

# The SiPM Physics and Technology

## - a Review -

**G.Collazuol**

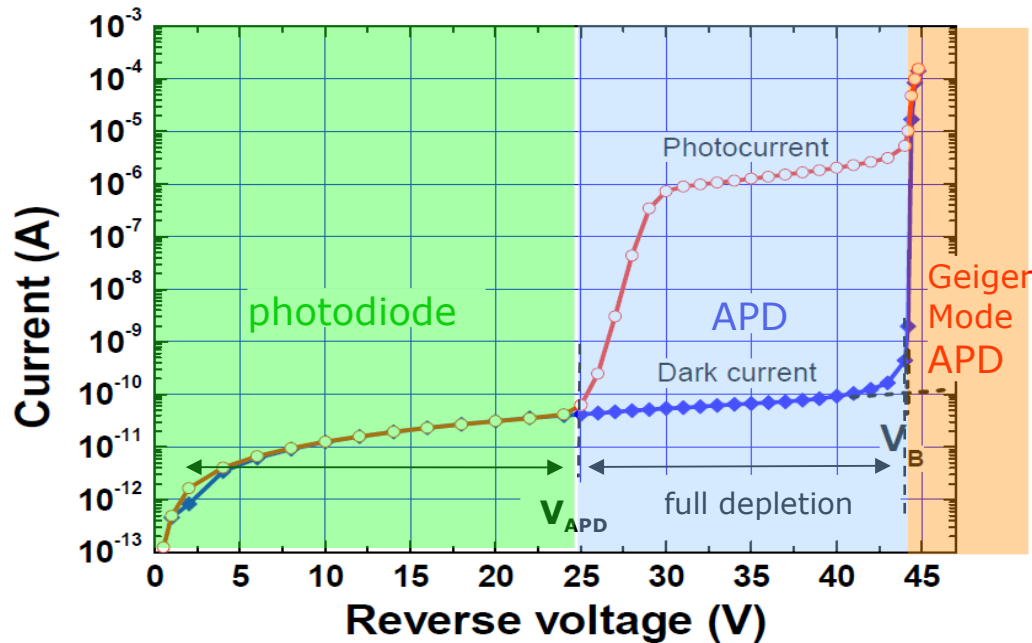
Department of Physics and Astronomy, University of Padova and INFN

### Overview

- Introduction
  - Key physics and technology features
    - I-V characteristics
      - Device response
        - Noises
          - Photo-detection efficiency
          - Timing properties
          - Summary and Future

# The silicon PM: array of GM-APD

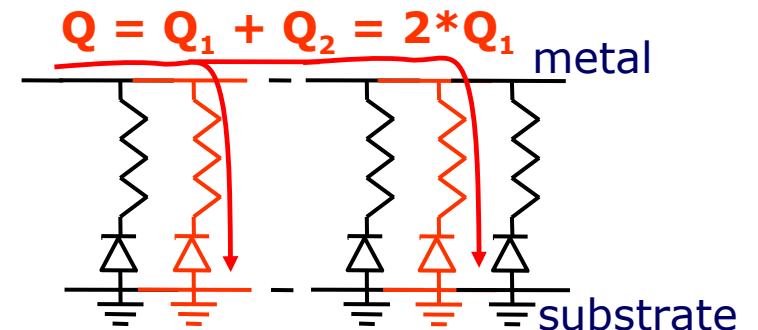
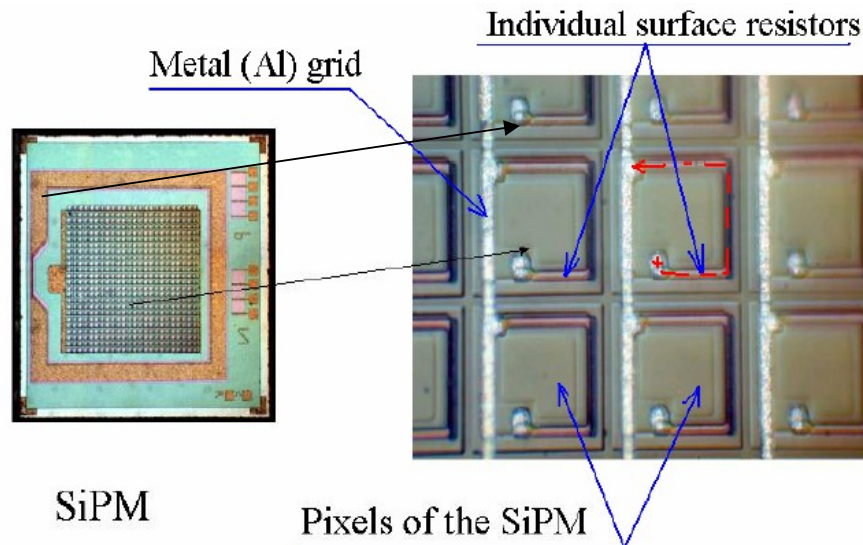
Single GM-APD gives no information on light intensity → **MATRIX structure** first proposed in the late '80-ies by **Golovin and Sadygov**



A SiPM is segmented in tiny GM-APD cells and connected in parallel through a **decoupling resistor**, which is also used for **quenching** avalanches in the cells

Each element is independent and gives the same signal when fired by a photon

In principle output charge is **proportional** to the number of of incident photons



$\Sigma$  digital signals → analog signal !!!

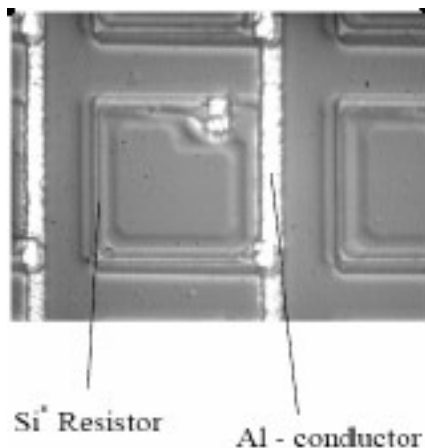
# A bit of history

## Pioneering work since late 80-ies at Russian institutes

Investigations of various multi-layer silicon structures with local micro-plasma suppression effect to develop low-cost GM-APD arrays

Early devices ageing quickly, unstable, noisy

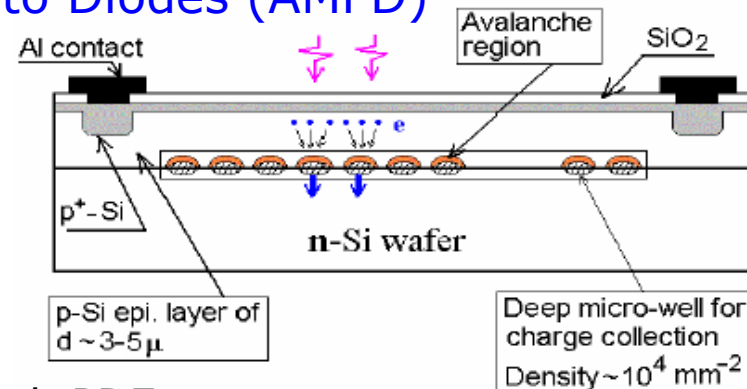
## Dolgoshein - MePhi/Pulsar (Moscow) Poly-silicon resistor



- Low fill-factor
- Simple fabrication technology

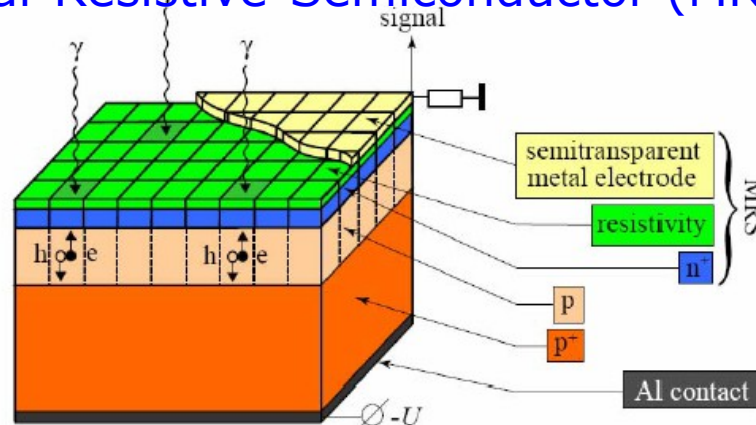
*e.g., Dolgoshein, NIMA 563 (2006)*

## Sadygov - JINR/Micron (Dubna) Avalanche Micro-channel/pixel Photo Diodes (AMPD)



- high PDE
- very high density of micro-cells  
*eg Sadygov, NIMA 567 (2006)*

## Golovin - Obninsk/CPTA (Moscow) Metal-Resistive-Semiconductor (MRS)



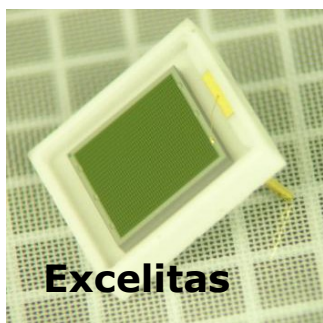
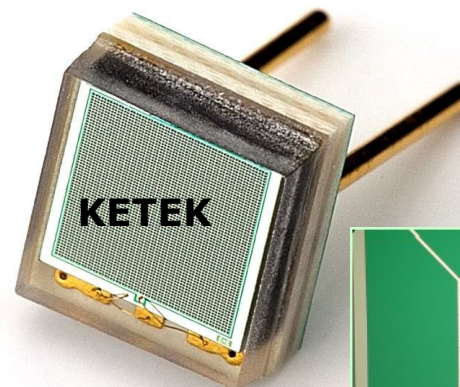
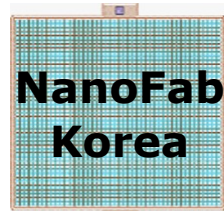
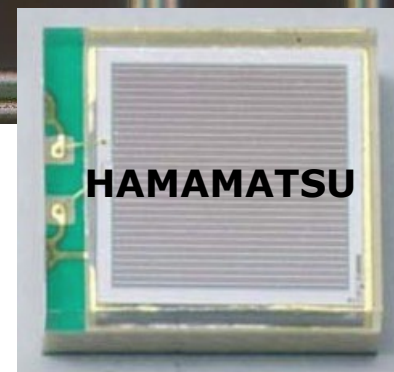
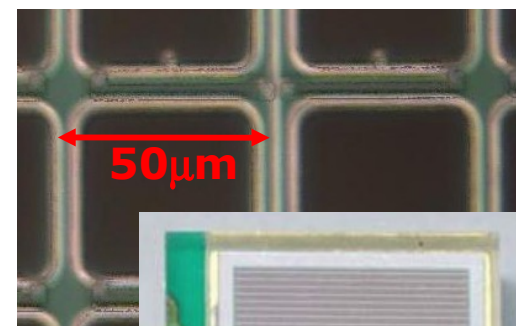
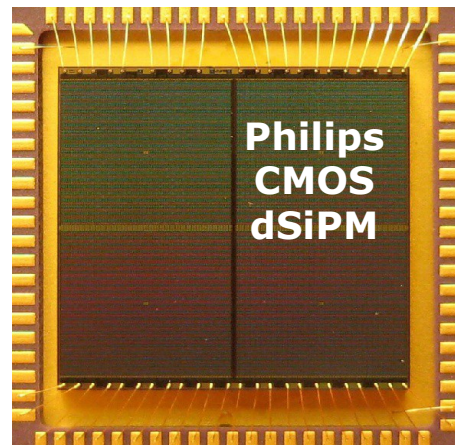
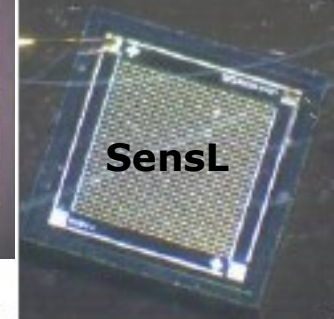
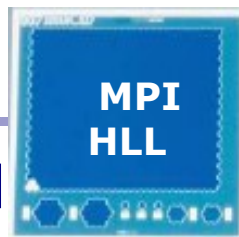
- High fill factor
- Good pixel to pixel uniformity

*e.g., Golovin  
NIMA 539 (2005)*

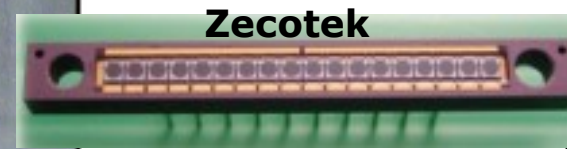
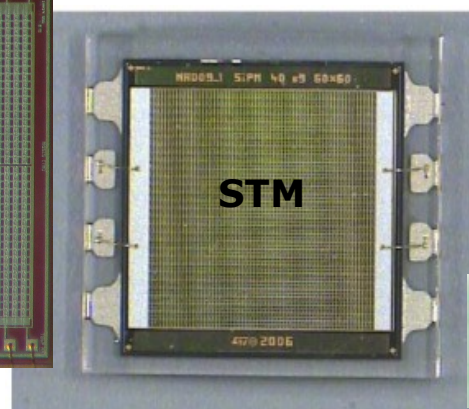
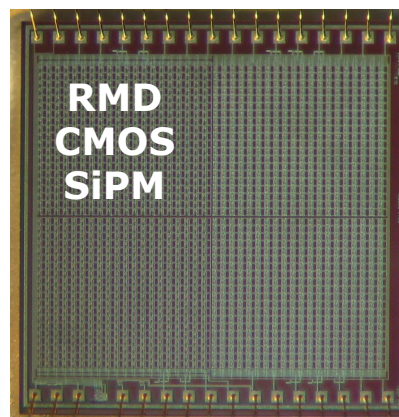
# Today


Many institutes/companies are involved in SiPM development/production:

- **CPTA**, Moscow, Russia
- **MePhi/Pulsar Enterprise**, Moscow, Russia
- **Zecotek**, Vancouver, Canada
- **Hamamatsu HPK**, Hamamatsu, Japan
- **FBK-AdvanSiD**, Trento, Italy
- **ST Microelectronics**, Catania, Italy
- **Amplification Technologies** Orlando, USA
- **SensL**, Cork, Ireland
- **MPI-HLL**, Munich, Germany
- **RMD**, Boston, USA
- **Philips**, Aachen, Germany
- **Excelitas tech.** (formerly Perkin-Elmer)
- **KETEK**, Munich, Germany
- **National Nano Fab Center**, Korea
- **Novel Device Laboratory (NDL)**, Beijing, China
- **E2V**
- **CSEM**



**Amplification Technologies (DAPD)**





# Physics & Technology

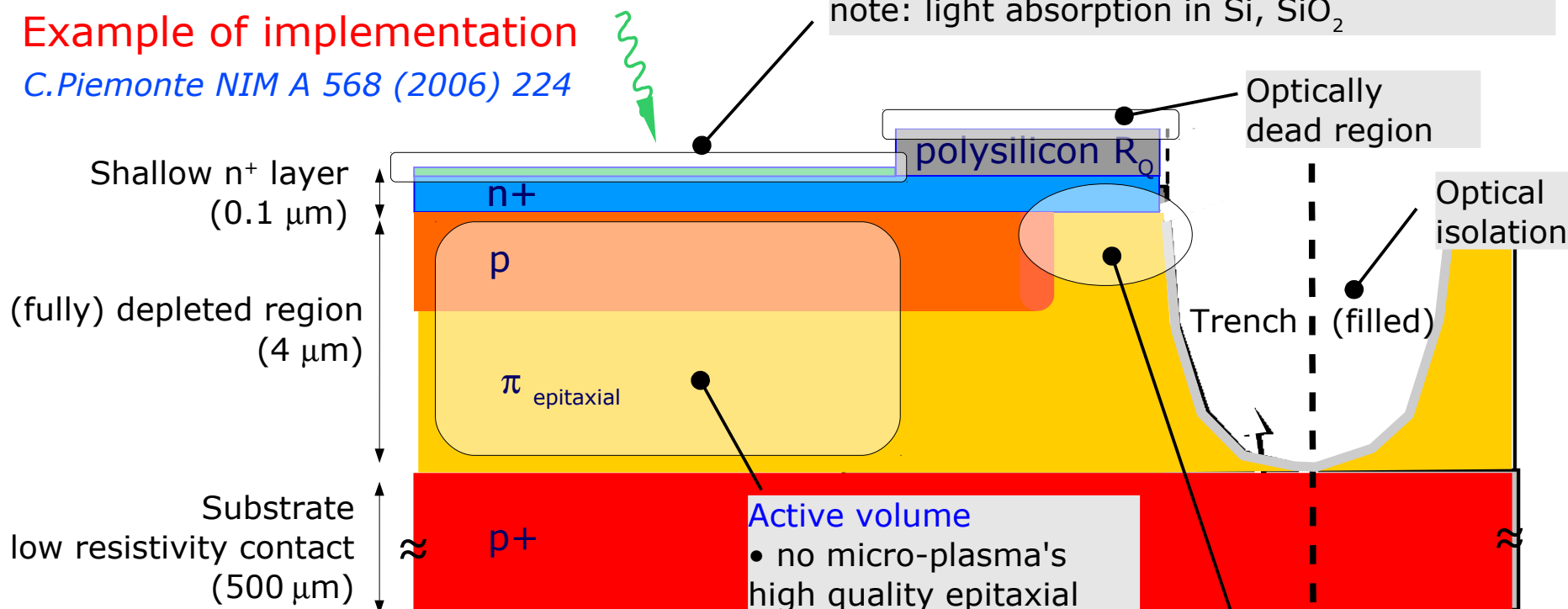
## Key features

- Closeup of a cell – Custom vs CMOS
- Guard Ring and Optical isolation
- Operation principles of GM-APD and quenching modes

# Close up of a cell – custom process

## Shallow-Junction APD Example of implementation *C.Piemonte NIM A 568 (2006) 224*

Optical window  
note: light absorption in Si, SiO<sub>2</sub>



**Active volume**  
 • no micro-plasma's  
 high quality epitaxial  
 doping / E field profile  
 engineering

**Critical region:**

- Leakage current
- Surface charges
- **Guard Ring** for
  - preventing early edge-breakdown
  - isolating cells
  - tuning E field shape

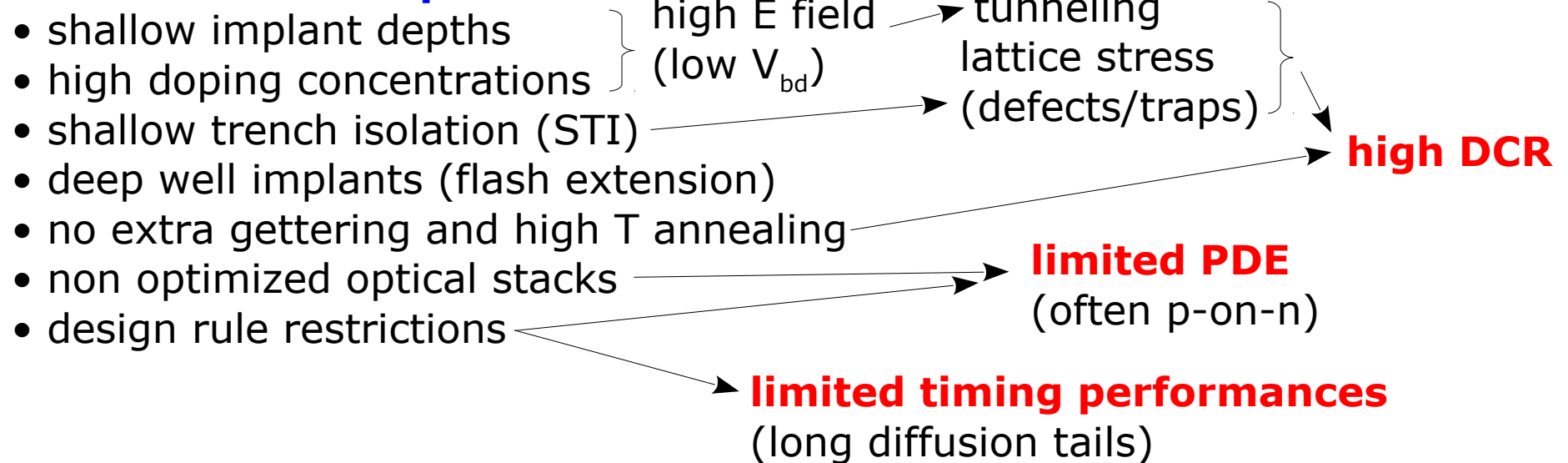
→ impact on Fill Factor

Optimization for  
blue light (420nm)

- n<sup>+</sup> on p abrupt junction structure
- Anti-reflective coating (ARC)
- **Very thin (100nm) n<sup>+</sup> layer:** "low" doping  
→ minimize Auger and SHR recombination
- **Thin high-field region:** "high" doping p layer  
→ limited by tunneling breakdown  
→ fixes V<sub>BD</sub> junction well below V<sub>BD</sub> at edge
- R<sub>Q</sub> by poly-silicon
- Trenches for optical insulation (**cross-talk**)
- Fill factor: 20% - 80%

# CMOS vs Custom processes

## “Standard” CMOS processes



**Recent progresses** in CMOS APDs due to:

- 1) **high voltage (flash) extension** often available in **standard** processes
  - deep wells (needed for the high voltages used in flash memories)
- 2) **Additional processes** (custom) available:
  - buried implants
  - deep trench isolation
  - optical stack optimization

### Key elements for CMOS SiPMs

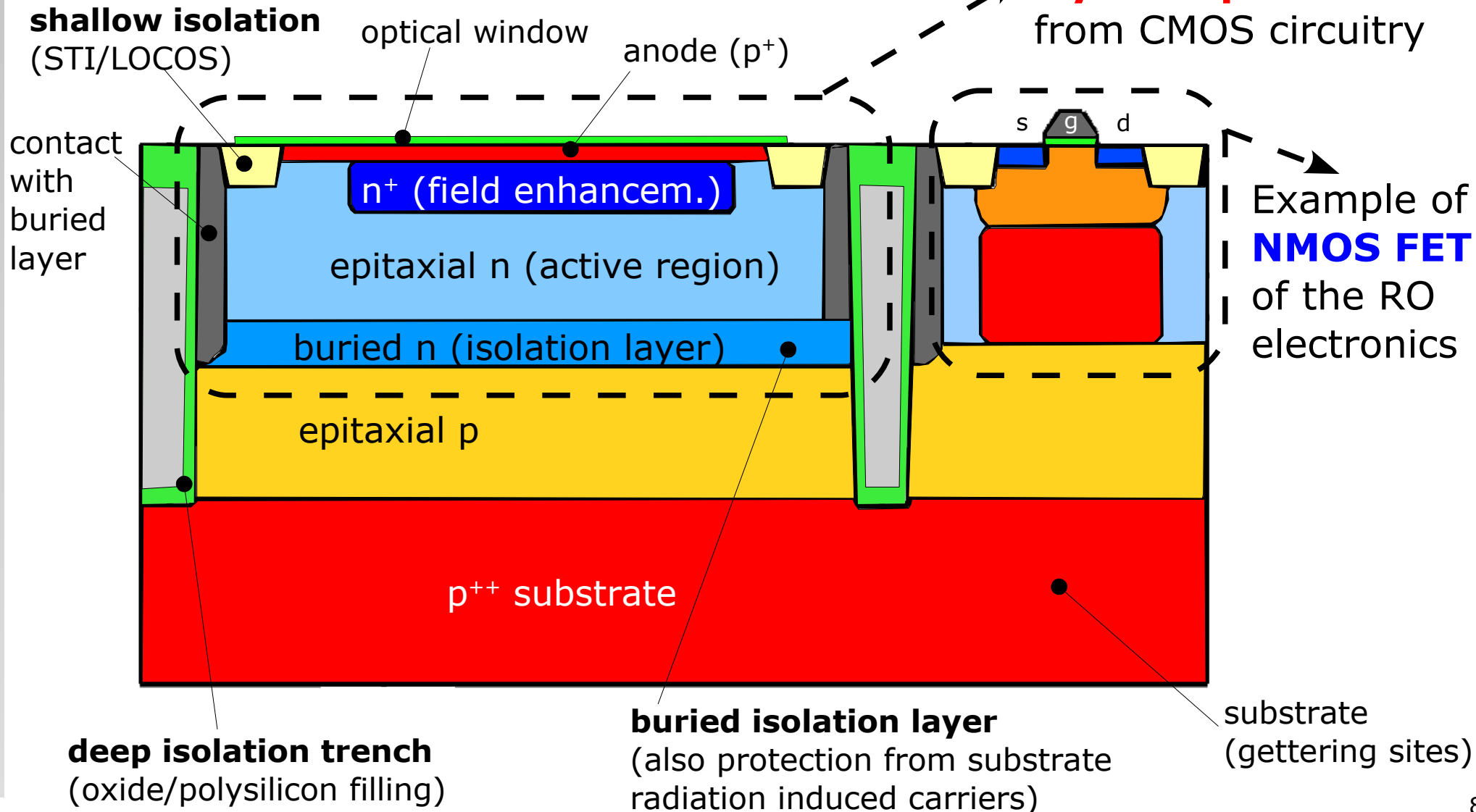
- **APD cell isolation** from CMOS circuitry
- **guard ring** (again)

# Close up of a CMOS cell

## APD integration into CMOS

Example of implementation *T.Frach in US patent 2010/0127314*

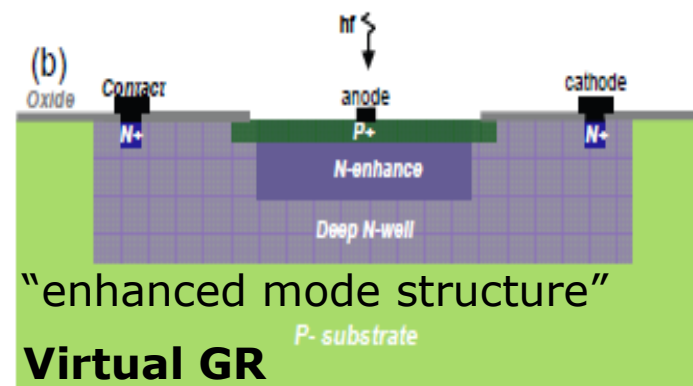
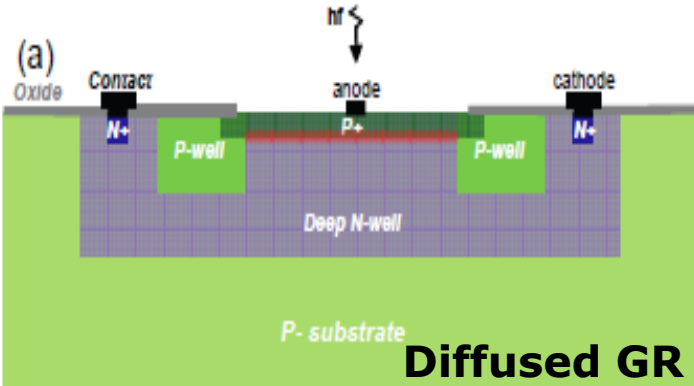
- Note
- extended CMOS processes exploited
  - careful design of cell isolation and guard ring



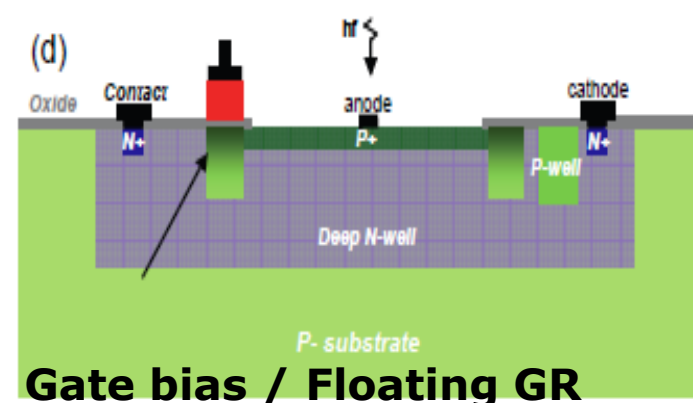
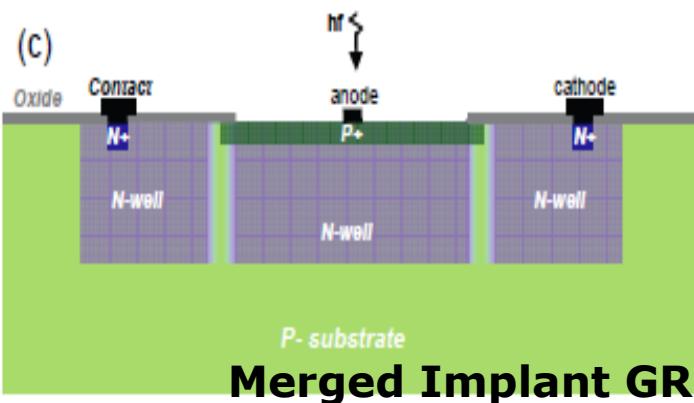


# The Guard Ring structure

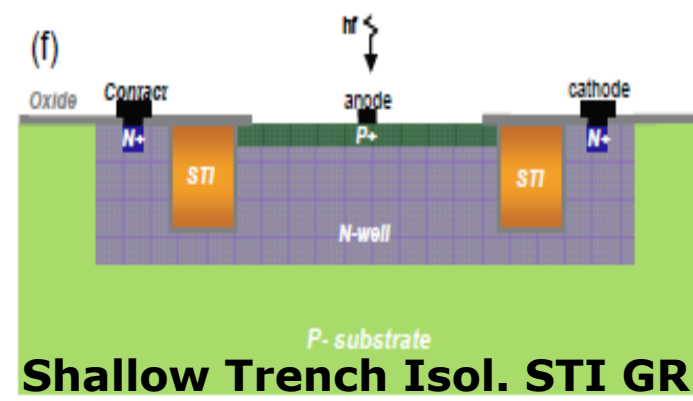
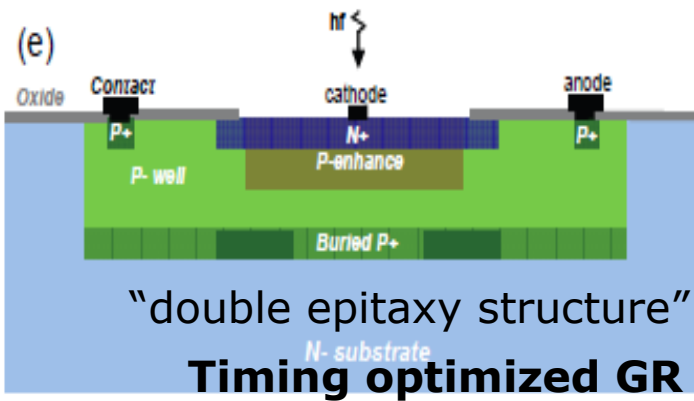
- high E field structure, not uniform



- well tuned high E field structure
- no additional neutral regions
- fill factor less limited



- less commonly exploited
- careful modeling required



- physically blocks and confines the high E field in active region
- might cause high DCR due to
  - tunneling
  - etching induced defects/traps

- neutral region (timing tails)

- limited fill factor

- alternative to Diffused GR

- difficult to implement

- developed by S.Cova and coll. (fully custom)

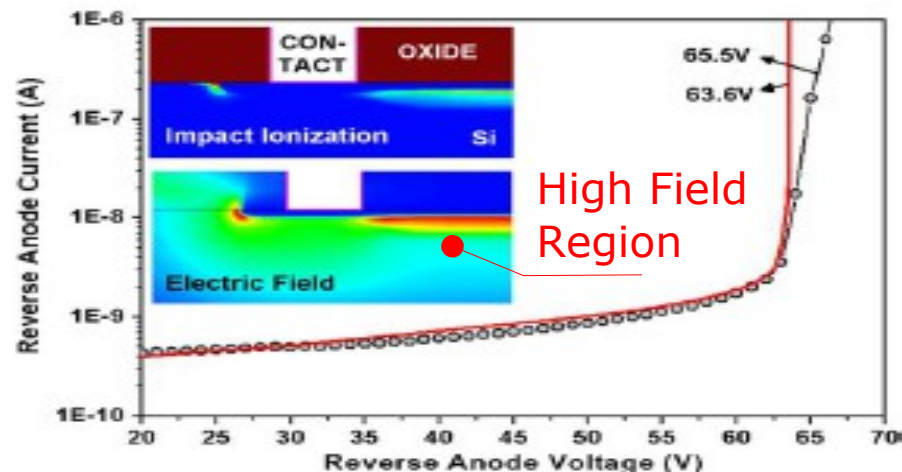
- state of the art SPAD timing and PDE (red enhanced)

from "Avalanches in Photodiodes" G.F.Dalla Betta Ed., InTech Pub. (2011)

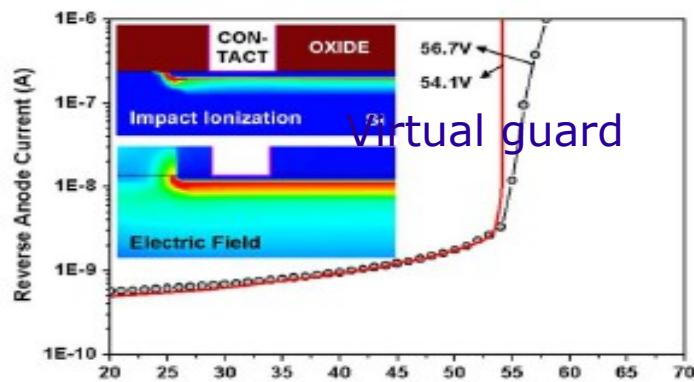
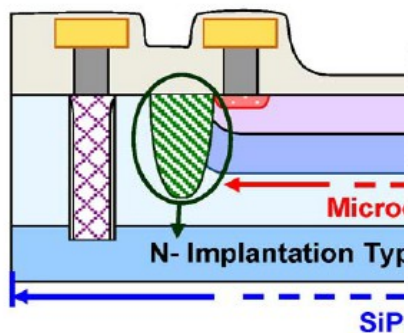
# Guard Ring structures in SiPM

Sul et al, IEEE EDL 31 2010 "G.R. Structures for SiPM"

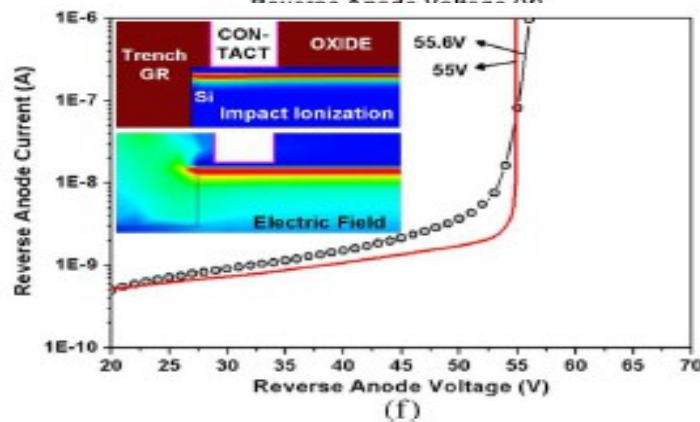
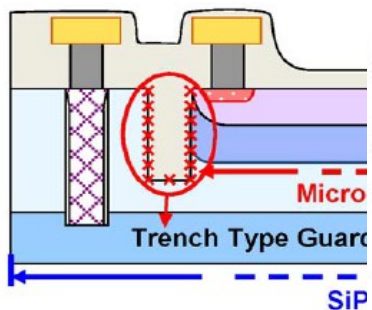
Virtual guard ring most often used



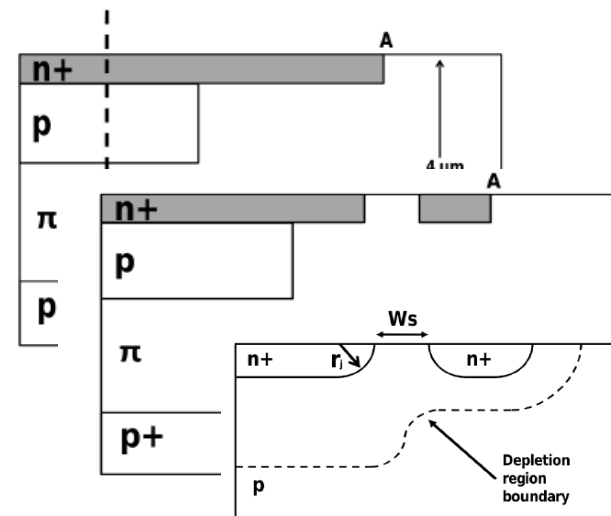
Implant / Gate bias



Trench type



Maresca et al. Proc. of SPIE Vol. 8072 "Floating field ring ... to enhance fill factor of SiPM"



# Operation principle of a GM-APD

Avalanche processes in semiconductors are studied in detail since the '60 for modeling micro-plasma instabilities

*McIntyre JAP 32 (1961), Haitz JAP 35 (1964) and Ruegg IEEE TED 14 (1967)*

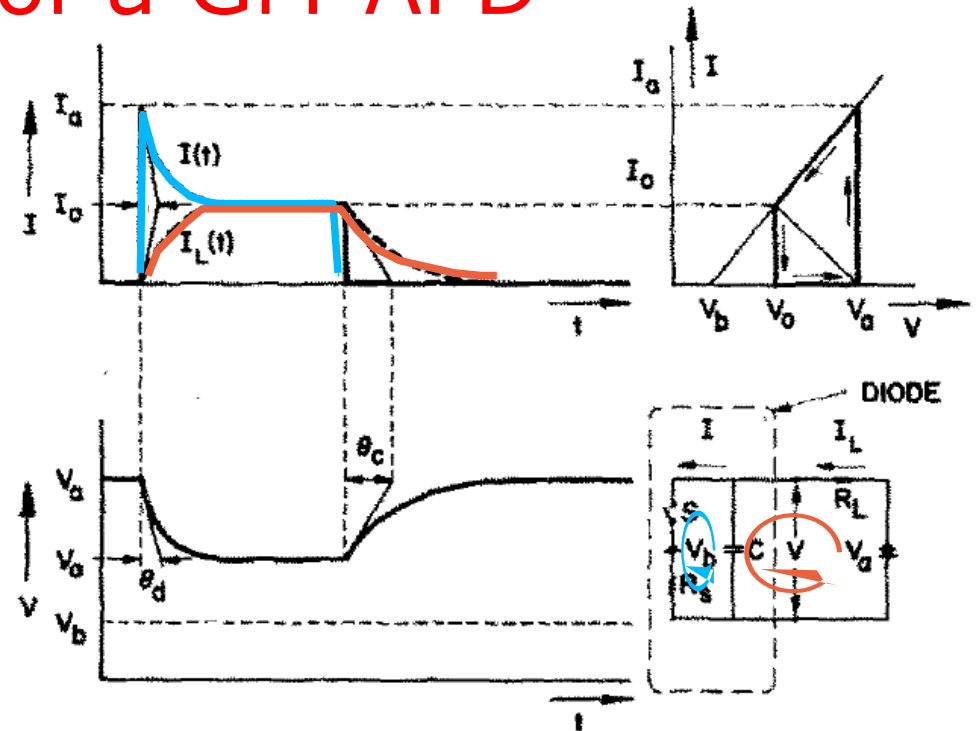
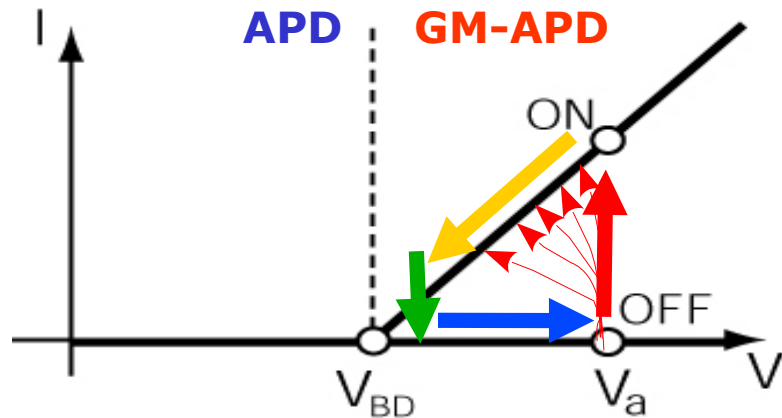


FIG. 3. Shape of current pulse for  $\theta_d \ll \tau_{r1}(I_0)$ .

**OFF condition:** avalanche quenched, switch open, capacitance charged until no current flowing from  $V_{bd}$  to  $V_{BIAS}$  with time constant  $R_q \times C_d = \tau_{quenching}$  ( $\rightarrow$  recovery time)

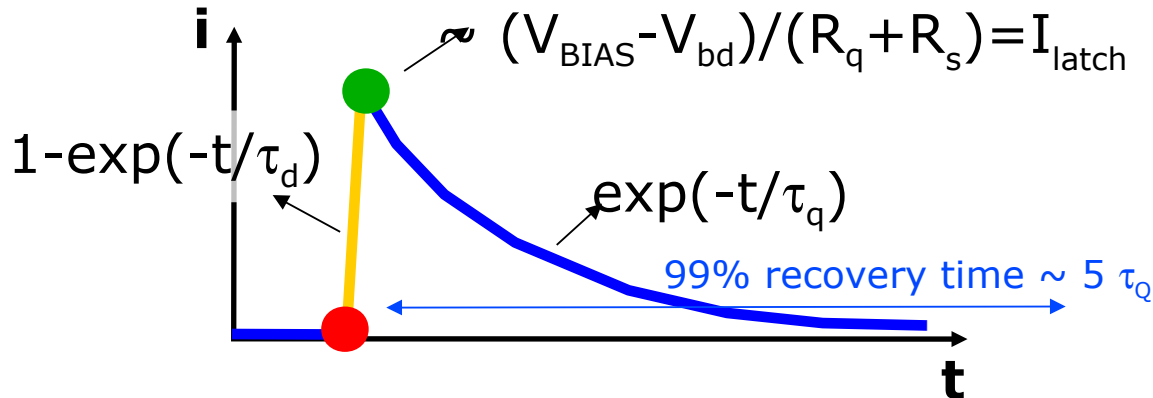
$P_{01}$  = turn-on probability  
probability that a carrier traversing the high-field region triggers the avalanche

$P_{10}$  = turn-off probability  
probability that the number of carriers traversing the high-field region fluctuates to 0

**ON condition:** avalanche triggered, switch closed  $C_d$  discharges to  $V_{bd}$  with a time constant  $R_d \times C_d = \tau_{discharge}$ , at the same time the external current asymptotic grows to  $(V_{bias} - V_{bd}) / (R_q + R_d)$

# Passive Quenching

If  $R_Q$  is high enough the internal current is so low that statistical fluctuations may quench the avalanche



The leading edge of the signal is much faster than trailing edge:

1.  $\tau_d = R_s C_d \ll R_q C_d = \tau_q$
2. turn-off mean time is very short (if  $R_q$  is sufficiently high,  $I_{\text{latch}} \sim 20 \mu\text{A}$ )

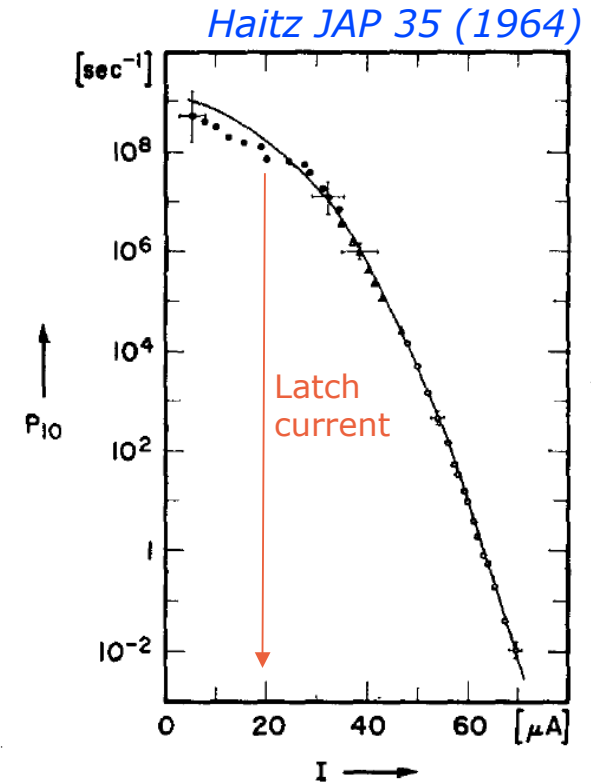


FIG. 2. Turnoff probability per second as function of pulse current.

The charge collected per event is the **area under the exponential** which is determined by circuital elements and bias.

