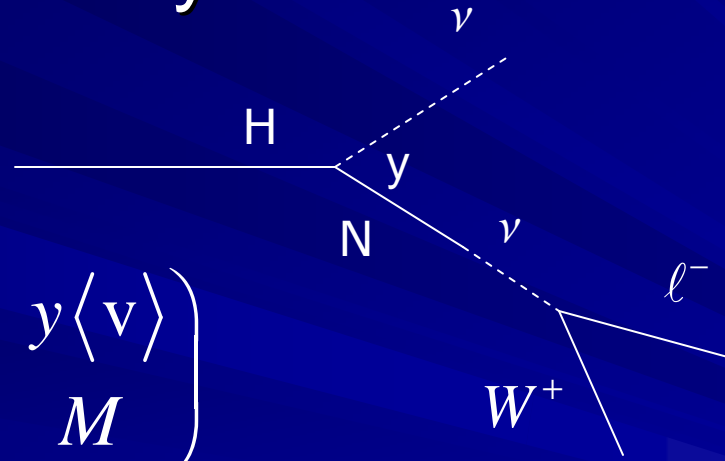
$$\varepsilon \rightarrow 0, \det(M) \rightarrow 0 \Rightarrow m_1 \rightarrow 0$$

Neutrino mass goes to zero as  $\varepsilon \rightarrow 0$ , but mixing still large!

# For collider physics

- Enhanced  $y \rightarrow$  large branching fraction for exotic Higgs decays

$$m = \begin{pmatrix} 0 & y \langle v \rangle \\ y \langle v \rangle & M \end{pmatrix}$$

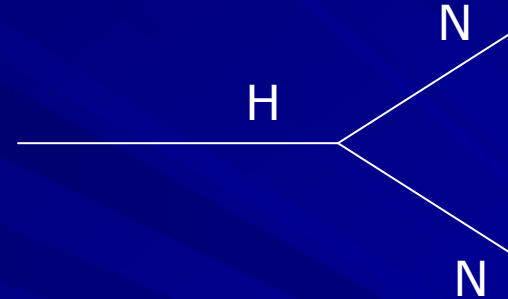


- $H \rightarrow$  missing energy +  $W^+ + l^-$

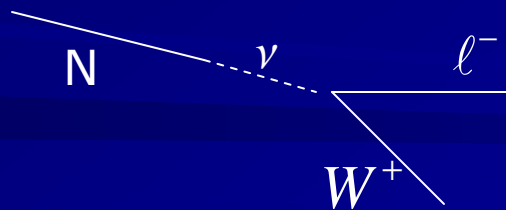
# For collider physics

- Significant Higgs branching to neutrino singlets (Graesser 0704.0438, 0705.2190)

$$\frac{\lambda H^\dagger H N N}{\Lambda}$$

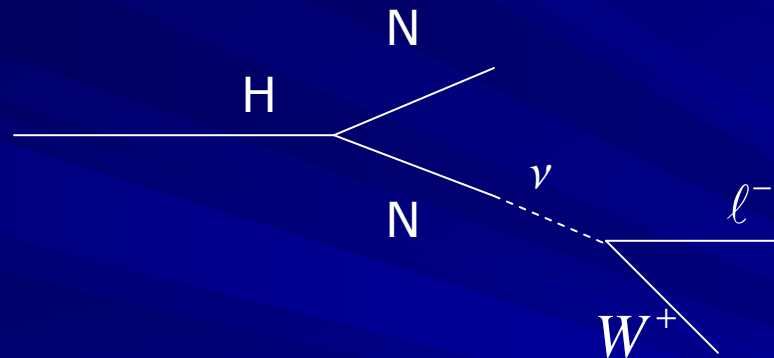


- Neutrinos decay through see-saw operators



# Displaced vertices and hidden sectors

- Significant branching, but long lifetimes

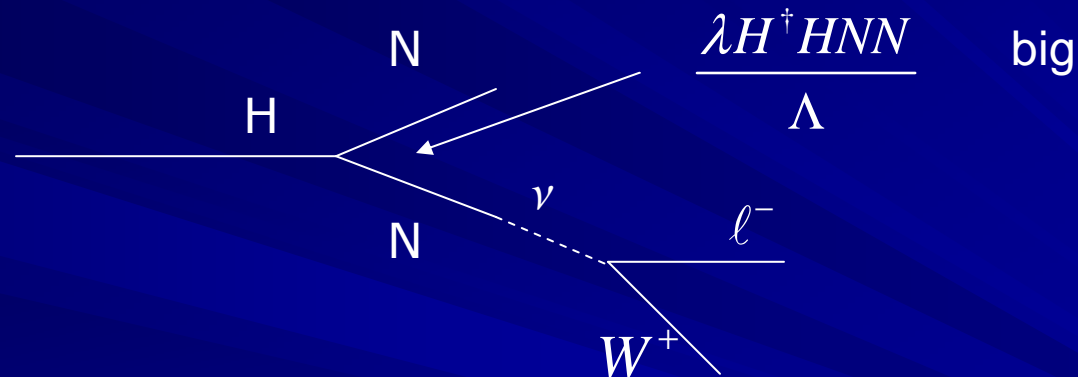


- Decay length

$$\ell_N = 0.9 \text{ m} \left( \frac{30 \text{ GeV}}{M} \right)^3 \left( \frac{120 \text{ keV}}{m_D} \right)^2$$

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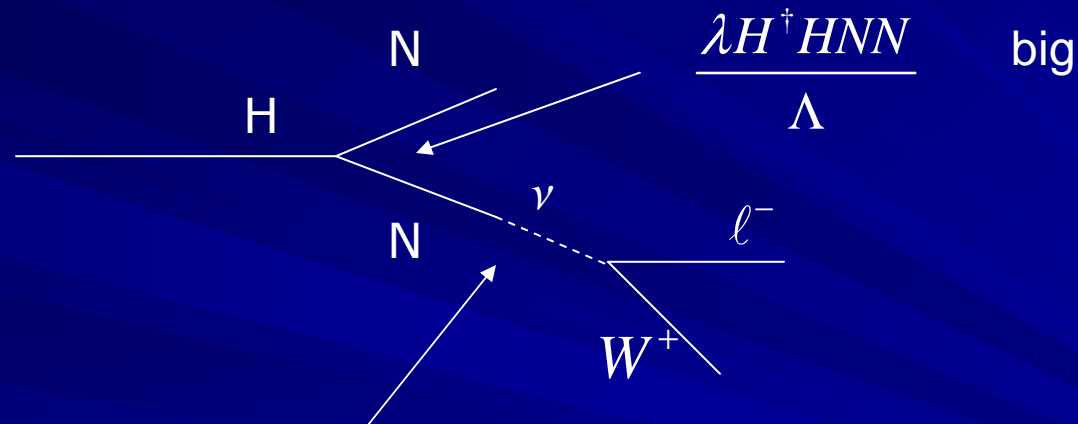


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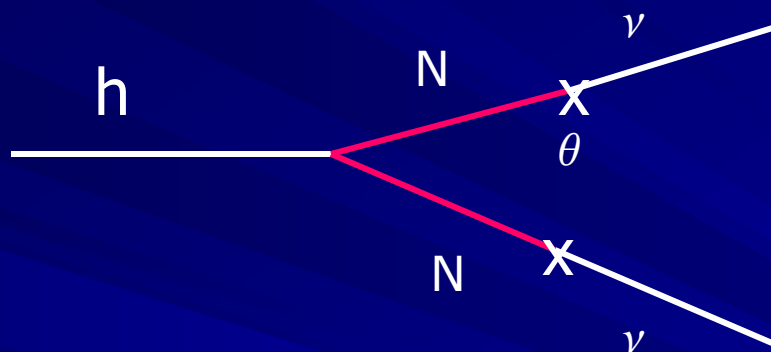
$$\theta \sim m_D / M \ll 1 \quad \text{small}$$

