

Beam Position Monitor for Low Energy Antiprotons at the USR

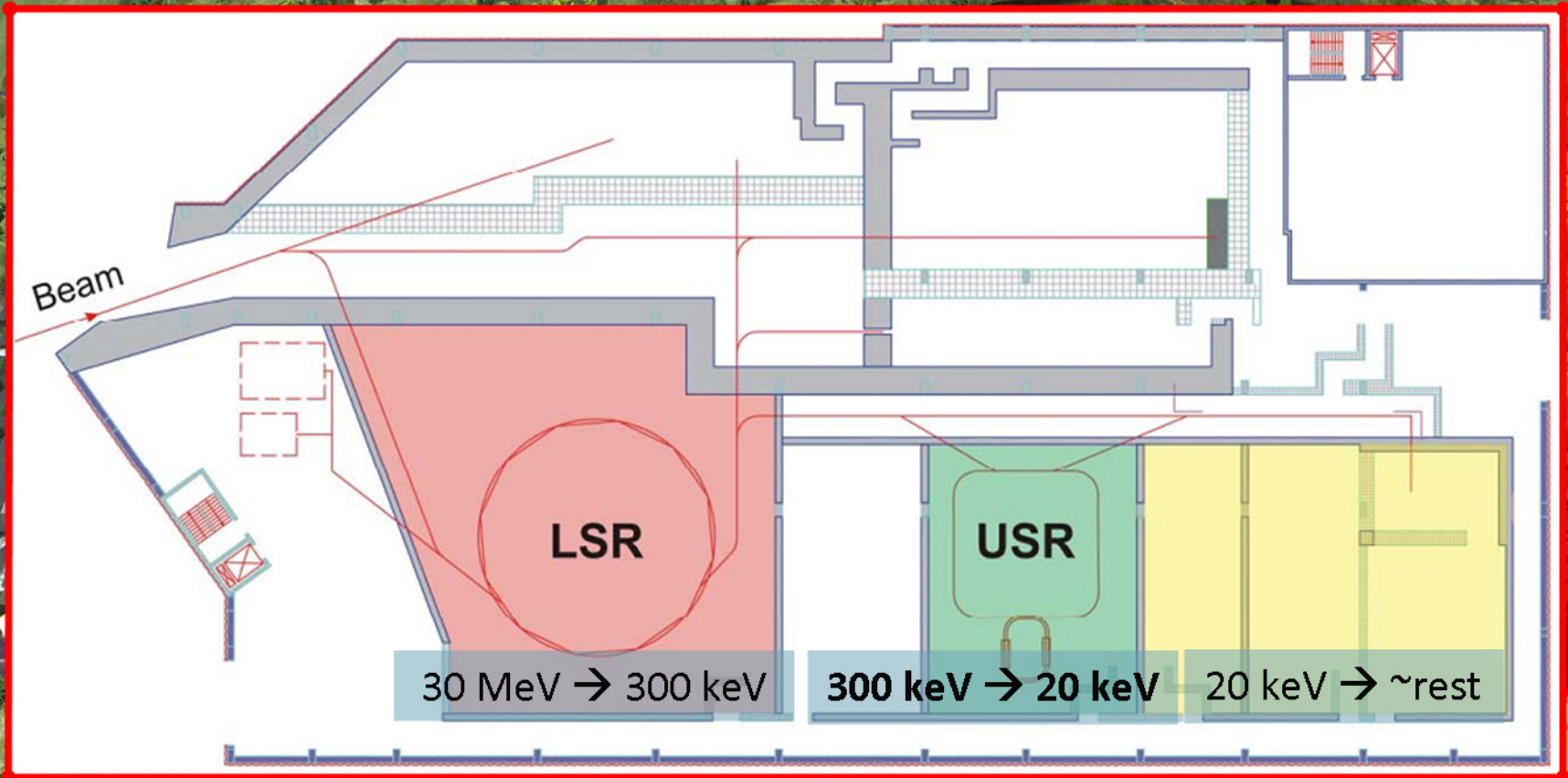
Janusz Harasimowicz

University of Liverpool
Cockcroft Institute



FAIR @ GSI

Facility for Antiproton and Ion Research



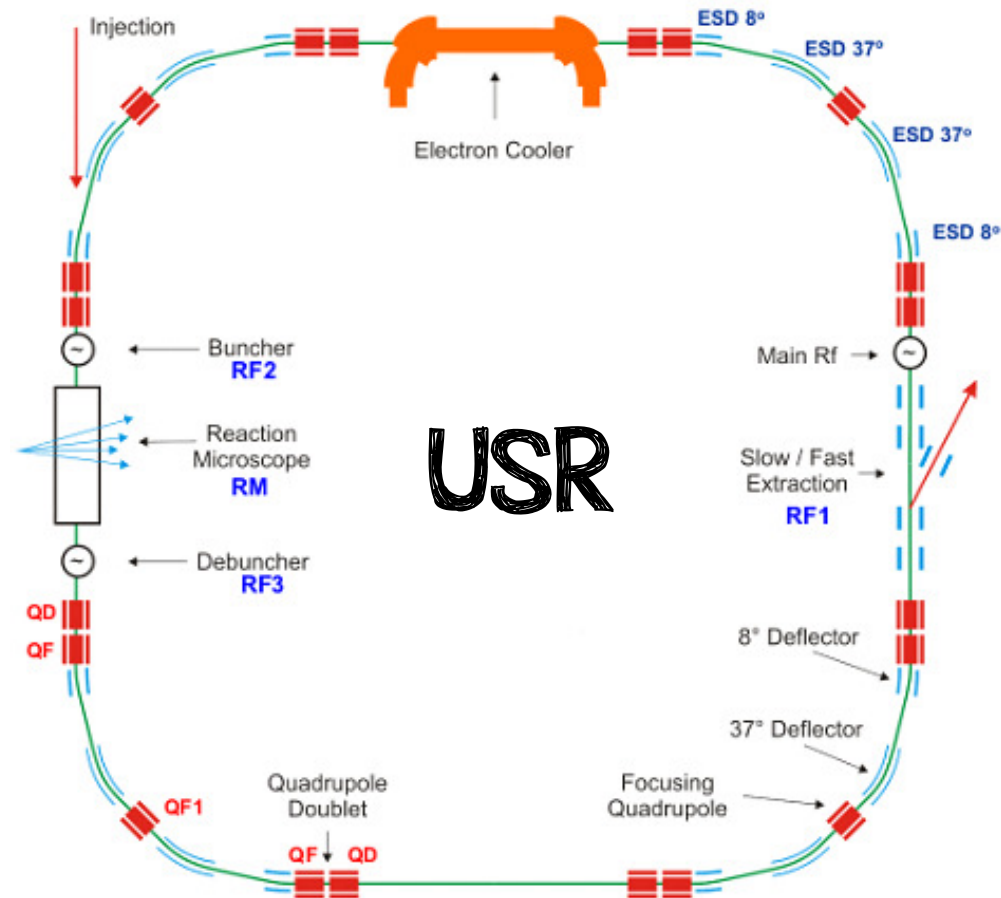
Ultra-low Energy Storage Ring

USR @ FLAIR

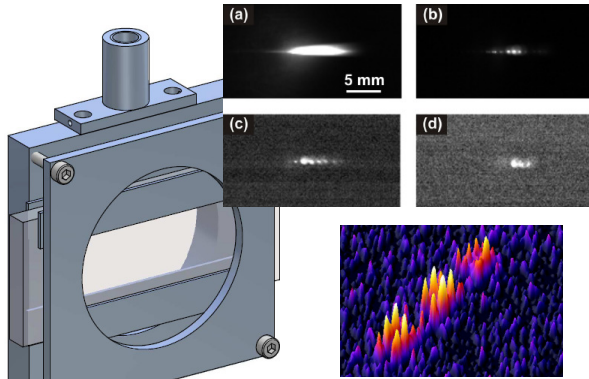
Facility for Low-energy Antiproton and Ion Research

Ultra-low Energy Storage Ring

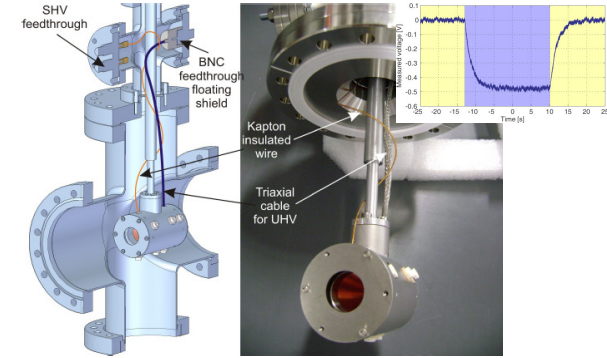
- Electrostatic ring
- Antiprotons & protons/ions
- Deceleration from **300 keV to 20 keV**
- Space charge limit: **2×10^7 p @ 20 keV**
- Average currents: **~ 100 nA to ~ 1 μ A**



Beam Instrumentation

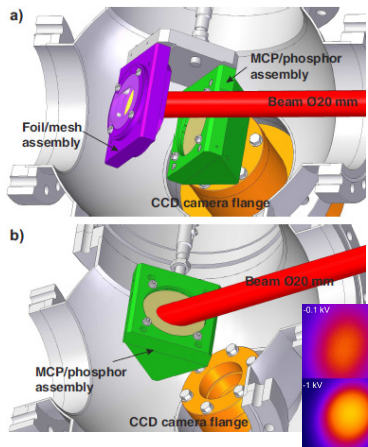


Scintillators

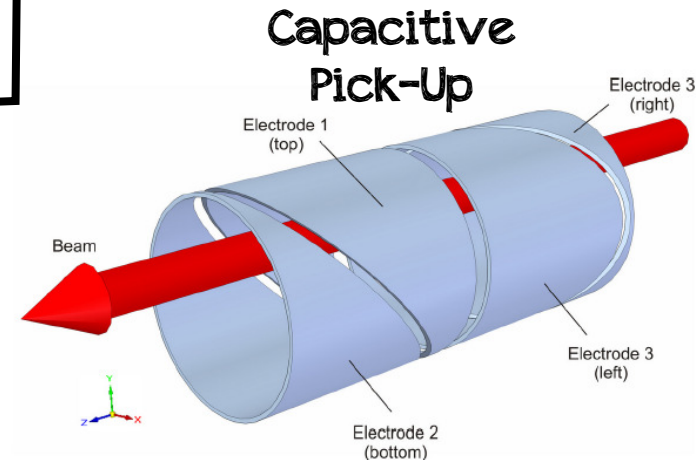


Faraday Cup

PhD
Project

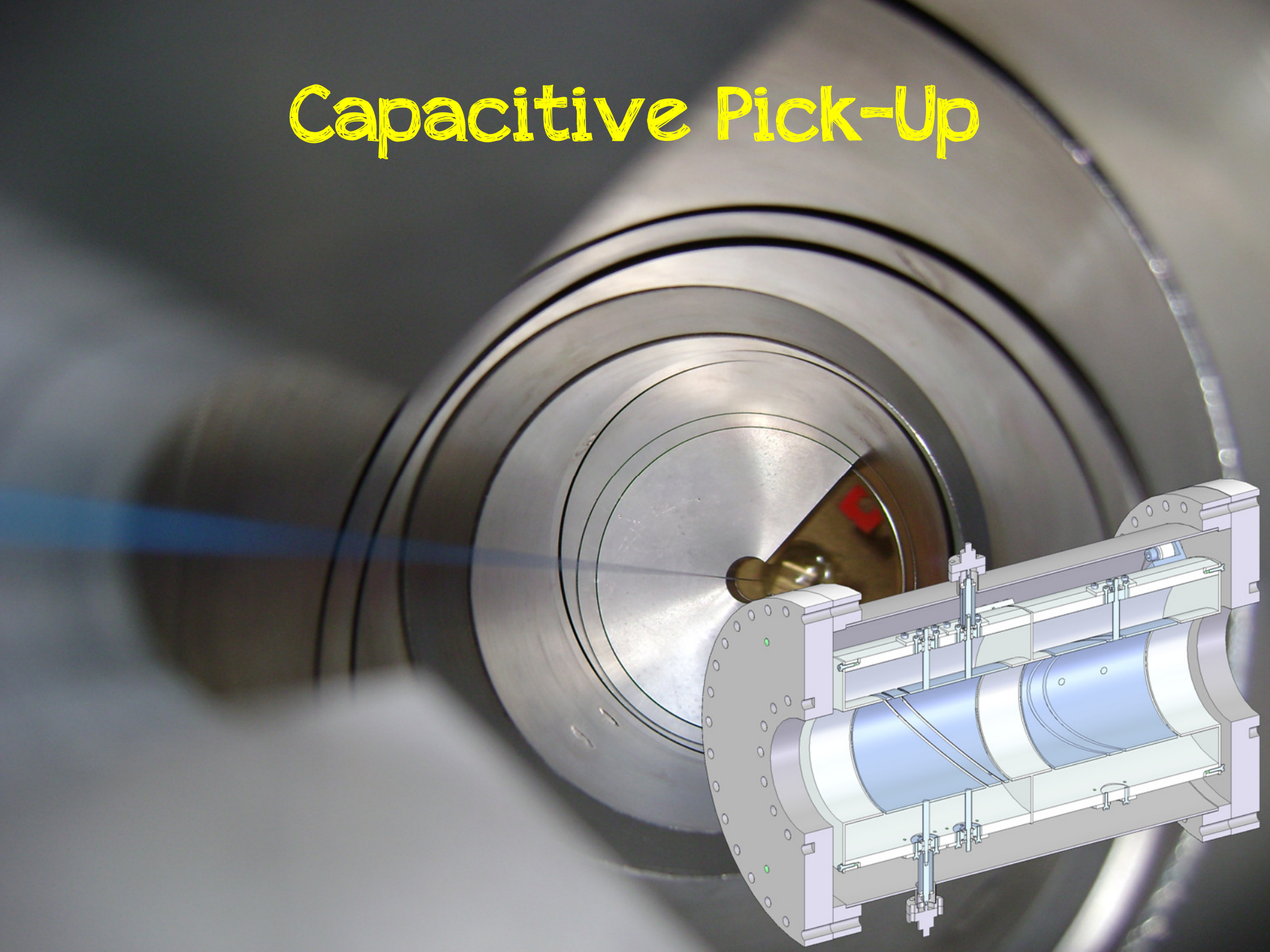


Secondary
Emission
Monitor



Capacitive
Pick-Up

Capacitive Pick-Up



Problem Statement

- Beam currents: ~ 100 nA - ~ 1 μ A
- Beam energies: 20 keV - 300 keV
- Rev. frequencies: ~ 50 kHz - ~ 200 kHz
- Both cooled and uncooled beams
- Resolution: < 0.5 mm
- Accuracy: < 0.5 mm