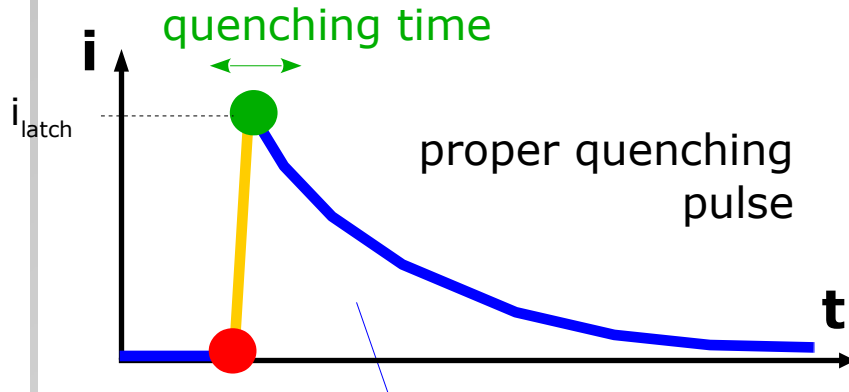
➡ It is possible to **define a GAIN** (discharge of a capacitor)

$$G = \frac{I_{\text{max}} \cdot \tau_q}{q_e} = \frac{(V_{\text{bias}} - V_{\text{bd}}) \cdot \tau_q}{(R_q + R_s) \cdot q_e} = \frac{(V_{\text{bias}} - V_{\text{bd}}) \cdot C_d}{q_e}$$

➡ Gain **fluctuations** in GM-APD are **smaller than in APD** essentially because electrons and holes give the same signal

# Passive Quenching Regime

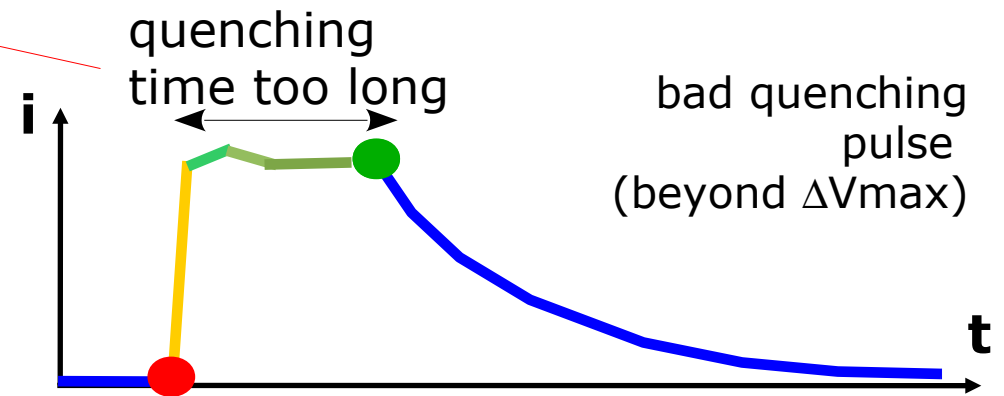
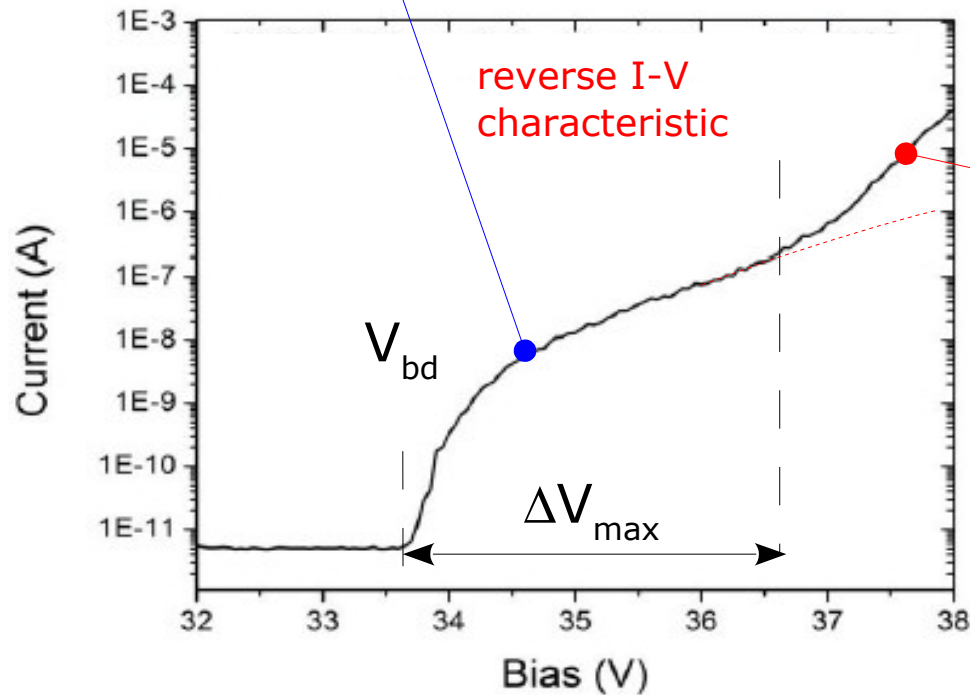
Proper value of quenching resistance  $R_q$  is crucial to let the internal current decrease to a level such that **statistical fluctuations may quench the avalanche**  
 → sub-ns quenching time → crucial to have **well defined gain**



Given  $R_q$  the proper quenching regime is for  $\Delta V$  in the range:

$$0 < \Delta V < R_q I_{latch}$$

where as a rule of thumb  
 $I_{latch} \sim 20\mu A \rightarrow \Delta V_{max} \sim$  a few Volts (typically)



# Operative $\Delta V$ Range - $I_{\text{dark}}/\text{DCR}$

Operative  $\Delta V$  limited by:

- 1)  $I_{\text{latch}} \sim 20\mu\text{A} \rightarrow \Delta V < I_{\text{latch}} R_q$  (non-quenching regime)
- 2) Dark Count Rate (DCR) acceptable level  $\leftarrow$  PDE vs  $\Delta V \leftarrow$  E field shape
- 3)  $V_{\text{bd}}^{\text{edge}}$  edge breakdown (usually some 10V above  $V_{\text{bd}}$ )

A practical method for estimating the operative range (limited by effect 1) is to measure the ratio  $R_I$  of the measured dark current  $I_D$  to the dark current  $I'_D$  calculated from the measured dark rate and pixel count spectra:

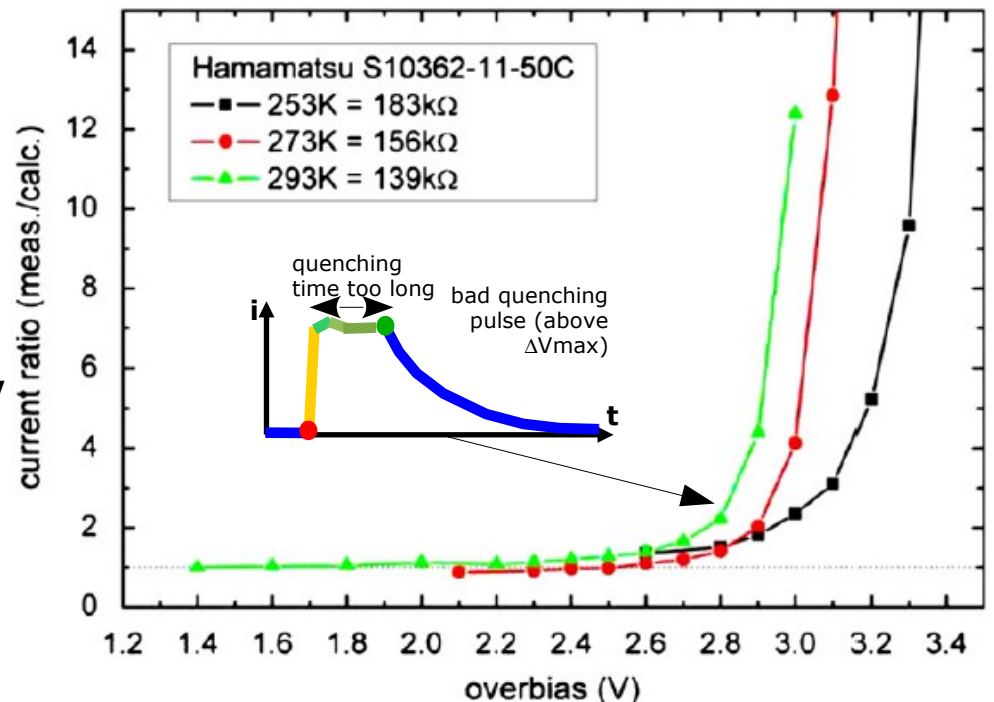
$$R_I = \frac{I_D}{I'_D = \text{DCR} \cdot \bar{N} \cdot G \cdot q_e}$$

where  $\bar{N}$  is the average  $N$  of fired cells

Non-quenching regime for values of  $\Delta V$  when  $R_I$  deviates significantly from 1

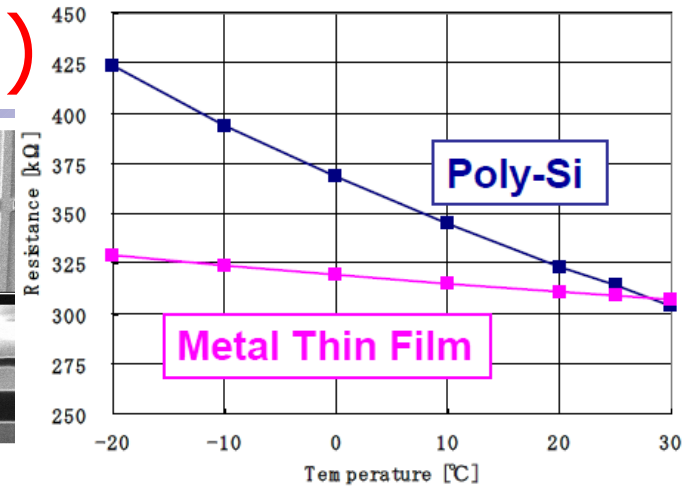
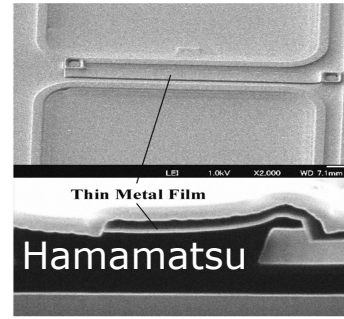
Jendrysik et al suggest  $R_I=2$  as reasonable threshold

after Jendrysik et al NIM A 2011  
doi:10.1016/j.nima.2011.10.007



# Passive Quenching (Resistive)

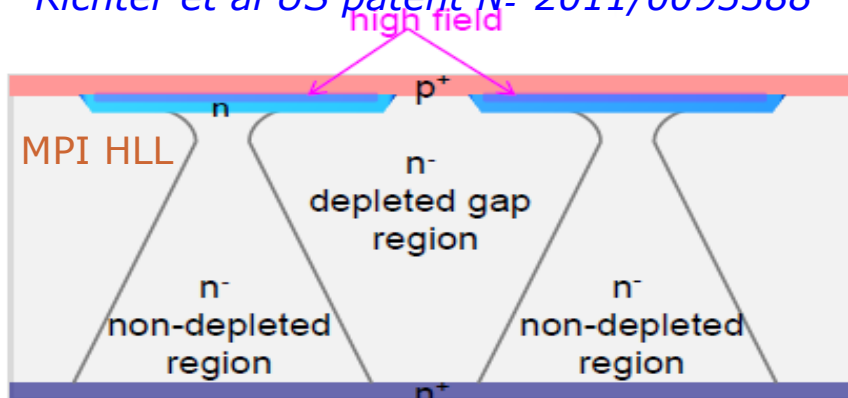
- 1) common solution: poly-silicon
- 2) alternative: metal thin film
  - higher fill factor
  - milder T dependence
- 3) alternative principle: bulk integrate resistor
  - flat optical window → simpler ARC
  - fully active entrance window
    - high fill factor (constraints only from guard ring and X-talk)
  - diffusion barrier against minorities
    - less X-talk
  - positive T coeff. ( $R \sim T^{+2.4}$ )
  - production process simplified → cost



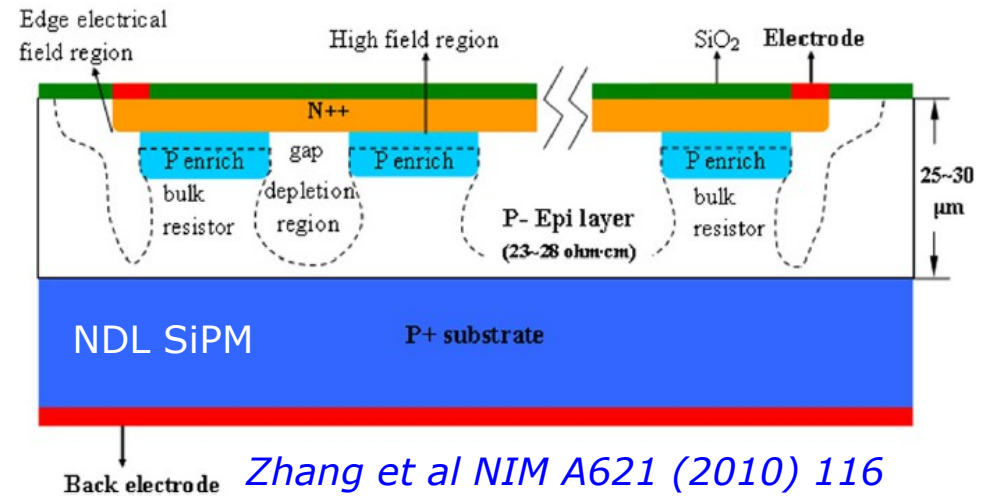
Nagano IEEE NSS-MIC 2011

- pro
  - ← Rq matching constraints
  - cells' pitch/wafer thickness
- contra
  - ← vertical R is JFET
  - non-linear I-V
  - long recovery

Ninkovic et al NIM A610 (2009) 142  
 and NIM A628 (2011) 407  
 Richter et al US patent N° 2011/0095388



principle proved



Zhang et al NIM A621 (2010) 116

# Passive Quenching (Capacitive)

Quenching feedback due to charge accumulated by means by semiconductor barriers

AmplificationTechnologies

Shushakov et al US Patents

Nº 2004/6885827 and Nº 2011/7899339

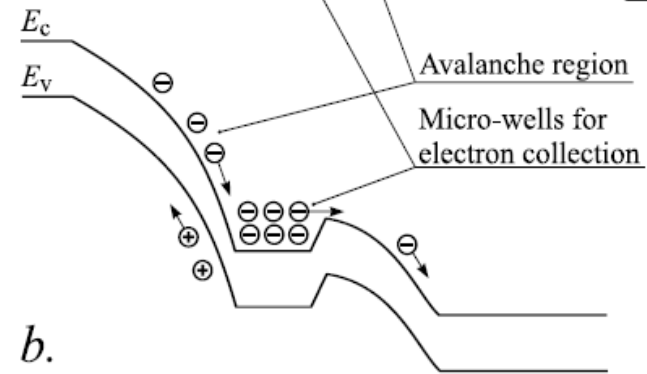
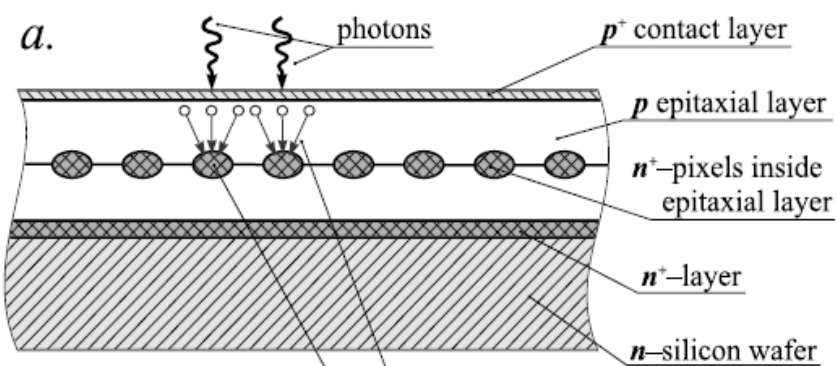
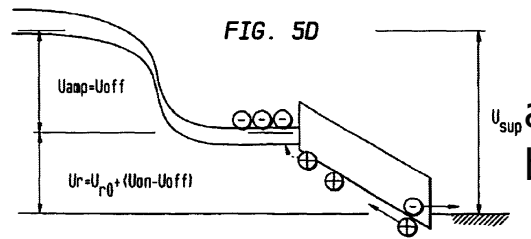
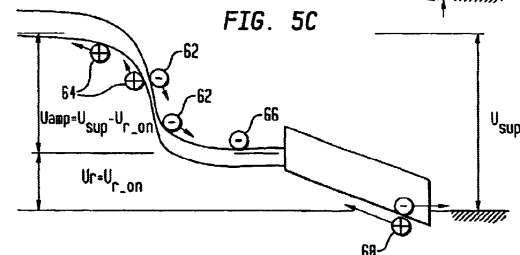
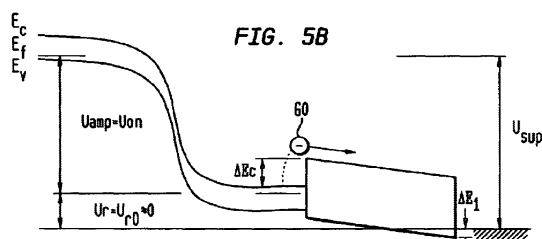
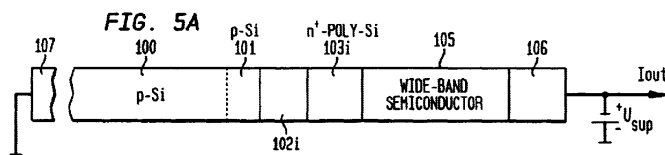
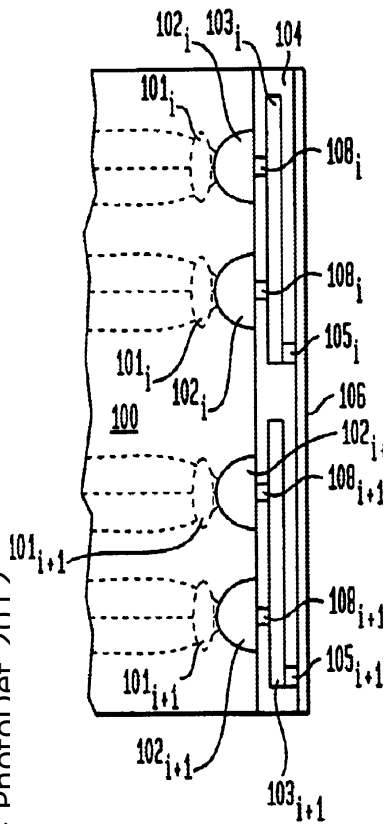
Zecotek

Sadygov et al arXiv 1001.3050

Sadygov RU Patents Nº 1996/2102820

and Nº 2006/2316848

FIG. 3

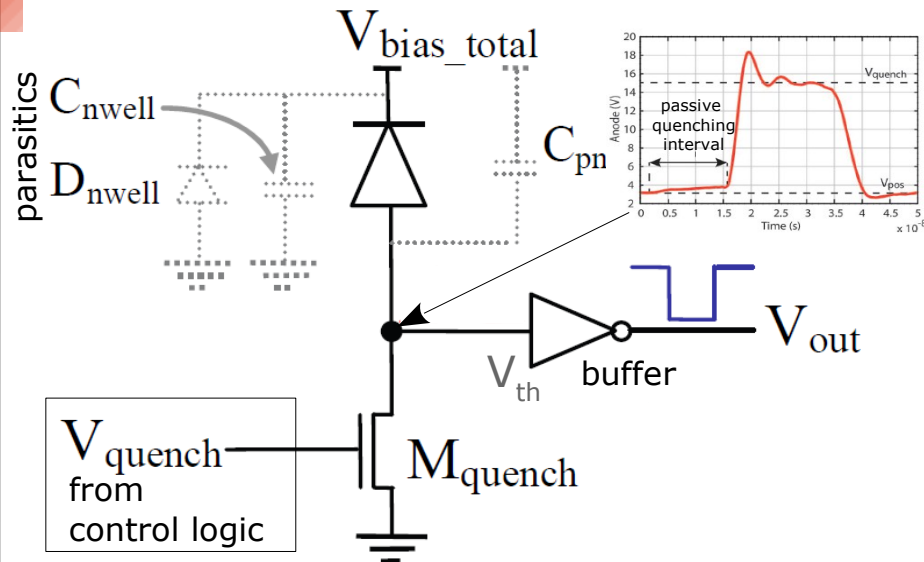


- a) avalanche at internal high field regions
- b) charges accumulated in isolated potential wells
  - E field reduced (locally) → avalanche quenched
  - Fast signal induced (capacitive) outside
- c) potential wells discharge slowly by tunneling (discharge must be delayed for good quenching)
  - high E field recovered

Note: induced signal is fast (ns) but recovery quite slow (ms) (non exponential)



# Active Quenching



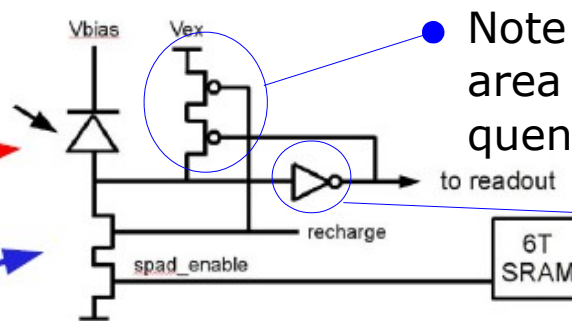
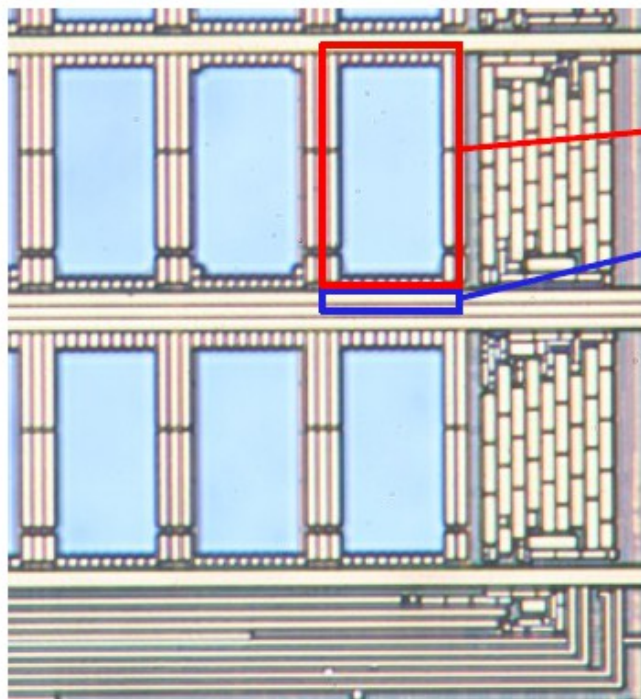
## Basic circuit elements:

- 1) quench circuit to **detect and stop** the avalanche and **restore bias conditions**
- 2) buffer (low capacitive load) for isolating the APD from the **external electronics capacitance**

Configuration with anode to ground potential is best: only  $C_{det}$  is involved  $\rightarrow$  minimum RC load

- $\rightarrow$  **minimum quenching dead-time**
- $\rightarrow$  **minimum charge flow in APD** (less after-pulses)

(in addition n-well regions (cathode) can be shared among many cells)



Note: use of PMOS to minimize the area wrt NMOS for the same target quenching resistance

buffer  $\rightarrow$  simple inverter as input signal is already digital

## dSiPM cell electronics

- Cell electronics area:  $120\mu\text{m}^2$
- 25 transistors including 6T SRAM
- $\sim 6\%$  of total cell area
- Modified  $0.18\mu\text{m}$  5M CMOS
- Foundry: NXP Nijmegen

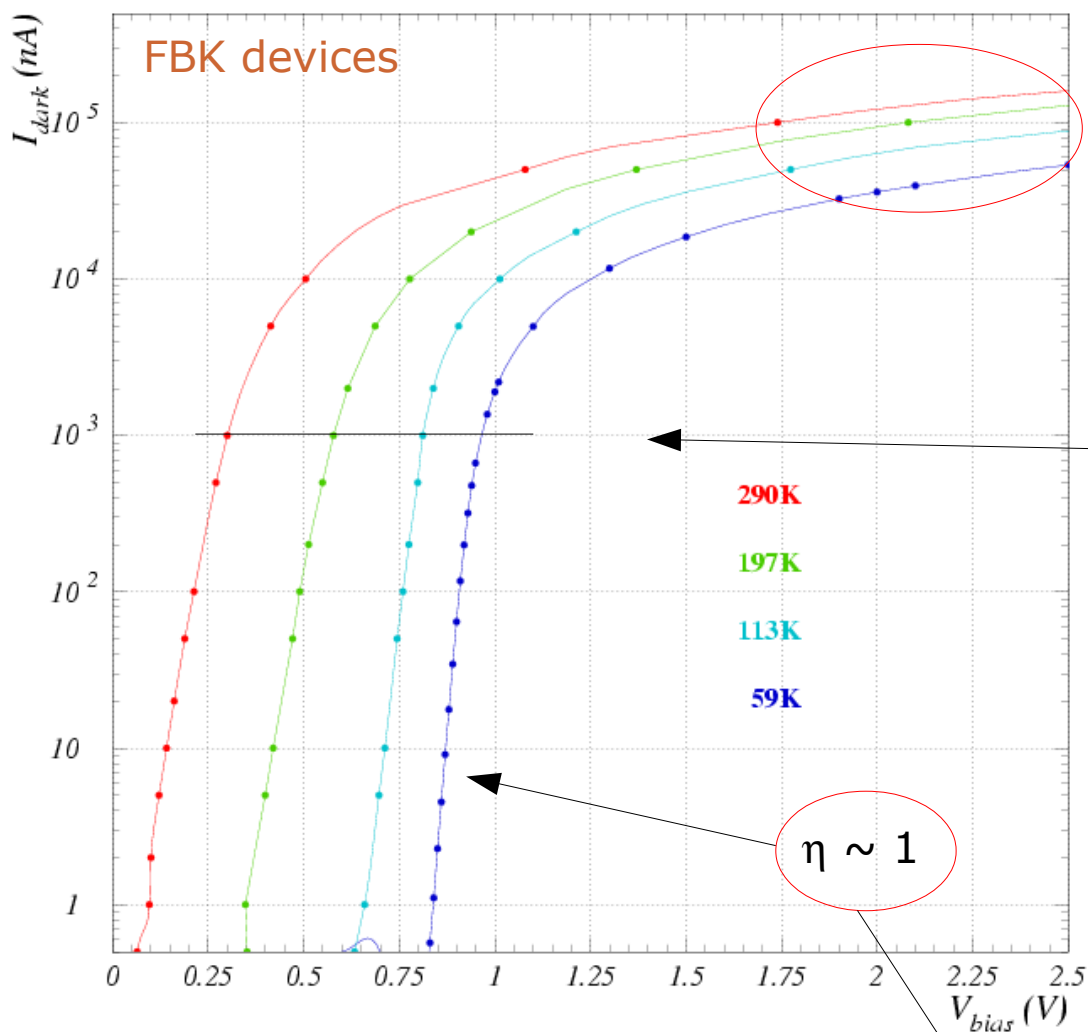
- Cell area  $\sim 30 \times 50\mu\text{m}^2$
- Fill Factor  $\sim 50\%$

*T.Frach at LIGHT 2011*

# I-V characteristics

- Information from Forward current →
  - $R_q$
  - junction Temperature
  - ...
- Information from Reverse current →
  - breakdown  $V_{bd}$
  - T coefficient
  - ...

# I-V characterization: forward bias



③ **Ohmic** behavior at high current

Linear fit  $\rightarrow R_{series} \sim R_q / N_{cells}$

② **Voltage drop** ( $V_d$ ) decreases linearly with T decreasing (e.g. at  $1\mu A$ )

① **Forward current**

$$I_{forward} \sim C(\eta) A(T) \left[ \exp\left(\frac{qV_d}{\eta kT}\right) - 1 \right]$$

*Shockley et al. Proc. IRE 45 (1957)*

$\eta$  ideality factor

Diffusion current dominating:  $\eta \rightarrow 1$

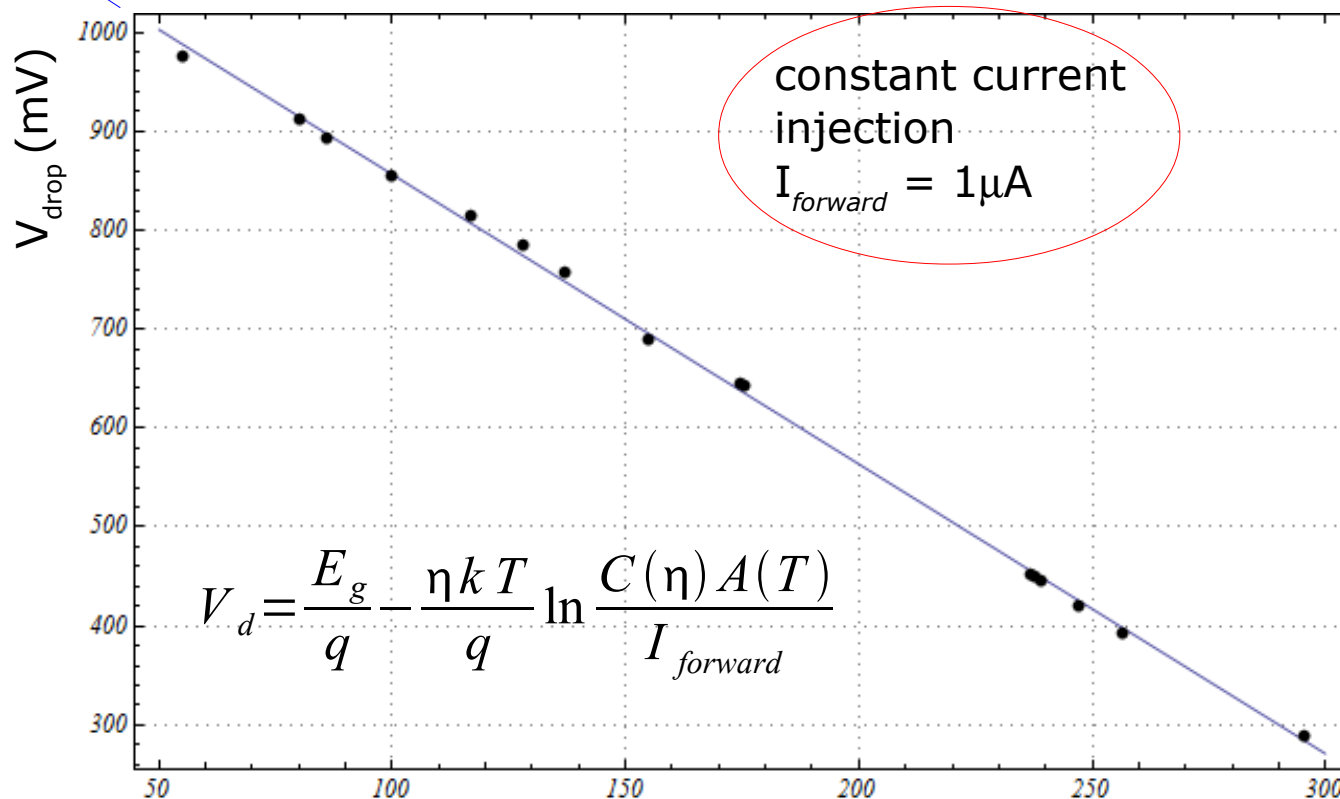
Recombination current dominating:  $\eta \rightarrow 2$

# Forward I-V → Junction Temperature probe

Voltage drop at fixed forward current → precise **measurement of junction T...**

for  $T \rightarrow 0$  ideally  $V_d \rightarrow E_g$   
(freeze-out effects apart)

... otherwise not trivially measured !

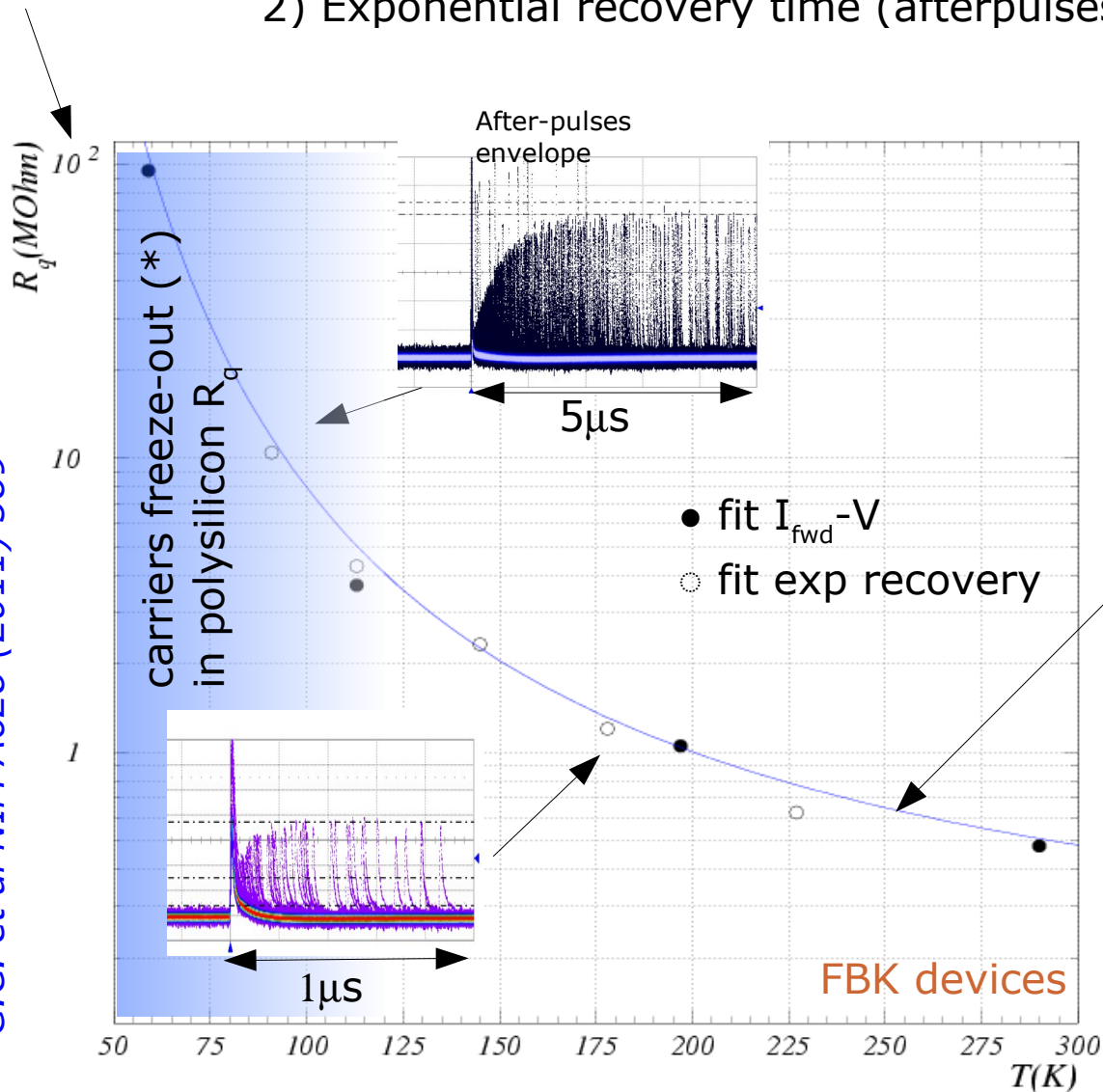


- (almost) linear dependence with slope  $dV_{drop}/dT|_{1\mu A} \sim -3mV/K^T$  (K)  
(we don't see freeze-out effects down to 50K )
- direct and precise **calibration/probe** of junction(s) Temperature

# Forward I-V → Series Resistance (vs T)

## Two ways for measuring series resistance ( $R_s$ )

- 1) Fit at high V of forward characteristic
- 2) Exponential recovery time (afterpulses envelope)

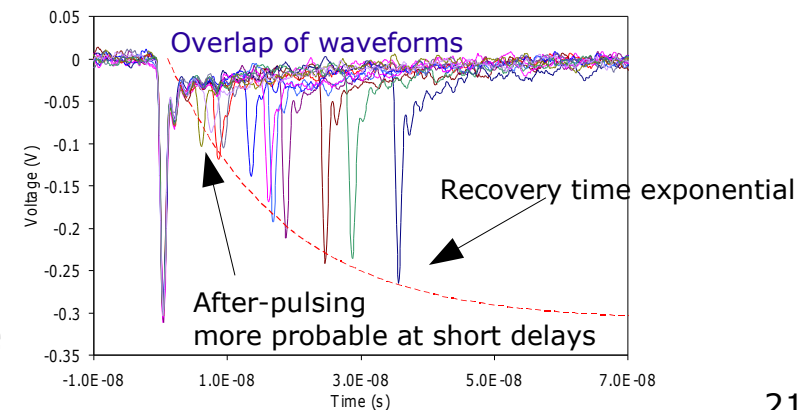


Measurements (1) and (2) consistent  
→ **dominant effect from quenching resistor  $R_q$**   
(→ series R bulk gives smaller contribution)

Empirical fit:

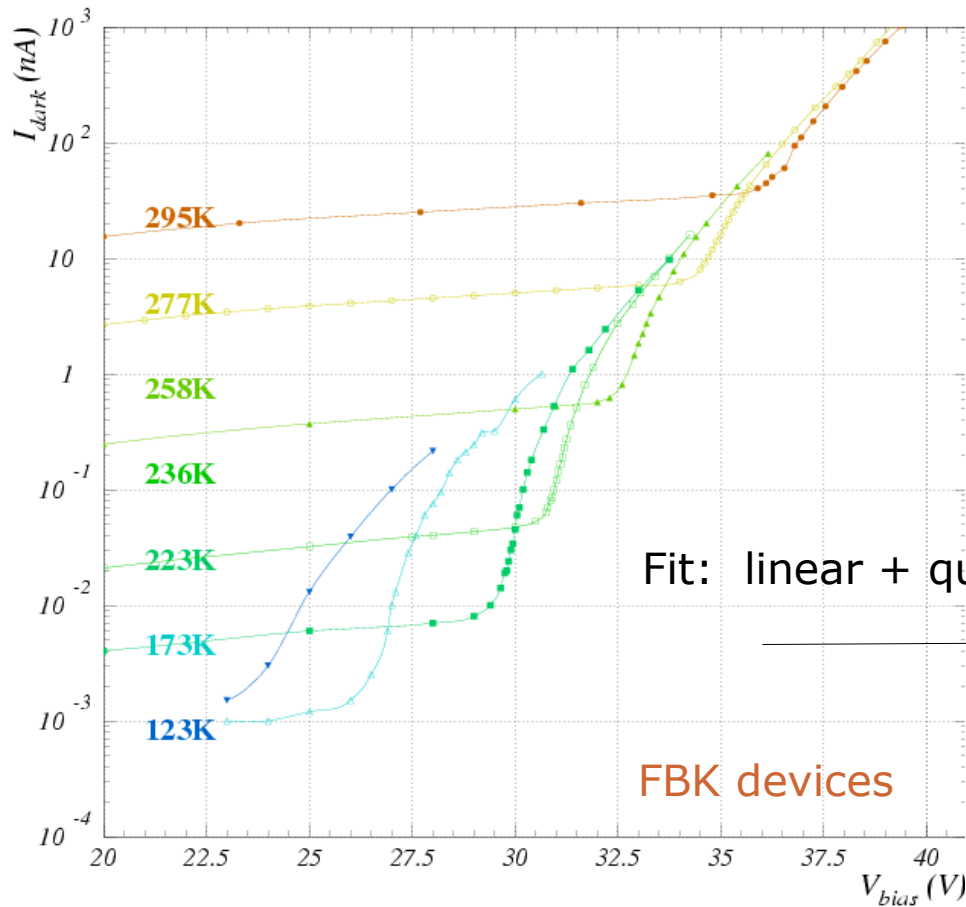
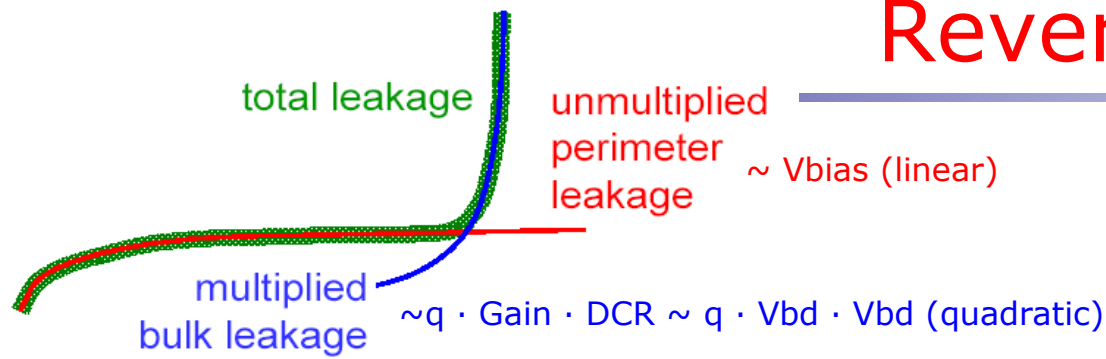
$$R_q(T) \sim 0.13 (1 + 300/T e^{300/T}) M \Omega$$

## Afterpulses envelope

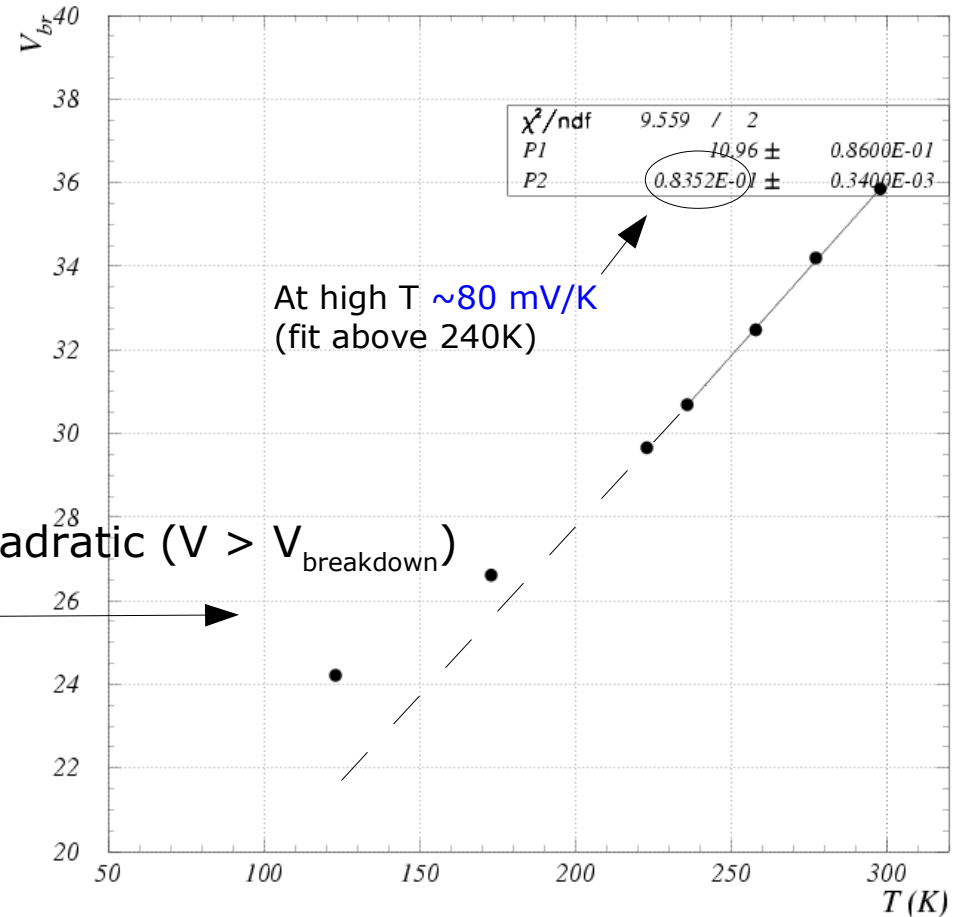


Note: SiPM for low T applications must have appropriate quenching R (not quenching at room T !)

# Reverse I-V



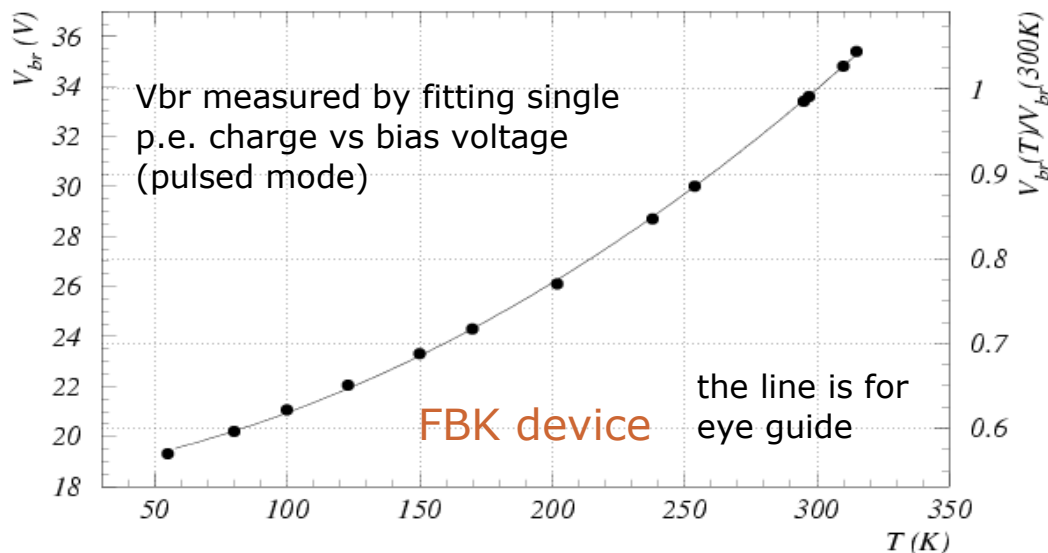
$V_{bd}$  dependence on T



Breakdown voltage decreases at low T due to larger carriers mobility  
 → larger ionization rate (electric E field fixed)

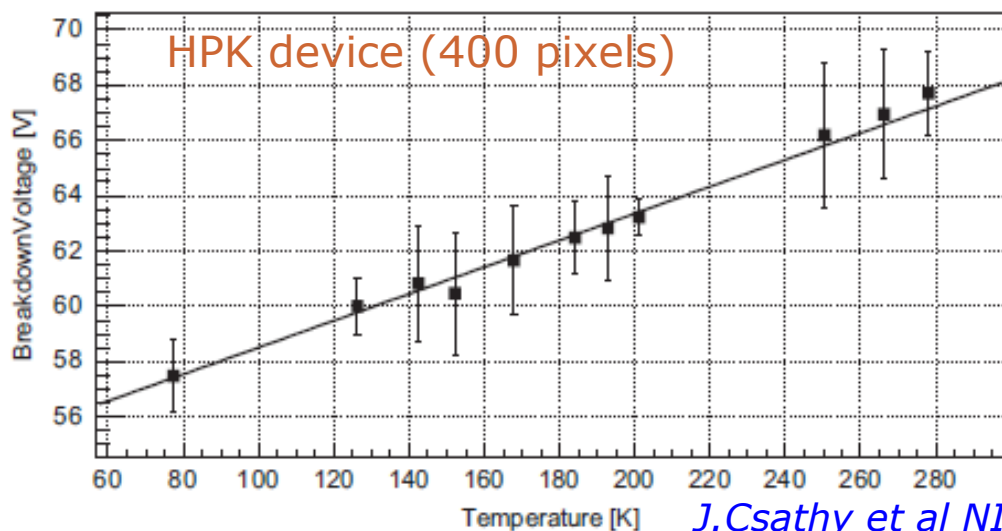
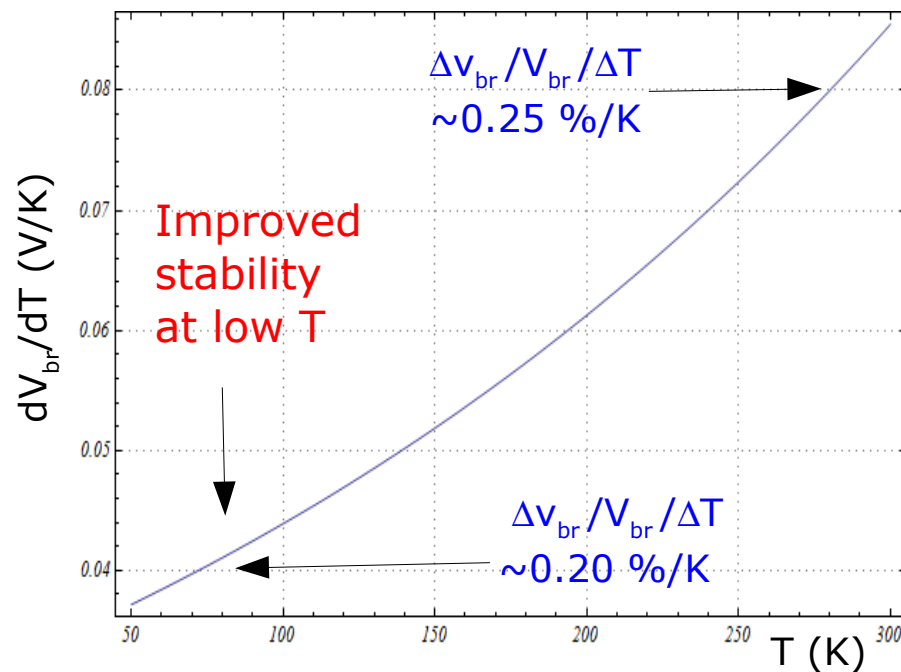
# $V_{bd}$ vs $T \rightarrow T$ coefficient ( $\Delta V$ stability)

## Breakdown Voltage



*G.C. et al NIM A628 (2011) 389*

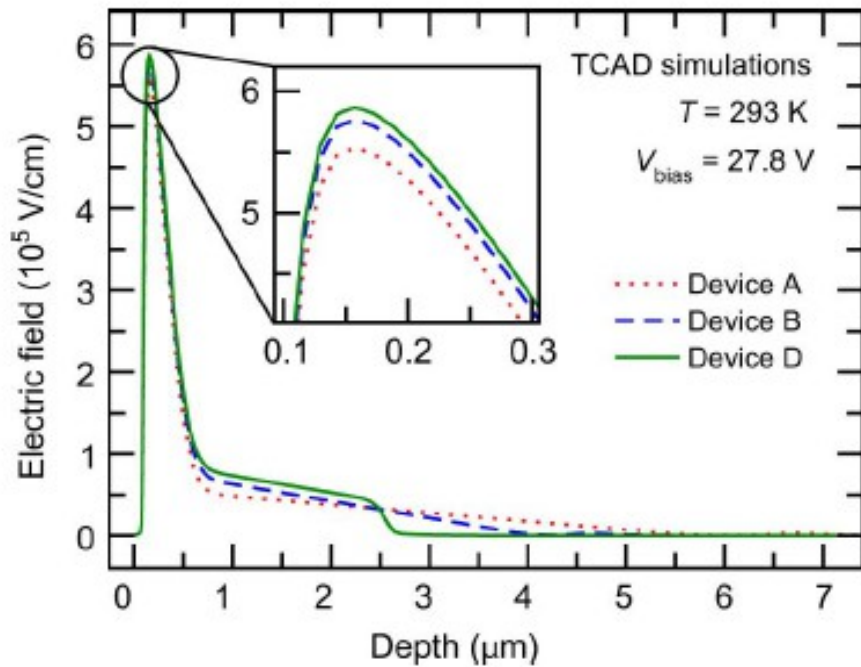
## Temperature coefficient



*J.Csathy et al NIM A 654 (2011) 225*

Fig. 6. Breakdown voltage as a function of temperature of the MPPC with 400 pixels.

