



CP violation measurements with the ATLAS detector

“Determination of ϕ_S and $\Delta\Gamma_S$
from the Decay $B_S \rightarrow J/\psi \phi$ ”

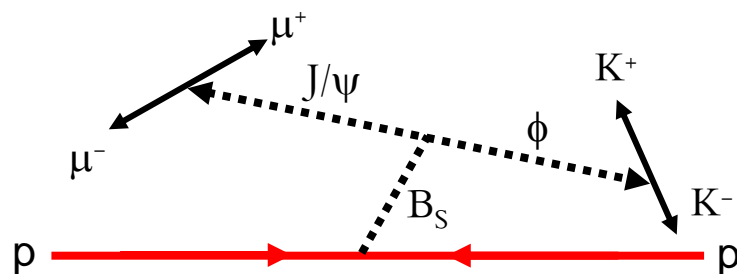
E. Kneringer – University of Innsbruck
on behalf of the ATLAS collaboration
BEACH2012, Wichita, USA





Motivation

- Main physics aim of this work of doing a time dependent **angular analysis** of $B_s \rightarrow J/\psi \phi$ decays in ATLAS:



Measurement of

- CP violating weak mixing phase ϕ_s
- precise measurement of $\Delta\Gamma_s$

- decay width difference between the mass eigenstates B_H and B_L

which could point to BSM physics.



Outline

- Introduction
 - CP violation and B_s Phenomenology
- ATLAS Detector
- The Measurement
 - Angular Correlations
 - Unbinned Maximum Likelihood Fit
- Results
 - Fit Projections
 - Systematic Uncertainties
 - Comparison with other Experiments
- Conclusions



CP violation and the CKM matrix

- Unitarity of CKM matrix

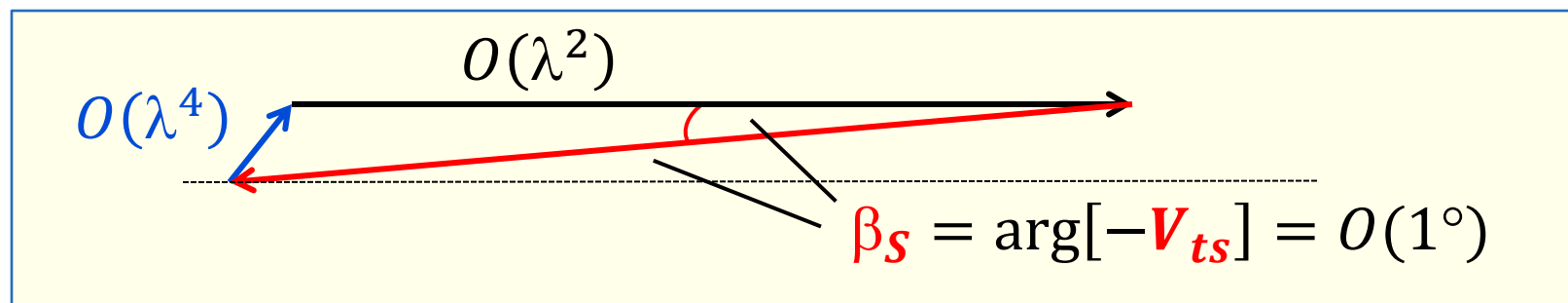
➤ constraint from 2nd and 3rd columns:

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & \mathbf{V_{ts}} & V_{tb} \end{pmatrix}$$

$$V_{us}V_{ub}^* + V_{cs}V_{cb}^* + \mathbf{V_{ts}}V_{tb}^* = 0$$

Wolfenstein parametrization:

$$O(\lambda^4): \lambda \cdot A\lambda^3(\rho + i\eta) + (1 - \frac{\lambda^2}{2}) \cdot A\lambda^2 + \mathbf{V_{ts}} \cdot 1 = 0$$



$$J = 2 \cdot \text{Area} = A\lambda^4\eta \cdot (1 - \frac{\lambda^2}{2}) A\lambda^2 = \underline{A^2\lambda^6\eta} + A^2\frac{\lambda^8}{2}\eta + O(\lambda^{10})$$

The quantity $\sin(2\beta_S)$ can be determined from a time dependent analysis of $B_S \rightarrow J/\psi\phi$.
Experimenters prefer $\phi_S \cong -2\beta_S$.



CP violation: neutral B_s system

- Interference of decays with and without mixing

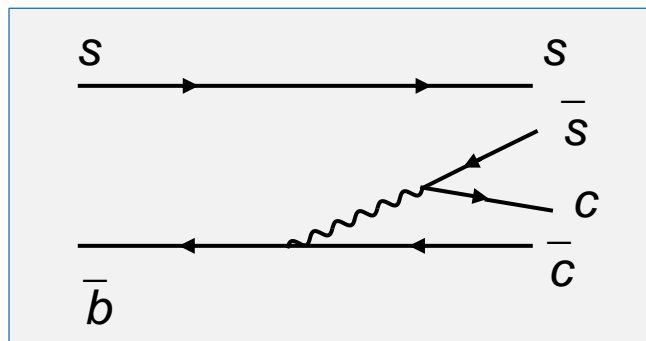
- Mixing induced CP violation

- Phase difference $\phi_S = 2 \cdot \arg[V_{ts}] = -2 \beta_S$

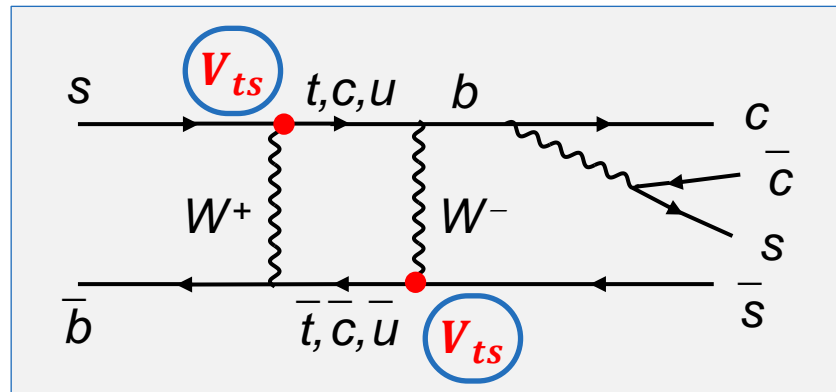
SM prediction: $\phi_S = -0.0368 \pm 0.0018$ rad

$B_S \rightarrow f$

$B_S \rightarrow \bar{B}_S \rightarrow f$



K^+
 K^-
 μ^+
 μ^-



μ^+
 μ^-
 K^+
 K^-

ϕ_S : This diagram justifies the name *weak mixing phase*.



Phenomenology of the B_S, \bar{B}_S system

- Mass eigenstates B_L, B_H are linear combinations of flavor eigenstates:

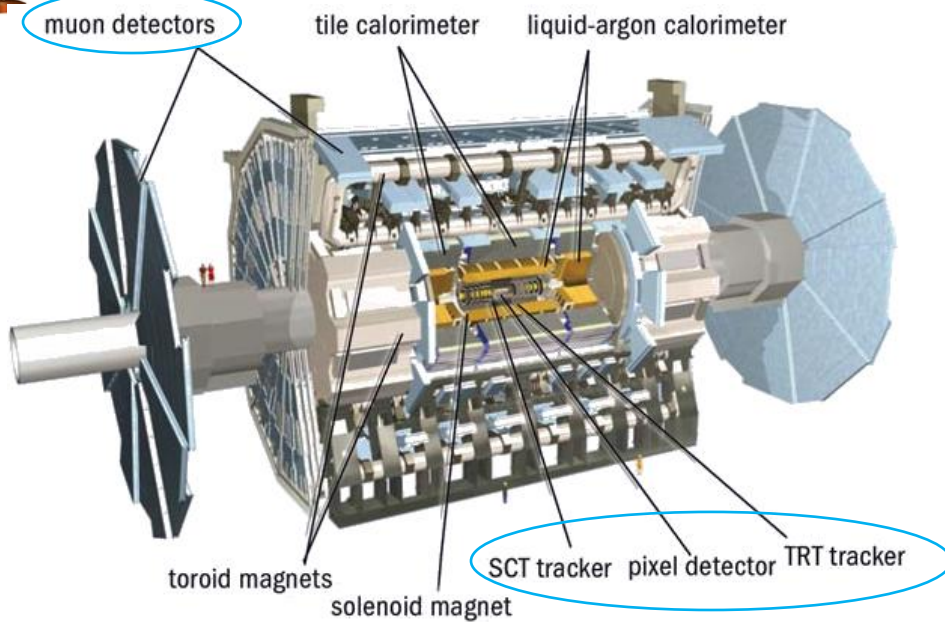
$$|B_{L,H}\rangle = p|B_S\rangle \pm q|\bar{B}_S\rangle$$