Diagonally Cut Pick-Up

$$x = k_x(x, y) \cdot \frac{\Delta U_x}{\Sigma U_x}$$

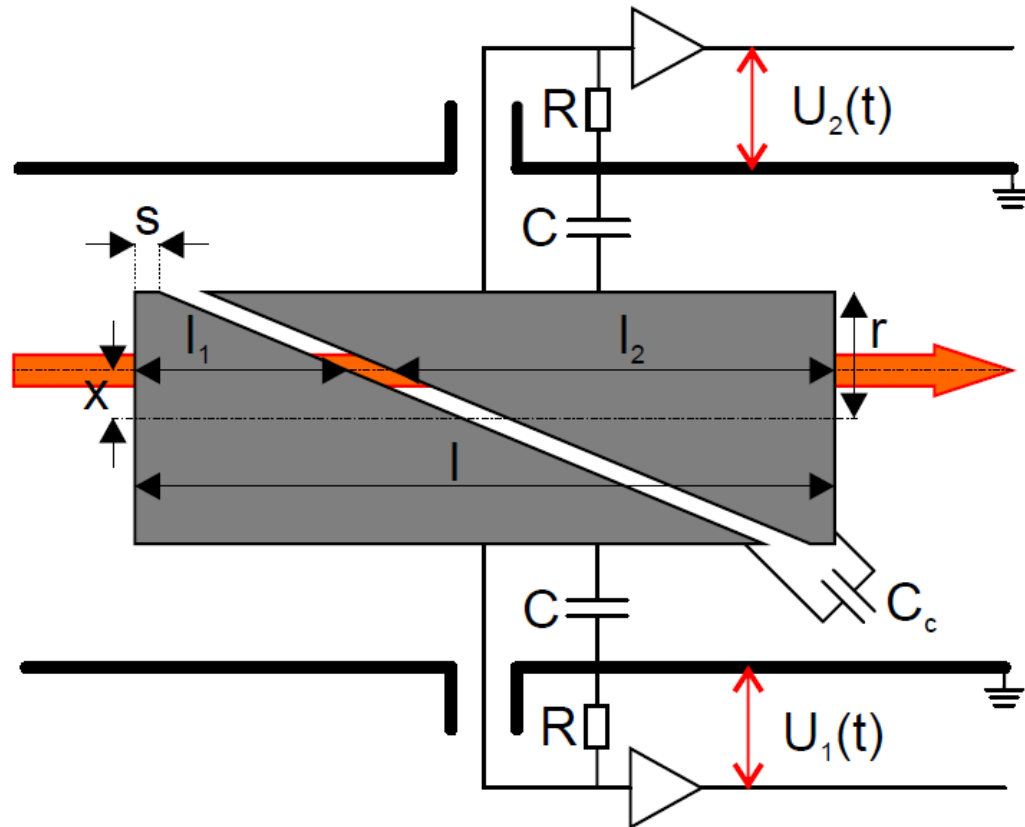
$$y = k_y(x, y) \cdot \frac{\Delta U_y}{\Sigma U_y}$$

$$\Sigma U = U_1 + U_2$$

$$\Delta U = U_1 - U_2$$

Diagonal cut:

$$k_x(x, y) = k_y(x, y) \equiv k = \text{const}$$



Diagonally Cut Pick-Up

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$$\Sigma U = U_1 + U_2$$

$$y = k_y(x, y) \cdot \frac{\Delta U_y}{\Sigma U_y}$$

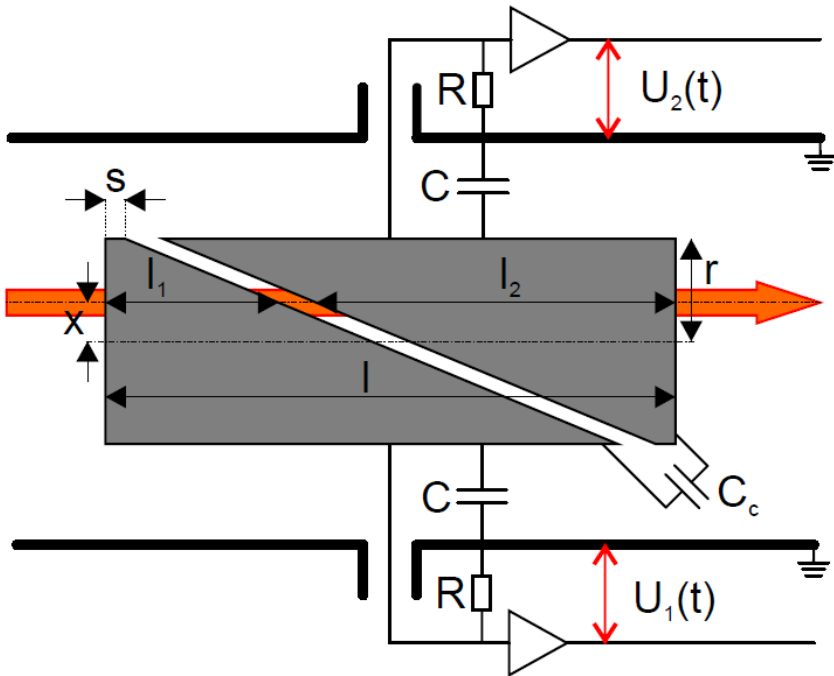
$$\Delta U = U_1 - U_2$$

Diagonal cut:

$$k_x(x, y) = k_y(x, y) \equiv k = \text{const}$$

$$k = \frac{r}{1 - 2 \cdot s/l} \cdot \left(1 + 2 \cdot \frac{C_c}{C}\right)$$

$$\hat{U} = \frac{1}{2} \cdot \frac{l}{C \cdot v} \cdot \bar{I}$$



Diagonally Cut Pick-Up

$$x = k_x(x, y) \cdot \frac{\Delta U_x}{\Sigma U_x}$$

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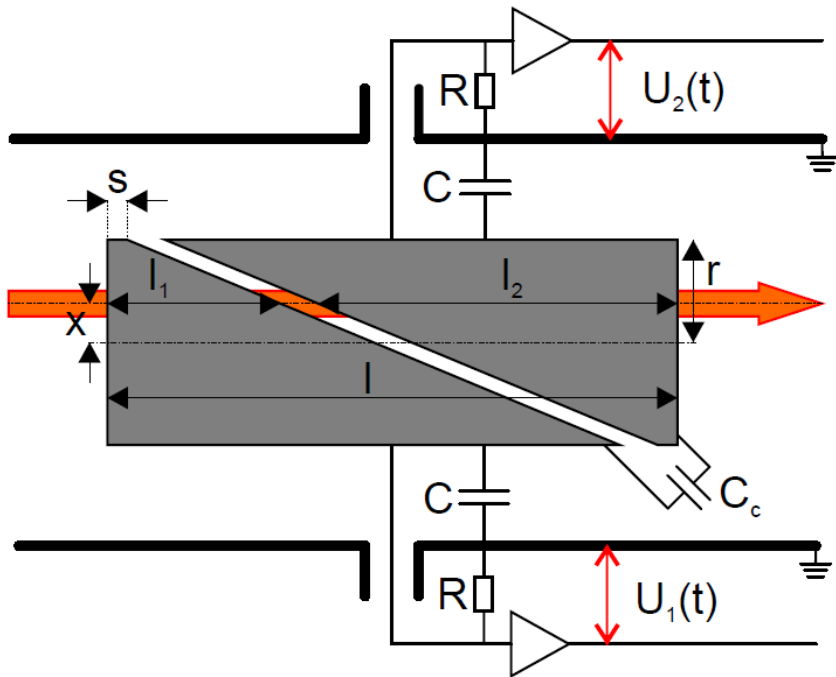
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USR example:

$$N = 2 \times 10^7, v = 0.006 c, I = 140 \text{ nA}$$

$$l = 100 \text{ mm}, C = 100 \text{ pF}$$

$$\Sigma U = 75 \mu\text{V}$$

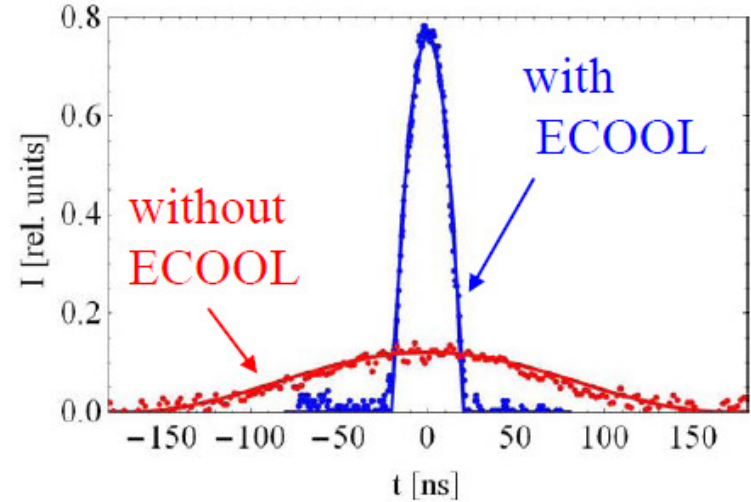
$$k = 100 \text{ mm}, x = 0.5 \text{ mm}$$

$$\Delta U = 375 \text{ nV}$$

$$\Delta U = 750 \text{ nV/mm}$$

Uncooled and Cooled Beams

$$I(t) = \sum_{n=0}^{\infty} I_n \cos(2 \cdot \pi \cdot n \cdot f_{RF} \cdot t)$$

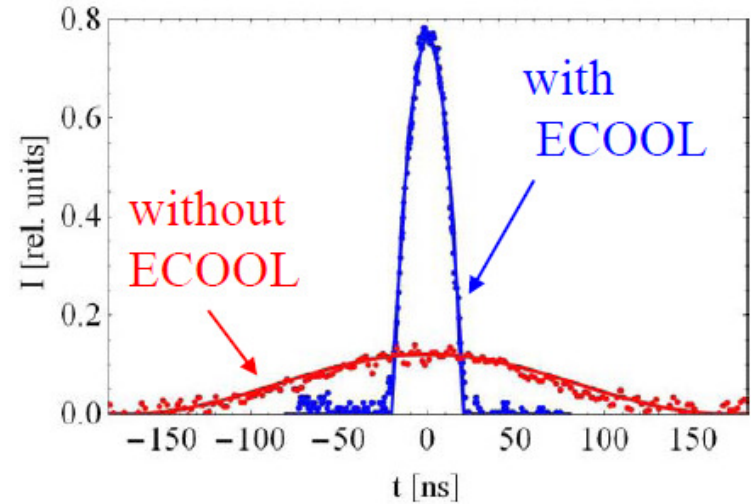


Uncooled and Cooled Beams

$$I(t) = \sum_{n=0}^{\infty} I_n \cos(2 \cdot \pi \cdot n \cdot f_{RF} \cdot t)$$

Uncooled beams:

$$I(t) = 2 \cdot \bar{I} \cdot \cos^2(\pi \cdot f_{RF} \cdot t)$$

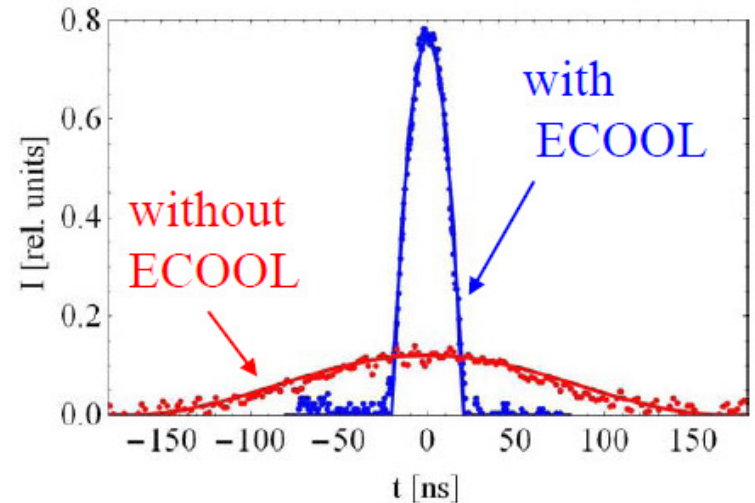


Uncooled and Cooled Beams

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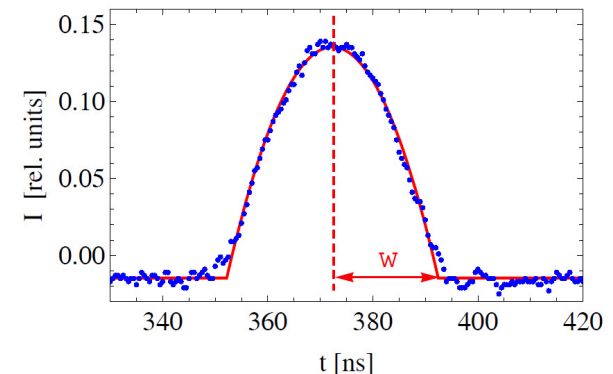
Uncooled beams:

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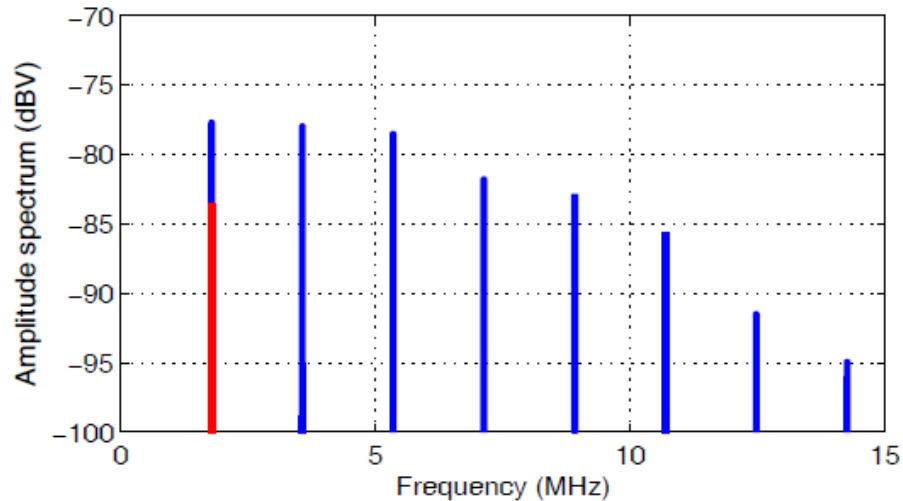
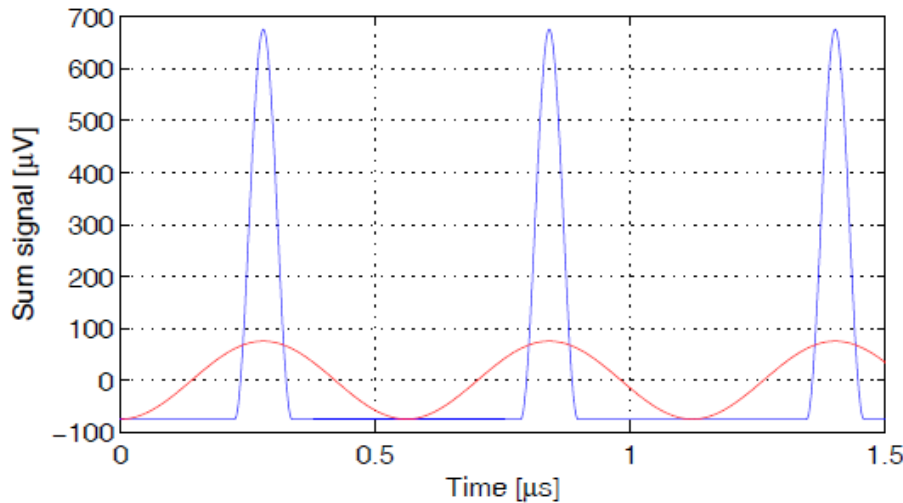


