

**Neutrinos: an open window  
on  
Fundamental physics and  
the Evolution of the Universe**

11 Feb 2011

MICE Collaboration Meeting  
RAL

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# Outline

**1. Neutrino properties: questions for the future**

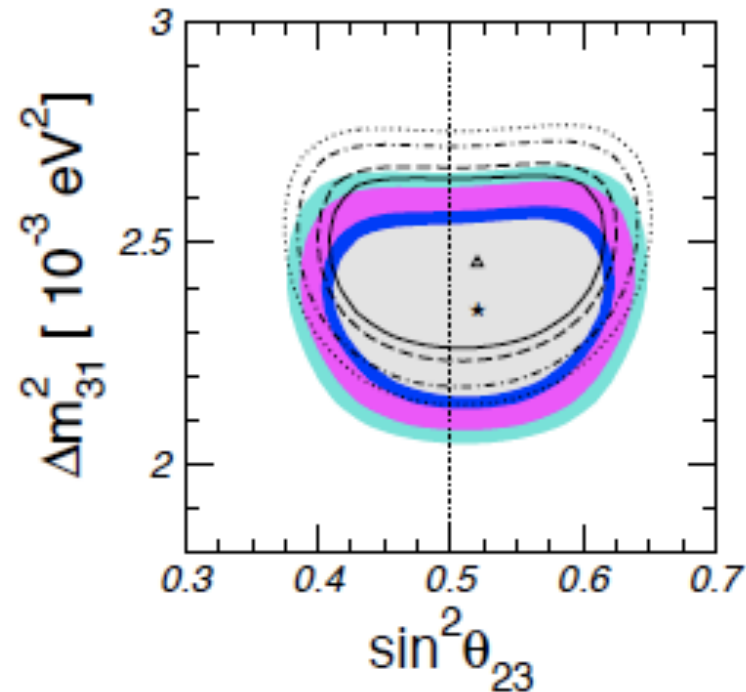
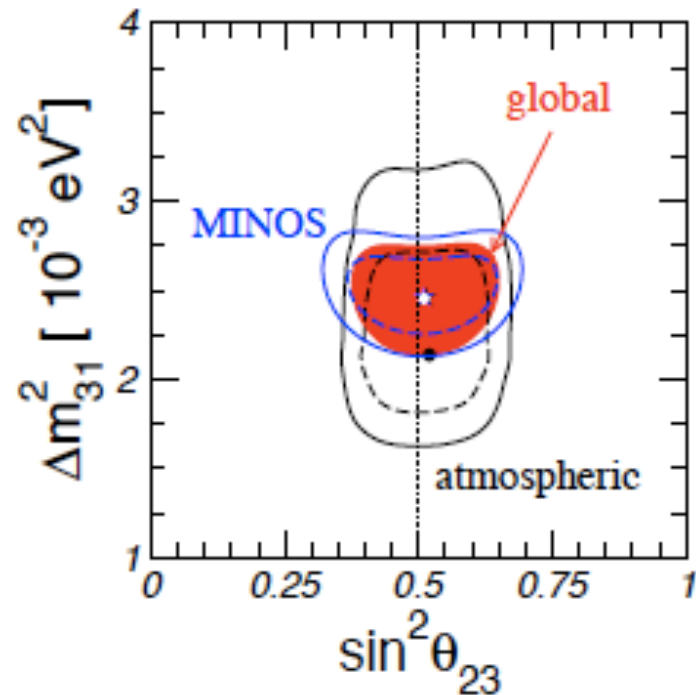
**2. Measuring the parameters in LBL**

**3. Theory: the origin of neutrino masses and the problem of flavour**

**4. Conclusions and outlook**

Neutrino oscillations measure **mass squared differences** and **mixing angles**.

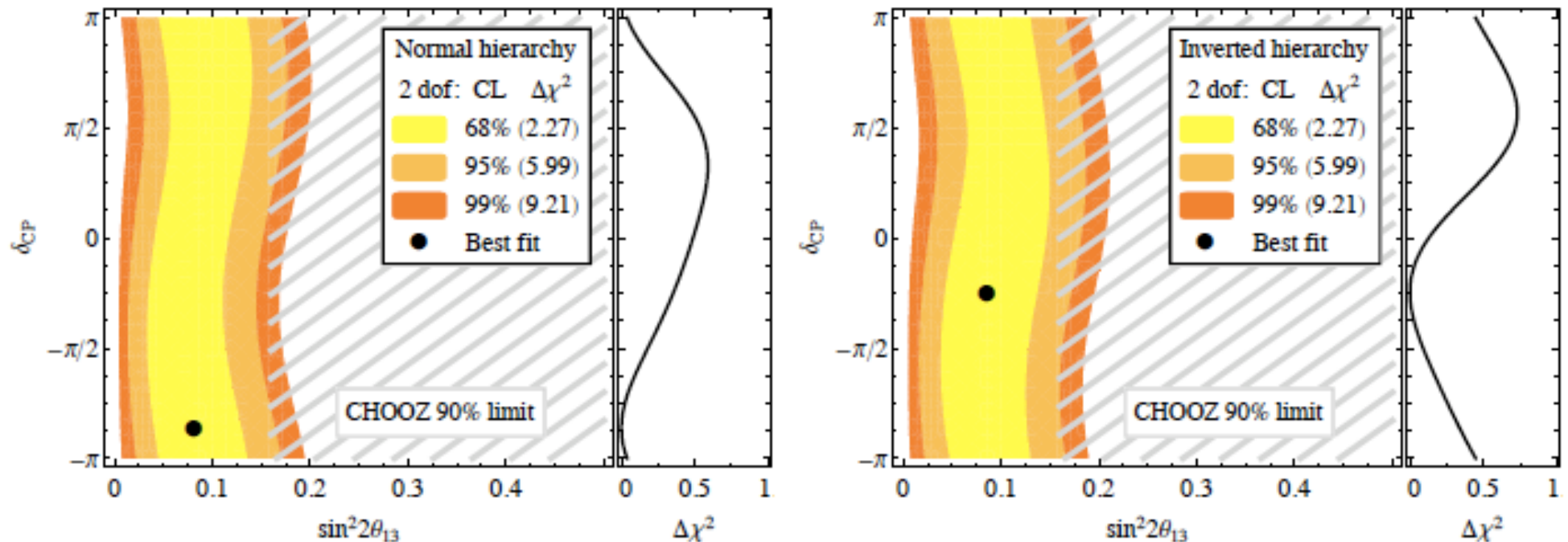
$$P(\nu_{\mu} \rightarrow \nu_e) = \sin^2 2\theta \sin^2 \frac{\Delta m_{21}^2 L}{4E}$$



Schwetz et al., I 103.0734

**Neutrino oscillations imply that neutrinos  
have mass and they mix!**  
**First evidence of physics beyond the SM.**

In 2011, the first hints of large  $\theta_{13}$  were found in T2K, MINOS and DoubleCHOOZ.