- CP violation $\rightarrow B_L, B_H \neq$ CP eigenstates
- Two particle system described by 4 parameters
 - oscillation frequency $\Delta m_S = m_H - m_L$
 - mean width $\Gamma_S = (\Gamma_L + \Gamma_H)/2$
 - width difference $\Delta\Gamma_S = \Gamma_L - \Gamma_H$
 - weak mixing phase $\phi_S \neq 0$ if CP violation

(plus nonperturbative parameters)



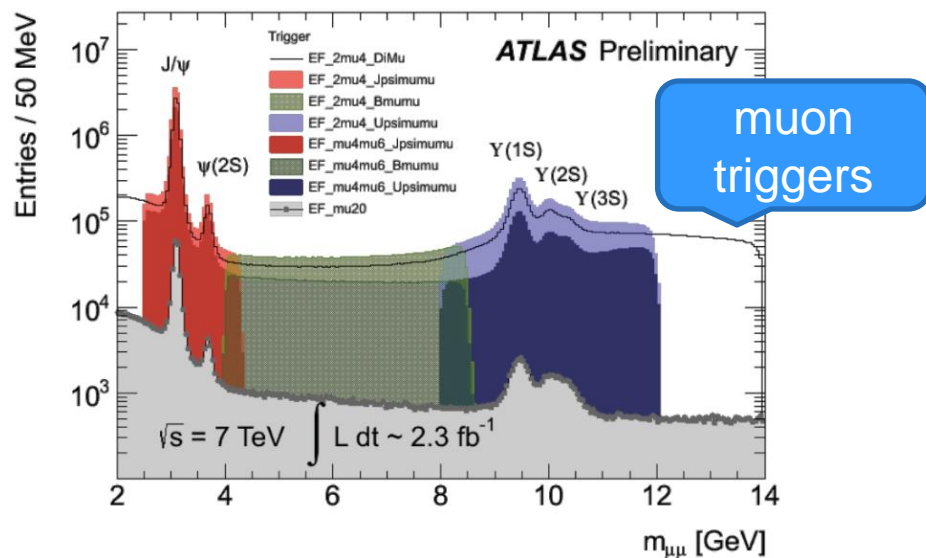
The ATLAS detector



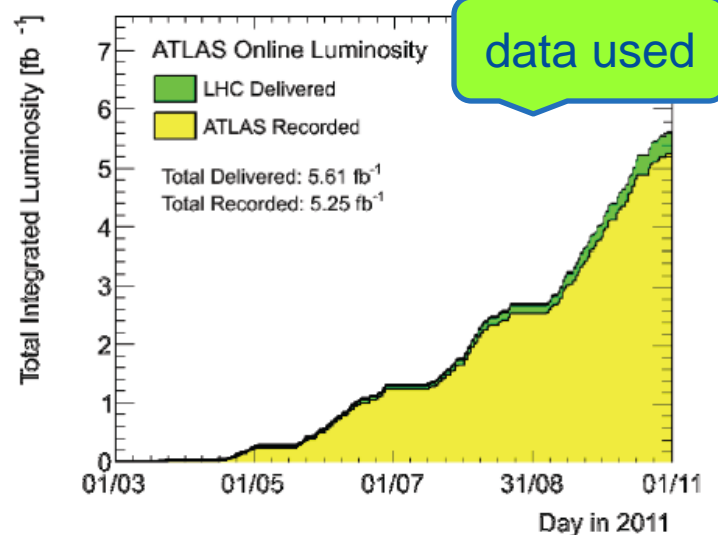
The ATLAS collaboration

38 Countries
185 Institutions
2866 Scientific Authors

every year:
several new applications
and expressions of interest
for membership



2011: $> 5 \text{ fb}^{-1}$ @ 7 TeV

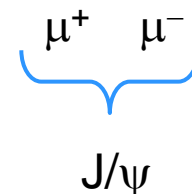




The measurement

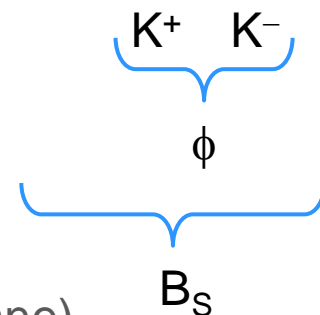
1. Trigger

- using 4.9 fb^{-1} of data collected 2011
- events selected by muon triggers (single, di-, J/ψ)
 - p_T threshold for muons: 4 – 10 GeV



2. Selection cuts

- different $J/\psi(\mu^+\mu^-)$ **mass windows** for barrel/endcap regions
 - since mass resolution depends on $|\eta|$ of muons
- $\phi(K^+K^-)$ invariant **mass window**: 22 MeV
 - p_T (kaons) > 1 GeV
- B-meson **secondary decay vertex fit**: $\chi^2/\text{dof} < 3$
 - mass m_i , proper decay time t_i (computed in transverse plane), decay angles



3. Acceptance calculated on large samples of signal and background Monte Carlo events

- e.g. $B^0 \rightarrow J/\psi K^{0*}$, $bb \rightarrow J/\psi X$, $pp \rightarrow J/\psi X$



$B_S(\bar{B}_S) \rightarrow J/\psi \phi$ and CP eigenstates

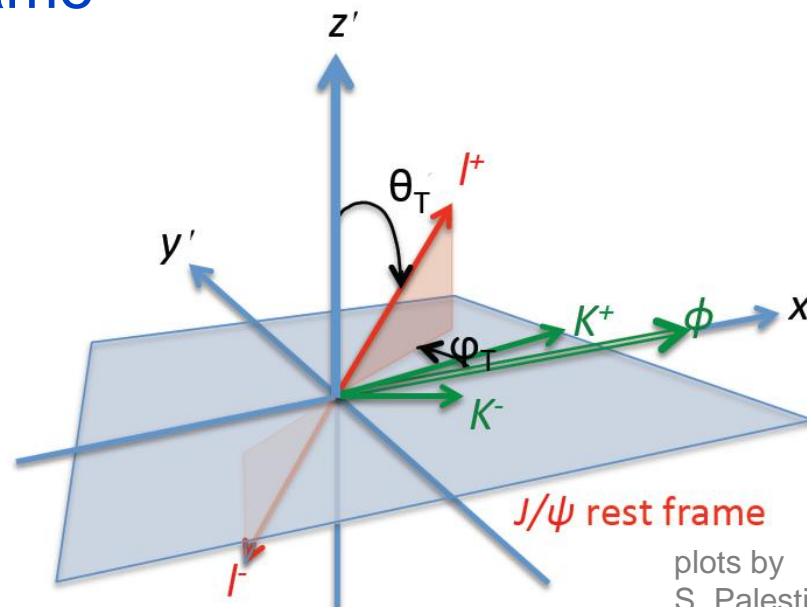
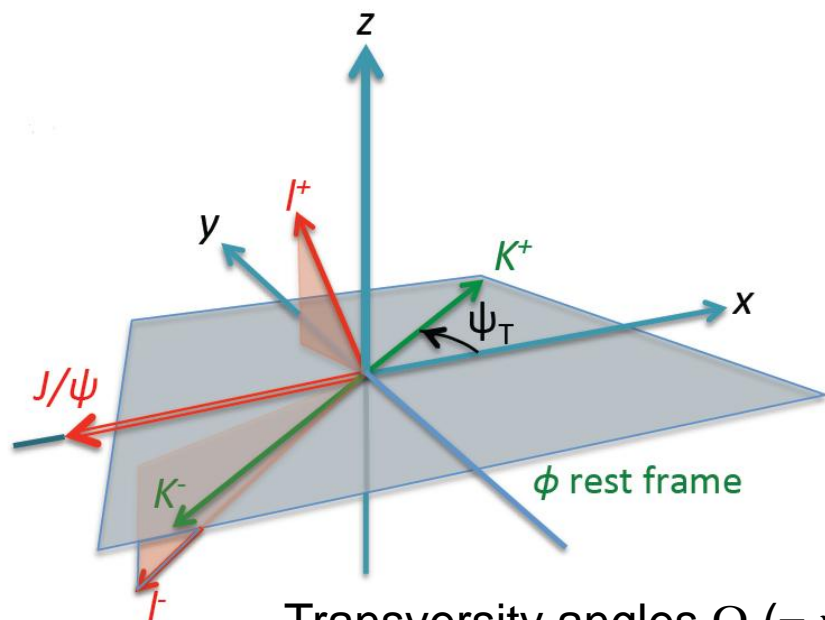
- Analysis does not distinguish the initial states, *i.e.* whether there is a B_S or a \bar{B}_S at the beginning = “untagged analysis”
 - Both initial states decay into the same final state
 - final state is a superposition of CP eigenstates
 - $J/\psi, \phi$ ($J^{PC} = 1^{--}, 1^{--}$) can have $L = 0, 1, 2$
- Pseudoscalar \rightarrow Vectormeson + Vectormeson, with relative L
- | | |
|---------------------------|-------------------------------|
| orbital angular momentum: | $L = 0, 2 \dots$ CP even (+1) |
| | $L = 1 \dots$ CP odd (−1) |
- CP eigenstates of final state can be distinguished (statistically) through their angular configuration
 - 4 particle final state $J/\psi (\rightarrow \mu^+ \mu^-)$ $\phi (\rightarrow K^+ K^-)$ can be described by three angles



Kinematics of the decay

- Transversity basis

- x-axis = direction of decay in B rest frame
- x-y plane = decay plane of K^+K^- ($K^+ \rightarrow +y$)
- ψ_T = angle between x-axis and K^+ direction (ϕ r.f.)
- θ_T and ϕ_T are the polar and azimuthal angles of the μ^+ in the J/ψ rest frame



plots by
S. Palestini

Transversity angles Ω ($= \psi_T, \theta_T, \phi_T$) are used to describe the angular distributions of the different CP (+1,-1) final states.