Cooled beams:

$$w = L_{ring} \cdot \sqrt[3]{\frac{3 \cdot \left(1 + 2 \cdot \ln \frac{R}{r}\right) \cdot \bar{I}}{2^4 \cdot \pi^2 \cdot c^4 \cdot \epsilon_0 \cdot \gamma^2 \cdot h^2 \cdot \beta^4 \cdot U_{RF}}}$$



Uncooled and Cooled Beams



USR example:

$$E = 300 \text{ keV}, N = 2 \times 10^7, h = 10$$

$$\Sigma U_{pk-pk} = \sim 150 \text{ } \mu\text{A}$$

$$\Delta U_{pk-pk} = \sim 1.5 \text{ } \mu\text{A/mm}$$

$$\Sigma U_{pk-pk} = \sim 750 \text{ } \mu\text{A}$$

$$\Delta U_{pk-pk} = \sim 7.5 \text{ } \mu\text{A/mm}$$

Noise Estimation

$$U_{noise} = \sqrt{\underbrace{e_{th}^2}_{\text{thermal contribution}} + \underbrace{|Z|^2 \cdot i_{amp}^2 + e_{amp}^2}_{\text{amplifier contribution}}} \cdot \Delta f \quad Z = (R^{-1} + i\omega C)^{-1}$$

$U_{noise} = 1 \text{ nV}/\sqrt{\text{Hz}}$	Δf	S/N			
		$\Delta U @ 0.1 \text{ mm}$	$\Delta U @ 0.5 \text{ mm}$	$\Sigma U_{uncooled}$	ΣU_{cooled}
Bunch structure	>20 MHz	0.02	0.09	33	170
Bunch by bunch	~2 MHz	0.06	0.3	100	530
Turn by turn	~200 kHz	0.2	0.9	330	1700

$\Delta f \ll 200 \text{ kHz}$: closed orbit measurements

Position Uncertainty

$$\sigma_x = \sqrt{\left(\frac{\delta x}{\delta U_1} \cdot U_{noise}\right)^2 + \left(\frac{\delta x}{\delta U_2} \cdot U_{noise}\right)^2}$$

Assumption:

$U_{noise} \rightarrow$ dominant uncertainty contribution

$$\sigma_x = 2 \cdot k \cdot U_{noise} \cdot \frac{\sqrt{U_1^2 + U_2^2}}{(U_1 + U_2)^2}$$

Position Uncertainty

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$$\sigma_x(x=0) = \frac{k}{\sqrt{2}} \cdot \frac{U_{noise}}{U_{electrode}}$$

$$\hat{U} = \frac{1}{2} \cdot \frac{l}{C \cdot v} \cdot \bar{I} = \frac{1}{2} \cdot \frac{l}{L} \cdot \frac{N \cdot e}{C}$$

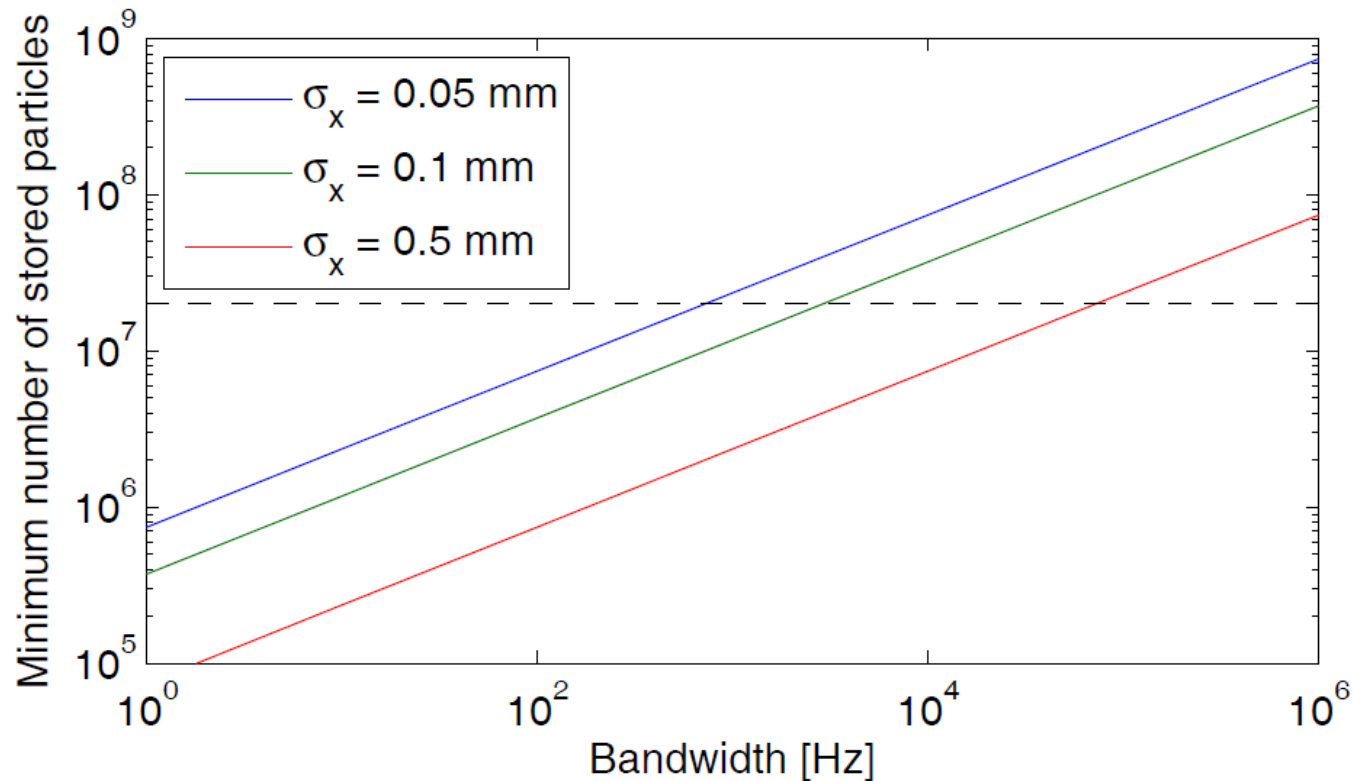
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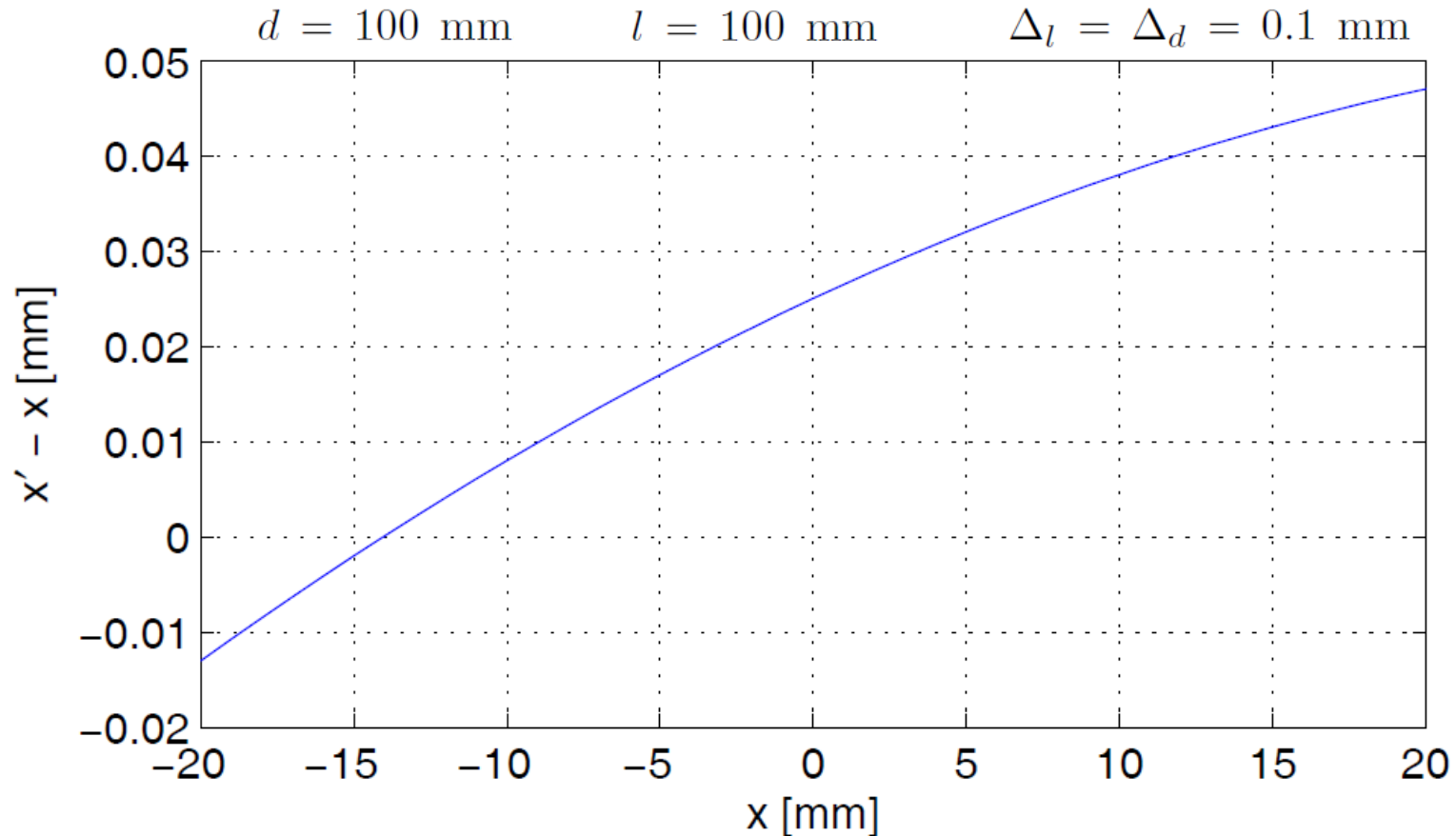
$\Delta f < 1$ kHz

Mechanical Tolerances

$$l_{left} = l \quad l_{right} = l - \Delta_l$$

$$d_{left} = d \quad d_{right} = d + \Delta_d$$

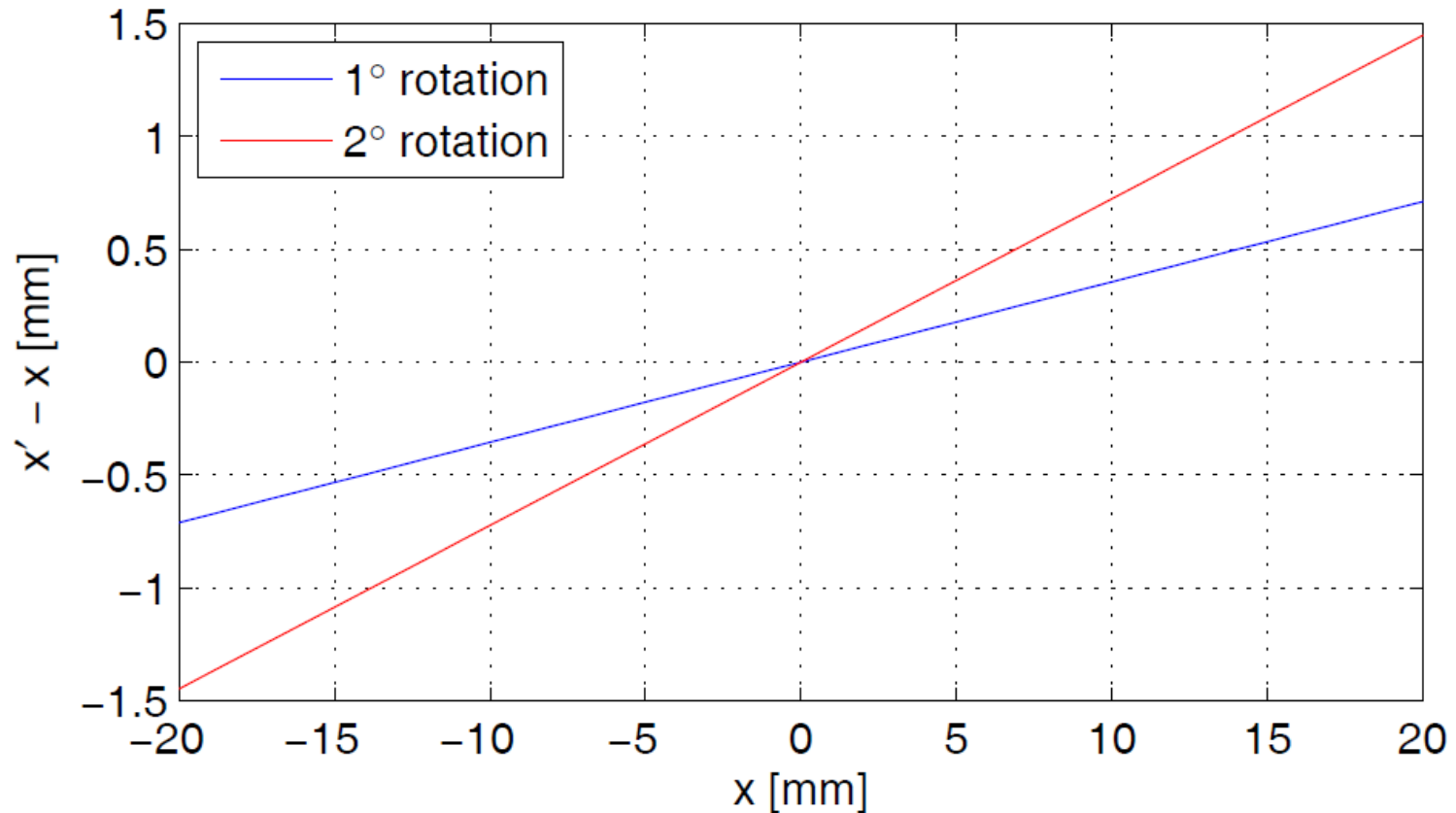
$$x' = k \cdot \frac{\Delta U}{\Sigma U} \cdot \frac{2 + \frac{\Delta_l}{l} \cdot \left(\left(\frac{\Delta U}{\Sigma U} \right)^{-1} - 1 \right)}{2 + \frac{\Delta_l}{l} \cdot \left(\frac{\Delta U}{\Sigma U} - 2 \right) + \frac{\Delta_d}{d} \cdot \left(\frac{\Delta U}{\Sigma U} - 2 \right)}$$