# Depletion layer $\rightarrow V_{bd}$ dependence on T



Serra et. al. (FBK) IEEE TNS 58 (2011) 1233  
 "Experimental and TCAD Study of Breakdown Voltage Temperature Behavior in n+/p SiPMs"

Note: precise agreement simulation/data is not trivial at all. Definition of ionization coefficients is device dependent...

Narrow depletion layer (high background doping(\*) or thin epitaxial layer)

$\rightarrow$  minimize  $V_{bd}$  dependence on T

$\rightarrow$  gain stability  $\frac{\delta V_{bd}/V_{bd}}{\delta T} = \frac{\delta G/G}{\delta T}$

(\*) resulting in epitaxial layer not fully depleted at  $V_{bd}$

Trade off:

$\rightarrow$  PDE (thickness)

$\rightarrow$  minimum gain (capacity) against after-pulses and cross-talk

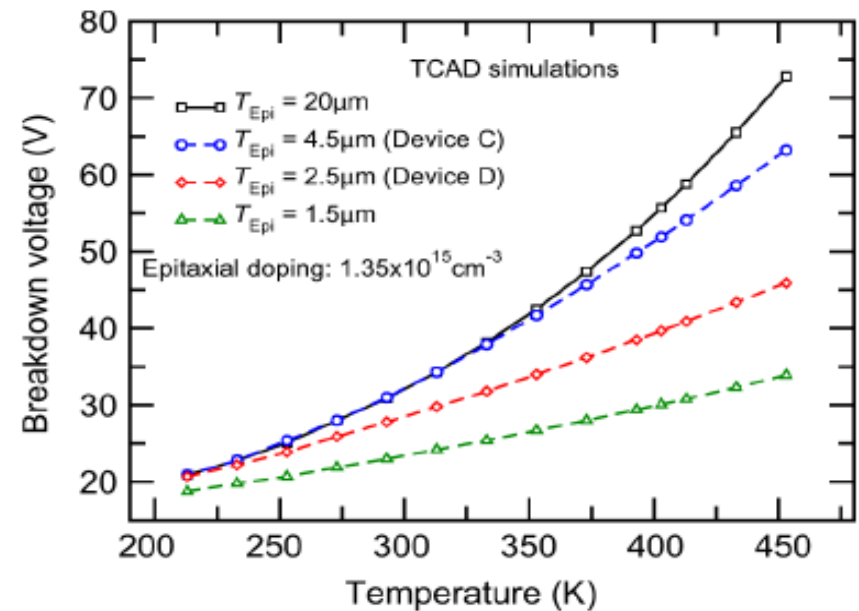


Fig. 9. TCAD simulated  $V_{BD}$  in the GM-APDs of this work (see Table I) in an extended temperature range. Two additional epitaxial layer thickness are considered ( $20 \mu\text{m}$ ,  $1.5 \mu\text{m}$ ) to emphasize the impact of the depletion layer width on the  $V_{BD}$  vs. temperature characteristic.





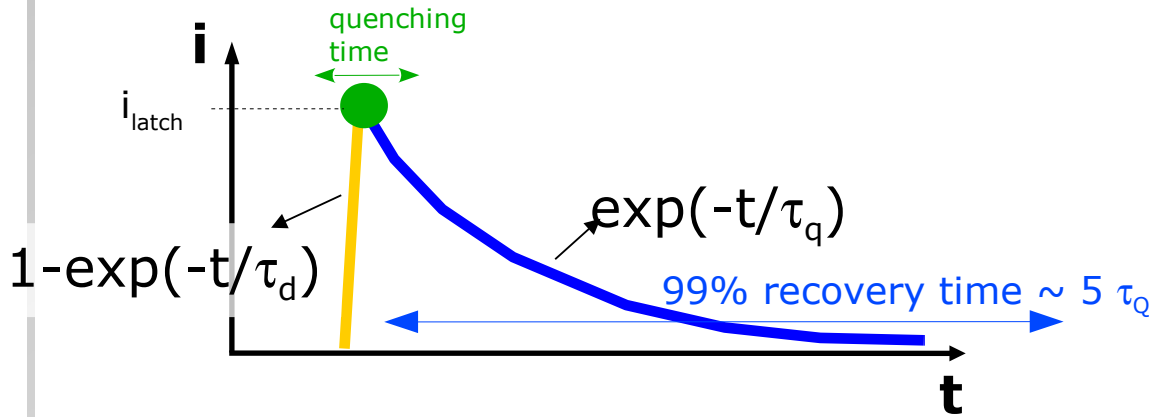
# Pulse shape, Gain and Response

- Detailed electrical model
- Pulse shape
- Gain and Gain fluctuation
- Response non-linearity

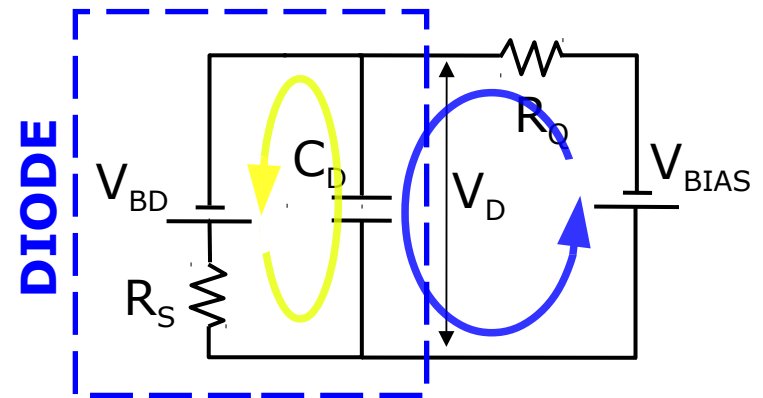
(mostly for passive mode)

# Basic electrical model

Fast Capacitor (cell) discharge and slow recharge (roughly speaking)



currents **internal** / **external**



Rise time  $\tau_d = R_d C_d$   $\ll$  Fall time (recovery)  $\tau_q = R_q C_d$

**Recovery time:** T dependence due to  $R_q$   
 $C_d$  is independent of T

**Rise time:** T dependent (to lesser extent) due to  $R_d$

**Gain  $\sim C \Delta V \rightarrow$  independent of T**  
 at fixed Over-Voltage ( $\Delta V = V_{bias} - V_{bd}$ )

# SiPM equivalent circuit (detailed model)

Single cell model  $\rightarrow (R_d || C_d) + (R_q || C_q)$

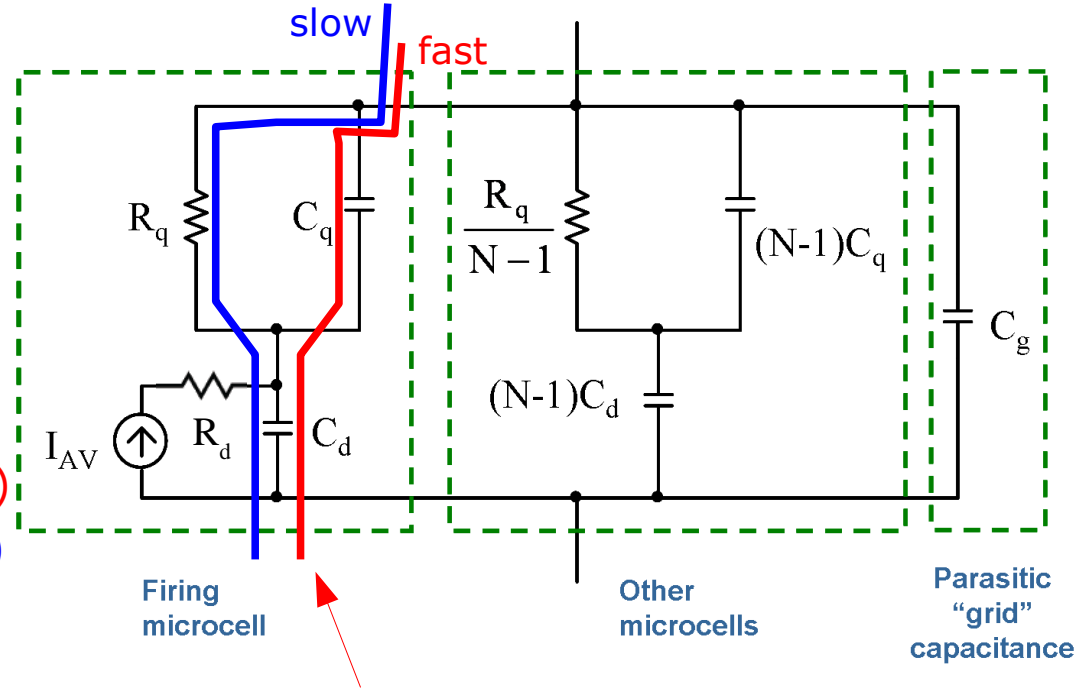
SiPM + load  $\rightarrow (||Z_{cell}) || C_{grid} + Z_{load}$

Signal = **slow** pulse ( $\tau_{d (rise)}, \tau_{slow (fall)}$ ) +  
+ **fast** pulse ( $\tau_{d (rise)}, \tau_{fast (fall)}$ )

- $\tau_{d (rise)} \sim R_d (C_q + C_d)$
- $\tau_{fast (fall)} = R_{load} C_{tot}$  (fast; parasitic spike)
- $\tau_{slow (fall)} = R_q (C_q + C_d)$  (slow; cell recovery)

*F.Corsi, et al. NIM A572 (2007) 416*

*S.Seifert et al. IEEE TNS 56 (2009) 3726*



**Cq  $\rightarrow$  fast current supply path in the beginning of avalanche**

## Pulse shape

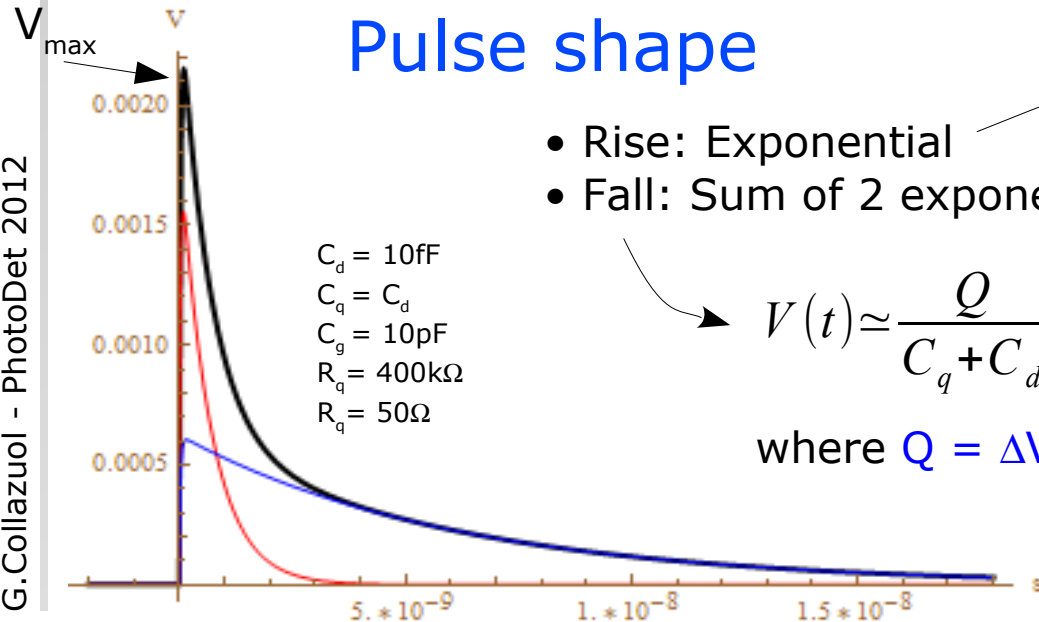
- Rise: Exponential
- Fall: Sum of 2 exponentials

Sp.Charge  $R_d \times C_d, q$  filtered by parasitic inductance, stray C, ... (Low Pass)

$$V(t) \approx \frac{Q}{C_q + C_d} \left( \frac{C_q}{C_{tot}} e^{-\frac{t}{\tau_{FAST}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{-\frac{t}{\tau_{SLOW}}} \right) \quad \text{for } R_{load} \ll R_q$$

where  $Q = \Delta V (C_q + C_d)$  is the total charge released by the cell

$\rightarrow$  'prompt' charge on  $C_{tot}$  is  $Q_{fast} = Q \frac{C_q}{(C_q + C_d)}$



# Pulse shape

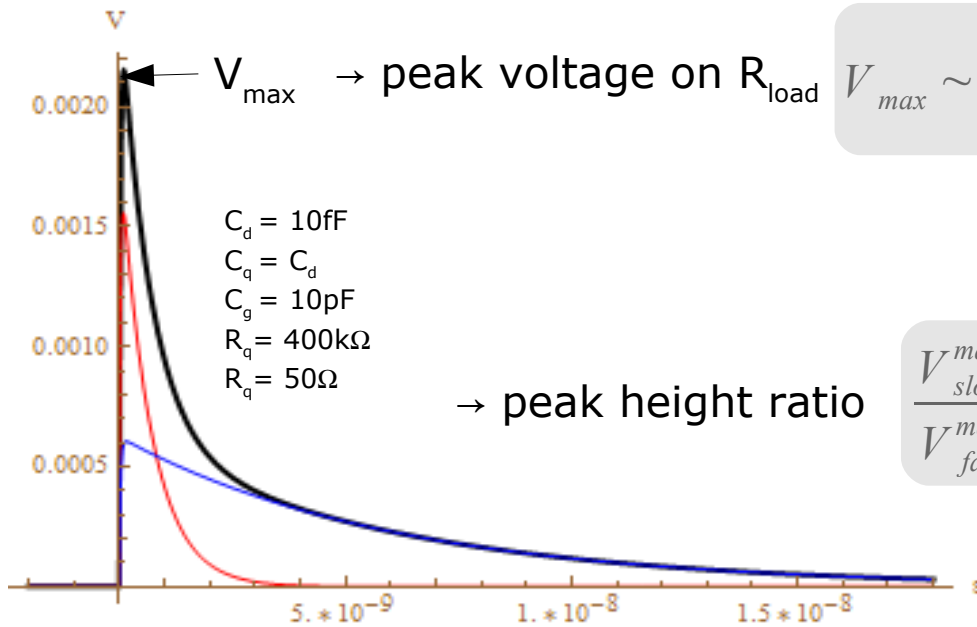
$$V(t) \simeq \frac{Q}{C_q + C_d} \left( \frac{C_q}{C_{tot}} e^{\frac{-t}{\tau_{fast}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{\frac{-t}{\tau_{slow}}} \right) = \frac{Q R_{load}}{C_q + C_d} \left( \frac{C_q}{\tau_{fast}} e^{\frac{-t}{\tau_{fast}}} + \frac{C_d}{\tau_{slow}} e^{\frac{-t}{\tau_{slow}}} \right)$$

→ gain  $G = \int dt \frac{V(t)}{q_e R_{load}} = Q/q_e = \frac{\Delta V (C_d + C_q)}{q_e}$  independent of  $R_q$

→ charge ratio  $\frac{Q_{slow}}{Q_{fast}} \sim \frac{C_d}{C_q}$

Note: valid for low impedance load  $R_{load} \ll R_q$

- $\tau_{fast} = R_{load} C_{tot}$
- $\tau_{slow} = R_q (C_q + C_d)$



$V_{max}$  → peak voltage on  $R_{load}$

$$V_{max} \sim R_{load} \left( \frac{Q_{fast}}{\tau_{fast}} + \frac{Q_{slow}}{\tau_{slow}} \right)$$

dependent on  $R_q$  (increasing with  $1/R_q$ )

→ peak height ratio

$$\frac{V_{slow}^{max}}{V_{fast}^{max}} \sim \frac{C_d C_{tot} R_{load}}{C_q^2 R_q}$$

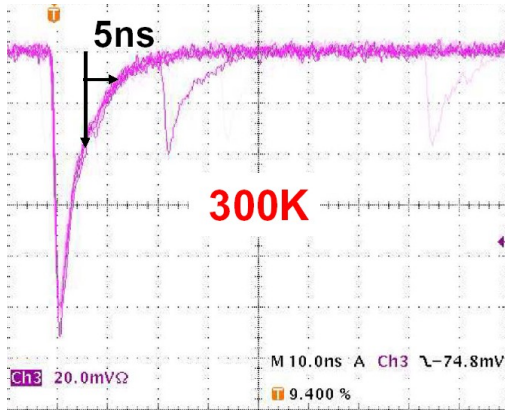
increasing with  $C_d$  and  $1/R_q$

# Pulse shape: dependence on Temperature

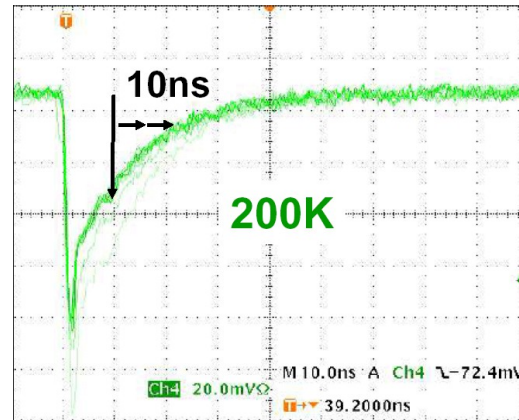
The two current components behave differently with Temperature

→ fast component is independent of T because  $C_{tot}$  couples to external  $R_{load}$

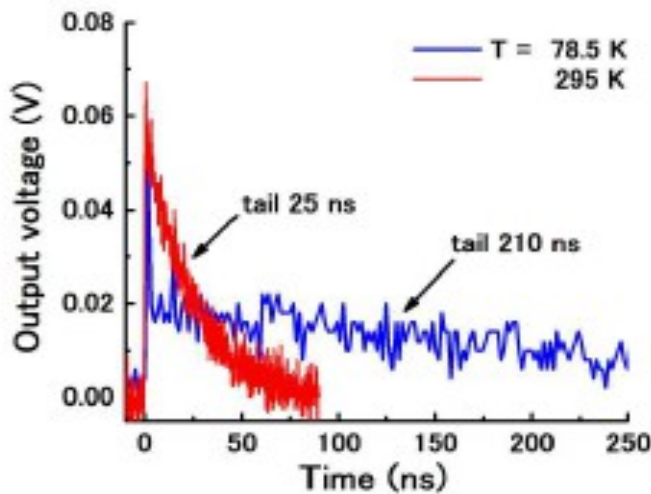
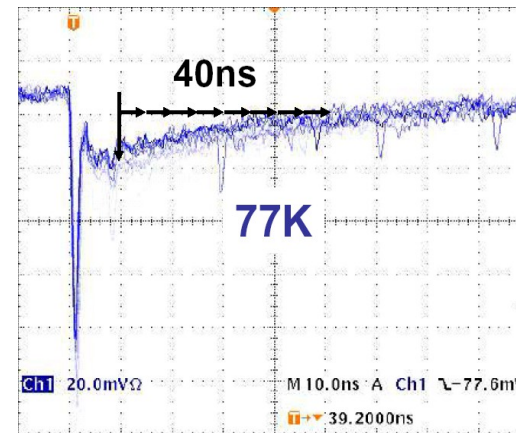
→ slow component is dependent on T because  $C_{d,q}$  couple to  $R_q(T)$



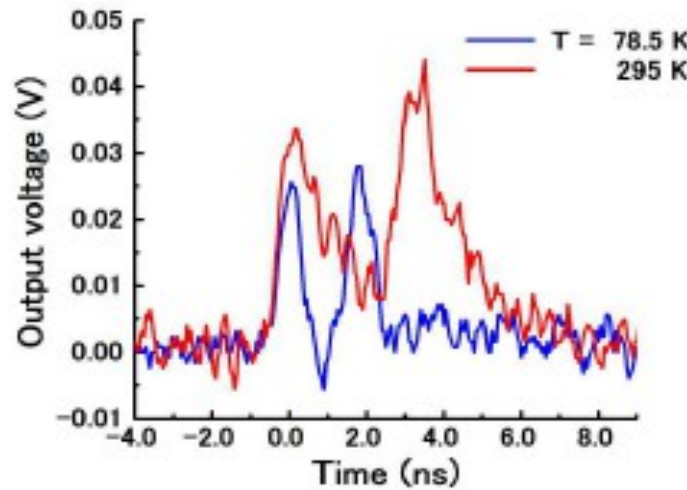
HPK MPPC



H.Otono, et al. PD07



(a)



(b)

HPK MPPC

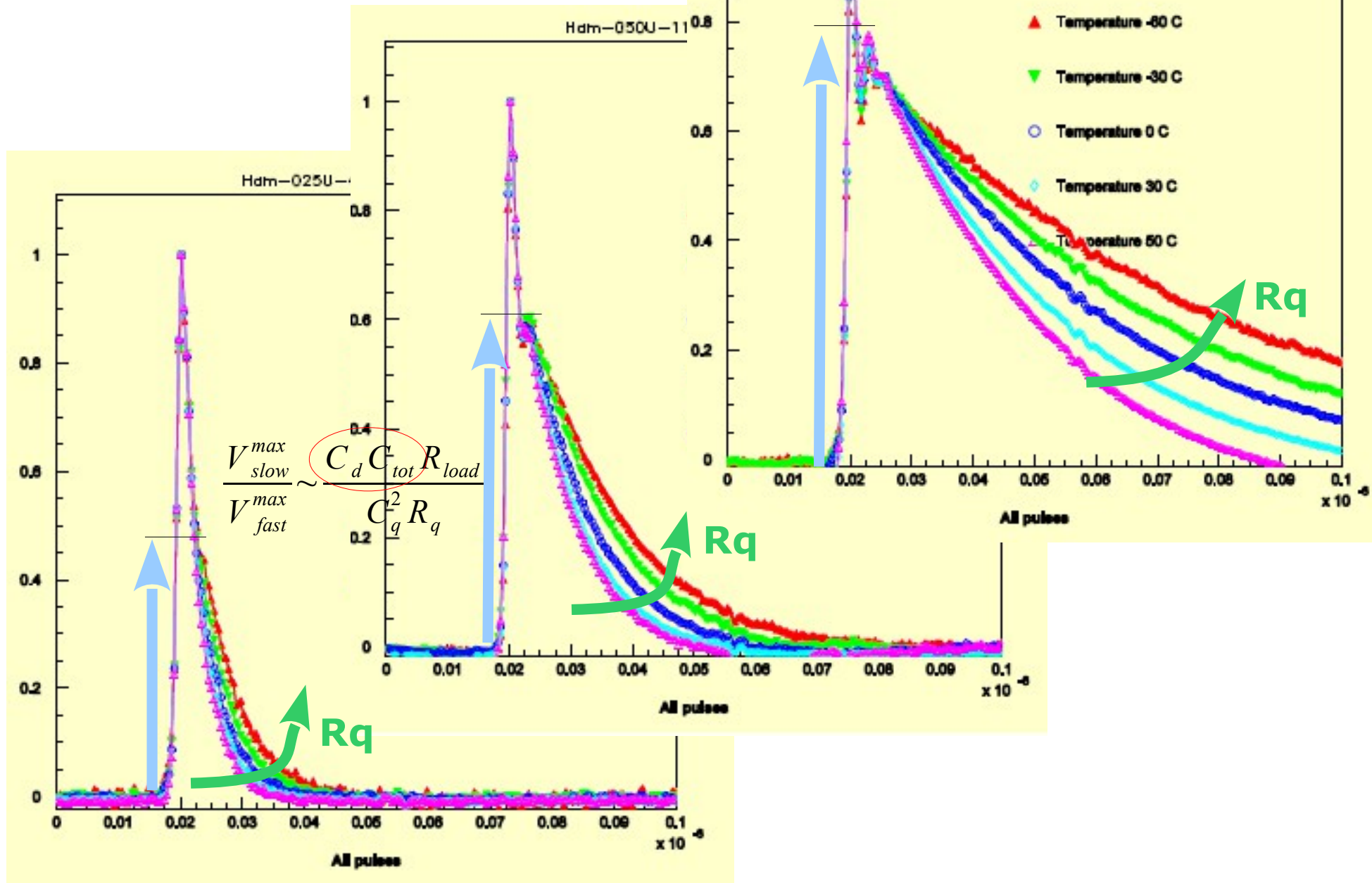
high pass filter / shaping  
→ recover fast signals

Fig. 2. (a) Output signals from the MPPC when no high-pass filter is used, and (b) output signals from the high-pass filter when two pulses were generated successively.

Akiba et al Optics Express 17 (2009) 16885

# Pulse shape vs T

HPK MPPC: 25 $\mu$ m, 50 $\mu$ m, 100 $\mu$ m



# Gain and its Fluctuations

$$G = \Delta V (C_q + C_d) / q_e$$

→ Gain is linear if  $\Delta V$  in quenching regime

but

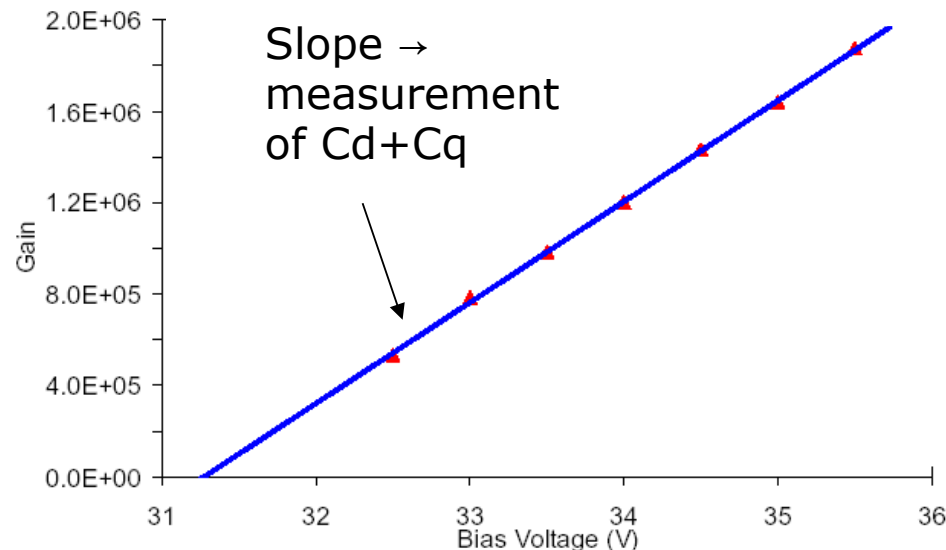
there are many sources for non-linearity of response (non proportionality)

SiPM gain fluctuations (intrinsic) differ in nature compared to APD where the statistical process of internal amplification shows a characteristic fluctuations

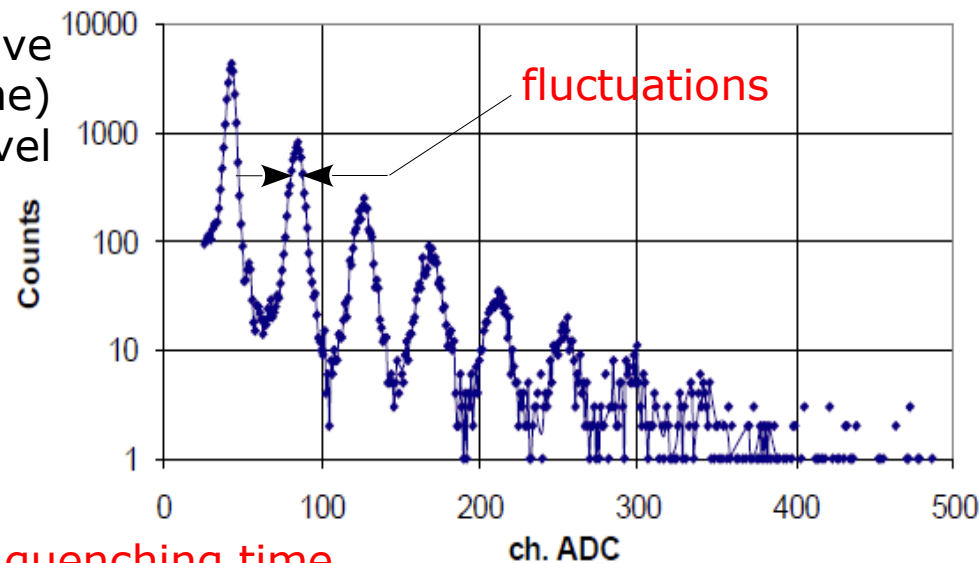
$$\frac{\delta G}{G} = \frac{\delta V_{bd}}{V_{bd}} \oplus \frac{\delta C_{dq}}{C_{dq}}$$

cell to cell uniformity (active area and volume) control at % level

- doping densities (Poisson):  
 $\delta V_{bd} \geq 0.3V$   
*Shockley, Sol. State Ele. 2 (1961) 35*
- doping, epitaxial, oxide (processing):  
 $\delta V_{bd} \sim O(0.1V)$



SES MEPhI/PULSAR APD, U=57.5V, T=-28 C



In addition  $\delta G$  might be due to fluctuations in quenching time  
 ... and of course after-pulses contribute too (not intrinsic → might be corrected)

# Response Non-Linearity

Non-proportionality of charge output w.r.t. number of photons (i.e. response) at level of **several %** might show up even in quenching regime (negligible quenching time), depending on  $\Delta V$  and on the **intensity** and **duration of the light pulse**.

Main sources are:

- finite number of pixels
- finite recovery time w.r.t. pulse duration
- after-pulses, cross-talk
- drop of  $\Delta V$  during the light pulse due to relevant signal current on (large) series resistances (eg ballast)

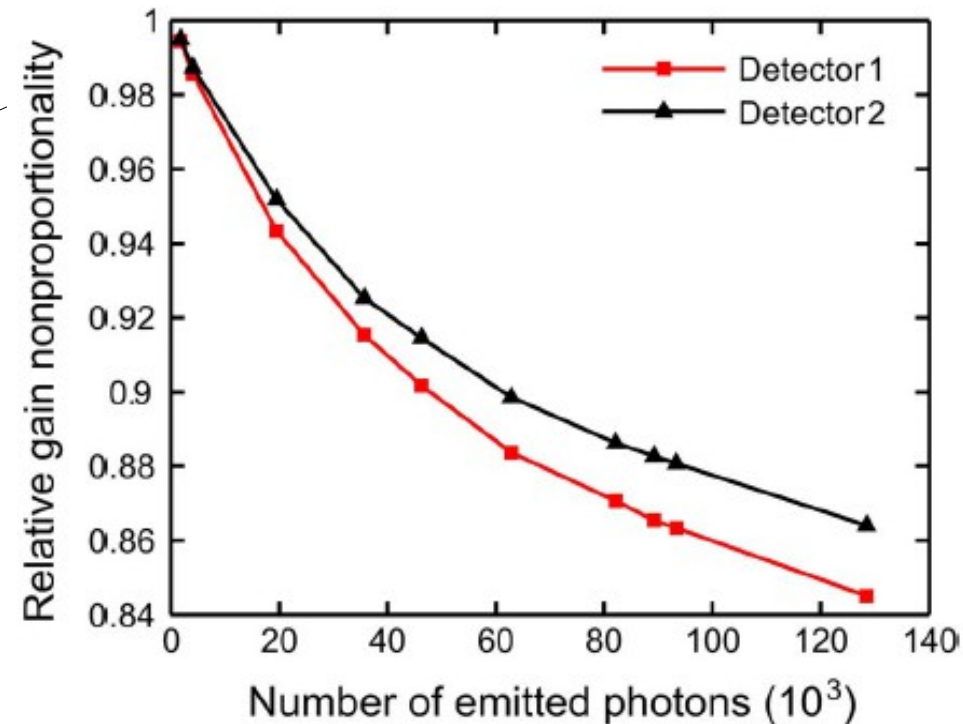
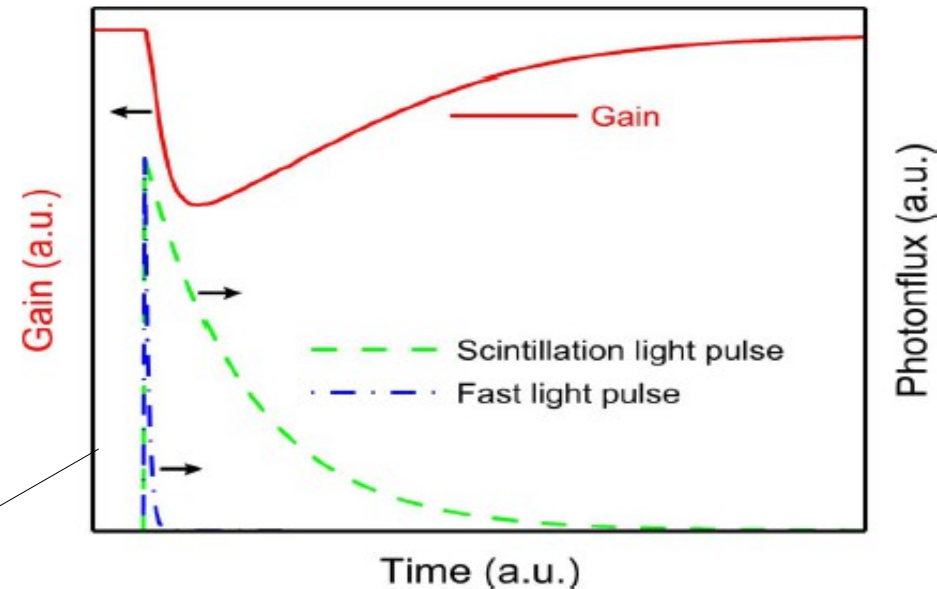
*T.van Dam IEEE TNS 57 (2010) 2254*  
*Detailed model to estimate non-lin. corrections*

Finite number of cells is main contribution in case number of photons  $\sim O(\text{number of cells})$  (dynamic range not adequate to application)

→ saturation 
$$n_{\text{fired}} = n_{\text{all}} \left( 1 - e^{-\frac{n_{\text{phot}} \cdot \text{PDE}}{n_{\text{all}}}} \right)$$

→ loss of energy resolution

see *Stoykov et al JINST 2 P06500* and *Vinogradov et al IEEE NSS 2009 N28-3*



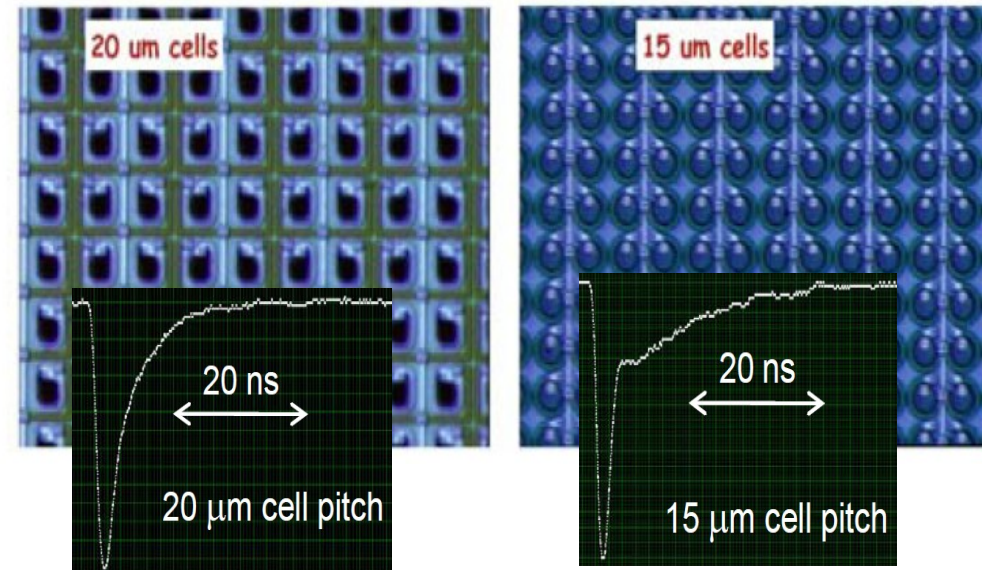


# New high dynamic range SiPMs

Latest MPPC tiny cell by Hamamatsu

Different types available or in preparation:

- **tiny cells**  
→ HPK, FBK, NDL, MPI-LL
- **micro cells**  
→ Zecotek, AmplificationTech

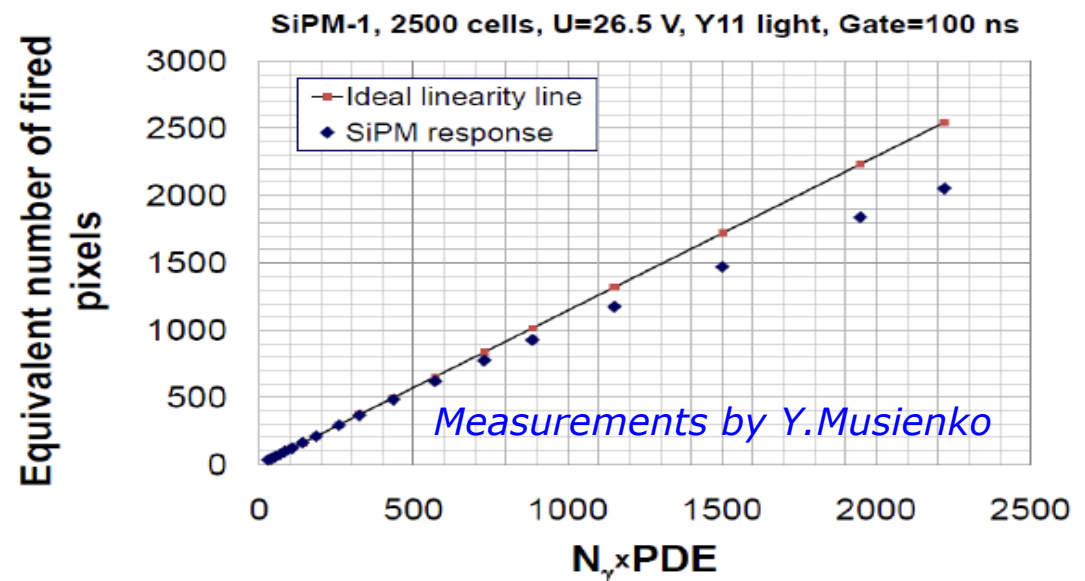


## SiPMs NDL (Beijing)

Zhang et al NIM A621 (2010) 116

Han at NDIP 2011

- type: n-on-p, Bulk Rq
  - high cell density (10000/mm<sup>2</sup>)
  - fast recovery (5ns)
  - low gain
- dynamic range
- radiation hardness



## Noise sources:

Dark counts

pulses triggered by non-photo-generated carriers (**thermal / tunneling generation** in the bulk or in the surface depleted region around the junction)

After-pulsing

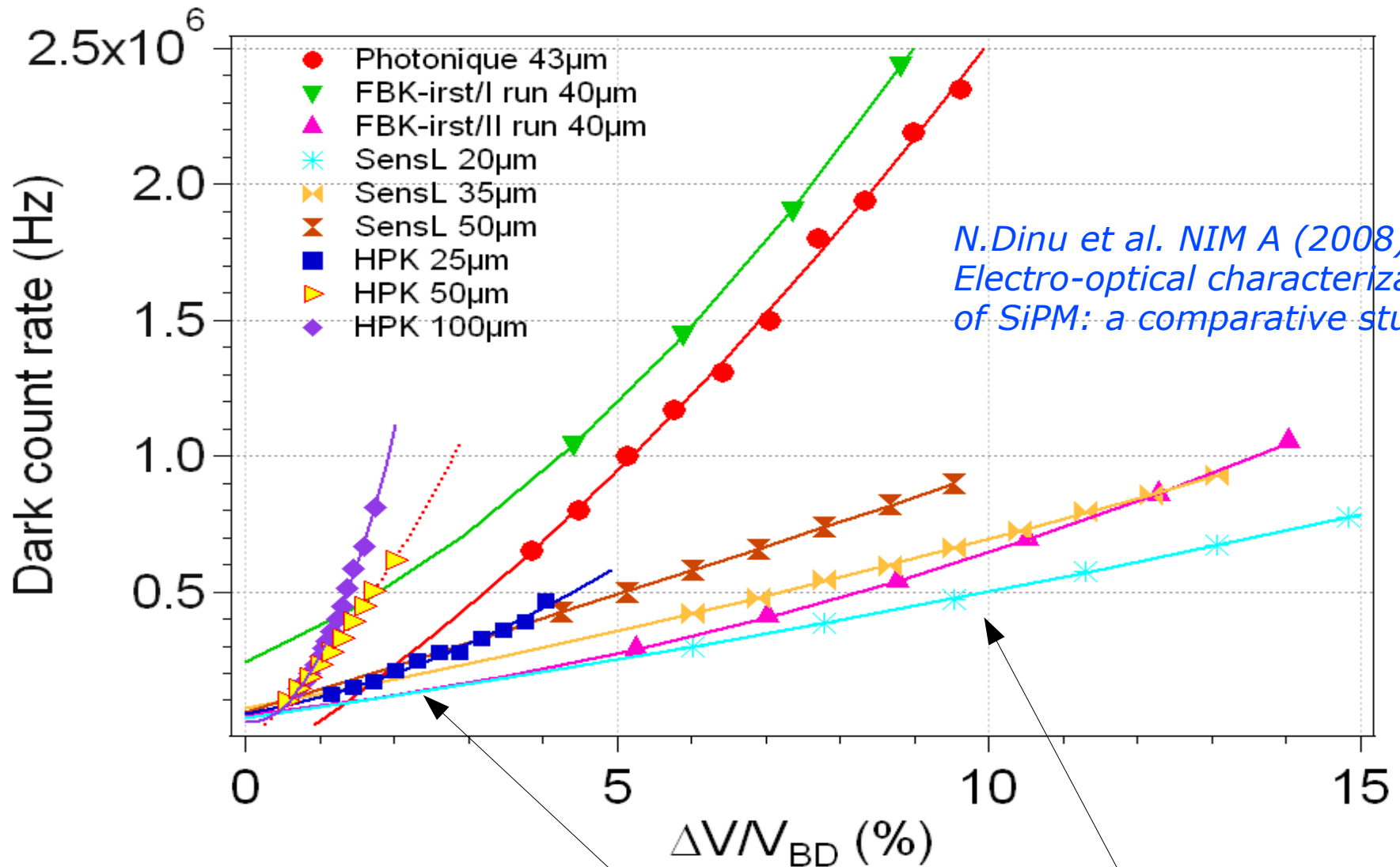
**carriers can be trapped** during an avalanche and then released triggering another avalanche

Cross-Talk

"optical"

**photo-generation during the avalanche discharge.** Some of the photons can be absorbed in the adjacent cell possibly triggering new discharges

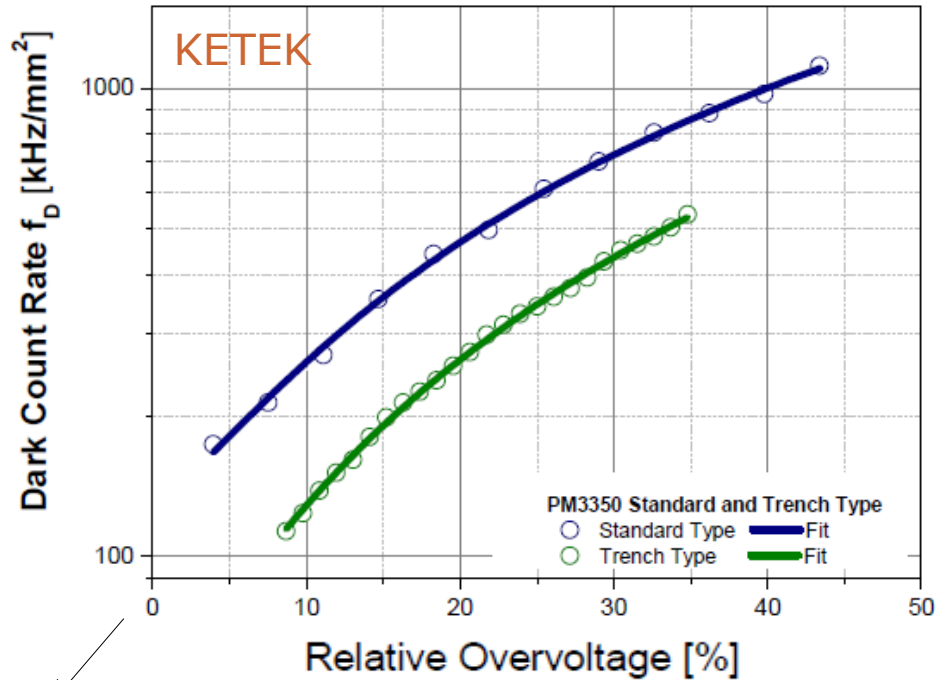
# Dark Count Rate



- DCR → linear dependence due to  $P_{01} \propto \Delta V$  (→ same as PDE vs  $\Delta V$ )  
 → non-linear at high  $\Delta V$  due to **cross-talk and after-pulsing** →  $\propto \Delta V^2$
- DCR scales with **active surface** (not with volume: **high field region dominating**)

# Dark Count Rate

KETEK PM 3350 (p<sup>+</sup>-on-n, shallow junction)  
 3x3mm<sup>2</sup> active area pixel size 50x50 μm<sup>2</sup>



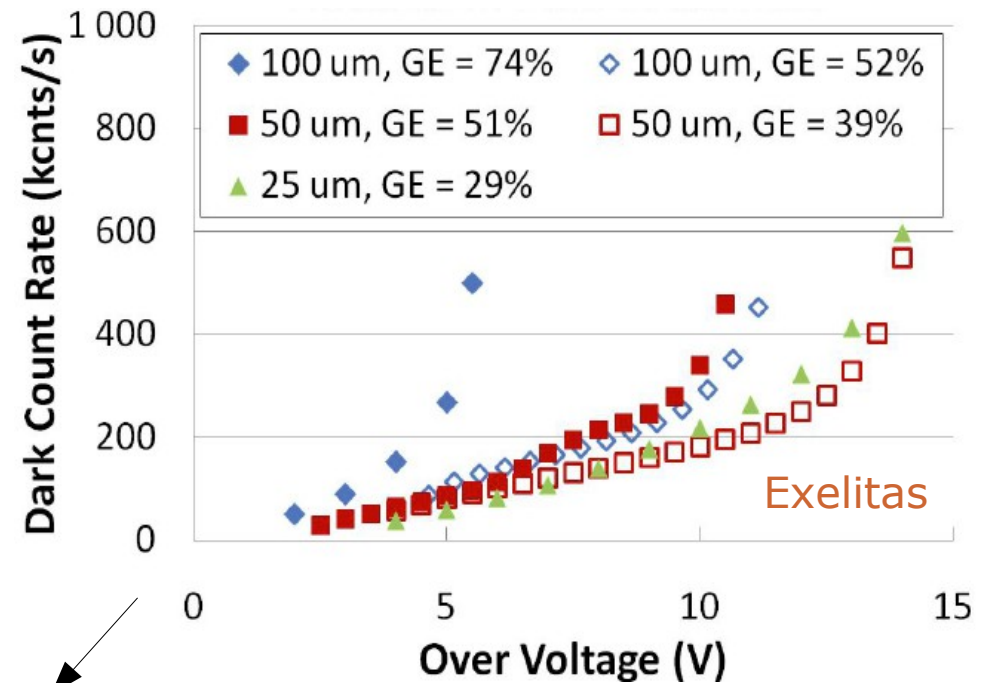
$V_{bd} \sim 25V$

*F. Wiest – AIDA 2012 at DESY*

Critical issues:

- quality of epitaxial layer
- gettering techniques
- Efield engineering (low T)

Exelitas 1<sup>st</sup> generation SiPM 2011  
 (p<sup>+</sup>-on-n) 1x1mm<sup>2</sup>



$V_{bd} \sim 140V$

*P. Berard – NDIP 2011*

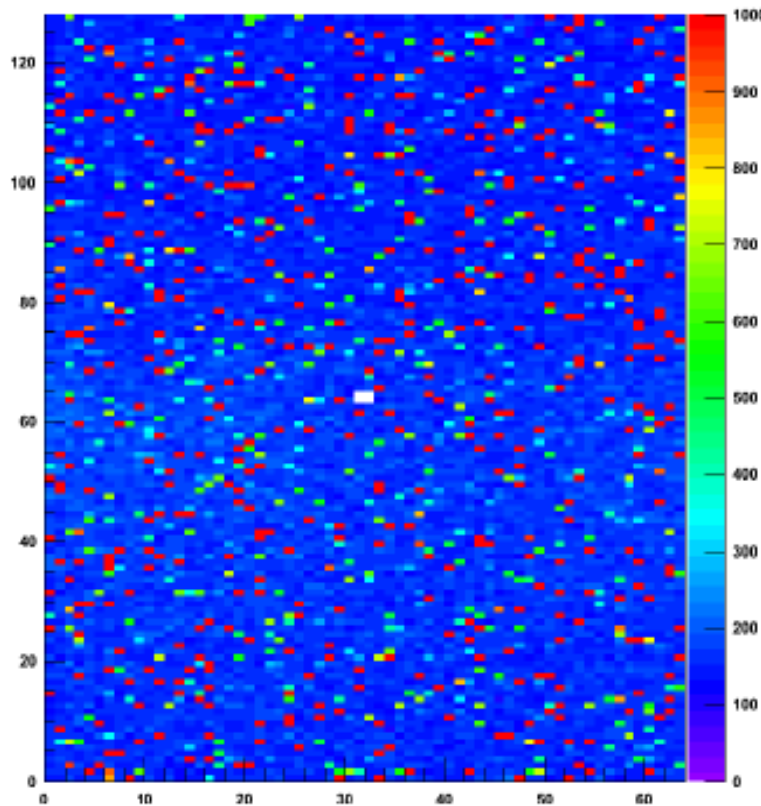
Latest Hamamatsu devices reached  $\sim 80\text{kHz/mm}^2$

HPK claiming for additional improvements coming  
 (*HPK at LIGHT 2011*)

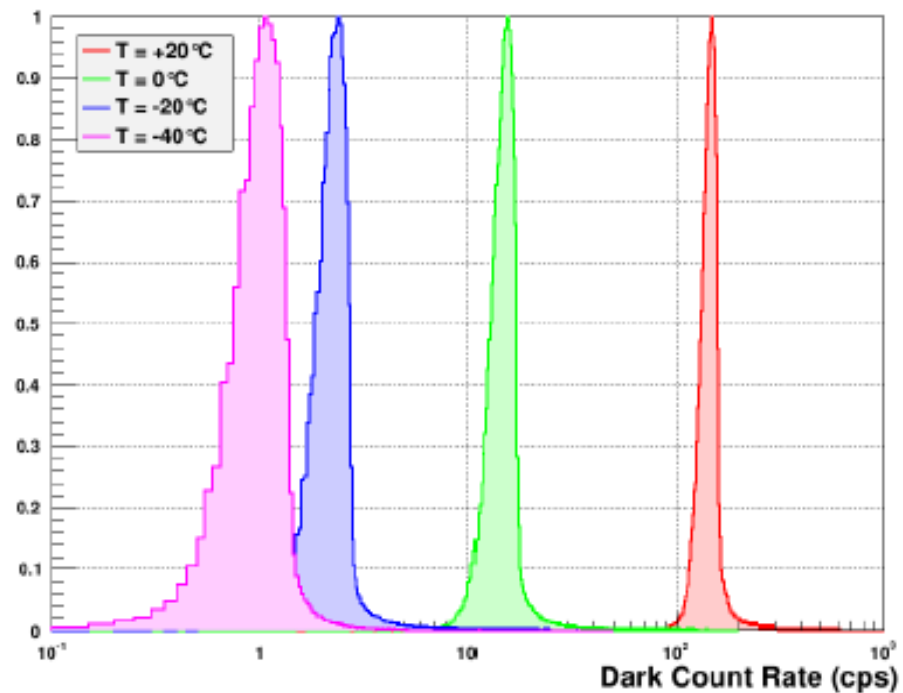
# Dark Count Rate

dSiPM

Control over individual SPADs enables detailed device characterization



SPAD Dark Count Rate Distribution



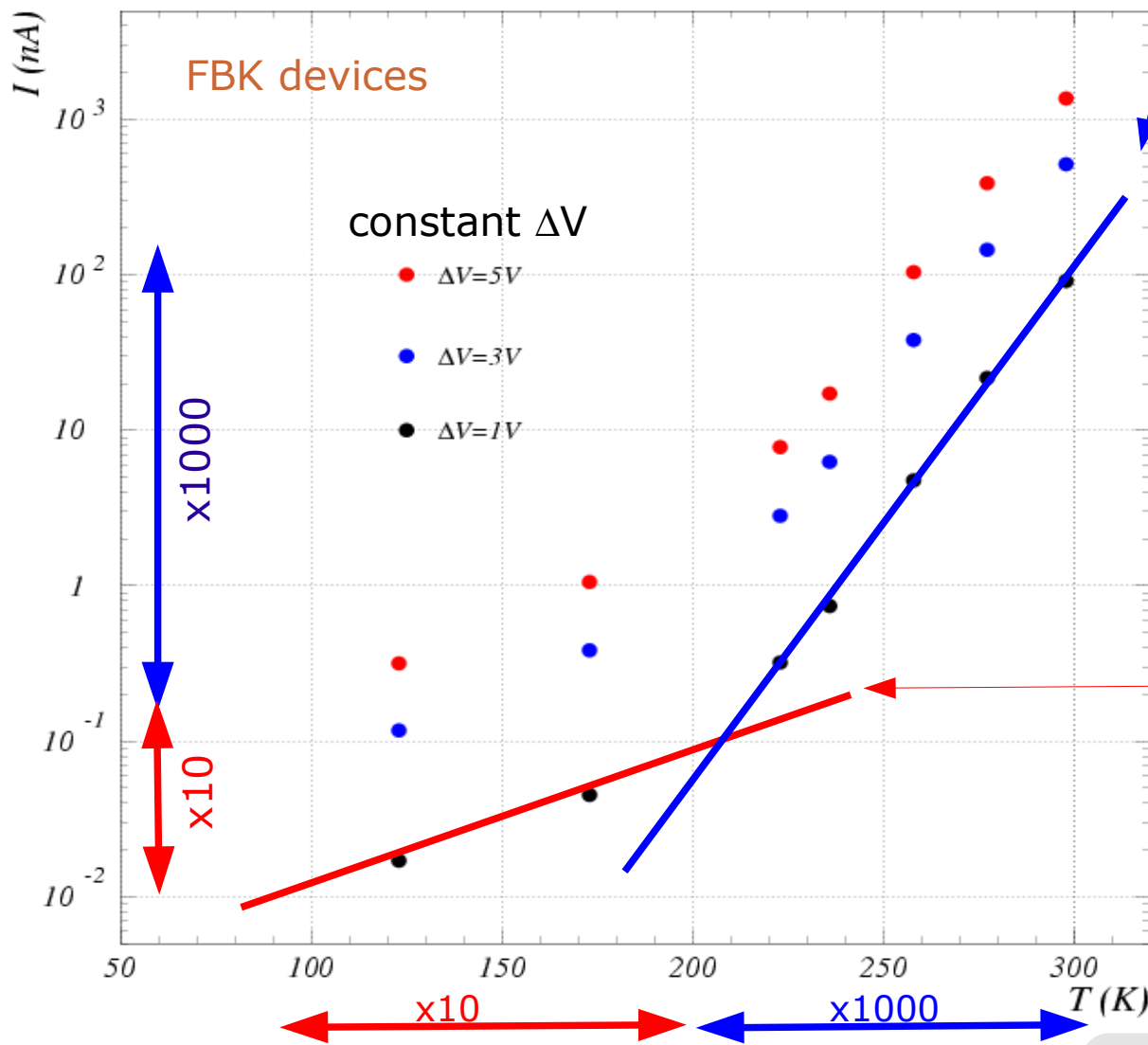
- Over 90% good diodes (dark count rate close to average)
- Typical dark count rate at  $20^\circ\text{C}$  and 3.3V excess voltage:  $\sim 150\text{cps}$  / diode
- Low dark counts ( $\sim 1\text{-}2\text{cps}$ ) per diode at  $-40^\circ\text{C}$

*T.Frach at NDIP 2011*

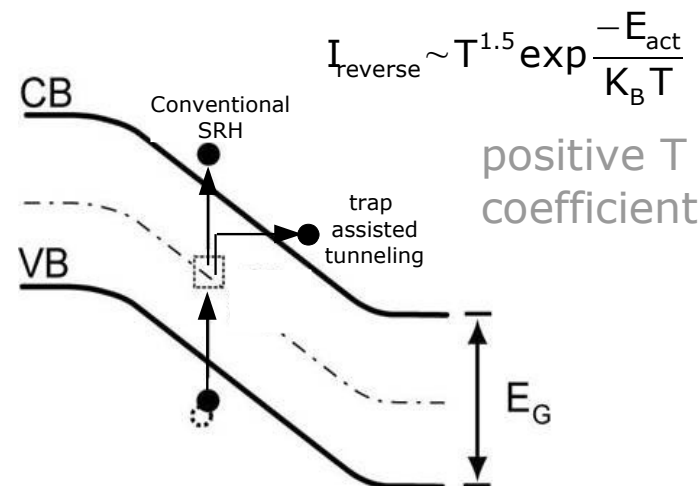
# Dark current vs T sources of DCR

contribution to DCR from diffusion of minority carriers negligible below 350K

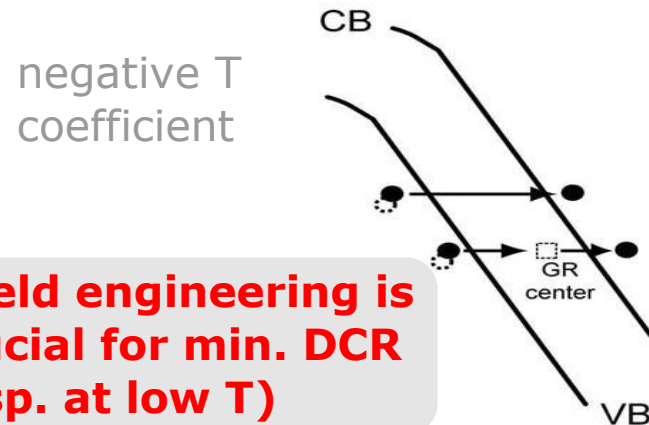
Noise mainly comes from the high E Field region (no whole depletion region)



1) Generation/Recombination SRH noise (enhanced by trap assisted tunneling)



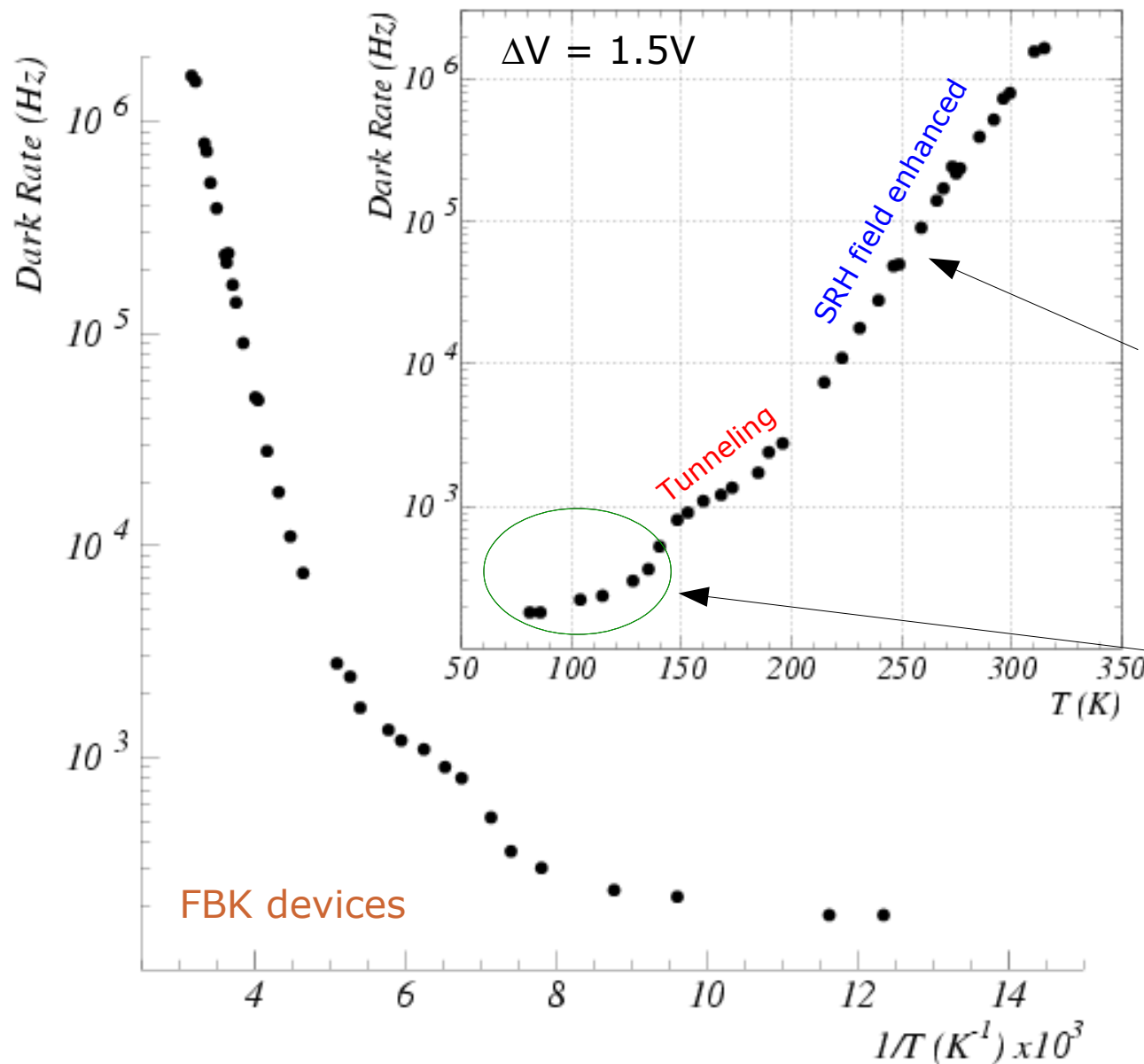
2) Band-to-band Tunneling noise (strong dependence on the Electric field profile)



Tunneling noise dominating for  $T < 200K$  (FBK devices have E field quite peaked)

Efield engineering is crucial for min. DCR (esp. at low T)

# Dark Count Rate vs T (constant $\Delta V$ )



Measurement of **counting rate of  $\geq 1p.e.$**  at fixed  $\Delta V=1.5V$  ( $\rightarrow$  constant gain)

$$DCR \sim T^{1.5} \exp\left(\frac{-E_{act}}{2K_B T}\right)$$

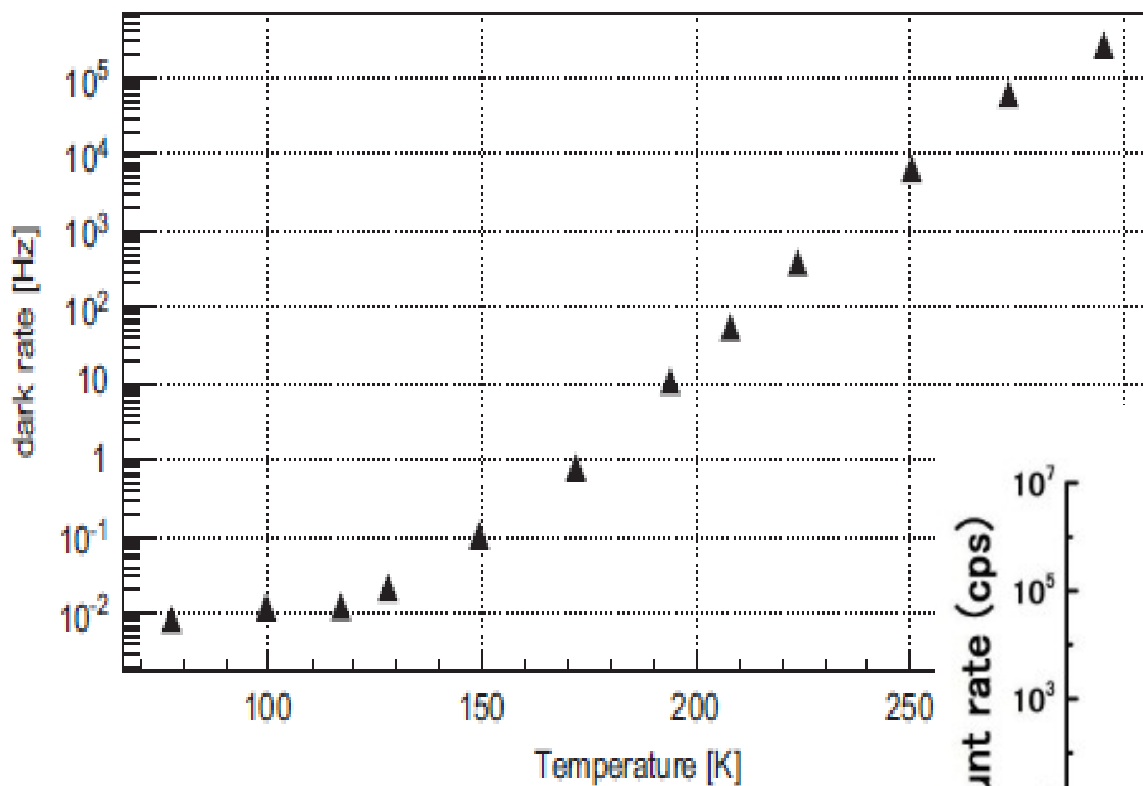
Activation energy  $E_{act} \sim 0.72eV$

Note:  $E_{act}$  should be  $\sim E_g$  but tunneling makes effective gap smaller

Additional structure carriers **freeze-out** (?)

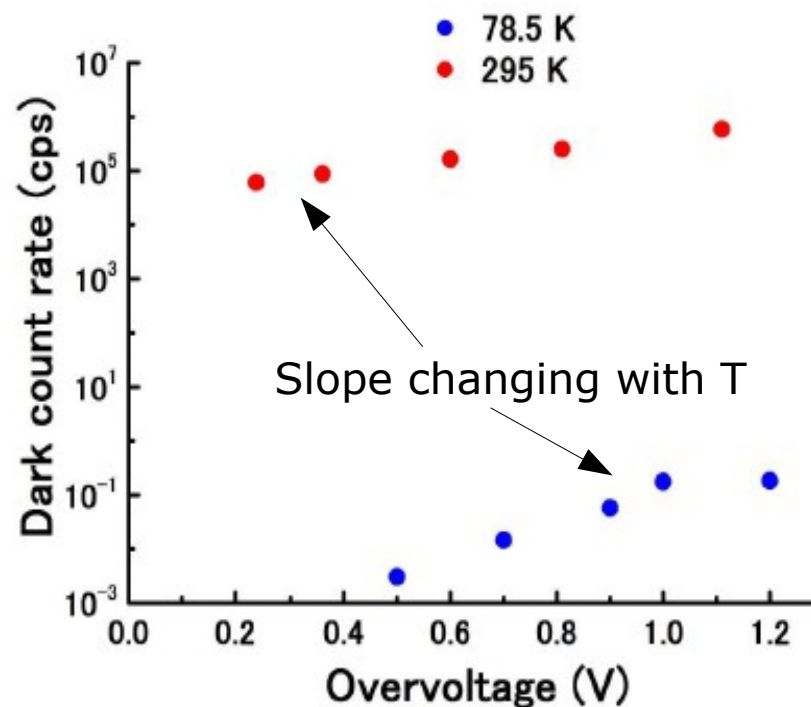
(carrier **collection losses** at very low T due to ionized impurities acting as shallow traps  $\rightarrow$  drop in PDE)

# Dark Count Rate vs T



Hamamatsu  
(100µm pixels)

*J.Csathy et al NIM A 654 (2011) 225*

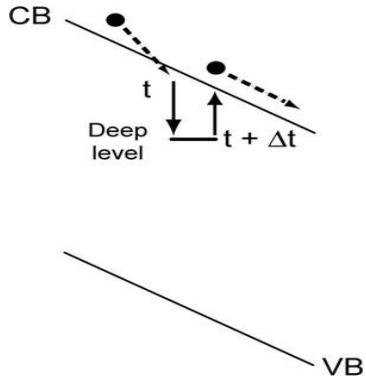


Comprehensive MPPC  
characterization at low T

*Akiba et al Optics Express 17 (2009) 16885*



# After-Pulsing Carrier trapping and delayed release



$$P_{\text{afterpulsing}}(t) = P_c \cdot \frac{\exp(-t/\tau)}{\tau} \cdot P_{01} \propto \Delta V^2 \quad \sim \text{Few \% level at 300K}$$

avalanche triggering probability  $\propto \Delta V(t)$

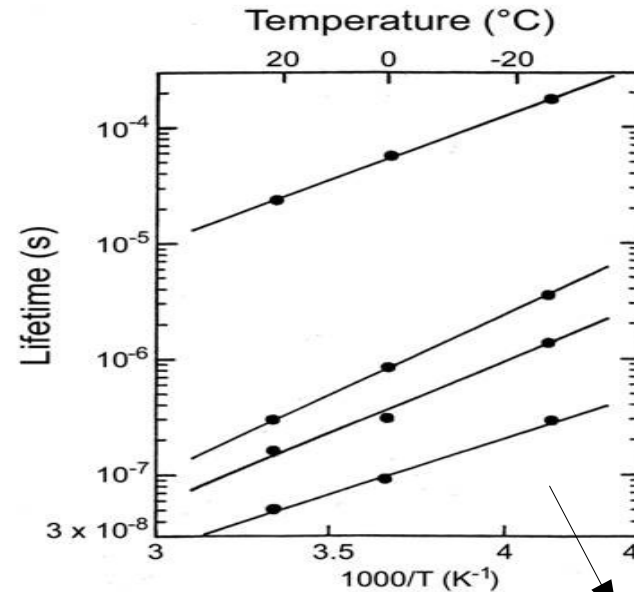
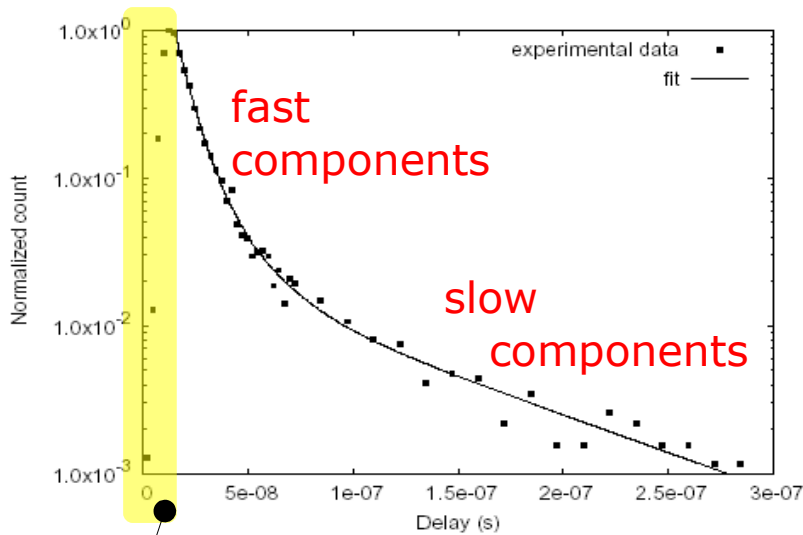
$\tau$  : trap lifetime depends on trap level position

quadratic dependence on  $\Delta V$

$P_c$  : trap capture probability

$\propto$  carrier flux (current) during avalanche  $\propto \Delta V$

$\propto N$  traps



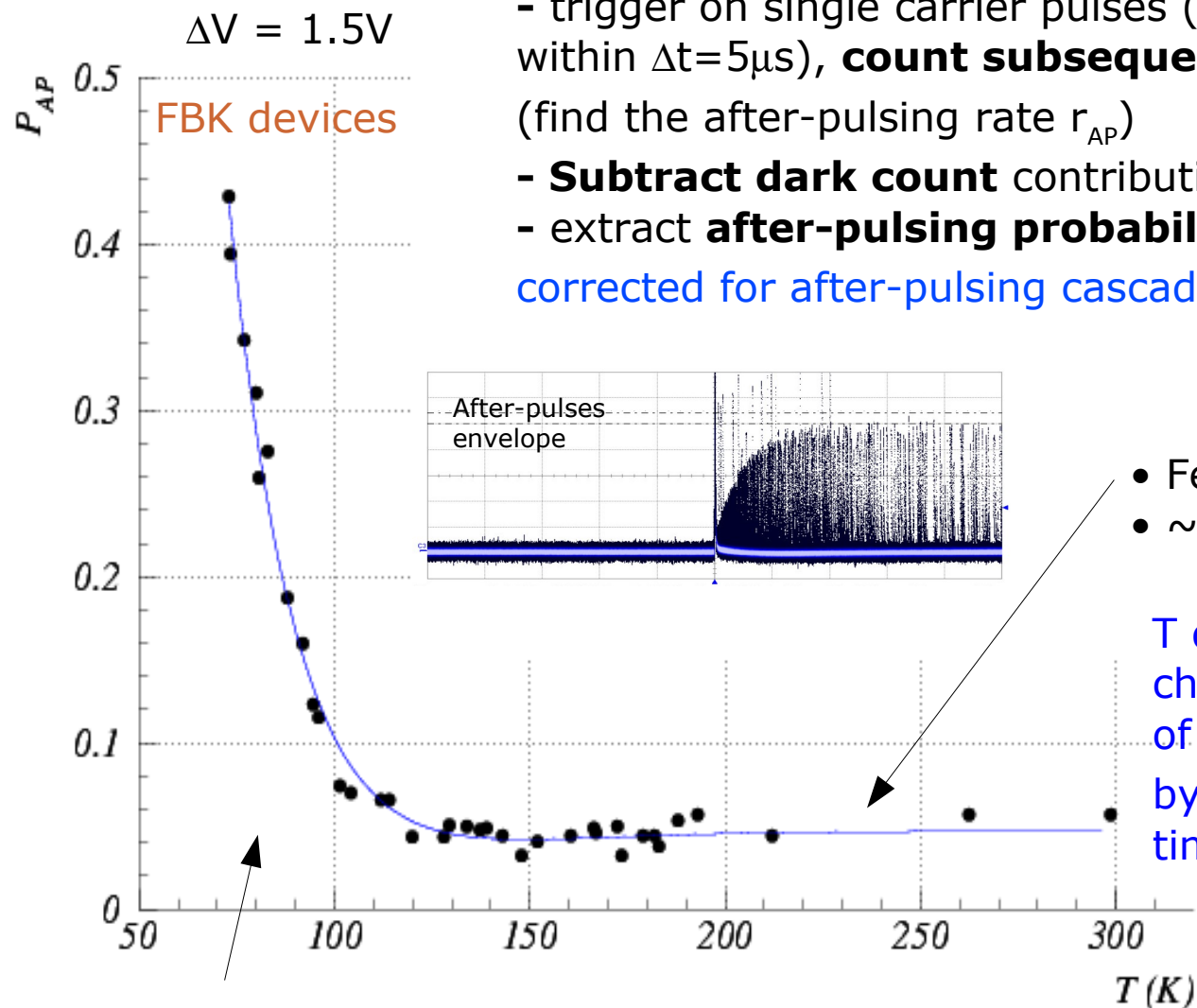
S.Cova, A.Lacaita, IEEE EDL (1991)  
G.Ripamonti, IEEE EDL (1991)

Fig. 10. Spectrum of the delay time from the primary pulse to the after-pulse.

Only partially sensitive to after-pulsing during recovery  
ie recovery hides After-pulses (does not cancel them)

not trivial dependence on T

# After-Pulses vs T (constant $\Delta V$ )



Measurement by waveform analysis:

- trigger on single carrier pulses (with no preceding pulses within  $\Delta t=5\mu s$ ), **count subsequent pulses** within  $\Delta t=5\mu s$  (find the after-pulsing rate  $r_{AP}$ )

- **Subtract dark count** contribution
- extract **after-pulsing probability  $P_{AP}$**

corrected for after-pulsing cascade ●

$$P_{AP} = \frac{r_{AP}}{1 + r_{AP}}$$

- Few % at room T
- ~constant down to ~120K

T decreasing: increase of characteristic time constants of traps ( $\tau_{traps}$ ) compensated by increasing cell recovery time ( $R_q$ )

- several % below 100K

T < 100K: additional trapping centers activated possibly (?) related to onset of carriers freeze-out

→ Analysis of life-time evolution vs T of the various traps (at least 3 types at  $T_{room}$ )

# Optical cross-talk Avalanche luminescence (NIR)

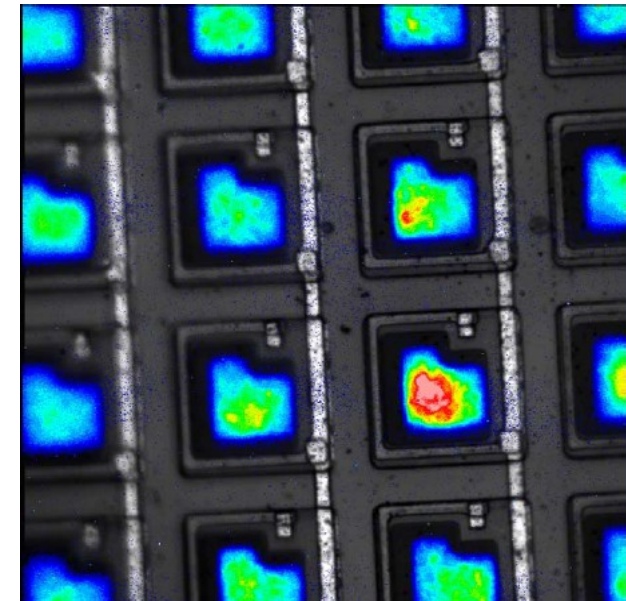
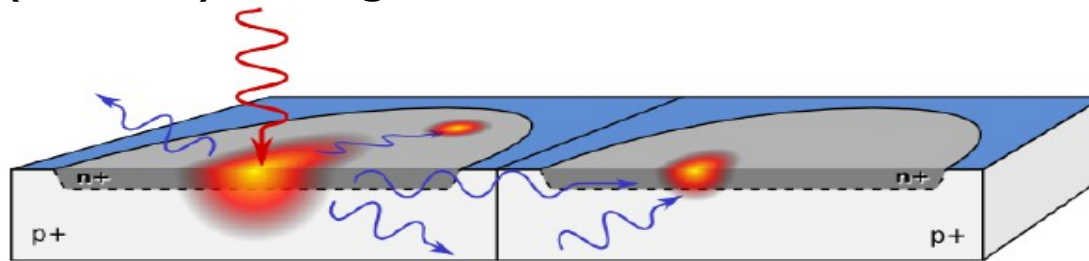
Carriers' luminescence (spontaneous direct relaxation in the conduction band) during the avalanche: probability  $3 \cdot 10^{-5}$  per carrier to emit photons with  $E > 1.14$  eV

*A.Lacaita et al. IEEE TED (1993)*

Photons can induce avalanches in neighboring cells. Depends on distance between high-field regions

$\Delta V^2$  dependence on over-voltage:

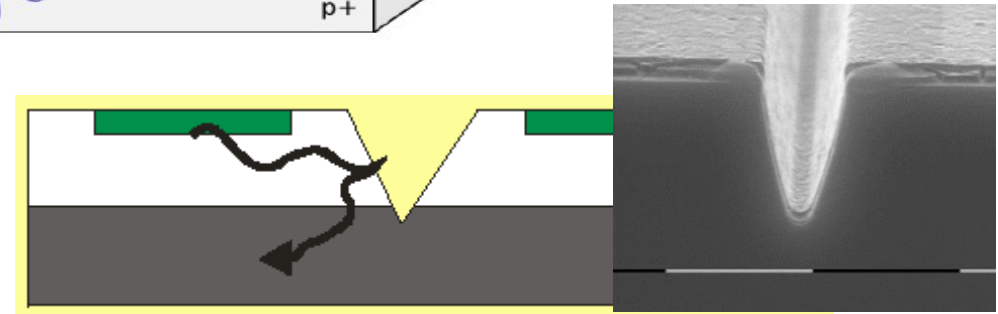
- carrier flux (current) during avalanche  $\propto \Delta V$
- gain  $\propto \Delta V$



N.Otte, SNIC 2006

Counteract:

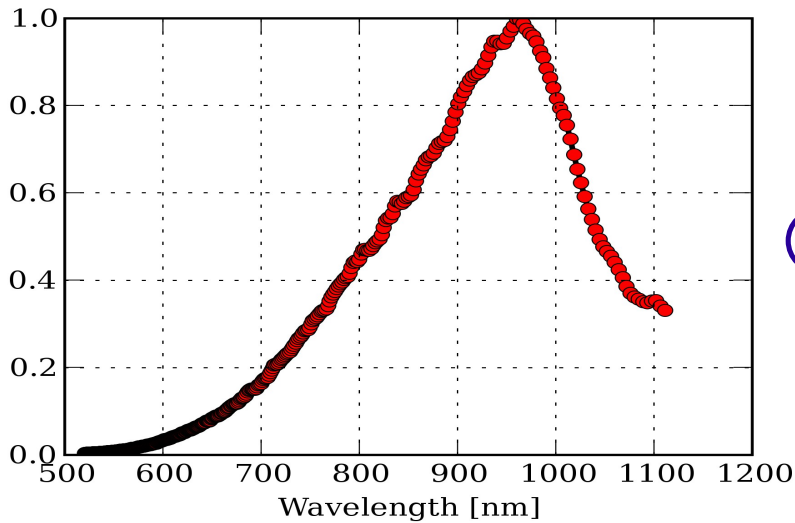
- optical isolation between cells by trenches filled with opaque material
- low over-voltage operation helps



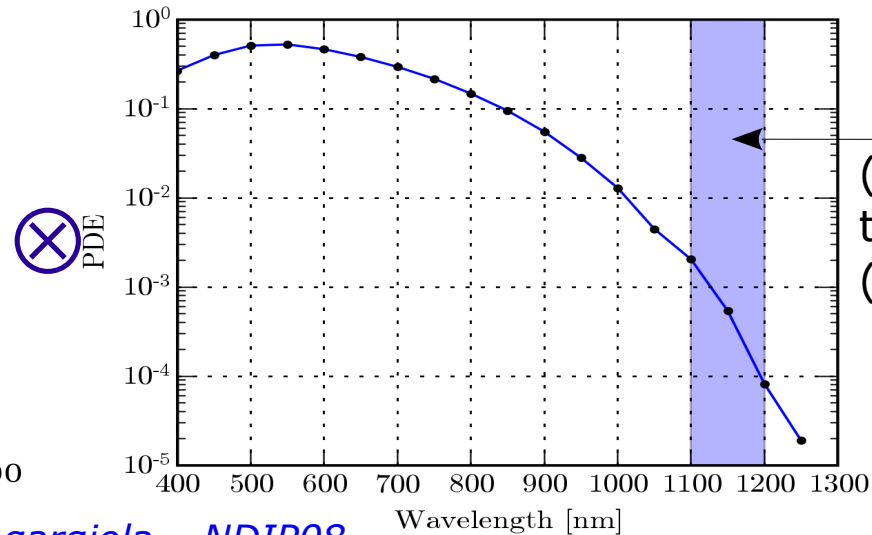
It can be reduced to a level below % in a wide  $\Delta V$  range

# Optical cross-talk: reflections from the bottom

Measured Emission spectrum

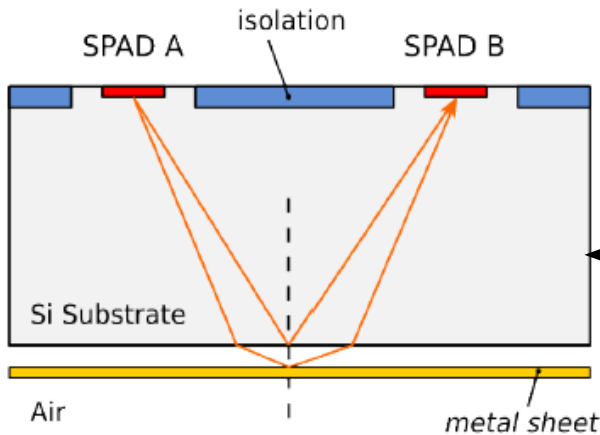


PDE



(1) Cross-talk due to narrow  $\lambda$  range (<100nm)

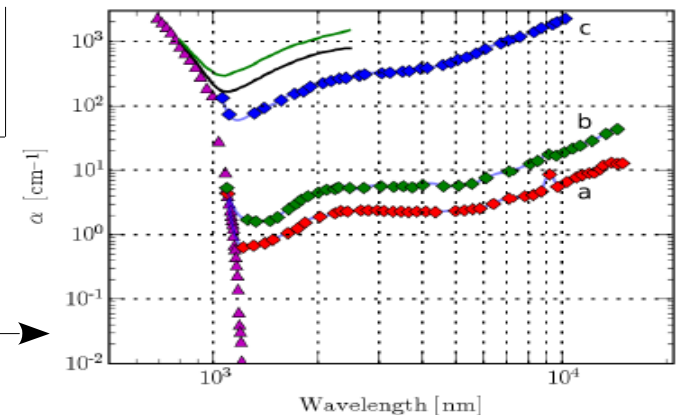
A. Ingargiola - NDIP08  
Rech et al Proc. of SPIE Vol. 6771 677111-1



(2) Main component due to total reflection internal from the bottom (substrate)

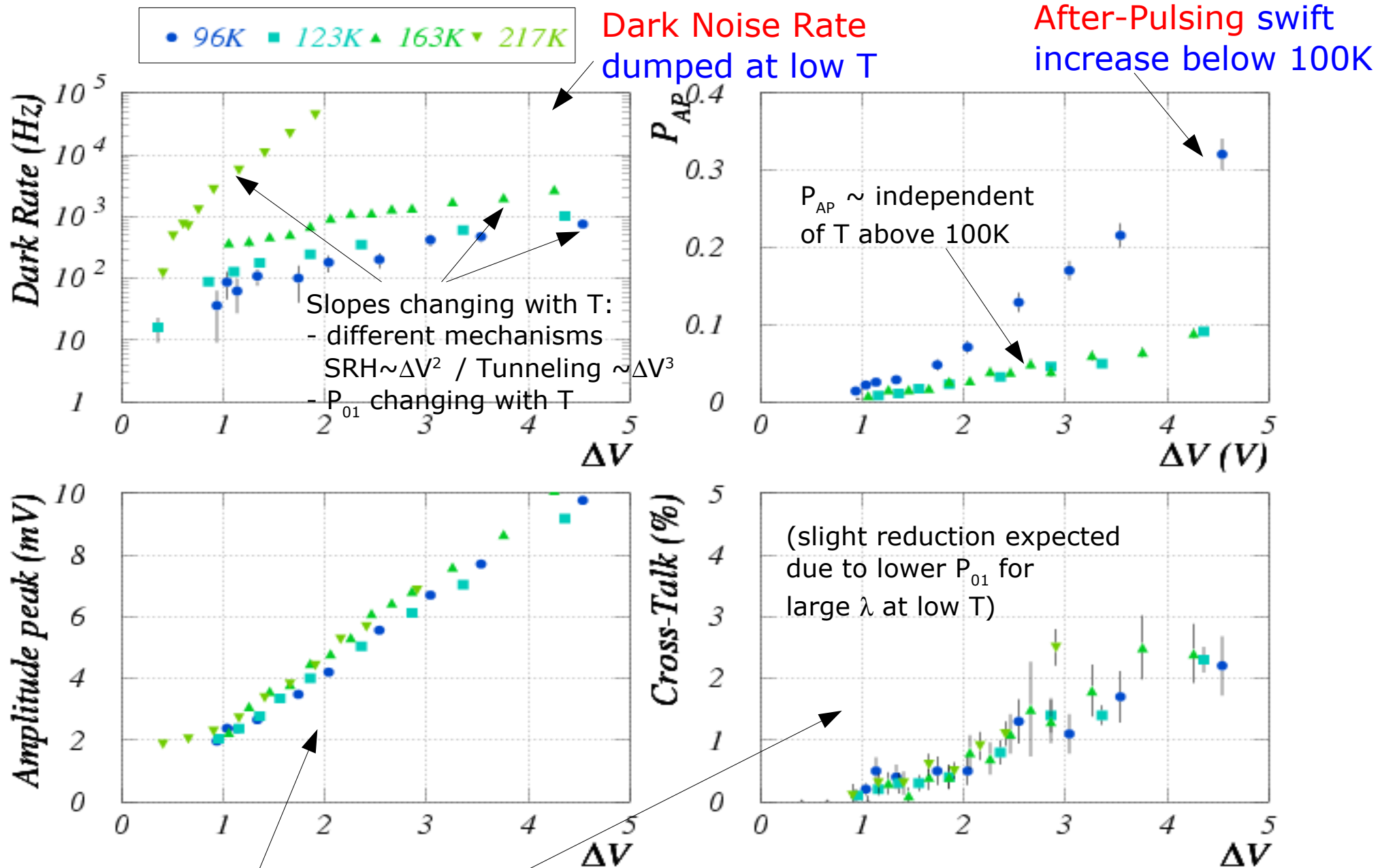
(3) Isolation implants are sufficient to stop direct component

Silicon absorption coefficients:



- Crosstalk **can't be eliminated** simply by means of **trenches**
- Main contribution to crosstalk comes from **bottom reflections** (using trenches)

# DCR, AP, Gain, X-talk vs $\Delta V$ (various T)



Gain and Cross-Talk are independent of T

FBK devices

G.C. et al NIM A628 (2011) 389



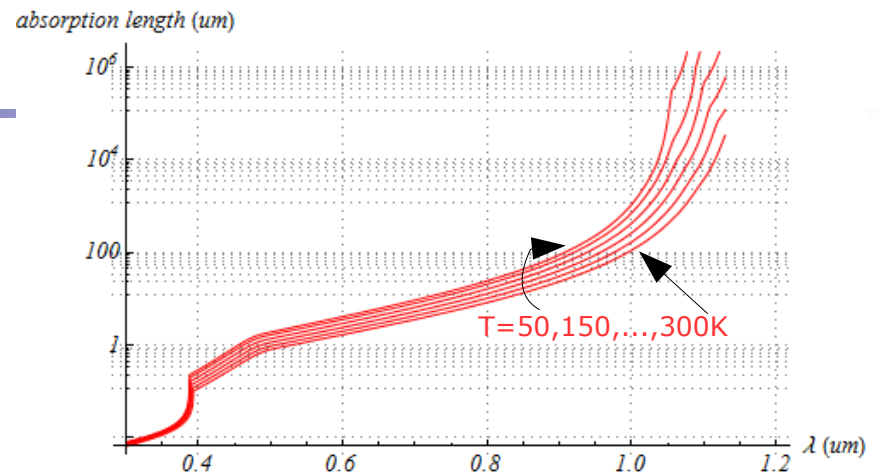
# Photo-Detection Efficiency (PDE)

$$PDE = QE \cdot P_{01} \cdot FF$$

## QE: carrier Photo-generation

probability for a photon to generate a carrier that reaches the high field region

- $\lambda$  and T dependent
- $\Delta V$  independent if full depletion at  $V_{bd}$

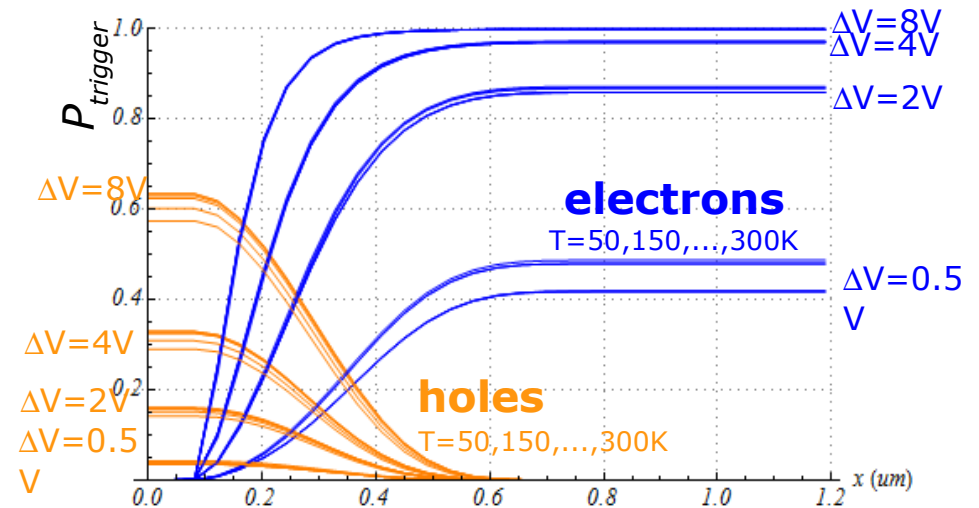


Rajkanan et al, Solid State Ele 22 (1979) 793

## $P_{01}$ : avalanche triggering probability

probability for a carrier traversing the high-field to generate the avalanche

- $\lambda$ , T and  $\Delta V$  dependent

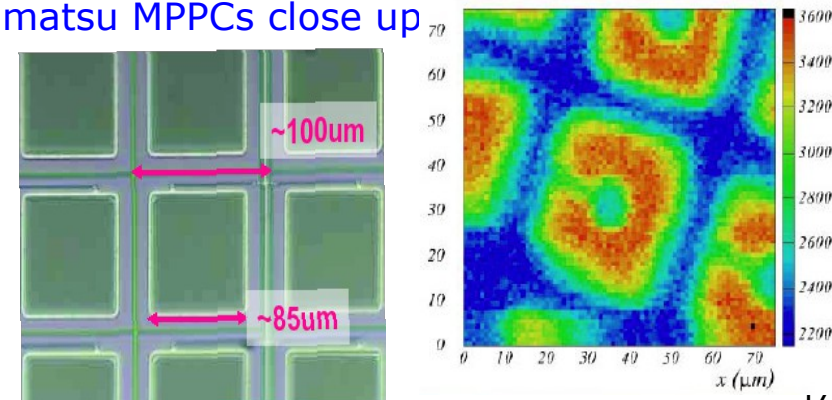


Hamamatsu MPPCs close up

## FF: geometrical Fill Factor

fraction of dead area due to structures between the cells, eg. guard rings, trenches