- Decay length

$$\ell_N = 0.9 \text{ m} \left( \frac{30 \text{ GeV}}{M} \right)^3 \left( \frac{120 \text{ keV}}{m_D} \right)^2$$

# Extend beyond neutrino singlets

- Hidden sector Higgs decays

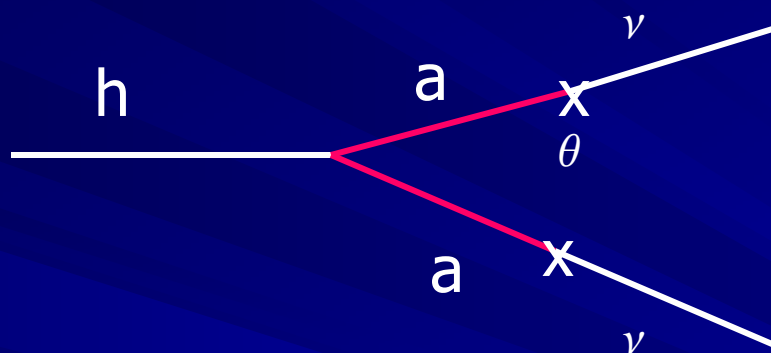


- $a$  is hidden sector pseudoscalar in NMSSM
- $a \rightarrow -a$  symmetry nearly exact
  - Mixing  $\theta$  with Higgs small
  - Lifetimes long
  - Appearance of displaced vertices
  - Strassler and KZ, hep-ph/0605193



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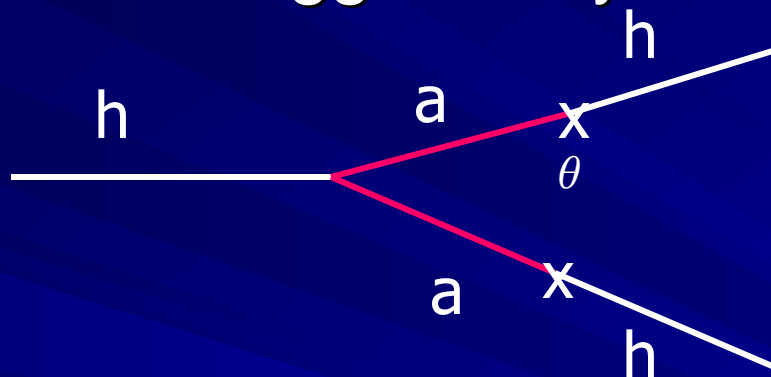


Dermisek and Gunion  
PRL95:041801,2005

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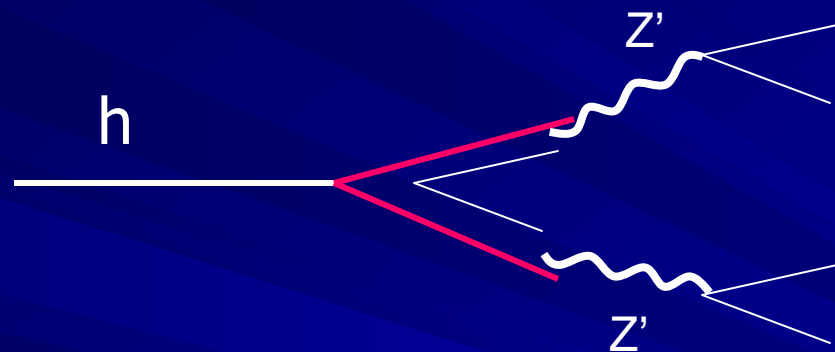


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# Extend beyond neutrino singlets

## ■ Hidden sector Higgs decays



Strassler and Zurek  
hep-ph/0604261

- Create light hidden sector bound states
- Long lived: decay through heavy  $Z'$

# Collider physics and cosmology

## ■ Higher dimension operators

### – Exotic Higgs decays

- Significant branching to singlet states  $h \rightarrow NN$  or  $h \rightarrow \nu N$

- Singlets long lived

- Decay through higher dimension operators

- Displaced vertices

## ■ CMB (can be) very sensitive to higher dimension operators of this type

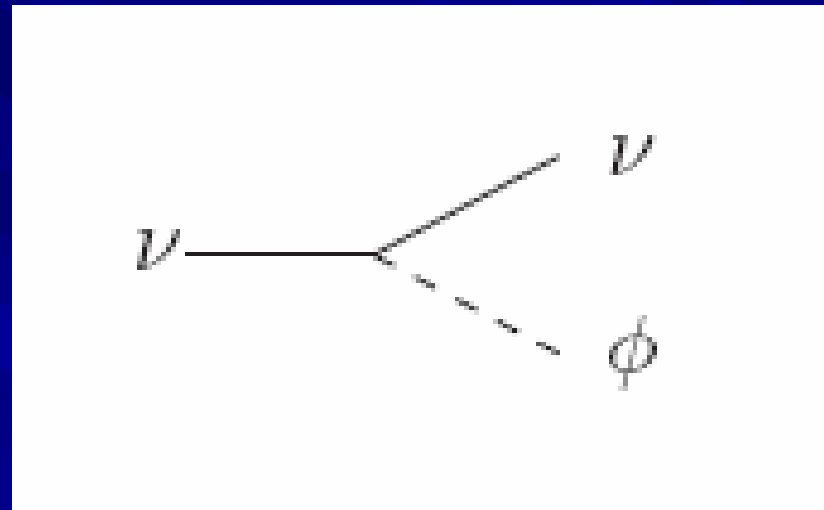
- Provided the operator invokes light states (neutrinos)

# Return to CMB

$$L_{mass} = \frac{y^2 LHLH}{M} \frac{\lambda\Phi}{M} \rightarrow g\phi\nu\nu$$

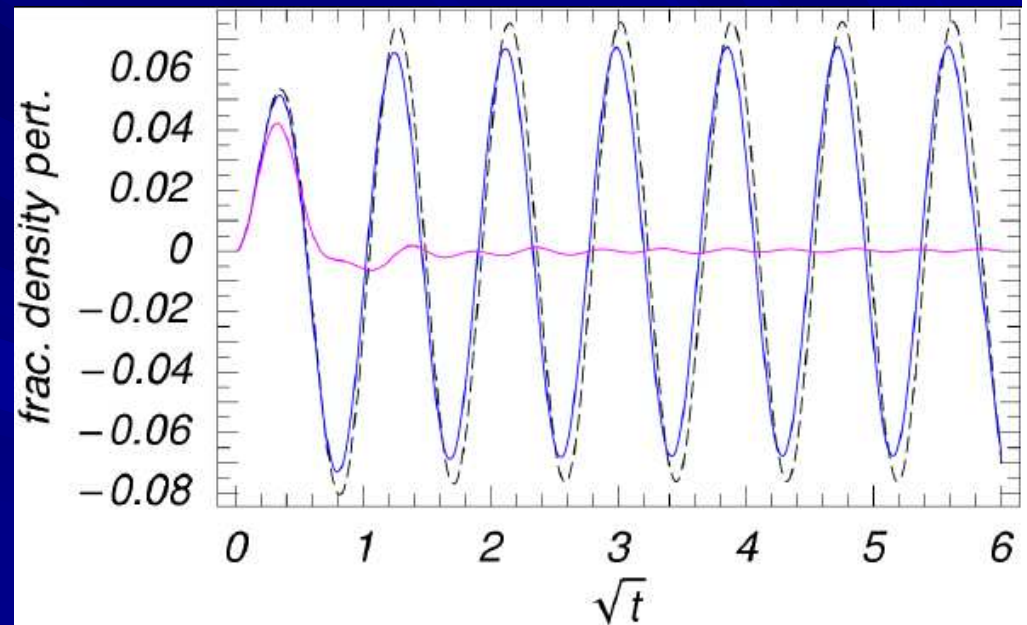
$$g \sim \frac{m_\nu}{M}$$

- Coupling turns off neutrino free-streaming if  $g > 10^{-13}$



# Effects of neutrinos on the CMB

- Gravitational coupling of neutrinos to photons has two effects
  - Oscillation amplitude suppressed ( $\sim 10\%$ )
  - Oscillation phase shifted



