

# Numerical Methods for Beam Position Evaluation at GSI

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# Outline

- Introduction
- Position Measurement System at GSI
- Position Evaluation Methods
  - Bunch Detection
  - Bunch Signal Processing
- Summary

# GSI SIS-18 Synchrotron

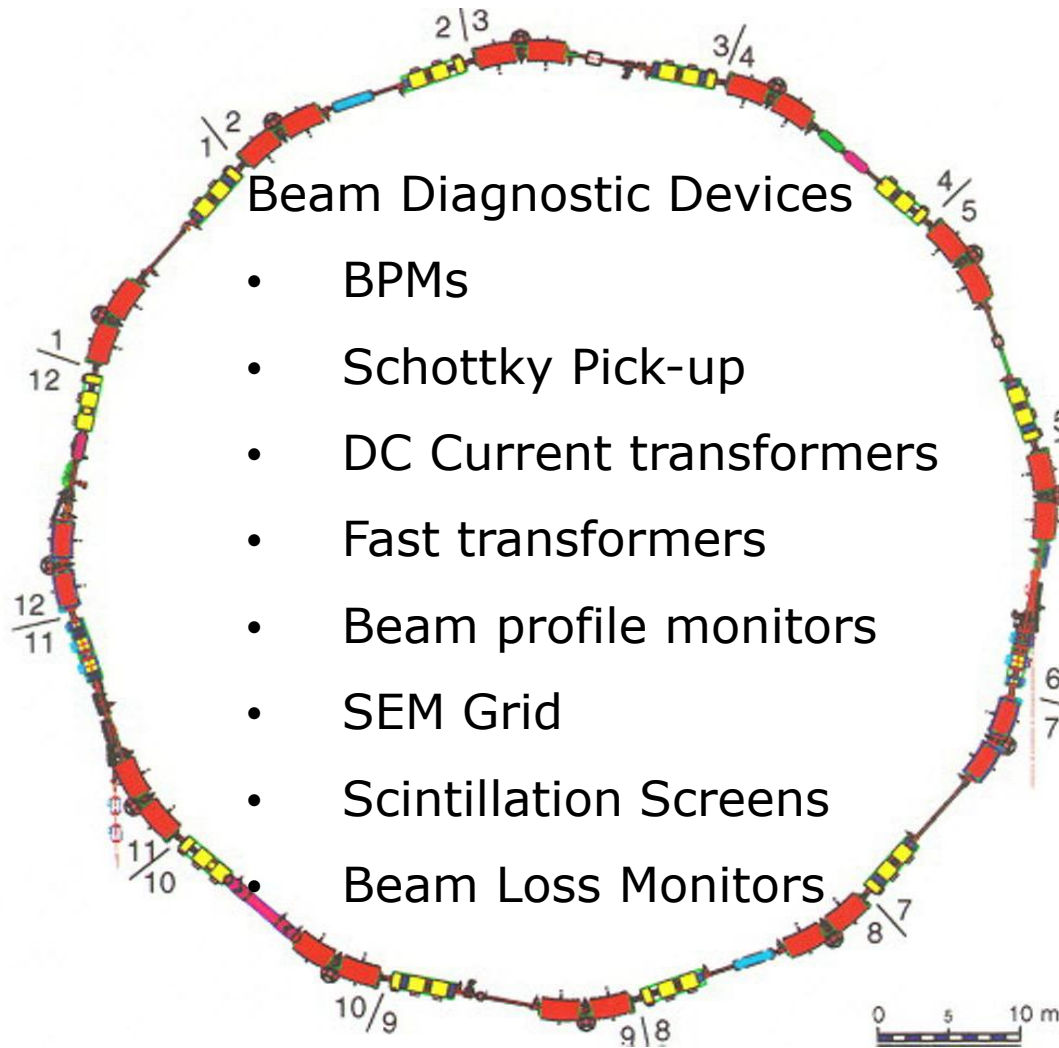


## Important parameters of SIS-18

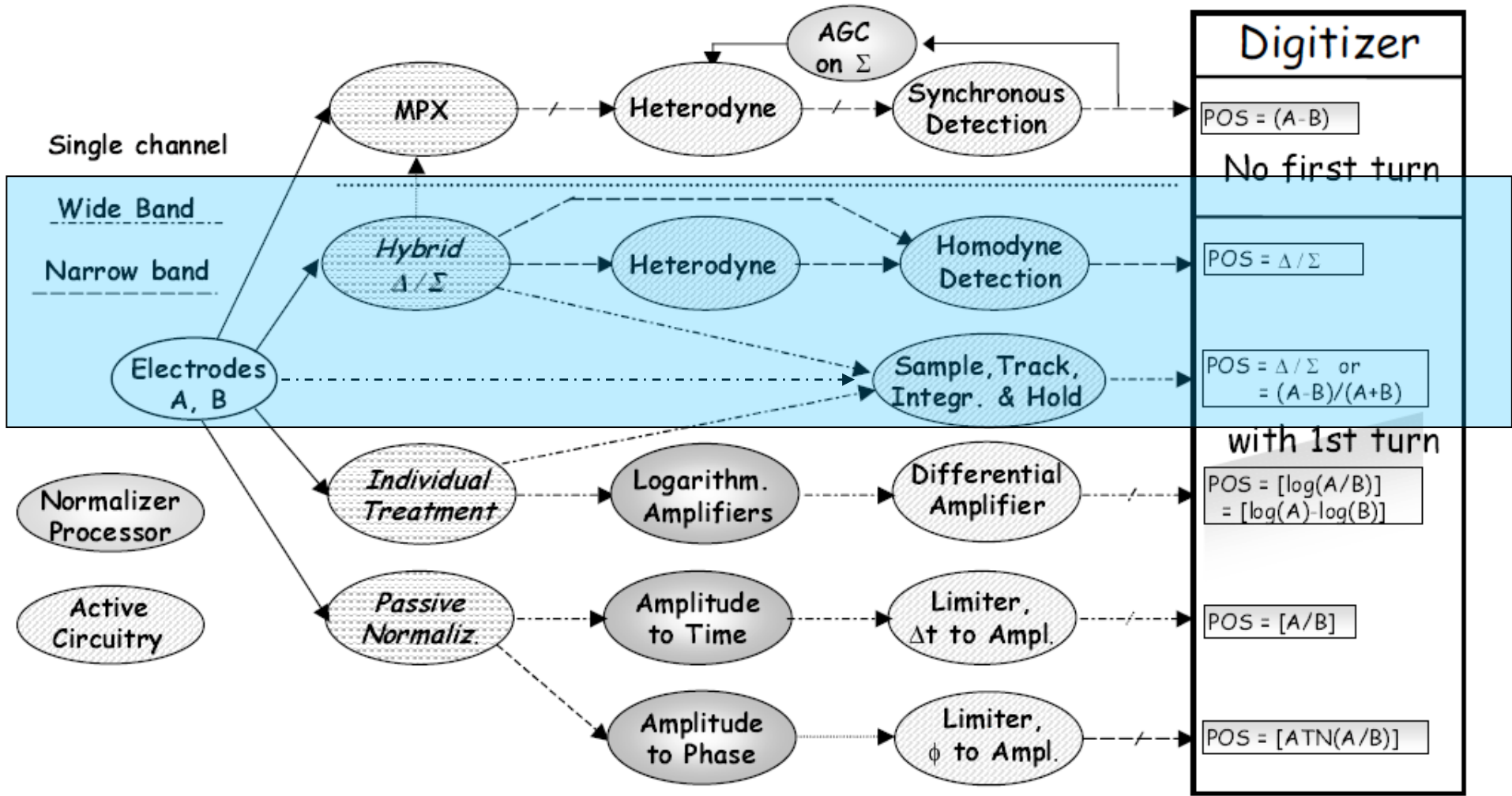
Circumference	216 m
Inj. type	Multiturn
Energy range	11 MeV → 2 GeV
Acc.RF	0.8 → 5 MHz
Harmonic number	4 (no. of bunches)
Bunching factor	0.6 → 0.2
Ramp duration	0.06 → 1.5 s
Ion range (Z)	1 → 92 (p to U)

### Beam Diagnostic Devices

- BPMs
- Schottky Pick-up
- DC Current transformers
- Fast transformers
- Beam profile monitors
- SEM Grid
- Scintillation Screens
- Beam Loss Monitors