Misalignment

Rotation by a small angle α

$$x' = k \cdot \frac{\Delta U}{\Sigma U} \cdot \frac{1 + \frac{l}{d} \cdot \alpha}{1 - \frac{l}{d} \cdot \alpha}$$



Signal Quantization

Quantization step size: $U_q = \frac{2 \cdot U_{adc}}{2^b - 1}$

Number of bits: b

Input range: $\pm U_{adc}$

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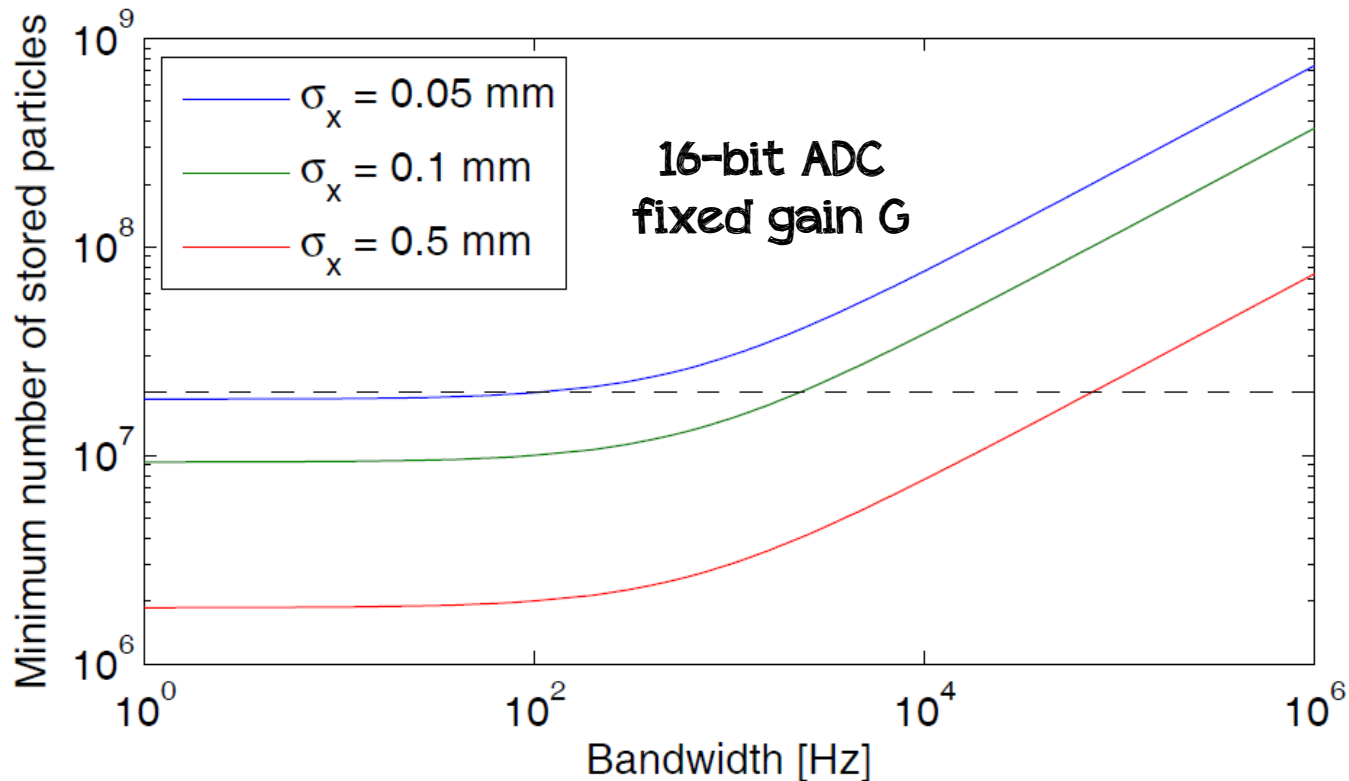
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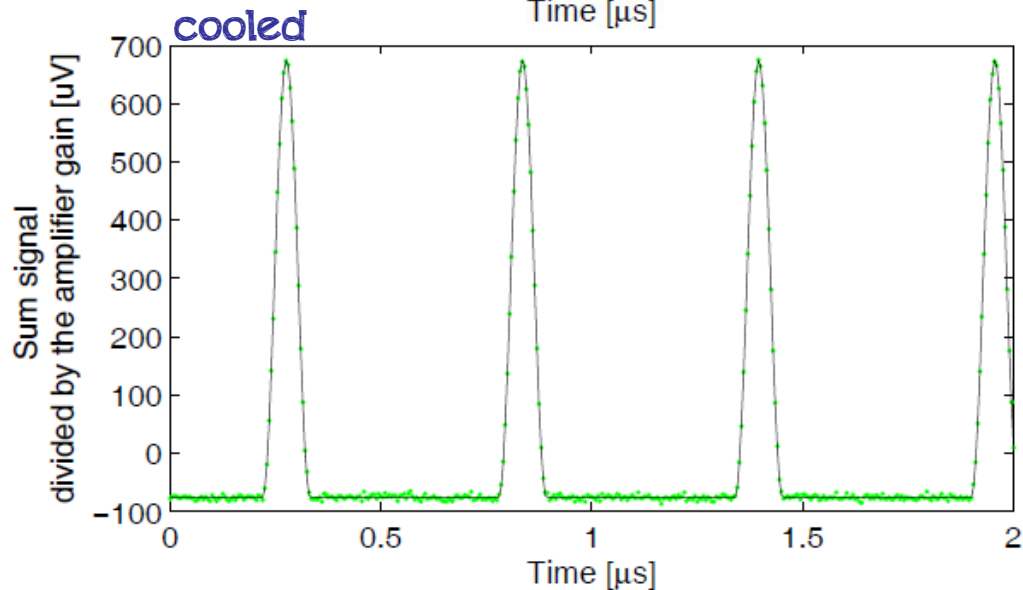
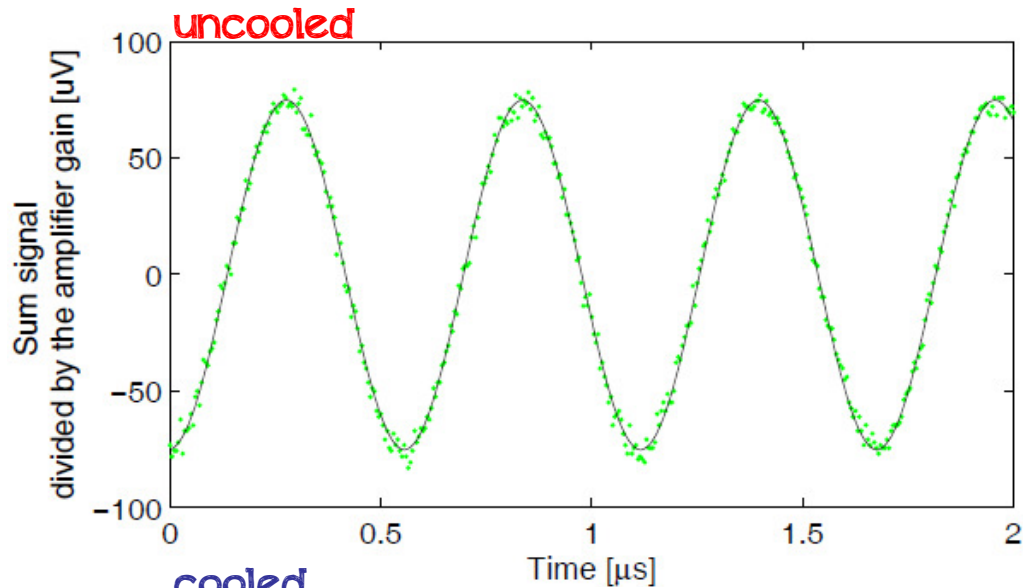
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Signal Quantization



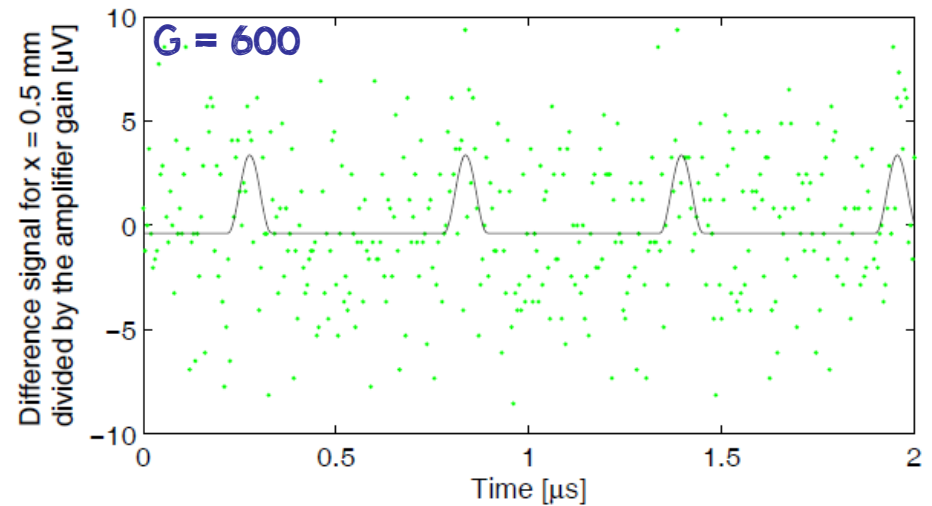
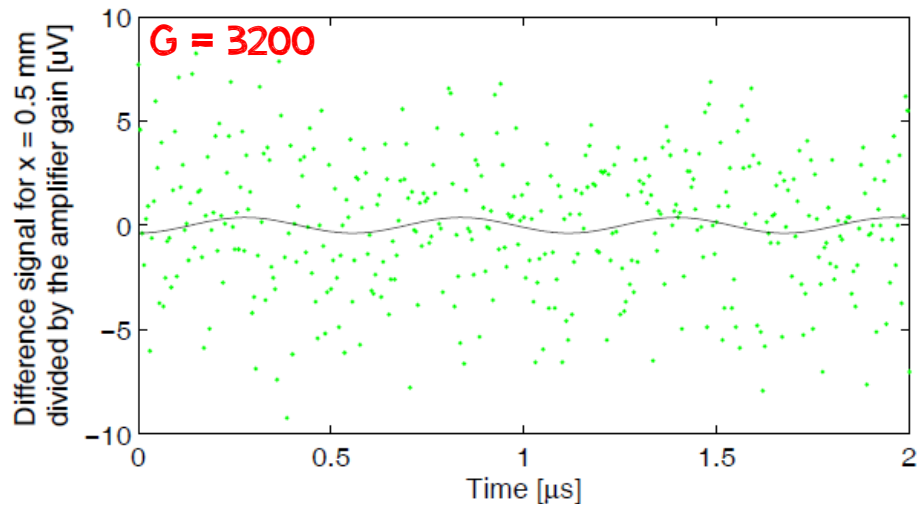
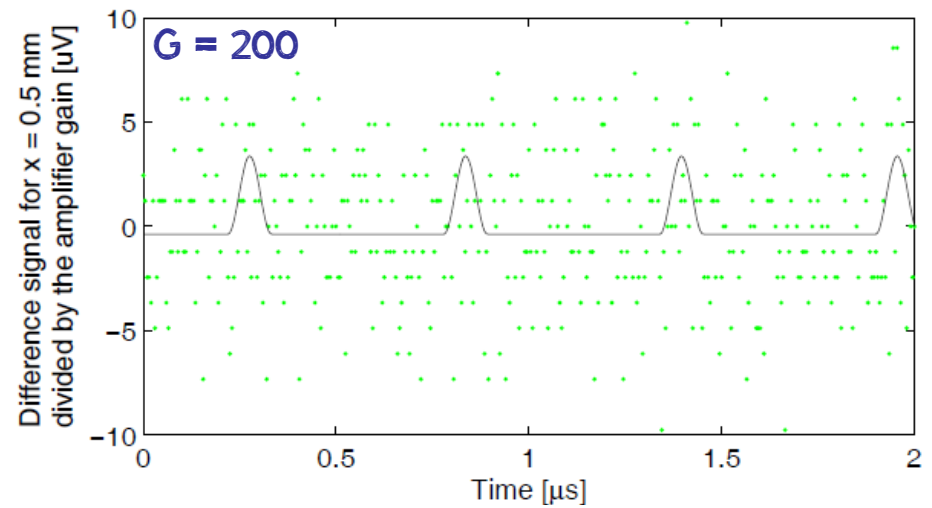
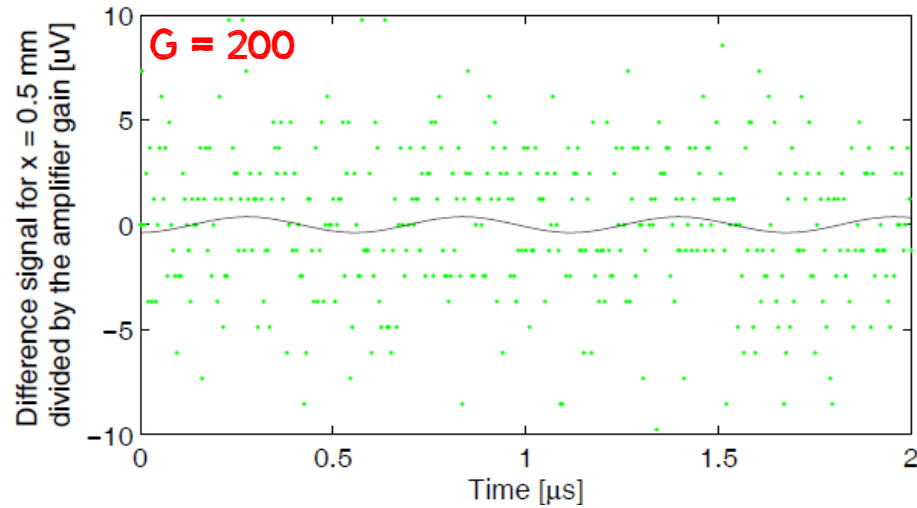
Example:

12 bit ADC, 200 MS/s, $G = 200$,
ADC input range ± 500 mV,
20 MHz bandwidth

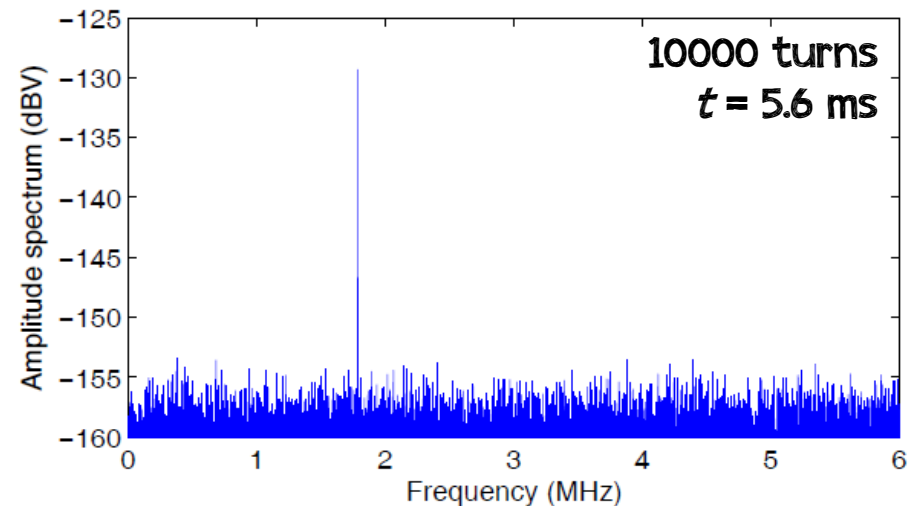
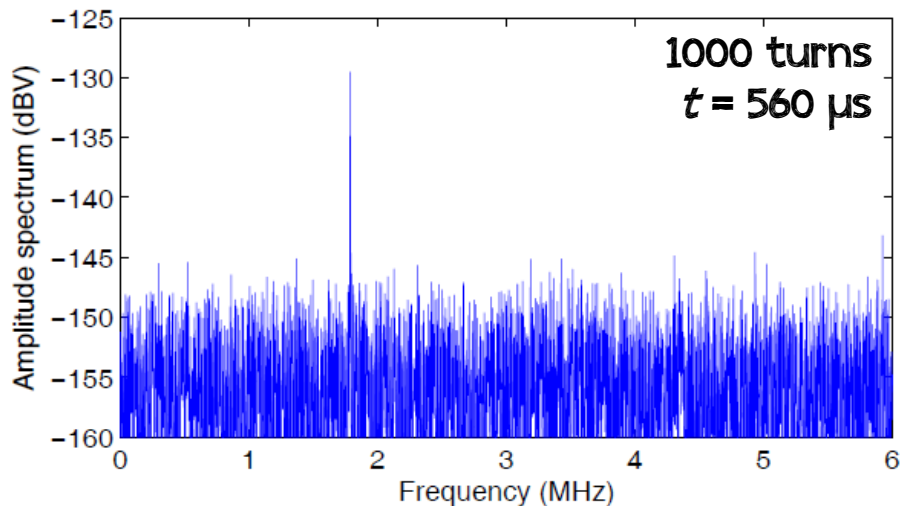
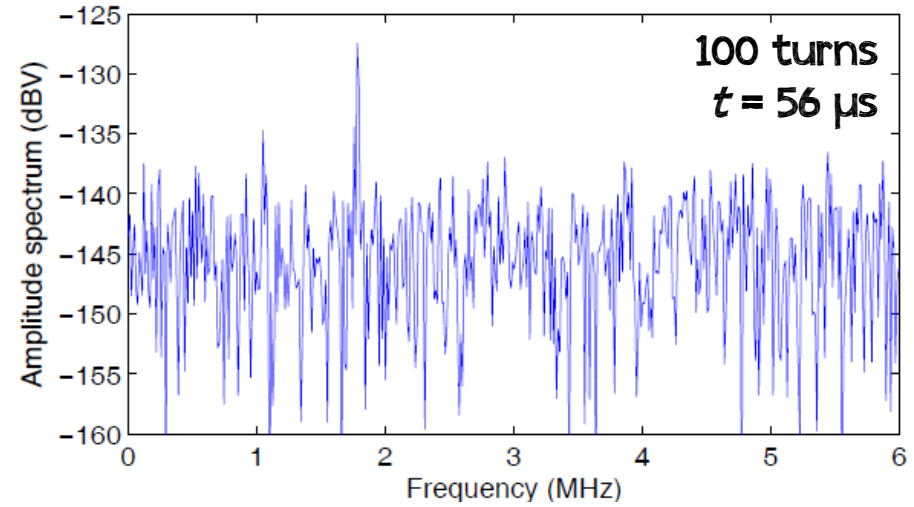
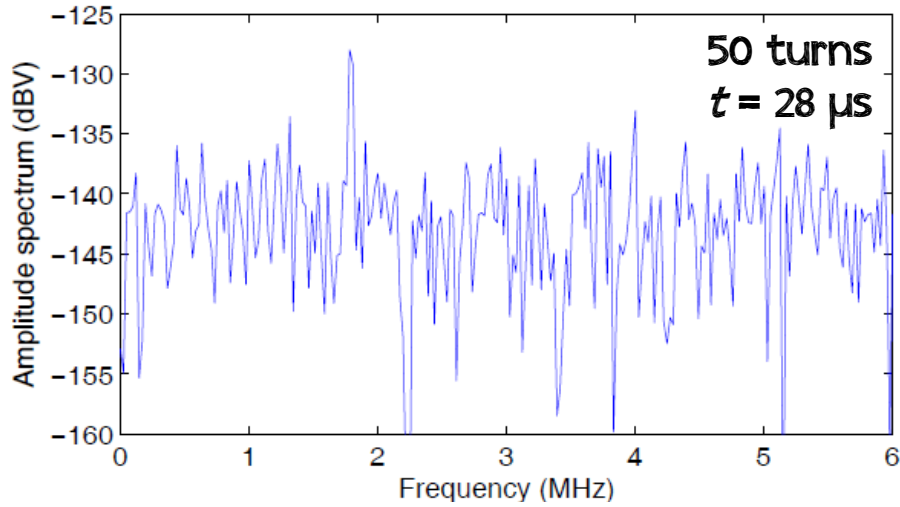
Noise:

- thermal
- amplifier
- ADC

Signal Quantization

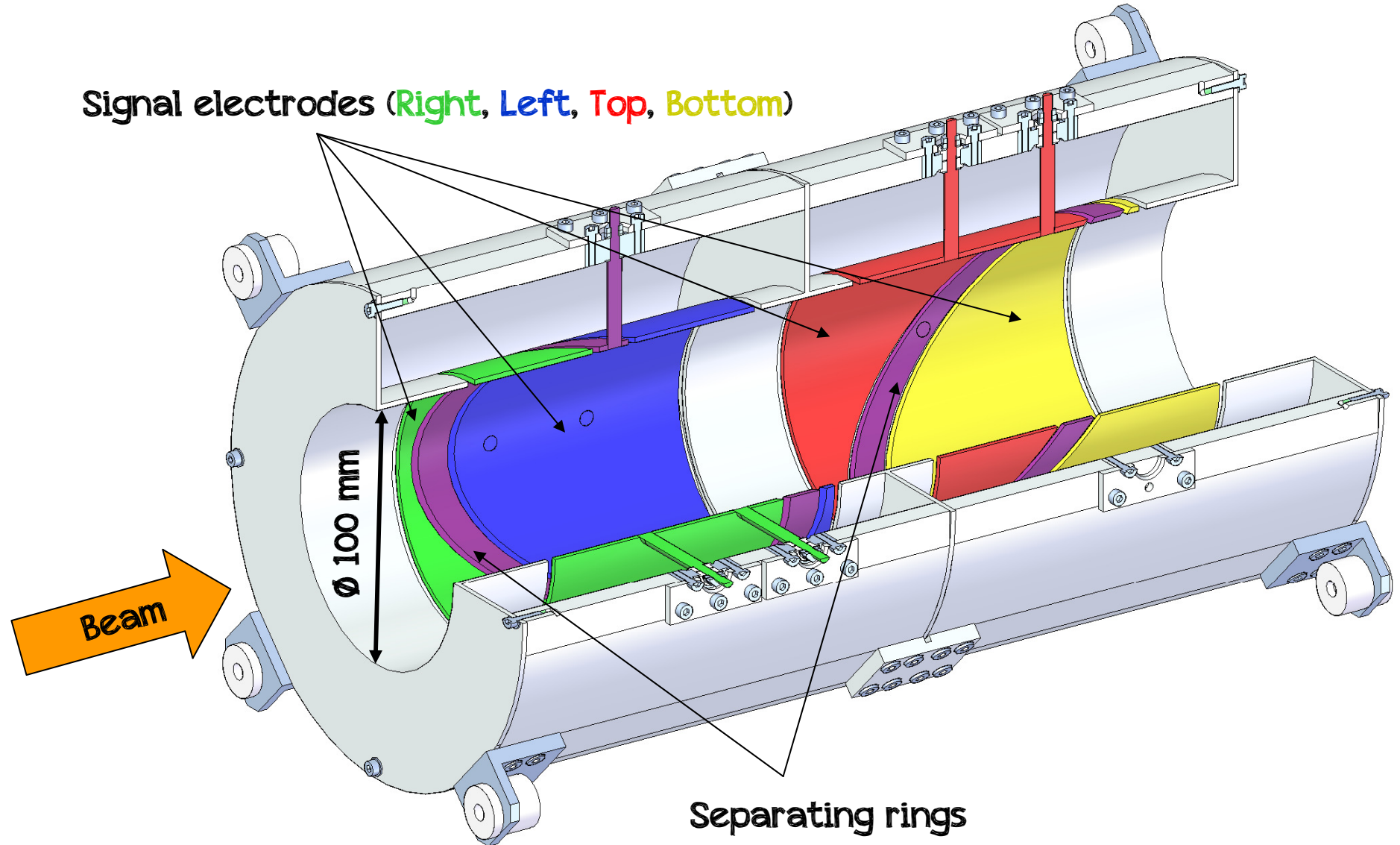


Spectrum



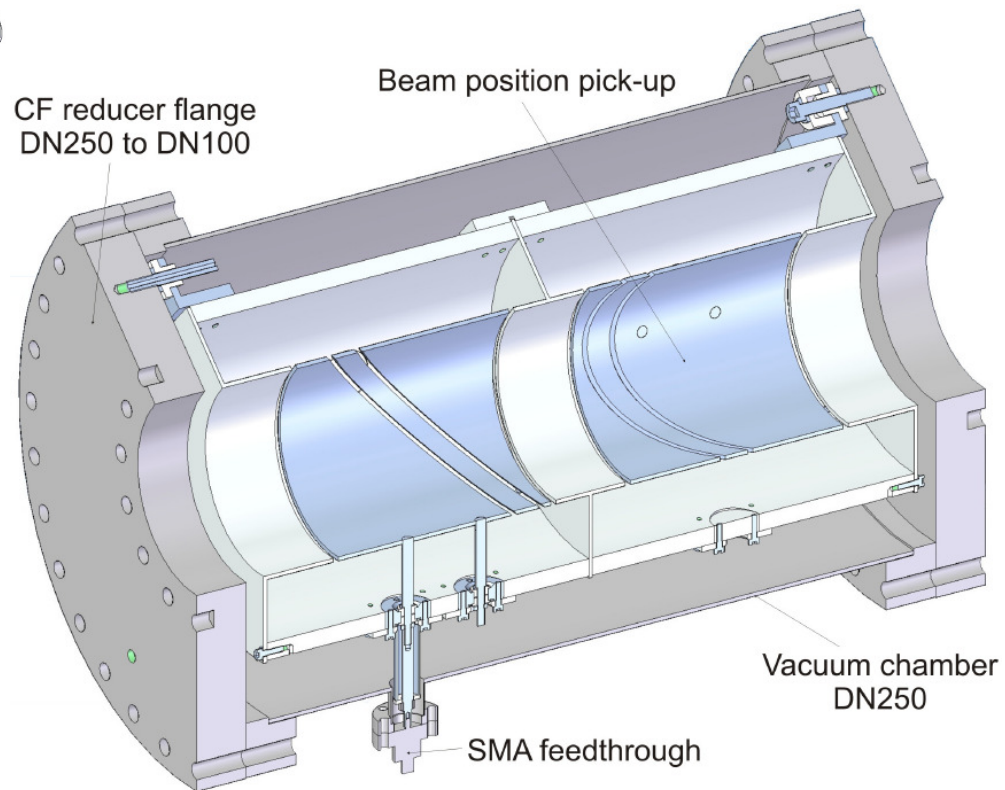
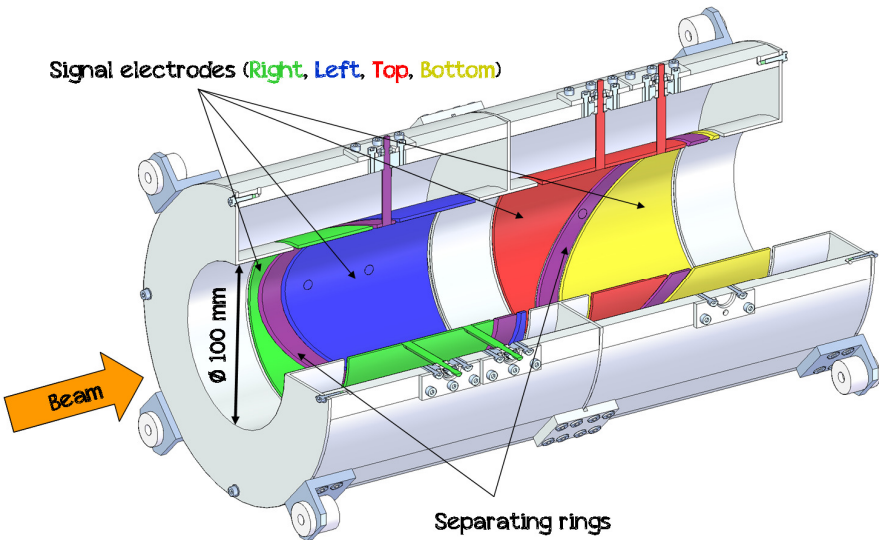
Pick-Up Prototype

Signal electrodes (Right, Left, Top, Bottom)