Angular and proper time distributions

• Differential decay rate

$$\frac{d^4\Gamma}{dt d\Omega} = \sum_{k=1}^{10} \mathcal{O}^{(k)}(t) g^{(k)}(\theta_T, \psi_T, \varphi_T)$$

k	$\mathcal{O}^{(k)}(t)$	$g^{(k)}(\theta_T, \psi_T, \varphi_T)$
1	$\frac{1}{2} A_0(0) ^2 \left[(1 + \cos \phi_s) e^{-\Gamma_L^{(s)} t} + (1 - \cos \phi_s) e^{-\Gamma_H^{(s)} t} \right]$	$2 \cos^2 \psi_T (1 - \sin^2 \theta_T \cos^2 \varphi_T)$
2	$\frac{1}{2} A_{\parallel}(0) ^2 \left[(1 + \cos \phi_s) e^{-\Gamma_L^{(s)} t} + (1 - \cos \phi_s) e^{-\Gamma_H^{(s)} t} \right]$	$\sin^2 \psi_T (1 - \sin^2 \theta_T \sin^2 \varphi_T)$
3	$\frac{1}{2} A_{\perp}(0) ^2 \left[(1 - \cos \phi_s) e^{-\Gamma_L^{(s)} t} + (1 + \cos \phi_s) e^{-\Gamma_H^{(s)} t} \right]$	$\sin^2 \psi_T \sin^2 \theta_T$
4	$\frac{1}{2} A_0(0) A_{\parallel}(0) \cos \delta_{\parallel} \left[(1 + \cos \phi_s) e^{-\Gamma_L^{(s)} t} + (1 - \cos \phi_s) e^{-\Gamma_H^{(s)} t} \right]$	$\frac{1}{\sqrt{2}} \sin 2\psi_T \sin^2 \theta_T \sin 2\varphi_T$
5	$\frac{1}{2} A_{\parallel}(0) A_{\perp}(0) \left(e^{-\Gamma_H^{(s)} t} - e^{-\Gamma_L^{(s)} t} \right) \cos(\delta_{\perp} - \delta_{\parallel}) \sin \phi_s$	$\sin^2 \psi_T \sin 2\theta_T \sin \varphi_T$
6	$-\frac{1}{2} A_0(0) A_{\perp}(0) \left(e^{-\Gamma_H^{(s)} t} - e^{-\Gamma_L^{(s)} t} \right) \cos \delta_{\perp} \sin \phi_s$	$\frac{1}{\sqrt{2}} \sin 2\psi_T \sin 2\theta_T \cos \varphi_T$
7	$\frac{1}{2} A_S(0) ^2 \left[(1 - \cos \phi_s) e^{-\Gamma_L^{(s)} t} + (1 + \cos \phi_s) e^{-\Gamma_H^{(s)} t} \right]$	$\frac{2}{3} (1 - \sin^2 \theta_T \cos^2 \varphi_T)$
8	$-\frac{1}{2} A_S(0) A_{\parallel}(0) \left(e^{-\Gamma_H^{(s)} t} - e^{-\Gamma_L^{(s)} t} \right) \sin(\delta_{\parallel} - \delta_S) \sin \phi_s$	$\frac{1}{3} \sqrt{6} \sin \psi_T \sin^2 \theta_T \sin 2\varphi_T$
9	$\frac{1}{2} A_S(0) A_{\perp}(0) \left[(1 - \cos \phi_s) e^{-\Gamma_L^{(s)} t} + (1 + \cos \phi_s) e^{-\Gamma_H^{(s)} t} \right] \sin(\delta_{\perp} - \delta_S)$	$\frac{1}{3} \sqrt{6} \sin \psi_T \sin 2\theta_T \cos \varphi_T$
10	$-\frac{1}{2} A_0(0) A_S(0) \sin(-\delta_S) \left(e^{-\Gamma_H^{(s)} t} - e^{-\Gamma_L^{(s)} t} \right) \sin \phi_s$	$\frac{4}{3} \sqrt{3} \cos \psi_T (1 - \sin^2 \theta_T \cos^2 \varphi_T)$

CP
+1
+1
-1

polarization
state
long.
trans.
trans.

interference
terms

Terms related to
non-resonant
and via the f_0 state
 K^+K^- production
(S-wave) \rightarrow small

Normalization: $|A_0(0)|^2 + |A_{\parallel}(0)|^2 + |A_{\perp}(0)|^2 + |A_S(0)|^2 = 1$

Each amplitude A_X comes with its strong phase δ_X .

Define strong phases relative to $A_0(0)$: choose $\delta_0 = 0$

\rightarrow 3 amplitudes + 3 strong phases = 6 parameters for the fit!

$$\sin \phi_s \approx \phi_s$$

$$\cos \phi_s = 1 + \mathcal{O}(\phi_s^2)$$



Symmetries

- ϕ_S enters the likelihood via the 10 functions describing the proper decay time distribution, e.g. terms:

$$f(\Delta\Gamma_S) \cos(\delta_\perp - \delta_\parallel) \stackrel{(-1)}{\sin} \phi_S$$

$$e^{-\Delta\Gamma_S} \cos \phi_S - e^{+\Delta\Gamma_S} \cos \phi_S$$
- Likelihood is invariant under the transformations

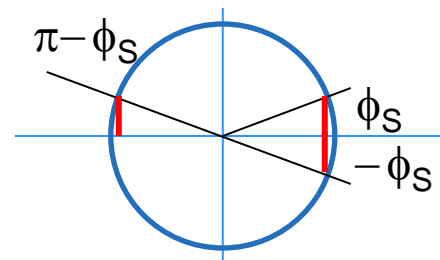
$\{\phi_S, \delta_\perp, \delta_\parallel, \delta_S, \Delta\Gamma_S\} \rightarrow \{-\phi_S, \pi - \delta_\perp, -\delta_\parallel, -\delta_S, \Delta\Gamma_S\}$

but also

$\{\phi_S, \delta_\perp, \delta_\parallel, \delta_S, \Delta\Gamma_S\} \rightarrow \{\pi - \phi_S, \pi - \delta_\perp, -\delta_\parallel, -\delta_S, -\Delta\Gamma_S\}$

and the combination of the two.

➤ 4-fold symmetry of the fit result
- ATLAS is not yet able to resolve the ambiguities
 needs external input