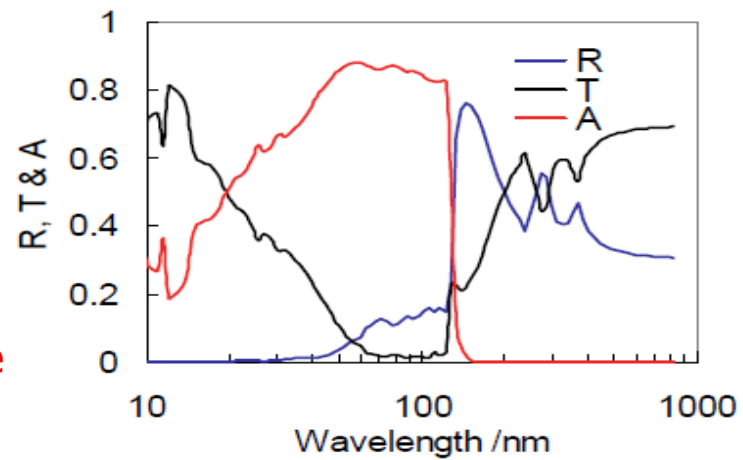
- mild  $\Delta V$  dependence (cell edges)



# QE

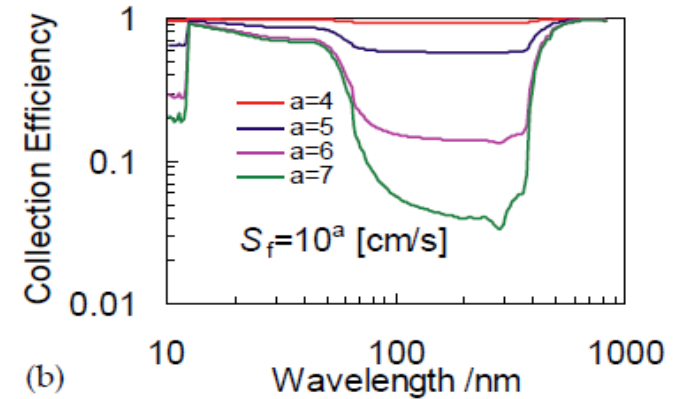
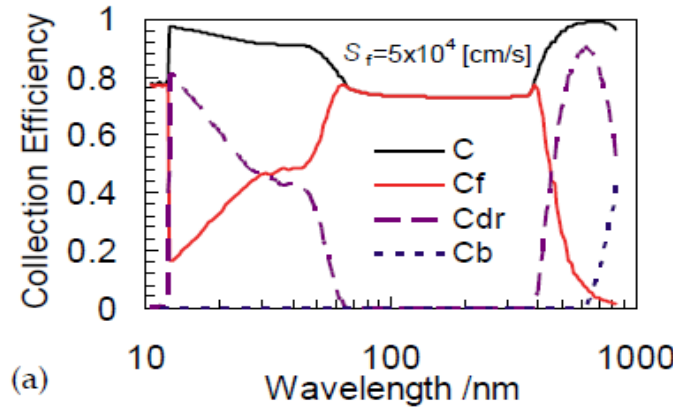
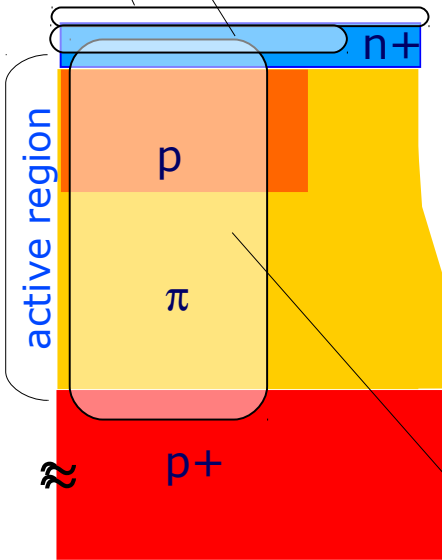
optical  $T, A, (R)$  of the entrance window (dielectric on top of silicon surface)

→ angular and polarization dependence



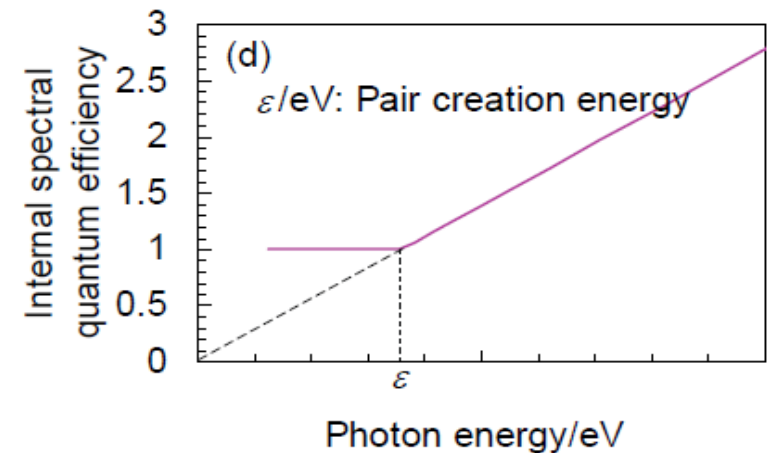
calculation for 30nm SiO<sub>2</sub> on Si layer

carrier recombination loss: collection efficiency front, depl. region, back



- front region critical for  $60\text{nm} < \lambda < 400\text{nm}$
- C eff. depends on surface recombination velocity  $S_f$
- freeze-out at low T

internal quantum efficiency: probability to photo-generate an e-h pair  $\sim$  photon E (above threshold)



eg of QE optimization (blue)

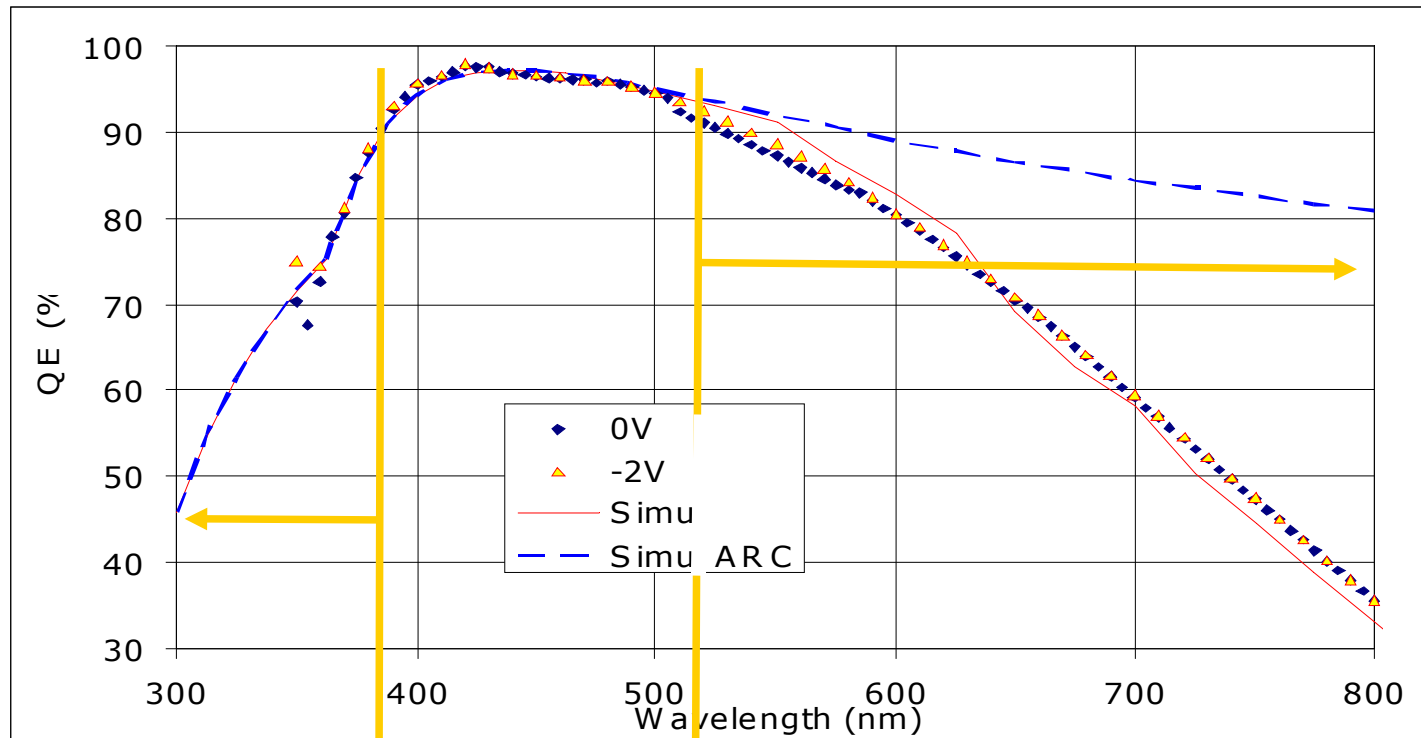
- Anti-reflective coating (ARC)
- Shallow junctions for short  $\lambda$
- Thick epi layers for long  $\lambda$



# QE single cell

FBK single cell

photo-voltaic regime ( $V_{bias} \sim 0$  V)

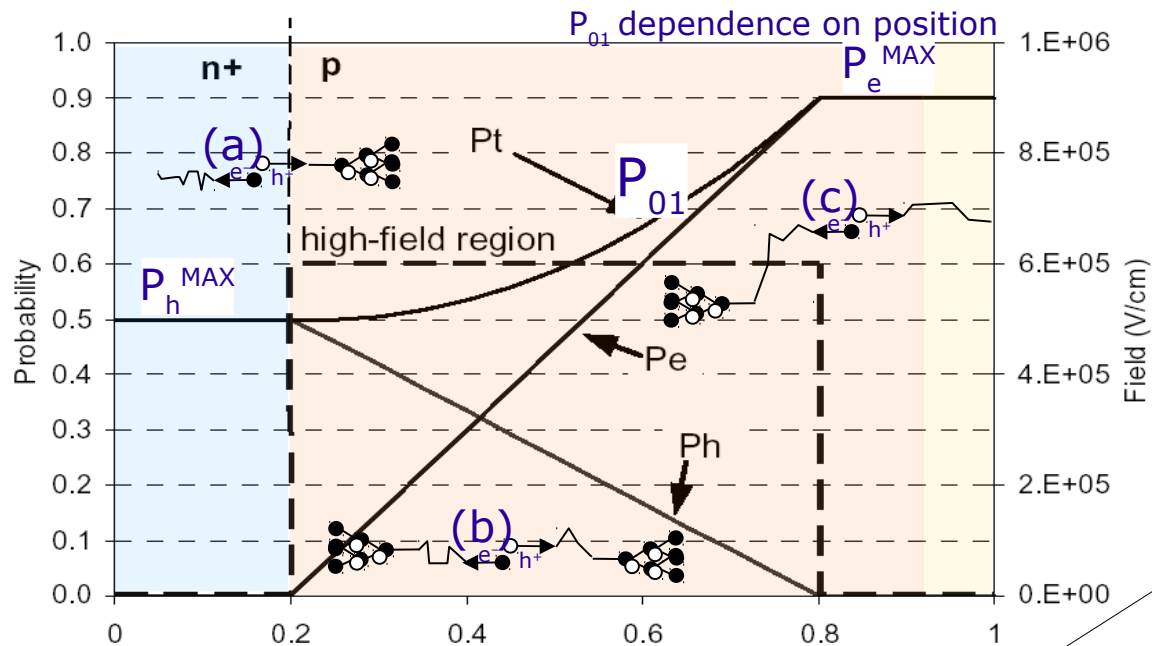


limited by  
ARC Transmittance  
&  
Superficial  
Recombination

limited by the  
small  $\pi$  layer thickness

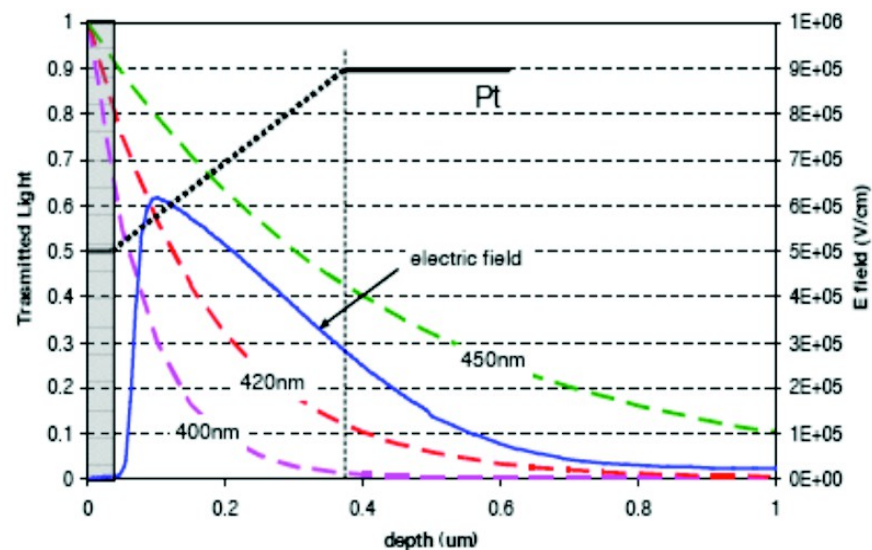
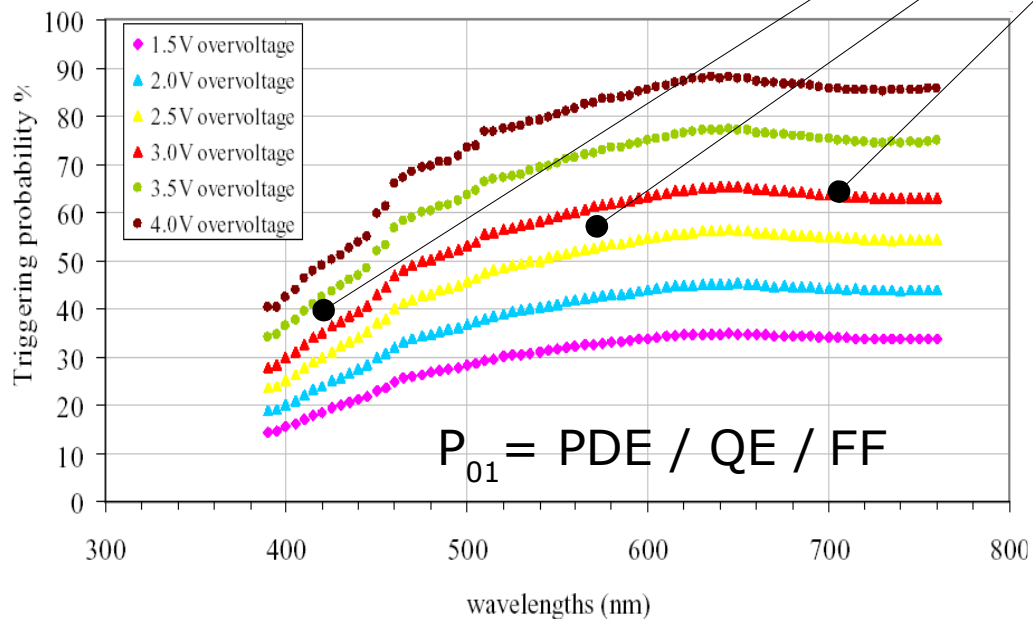
Most critical issue for **Deep UV SiPM**  
note: reduced superficial recombination  
in n-on-p wrt p-on-n

# Avalanche trigger probability ( $P_{01}$ )



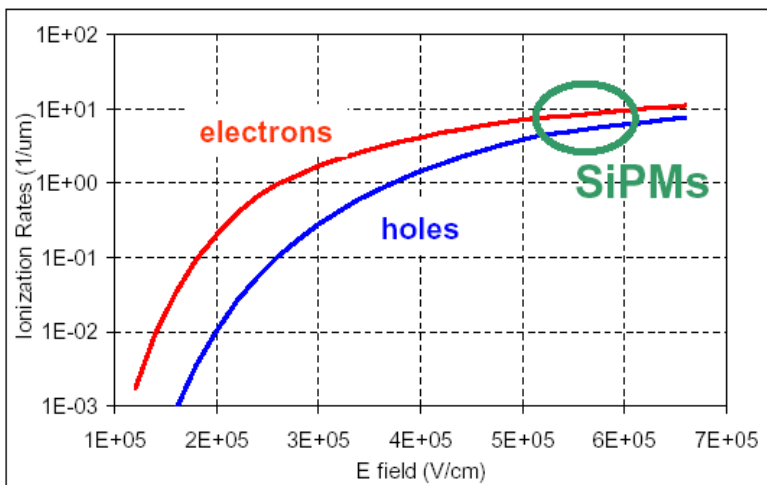
Probability calculations after *W. Oldham et al. IEEE TED (1972)*

Example with constant high-field:  
 (a) only holes trigger the avalanche  
 (b) both electrons and holes trigger  
 (c) only electrons trigger



# PDE vs $\Delta V$

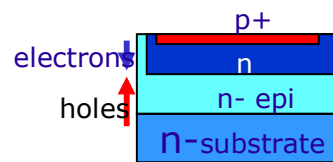
## Ionization rate in Silicon



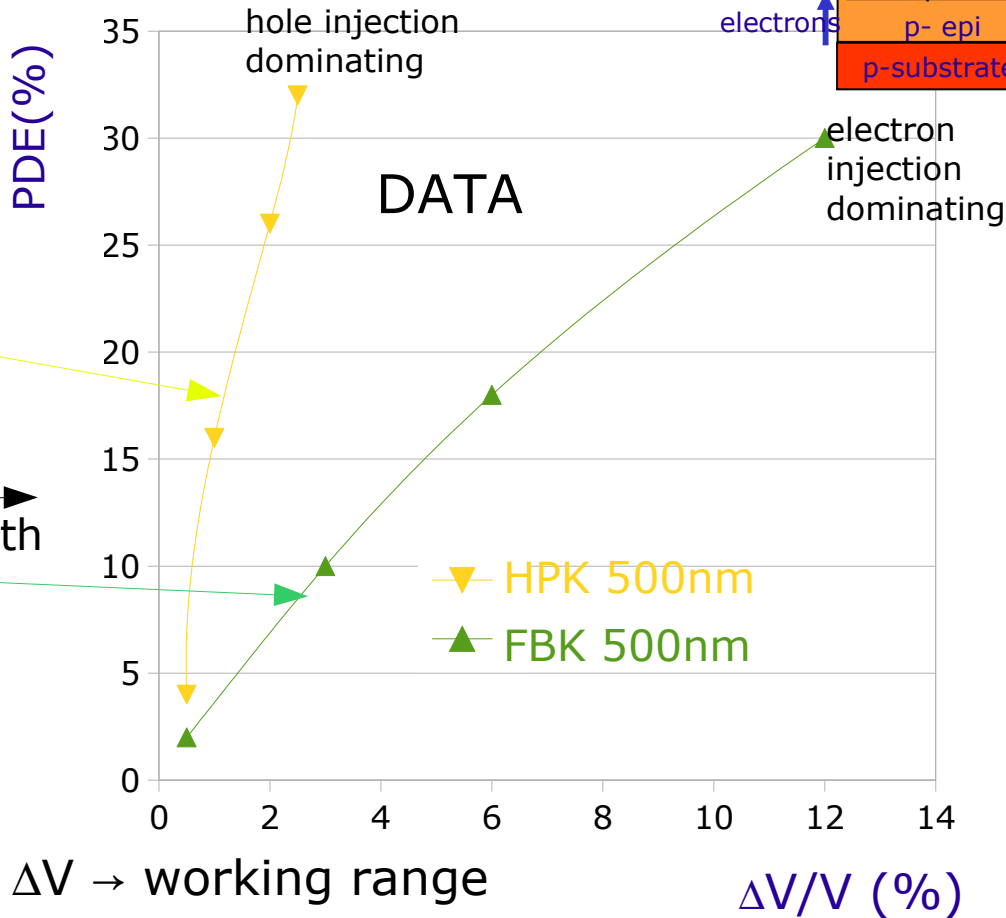
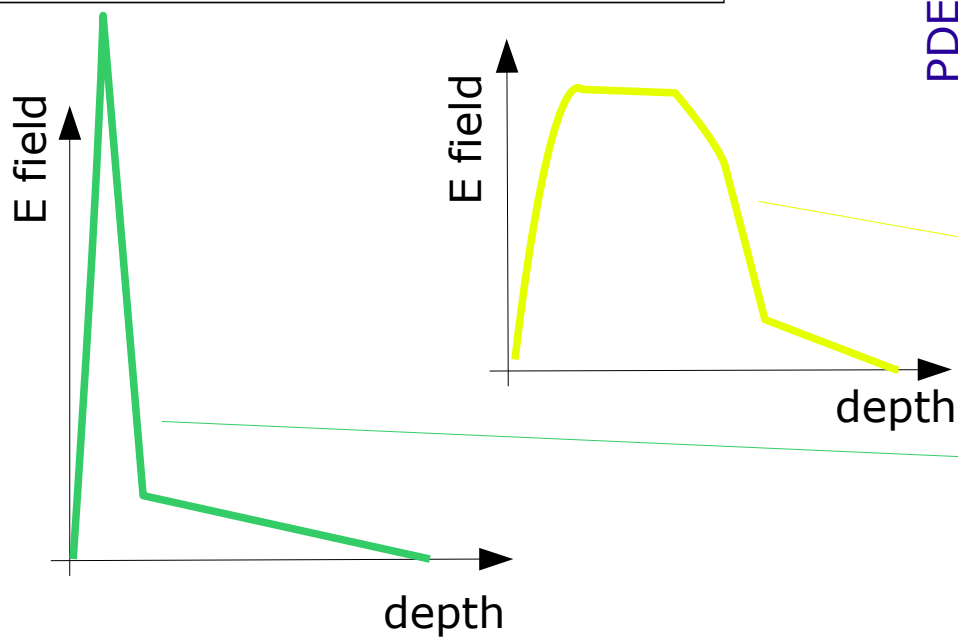
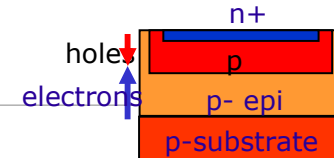
$P_{01}$  optimization (n-on-p)

- high over-voltage
- photo-generation in the p-side of the junction

## p-on-n structure



## n-on-p structure



E field profile  $\rightarrow$  the slope of PDE vs  $\Delta V$

note:  $P_{01}$  fixes also the slope of DCR vs  $\Delta V \rightarrow$  working range

$\Delta V/V$  (%)

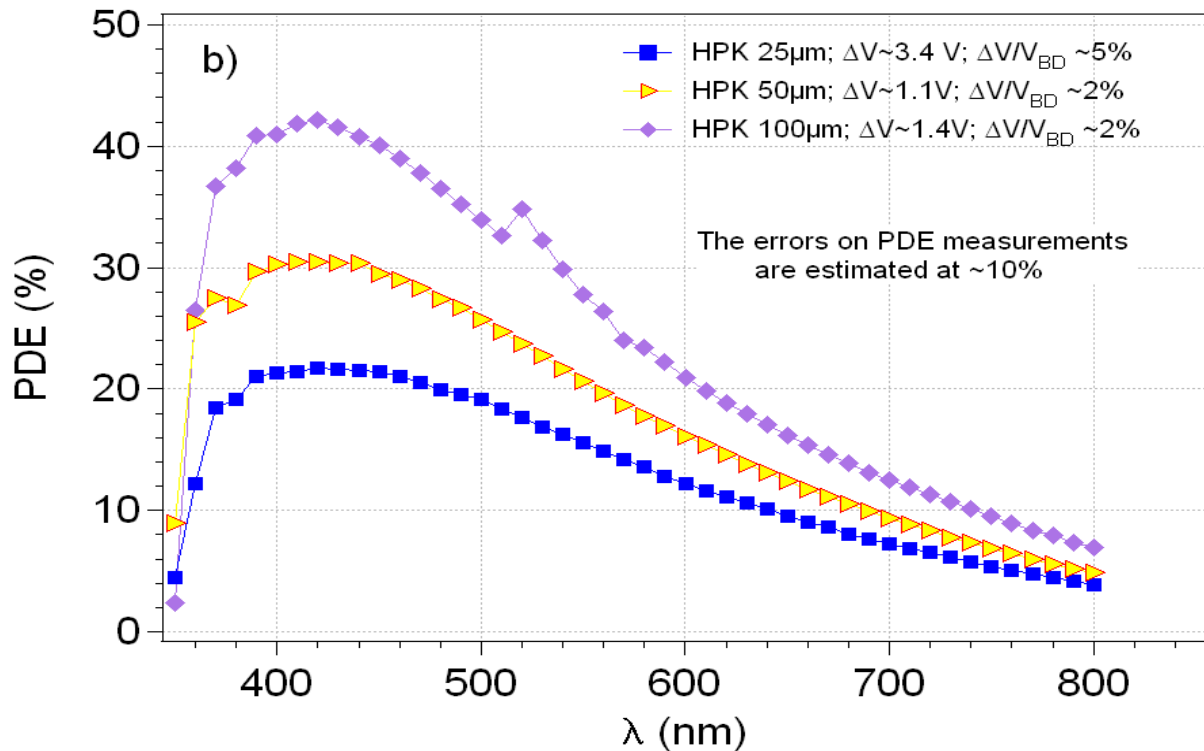
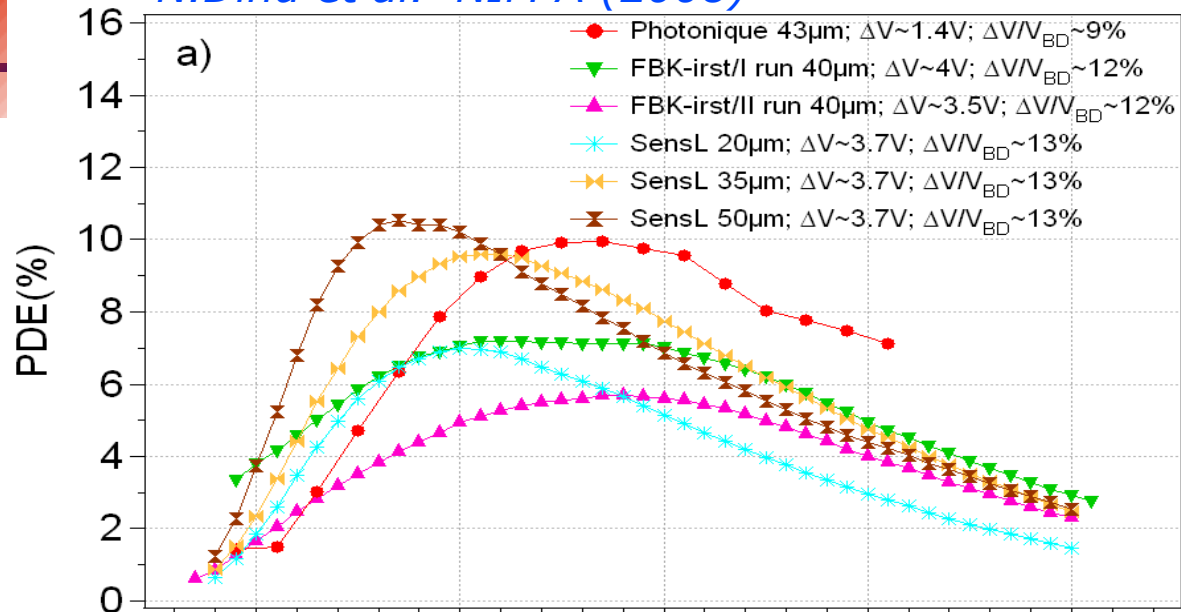
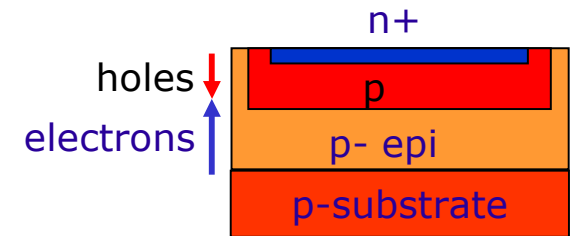


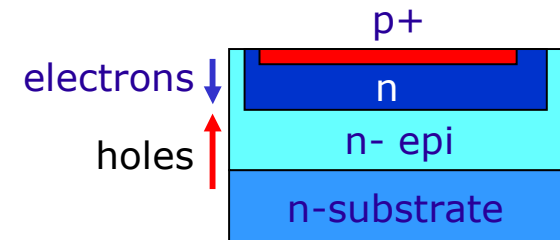
Fig. 5a) The PDE vs.  $\lambda$  of the Photonique, FRK-irst and SensL devices and b) HPK

# PDE VS $\lambda$ (shape)

n-on-p structures



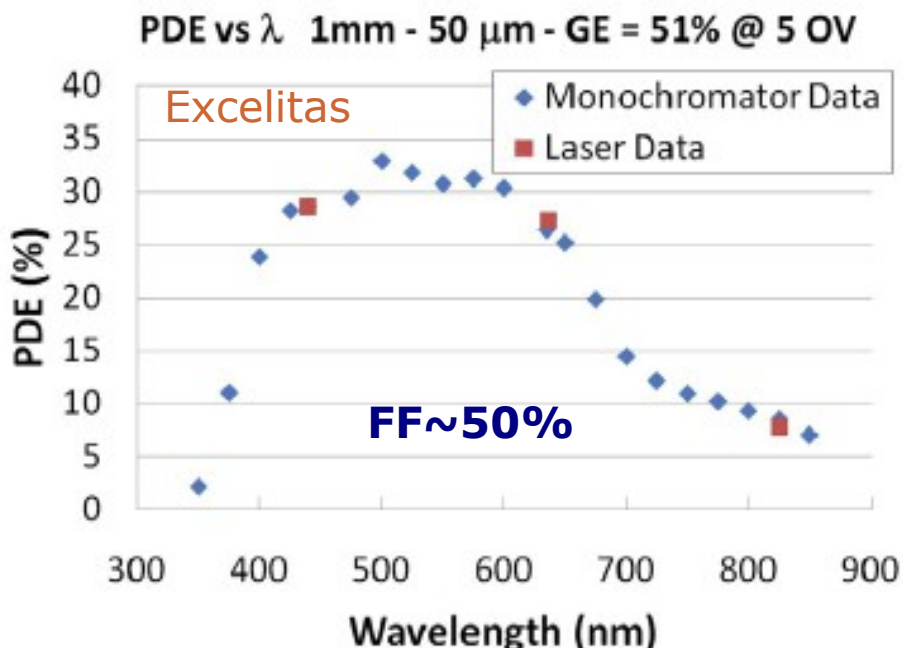
p-on-n structure



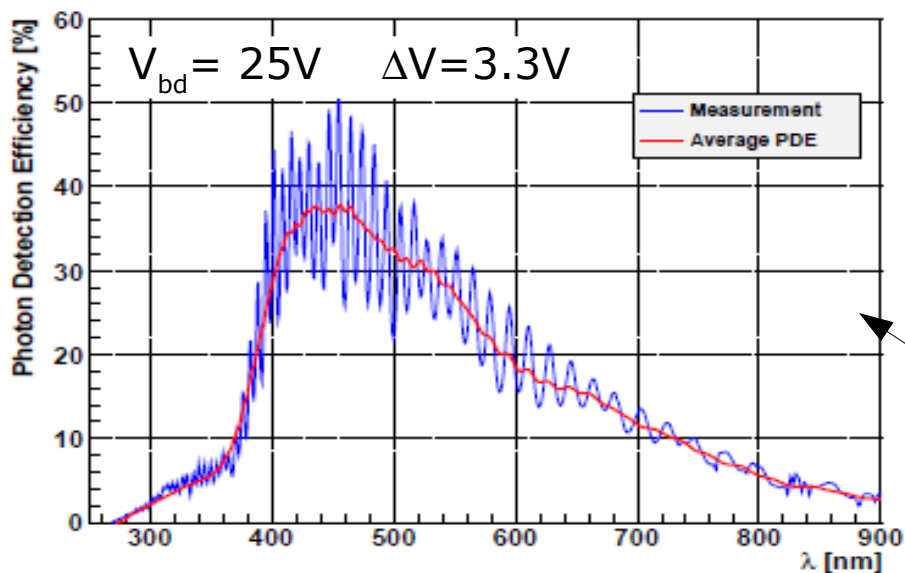
Note: geometrical fill factor included

# Improving PDE

Barlow - LIGHT 2011



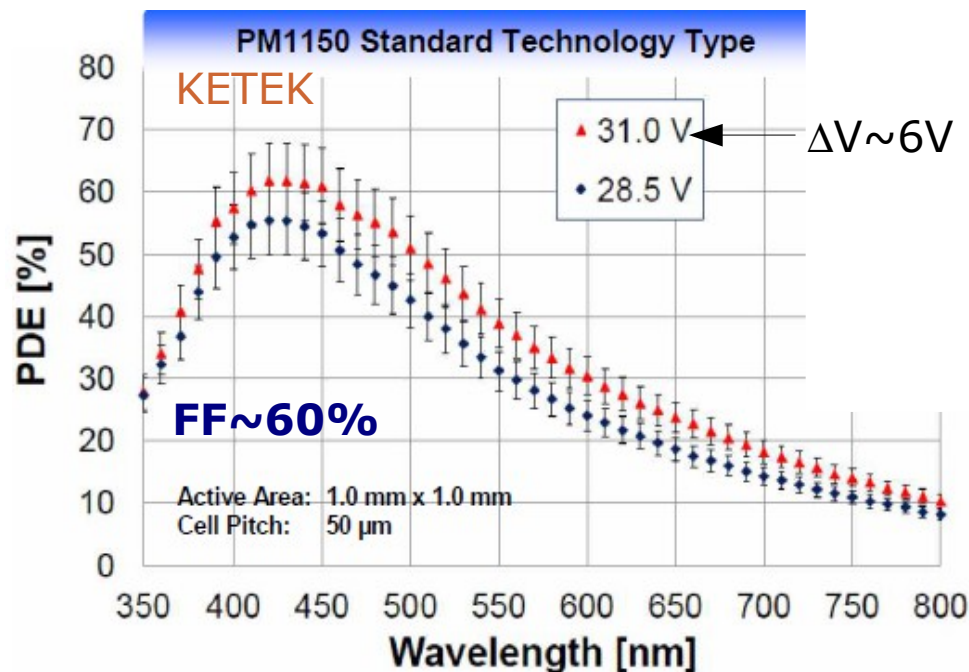
Photon Detection Efficiency



T.Frach 2012 JINST 7 C01112

- PDE peak constantly improving for many devices
- every manufacturer shape PDE for matching target applications
- UV SiPM eg from MePhi/Excelitas (see *E.Popova at NDIP 2011*)
- DUV SiPMs in development too

F.Wiest - AIDA 2012 at DESY



dSiPM (latest sensor 2011)

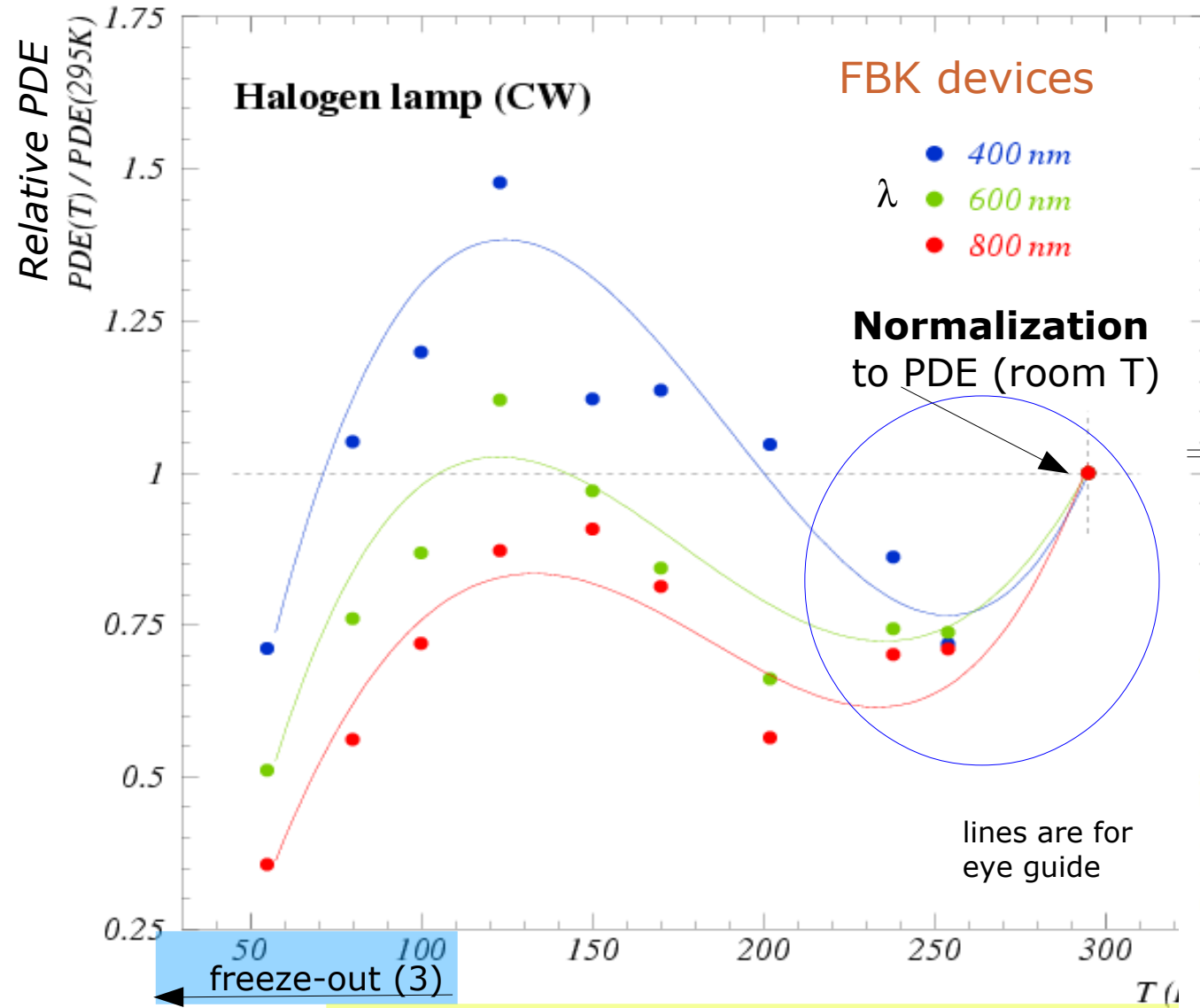
- up to now no optical stack optimization
- no anti-reflecting coating
- potential improvement up to 60% peak PDE (*Y.Haemish at AIDA 2012*)

# PDE vs T ( $\Delta V$ constant)

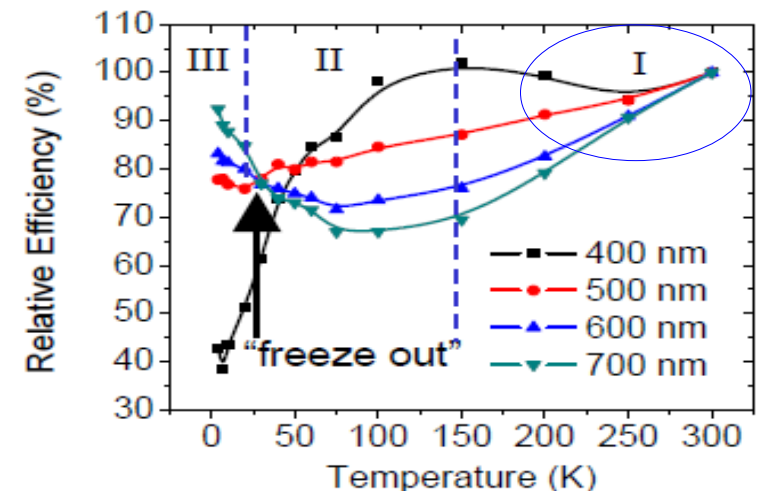
G.C. et al NIM A628 (2011) 389

When T decreases:

- 1) silicon  $E_{\text{gap}}$  increasing
  - larger attenuation length
  - lower QE (for larger  $\lambda$ )
- 2) mobility increasing
  - larger impact ionization
  - larger trigg. avalanche  $P_{01}$
- 3) carriers freeze-out
  - onset below 120K
  - loss of carriers



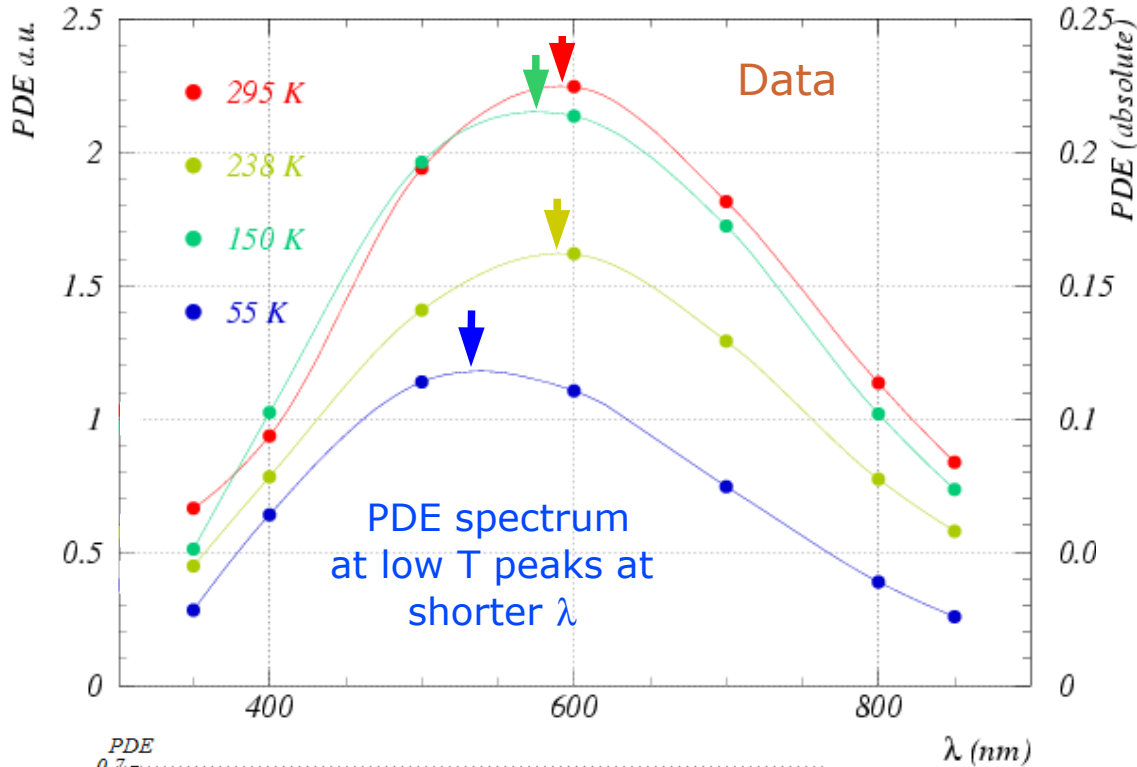
RMD APD at  $400\text{nm} < \lambda < 700\text{nm}$   
 Johnson et al, IEEE NSS 2009



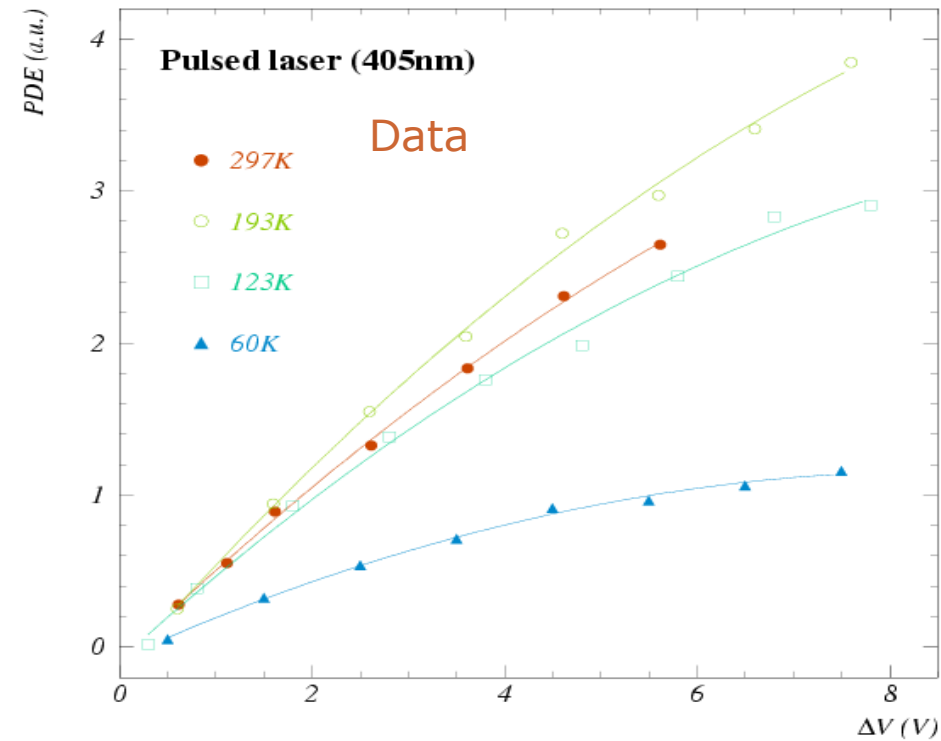
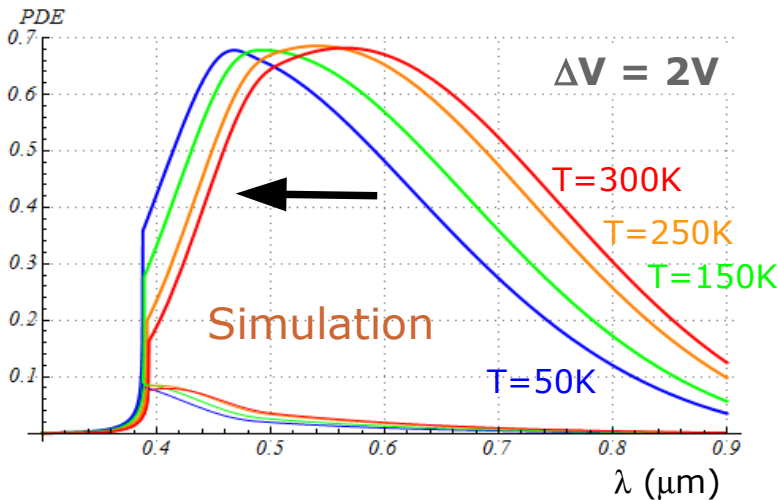
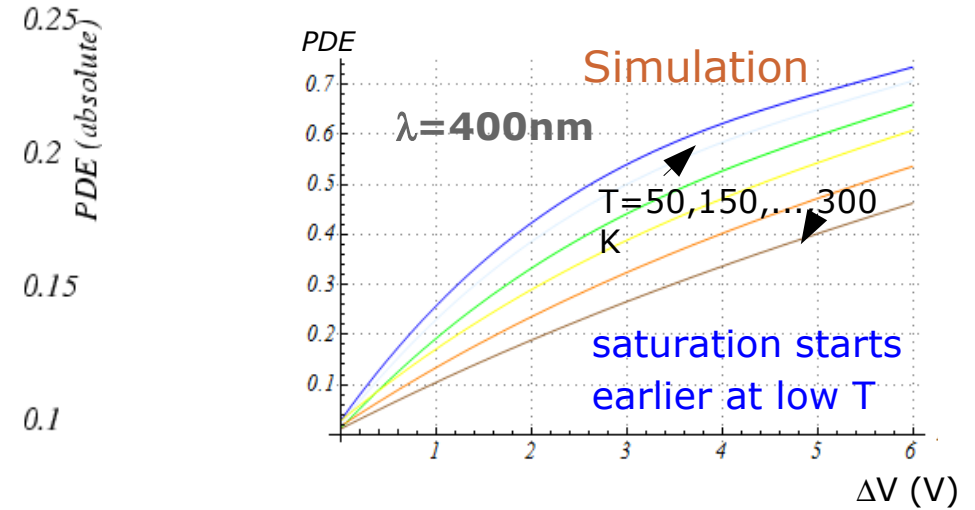
Additional effects in APD  
 (depletion region depends on T, ...)

