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# Charming CPV

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# Why are we here?

We are all here to discuss “one” number

$$\mathcal{A}_{CP}(D \rightarrow f) \equiv \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})}$$

The data:

$$\begin{aligned} \Delta\mathcal{A}_{CP} &\equiv \mathcal{A}_{CP}(D \rightarrow K^+ K^-) - \mathcal{A}_{CP}(D \rightarrow \pi^+ \pi^-) \\ &= \begin{cases} (-0.82 \pm 0.21 \pm 0.11)\% & \text{LHCb} \\ (-0.65 \pm 0.18)\% & \text{World average} \end{cases} \end{aligned}$$

**3.6 $\sigma$  from zero**

# New physics with charm

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The main motivation for meson physics is to look for new physics. Charm decays have several nice properties:

- In the SM charm physics is CP conserving to very good approximation (only two generations)
- Many  $D$  mesons are produced in colliders
- It is “easy” to tag the flavor of the  $D^0$
- The sensitivity to new physics is different from that of  $B$  physics (let’s talk about it)

# Where are we now?

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- Many interesting  $D$  observables
  - Mixing
  - DCS decays
  - CPV
  - Multi body final states
- The one we care about today is CPV in singly Cabibbo suppressed decays

$$a_f \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)}$$

in particular with  $f = K^+ K^-$  and  $\pi^+ \pi^-$

# Outline

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- General formalism
  - The SM predictions
  - More modes and checks
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I will not talk about

- Experimental situation
- New physics explanations

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# Formalism

# The three types of $D$ decay

- Cabibbo Favored (CF)

$$c \rightarrow s\bar{d}u \quad (D \rightarrow K^- \pi^+)$$

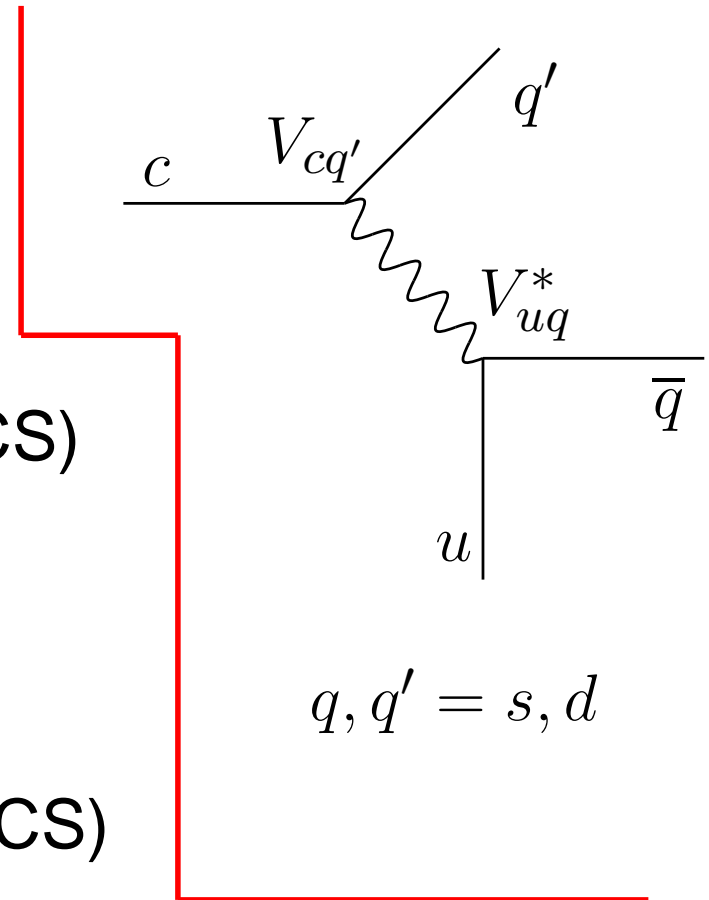
- Singly Cabibbo Suppressed (SCS)

$$c \rightarrow s\bar{s}u \quad (D \rightarrow K^- K^+)$$

$$c \rightarrow d\bar{d}u \quad (D \rightarrow \pi^- \pi^+)$$

- Doubly Cabibbo Suppressed (DCS)