Machado et al., 1111.3330

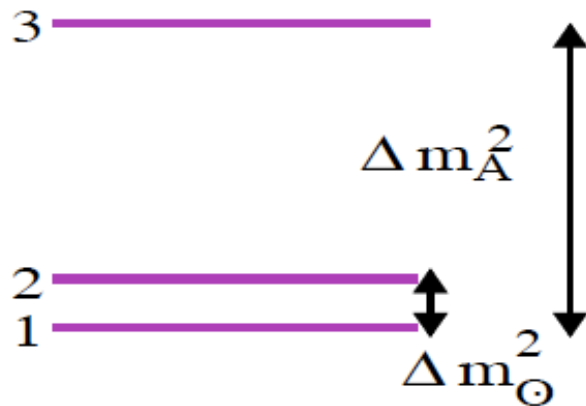
T2K, DoubleCHOOZ, RENO, Daya Bay will be able to confirm such hints very soon.

This will have important implications for experiments and theory.

# Present status of (standard) neutrino physics

$\Delta m_s^2 \ll \Delta m_A^2$  implies at least 3 massive neutrinos.

## Normal ordering

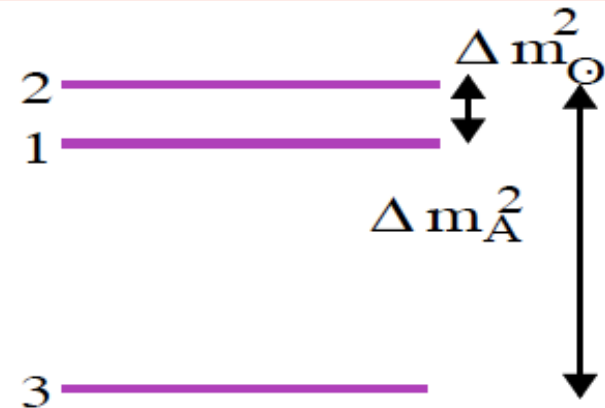


$$m_1 = m_{\min}$$

$$m_2 = \sqrt{m_{\min}^2 + \Delta m_{\text{sol}}^2}$$

$$m_3 = \sqrt{m_{\min}^2 + \Delta m_A^2}$$

## Inverted ordering



$$m_3 = m_{\min}$$

$$m_1 = \sqrt{m_{\min}^2 + \Delta m_A^2 - \Delta m_{\text{sol}}^2}$$

$$m_2 = \sqrt{m_{\min}^2 + \Delta m_A^2}$$

Measuring the masses requires:  $m_{\min}$  and the ordering.

Mixing is described by a unitary mixing matrix.

$$U = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \\
 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{-i\delta} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{-i\alpha_{21}/2} & 0 \\ 0 & 0 & e^{-i\alpha_{31}/2+i\delta} \end{pmatrix}$$

Solar, reactor  $\theta_{\odot} \sim 30^\circ$ 
Atm, Acc.  $\theta_A \sim 45^\circ$

CPV phase
Reactor, Acc.  $\theta < 12^\circ$ 
CPV Majorana phases

If  $U \neq U^*$ , there is **leptonic CP-violation**

$$P(\nu_l \rightarrow \nu_{l'}) \neq P(\bar{\nu}_l \rightarrow \bar{\nu}_{l'})$$

This is a **fundamental question to answer and is related to leptogenesis** and the possible origin of the baryon asymmetry of the Universe.

# Phenomenology questions for the future

- What is the nature of neutrinos (Majorana vs Dirac)?

- What are the values of the masses?

Neutrinoless double  
beta decay

Direct mass searches + Cosmology

- Is there CP-violation? What are the values of mixing angles (tribimaximal mixing?)

LBL

- Is the standard picture correct?

Reactor

A wide experimental programme is under way or at the proposal stage. Other relevant searches are: solar (Borexino), atmospheric (megaton-scale detector, INO), supernova neutrinos, SBL exp for sterile neutrino searches such as the VLENF.

# Long baseline neutrino oscillations

Long baseline neutrino oscillation experiments (T2K, LBNE, EU superbeams, neutrino factories and beta beams) will aim at studying the subdominant channels

$$\nu_{\mu,e} \rightarrow \nu_{e,\mu} \quad \bar{\nu}_{\mu,e} \rightarrow \bar{\nu}_{e,\mu}$$

$$P(\nu_{\mu} \rightarrow \nu_e) \sim \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$

for negligible matter and CPV effects.

in order to establish

1. **the mixing angles** ( $\theta_{13}$ )
2. **the mass hierarchy**
3. **Leptonic CPV**
4. **Non-standard effects.**



## Matter effects

These oscillations take place in the Earth (e, p, n).  
 A potential  $V$  in the Hamiltonian describes matter effects:

$$V = \sqrt{2}G_F(N_e - N_n/2)$$

$$P_{\nu_\mu \rightarrow \nu_e} = \sin^2 \theta_{23} \sin^2 2\theta_{13}^m \sin^2 \frac{\Delta_{13}^m L}{2}$$

The mixing angle changes wrt vacuum

$$\sin 2\theta_m = \frac{(\Delta_{13}^m/2) \sin 2\theta}{\sqrt{\left(\frac{\Delta m^2}{2E} \sin 2\theta\right)^2 + \left(\frac{\Delta m^2}{2E} \cos 2\theta - \sqrt{2}V\right)^2}}$$

and the probability gets enhanced for neutrinos (antineutrinos) depending on the mass ordering.