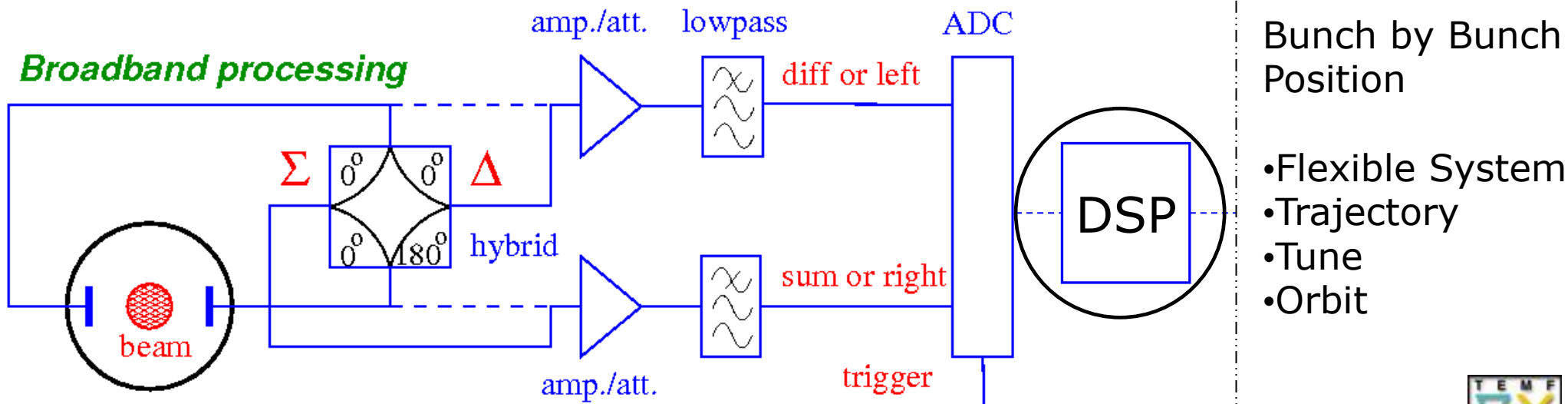
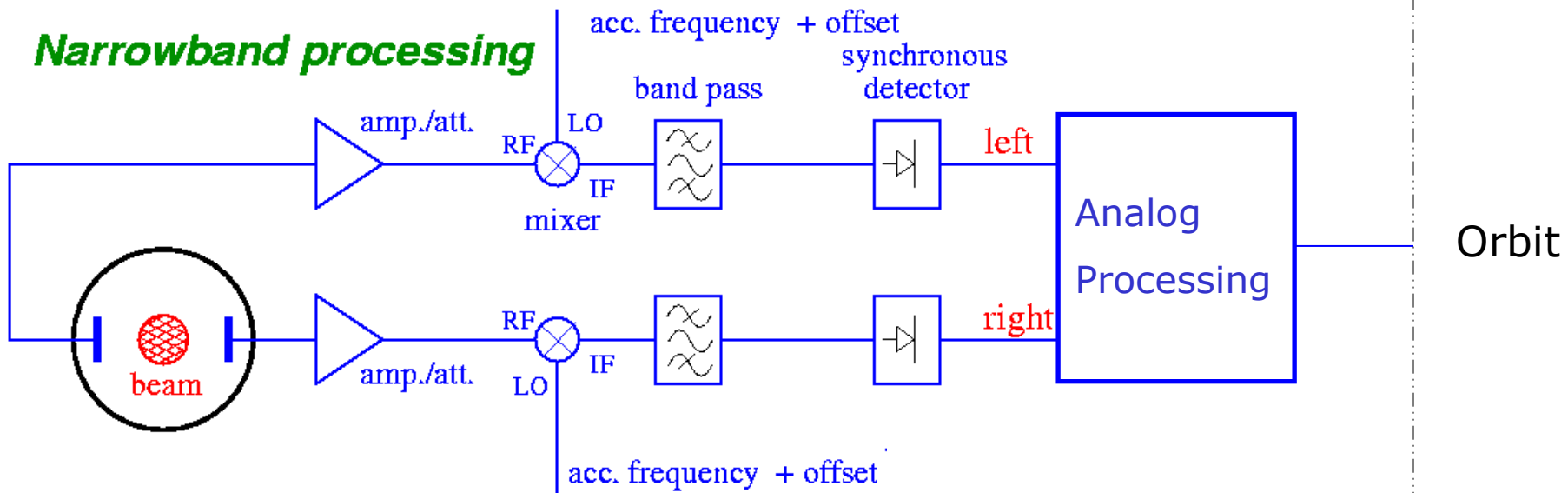
# Position Measurement Methods