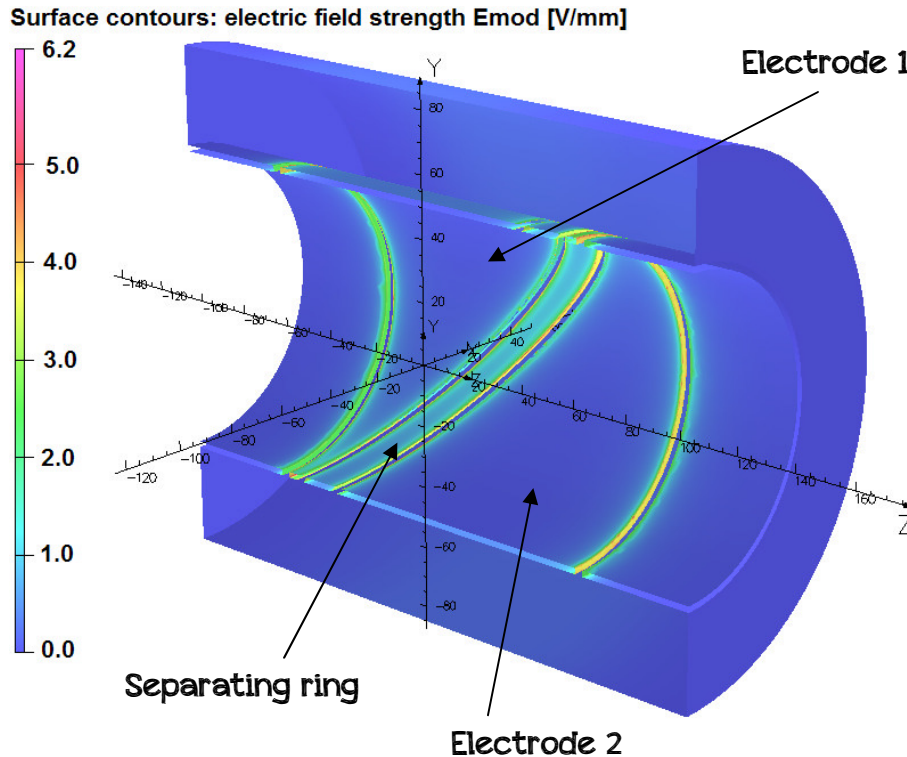
Separating rings

Pick-Up Prototype



Capacitance Simulations

Opera 3D, Tosca
Electrostatic Solver



1. No separating ring:

$$C = 13.7 \text{ pF}$$

$$C_c = 3.1 \text{ pF}$$

$$C_c/C = 0.22$$

$$k = 78 \text{ mm}$$

2. Grounded ring:

$$C = 18.8 \text{ pF}$$

$$C_c = 1.2 \text{ pF}$$

$$C_c/C = 0.06$$

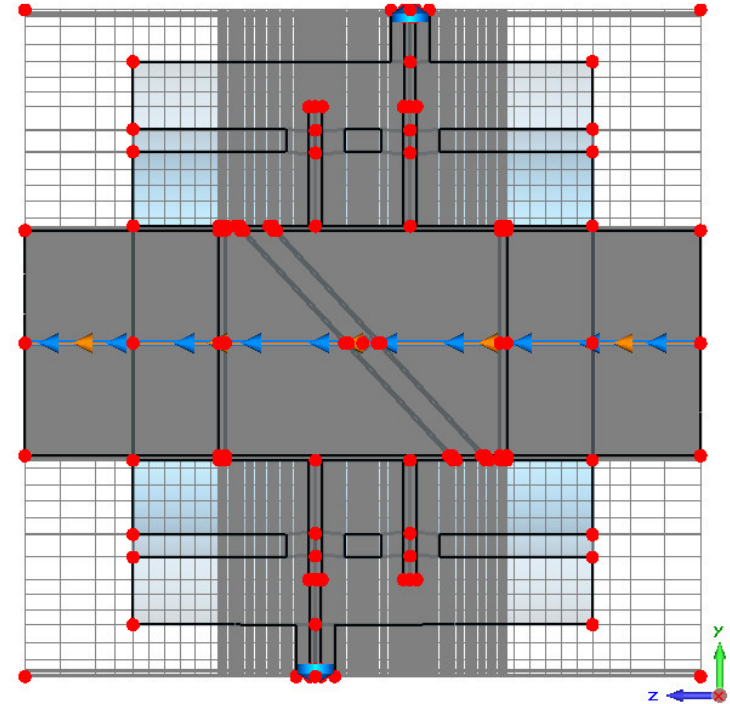
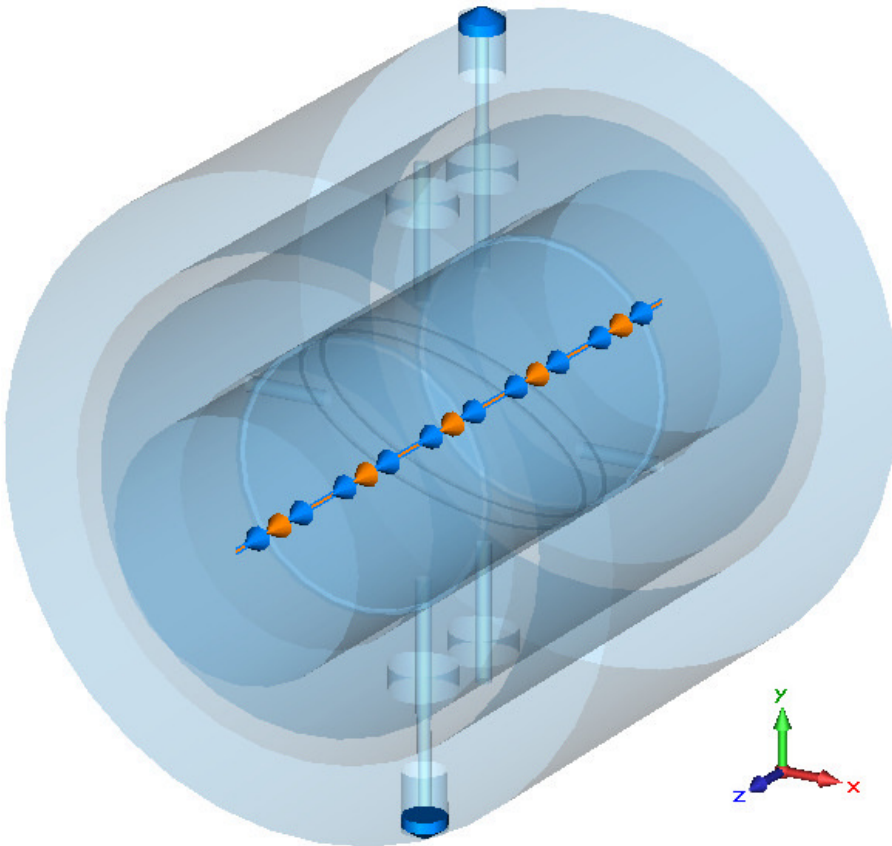
$$k = 60 \text{ mm}$$

Capacitance insensitive to a small tilt of the separating ring.

Real C increased by the contribution of the connections and the amplifier.

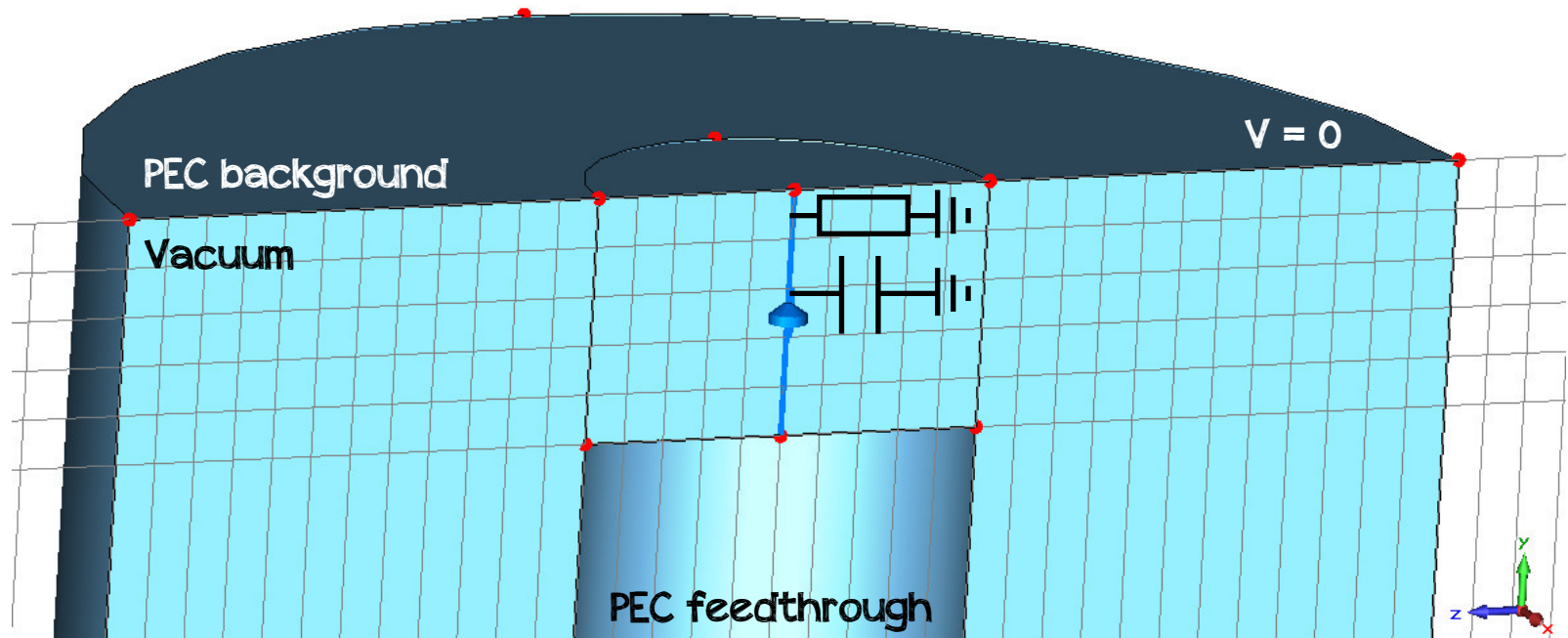
Pick-Up Response Simulations

CST Particle Studio
Wakefield Solver



$\sim 7 \times 10^6$ mesh cells (already reduced by a factor of 2 by a symmetry plane)

Pick-Up Response Simulations



Voltage monitored at lumped components attached to the feedthroughs with C and R of the amplifier input

Pick-Up Response Simulations

With the ring:

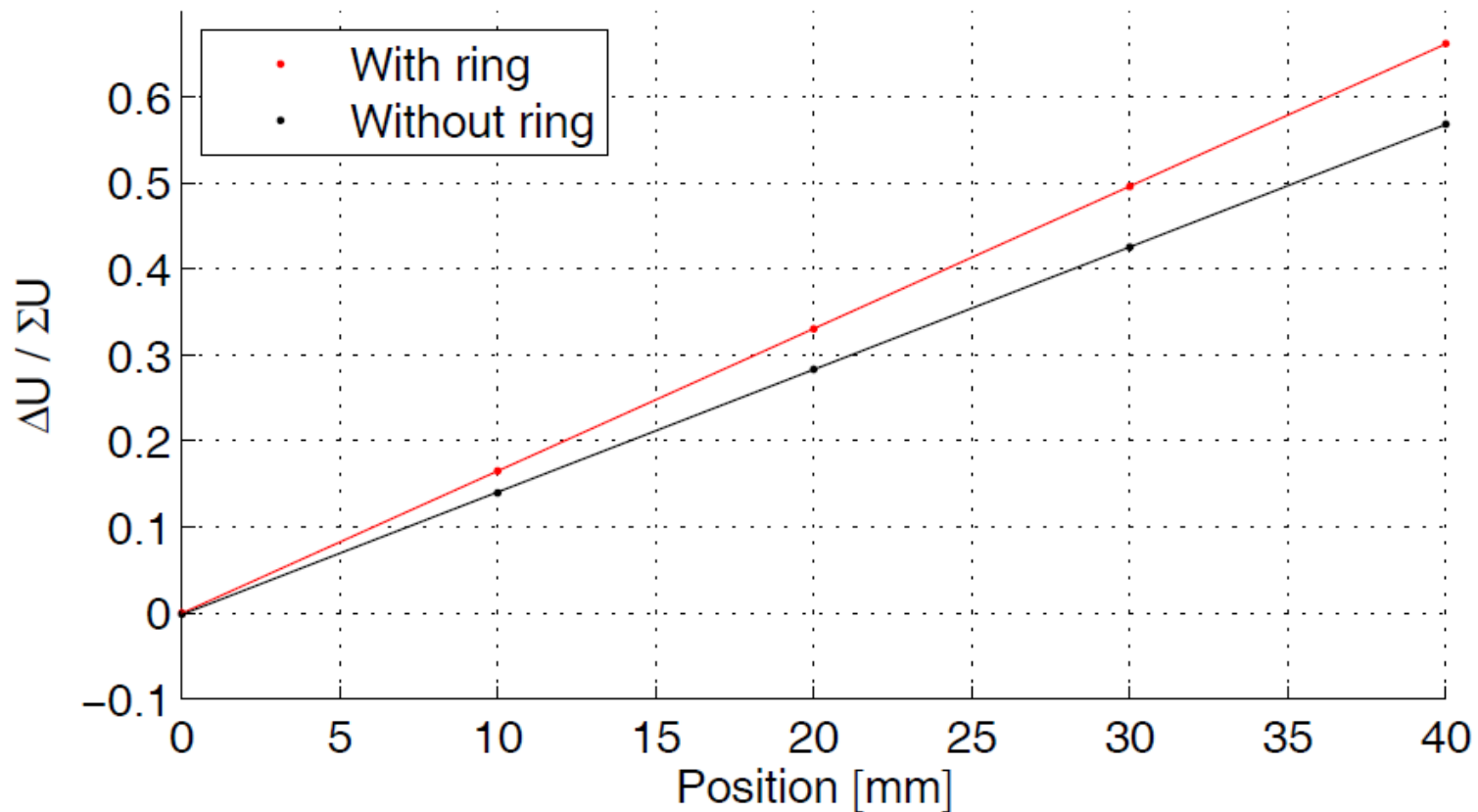
$$k = 60.4 \text{ mm} \pm 0.1 \text{ mm}$$