# CP-violation

A measure of CPV effects is given by

$$A_{CP} = \frac{P(\nu_l \rightarrow \nu_{l'}) - P(\bar{\nu}_l \rightarrow \bar{\nu}_{l'})}{P(\nu_l \rightarrow \nu_{l'}) + P(\bar{\nu}_l \rightarrow \bar{\nu}_{l'})} \propto J_{CP} \propto \sin \theta_{13} \sin \delta$$

The full probability can be approximated as

$$P(\bar{P}) \simeq s_{23}^2 \sin^2 2\theta_{13} \left( \frac{\Delta_{13}}{A \mp \Delta_{13}} \right)^2 \sin^2 \frac{(A \mp \Delta_{13})L}{2} - \tilde{J} \frac{\Delta_{12}}{A} \frac{\Delta_{13}}{A \mp \Delta_{13}} \sin \frac{AL}{2} \sin \frac{(A \mp \Delta_{13})L}{2} \cos \left( \mp \delta + \frac{\Delta_{13}L}{2} \right) + c_{23}^2 \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \frac{AL}{2}$$

Matter effects

CP violation

# Degeneracies

The determination of CPV and the mass ordering is complicated by the issue of **degeneracies**: different sets of parameters which provide an equally good fit to the data (eight-fold degeneracies).

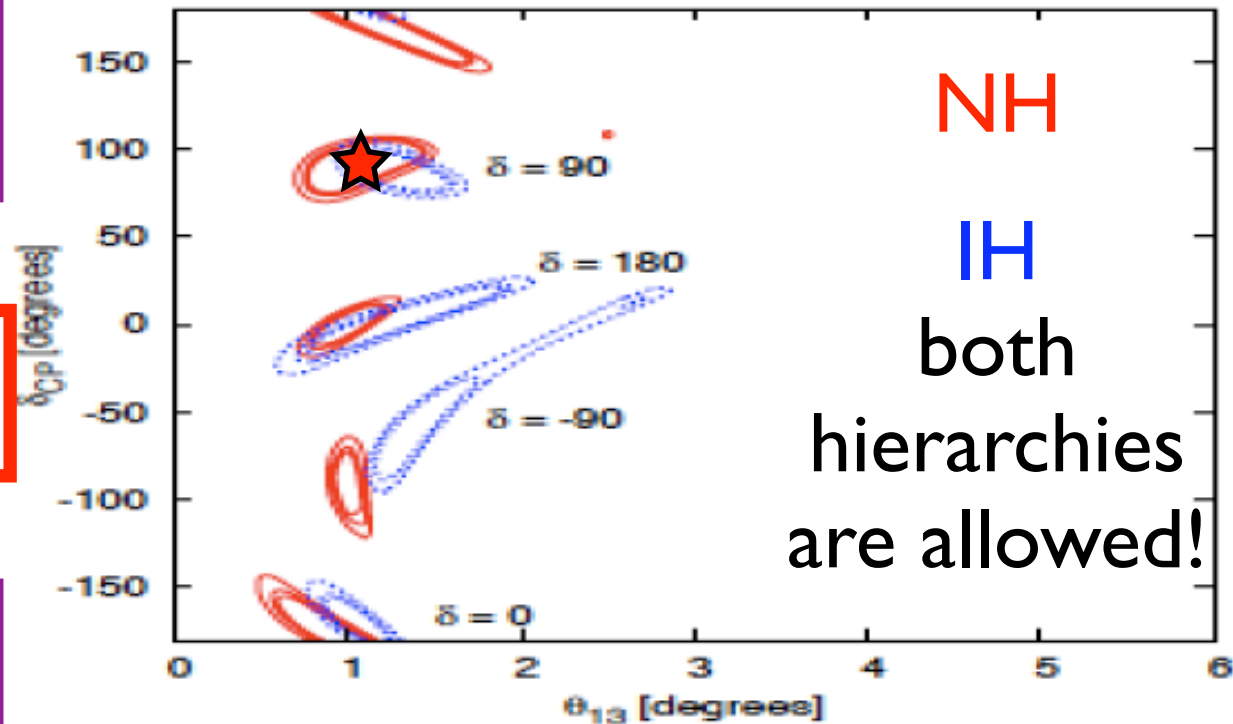
$$\theta_{13}, \delta, \text{sgn}(\Delta m_{31}^2), \theta_{23}$$



$$P(L/E) \quad \text{and} \quad \bar{P}(L/E)$$



$$\theta'_{13}, \delta', \text{sgn}'(\Delta m_{31}^2), \theta'_{23}$$

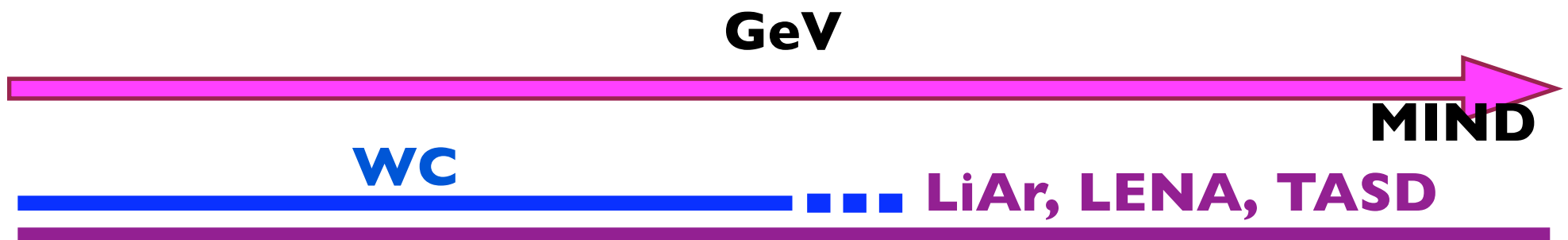


# Future long baseline experiments

Different options are considered, depending of the neutrino production technique:

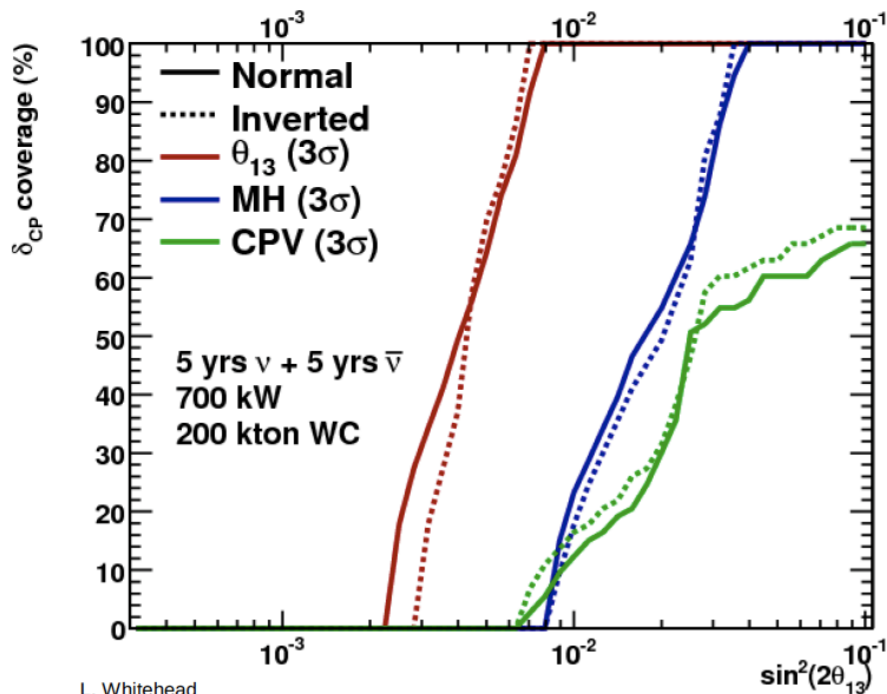
- **superbeams**
- **beta beams**
- **neutrino factory**

The **baseline determines the energy** of the beam and viceversa: exploit first oscillation maximum for best sensitivity. The energy and the oscillation channels impact on the type of detector used.

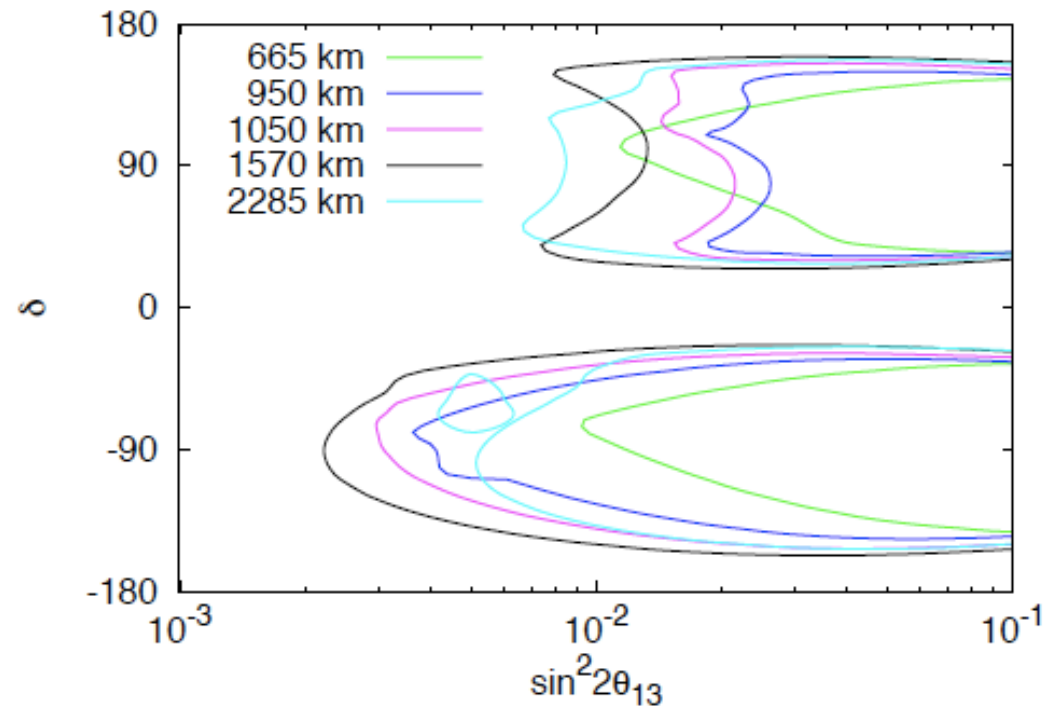


# Superbeams

Muon neutrinos come from pion decays with high fluxes and large detectors (T2K, NOvA, T2K-II, LBNE, SPL in EUROnu, LAGUNA-LBNO) at  $L \sim 100-2000$  km. Their sensitivity is ultimately limited by intrinsic background, systematics....