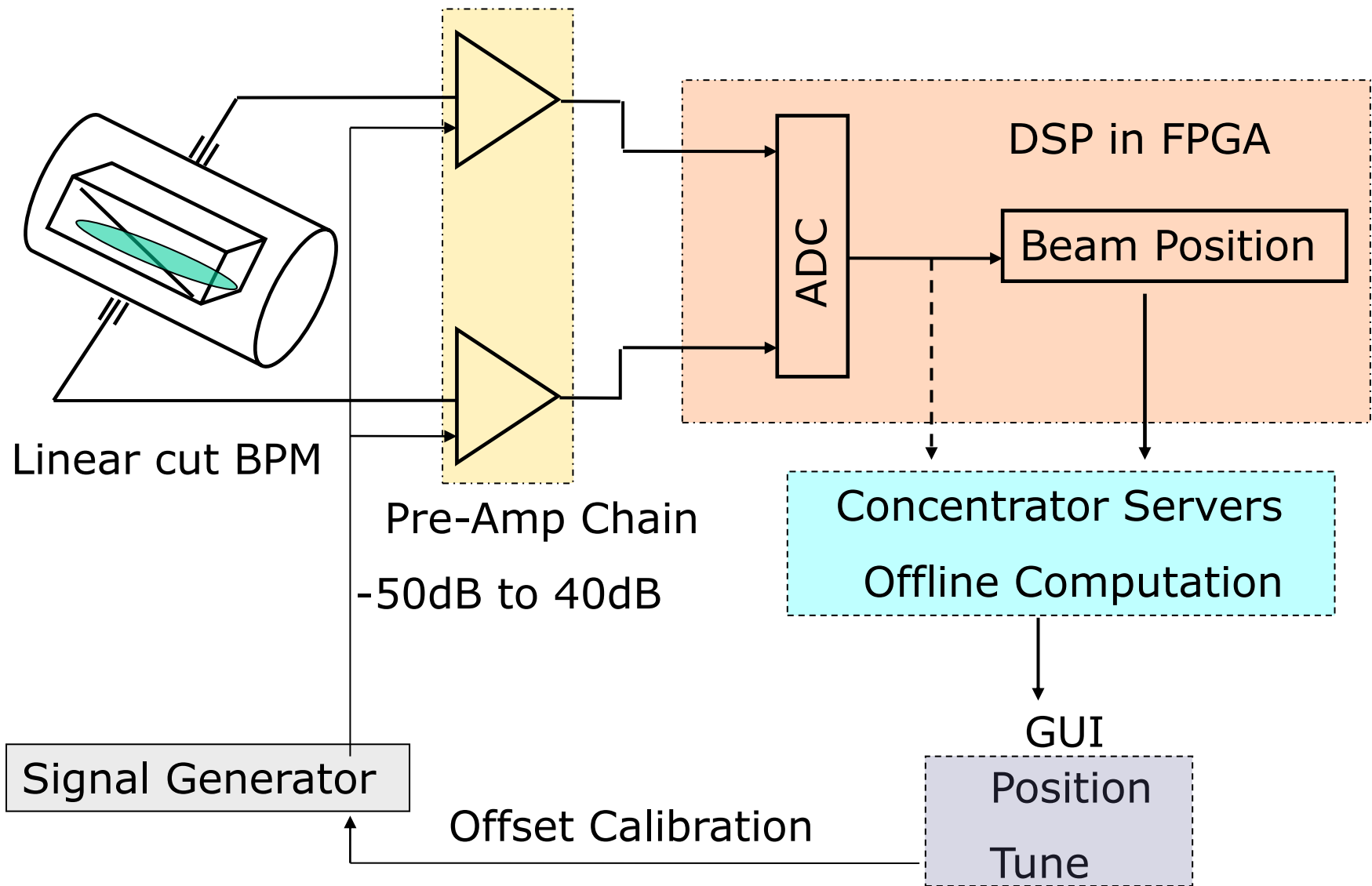
G. Vismara : DSM for BPM, BIW 2000



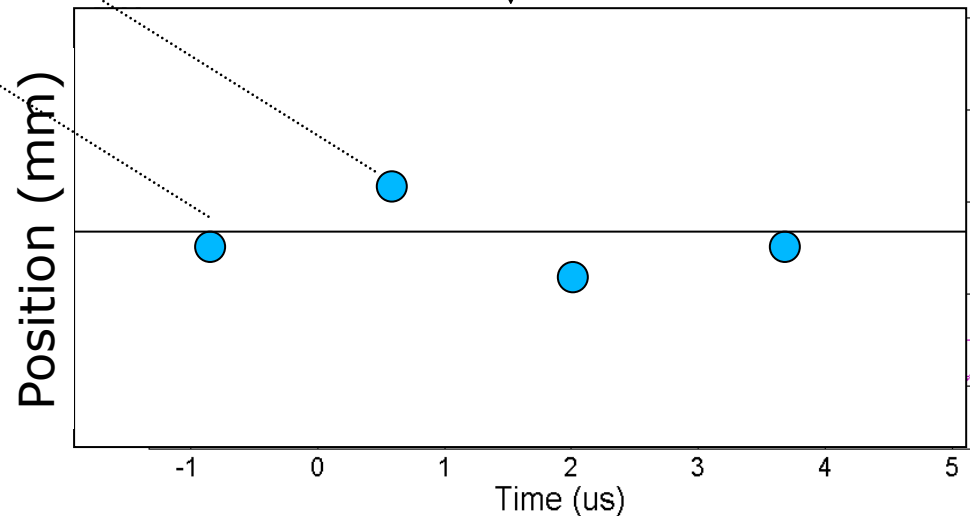
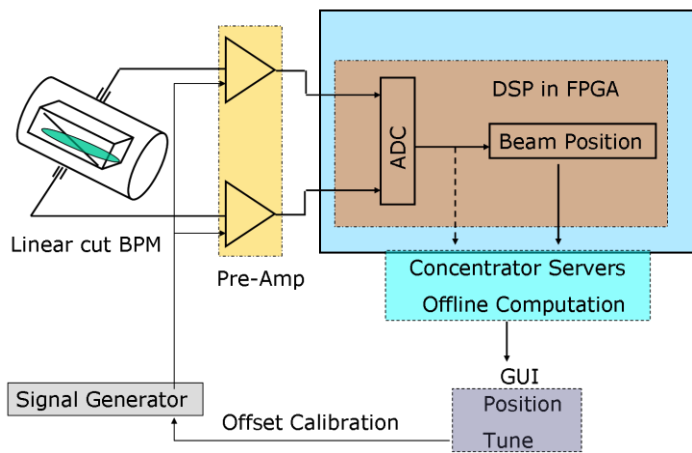
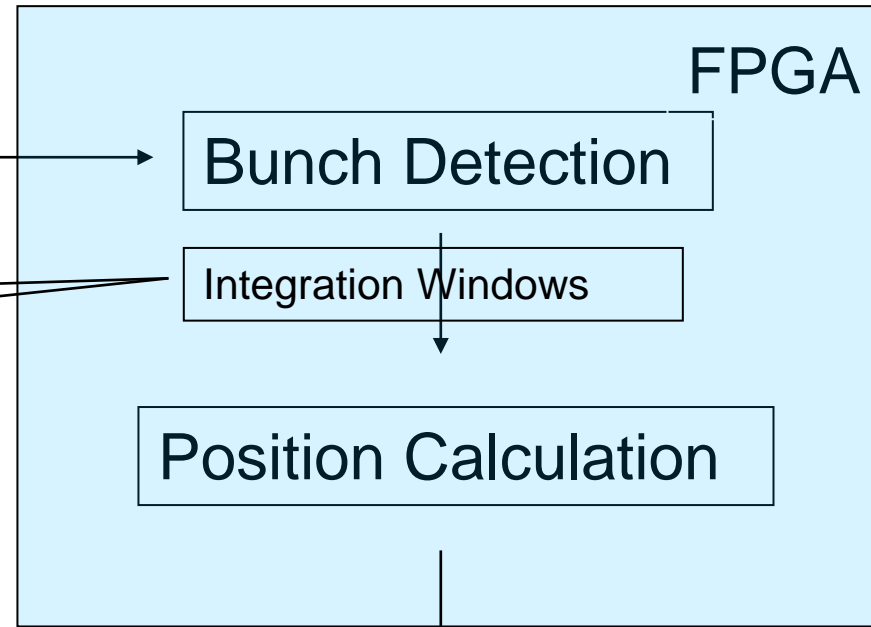
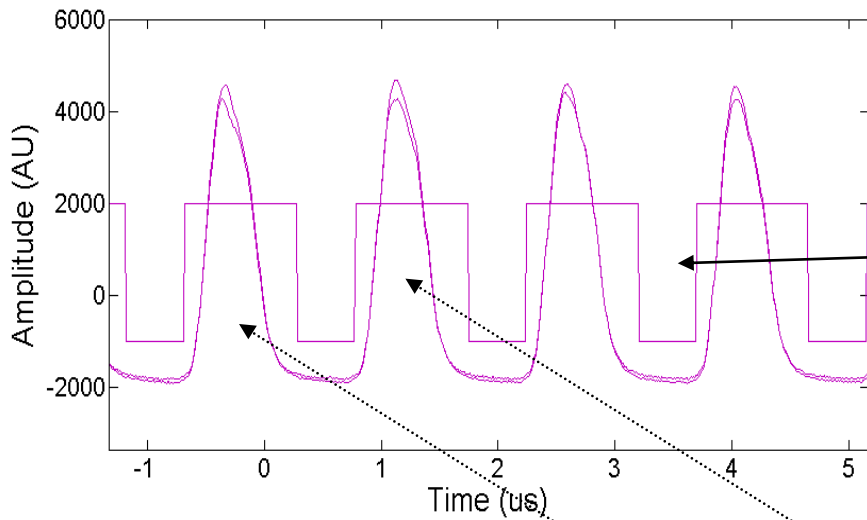
# Position Measurement Principle at GSI



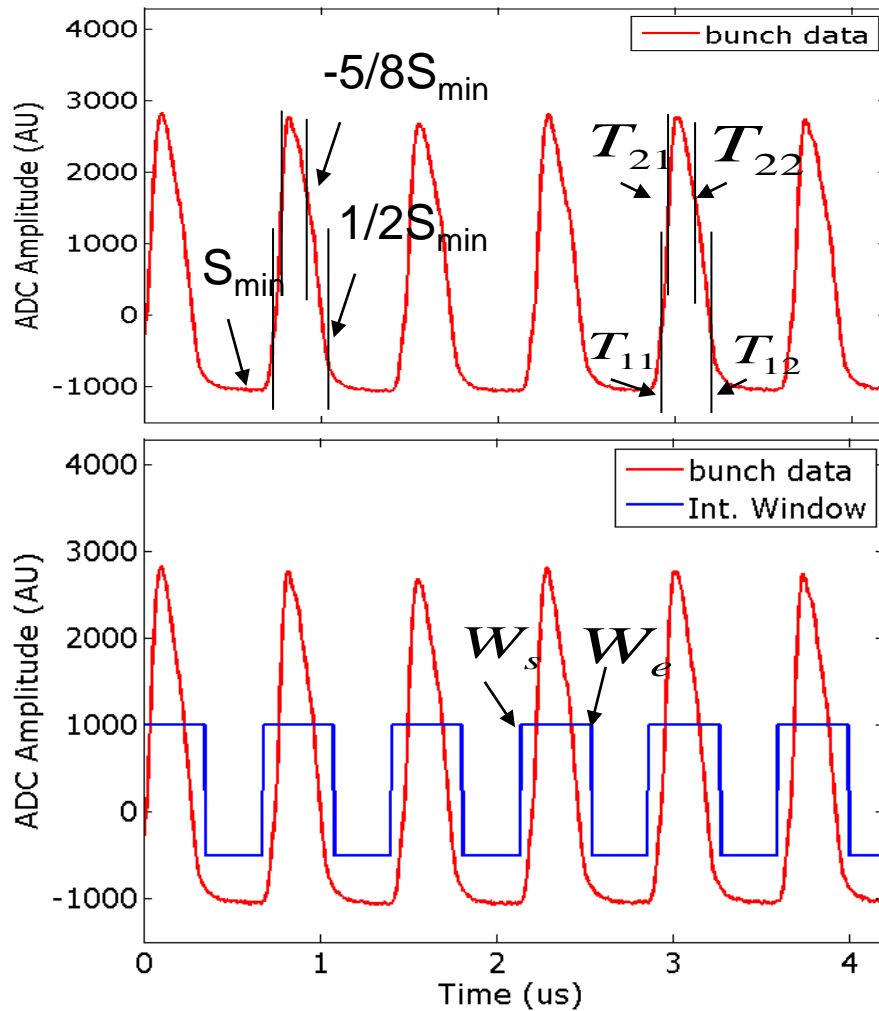
# Digital Position Measurement System (TOPOS)



# Position Calculation in FPGA



# Bunch Detection- Double Threshold Algorithm



- 1) A minimum is found between two adjacent bunches.
- 2) Using the minimum level  $S_{min}$  two thresholds are calculated at  $T_{1(1,2)} = \frac{1}{2} S_{min}$  and  $T_{2(1,2)} = -\frac{5}{8} S_{min}$
- 3) When the bunch signal passes through all these thresholds, it is detected.
- 4) Time window for the bunch is calculated which is passed to position evaluation part of the algorithm.

$$W_{sn} = T_{11} - (T_{21} - T_{11})$$

$$W_{en} = T_{12} + (T_{12} - T_{22})$$



# Bunch Signal Processing Algorithms

## Characteristics :

- Fast :  $< 1\mu\text{s}$
- Robust : Varying bunch lengths(500  $\rightarrow$  100 ns), mismatch
- Minimize variance
- Unbiased : Should not add any offset

## Methods :

- Baseline restoration and  $\frac{\Delta}{\Sigma}$
- Linear regression fit

# Bunch Signal Processing Algorithms

## Characteristics :

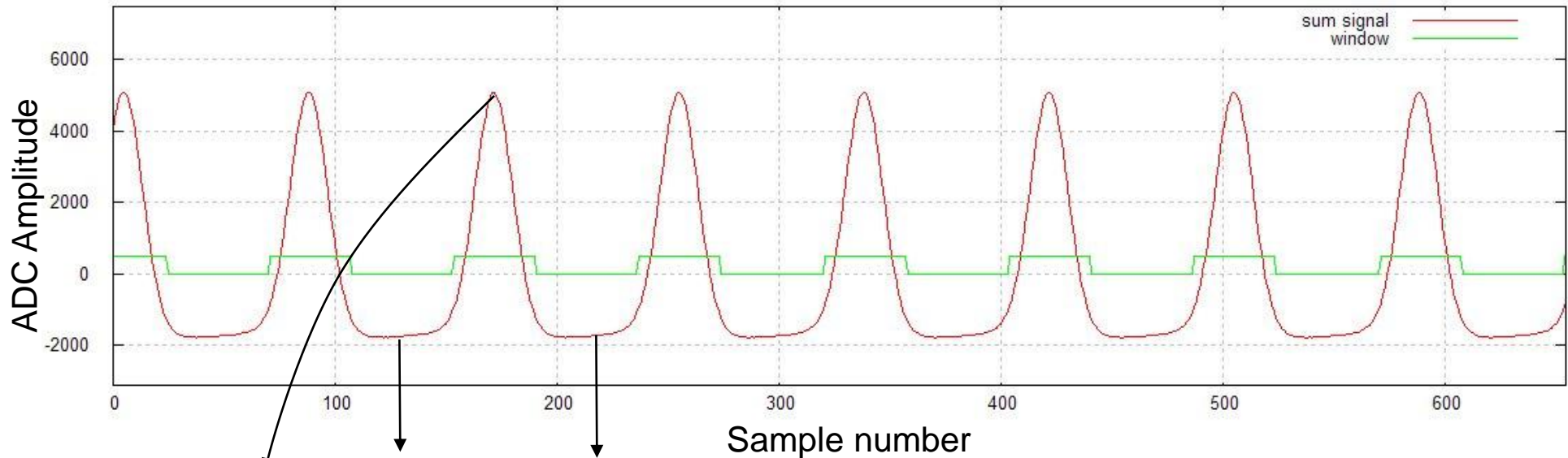
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## Methods :