$$c \rightarrow d\bar{s}u \quad (D \rightarrow \pi^- K^+)$$



# Penguins

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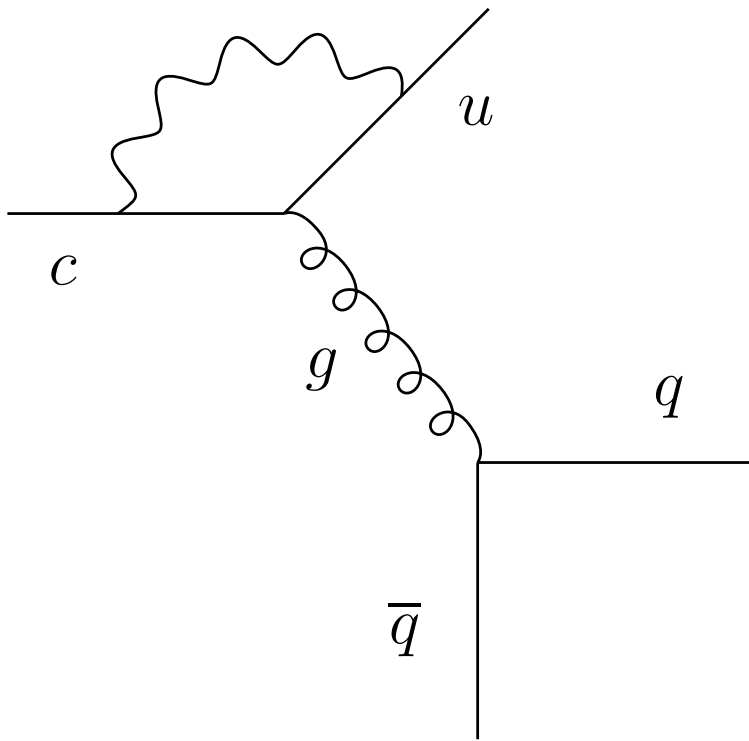
Beside the leading tree amplitudes, there are also loop decays

- Out of the loop decays, penguins are the largest
- Penguins can only contribute to SCS decays
- While they are very small, they carry a weak phase relative to the tree amplitude

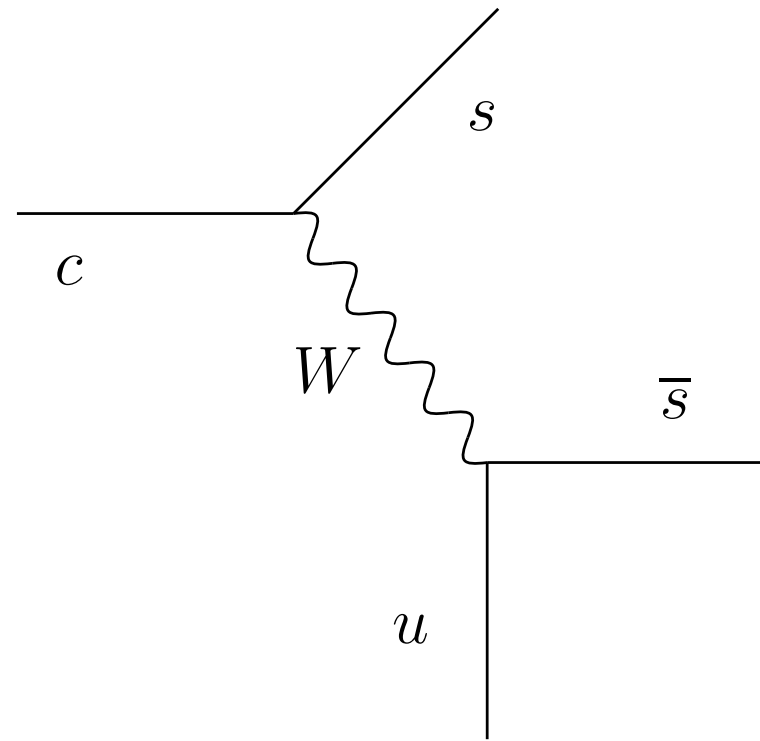


# $D \rightarrow K^+ K^-$ diagrams

(P)