$$x_0 = 0.03 \text{ mm} \pm 0.02 \text{ mm}$$

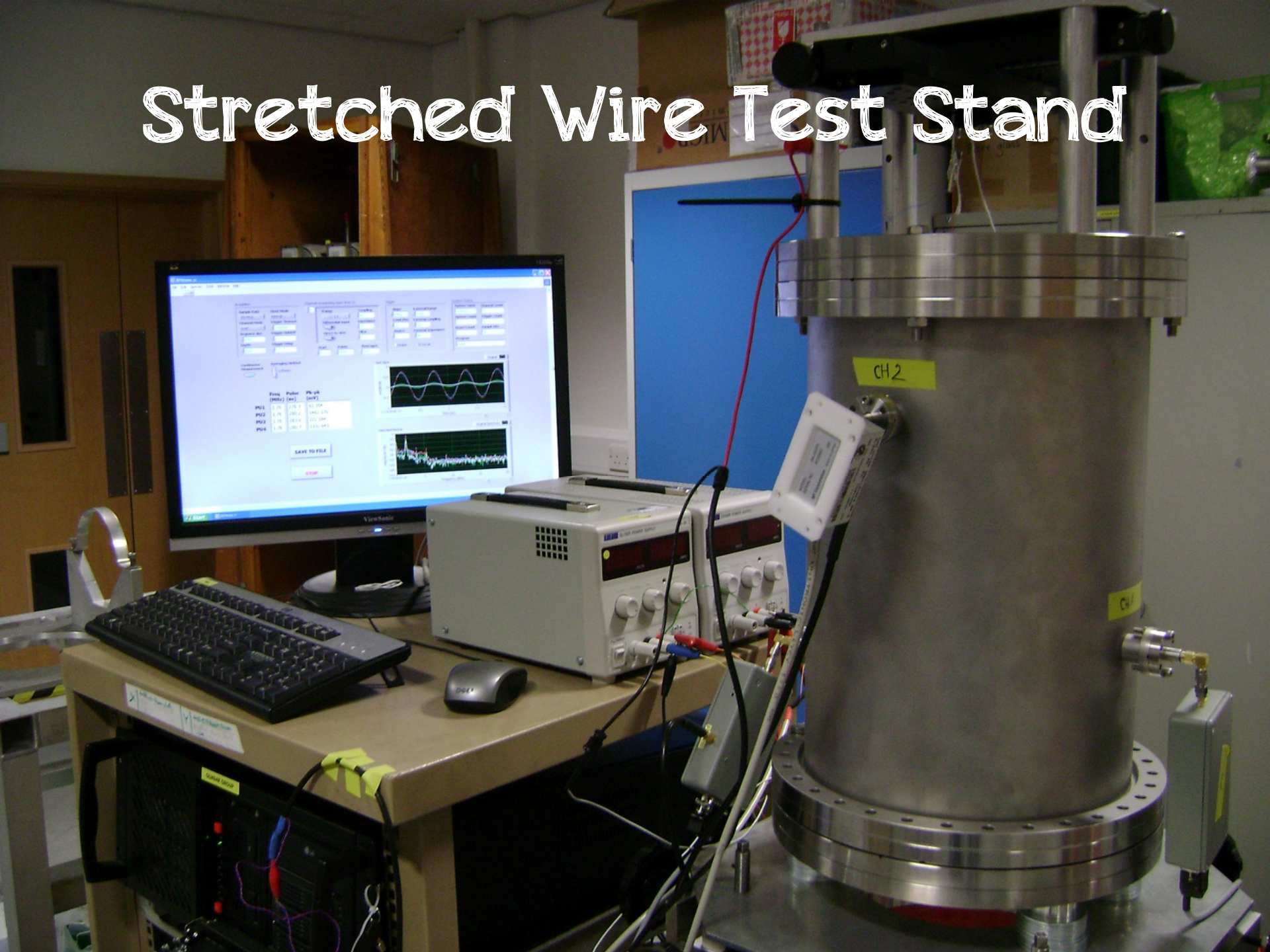
Without the ring:

$$k = 70.1 \text{ mm} \pm 0.1 \text{ mm}$$

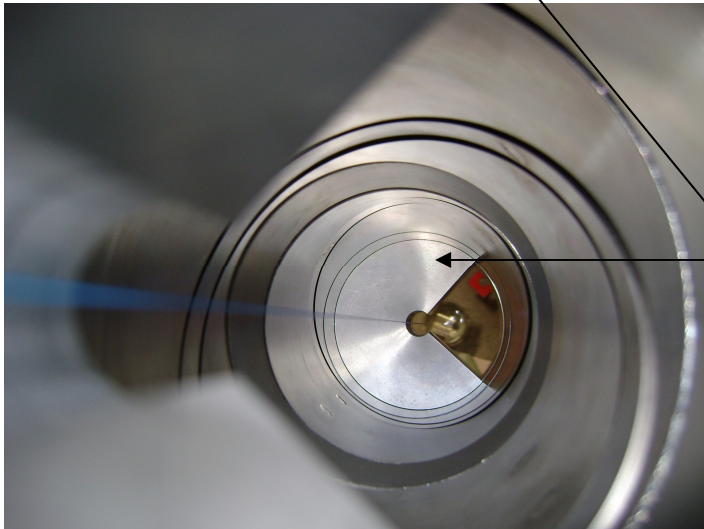
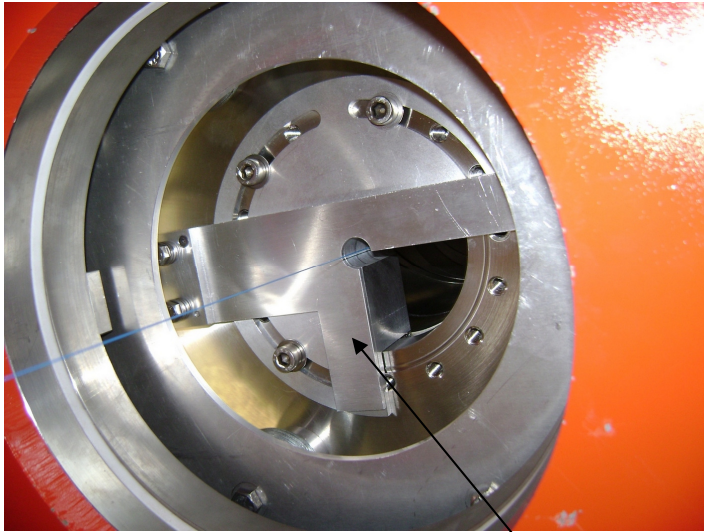
$$x_0 = 0.15 \text{ mm} \pm 0.04 \text{ mm}$$



Stretched Wire Test Stand



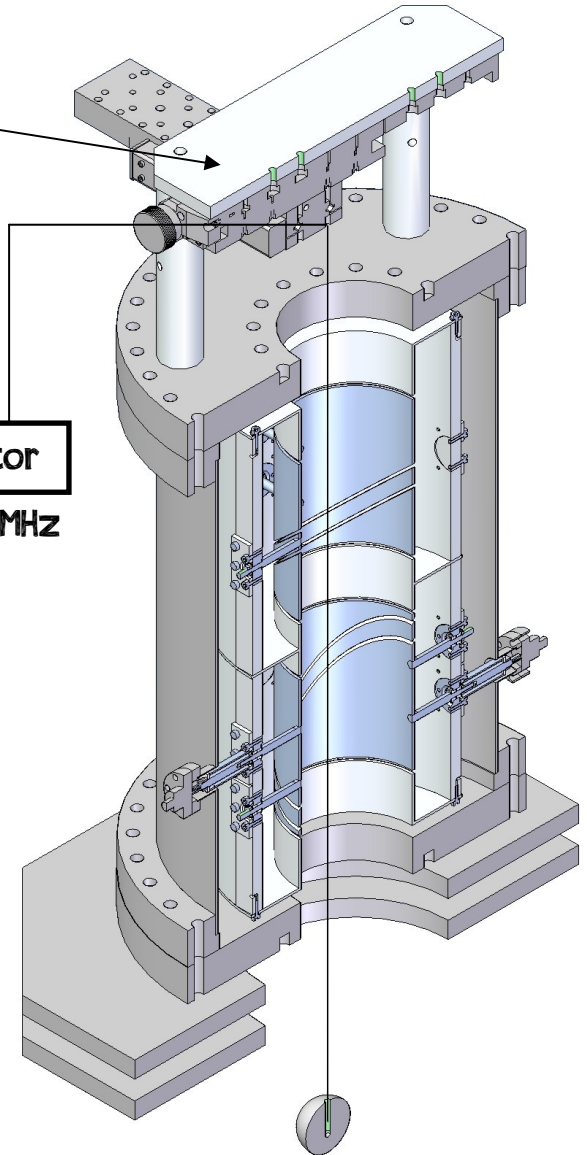
Stretched Wire Test Stand



Translation stages

Signal generator
sine wave 1.78 MHz

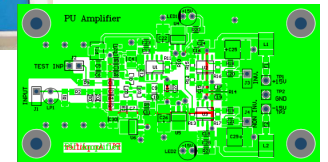
Alignment tools



Stretched Wire Test Stand



PU amps	NF SA-220F5	MSL, A. Paal
Input impedance	1 MΩ 57 pF	5 MΩ 30 pF
Input noise	0.5 nV/√Hz	0.9 nV/√Hz
Voltage gain	46 dB	54 dB



Digitizer	CS1642
Channels	4
Resolution	16 bit
Sampling	200 MS/s
Bandwidth	125 MHz
Memory	128 MB



Measurements vs. Simulations

With the ring:

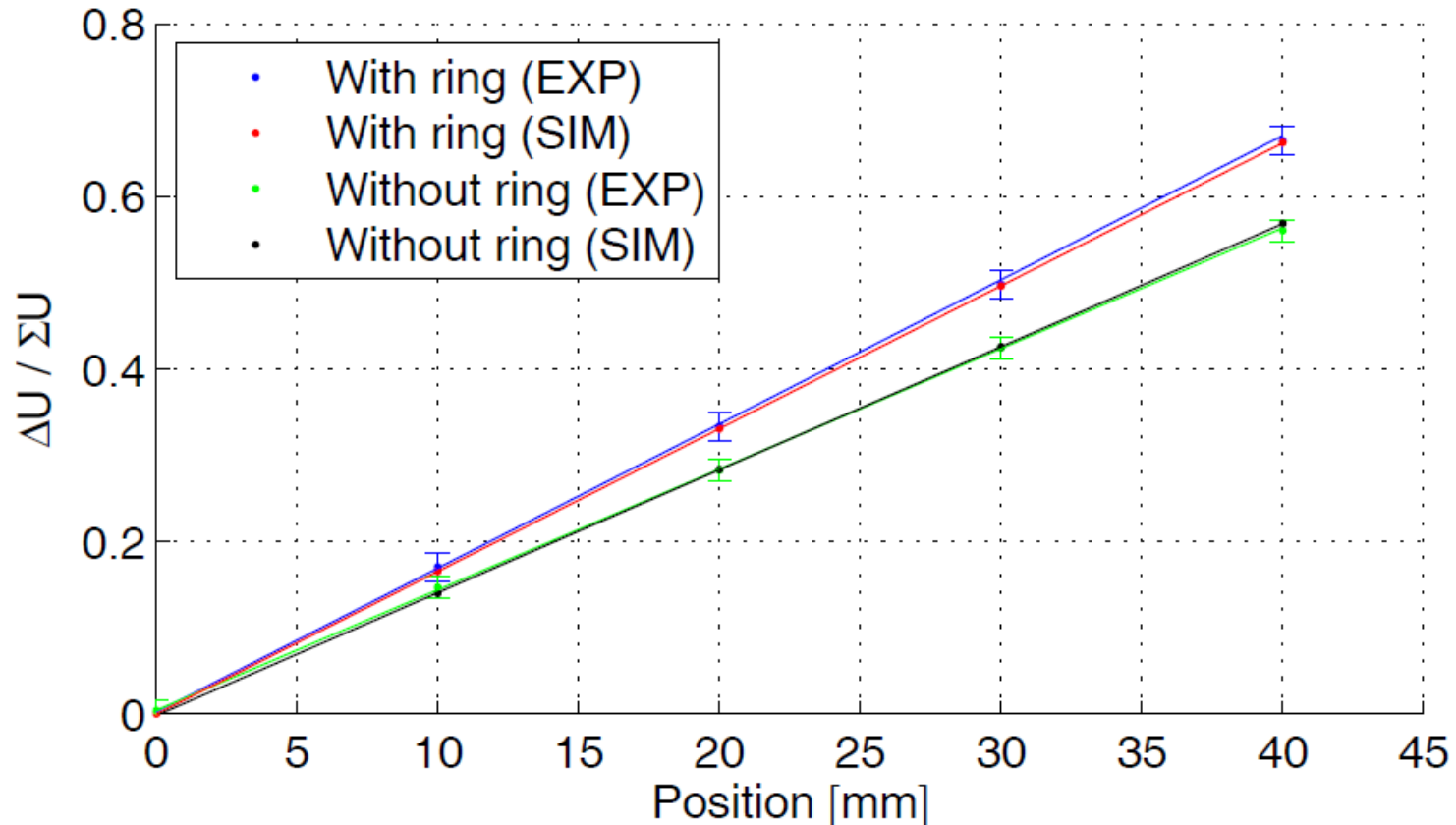
$$k = 59.8 \text{ mm} \pm 0.1 \text{ mm}$$

$$x_0 = -0.1 \text{ mm} \pm 0.1 \text{ mm}$$

Without the ring:

$$k = 71.5 \text{ mm} \pm 0.1 \text{ mm}$$

$$x_0 = -0.3 \text{ mm} \pm 0.2 \text{ mm}$$



Separating Ring

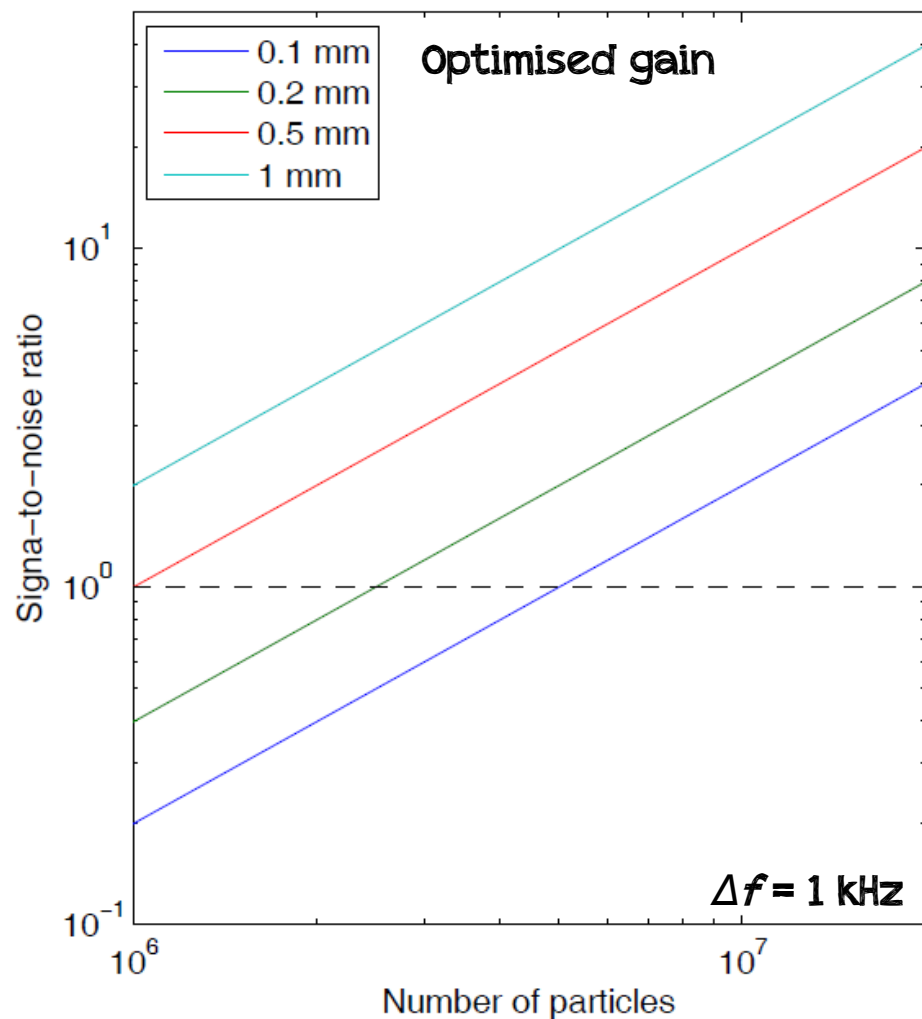
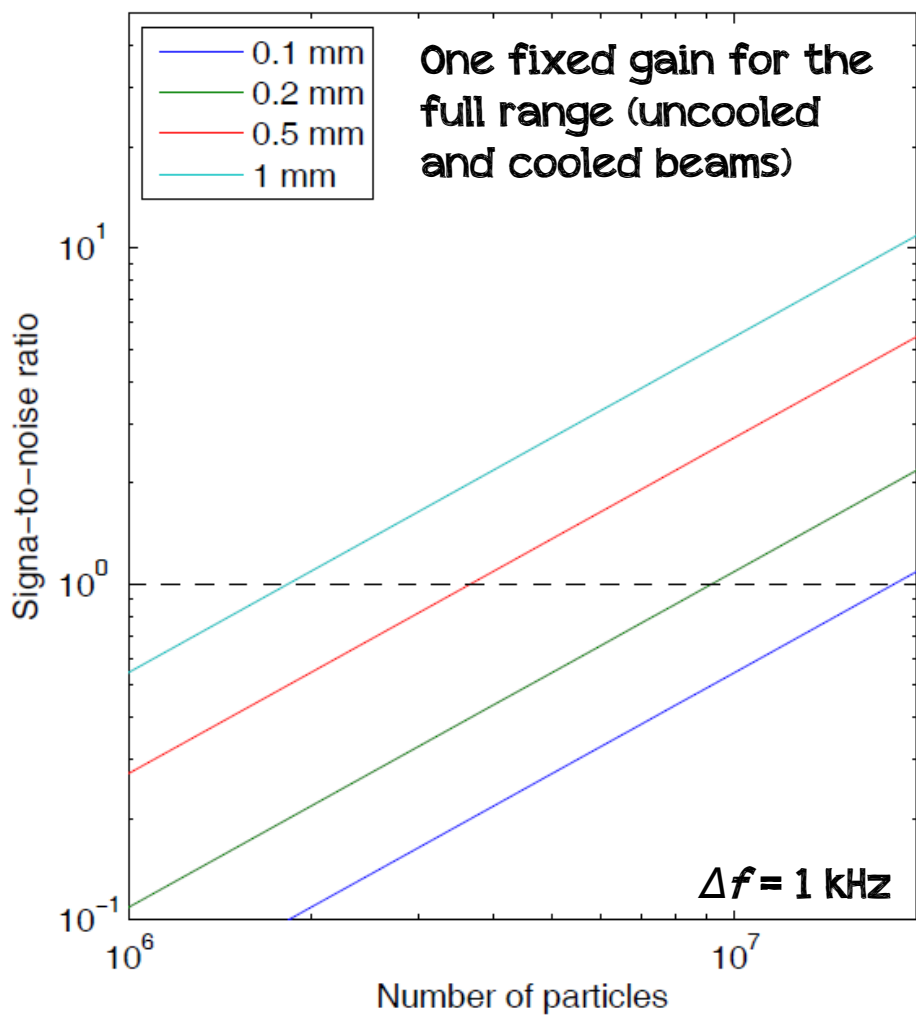
Improvement in sensitivity..

$$k \Rightarrow \sim 115\% k$$

..but at the cost of the signal strength

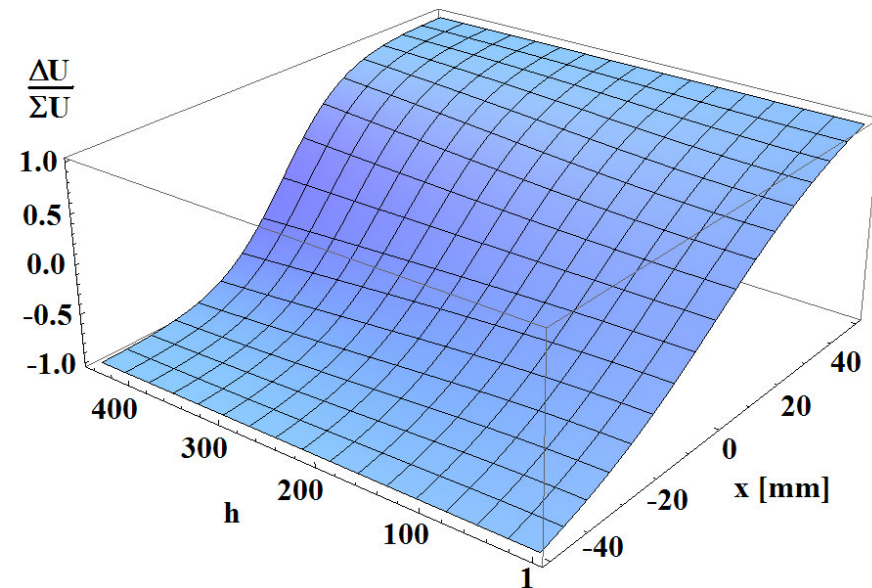
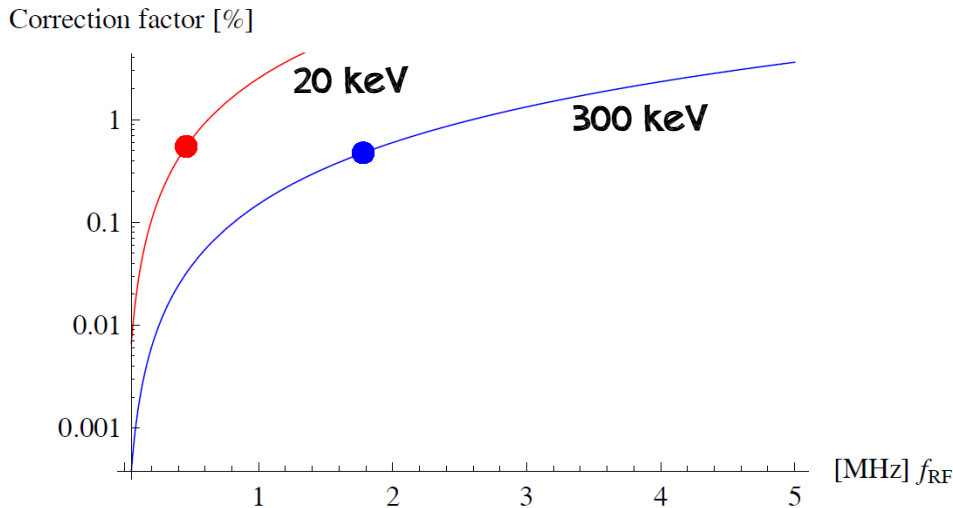
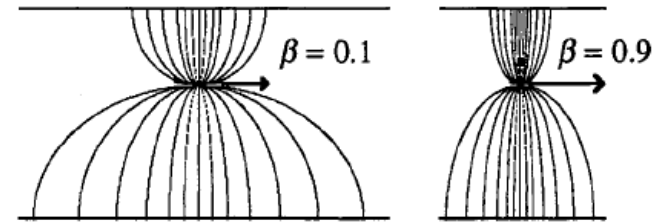
$$U \Rightarrow \sim 80\% U$$

Position Resolution



Low β Beams

- Theoretical calculations: difference below 0.5%-1% for low frequencies (RF harmonic numbers)
- Preliminary CST simulations: difference not bigger than a few percent (mesh size?), further studies needed

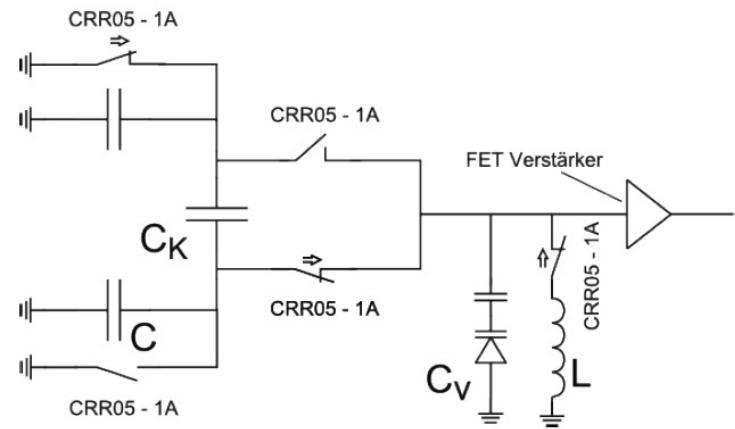
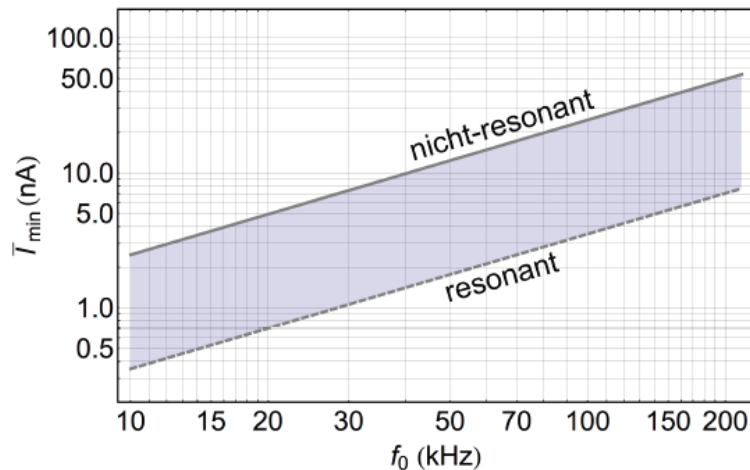


Prototype Status

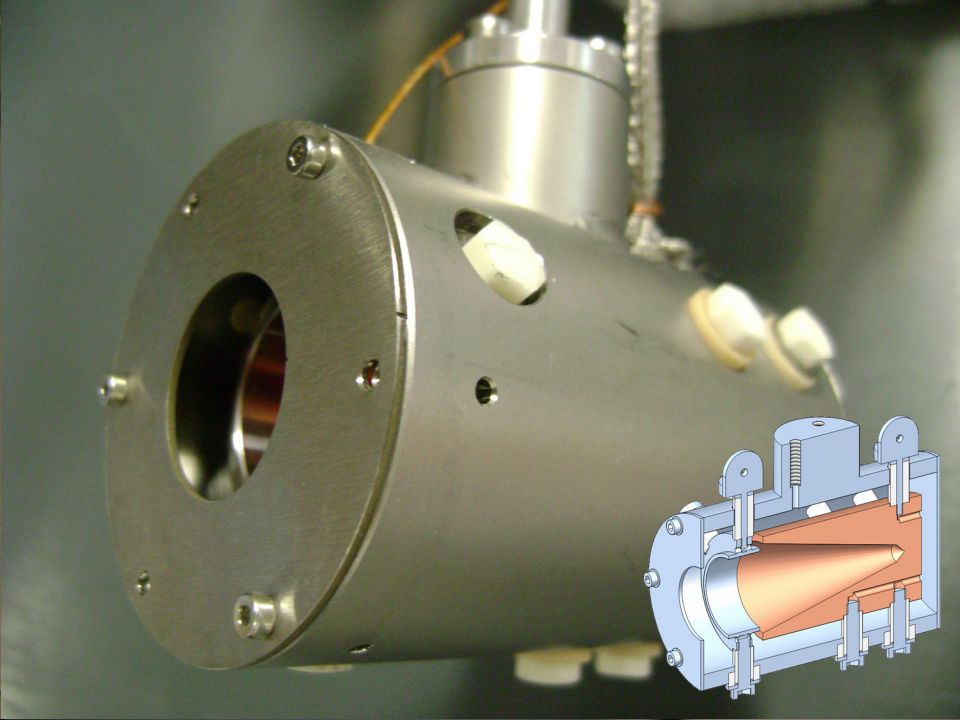
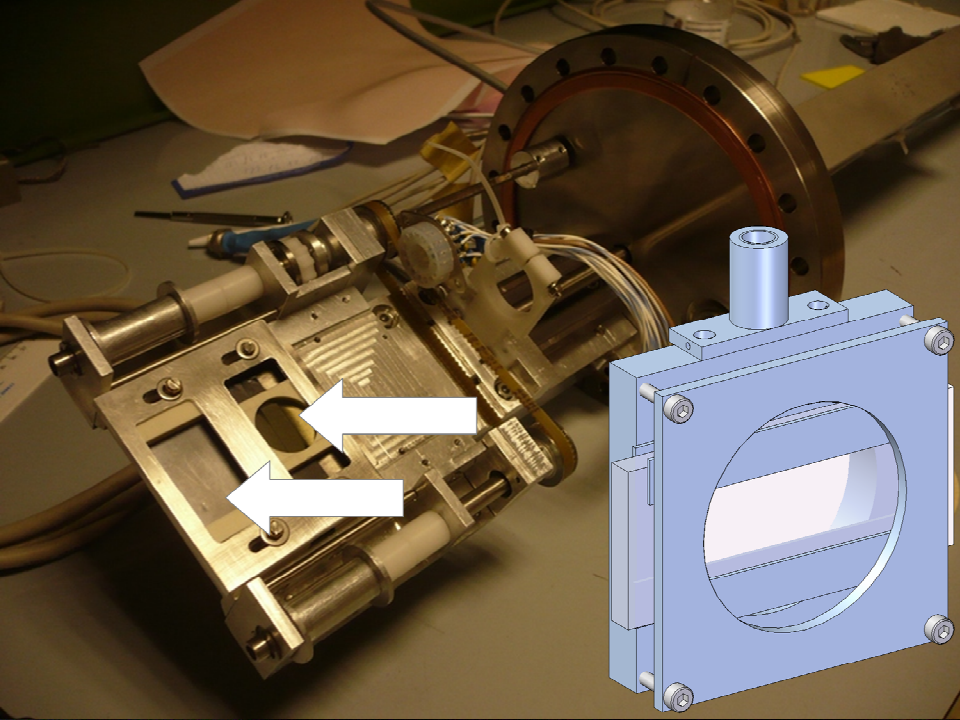
- Diagonal cut => linear response
- Sensitivity: ~ 0.1 mm (depending on the bandwidth and gain), **closed orbit** measurements only (<1 kHz)
- Mechanical accuracy: < 0.5 mm
- Tested only with a stretched wire and simulated for $\beta = 1$

Perspectives

- Systematic simulations for $\beta \ll 1$
- Sensitivity can be improved with a **resonant circuit** (one order of magnitude)



- Beam **current** measurements, etc.



Thank you for attention