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# Baseline Restoration

Generated Gaussian Signal (1.5MHz period)



$$R_{S_{ni}} = R_{ni} - \frac{(R_{ni-N/2} + R_{ni+N/2})}{2}$$

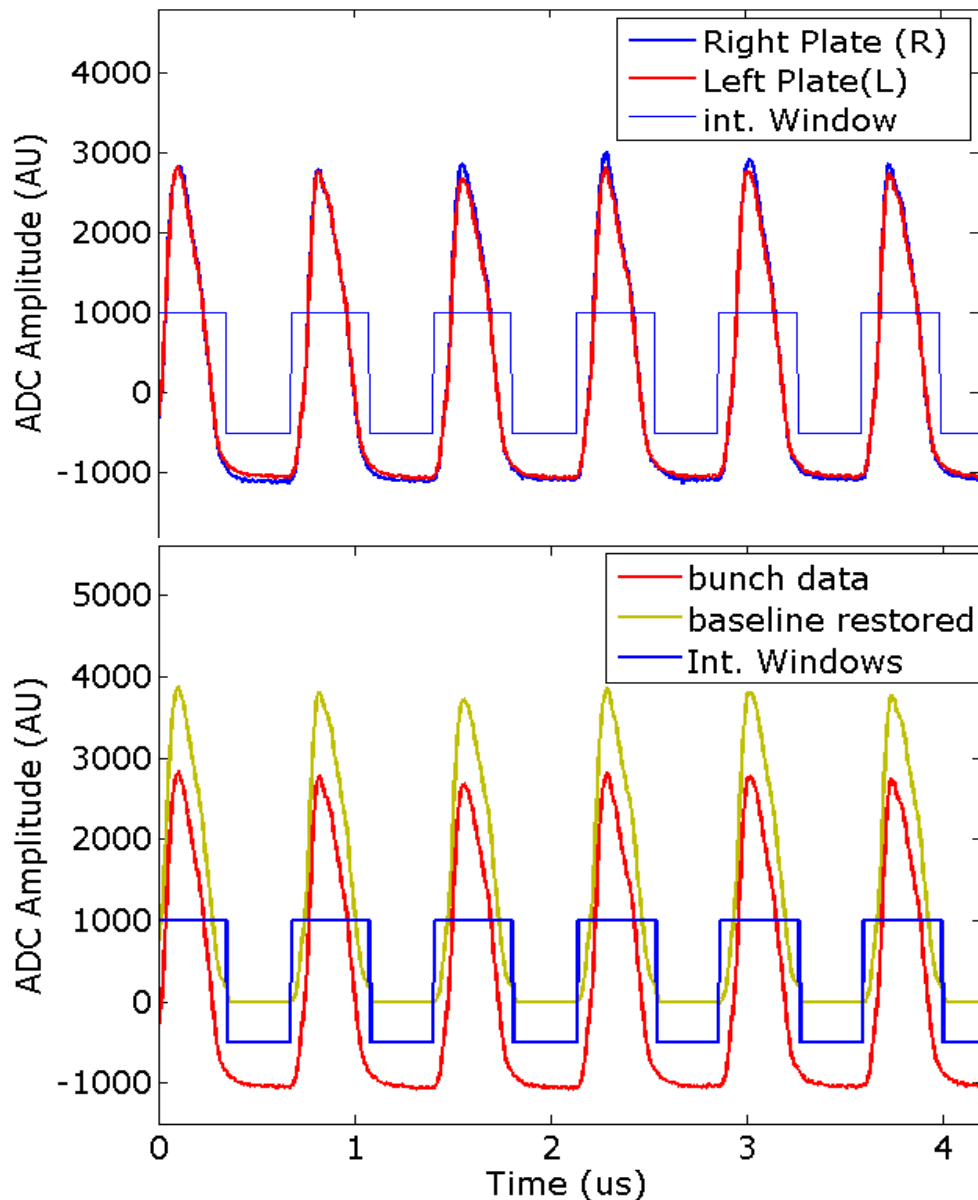
Max. period of T: 1.25μs (0.8KHz)

=> T/2 = 625ns = 79 samples

**Baseline is calculated for each sample inside the integration window**

\* A. Galatis et al. DIPAC 2007

# Baseline Restoration Algorithm



Let  $R_{ni}$  and  $L_{ni}$  be the signal of the  $n$ th bunch of both plates in the integration window of length  $N$  generated by bunch detection algorithm

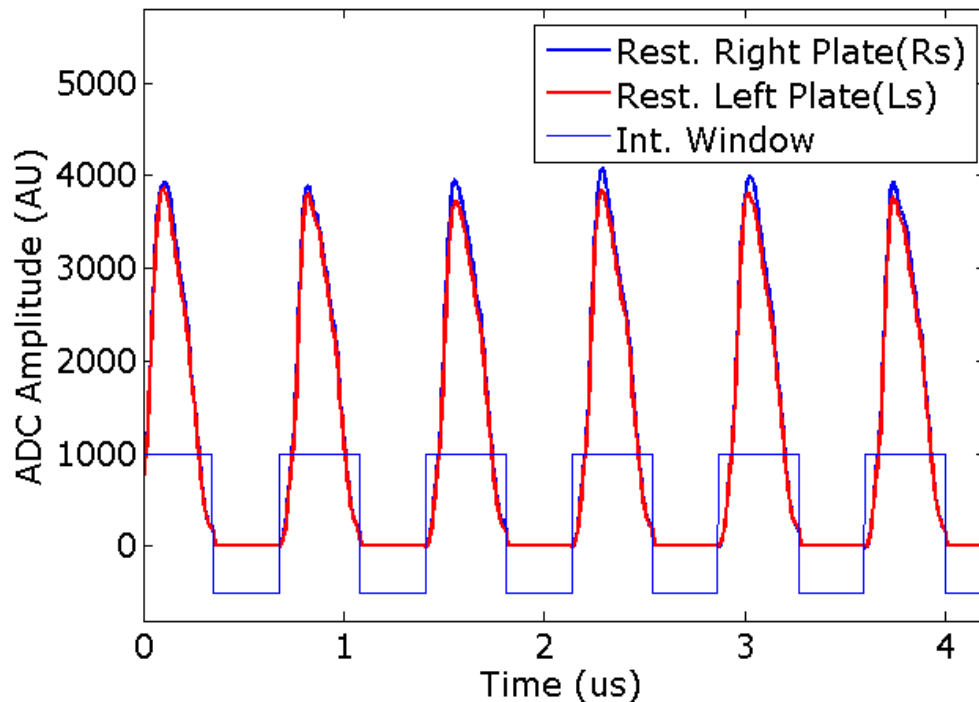
The steps in the algorithm for bunch  $n$  is :

1) The baseline for both the electrode signals is calculated and is given by  $br_{ni}$  and  $bl_{ni}$  respectively.

2) Add these baseline values to the original signal

$$Rs_{ni} = R_{ni} + br_{ni}; \quad Ls_{ni} = L_{ni} + bl_{ni};$$

# Baseline Restoration Algorithm

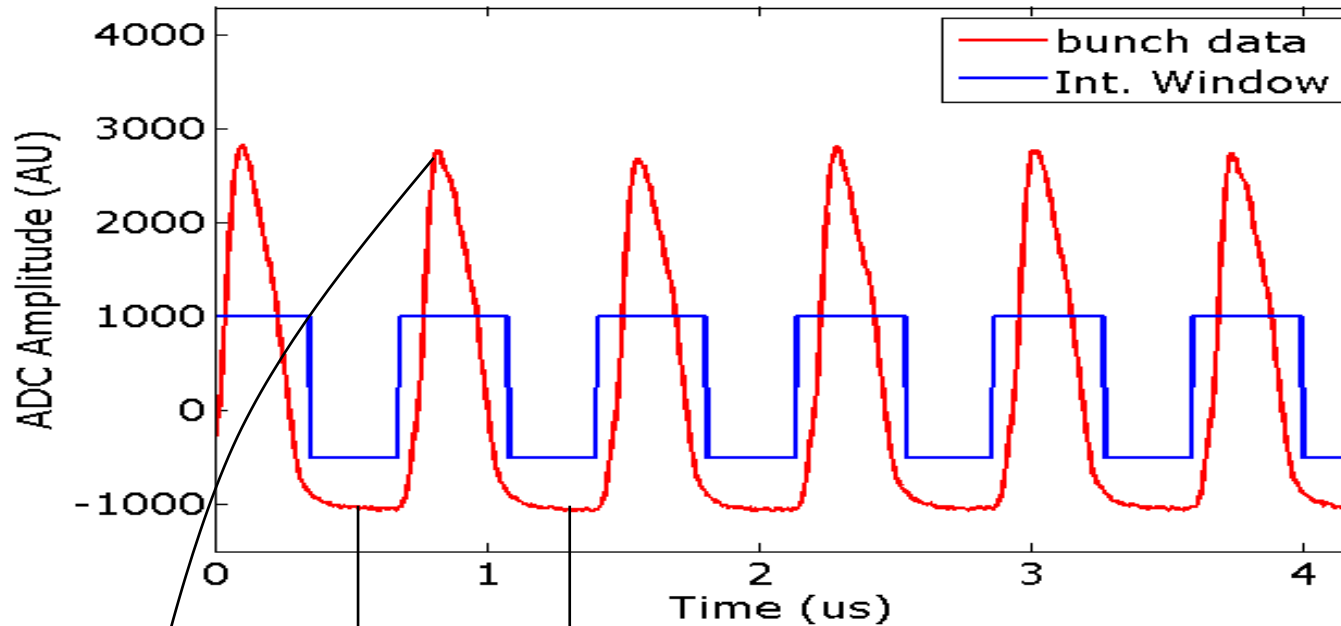


3) Integration of both plate signals and difference over sum

$$p_n \propto \frac{\sum_{i=W_{sn}}^{W_{en}} Rs_{ni} - Ls_{ni}}{\sum_{i=W_{sn}}^{W_{en}} Rs_{ni} + Ls_{ni}}$$