# PDE dependences, changing with T

## PDE vs $\lambda$ ( $\Delta V$ constant)



## PDE $\Delta V$ vs ( $\lambda$ constant)

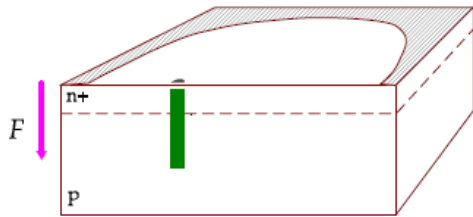


# Timing

- SiPM are **intrinsically very fast**
  - jitter (gaussian) below **100ps**, depending on  $\Delta V$
  - but also** → non-gaussian tails up to **O(ns)**, depending on wavelength
- **Timing measurement:**
  - use of fast signal shape component
  - use waveform, better than CFD (much than ToT)



# GM-APD avalanche development



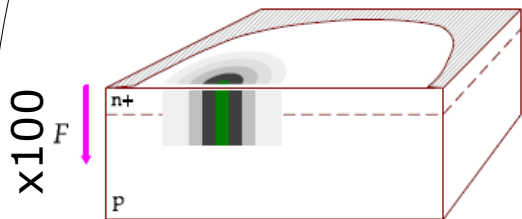
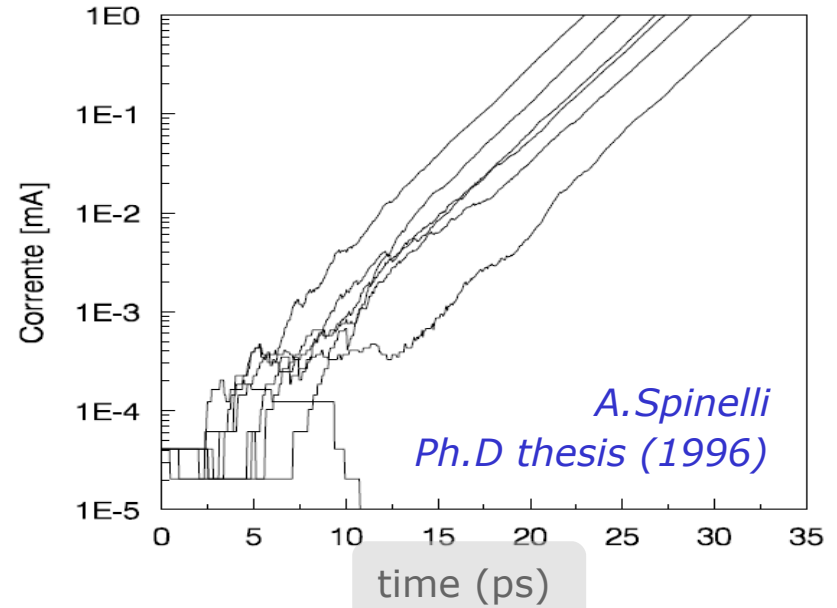
## Longitudinal multiplication

Duration  $\sim$  few **ps**  
Internal current up to  $\sim$  few  **$\mu$ A**

(1) Avalanche "seed": free-carrier concentration rises exponentially by "**longitudinal**" multiplication

(1') Electric field locally lowered (by **space charge R effect**) towards breakdown level

Multiplication is self-sustaining  
Avalanche current steady until new multiplication triggered in near regions



## Transverse multiplication

Duration  $\sim$  few **100ps**  
Internal current up to  $\sim$  several **10 $\mu$ A**

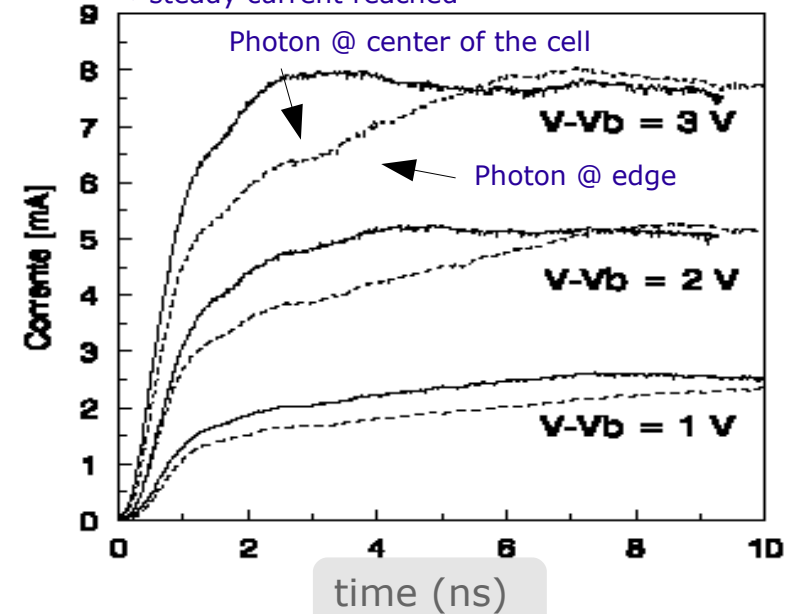
(2) **Avalanche spreads "transversally"** across the junction

(diffusion speed  $\sim$  up to **50 $\mu$ m/ns** enhanced by multiplication)

(2') **Passive quenching mechanism** effective after transverse **avalanche size  $\sim$ 10 $\mu$ m**

(if no quench, avalanche spreads over the whole active depletion volume  $\rightarrow$  avalanche current reaches a final saturation steady state value)

Simulation w/o quenching:  
 $\rightarrow$  steady current reached



# GM-APD avalanche transverse propagation

Avalanche transverse propagation by a kind of **shock wave**: the **wavefront** carries a **high density of carriers** and high E field gradients (inside: carriers' density lower and E field decreasing toward breakdown level)

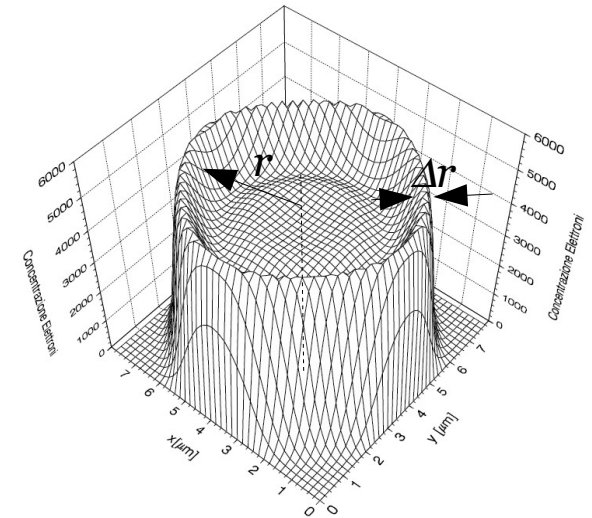
$$\frac{dS}{dt} = \frac{d}{dt} 2\pi r(t) \Delta r = 2\pi v_{diff} \Delta r = 4\pi \Delta r \sqrt{\frac{D}{\tau}}$$

Rate of current production:  $\frac{dI}{dt} = \frac{dI}{dS} \frac{dS}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$

$$\frac{dI}{dS} = J = \frac{V_{bias}}{R_{sp}(S)}$$

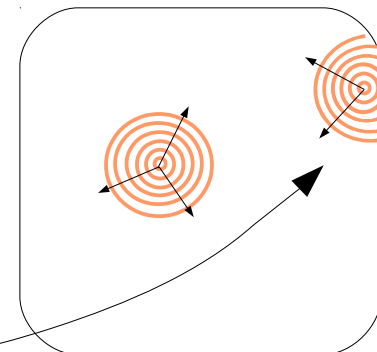
Internal **current rising front**:  
the **faster it grows, the lower the jitter**  
 $dI/dt \rightarrow$  understand/engineer timing features of SiPM cells

- $\rightarrow$  timing resolution improves at **high  $V_{bias}$**
- $\rightarrow$  **E field profile affects  $\tau$  and  $R_{sp}$**  (wider E field profile  $\rightarrow$  smaller R) (should be engineered when aiming at ultra-fast timing)
- $\rightarrow$  **T dependence of timing** through  $\tau$  and D
- $\rightarrow$  slower growth at GAPD cell edges  $\rightarrow$  **higher jitter at edges**  
reduced length of the propagation front



$S$  = surface of wavefront (ring of area  $2\pi r \Delta r$ )  
 $R_{sp}(S)$  = space charge resistance  $\sim w^2/2\epsilon v \sim O(50 \text{ k}\Omega \mu\text{m}^2)$   
 $v_{diff} \sim O(\text{some } 10 \mu\text{m}/\text{ns})$   
 $D$  = transverse diffusion coefficient  $\sim O(\mu\text{m}^2/\text{ns})$   
 $\tau$  = longitudinal (exponential) buildup time  $\sim O(\text{few ps})$

$$\tau \sim \frac{1}{1 - (E_{max}/E_{breakdown})^n}$$



SiPM cell

# GM-APD timing jitter: fast and slow components

## 1) Fast component: gaussian with time scale $O(100\text{ps})$

Statistical fluctuations in the avalanche:

- **Longitudinal** build-up (minor contribution)
- **Transversal** propagation (main contribution):
  - via multiplication assisted diffusion (dominating in few  $\mu\text{m}$  thin devices)  
*A.Lacaita et al. APL and El.Lett. 1990*
  - via photon assisted propagation (dominating in thick devices –  $O(100\mu\text{m})$ )  
*PP.Webb, R.J. McIntyre RCA Eng. 1982*  
*A.Lacaita et al. APL 1992*

**Fluctuations** due to  
**a) impact ionization statistics**

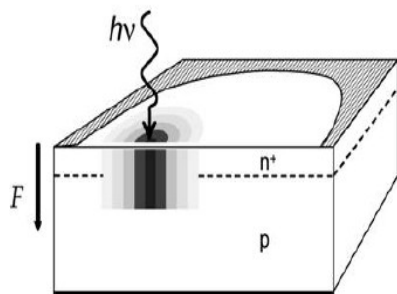
**b) variance of longitudinal position** of photo-generation: finite drift time even at saturated velocity note: saturated  $v_e \sim 3 v_h$  (**n-on-p** are faster in general)

→ Jitter at minimum →  **$O(10\text{ps})$**  (very low threshold → not easy)

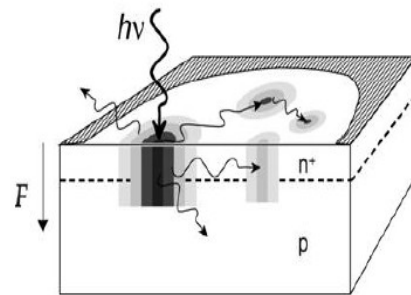
**Fluctuations** due to  
**c) variance of the transverse diffusion speed  $v_{diff}$**

**d) variance of transverse position** of photo-generation: slope of current rising front depends on transverse position

→ Jitter →  **$O(100\text{ps})$**  (usually threshold set high)



Multiplication assisted diffusion



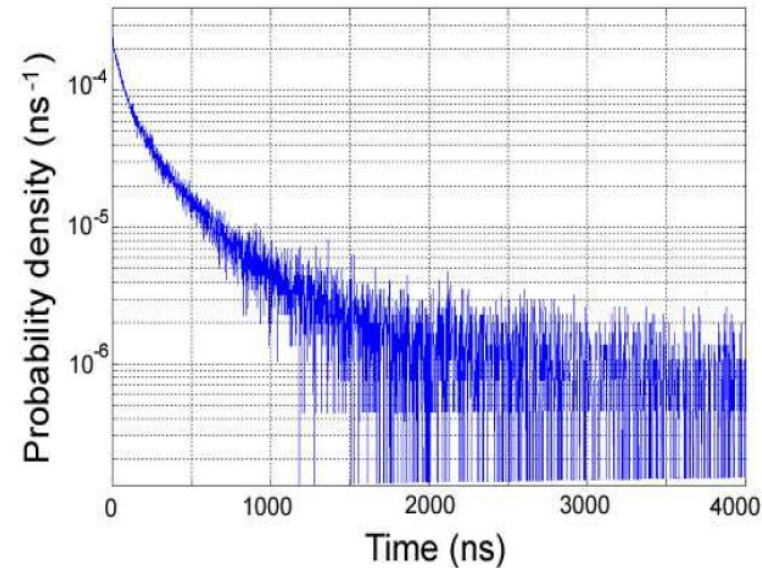
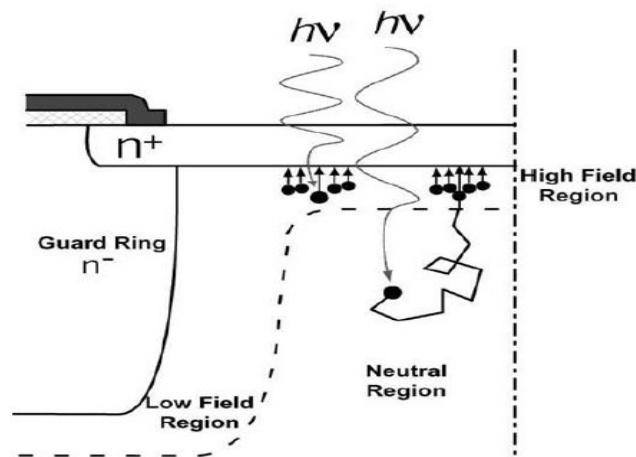
Photon assisted propagation

# GM-APD timing jitter: fast and slow components

## 2) Slow component: non-gaussian tails with time scale O(ns)

Carriers photo-generated in the neutral regions above/beneath the junction and reaching the electric field region by diffusion

*G.Ripamonti, S.Cova Sol.State Electronics (1985)*



*S.Cova et al. NIST Workshop on SPD (2003)*

tail lifetime:  $\tau \sim L^2 / \pi^2 D \sim$  up to some ns

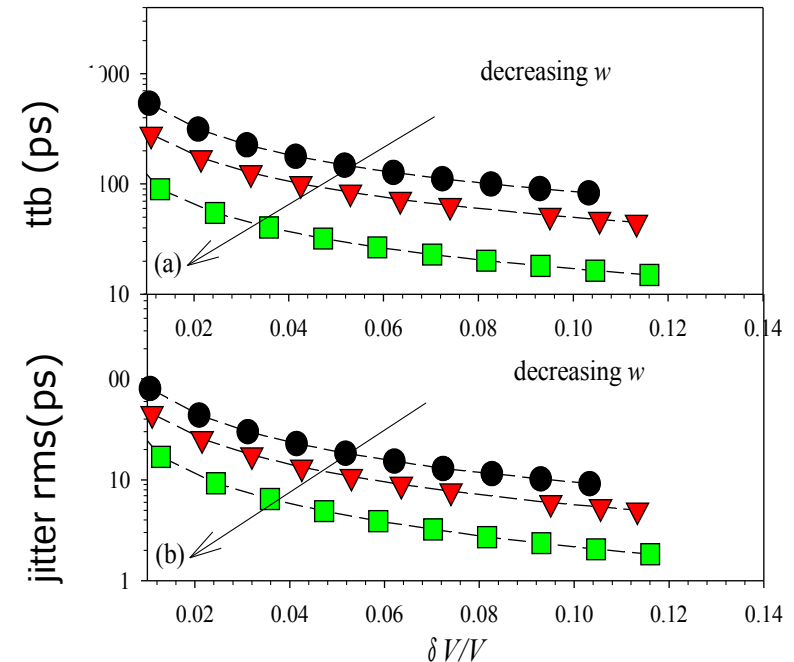
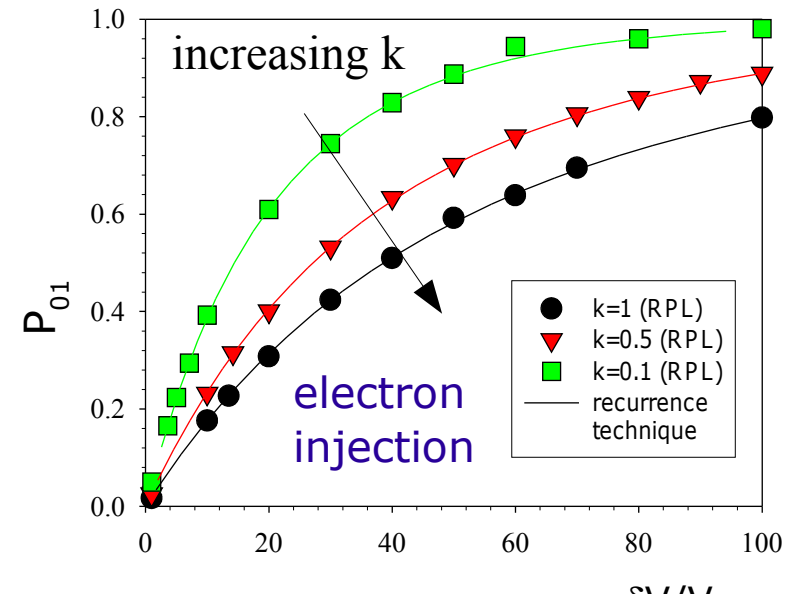
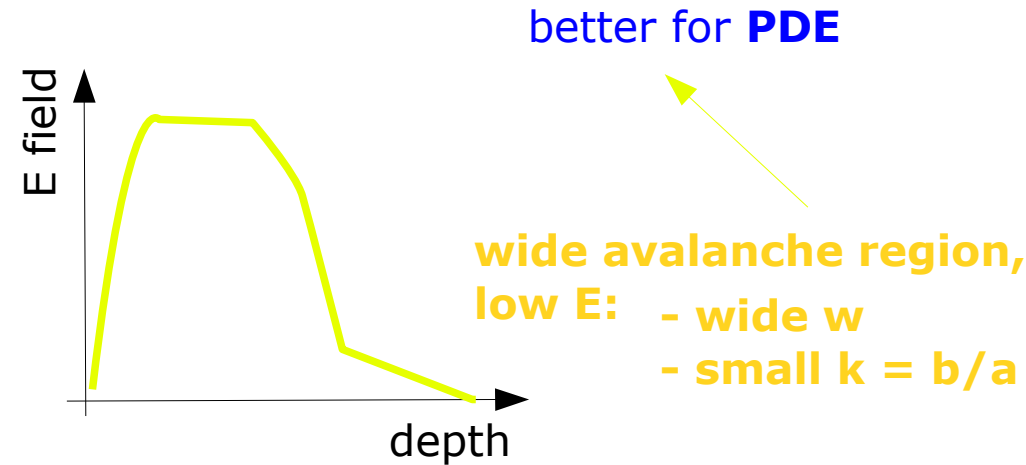
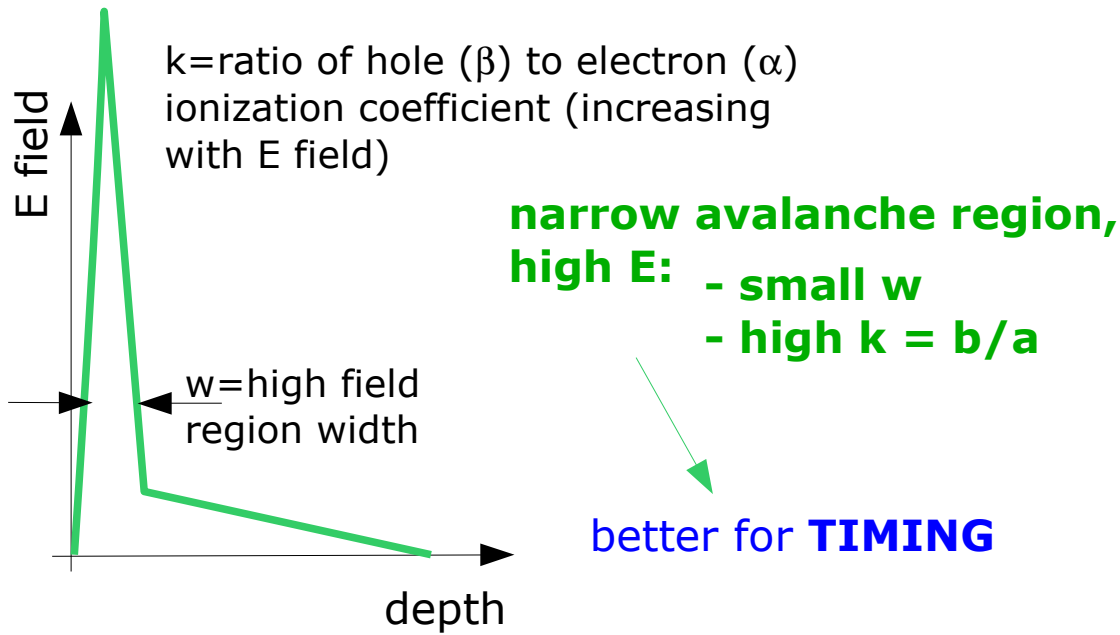
L = effective neutral layer thickness

D = diffusion coefficient

- **Neutral regions** underneath the junction : timing tails for long wavelengths
- **Neutral regions** in APD entrance: timing tails for short wavelengths

# PDE vs timing optimization

C.H.Tan et al IEEE J.Quantum Electronics 13 (4) (2007) 906



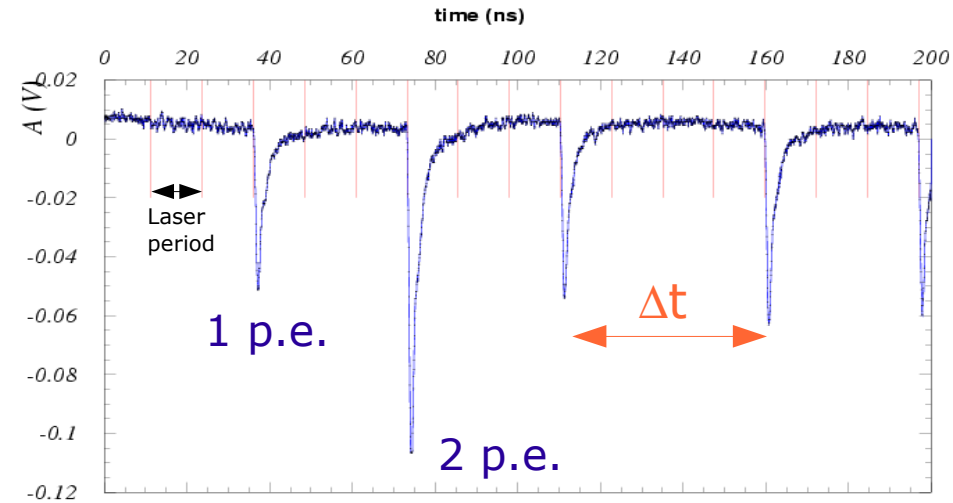
Plots are courtesy of C.H.Tan

# Waveform analysis: optimum timing filter

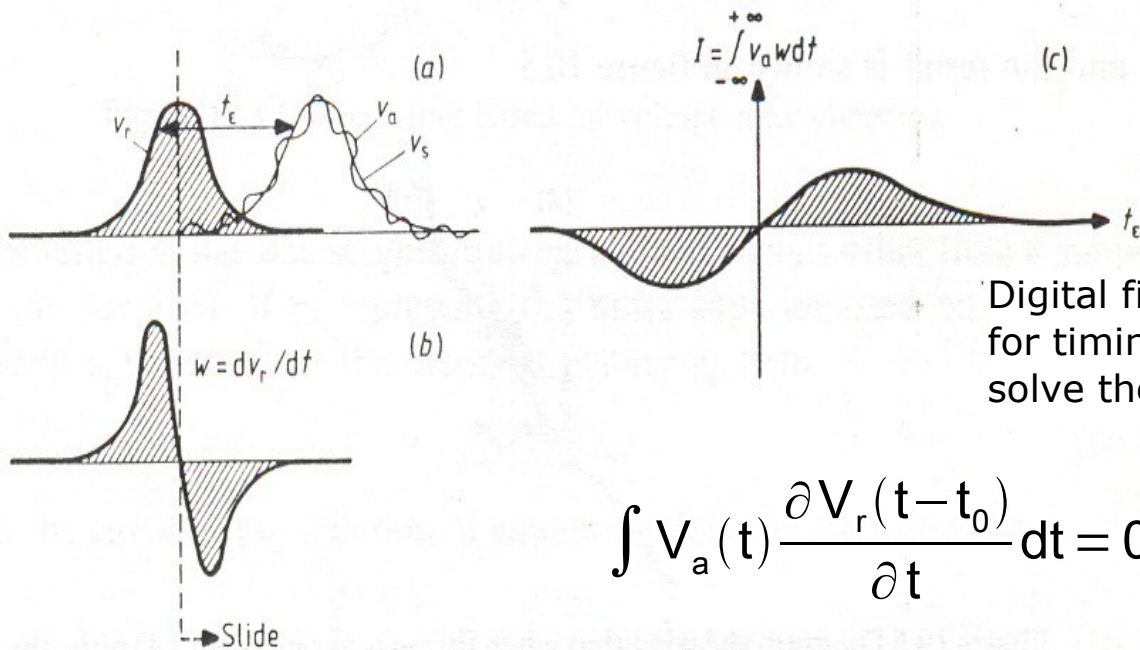
Example of intrinsic SPTR measurement from  $\Delta t$  of consecutive pulses by laser shots

Different algorithms to reconstruct the time of the pulses:

- ✗ parabolic fit to find the peak maximum
- ✗ CFD (digital)
- ✗ average of time samples weighted by the waveform derivative
- ✓ digital filter: weighting by the derivative of a reference signal  
→ optimum against (white) noise (if signal shape fixed)



*G.C. et al NIMA 581 (2007) 461*



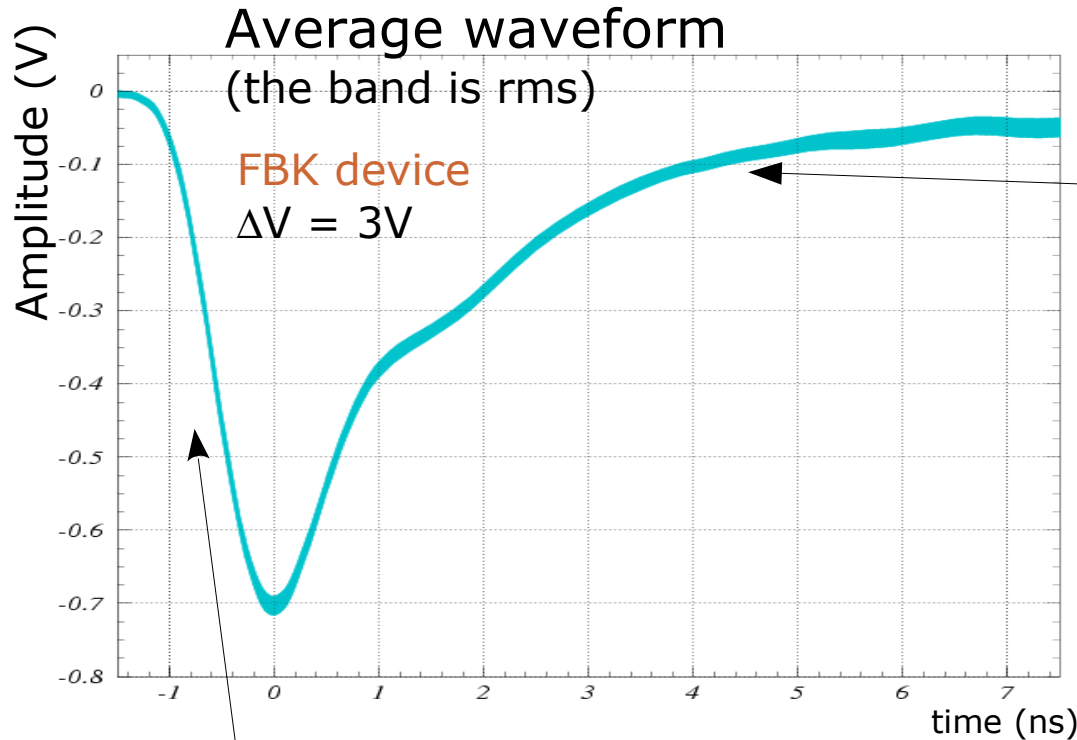
Digital filter to minimize N/S for timing measurements:  
solve the following equation on  $t_0$  :

$$\int V_a(t) \frac{\partial V_r(t-t_0)}{\partial t} dt = 0$$

$V_a$  = measured signal (includes noise)  
 $V_r$  = reference signal  
 $t_0$  = reference time

see e.g. Wilmshurst "Signal recovery from noise in electronic instrumentation"

# Waveform (single p.e.)



Falling signal shape fluctuates considerably (due eg to after-pulses)  
→ signal tail is non useful for timing, if not detrimental

note: using **Time-over-Threshold** method for slew correction might lead to worse resolution

Reminder:

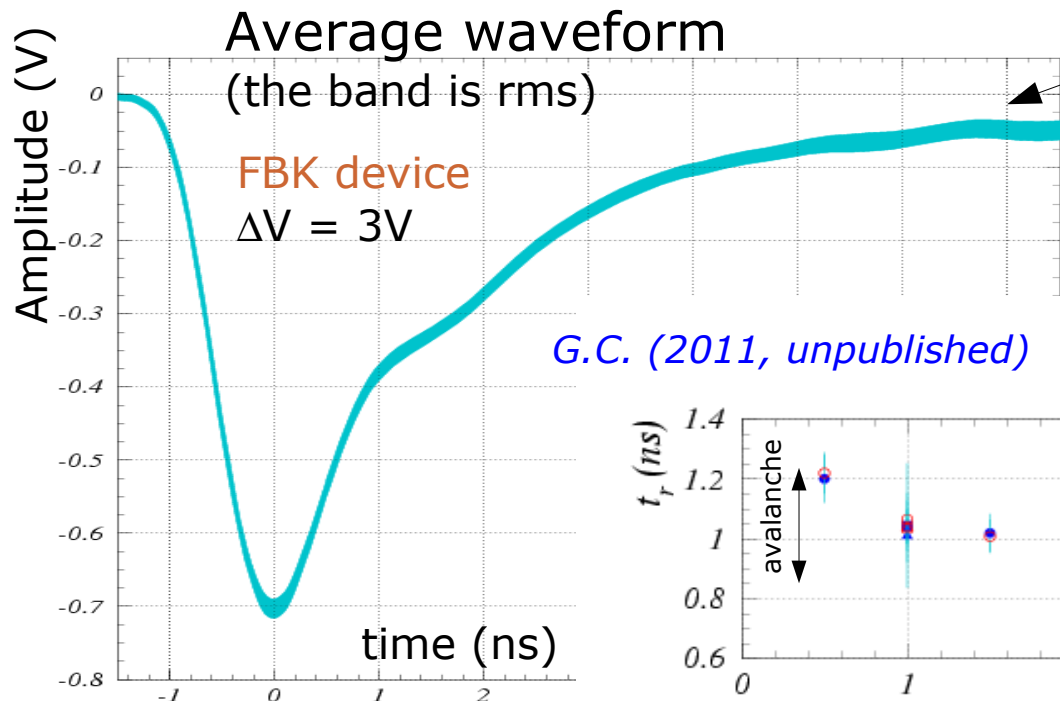
$$\frac{dI}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$$
$$\tau \sim \frac{1}{1 - (E_{max}/E_{breakdown})^n}$$

Rise-time depends on  $\Delta V$ ,  $T$  and **impact position** ie **signal shape is not constant**, then:

- 1) CFD method only partially effective in canceling time walk effects
- 2) any digital timing filter should account for shape variations ( $\Delta V$ ,  $T$ )

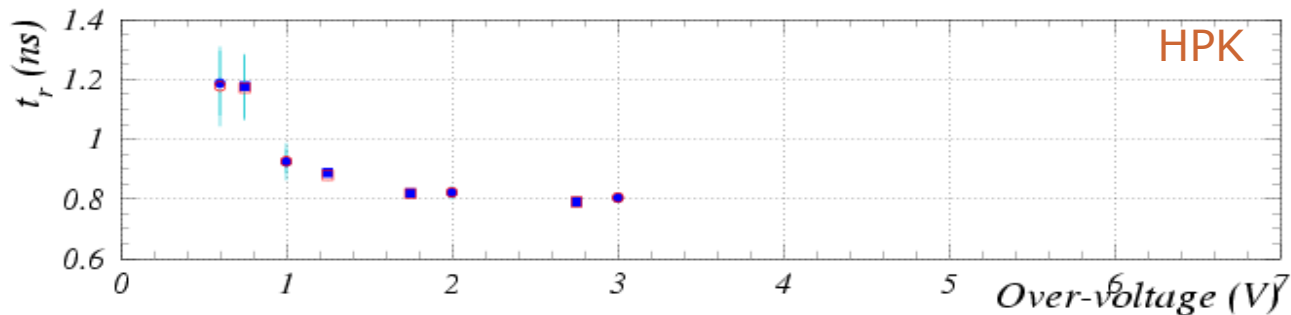
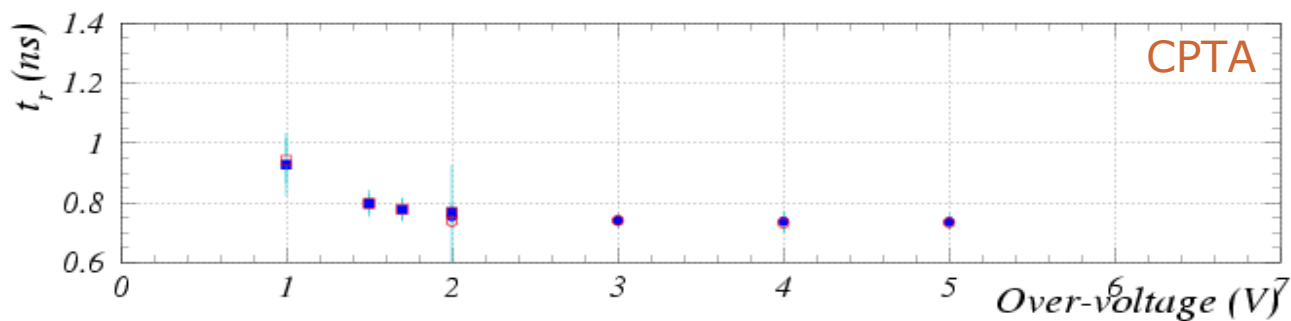
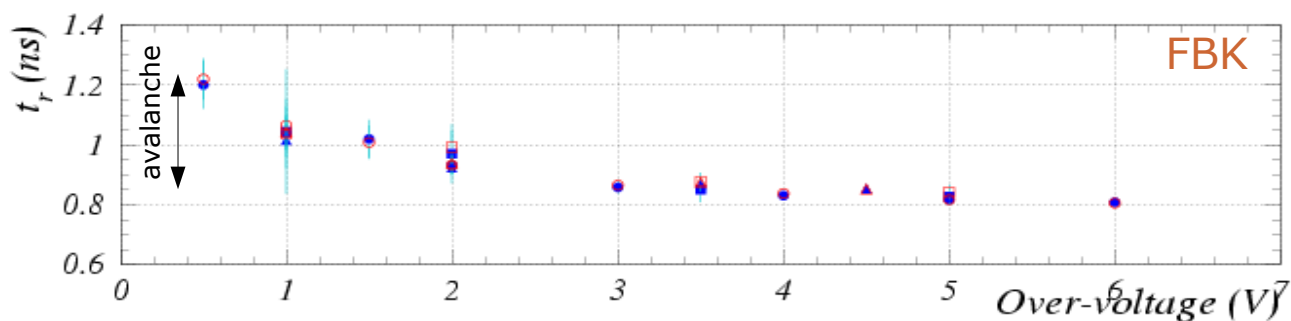
For comparison about **waveform method** and various digital algorithms see *Ronzhin et al NIM A 668 (2012) 94*

# Waveform analysis: 1 p.e. reference signal



Additional contribution to rms  
(after-pulses)

Rise time (10%-90%)  
(dominated by electronics contribution)



Reminder:

$$\frac{dI}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$$

$$\tau \sim \frac{1}{1 - (E_{max}/E_{breakdown})^n}$$

For comparison about rise-time of HKP devices see  
[P.Avella et al doi:10.1016/j.nima.2011.11.049](https://doi.org/10.1016/j.nima.2011.11.049)



# Single Photon Time Resolution = gaussian + tails

Time resolution of SiPM is not just a gaussian, but gaussian + tails (in particular at long wavelengths)

*G.C. et al NIMA 581 (2007) 461*

Data at  $\lambda=400\text{nm}$

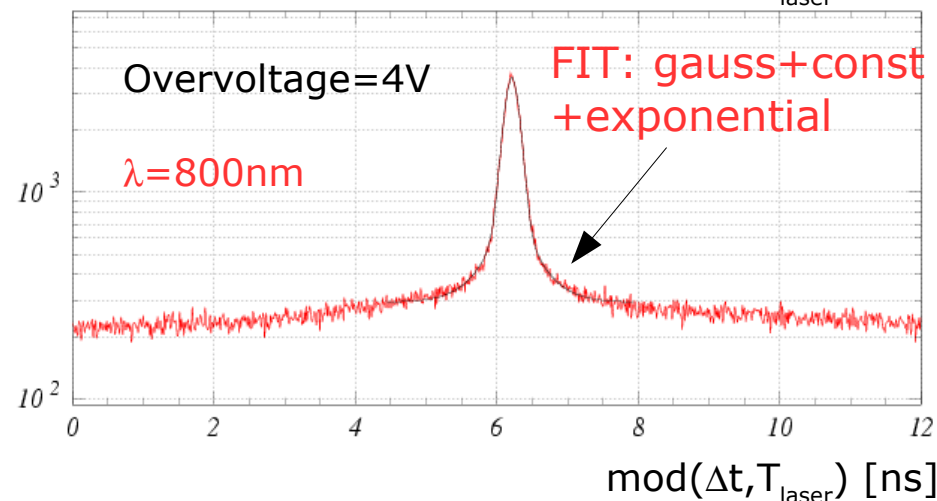
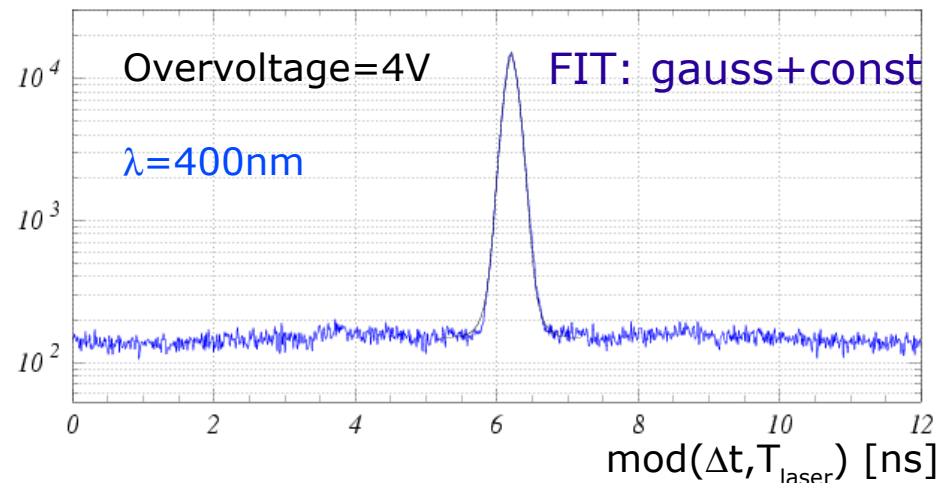
A simple **gaussian component** fits fairly

Data at  $\lambda=800\text{nm}$

fit gives reasonable  $\chi^2$  in case of an **additional exponential term**  $\exp(-|\Delta t|/\tau)$  summed with a weight

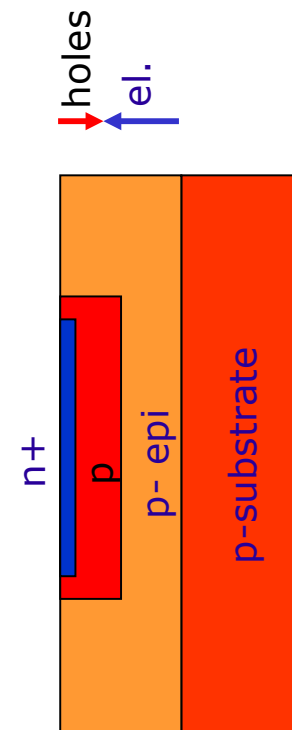
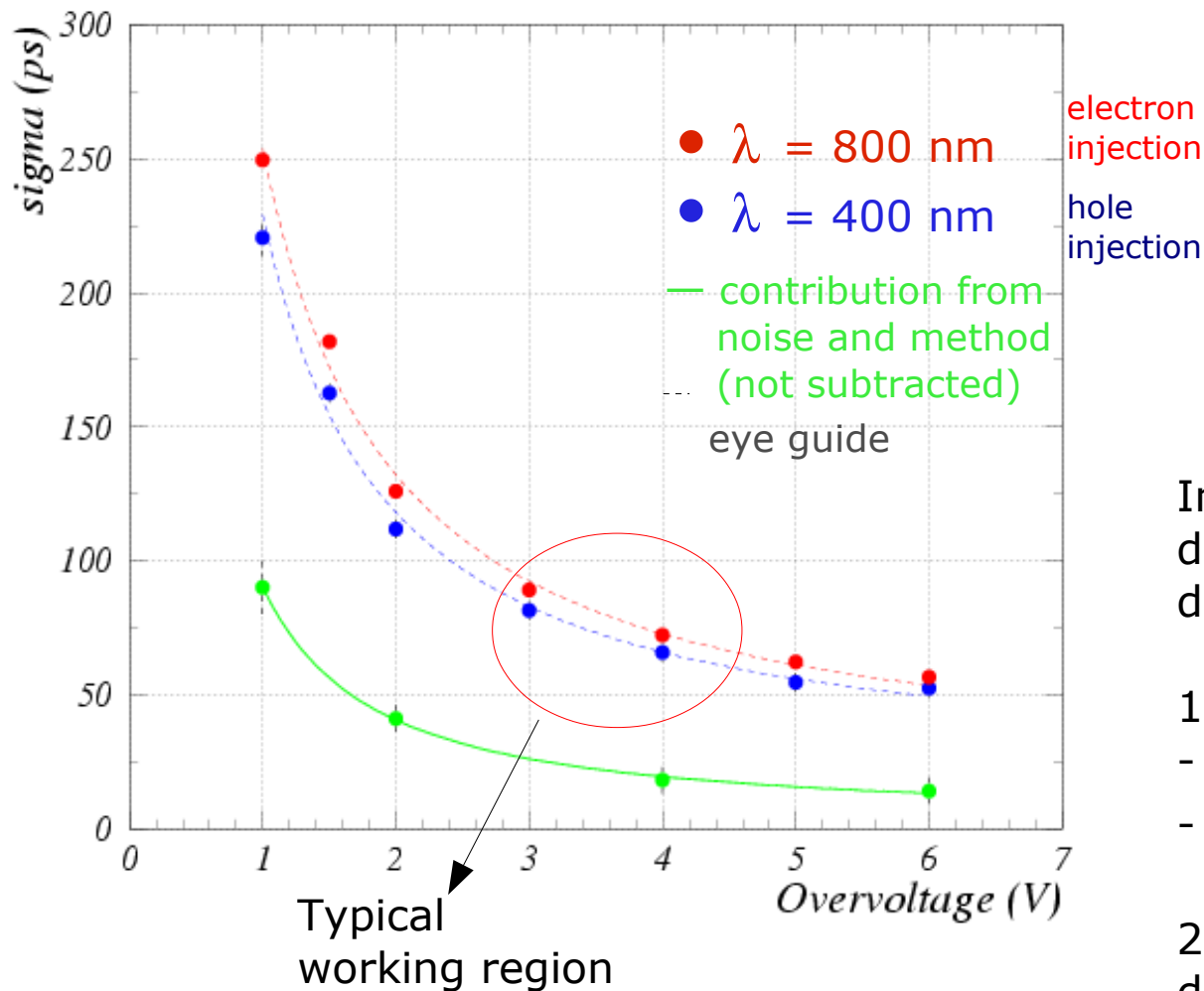
- $\tau \sim 0.2 \div 0.8\text{ns}$  (depending on device) in rough agreement with diffusion tail lifetime:  $\tau \sim L^2 / \pi^2 D$  wher L is the diffusion length
- Weight of the **exp. tail**  $\sim 10\% \div 30\%$  (depending on device)

**Gaussian** + **Tails (long  $\lambda$ )**  
rms  $\sim 50\text{-}100\text{ ps}$   $\sim \exp(-t / O(\text{ns}))$   
contrib. several % for long wavelengths



Distributions of the difference in time between successive peaks

# SPTR: FBK devices – shallow junction



In general due to drift, resolution differences

1) **high field junction position**

- shallow junction:  $\sigma_t^{\text{red}} > \sigma_t^{\text{blue}}$

- buried junction:  $\sigma_t^{\text{red}} < \sigma_t^{\text{blue}}$

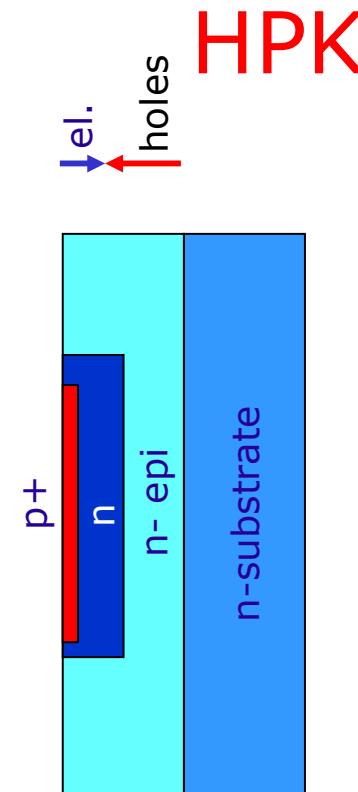
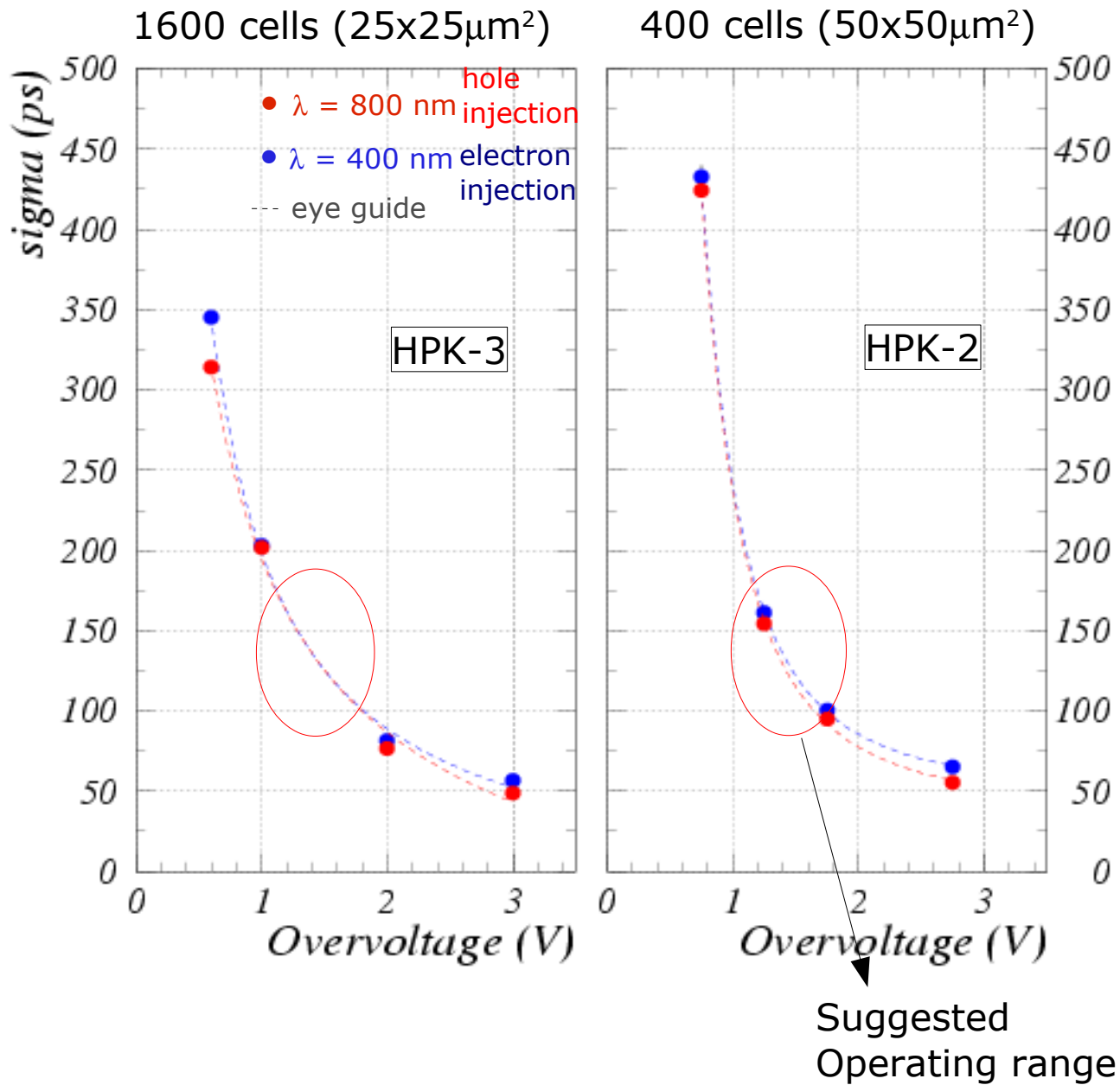
2) **n<sup>+</sup>-on-p smaller jitter than p<sup>+</sup>-on-n** due to electrons drifting faster in depletion region (but  $\lambda$  dependence)