L. Whitehead

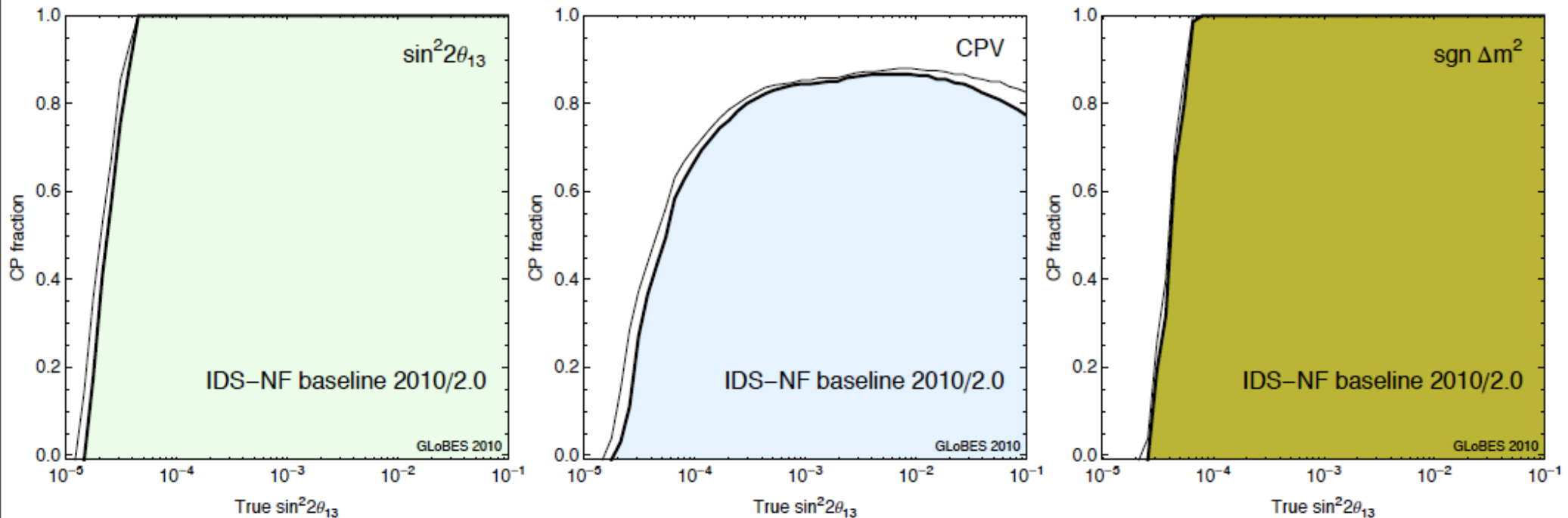


Coloma, SP, Li, in preparation

# Neutrino factory

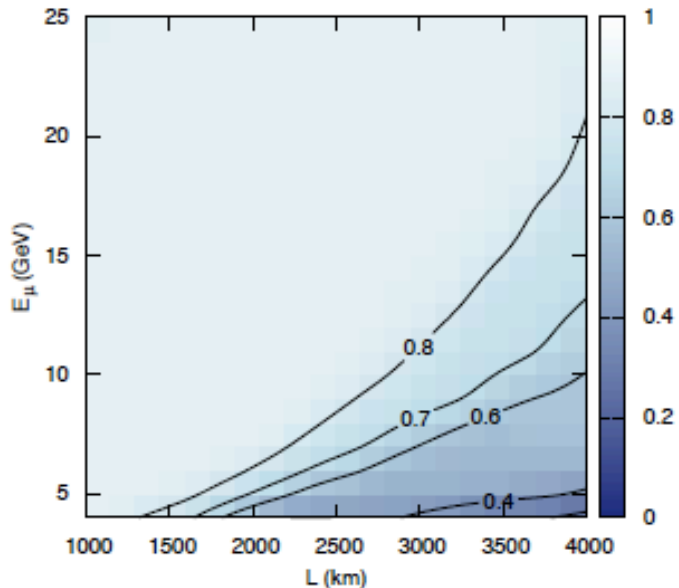
Neutrinos from muon decays at  $L \sim 1500-7000$  km.  
Pure beam and multiple oscillation channels but  
requires magnetised detector (MIND, LiAr).

See e.g. de Rujula, Gavela, Hernandez; Cervera et al.; Freund, Huber, Lindner; Rubbia ...

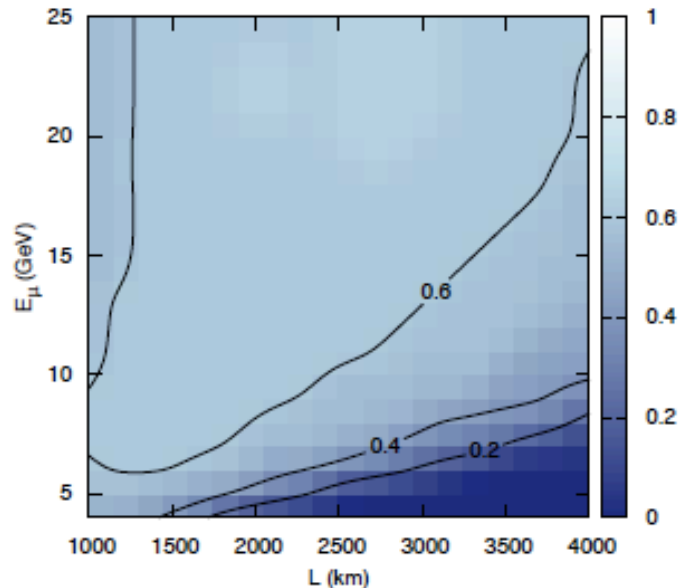


GLOBES, Huber, Lindner, Winter and Huber, Kopp, Lindner, Rolinec, Winter; see IDS-NF

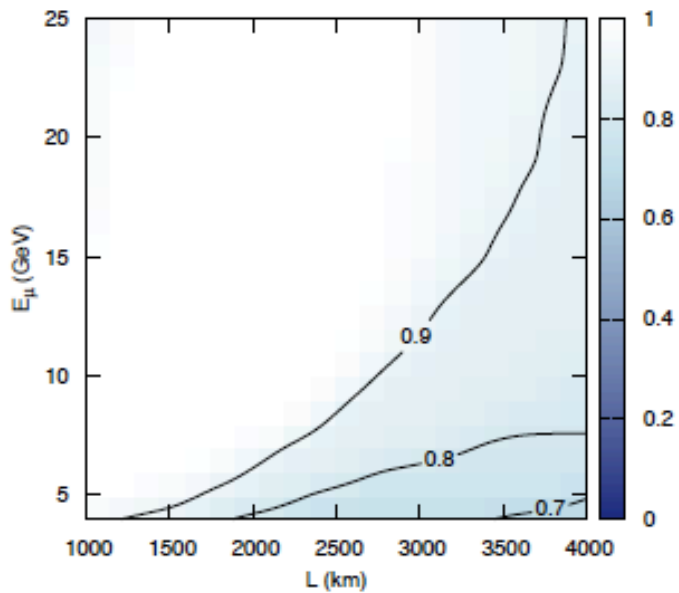
Neutrino factories (HENF, LENF) have excellent reach.



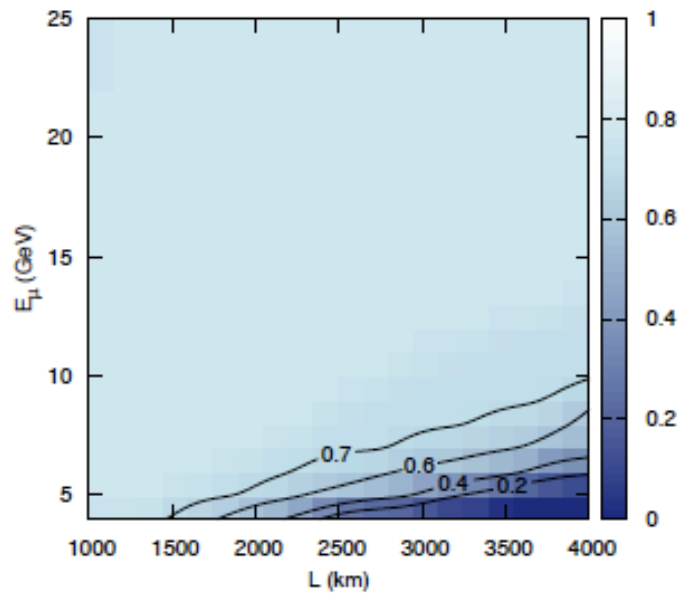
(a)TASD:  $\sin^2 2\theta_{13} = 10^{-2}$