Construction of the Likelihood function \mathcal{L}

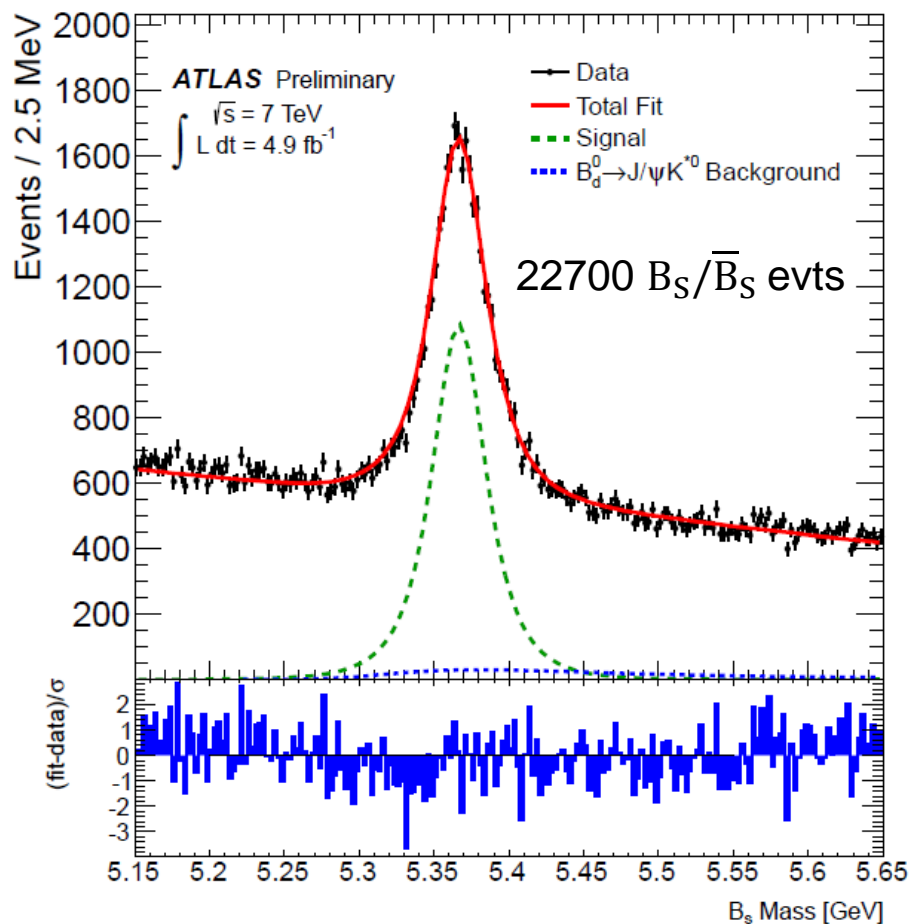
- Measured variables (*vars*)
 - $(m_i, \sigma_{m_i}), (t_i, \sigma_{t_i}), \Omega_i,$
 - set of nuisance parameters to describe background
- 27 parameters in the full fit (*pars*)
 - 9 physics parameters
 - 3 parameters of the B_S, \bar{B}_S system (not Δm_S)
 - 3 transversity amplitudes $|A_0|, |A_{||}|, |A_S|$
 - 3 strong phases $\delta_{\perp}, \delta_{||}, \delta_S$
 - signal fraction $f_S \rightarrow$ number of signal events
 - parameters describing various distributions
 - the J/ψ signal mass distribution, angular background distributions, estimated decay time uncertainty distributions for signal and background events, scale factors

$\max \mathcal{L}(pars; vars) \rightarrow$ best fit

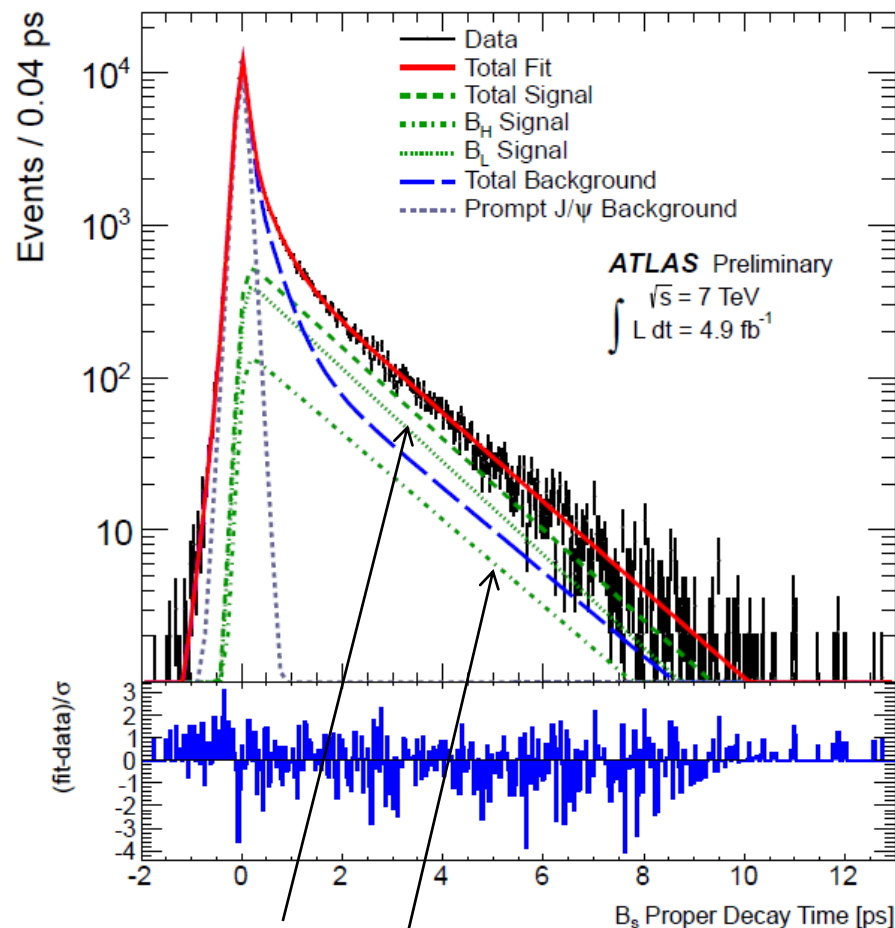


Result of the fit: fit projections

B_s meson mass



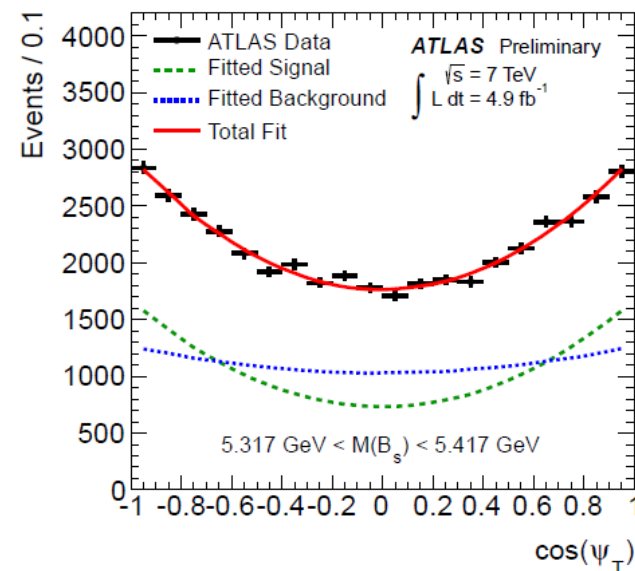
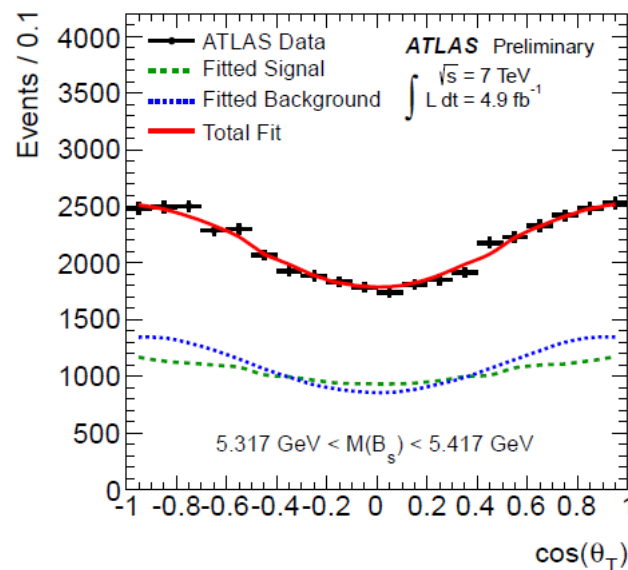
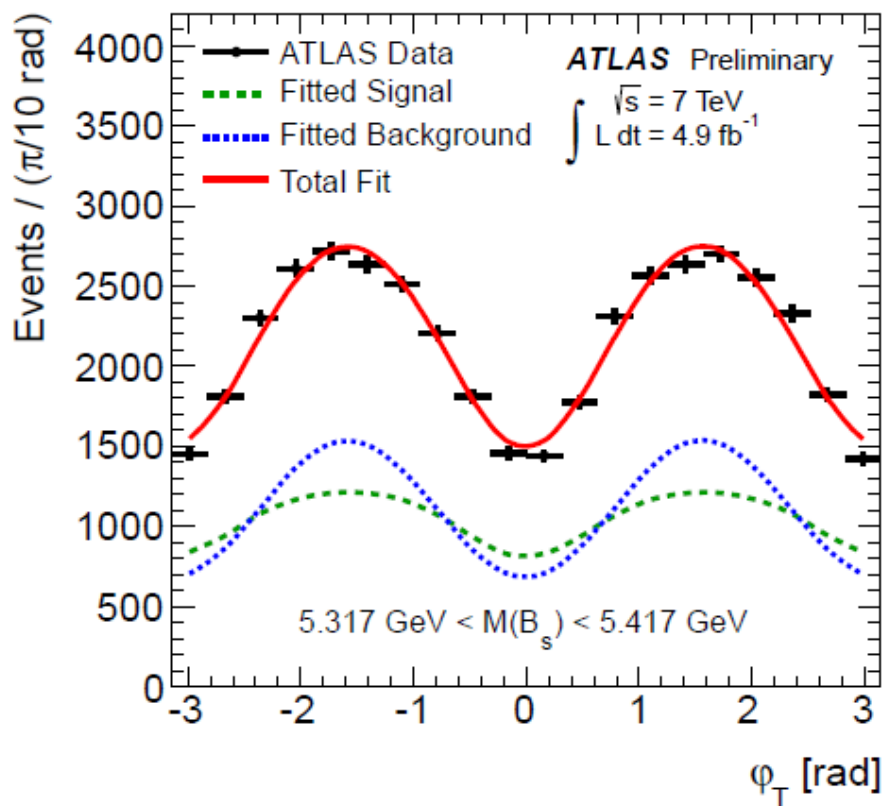
proper decay time



$$\Delta\Gamma_S = \Gamma_L - \Gamma_H$$



Fit projections – transversity angles



Important for measuring the absolute values of the transversity amplitudes A_0 , A_{\parallel} , A_{\perp} , A_S .