# Baseline Restoration



$$R_{S_{ni}} = R_{ni} - \frac{(R_{ni-N/2} + R_{ni+N/2})}{2}$$

**Problems!!**

- 1) Issues with larger bunches at injection
- 2) Adds noise to the signal
- 3) High latency i.e takes 2/3 of total calculation time

# Bunch Signal Processing Algorithms

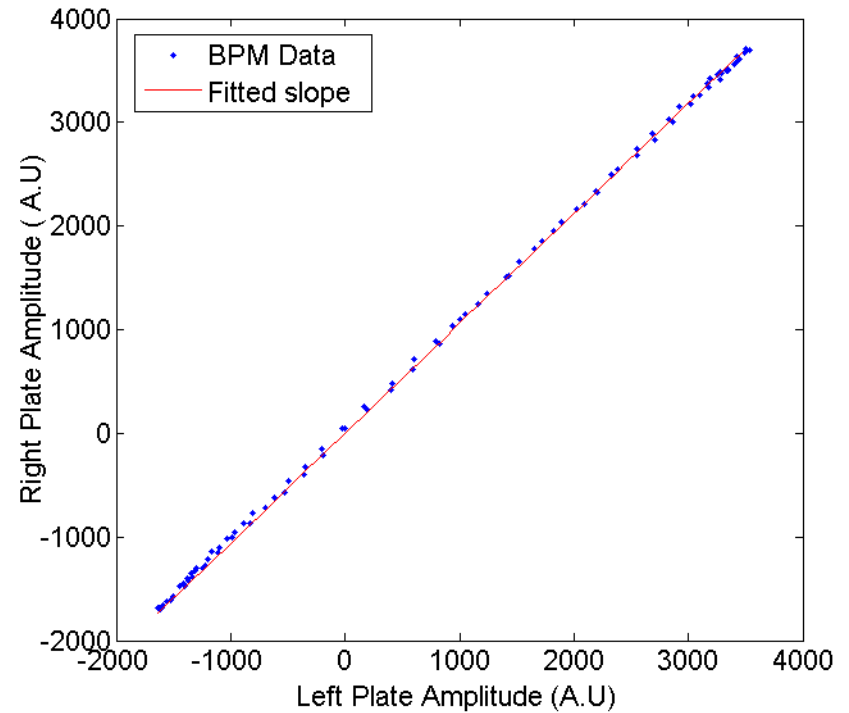
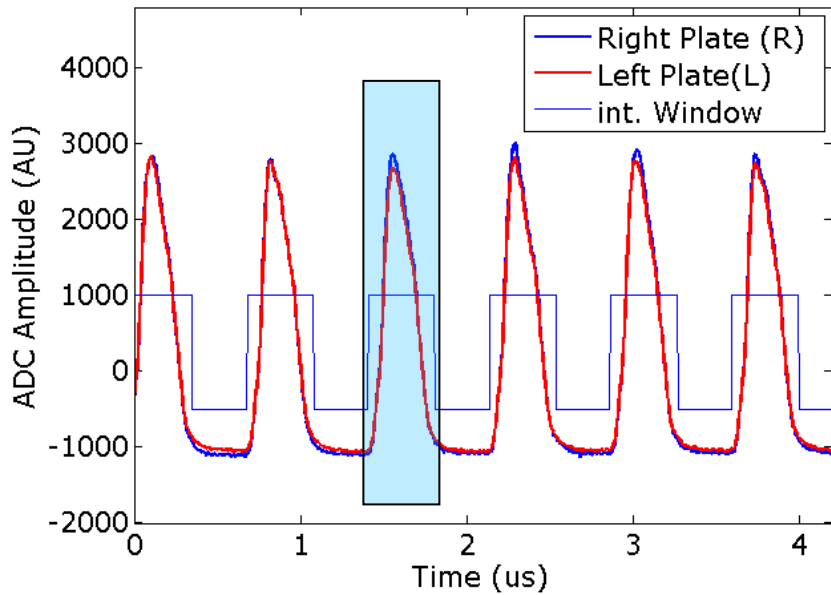
## Characteristics :

- Fast :  $< 1\mu\text{s}$
- Robust : Varying bunch lengths from 100 to 500 ns
- Minimize variance
- Unbiased : Does not add any offset

## Methods :

- Baseline restoration and  $\frac{\Delta}{\Sigma}$
- Linear regression fit

# Linear Regression



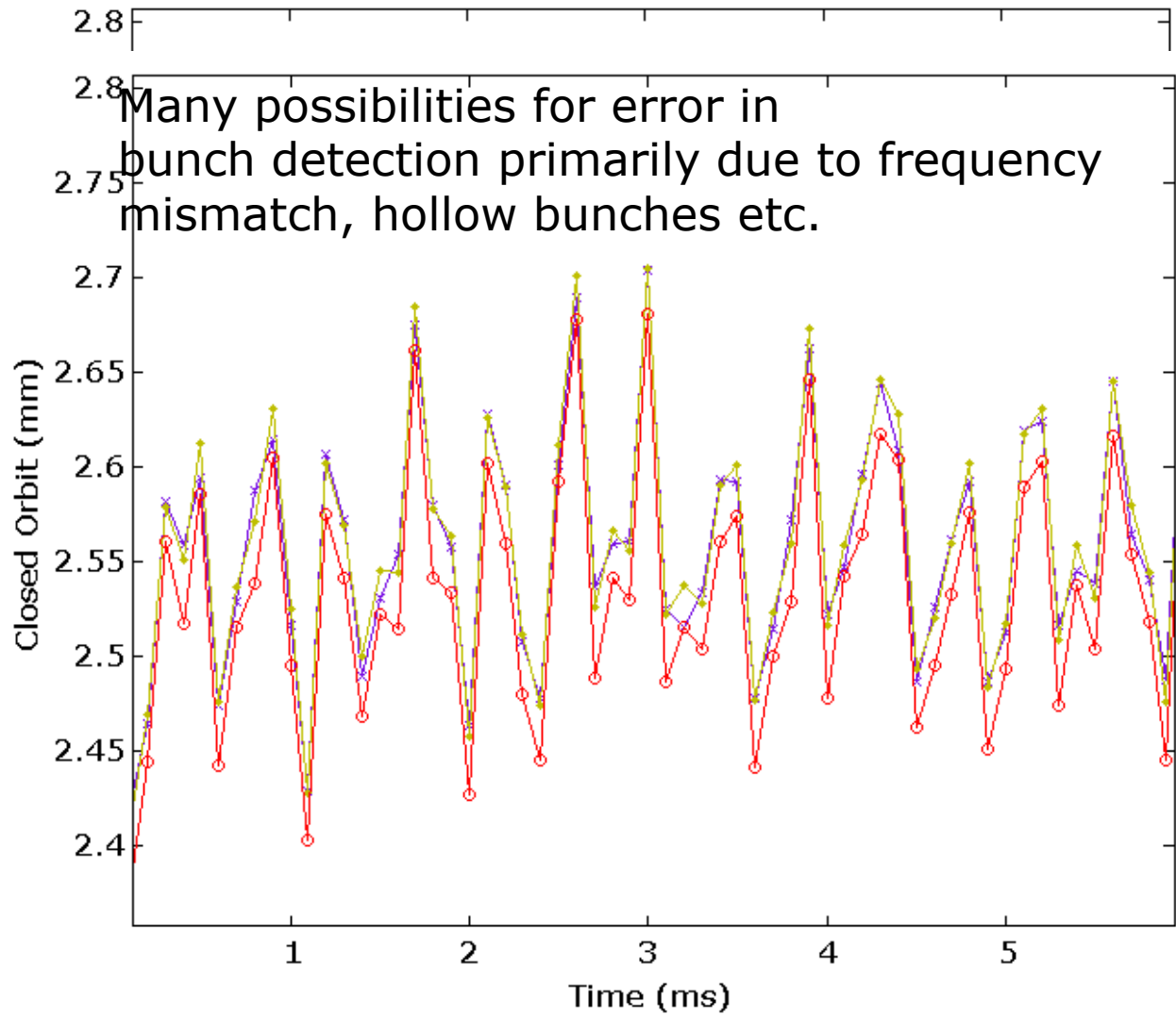
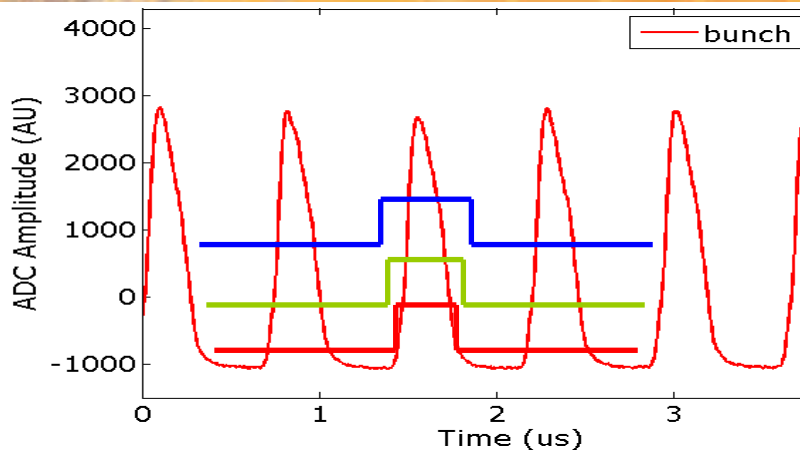
$$p_n \approx \propto \frac{1 - s_n}{1 + s_n}$$



$$s_n = \frac{\sum_{i=W_{sn}}^{W_{en}} R_{ni} L_{ni}}{\sum_{i=W_{sn}}^{W_{en}} R_{ni}^2}$$