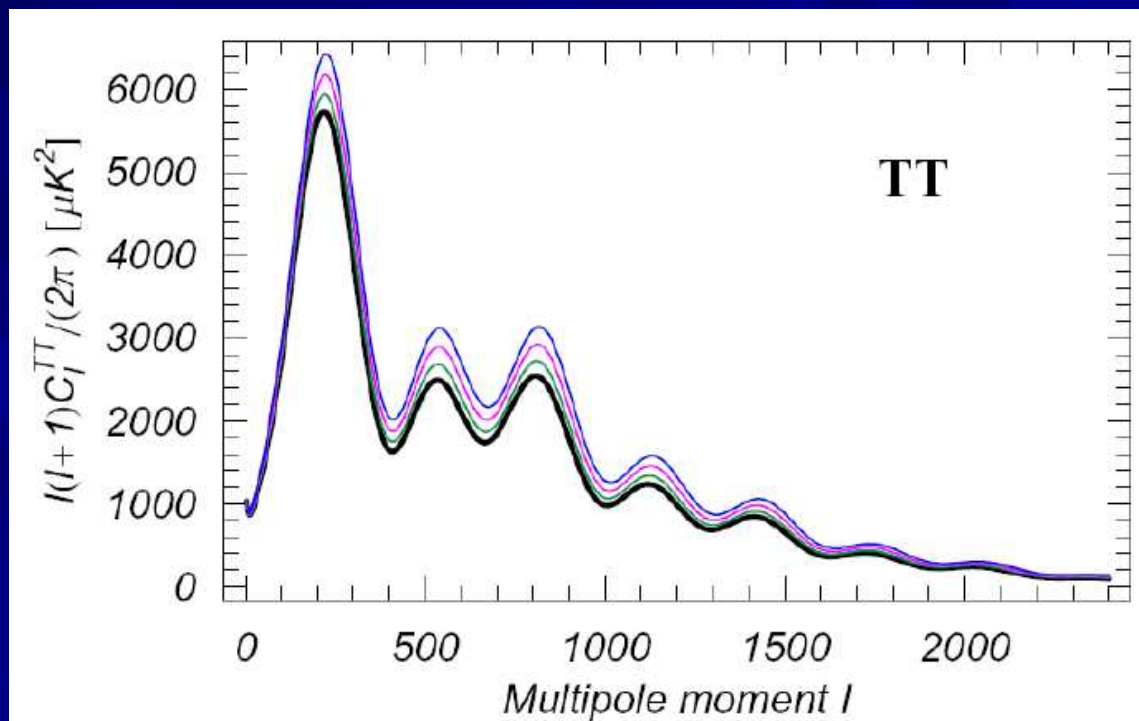
Peebles 1973

# Turn off free-streaming with CMBFast

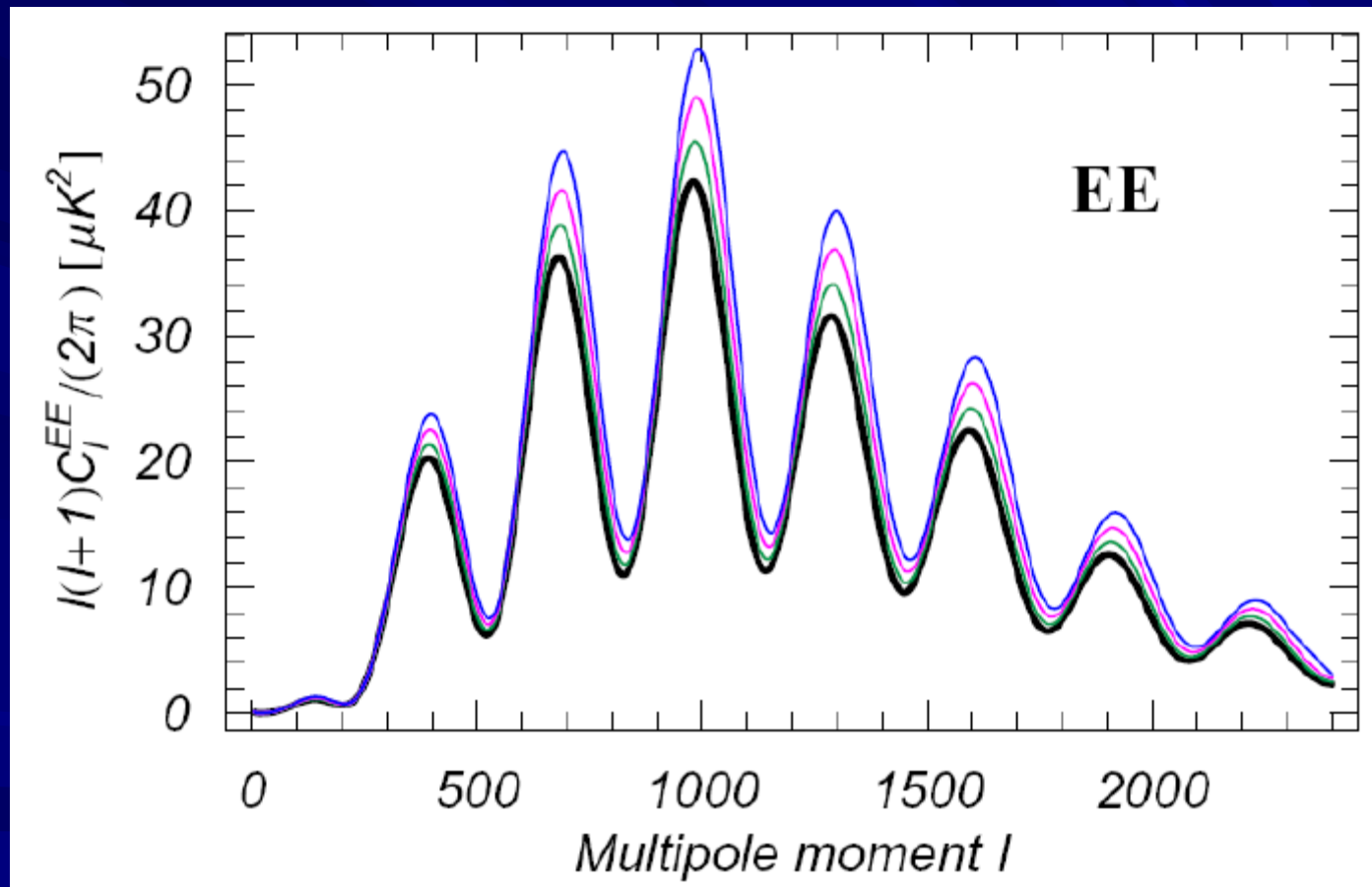
$$\dot{\delta}_v = -\frac{4}{3}\theta_n - \frac{2}{3}\dot{h}_v$$