3) above differences more relevant in **thick devices than thin**

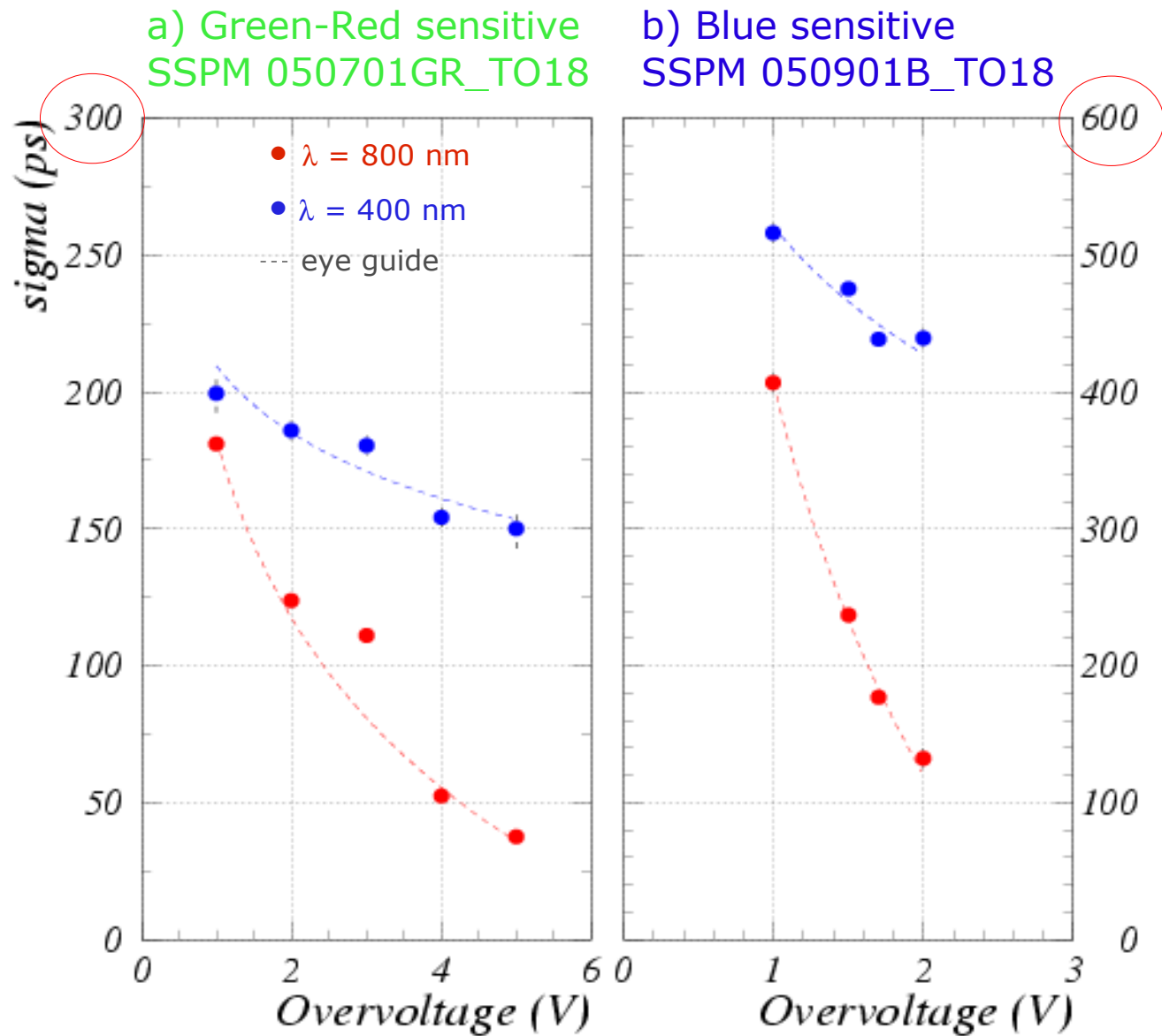
*G.C. et al NIMA 581 (2007) 461*

NOTE: good timing performances kept up to 10MHz/mm<sup>2</sup> photon rates

# SPTR: Hamamatsu



# SPTR: CPTA/Photonique – thick structures



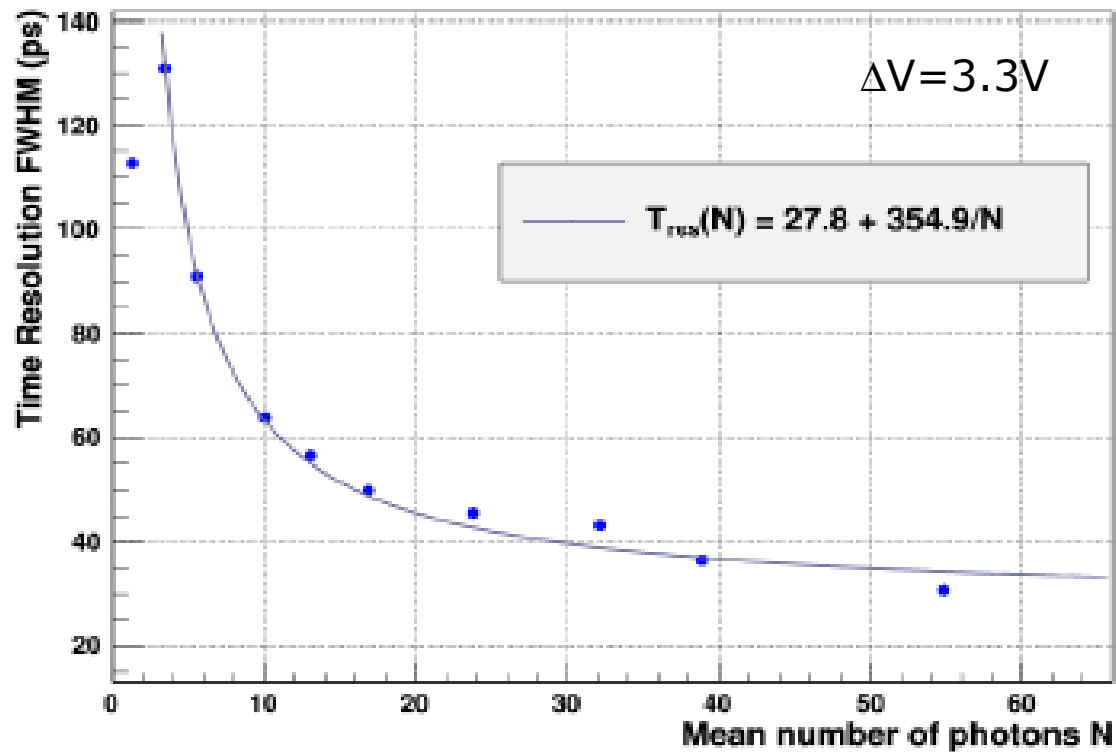
- **thick structures**  
- **deep junctions**

a)  $n^+$ -on-p  
→ electrons drift

b)  $p^+$ -on-n  
→ holes drift ( $v_e/3$ )

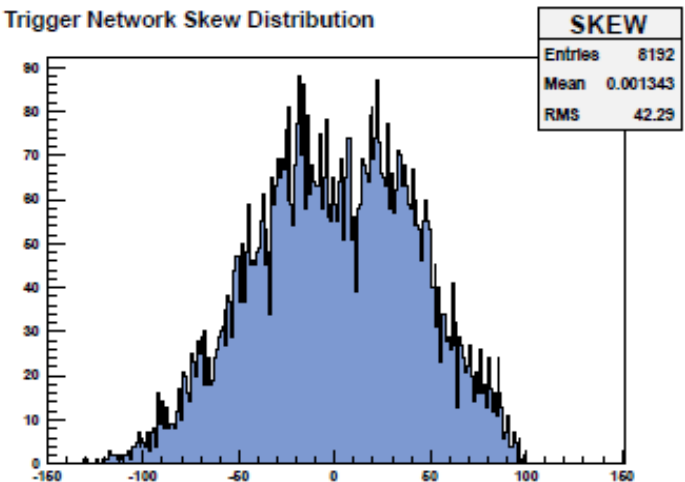
# dSiPM timing resolution

Time Resolution



*T.Frach at LIGHT 2011*

Trigger Network Skew Distribution

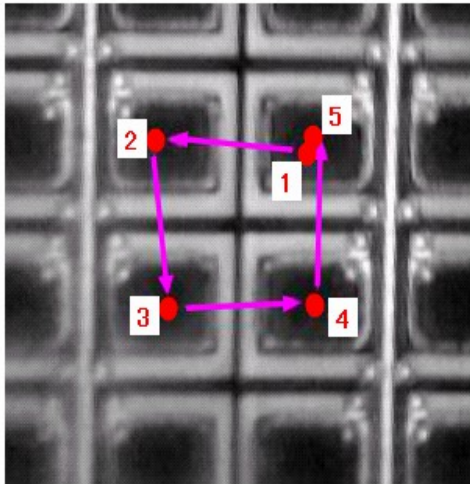


- Sensor triggered by attenuated laser pulses at first photon level
- Laser pulse width: 36ps FWHM,  $\lambda = 410\text{nm}$
- Contribution to time resolution (FWHM):

SPAD: 54ps, trigger network: 110ps, TDC: 20ps

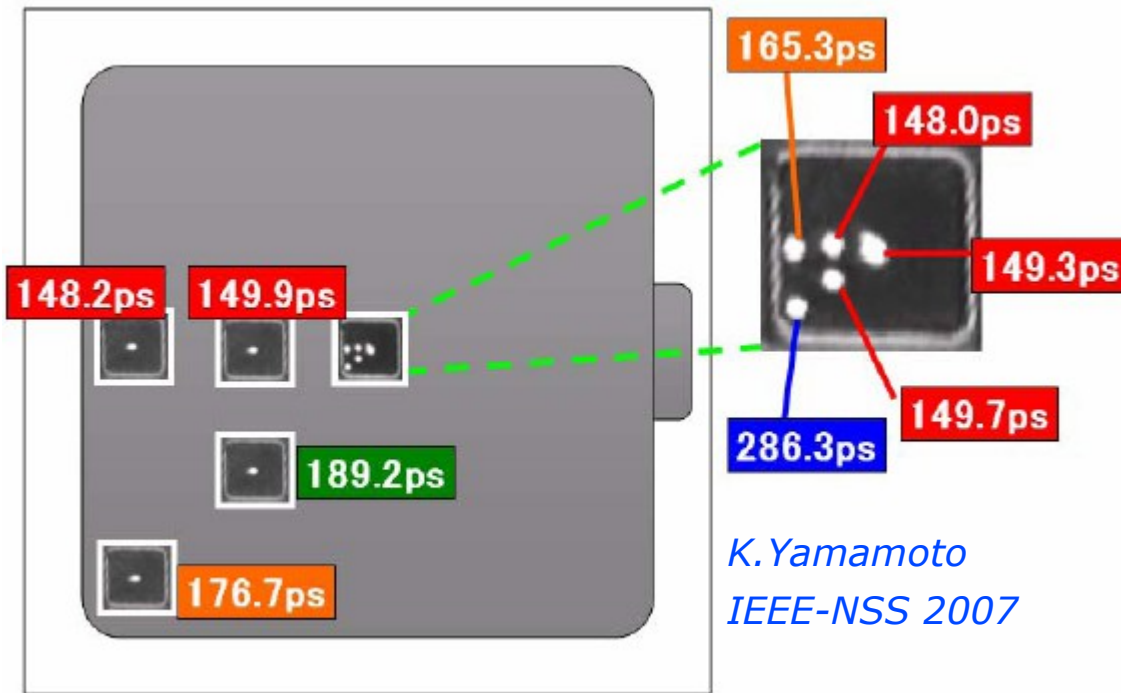
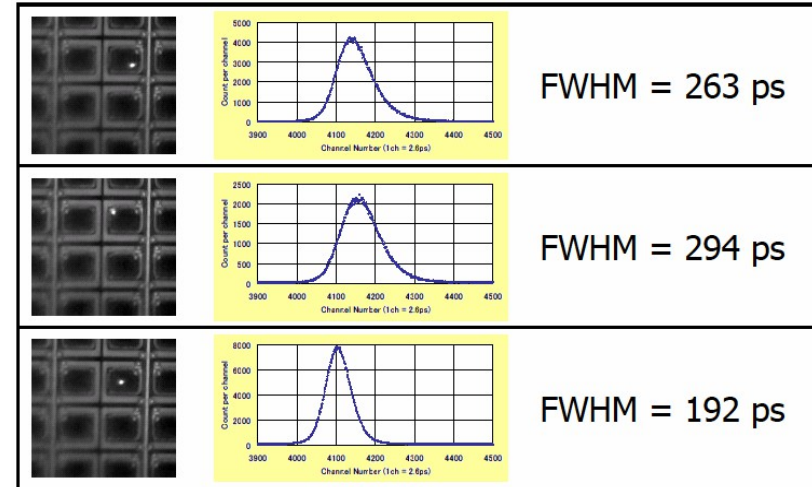
- Trigger network skew currently limits the timing resolution

# SPTR: position dependence → cell size



	FWHM (ps)	FWTM (ps)
1	199	393
2	197	389
3	209	409
4	201	393
5	195	383

*K. Yamamoto PD07*

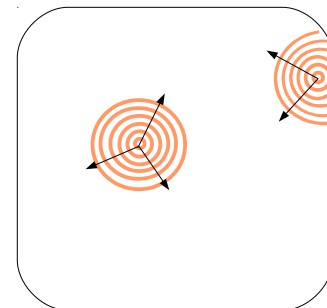


Larger jitter if photo-conversion at the border of the cell

Due to:  
1) slower avalanche front propagation

2) lower E field at edges

→ cfr PDE vs position



Data include the system jitter (common offset, not subtracted)

# SPTR: timing at low T

## Timing: improves at low T

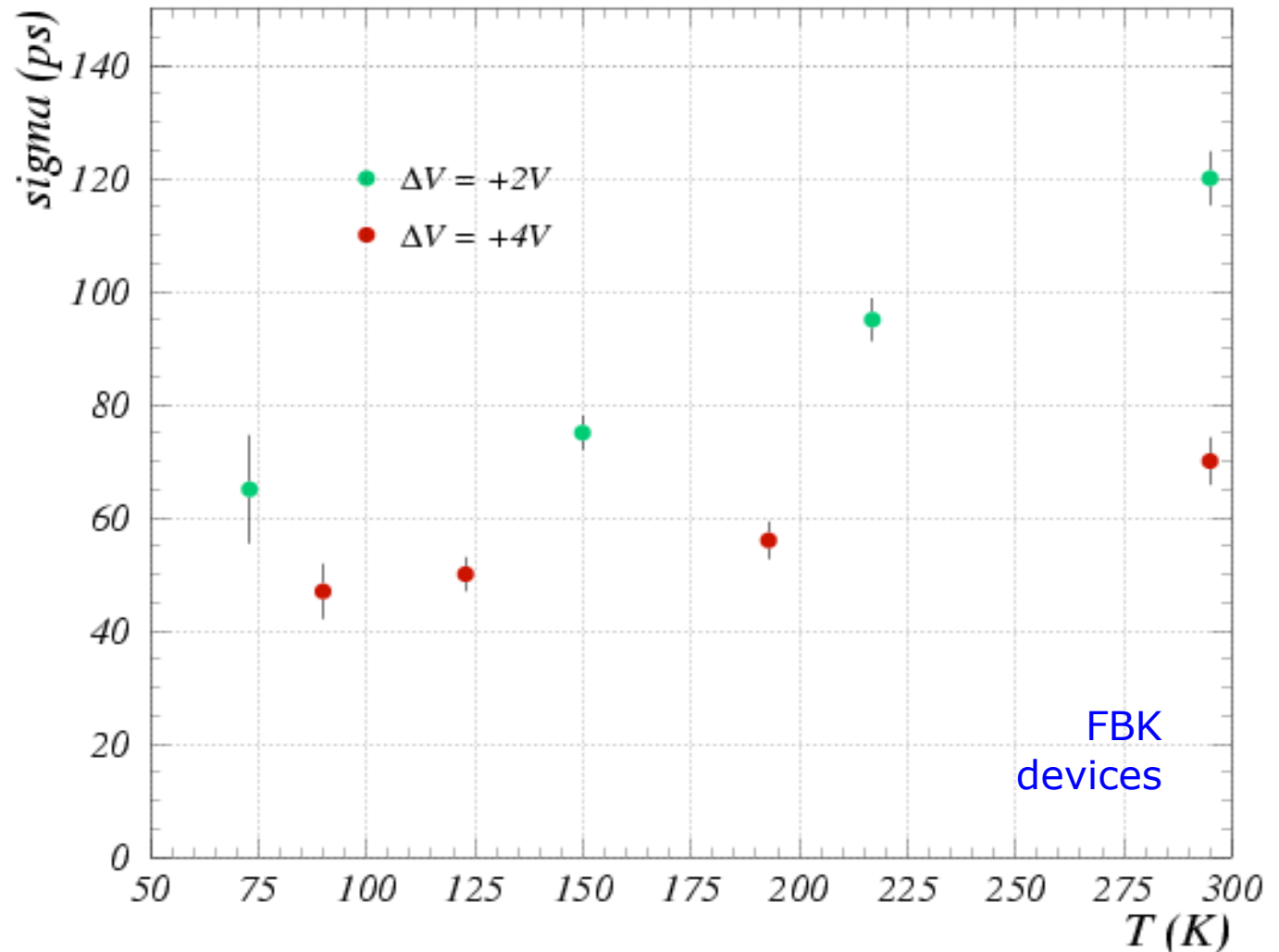
Lower jitter at low T due to **higher mobility**:

- a) avalanche process is faster
- b) reduced fluctuations

(Over-voltage fixed)

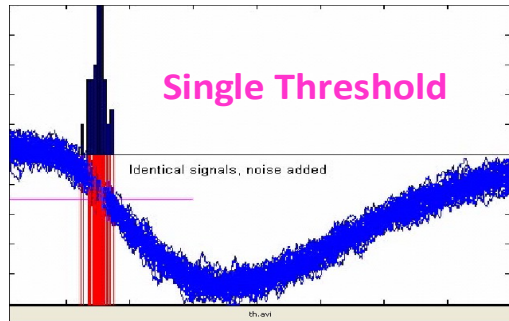
Note:

$$\frac{dI}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$$



G.C. (2011, unpublished)

# Optimizing signal shape for timing



## Timing by (single) threshold:

→ time spread proportional to 1/rise-time and noise

$$\sigma_{time} = \frac{\sigma_{amplitude}}{\frac{df(t)}{dt}}$$

## Timing with optimum filtering:

→ best resolution with  $f'(t)$  weighting function

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{\int dt \left[ \frac{df(t)}{dt} \right]^2}$$

## Pulse sampling and Waveform analysis:

Sample, digitize, fit the (known) waveform  
→ get time and amplitude

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{N_{samples} \int dt \left[ \frac{df(t)}{dt} \right]^2}$$

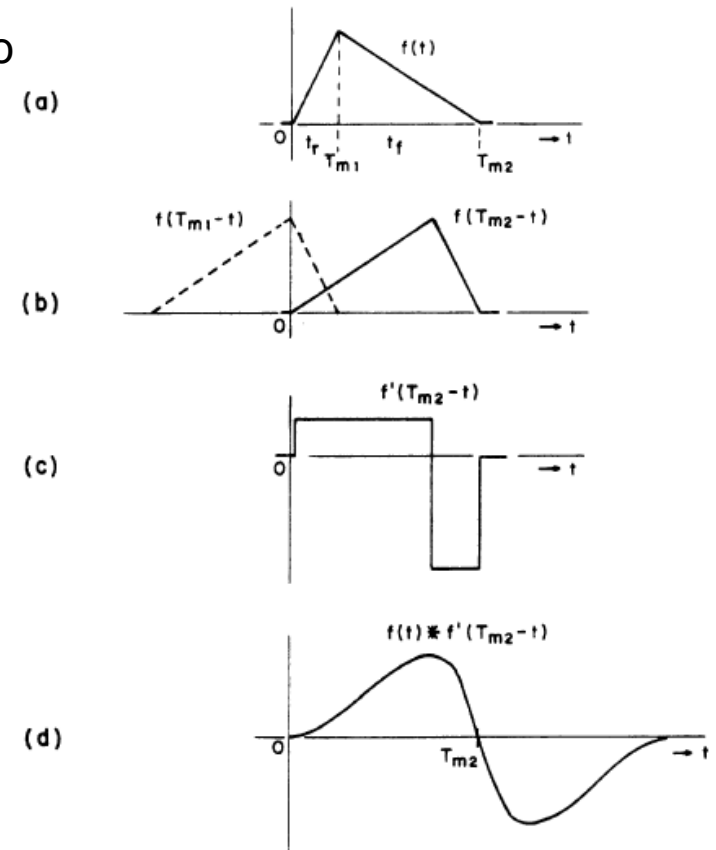


Fig. 7. Optimum filter for timing in presence of white noise (method of derivation).

- (a) signal waveform
- (b) optimum filter for amplitude measurements.
- (c) optimum filter for timing - derivative of (b).
- (d) output waveform.

V.Radeka IEEE TNS 21 (1974)...



# Optimizing signal shape for timing

Single cell model  $\rightarrow (R_d || C_d) + (R_q || C_q)$

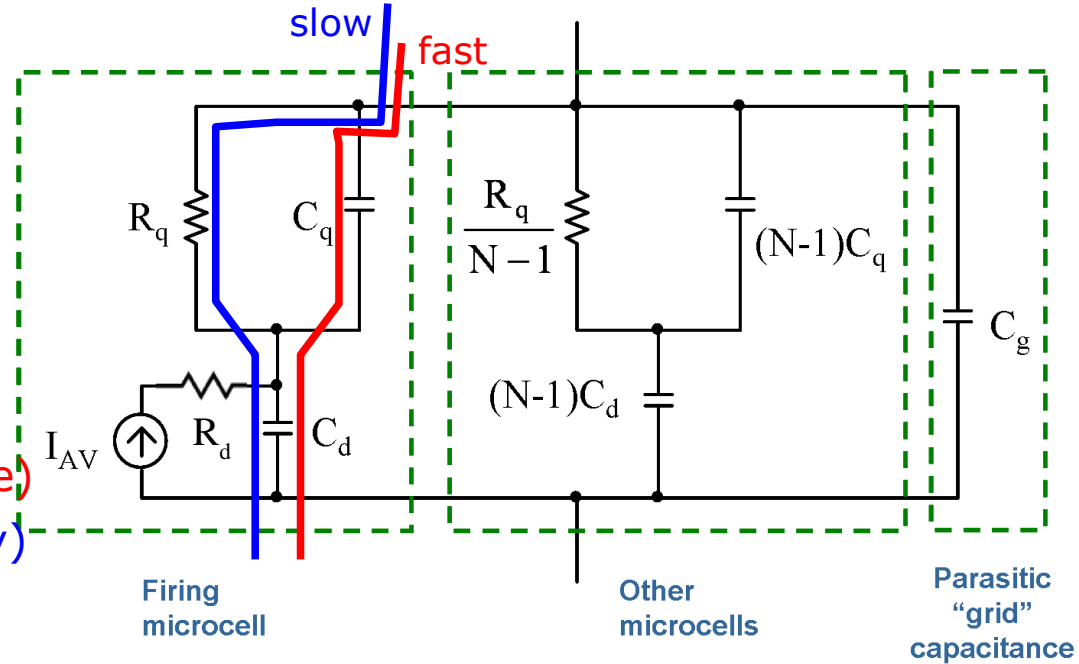
SiPM + load  $\rightarrow (||Z_{cell}) || C_{grid} + Z_{load}$

Signal = **slow** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q \text{-slow (fall)}}$ ) + **fast** pulse ( $\tau_{d \text{ (rise)}}, \tau_{q \text{-fast (fall)}}$ )

- $\tau_{d \text{ (rise)}} \sim R_d (C_q + C_d)$

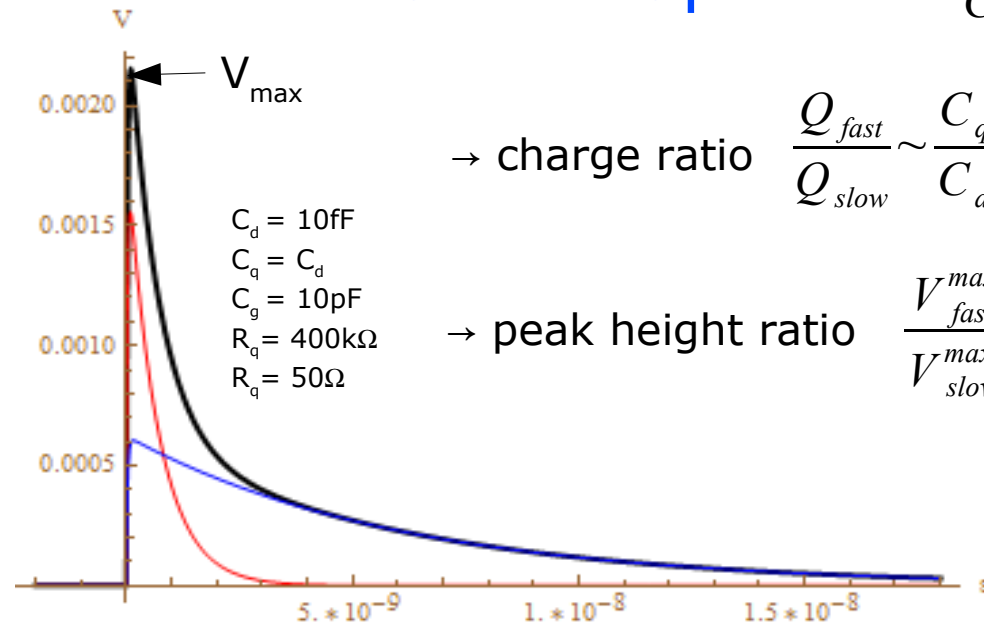
- $\tau_{q \text{-fast (fall)}} = R_{load} C_{tot}$  (fast; parasitic spike)

- $\tau_{q \text{-slow (fall)}} = R_q (C_q + C_d)$  (slow; cell recovery)



## Pulse shape

$$V(t) \simeq \frac{Q}{C_q + C_d} \left( \frac{C_q}{C_{tot}} e^{-\frac{t}{\tau_{FAST}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{-\frac{t}{\tau_{SLOW}}} \right)$$



$\rightarrow$  charge ratio  $\frac{Q_{fast}}{Q_{slow}} \sim \frac{C_q}{C_d}$

$\rightarrow$  peak height ratio  $\frac{V_{fast}^{max}}{V_{slow}^{max}} \sim \frac{C_q^2 R_q}{C_d C_{tot} R_{load}}$

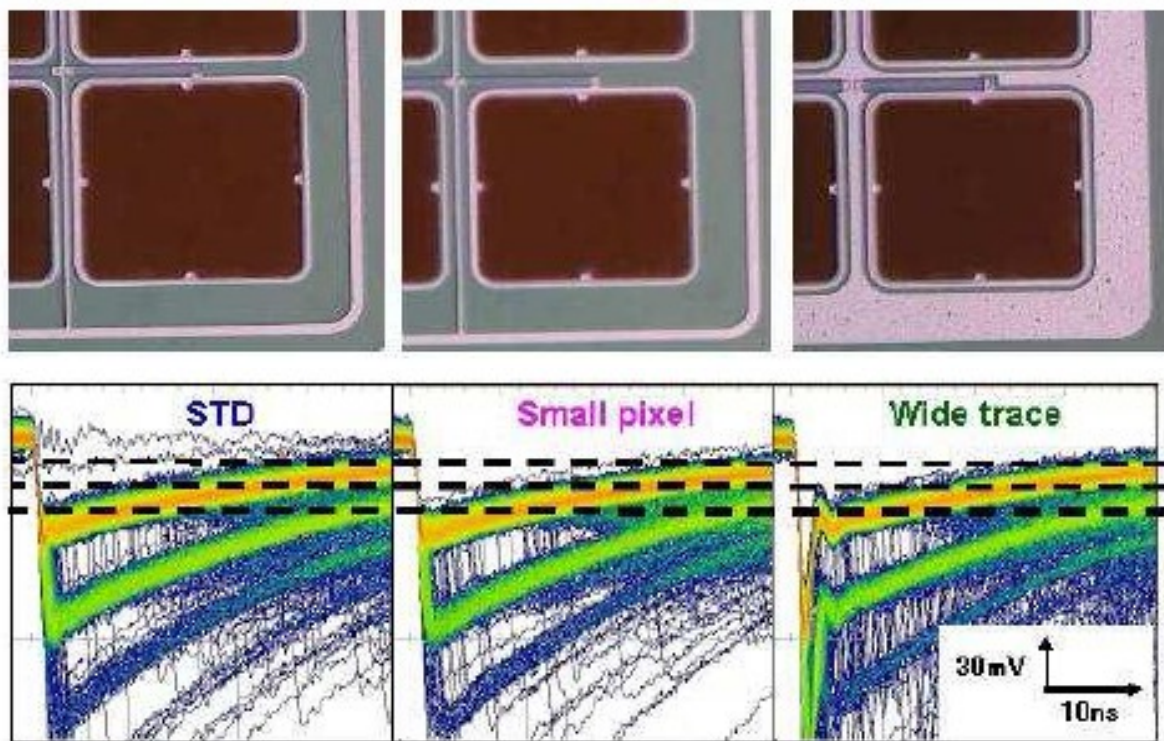
increasing with  $R_q$  and  $1/R_{load}$  (and  $C_q$  of course)

Increasing  $C_q/C_d$  or/and  $R_q/R_{load}$   
 $\rightarrow$  spike enhancement  
 $\rightarrow$  better timing

# Optimizing signal shape for timing (SPTR)

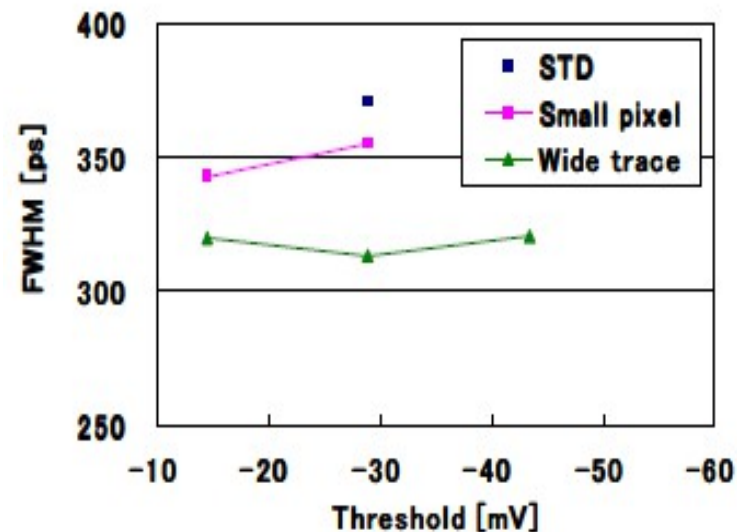
→ peak height ratio  $\frac{V_{fast}^{max}}{V_{slow}^{max}} \sim \frac{C_q^2 R_q}{C_d C_{tot} R_{load}}$

Enhancing  $C_q$  does improve timing performances



Yamamura et al. at PD09

1mm $\square$ 100 $\mu$ m (GAIN=2.4E+06, 25 $^{\circ}$ C)  
Timing resolution of 1p.e. vs threshold



Analogous method for timing optimization proposed in C.Lee et al NIM A 650 (2010) 125  
"Effect on MIM structured parallel quenching capacitor of SiPMs"

Note:

The **steep falling front** of the fast peak could be exploited too for optimum timing

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{N_{samples} \int dt [f'(t)]^2}$$

# Summary

**Significant development** of SiPMs over the last few years and **new players**

- **Operative  $\Delta V$  over-bias range:** from 2V (eg HPK) to 10V (eg FKB) depending on E field profile and Rq
- **T coefficient:** low, below 0.3%/°C for many devices  
→ might be lower, but **tradeoff** against PDE and noise
- **Pulse Shape** and **Gain:** tuned for matching application requirements (**tradeoffs**)  
→ photon counting and timing vs energy measurement (signal spike,  $E_{\text{field}}$  profile)
- **Dynamic range:** Large, up a few x10000 pixels (eg NDL, Zecotek)  
→ improved **radiation hardness** (not covered in this review) is relevant bonus  
→ trade-off with Fill Factor
- **PDE:** up to 60% for blue-green light (eg. KETEK)  
→ easily tuned to match applications (but only in visible optical range)
- **DCR** at T room can be < 100kHz/mm<sup>2</sup> (eg. Hamamatsu)
- **Cross-Talk:** can be as low as 1% in operative range (eg. FBK, MePhi/Pulsar)
- **After-Pulsing:** still at some % level for many devices  
→ exploiting higher Rq "just" to hide A-P is not a good practice...  
→ Digital SiPM is prone too, though less affected (active quenching)
- **Timing:** intrinsically fast, SPTR < 50ps in operative range  
→ but mind the **diffusion non-gaussian tails** in temporal response (long  $\lambda$ )
- **Calibration:** precise, thanks to existing detailed operative models

# Still missing and Future threads

- Avalanche **detailed physical models are still missing**. In particular for
  - **ultra-fast timing** applications there is room for device improvement
  - techniques for reducing **long timing tails** might be exploited
- Physical models might be of help also in further reducing **DCR** and **A-P**
  - eg: E field engineering for reducing tunneling
- **PDE**: expected soon are
  - improvements the **UV, VUV, EUV region**
  - devices with **through vias** → coupling with scintillators, fast imaging !
- GM-APD arrays for **NIR, IR sensitivity**: **different semiconductors**
  - InGaAs GM-APD arrays from AmplificationTechnologies do exist but... small area, noise and cost (!)
- **DCR**:
  - expected in 2012 a factor **x3 improvement** → larger area devices will follow
  - in the mean time devices tuned for working at **cryogenic T** easy to devise
- **Low T**: SiPM perform ~ideally in the range  $100K < T < 200K$ 
  - Rq should be tuned shorter recovery (ad hoc devices)
  - lower gain (small cells) might be desired to mitigate after-pulses



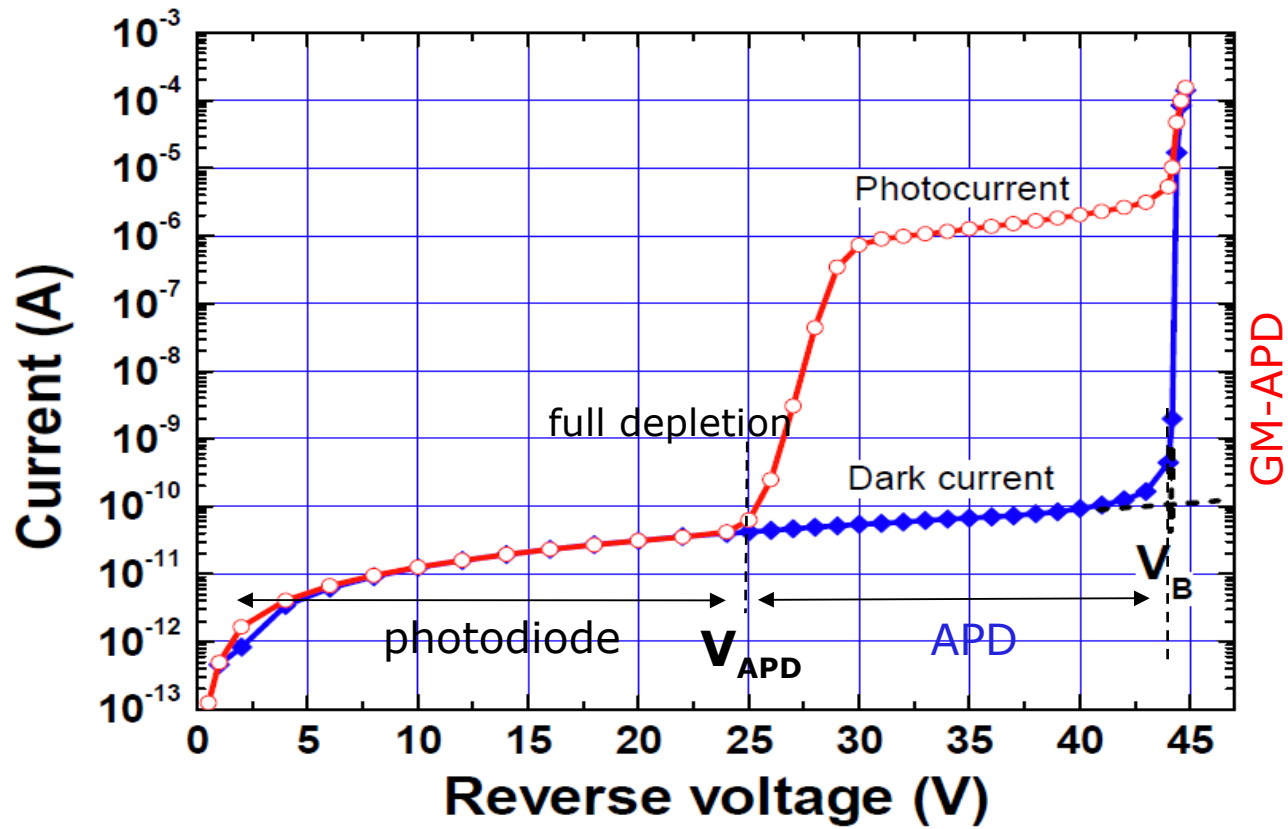
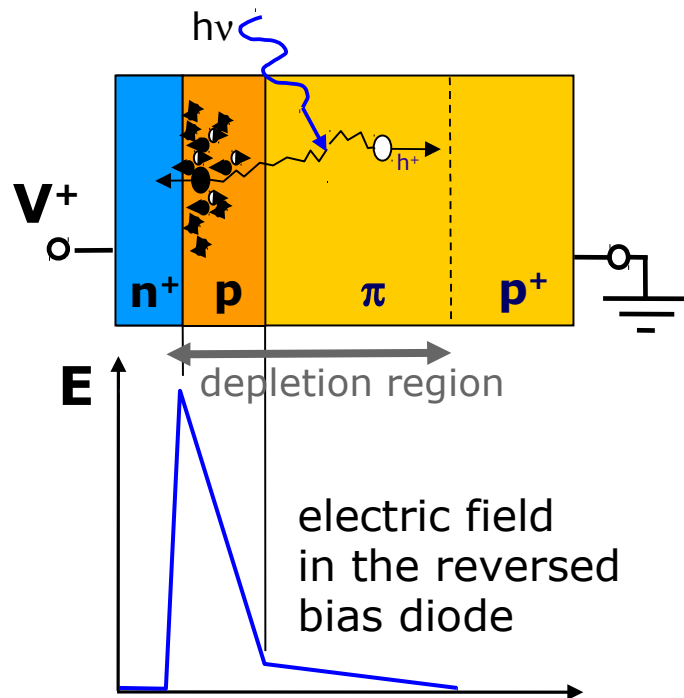
Thanks for your attention



# Additional material

# The building block of a SiPM: GM-APD

## Reverse biased junction



## APD: Linear-Proportional Mode

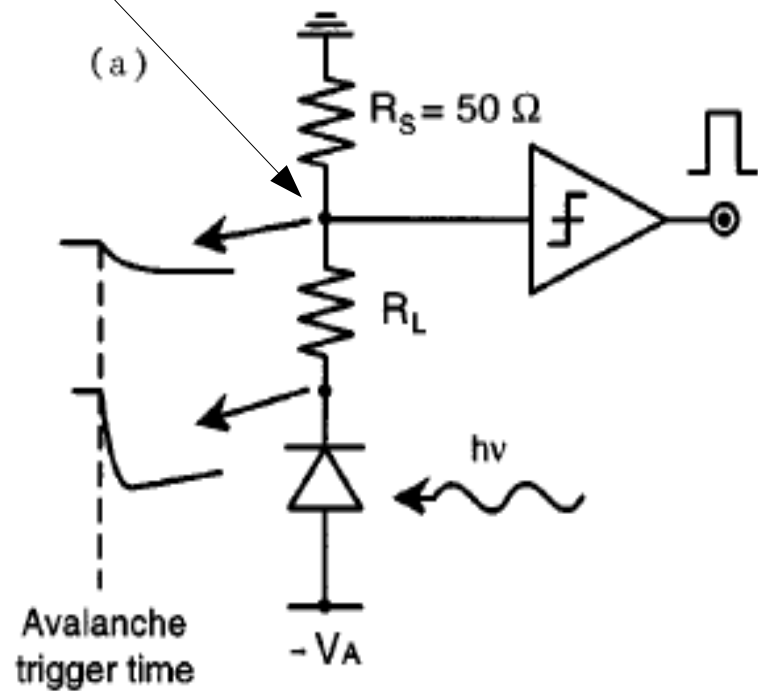
- Bias **BELOW**  $V_{BD}$  ( $V_{APD} < V < V_{BD}$ )
- It's an **AMPLIFIER**
- Multiplication: in practice limited to  $10^4$  by fluctuations
- No single photo-electron resolution  
...except at low T with slow electronics,  
*Dorokhov et.al. J.Mod.Opt. 51 (2004)*

## GM-APD: Geiger Mode

- Bias **ABOVE**  $V_{BD}$  ( $V - V_{BD} \sim$  a few volts)
- It's a **TRIGGER** (BINARY) device
- Multiplication:  $\infty$ ... in practice limited by macroscopic parameters (R,C)
- Limited by dark count rate
- Single photo-electron resolution
- Need Reset (Feedback - Quenching)

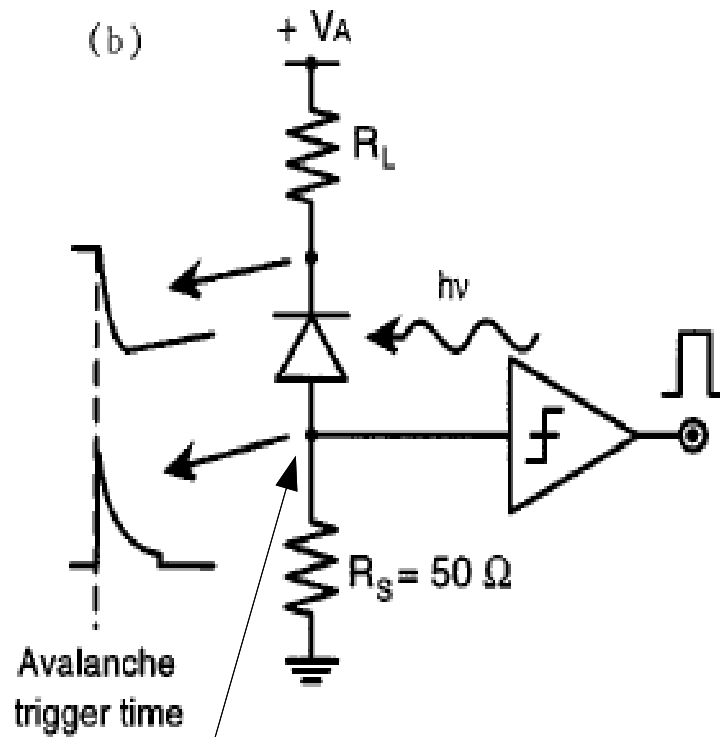
# Readout Mode

High Z node



**Voltage Mode**

**Current Mode**

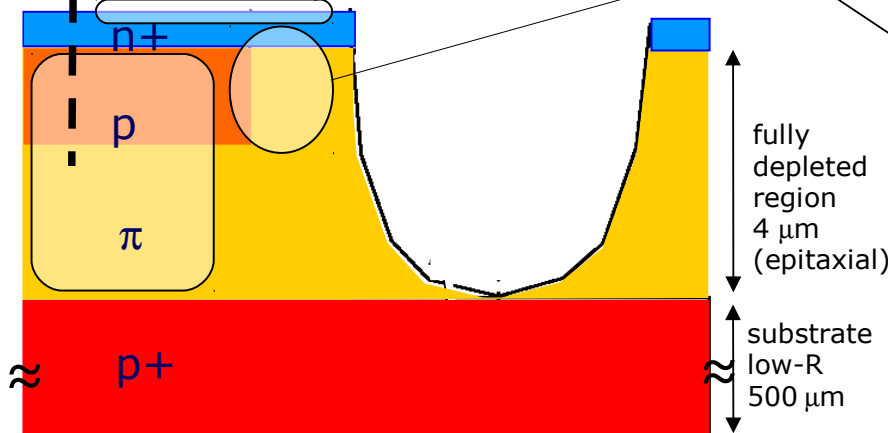
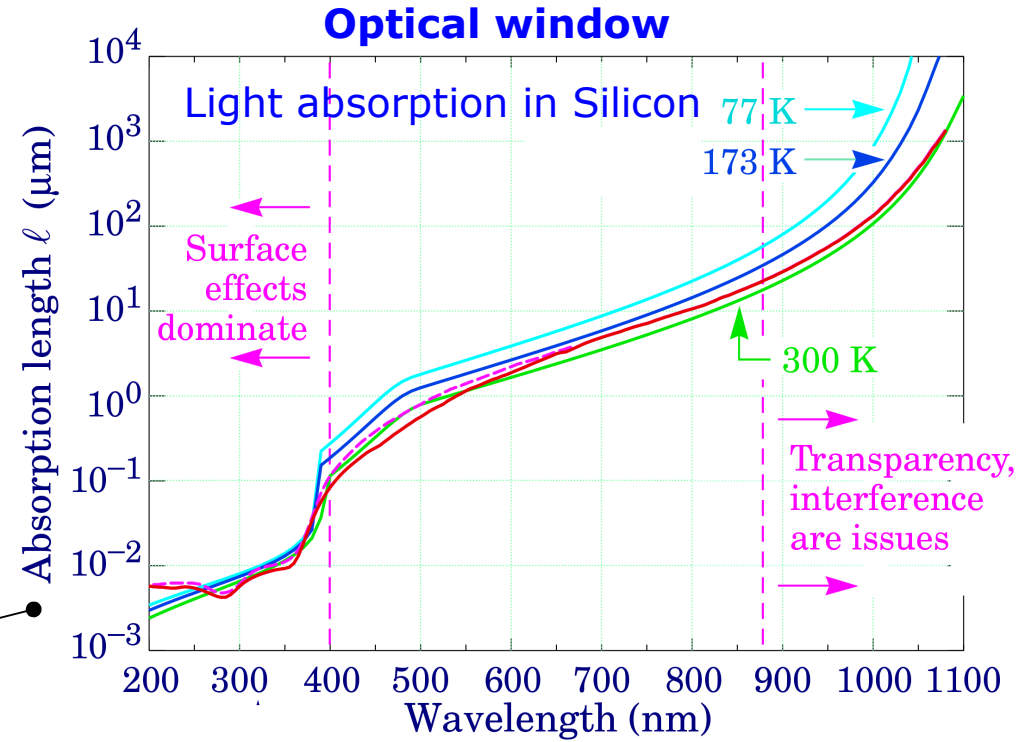
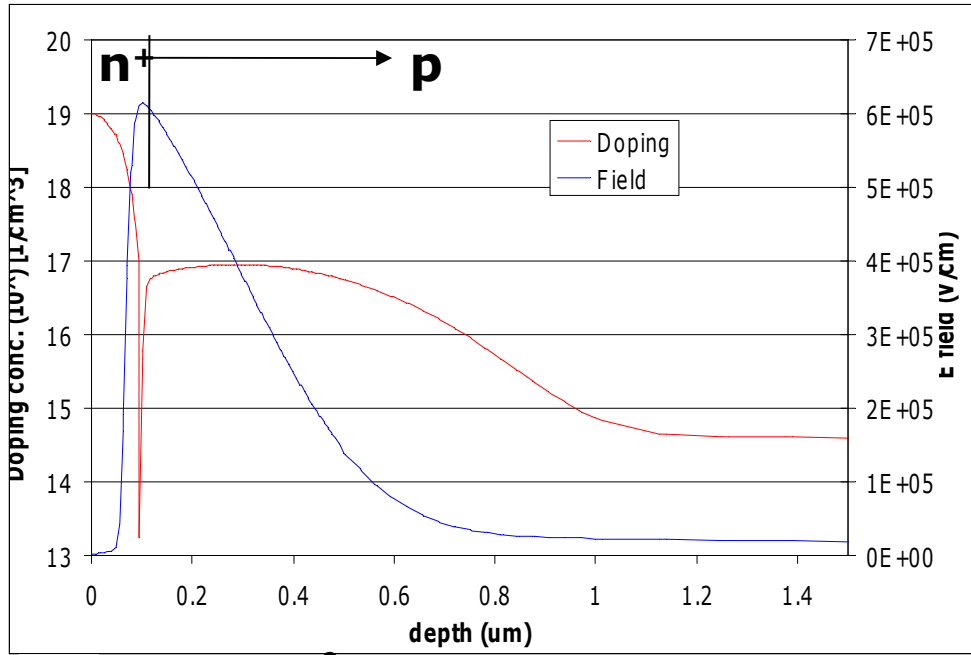