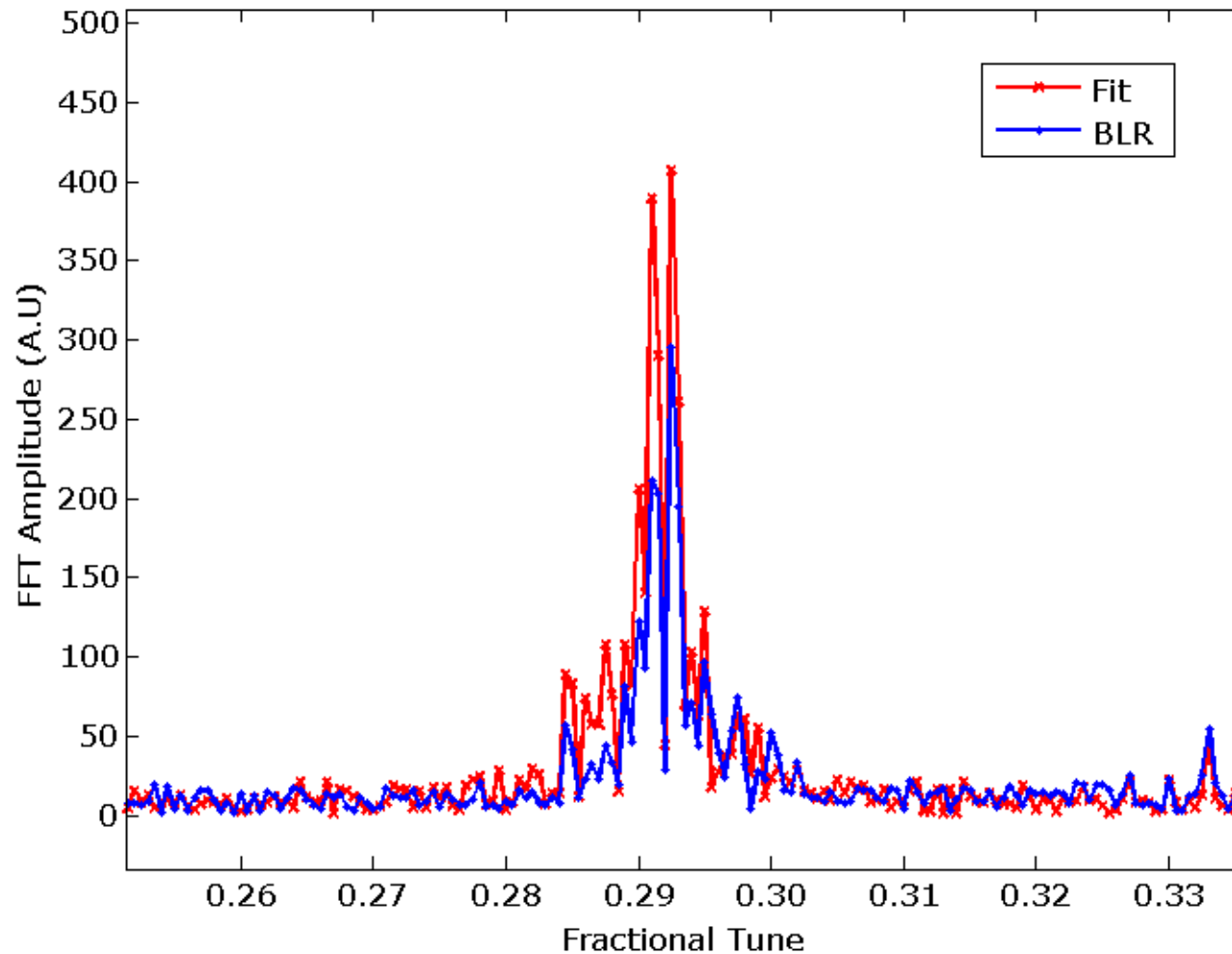
Assumption:  $\Delta \ll \Sigma$

# Robust to bunch detection errors



Linear Regression

# Variance



- Better Signal to noise ratio in the tune spectra for regression fit over BLR

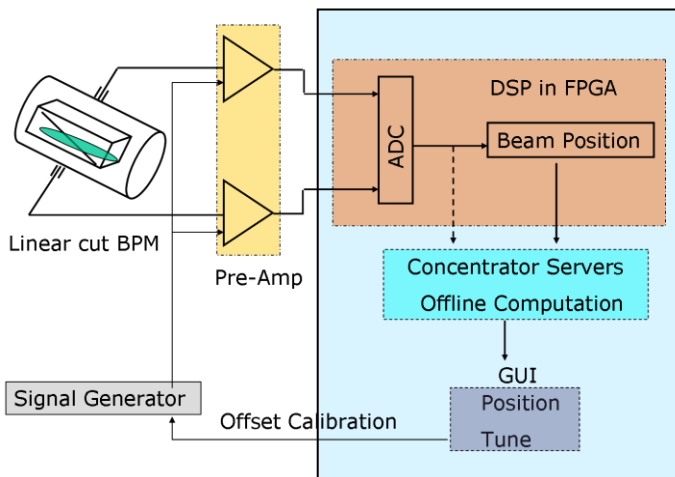
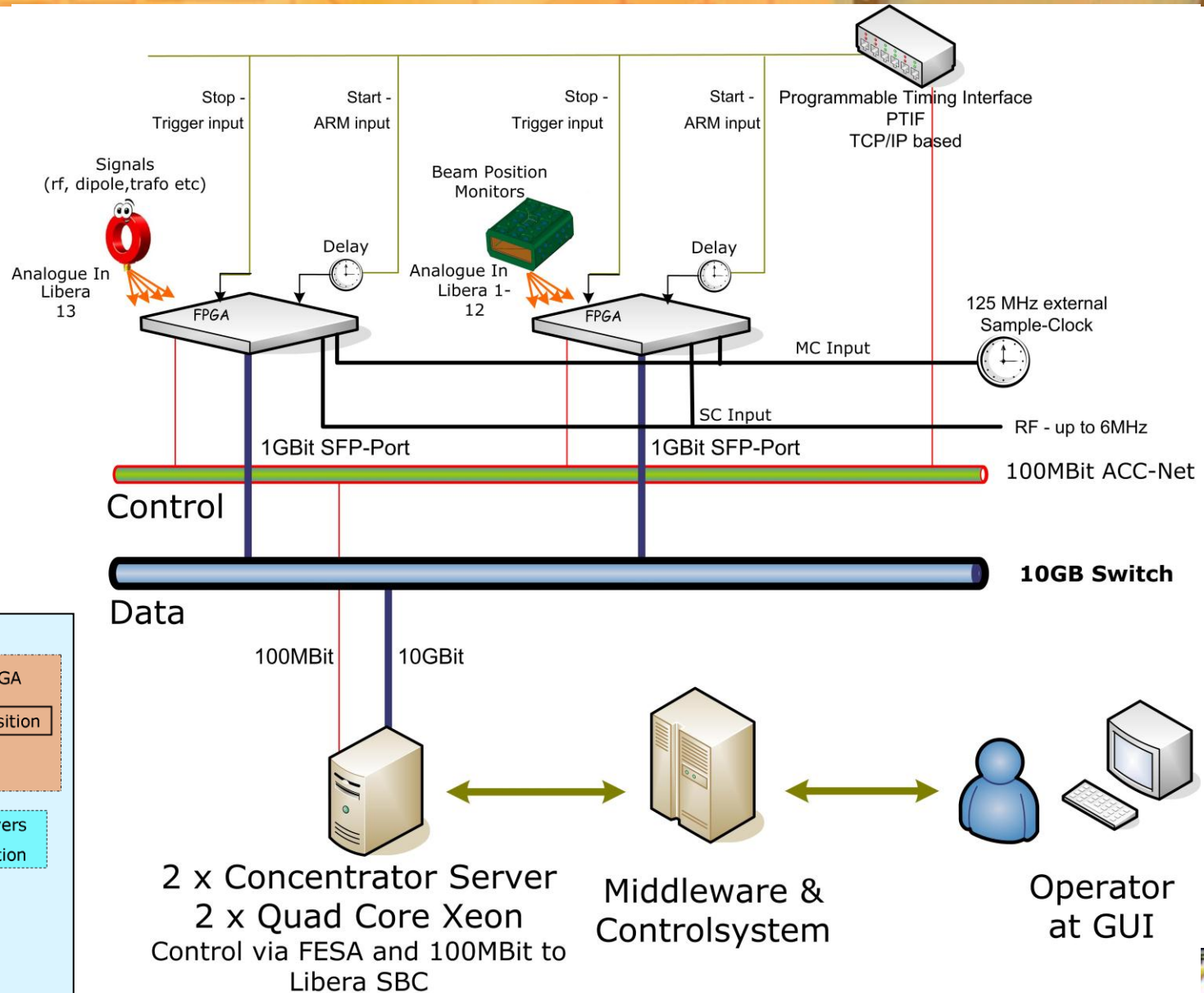