$$\dot{\theta}_v = k^2 \left( \frac{1}{4}\delta_n - \sigma_v \right)$$

$$\dot{F}_{vl} = \frac{k}{2l+1} \left[ lF_{v(l-1)} - (l+1)F_{v(l+1)} \right]$$

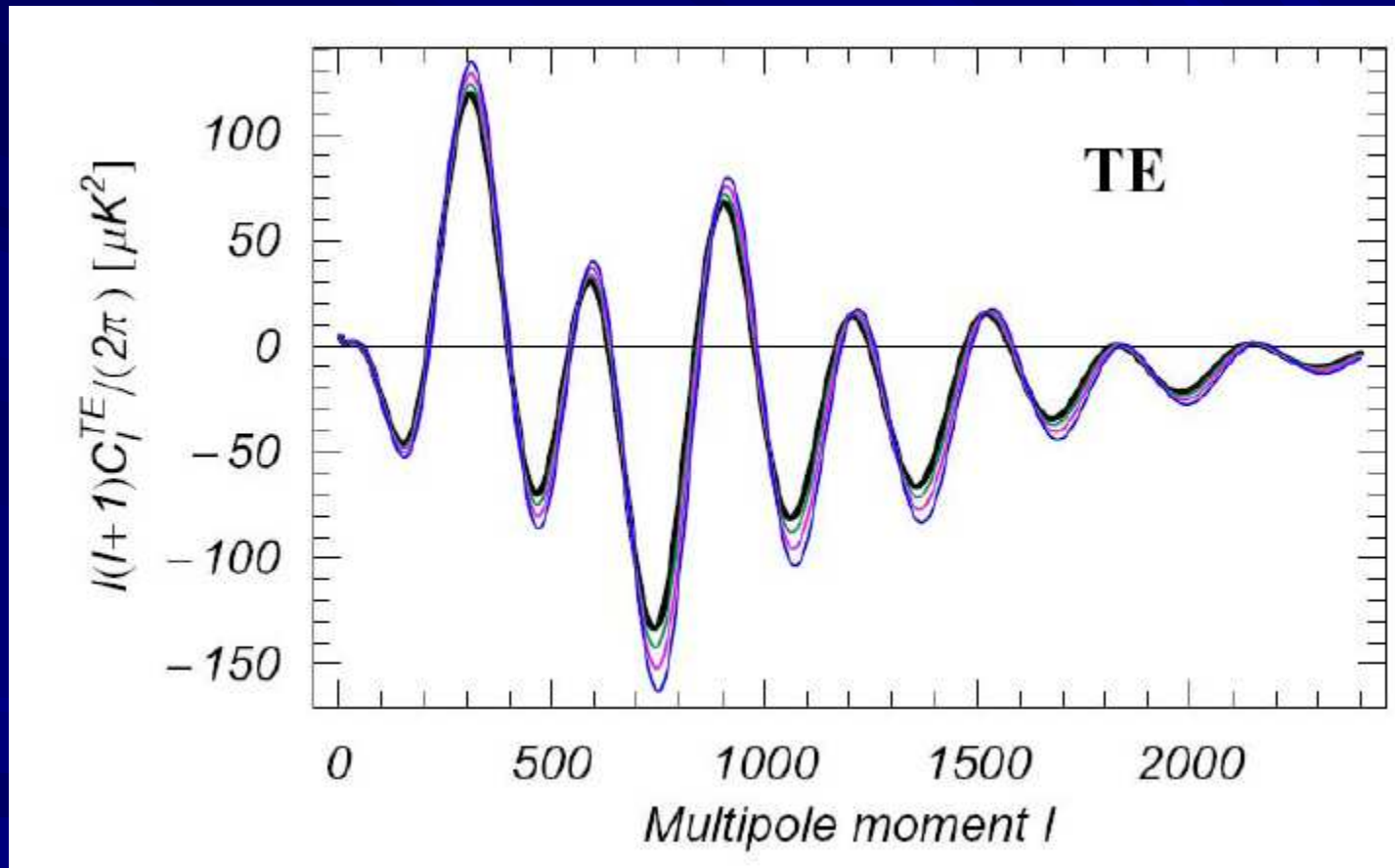


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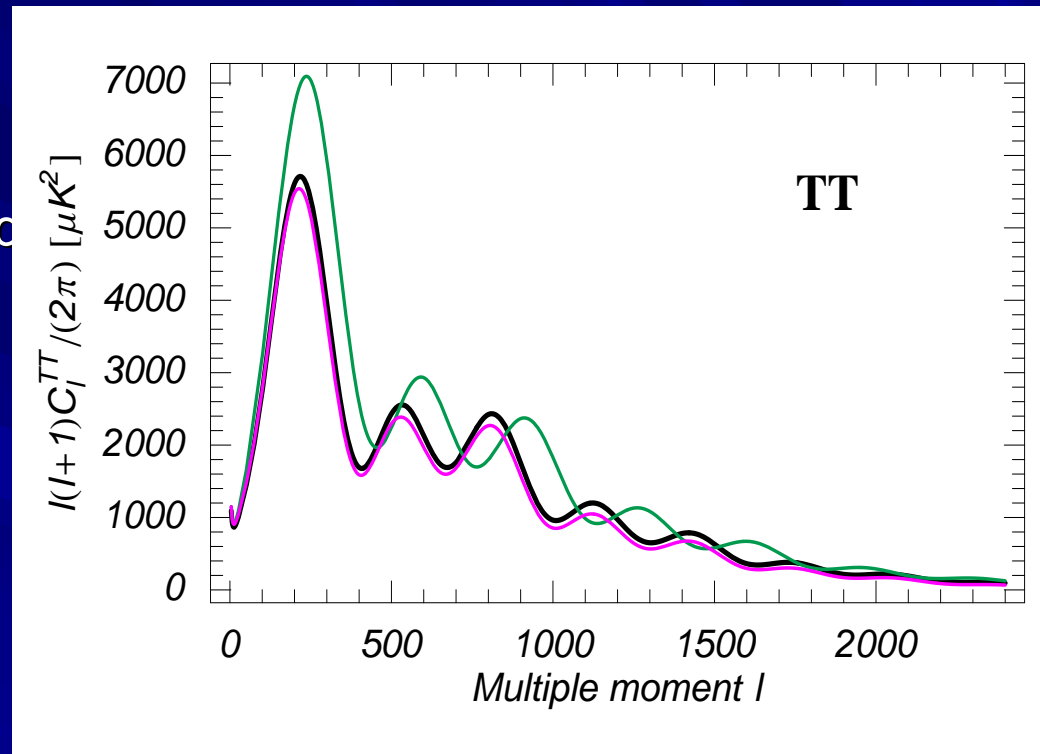
# Coupled Neutrinos

- Effect appears to be large
- Current constraints on 3 coupled neutrinos
  - Trota and Melchiorri,  $2.4\sigma$  with all data
  - Bell, Pierapaoli, Sigurdson,  $2\sigma$  with all data
- Single coupled neutrino unconstrained
- They are quite weak—why?
- Parameter degeneracies

$$\left( \rho_m, \rho_b, \omega_{\nu \text{ massive}}, N_\nu, N_\nu^{fs}, \rho_{de}, w_{de}, \tau_{reion}, P, n_s, n_s', Y \right)$$

# Illustrated with extra neutrinos

- 3 neutrinos (black) → 7 neutrinos (green)
- Surprising results
  - The plot shows a boost and not a suppression in the amplitude
  - Effect is very big → might imply high exclusion of additional neutrinos
  - Current constraints:  $N_{\text{FS}} = 5^{+2}_{-2}$