Systematic uncertainties

- They are calculated using **different techniques**, including changes in detector simulation (alignment), data based studies (efficiency), Monte Carlo pseudo experiments (mass models) and variations in analysis methods and assumptions.

Systematic Uncertainty	$\phi_s(\text{rad})$	$\Delta\Gamma_s(\text{ps}^{-1})$	$\Gamma_s(\text{ps}^{-1})$	$ A_{\parallel}(0) ^2$	$ A_0(0) ^2$	$ A_S(0) ^2$
Inner Detector alignment	0.04	< 0.001	0.001	< 0.001	< 0.001	< 0.01
Trigger efficiency	< 0.01	< 0.001	0.002	< 0.001	< 0.001	< 0.01
Signal mass model	0.02	0.002	< 0.001	< 0.001	< 0.001	< 0.01
Background mass model	0.03	0.001	< 0.001	0.001	< 0.001	< 0.01
Resolution model	0.05	< 0.001	0.001	< 0.001	< 0.001	< 0.01
Background lifetime model	0.02	0.002	< 0.001	< 0.001	< 0.001	< 0.01
Background angles model	0.05	0.007	0.003	0.007	0.008	0.02
B^0 contribution	0.05	< 0.001	< 0.001	< 0.001	0.005	< 0.01
Totals	0.10	0.008	0.004	0.007	0.009	0.02



Results of the fit in numbers

- Statistical error for ϕ_s rather large because of limited proper decay time resolution of ATLAS
 - but still competitive with Tevatron results

Parameter	Value	Statistical uncertainty	Systematic uncertainty
$\phi_s(\text{rad})$	0.22	0.41	0.10
$\Delta\Gamma_s(\text{ps}^{-1})$	0.053	0.021	0.008
$\Gamma_s(\text{ps}^{-1})$	0.677	0.007	0.004
$ A_0(0) ^2$	0.528	0.006	0.009
$ A_{\parallel}(0) ^2$	0.220	0.008	0.007
$ A_S(0) ^2$	0.02	0.02	0.02



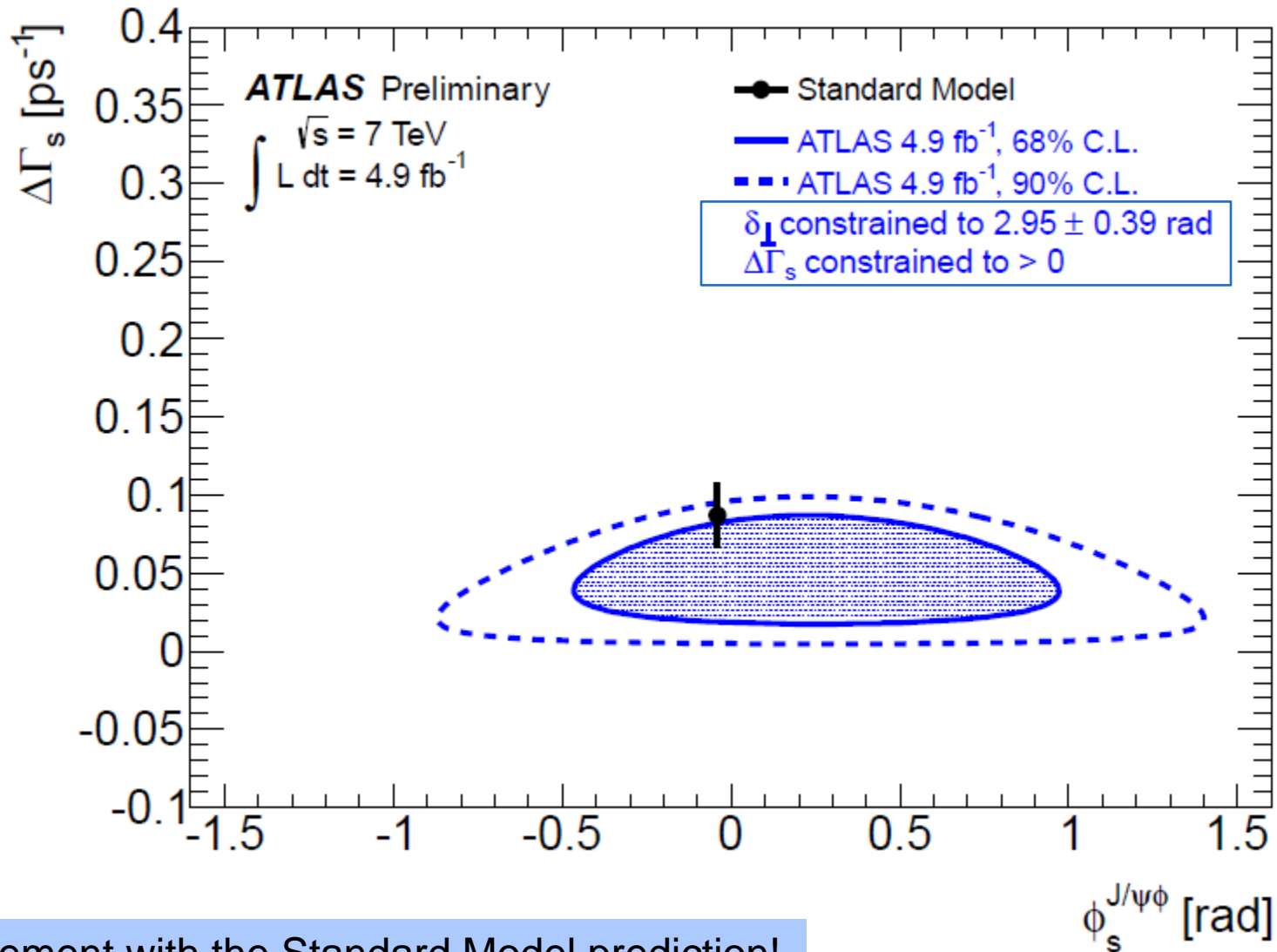
& correlation matrix

- Largest correlation between Γ_s and $\Delta\Gamma_s$
- B_s meson parameters are practically uncorrelated with the amplitudes.

	ϕ_s	$\Delta\Gamma_s$	Γ_s	$ A_0(0) ^2$	$ A_{\parallel}(0) ^2$	$ A_S(0) ^2$
ϕ_s	1.00	-0.13	0.38	-0.03	-0.04	0.02
$\Delta\Gamma_s$		1.00	-0.60	0.12	0.11	0.10
Γ_s			1.00	-0.06	-0.10	0.04
$ A_0(0) ^2$				1.00	-0.30	0.35
$ A_{\parallel}(0) ^2$					1.00	0.09
$ A_S(0) ^2$						1.00