# Comparison

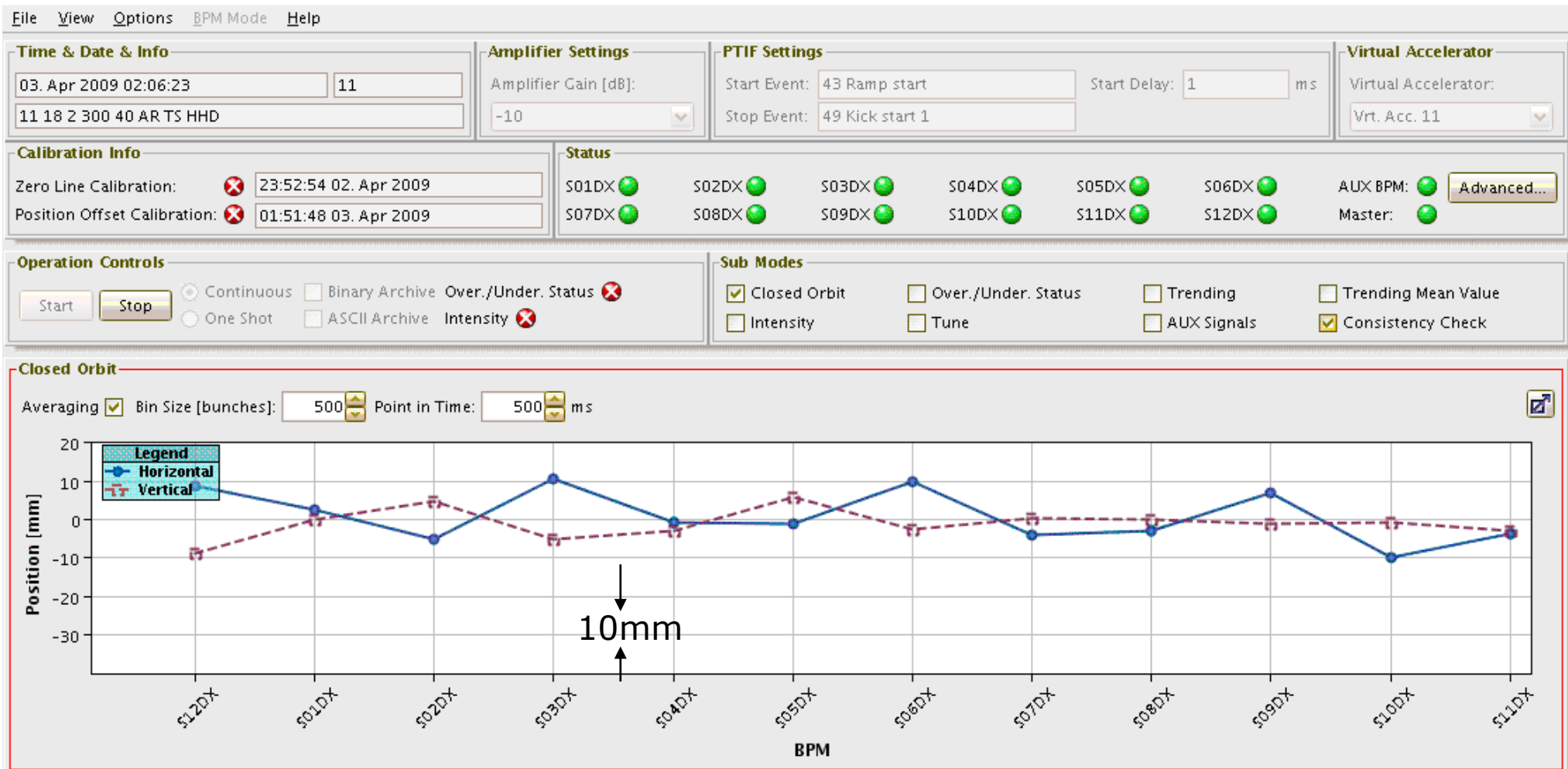
<b>Baseline Restoration Algorithm</b>	<b>Linear Regression Algorithm</b>
Difference over sum	Ordinary least square estimator
Adds noise to the pick-up data due to baseline restoration	No baseline restoration
Higher latency due to BLR, takes around 150 clock cycles	No BLR, 50 clock cycles
High dependence of position calculation on integration windows	Minimal dependence
Operational	Under implementation

# Data Acquisition Architecture

- 6 BPMs per Concentrator Server. One AUX in System
- Max. Data-Input of  $\approx 400$  MB/s per Concentrator Server via 10 GBit Ethernet
- Concentrator Server corrects the data with amplifier calibration and other offline calculations



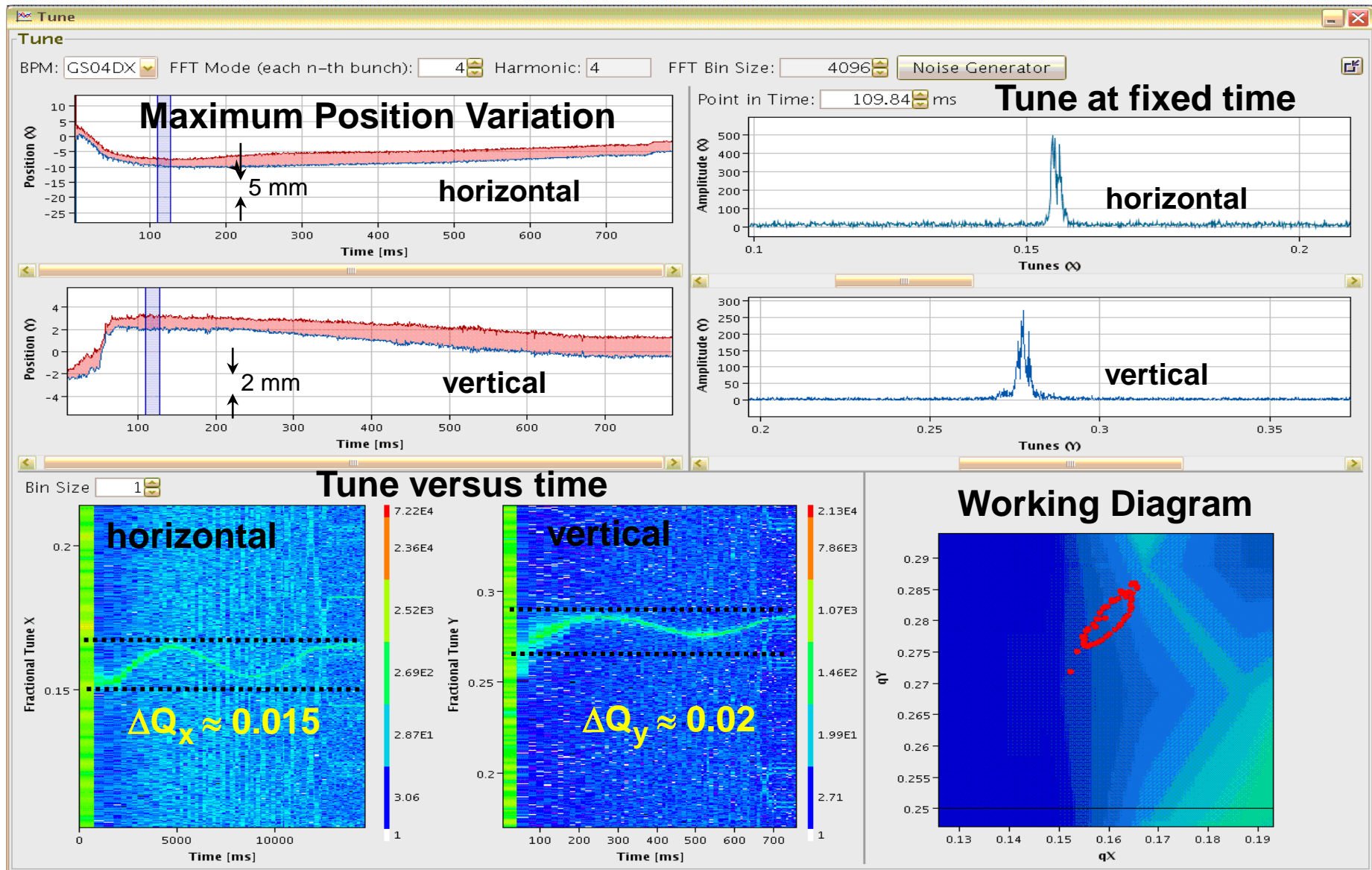
# GUI – Closed Orbit Mode



Closed orbit at the 12 BPM locations around the ring



# GUI – Position and Tune Mode



# Summary

- Presented the digital position calculation method at GSI SIS-18
- Suggested regression fit as a method for position evaluation over traditionally used baseline restoration method
- The bunch by bunch digital position calculation method offers a flexible method for detailed beam investigations



# Acknowledgement

European ITN- DITANET for funding the work and associated people to provide this opportunity

Thanks for your attention! Questions?

# References

- G.Vismara ; BIW 2000; SIGNAL PROCESSING FOR BEAM POSITION MONITORS
- A. Galatis et al.; DIPAC 2007; FIRST TESTS WITH THE SIS18 DIGITAL BPM SYSTEM

# Extra Slides

# Position Characteristics



Accuracy : Calibration Offset (Electronics and Pick-up), Numerical Estimator Bias

Resolution : Noise defined, Signal Processing

Dynamic Range : Defined by hardware

Stability : Temperature, Beam Intensity, Defined by hardware

# Basic analysis

$$x_i = Q(t_i)(O + k.p); y_i = Q(t_i)(O - k.p);$$

Where  $Q(t)$  is the charge profile,  $O$  is the common mode and  $k.p$  is the dipole mode