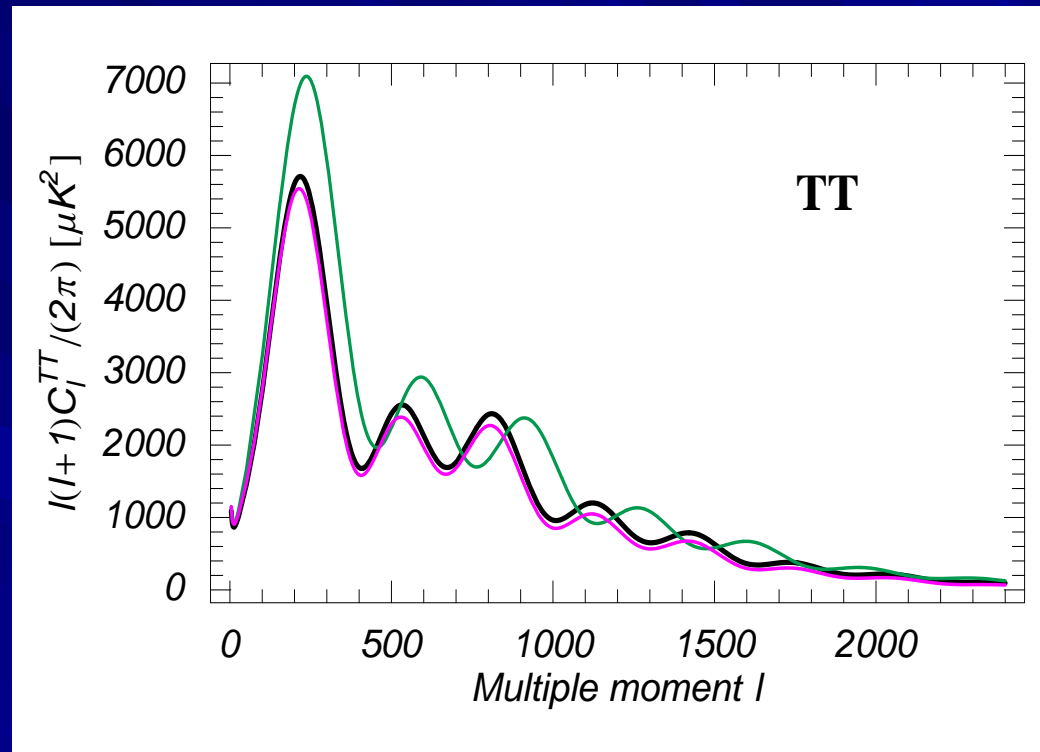


# Background effects

- Boost due to delay in  $z_{eq}$
- Rescale  $h$  to re-fix  $z_{eq}$  (magenta)

$$1 + z_{eq} = 4.05 \times 10^4 \frac{\Omega_m h^2}{1 + 0.6905 N_\nu / 3.04}$$

- Small suppression of Peebles' solution now evident
- Due to neutrino anisotropy



# Residual Effects

- Real challenge is to establish the **residual differences** between two models (within experimental precision) after “**nuisance parameters**” have been adjusted for
- The residual differences are much smaller
- Cannot be estimated analytically
  - **Fisher matrix** method can be used
  - Best to do a scan in the parameter space using **Monte Carlo**

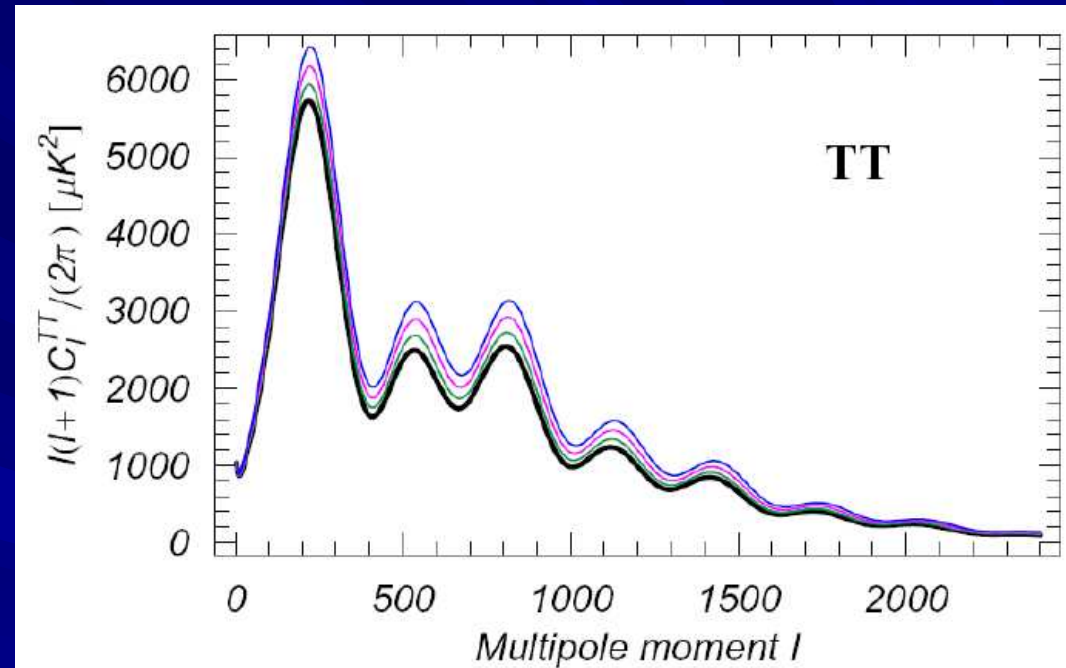
# WMAP alone

- WMAP cannot rule out coupled neutrinos, tells you little about  $N_{\text{coupled}}, N_{\text{FS}}$
- Parameter degeneracies
  - $N_{\text{FS}}$  Preserve  $\Omega_m h^2$ , compensate other residuals by bias and  $n_s$
  - $N_{\text{coupled}}$  Compensate primarily by bias and  $n_s$

$(N_{\text{FS}}, N_{\text{coupled}})$	$\delta\chi^2$	C.L.
(3, 0)	–	–
(2, 1)	0.2	$0.1\sigma$
(1, 2)	0.4	$0.2\sigma$
(0, 3)	1.4	$0.7\sigma$
(1, 0)	0.6	$0.3\sigma$
(5, 0)	0.6	$0.3\sigma$