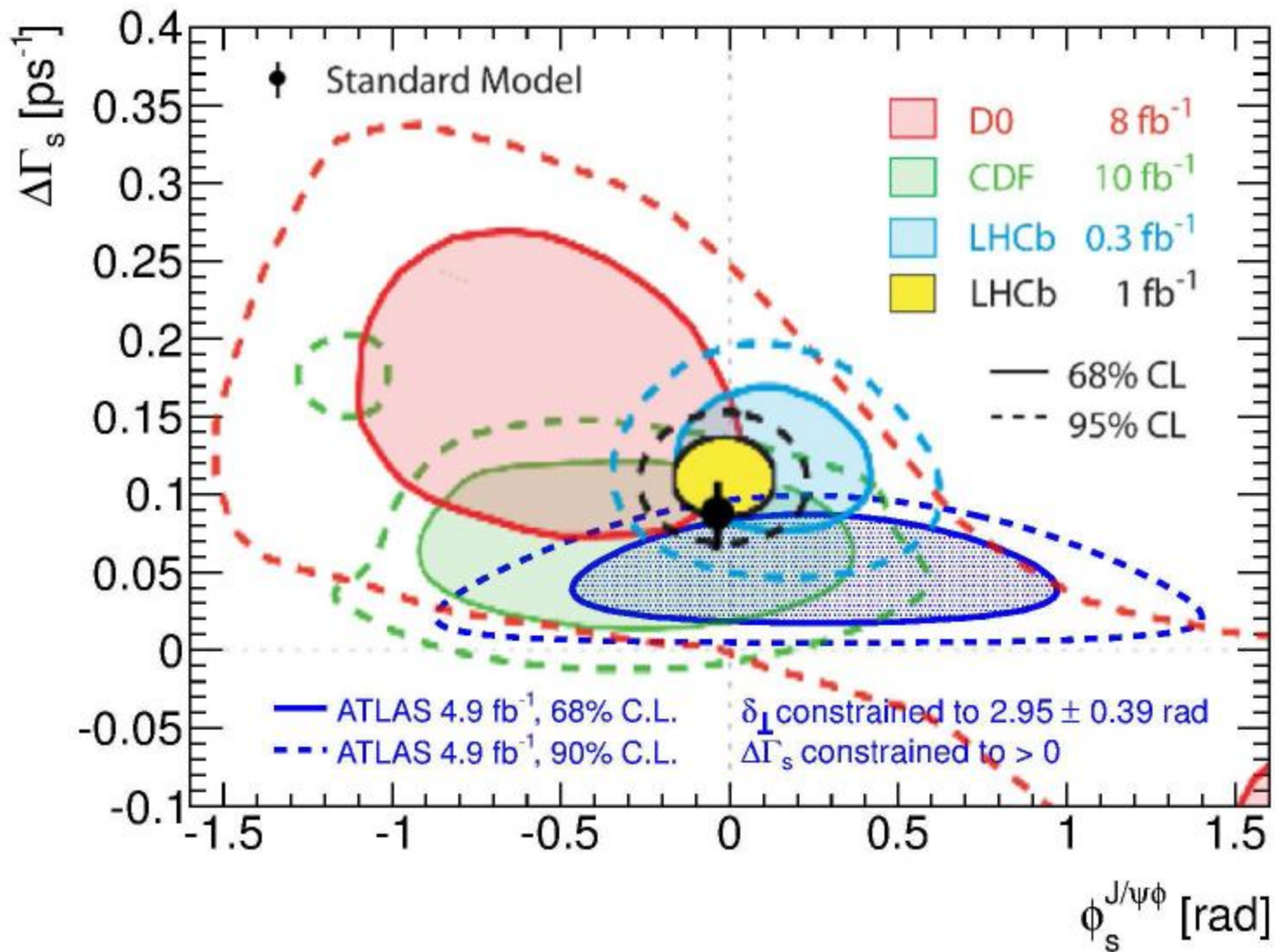
Likelihood contours: ϕ_s - $\Delta\Gamma_s$ plane



Agreement with the Standard Model prediction!



Comparison





Conclusion

- From 4.9 fb^{-1} of data collected by ATLAS in 2011 decay time and angular distributions have been studied in a sample of $22700 \text{ B}_s/\bar{\text{B}}_s \rightarrow \text{J}/\psi \phi$ decays. Without flavor tagging, and assuming $\delta_{\perp} = 2.95 \pm 0.39 \text{ rad}$ the results of the analysis are:

$$\begin{aligned}\phi_s &= 0.22 \pm 0.41 \text{ (stat.)} \pm 0.10 \text{ (syst.) rad} \\ \Delta\Gamma_s &= 0.053 \pm 0.021 \text{ (stat.)} \pm 0.008 \text{ (syst.) ps}^{-1} \\ \Gamma_s &= 0.677 \pm 0.007 \text{ (stat.)} \pm 0.004 \text{ (syst.) ps}^{-1} \\ |A_0(0)|^2 &= 0.528 \pm 0.006 \text{ (stat.)} \pm 0.009 \text{ (syst.)} \\ |A_{\parallel}(0)|^2 &= 0.220 \pm 0.008 \text{ (stat.)} \pm 0.007 \text{ (syst.)}\end{aligned}$$

- Future:
 - Plan to implement flavor tagging (distinguish $\text{B}_s/\bar{\text{B}}_s$)
 - Increased data sample in 2012 (\sim factor 3 is realistic), but fewer events $/\text{fb}^{-1}$ (due to increased p_{T} cuts); expect to half our statistical errors.



References

- SM expected values for ϕ_S , $\Delta\Gamma_S$
 - UTFit Collaboration, PRL 97, 151803 (2006)
- Decay time an angular correlation formalism
 - A. Dighe, I. Dunietz, R. Fleischer, EPJ-C 6 (1999) 647
- Results from other experiments (LHCb, CDF, D0)
 - CDF Collaboration: CDF-Public-Note-10778
 - D0 Collaboration: PRD85, 032006 (2012)
 - LHCb Collaboration: LHCb-CONF-2012-002;
PRL 108, 101803 (2012); PRL 108, 241801 (2012)
- This ATLAS analysis
 - ATLAS Collaboration, ATLAS-CONF-2012-xxx



backup slides



ATLAS result on strong phases

Input:

δ_{perp}	Constrained to 2.95 ± 0.39 rad
------------------------	------------------------------------

Likelihood fit:

δ_{par}	Best fit: π , 1σ range: $3.04\text{--}3.24$ rad
$\delta_{\text{perp}} - \delta_S$	0.03 ± 0.13 rad



Maximum Likelihood fit

$$\ln \mathcal{L} = \sum_{i=1}^N \left\{ w_i \cdot \ln(f_s \cdot \mathcal{F}_s(m_i, t_i, \Omega_i) + f_s \cdot f_{B^0} \cdot \mathcal{F}_{B^0}(m_i, t_i, \Omega_i) + (1 - f_s \cdot (1 + f_{B^0})) \mathcal{F}_{\text{bkg}}(m_i, t_i, \Omega_i)) \right\} + \underbrace{\ln P(\delta_{\perp})}_{\text{Gaussian constraint}}$$

signal:

$$\mathcal{F}_s(m_i, t_i, \Omega_i) = P_s(m_i | \sigma_{m_i}) \cdot \overbrace{P_s(\sigma_{m_i})}^{10 \text{ } O^{(k)}\text{-functions}} \cdot \underbrace{P_s(\Omega_i, t_i | \sigma_{t_i})}_{10 \text{ } O^{(k)}\text{-functions}} \cdot \overbrace{P_s(\sigma_{t_i})}^{10 \text{ } O^{(k)}\text{-functions}} \cdot \underbrace{A(\Omega_i, p_{Ti})}_{\text{angular sculpting}} \cdot \overbrace{P_s(p_{Ti})}^{10 \text{ } O^{(k)}\text{-functions}}$$

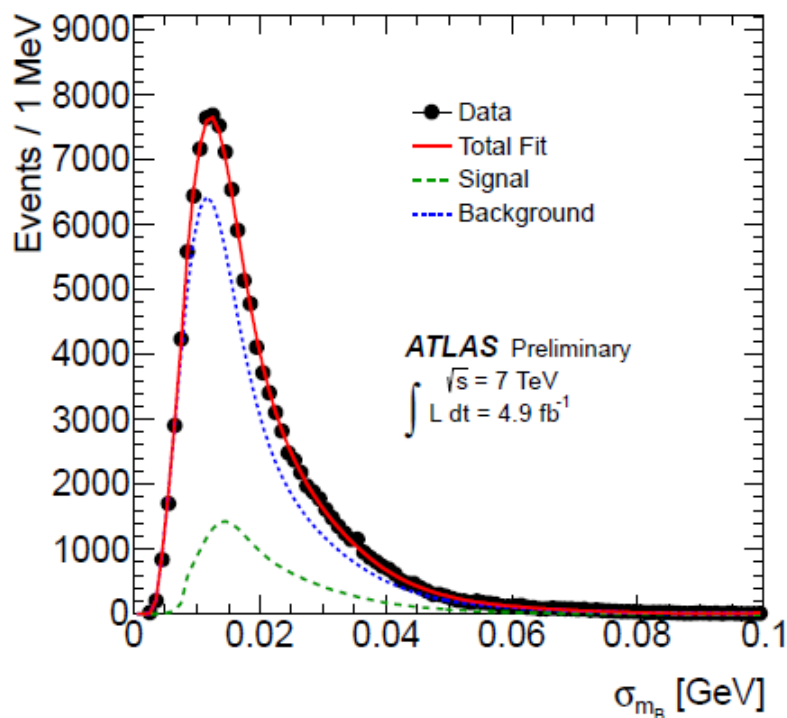
background:

$$\begin{aligned} \mathcal{F}_{B^0}(m_i, t_i, \Omega_i) &= P_{B^0}(m_i) \cdot P_s(\sigma_{m_i}) \cdot P_{B^0}(t_i | \sigma_{t_i}) \\ &\quad \cdot P_{B^0}(\theta_T) \cdot P_{B^0}(\varphi_T) \cdot P_{B^0}(\psi_T) \cdot P_s(\sigma_{t_i}) \cdot P_s(p_{Ti}) \\ \mathcal{F}_{\text{bkg}}(m_i, t_i, \Omega_i) &= P_b(m_i) \cdot P_b(\sigma_{m_i}) \cdot P_b(t_i | \sigma_{t_i}) \\ &\quad \cdot P_b(\theta_T) \cdot P_b(\varphi_T) \cdot P_b(\psi_T) \cdot P_b(\sigma_{t_i}) \cdot P_b(p_{Ti}) \end{aligned}$$