(b)TASD:  $\sin^2 2\theta_{13} = 10^{-3}$



(c)LAr (optimistic):  $\sin^2 2\theta_{13} = 10^{-2}$



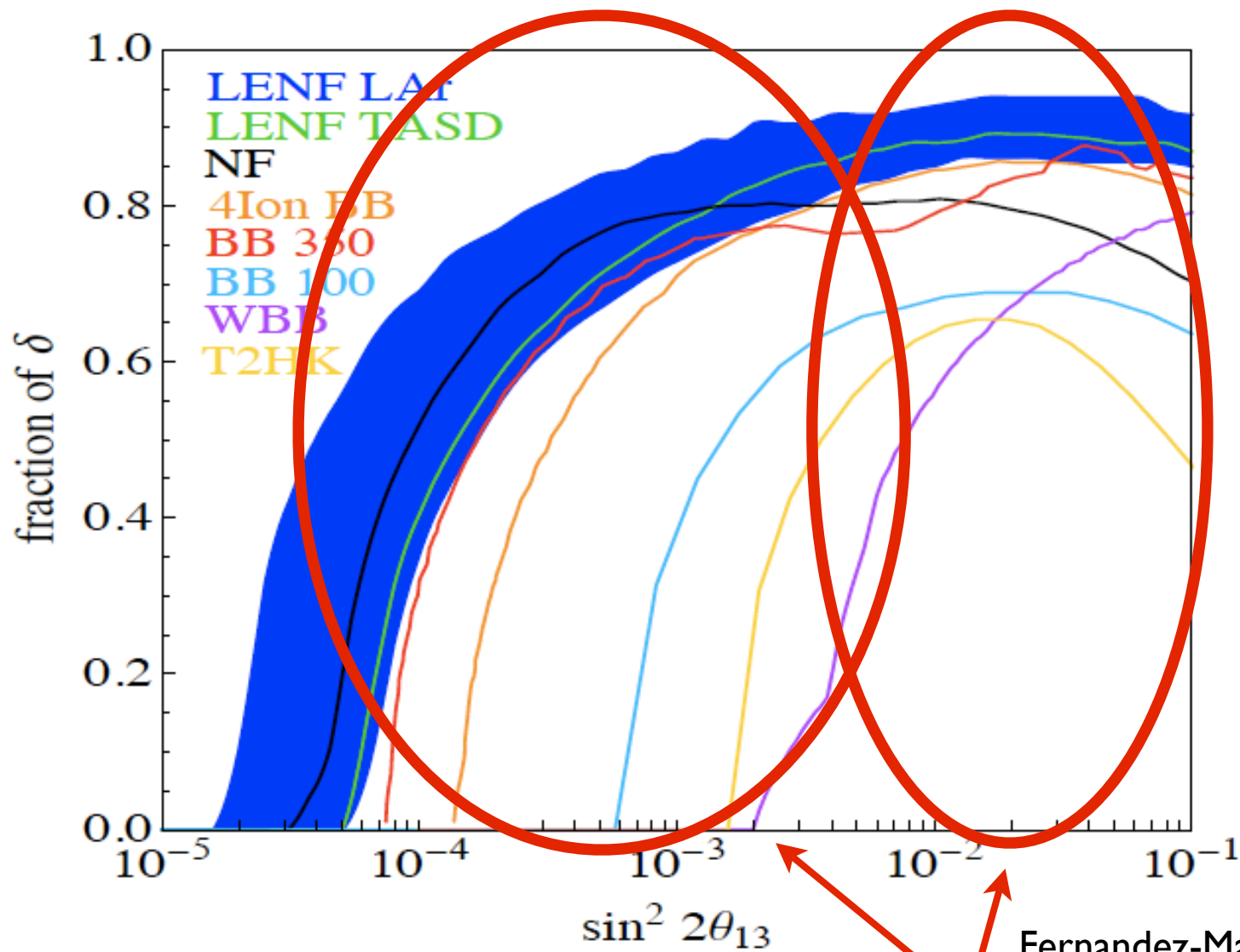
(d)LAr (optimistic):  $\sin^2 2\theta_{13} = 10^{-3}$

Sensitivity to CP-violation.

Lines show the fraction of delta for which CPV can be determined.

Excellent sensitivity for large  $\theta_{13}$  rather independent from L and E and increase in sensitivity with energy for small  $\theta_{13}$