(T)



# $D \rightarrow f$ amplitudes

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We talk only about SCS decay into a CP final state

- We can always write the decay amplitude as

$$\mathcal{A}(D \rightarrow f) = A_f \left[ 1 + r_f e^{i(\delta_f + \phi_f)} \right]$$

$$\mathcal{A}(\bar{D} \rightarrow \bar{f}) = A_f \left[ 1 + r_f e^{i(\delta_f - \phi_f)} \right]$$

- $\delta_f$  is a strong phase.  $\phi_f$  is a weak phase
- The whole point is to calculate  $r_f \sim P/T$
- The direct CP asymmetry is

$$a_{CP} = 2r_f \sin \delta \sin \phi$$

# Direct and indirect CPV

$D^0$  develop in time  $\Rightarrow D - \bar{D}$  mixing can affect the CP asymmetries. Both “indirect” (mixing) and “direct” (decay)

$$a_f = a_f^d + a^{ind}$$

- CP violation in decay (depend on  $f$ ):

$$a_f^d = 2r_f \sin \phi_f \sin \delta_f$$

- CP violation in mixing (universal):

$$a^{ind} = \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \left[ \frac{x}{2} \sin \varphi - \frac{y}{2} \cos \varphi \right]$$

# Separating the CP asymmetries

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$$a_f = a_f^d + a^{ind}$$

- Time integrated CP asymmetries are sensitive to both direct and indirect CP violation
- Since  $a^{ind}$  is universal

$$\Delta a_{CP} = a_{CP}(KK) - a_{CP}(\pi\pi) = a_{KK}^d - a_{\pi\pi}^d$$

- Mixing grows with time and thus the cut on the decay time enhances the sensitivity to  $a^{ind}$

$$a_f = a_f^d + \frac{\langle t \rangle}{\tau} a^{ind}$$

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# The SM

# SM amplitudes

How to relate the diagrams to the decay amplitudes?

$$\mathcal{A}(D \rightarrow K^+ K^-) = \lambda_d T_d + \lambda_s T_s + \lambda_b P$$

where

$$\lambda_q = V_{cq}^* V_{uq} \quad \lambda_d \approx \lambda_s \gg \lambda_b$$

• **Unitarity**  $\Rightarrow \lambda_d = -\lambda_s - \lambda_b \Rightarrow$

$$\mathcal{A}(D \rightarrow K^+ K^-) = \lambda_s (T_s - T_d) + \lambda_b (P - T_d) = C \left[ 1 + r_f e^{i(\delta + \gamma)} \right]$$

where

$$r_f = \left| \frac{V_{cb} V_{ub}}{V_{cs} V_{us}} \right| \times \left| \frac{P - T_d}{T_s - T_d} \right|$$

# Direct asymmetry in SCS decays

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$$a_f = 2r_f \sin \gamma \sin \delta_f \quad r_f = \left| \frac{V_{cb}V_{ub}}{V_{cs}V_{us}} \right| \times \left| \frac{P - T_d}{T_s - T_d} \right|$$

- Weak phase is  $\gamma$
- Hadronic matrix elements ( $T_q$  and  $P$ ) carry only strong phases

$$r_f \approx (6 \times 10^{-4}) \times X_H$$

What is  $X_H$ ?

# $r_f$ in the SM

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$$a_{CP}^f = 2r_f \sin \gamma \sin \delta_f$$

- A rough estimate. SU(3) and  $V_{us} = -V_{cd}$  implies

$$a_{CP}(KK) = -a_{CP}(\pi\pi)$$

- $\sin \gamma \approx 1$ , and we do not know the strong phase
- To get the central value of  $\Delta A_{CP} = 0.8\%$  we then need

$$4r_f \sin \delta \approx 80 \times 10^{-4} \Rightarrow r_f \sin \delta \approx 20 \times 10^{-4}$$



# Can the data be explained by the SM

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$$r_f \approx (6 \times 10^{-4}) \times X_H \quad X_H \sim P/T$$

- $X_H$  is a ratio of hadronic matrix elements
- The data needs  $r_f \sin \delta \sim 20 \times 10^{-4}$
- It can be done if
  - We have large strong phase (seems reasonable)
  - $X_H \gtrsim 3$ . Not so easy

# At the tropical forest

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- Tree?
- Loops?
- Hybrid!