# WMAP alone

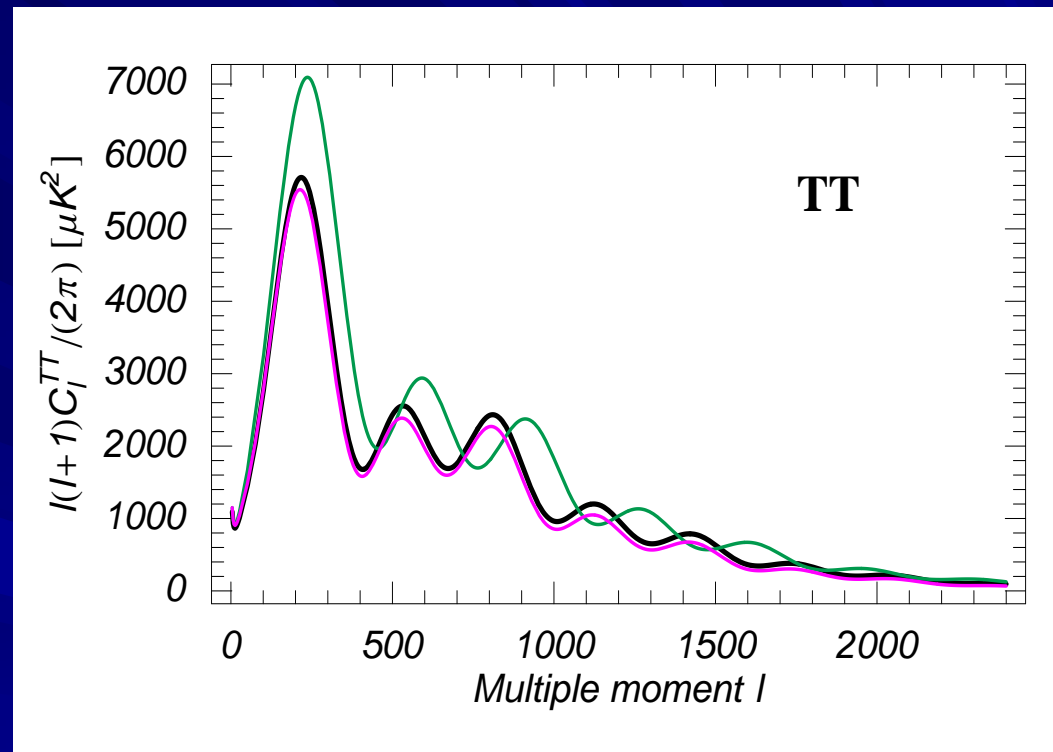
- WMAP cannot rule out coupled neutrinos, tells you little about  $N_{\text{coupled}}, N_{\text{FS}}$
- Parameter degeneracies
  - $N_{\text{FS}}$  Preserve  $z_{\text{eq}}$  by raising  $\Omega_m h^2$ , compensate other residuals by bias and  $n_s$
  - $N_{\text{coupled}}$  Compensate primarily by bias and  $n_s$



$N_{\text{coupled}}$	$n_s$	$\log(10_{10} A_s)$
0	.95	3.0
1	.93	2.9
3	.90	2.8

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$N_{\text{FS}}$	$\Omega_m h^2$	$n_s$	$\log(10_{10} A_s)$
3	.11	.95	3.0
5	.07	.91	2.9
1	.14	.97	3.1

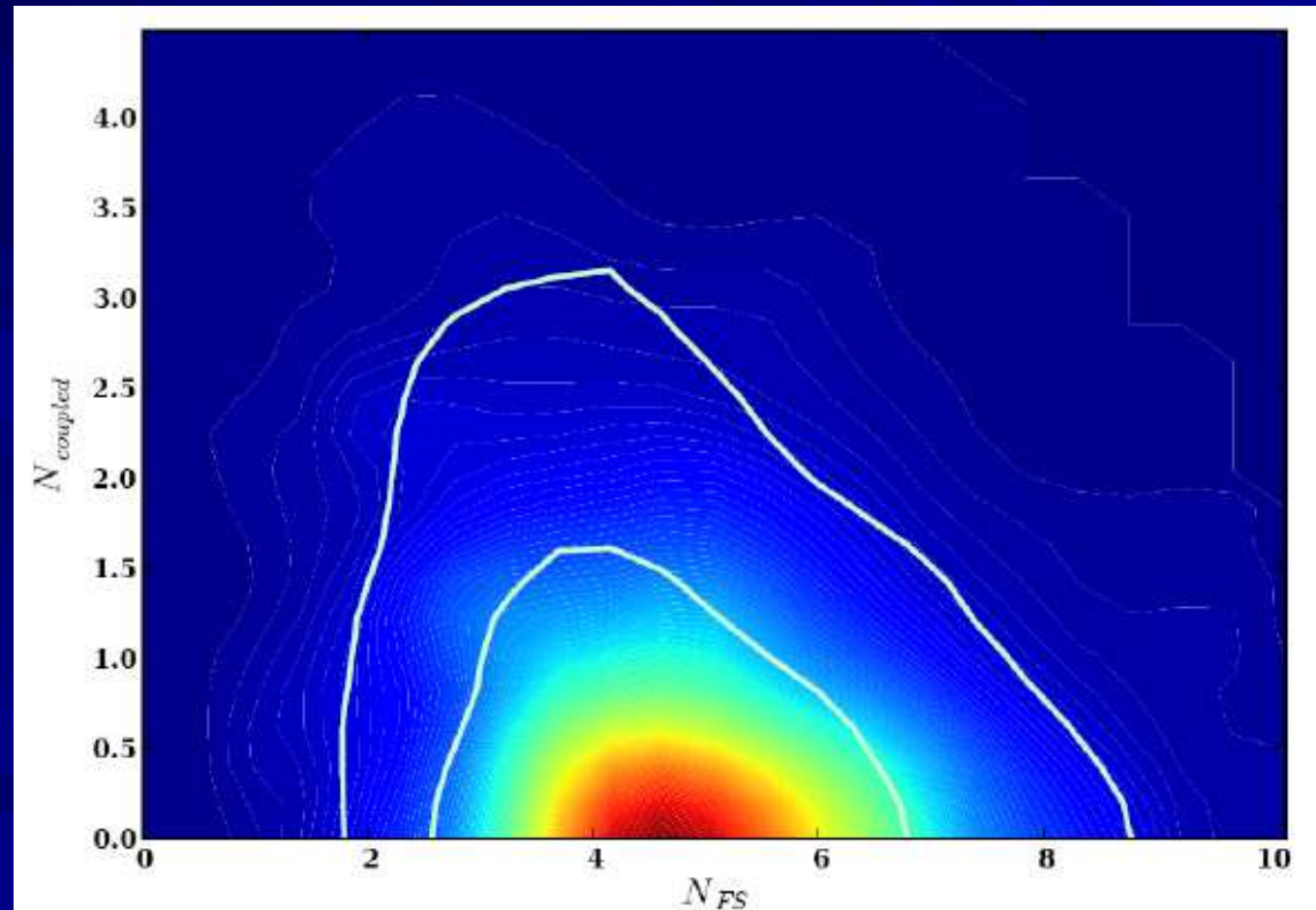


# WMAP+LSS+HST+SN Ia

- The LSS data do help break degeneracies
- ...But it depends strongly on which data are used
- SDSS main and LRG data samples are not equivalent