Diff over sum

$$\frac{\sum_{i=1}^N (x_i - y_i)}{\sum_{i=1}^N (x_i + y_i)} = \frac{k}{O} p$$

Linear regression

$$s = \frac{\sum_{i=1}^N x_i y_i}{\sum_{i=1}^N x_i^2}$$

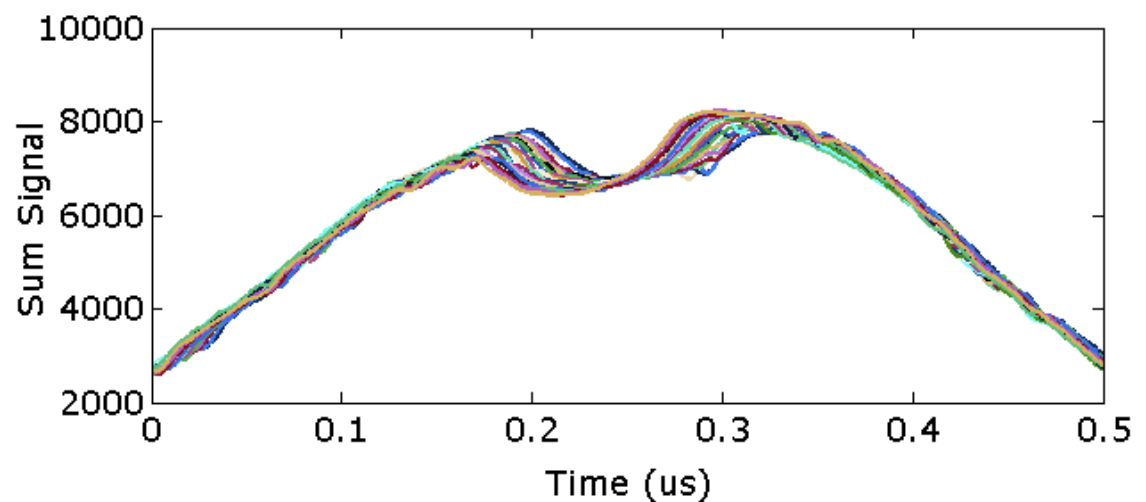
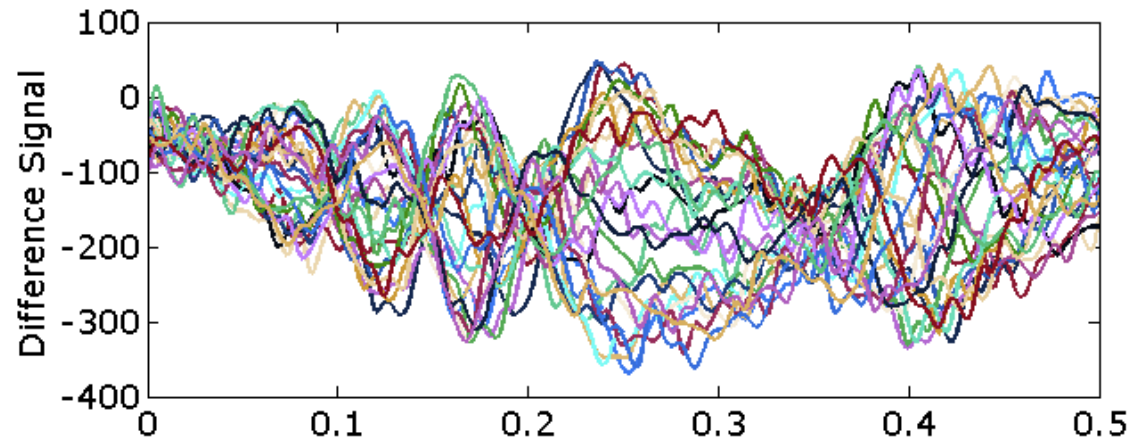
$$\frac{1-s}{1+s} = \frac{\sum x_i^2 - \sum x_i y_i}{\sum x_i^2 + \sum x_i y_i} \approx \frac{k}{O} p$$

$$O \gg kp$$



# Intra Bunch Motion at High Intensity

- No of stored  $\text{Ar}^{18+}$  Ions  $\sim 2e10$
- Energy = 11.4 MeV/u
- $F_{\text{rev}} = 214.5$  KHz
- Excitation  $\sim 1\text{mW/Hz}$
- Intra bunch oscillations i.e Head tail modes
- These effects are very important in view of FAIR

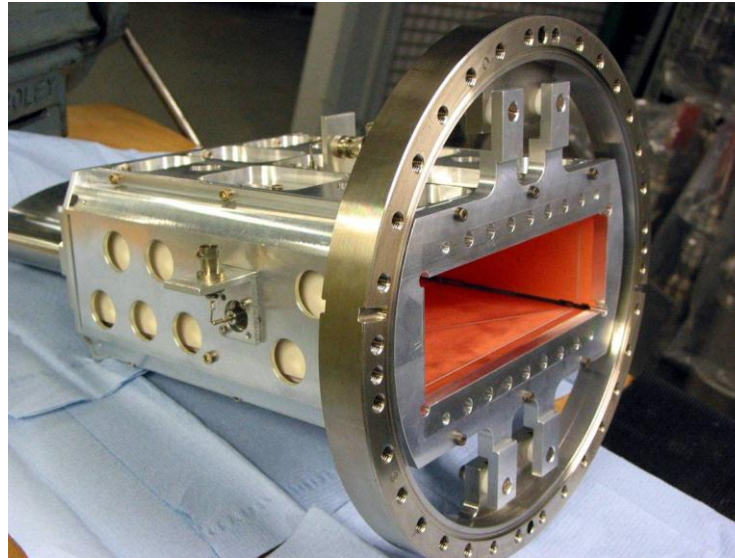
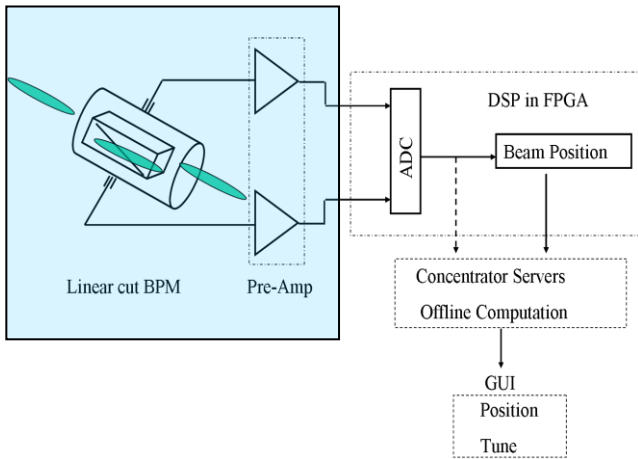
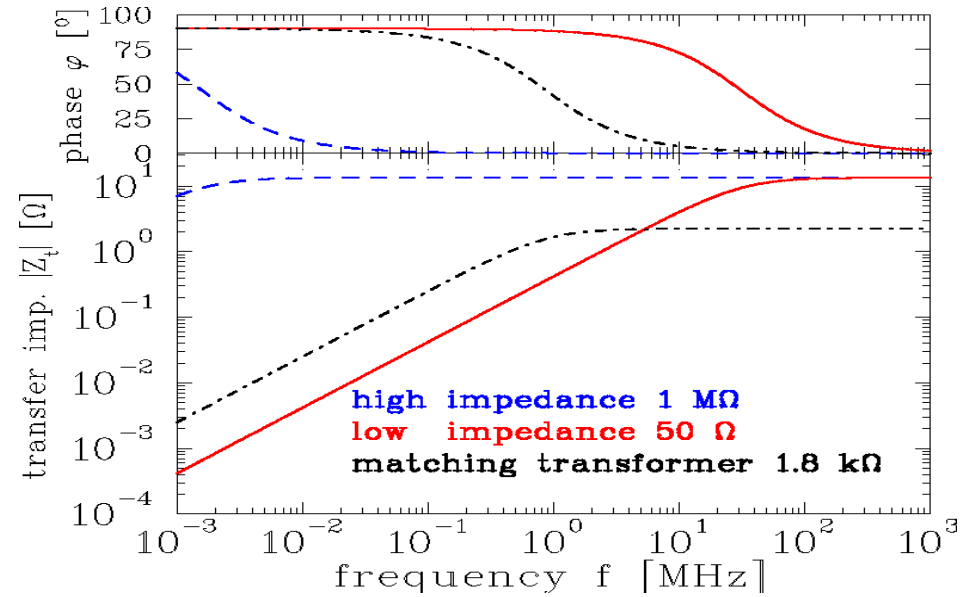
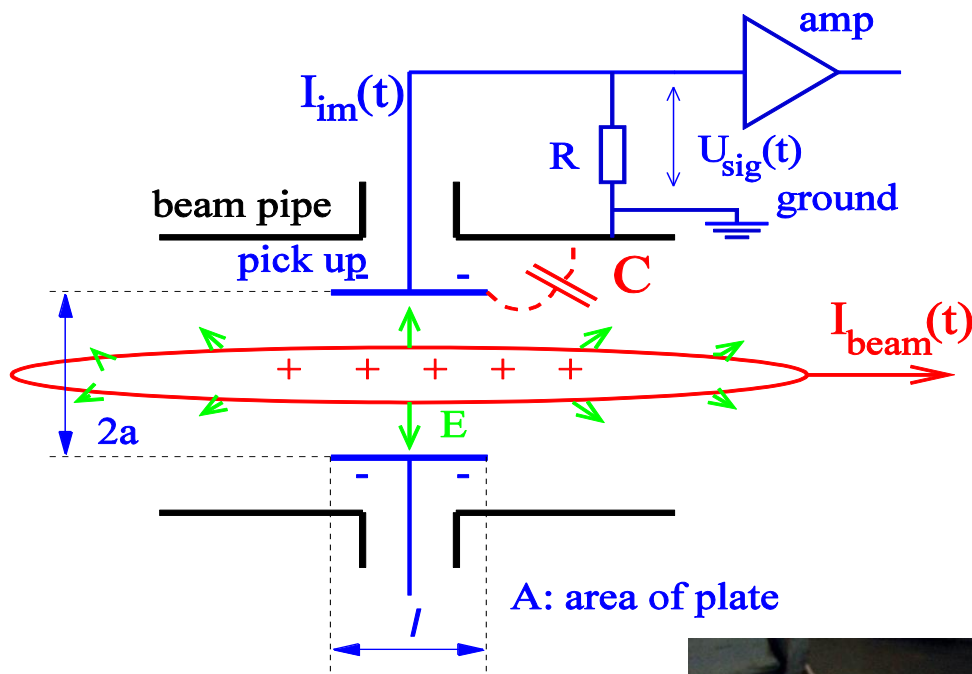


Bunch Length ( $\mu\text{s}$ )

# Linear Regression

- Linear regression with ordinary least square estimator
- Removes the need for baseline restoration
- Less dependence of bias on time window selection
- Less variance i.e higher SNR in tune spectra

# Shoe-Box BPMs



- Linear spatial sensitivity
- High pass response