Low Z node



# Key elements in SiPM cell

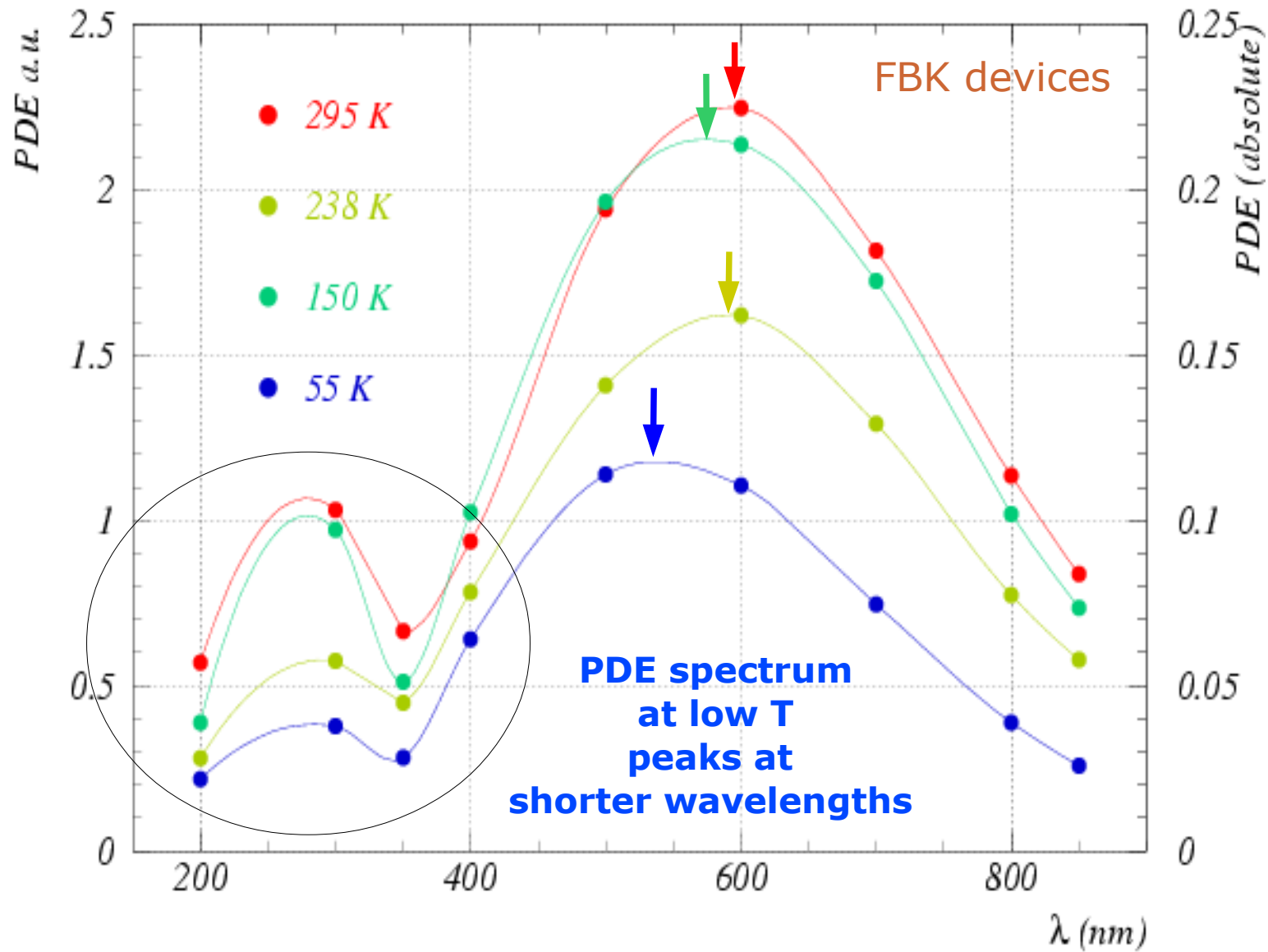
## Doping and Field profiles



## Guard Ring:

- for avoiding early edge breakdown
- for isolating cells
- for tuning E field shape
- has important impact on fill factor (more than  $R_q$  and metal grid)

# PDE vs $\lambda$ ( $\Delta V$ fixed, various T)



# RPL model: fast simulation

“Statistics of Avalanche Current Buildup Time in Single-Photon Avalanche diodes”  
C.H.Tan, J.S.Ng, G.J.Rees, J.P.R.David (Sheffield U.)  
IEEE J.Quantum Electronics 13 (4) (2007) 906

Numerical model (MC): **Random distribution of impact ionization Path Length (RPL)**

Analysis of **breakdown probability**, **breakdown time** and **timing jitter** as functions of avalanche region width ( $w$ ), ionization coefficient ratio ( $k = \beta_{\text{hole}} / \alpha_{\text{electron}}$ ) and dead space parameter ( $d$ ) (uniform E field, constant carrier velocity)

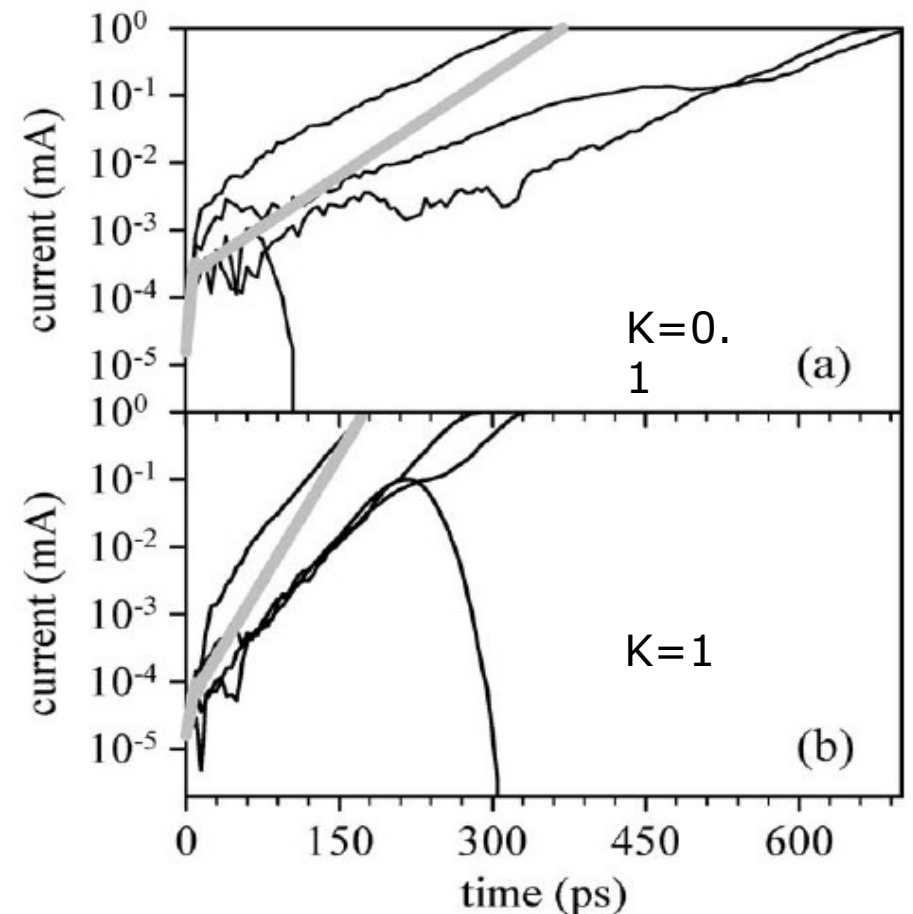
1) **increasing  $k$ :**

- **improves timing** performances
- but breakdown probability

$P_{\text{br}}$  **increases slowly** with overvoltage

1a) hole injection results in better timing than electron injection (in Si devices)

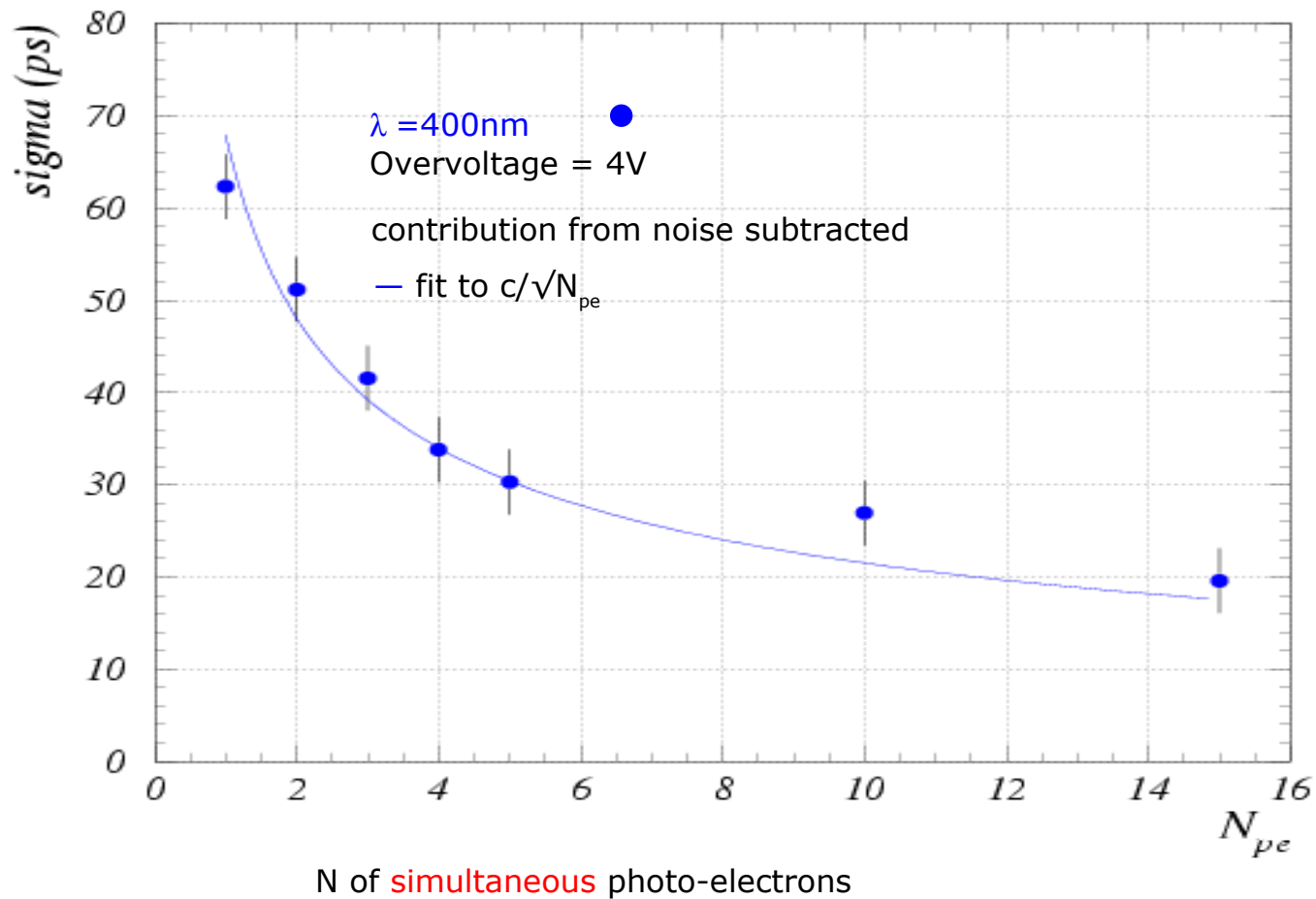
2) **dead space effects** worsen timing performances (the more at small  $k$ )  
Important for devices with **small  $w$**



# Many photons (simultaneous)

Dependence of SiPM timing on the  
number of simultaneous photons

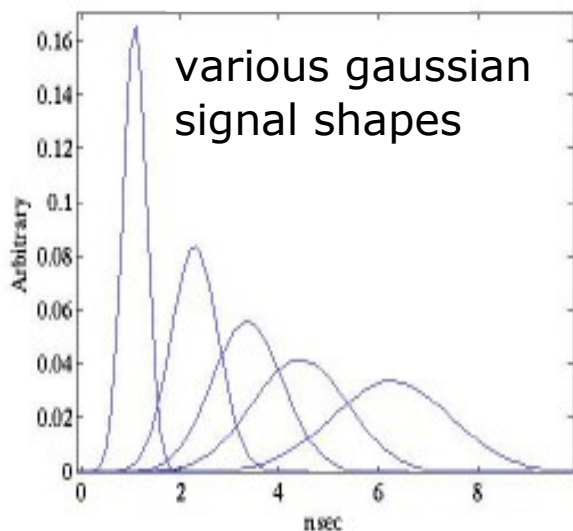
Poisson statistics:  $\sigma_t \propto 1/\sqrt{N_{pe}}$



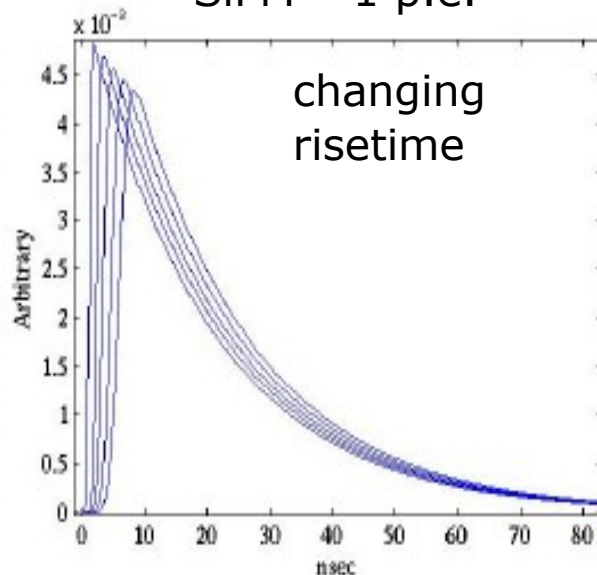
# Signal shape for timing - many photons

Single p.e. signal **slow falling-time** component  $\tau_{\text{fall}} = R_q (C_d + C_d)$   
 strongly affects **multi-photon signal risetime**

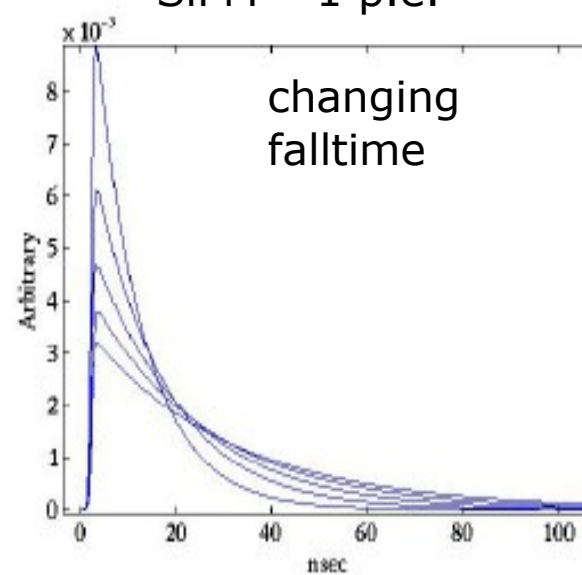
PMT - 1 p.e.



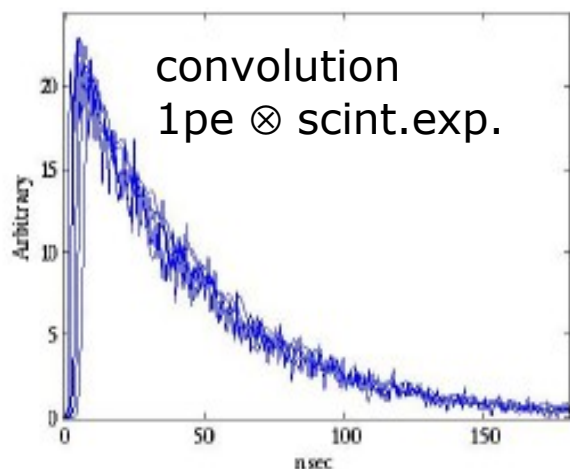
SiPM - 1 p.e.



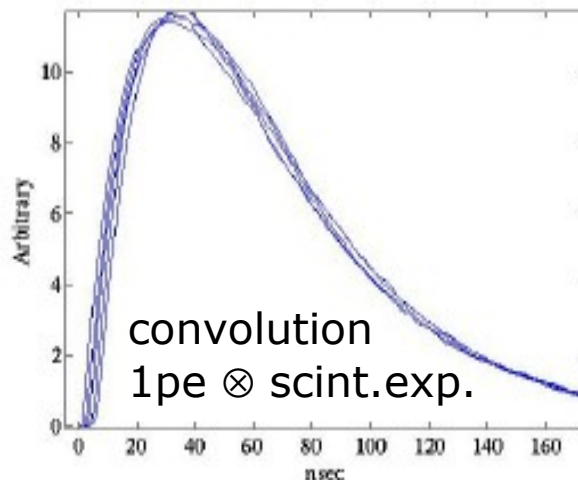
SiPM - 1 p.e.



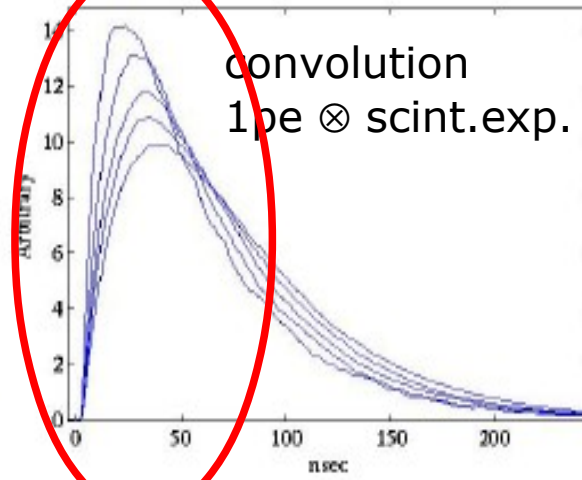
PMT - 511keV in LYSO



SiPM - 511keV in LYSO



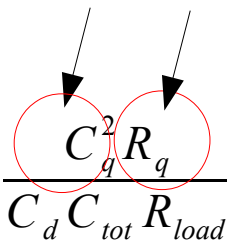
SiPM - 511keV in LYSO



convolution

# Optimizing shape for timing - many photons

→ peak height ratio

$$\frac{V_{fast}^{max}}{V_{slow}^{max}} \sim \frac{C_q^2 R_q}{C_d C_{tot} R_{load}}$$


Enhancing  $C_q$  and  $R_q$  does improve timing performances

## FBK devices type:

- Active area:  $4 \times 4 \text{mm}^2$ ;
- Cell size:  $67 \times 67 \mu\text{m}^2$ ;
- Fill factor: 60%;
- $C_Q + C_D$ : about 180fF;
- $R_Q$ : 1.1M;
- Dark noise rate:  
~100MHz at  $DV > 4V$

*C. Piemonte et al IEEE TNS (2011)*

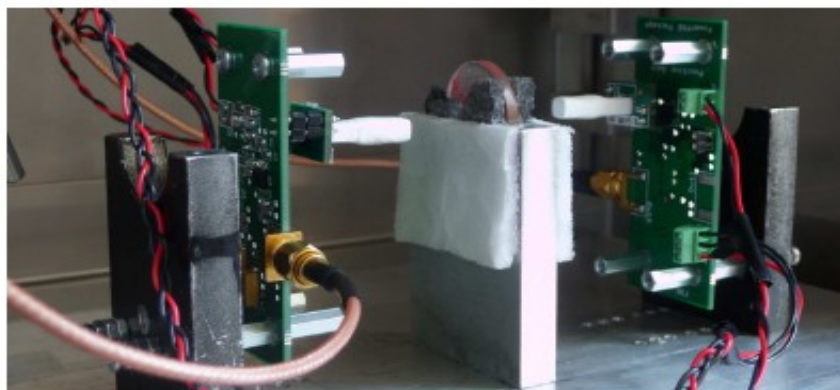
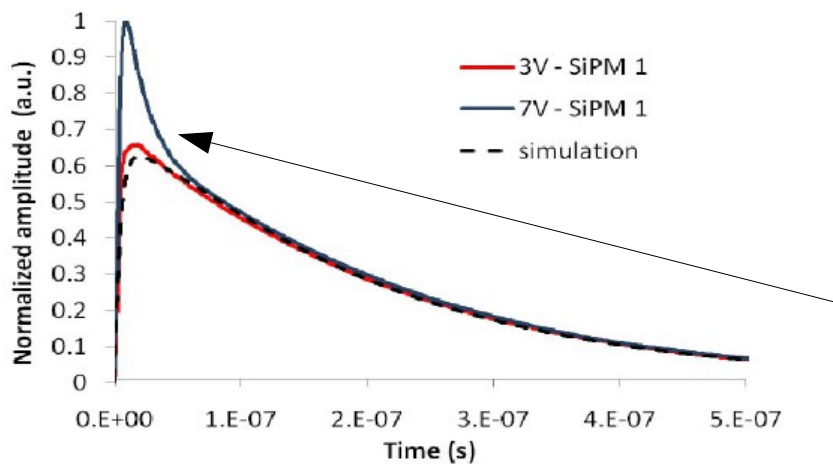


Fig. 2. Test set-up consists of two similar gamma ray detectors (LYSO crystal + SiPM) in coincidence. A  $^{22}\text{Na}$  source (disc in the middle) was used to generate two opposite 511keV photons in coincidence.



- Signal rise-time  $< 5\text{ns}$
  - CRT  $\sim 320\text{ps}$  (\*) FWHM triggering at 5% height
- Both are much better than for different structures with high  $C_{tot}$  and/or lower  $C_q, R_q$  (risetime up to several  $\times 10\text{ns}$ , CRT  $> 400\text{ps}$ )

??? peak shape is not scaling with  $\Delta V$   
(non linearity in the F.Corsi et al electrical model)  
Can be corrected → energy resol.  $\sim 11\%$

(\*)  $\sim 40\%$  from light propagation in crystals



# Radiation damage

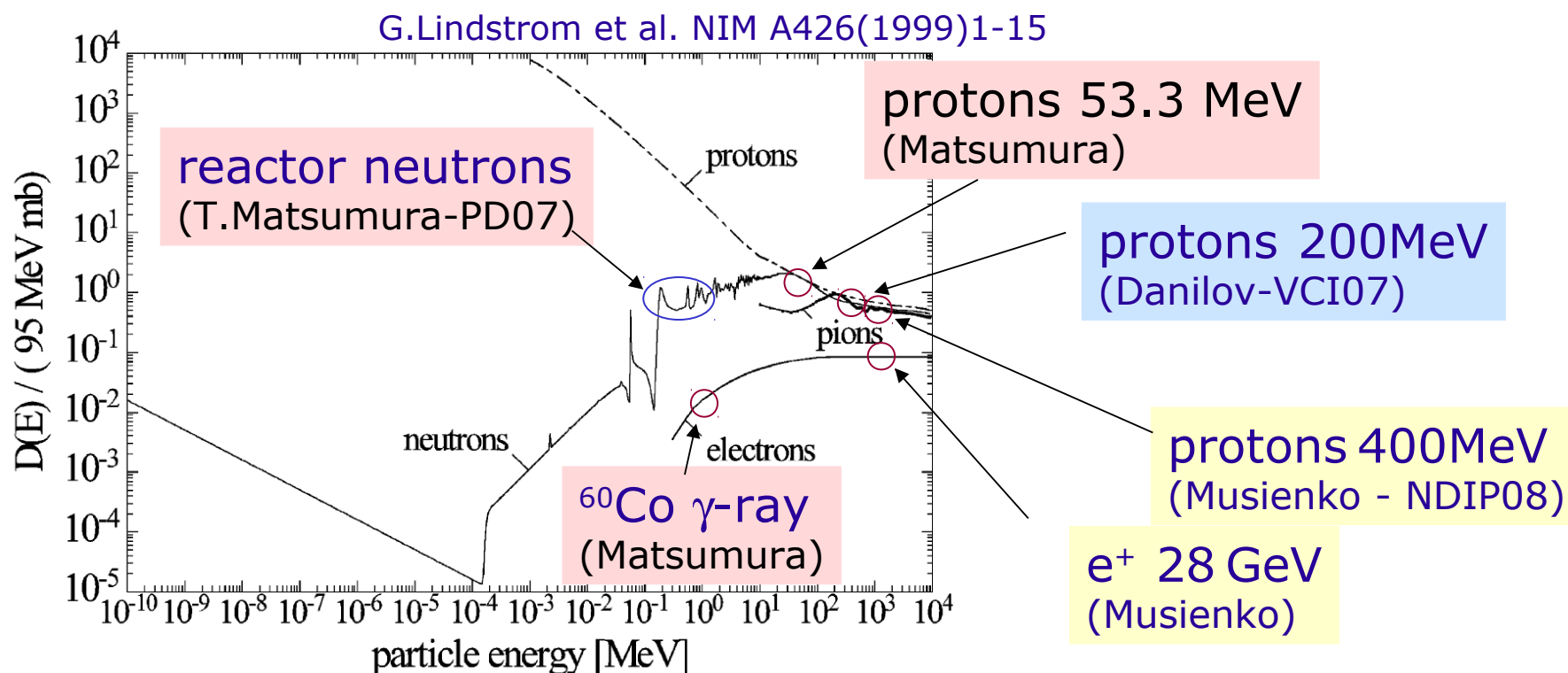
## Note:

- small cells smaller charge flow (small gain, high dynamic range)
- small epi-layered width

# Radiation damage: two types

- Bulk damage due to Non Ionizing Energy Loss (NIEL) ← neutrons, protons
- Surface damage due to Ionizing Energy Loss (IEL) ←  $\gamma$  rays  
(accumulation of charge in the oxide (SiO<sub>2</sub>) and the Si/SiO<sub>2</sub> interface)

Assumption: damage scales linearly with the amount of Non Ionizing Energy Loss (NIEL hypothesis)



Examples of radiation tolerances for HEP and space physics

ATLAS inner detector ...  $3 \times 10^{14}$  hadrons/cm<sup>2</sup>/10 year  
 $\sim 10^4$  hadrons/mm<sup>2</sup>/s

General satellites ...  $\sim 10$  Gy/year

Expectations:

protons /  $\gamma$ -ray  $\sim 100$

protons / neutrons  $\sim 2 \sim 10$



# Radiation damage: effects on SiPM

## 1) Increase of dark count rate due to introduction of generation centers

Increase ( $\Delta R_{DC}$ ) of the dark rate:

$$\Delta R_{DC} \sim P_{01} \alpha \Phi_{eq} Vol_{eff} / q_e$$

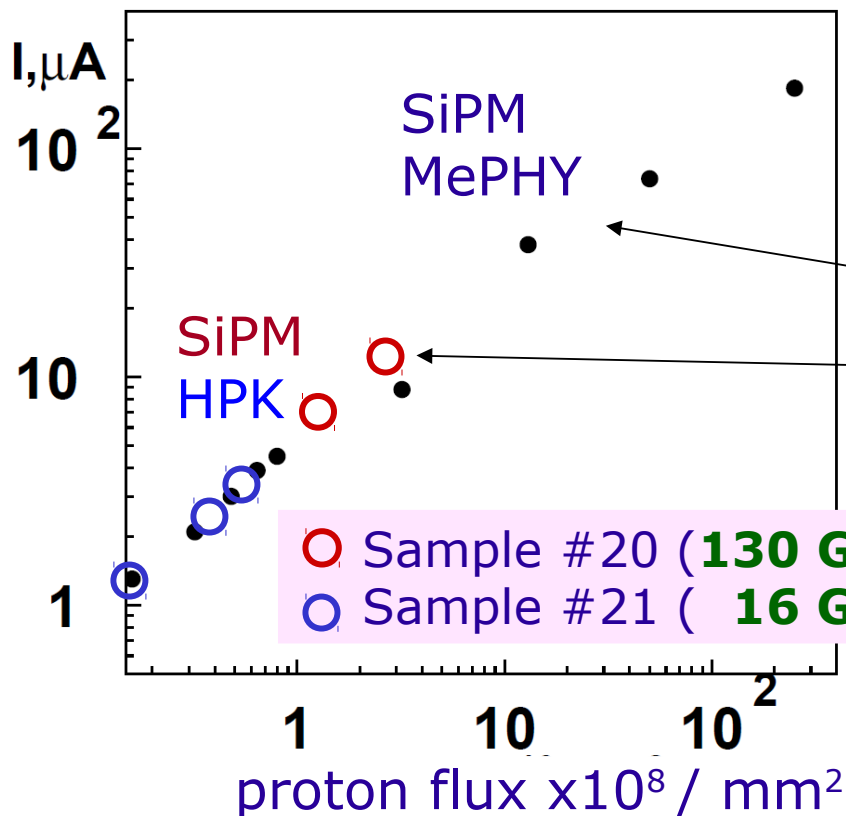
where  $\alpha \sim 3 \times 10^{-17}$  A/cm is a typical value of the radiation damage parameter for low E hadrons and  $Vol_{eff} \sim Area_{SiPM} \times \epsilon_{geom} \times W_{epi}$

NOTE:

- The effect is the same as in normal junctions:
- independent of the substrate type
  - dependent on particle type and energy (NIEL)
  - proportional to fluence

## 2) Increase of after-pulse rate due to introduction of trapping centers

→ loss of single cell resolution → no photon counting capability



## Indications from measurements:

1) no dependence on the device  
similar effects found for SiPM from MePHY (Danilov) and HPK (Matsumura) (normaliz. to active volume)

2) no dependence on dose-rate  
HPK (Matsumura)

3) n similar damage than p

4) p  $\times 10^1$ - $10^2$  more damage than  $\gamma$



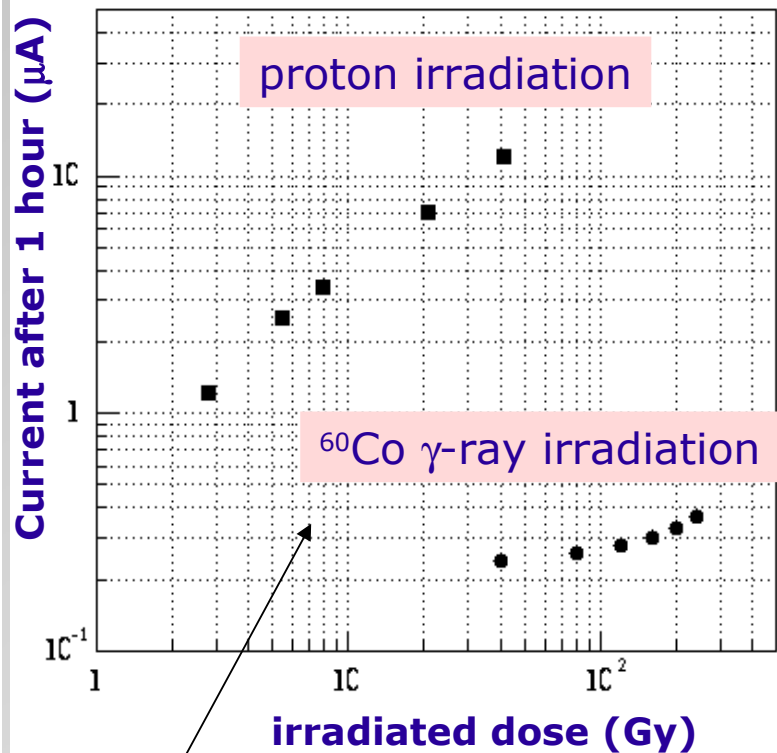
# Damage comparison

$2.3 \times 10^5$  p/mm<sup>2</sup>/s (130 Gy/h)

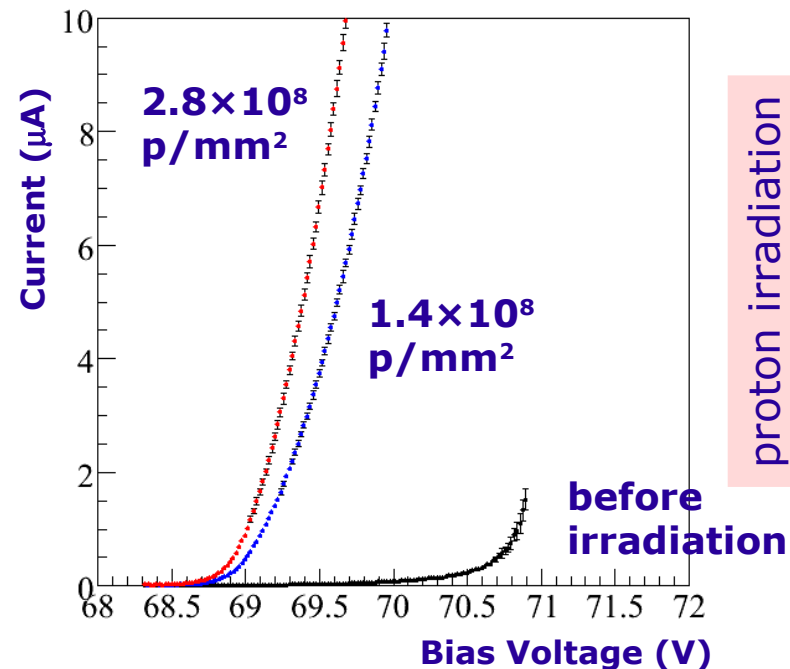
$I_{leak} @ (V_{op}, 1.4 \times 10^8 \text{ p/mm}^2) = 6.7 \mu\text{A}$

**Damage effect ...**  
almost the same for  
protons and neutrons

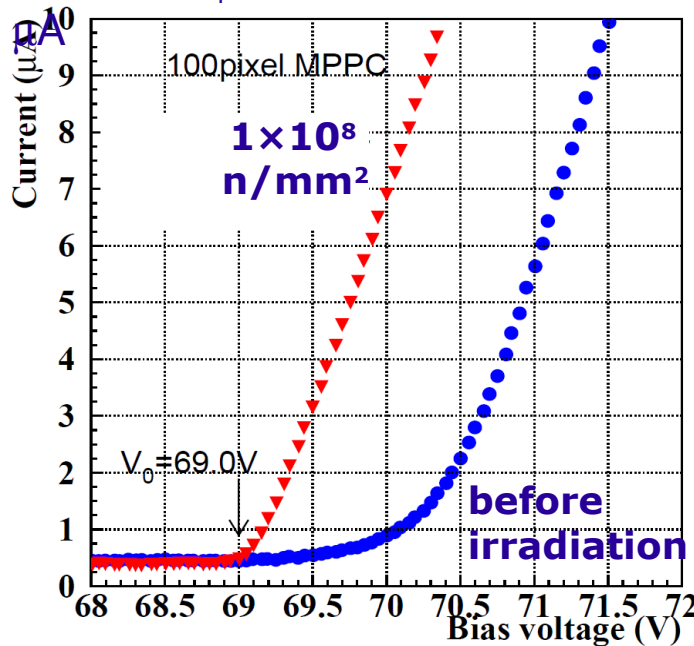
HPK devices  
T.Matsumura - PD07



**Damage effect ...**  
1~2 orders larger with protons  
than  $\gamma$ -ray irradiation



$4.2 \times 10^5$  n/mm<sup>2</sup>/s  
 $I_{leak} @ (V_{op}, 1.0 \times 10^8 \text{ n/mm}^2) = 8.5$



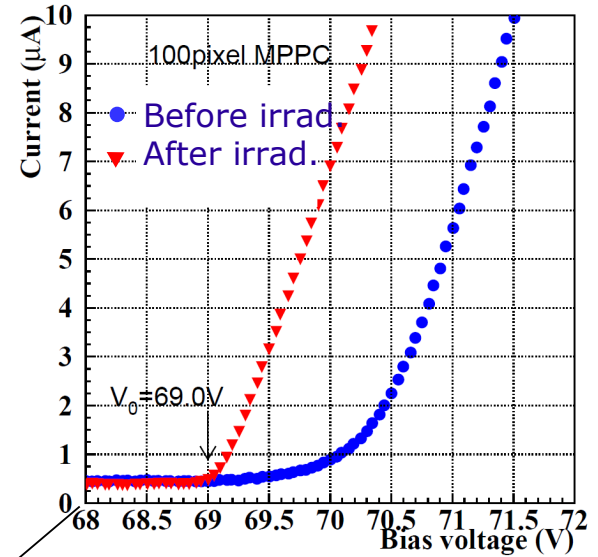
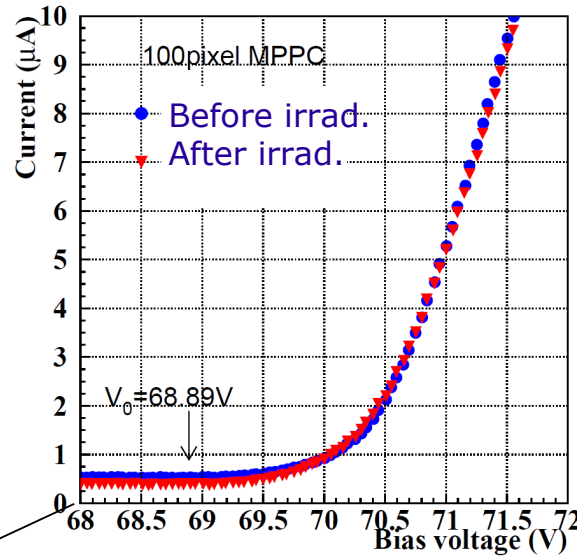
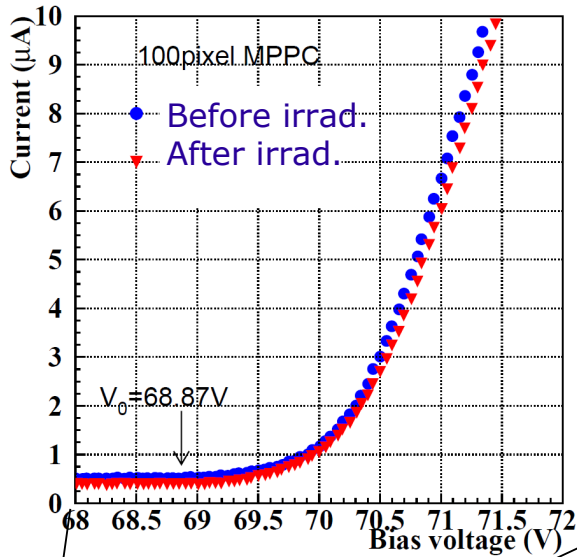
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# Radiation damage: neutrons (0.1 -1 MeV)

$8.3 \times 10^4 \text{ n/mm}^2$

$3.3 \times 10^5 \text{ n/mm}^2$

$1.0 \times 10^8 \text{ n/mm}^2$

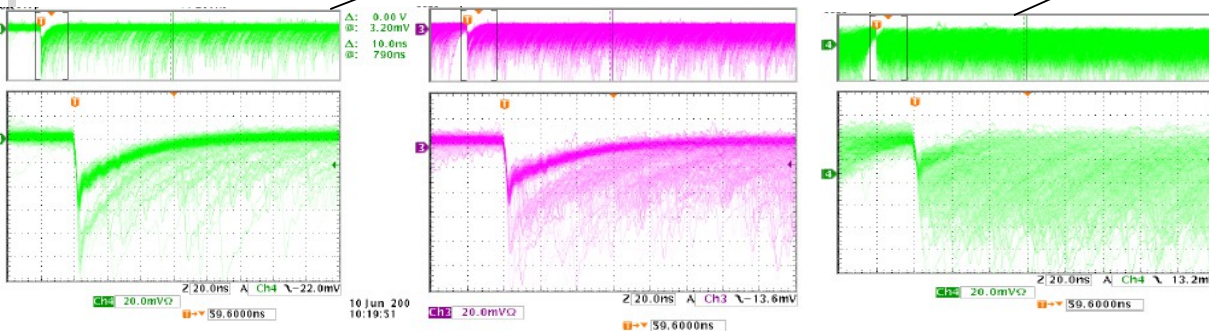


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$10^5 \text{ n/mm}^2$     $10^6 \text{ n/mm}^2$     $10^7 \text{ n/mm}^2$     $10^8 \text{ n/mm}^2$     $10^9 \text{ n/mm}^2$     $10^{10} \text{ n/mm}^2$

No significant change

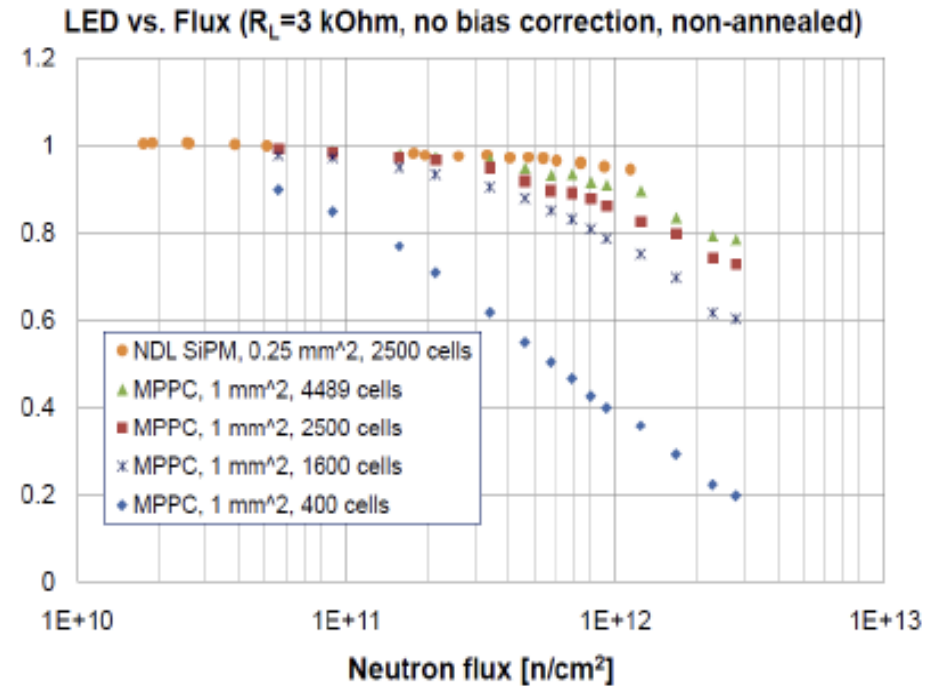
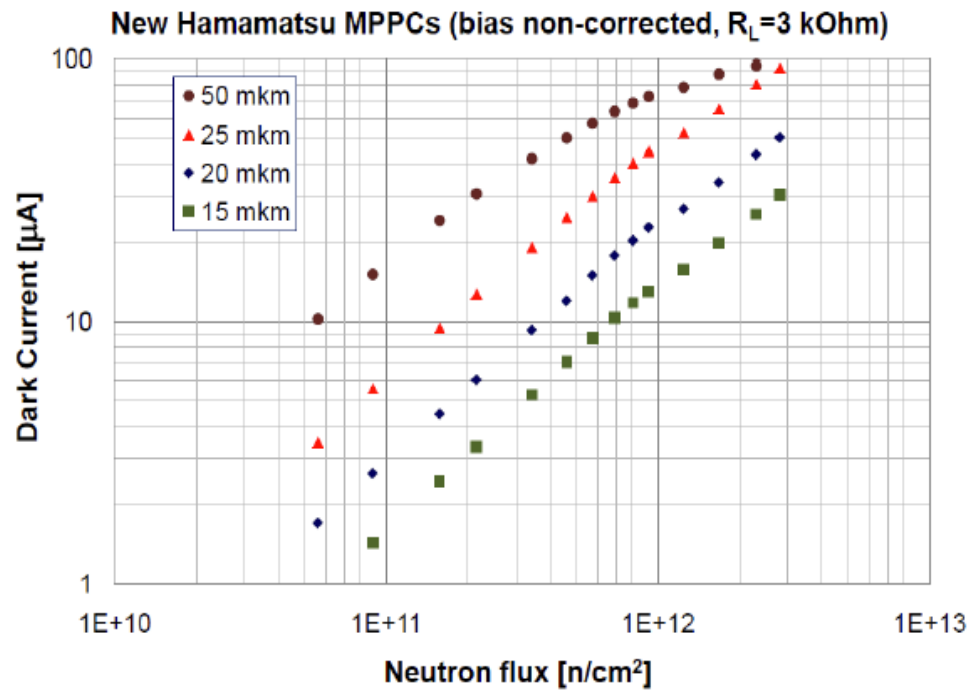
n dose



I-V drastically change. No signal  
Signal pulse is still there,  
but continuous pulse height.  
(No photon-counting capability)

Nakamura at NDIP08

# Radiation damage: neutrons 1 MeV $E_{eq}$



- No change of  $V_{bd}$  (within 50mV accuracy)
- No change of  $R_q$  (within 5% accuracy)
- $I_{dark}$  and DCR significantly increase

SiPMs with high cell density and fast recovery time can operate up to  $3 \cdot 10^{12} n/cm^2$  ( $\delta G < 25\%$ )

*Y.Musienko at SiPM workshop CERN 2011*