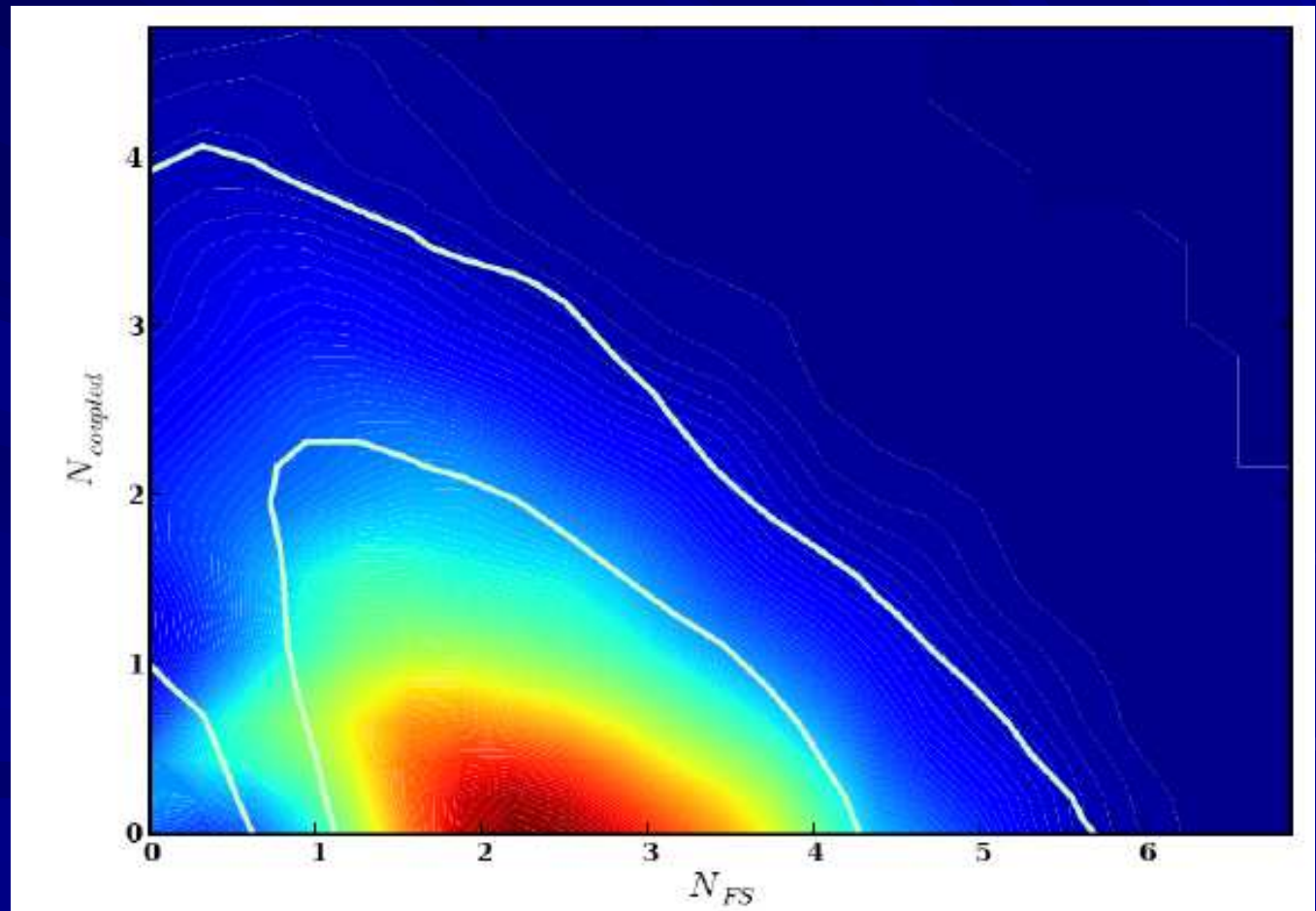
# WMAP+2dF+SDSS main+HST+SNIa

- Best fit  
 $N_{FS}=5$
- Excludes  
 $N_{coupled}=3$   
at  $> 3\sigma$



# WMAP+2dF+SDSS LRG+HST+SN Ia

- Best fit  
 $N_{FS}=3$
- $N_{\text{coupled}}=3$   
disfavored  
at  $< 2\sigma$



# Consistent with the trends in $N_{\text{FS}}$ observed in other works

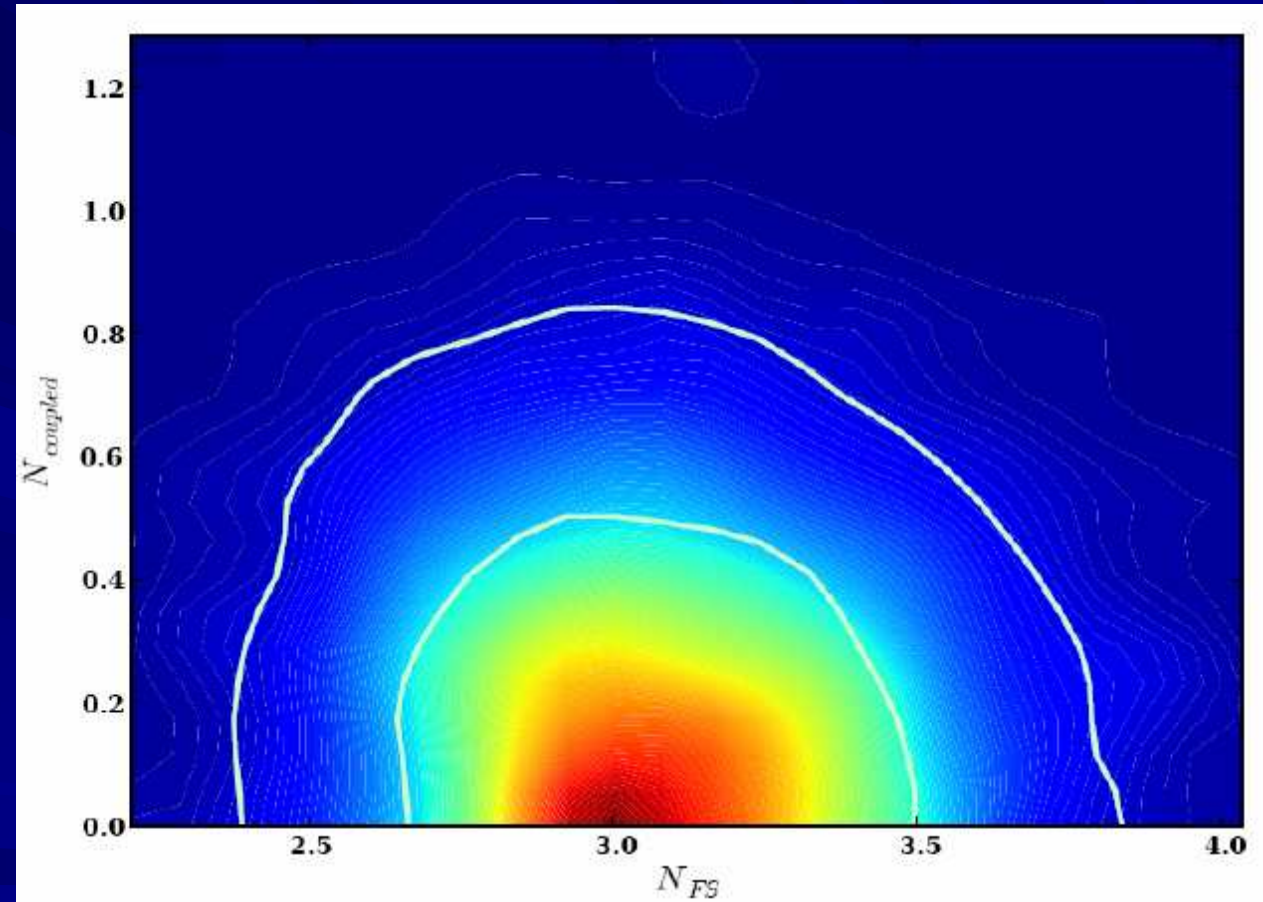
- LRG pulls the fit to smaller  $N_{\text{FS}}$ 
  - Ichikawa, Kawasaki, and Takahashi  $N_{\text{FS}}=3.1^{+5.1}_{-2.2}$
  - Hamann, Hannestad, Raffelt, Wong  $N_{\text{FS}}=2.7^{+6.2}_{-1.2}$
- $\text{Ly}\alpha$  tends to pull it up
  - Hamann, Hannestad, Raffelt, Wong  $N_{\text{FS}}=6.6^{+10}_{-3.3}$
  - Seljak, Slosar, McDonald All:  $N_{\text{FS}}=5.3^{+2.9}_{-1.7}$   
All –  $\text{Ly}\alpha$   $N_{\text{FS}}=3.9^{+2.9}_{-1.7}$
- Also shown to be sensitive to type of statistical inference utilized
  - Hamann, Hannestad, Raffelt, Wong