Ballett, SP



**The best reach in CPV!**

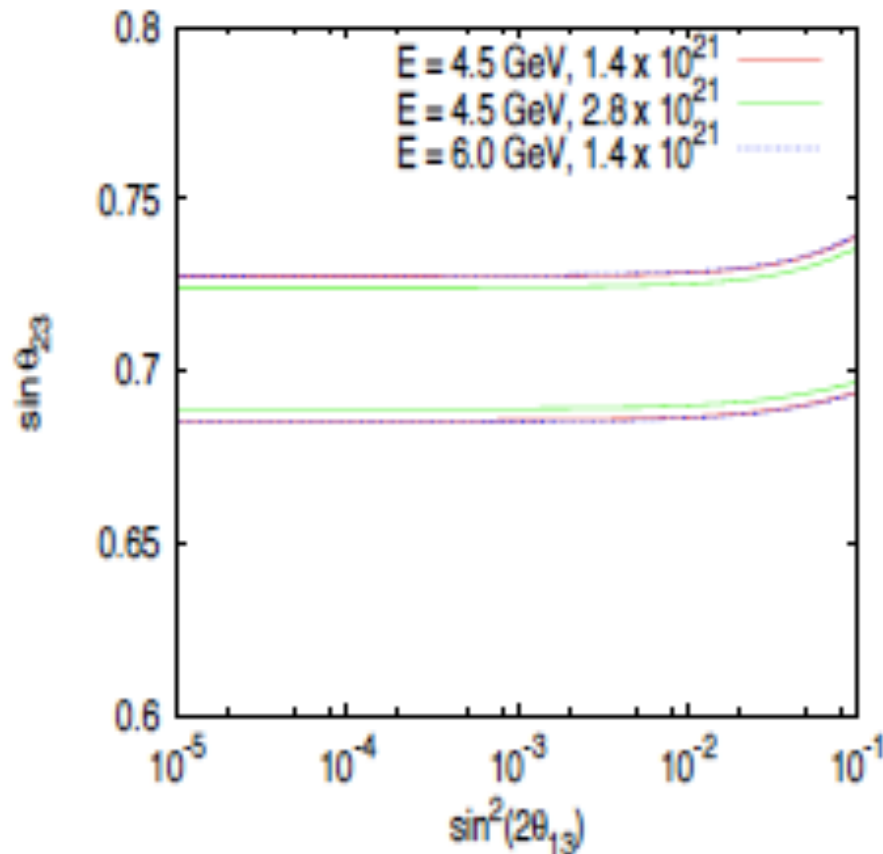
Fernandez-Martinez et al., 0911.3776

Depending on the values of  $\theta_{13}$  and on the precision required, **different experimental setups and optimisations are required.**



## Standard scenario: precision measurements

In order to discriminate models of flavour, it is important to measure with great precision the angles.



In particular,  
deviations from 45  
of  $\theta_{23}$   
from 0 of  $\theta_{13}$   
and the value  
of  $\theta_{12}$

# Testing the standard scenario

A plethora of hints of physics beyond 3 neutrino mixing and SM interactions is present.

LSND appearance experiment

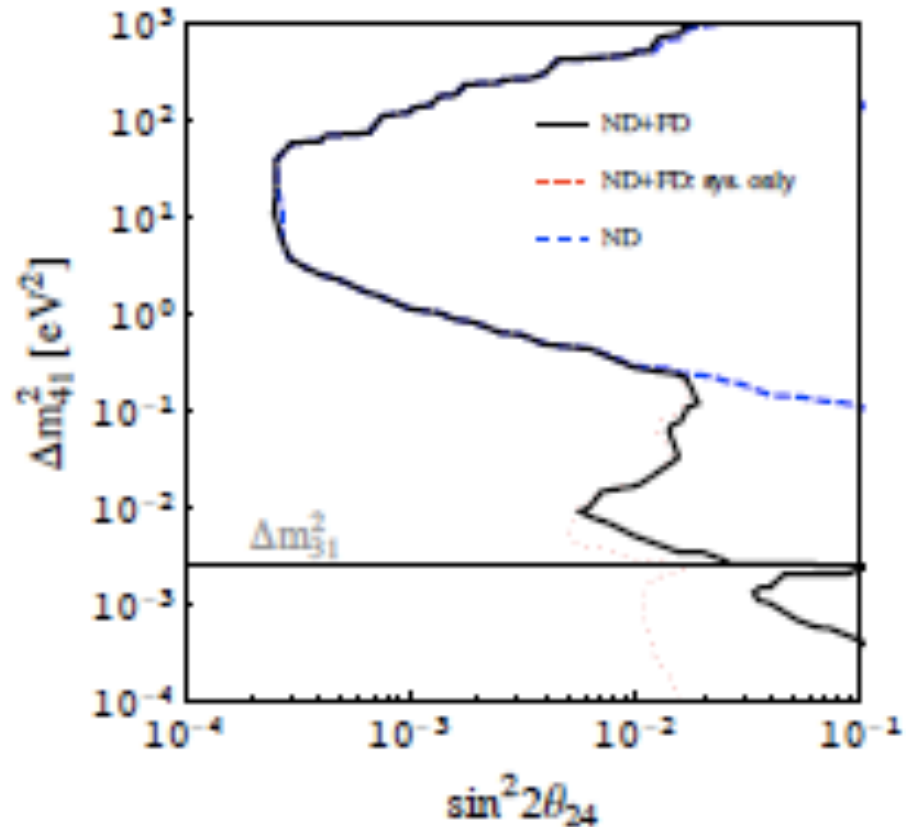
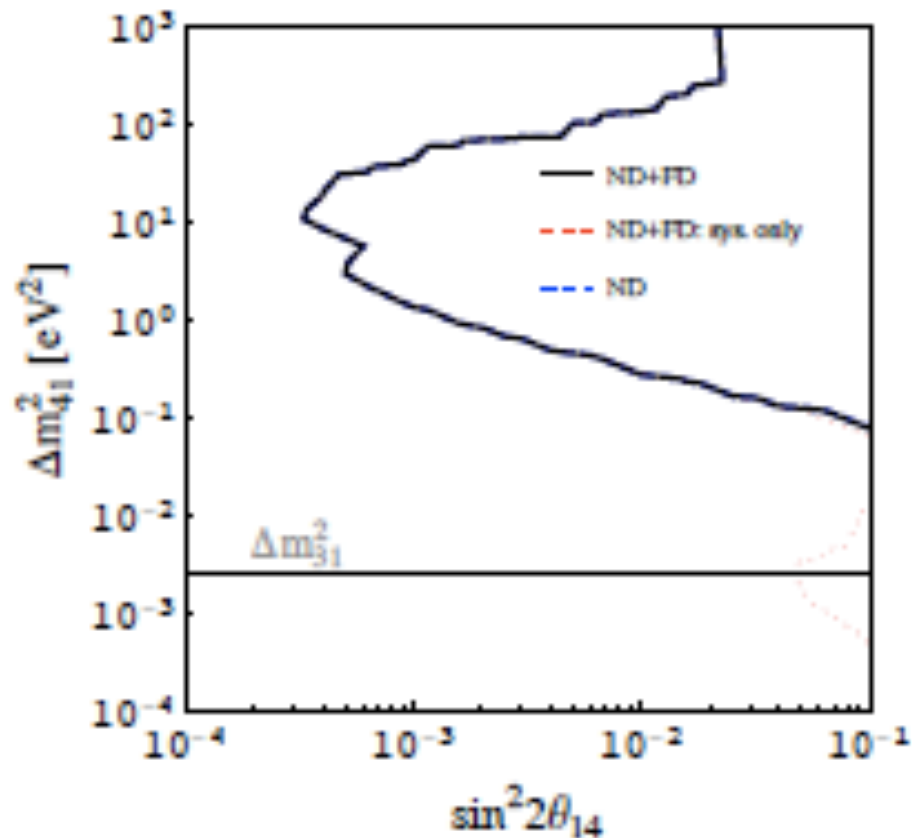
MiniBooNE neutrino and antineutrino results

Reactor anomaly

If confirmed, it would lead to a radical shift in our understanding of neutrino and physics BSM and would require a reanalysis of the reach of future neutrino oscillation experiments.