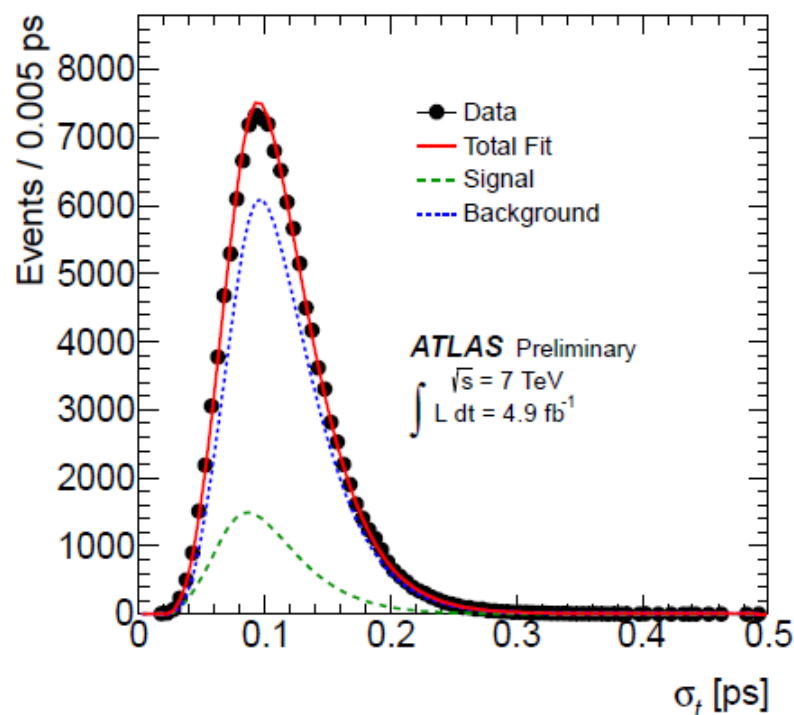


Uncertainty distributions $P_{s,b}(\sigma_{m,t})$

Mass and decay-time measurements enter the likelihood with event-by-event uncertainties. The error distributions are extracted from data. Checks done → no significant systematics.



Mass uncertainty distribution from data, the fits to the background and the signal fractions and the sum of the two fits.



Same for:
Proper decay time uncertainty distribution.



Mass distributions

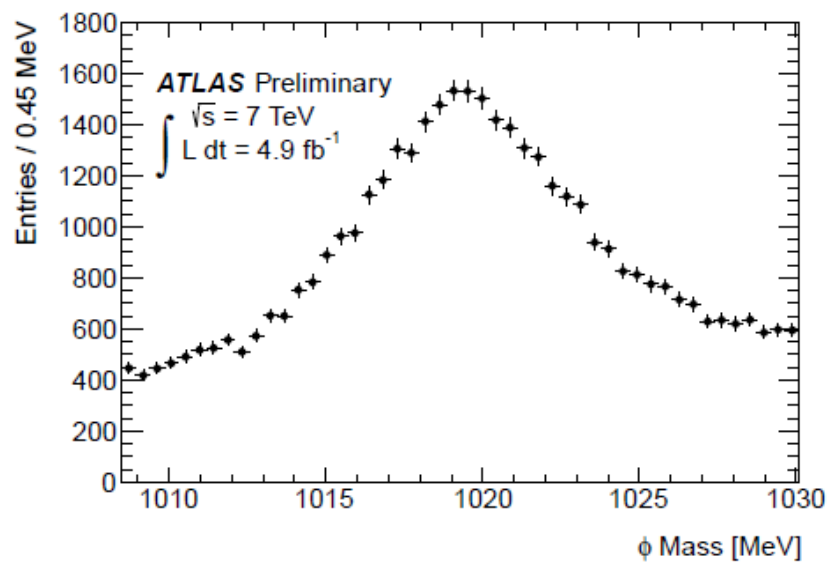
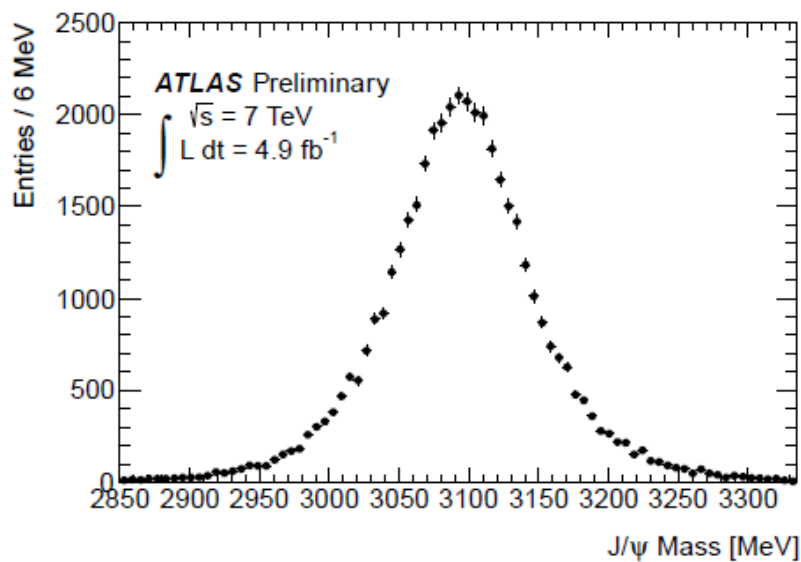
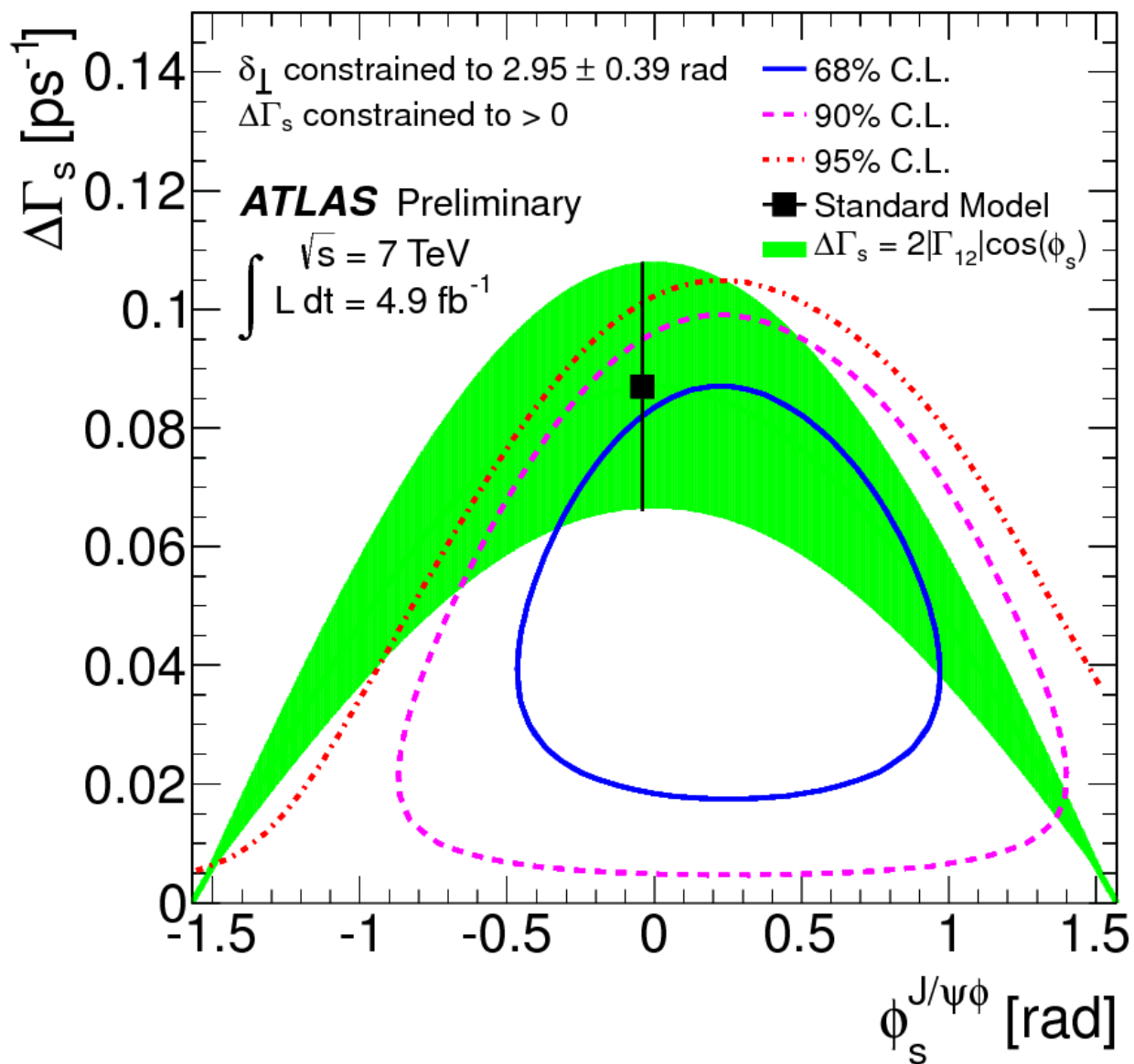