# At the end of the day....

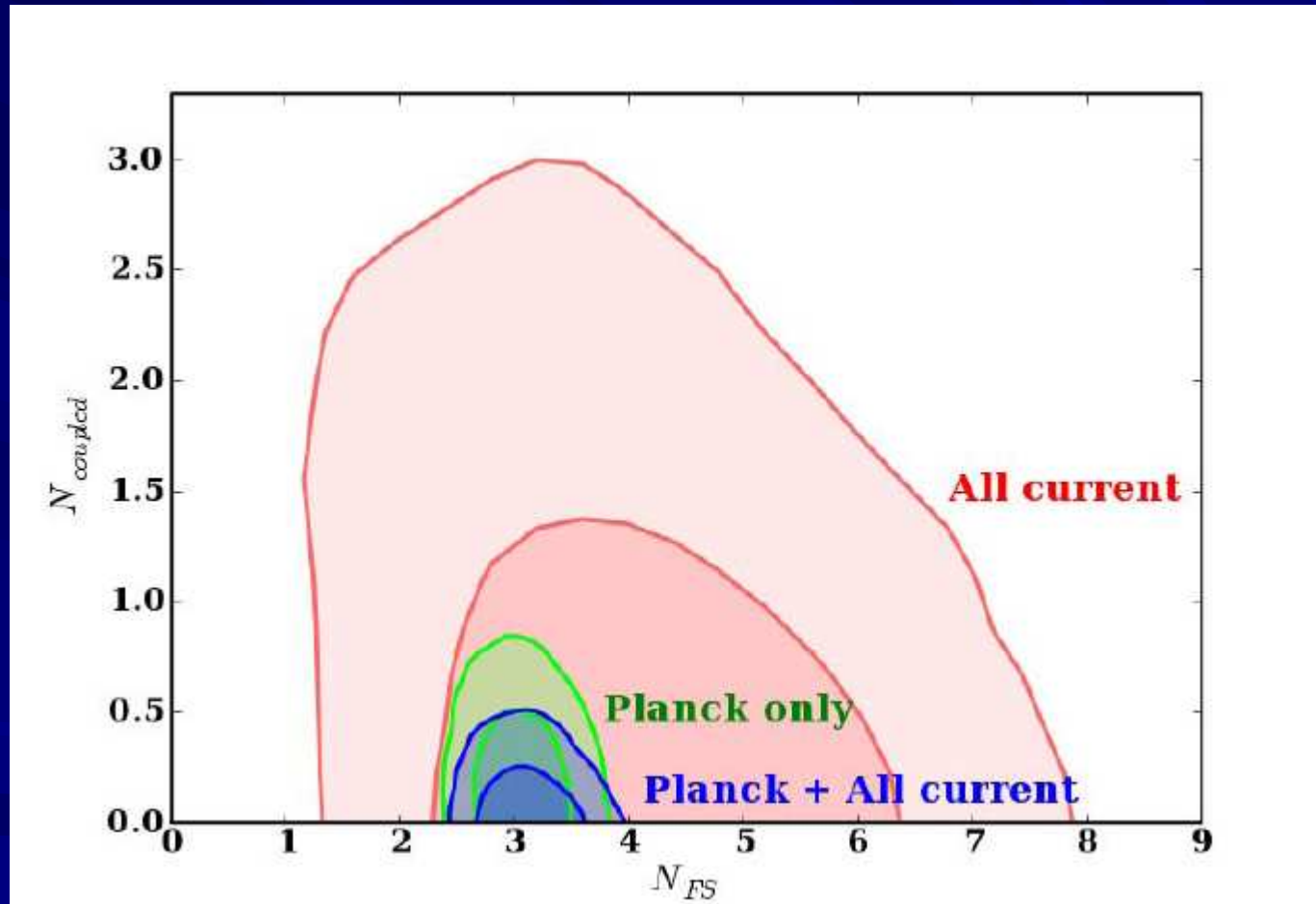
- Data consistent with 3 SM neutrinos
  - Seljak, Slosar, McDonald  $N_{\text{FS}}=5.3^{+2.9}_{-1.7}$
  - Large errors (+/- **several** neutrinos)
- Data constant with having those neutrinos coupled at CMB temperatures
  - Friedland, KZ, Bashinsky
- Strongly dependent on the data set
- **Constraints are not conclusive!**

# Planck trumps all

- Only Planck
- $\Delta N_{\text{FS}} = {}^{+0.5}_{-0.3}$
- $\Delta N_{\text{coupled}} = {}^{+0.4}$
- Other data doesn't change exclusion on  $\Delta N_{\text{FS}}$

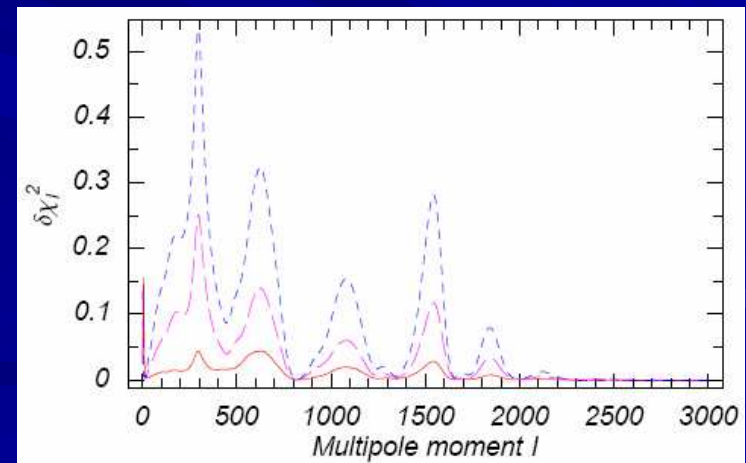
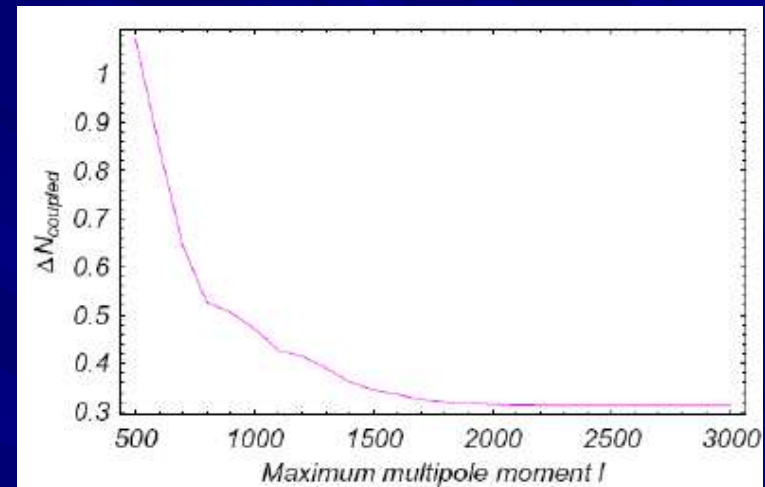


# Planck trumps all



# Why does Planck do so well?

- High multipole or good polarization info?





# Conclusions

- Many interesting models generate non-standard neutrino interactions
  - Neutrino see-saws
  - Majoron models
- These models may generate signals in CMB through removing neutrino free-streaming / populating extra states
- Some of the same models generate exotic Higgs physics
- While WMAP + all other data constrains rather little neutrino free-streaming and additional thermalized neutrinos, Planck will rule out (or detect at  $2 - 3 \sigma$  level) single coupled neutrino or additional neutrinos.