# How large can $X_H$ be?

- To explain the data we need  $X_H \gtrsim 3$

- Naively

$$X_H \sim \frac{P}{T} \sim \frac{\alpha_S(m_c)}{\pi} \sim 0.1$$

- In  $B$  physics we get it from  $B \rightarrow K\pi$  and  $B \rightarrow \pi\pi$

$$X_H \sim 0.15$$

- In the heavy quark limit

$$\frac{X_H(D)}{X_H(B)} \sim \frac{\alpha_S(m_c)}{\alpha_S(m_b)} \sim 2 \Rightarrow X_H \sim 0.3$$

# Is the charm heavy?

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Is the above estimate reliable?

- Golden and Grinstein (89); Brod, Kagan, Zupan (11):  $X_H$  can be large!
- One day I will make a horror movie: “The  $\Delta I = 1/2$  rule”
  - Unexplained enhancement of factor of (maybe?) 7
  - Very low energy
- The “penguin” vs “tree” is a perturbative picture. At low energy it is all messed up
- Using ideas like QCD factorization, BKZ found  $X_H \sim 0.3$  at leading order. Estimate the breaking of factorization they could go to  $X_H \sim 1.2$

# SM calculation: Where are we?

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$$X_H^{exp} \gtrsim 3 \quad X_H^{best} \sim 0.3$$

- There seems to be indications that the naive estimate is an underestimate
- Still, very hard to explain the experimental central value by the SM
- Hard to claim that the data is clearly NP, since the theoretical errors on the best estimate are large

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What next?

# What else we could do?

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- More data! The higher the value is, harder to argue that it is the SM
- Measure  $a_{KK}$  and  $a_{\pi\pi}$  separately
- Look for other  $D$  decays: Charged  $D$ , multi body,  $D_s$

# SU(3) breaking

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SU(3) predicts that

$$a_{CP}(KK) = -a_{CP}(\pi\pi) \quad \Gamma(D \rightarrow KK) = \Gamma(D \rightarrow \pi\pi)$$

- The latter is broken by  $O(1)$
- We may argue that the SU(3) breaking in the asymmetry is smaller (It may also be suggested by CPT arguments)
- If one of the two  $a_{CP}$ s dominates  $\Delta A_{CP}$  then it is more likely that it is NP
  - We need bigger  $X_H$  in that one decay
  - The NP can violate the SM SU(3) relation



# Other decays

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- If we assume that  $X_H$  can be anything, what else can we check?
  - If it is the SM, we know it is LH penguins
  - Penguins are  $\Delta I = 1/2$
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- CPV in  $\Delta I = 3/2$
  - RH components to the penguin
  - So far no idea of how to find NP if it is in a “SM-like” penguin

$$\Delta I = 3/2$$

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- Similar ideas to Gronau-London in  $B \rightarrow \pi\pi$
- Using the fact that penguins cannot lead to final states with  $I = 2$
- $D$  is  $I = 1/2$ . CPV in a mode with final  $I = 2$  cannot come from penguins
- Several modes

$$D^+ \rightarrow \pi^+ \pi^0 \quad D^+ \rightarrow \rho^+ \rho^0$$

- Probably more can be done in

$$D \rightarrow \rho\pi \quad D \rightarrow KK\pi \quad D_s \rightarrow K\pi$$

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# Conclusions

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- CP violation in SCS  $D$  decays is very interesting
- Large uncertainties in the SM prediction, but it seems to be NP
- We would like to look for more decays, including non-CP eigenstates and multi-body final states

Can LHCb measure these asymmetries?