Figure 11. Mass distributions of $J/\psi \rightarrow \mu^+\mu^-$ and $\phi \rightarrow K^+K^-$ decays for B_s^0 candidates within the signal mass range $5.317 \text{ GeV} < m(B_s^0) < 5.417 \text{ GeV}$.

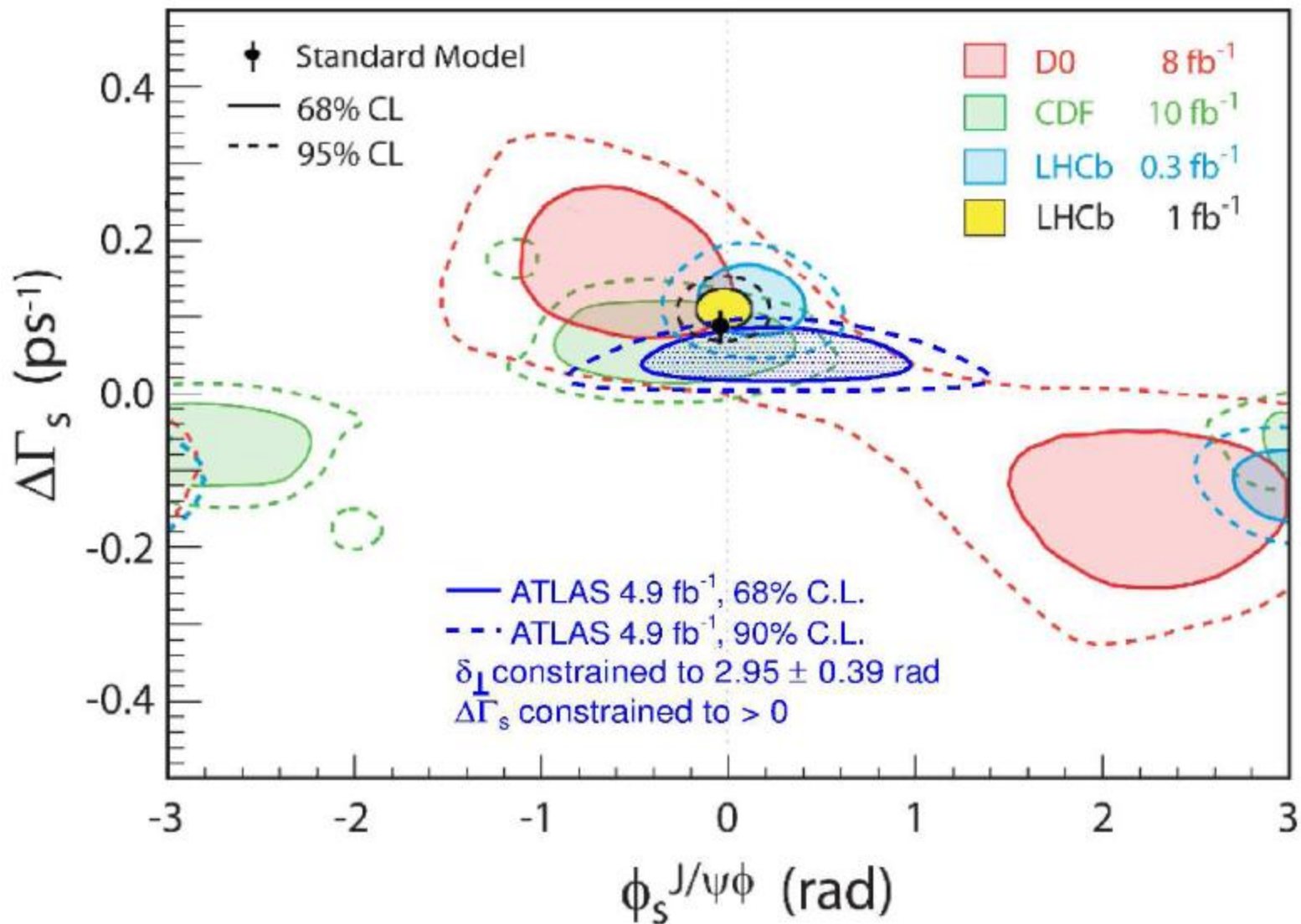


Contour plot





on a larger scale





Comparision of measurements

- compiled by S. Palestini

	Γ_s [ps-1]	$\Delta\Gamma_s$ [ps-1]	$ A_0 ^2$	$ A_{\text{par}} ^2$	φ_s [rad]	$ A_s ^2$	δ_{perp} [rad]	δ_{par} [rad]	δ_s [rad]	Signal sample
D0 (8 fb ⁻¹ , stat(+)syst $\Delta\Gamma_s > 0$ case)	0.693 -0.020 +0.015	0.179 -0.060 +0.059	0.565 ± 0.017	0.249 -0.022 +0.021	-0.56 -0.32 +0.36	0.173 ± 0.036 <i>effective</i>	<i>Near π</i> <i>[Assum. \cos</i> <i>(δ_{perp}) < 0]</i>	3.15 ± 0.19	$\cos(\delta_{\text{perp}} - \delta_s) = -0.20$ -0.27+0.26	~5300
CDF (10fb ⁻¹ , unpublished)	0.654 ± 0.008 ± 0.004	0.068 ± 0.026 ± 0.007	0.512 ± 0.012 ± 0.017	0.229 ± 0.010 ± 0.014	=SM <i>Fit: -0.2</i> <i>4± 0.36</i>	<i>Appar.</i> <i>small</i>	2.79 ± 0.53 ± 0.15	<i>Near π</i>	<i>Small</i> <i>effect</i>	11000
LHCb (1fb ⁻¹ , unpublished)	0.6580 ± 0.0054 ± 0.0066	0.116 ± 0.018 ± 0.006	0.523 ± 0.007 ± 0.024	0.231 ± 0.021 [*]	-0.001 ± 0.101 ± 0.027	0.022 ± 0.012 ± 0.007	2.90 ± 0.36 ± 0.07	<i>Near π</i> ± 0.33 ± 0.13	2.90 ± 0.36 ± 0.08	21000
ATLAS (4.9fb ⁻¹ , preliminary)	0.677 ± 0.007 ± 0.004	0.053 ± 0.021 ± 0.008	0.528 ± 0.006 ± 0.009	0.220 ± 0.008 ± 0.007	0.22 ± 0.41 ± 0.10	0.02 ± 0.02 ± 0.02	<i>Assum.</i> 2.95 ± 0.39	<i>near π</i>	<i>Near</i> δ_{perp}	23000

[*] from $|A_0|^2$ and $|A_{\text{par}}|^2$, summing stat. and syst. errors in quadrature and using quoted (negative) correlation coefficient.



New Physics in $B_S - \bar{B}_S$ mixing

- Would change the off-diagonal element M_{12} of the **mass matrix** (but not significantly affect the corresponding decay matrix element Γ_{12})
 - parametrization: $M_{12}^s \equiv M_{12}^{\text{SM},s} \cdot \Delta_s, \quad \Delta_s \equiv |\Delta_s| e^{i\phi_s^\Delta}.$
 - correction adds linearly to the weak phase, like in $\sin(\phi_s^{\text{SM}} + \phi_s^\Delta)$
 - for small ϕ_s only contributes quadratically to $\Delta\Gamma_s$:
$$\Delta\Gamma_s = 2|\Gamma_{12}^s| \cos(\phi_s^{\text{SM}} + \phi_s^\Delta)$$
 - magnitude measurable through oscillation frequency:
$$\Delta M_s = \Delta M_s^{\text{SM}} |\Delta_s|$$