## Sterile neutrinos

**Sterile neutrinos** could be present in extensions of the SM with masses from sub-eV to GUT scale. Of phenomenological interest for oscillations are those with sub-eV to multi-eV masses (LSND, MiniBooNE). **New angles and CPV phases appear.**



See e.g. Meloni, Tang, Winter, 1007.2419. Also, Donini et al., Antusch et al., Tang and Winter...

## NSI

NSI appear as additional effects in the H:

$$\hat{H}^{fl} = U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta_{21} & 0 \\ 0 & 0 & \Delta_{31} \end{pmatrix} U^\dagger \pm A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu}^* & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau}^* & \epsilon_{\mu\tau}^* & \epsilon_{\tau\tau} \end{pmatrix}$$

NSI can arise in extensions of the SM. For instance D=6 operators typically lead to

$$\mathcal{O}^6 = \frac{1}{\Lambda^2} (L \ \gamma \ L) (L \ \gamma \ L) \longleftrightarrow \epsilon \sim g^2 M_W^2 / (g_{NSI}^2 M_{NSI}^2)$$

Strong bounds arise from oscillations, pion decay, CKM unitarity..., typically  $< 0.001$ ,  $0.1$ , and at the loop-level, if charged current processes cannot be avoided.

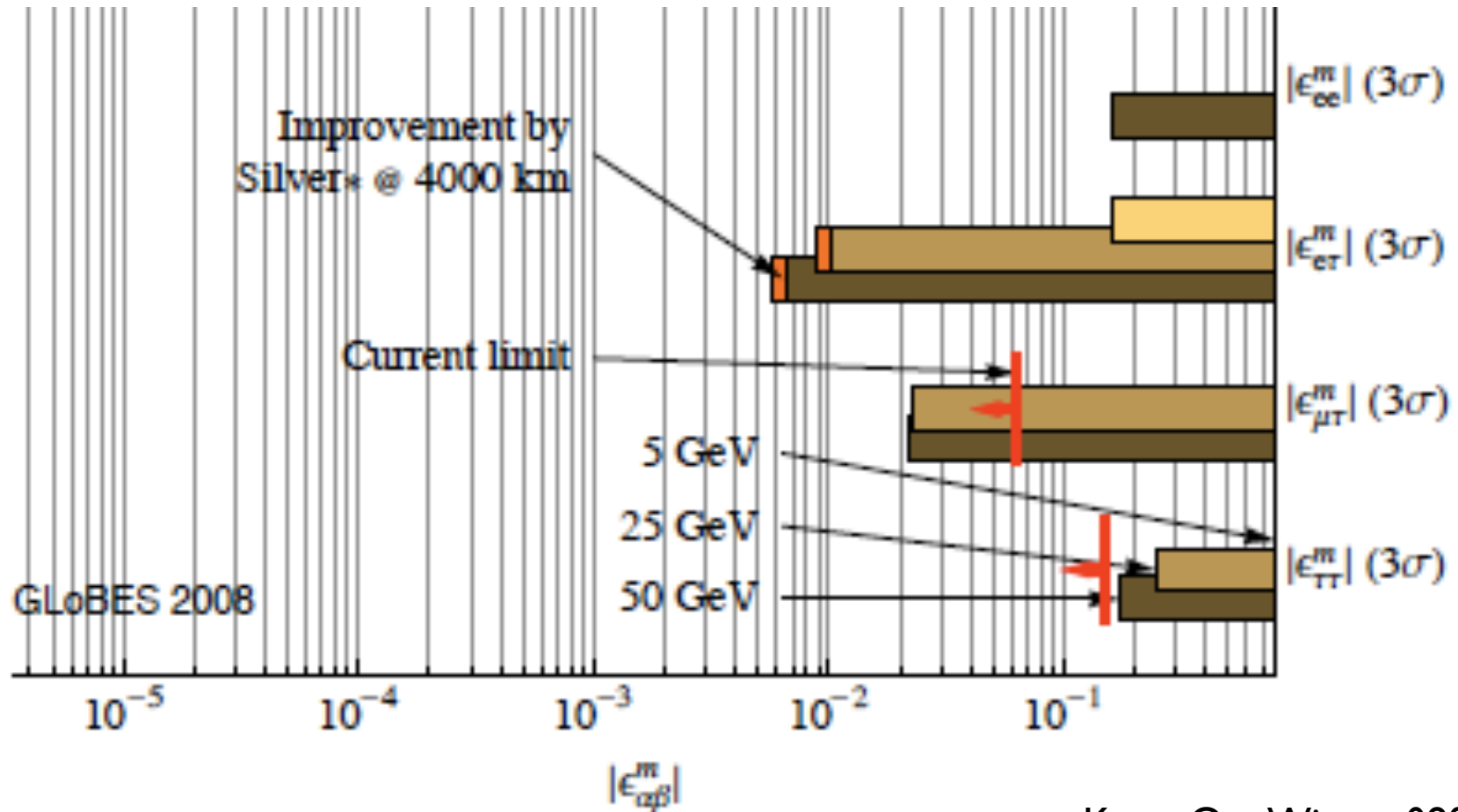
LBL experiments are also sensitive to **NSI** at source, propagation and detection (Grossman, 95):

matter effects

$$\begin{aligned}
 P_{\nu_e \rightarrow \nu_\mu} \simeq & \frac{s_{213}^2 s_{23}^2}{\left(1 - \frac{A}{\Delta_{31}}\right)^2} \\
 & + \frac{s_{213} c_{13} s_{212} s_{223}}{1 - \frac{A}{\Delta_{31}}} \frac{\Delta_{21}}{A} \sin\left(\frac{AL}{2}\right) \cos\left(\frac{\pi + AL}{2} - \delta\right) \\
 & - 4\varepsilon_{e\mu} \frac{s_{213} c_{23} s_{23}^2}{1 - \frac{A}{\Delta_{31}}} \sin\left(\frac{AL}{2}\right) \cos\left(\frac{\pi + AL}{2} - \delta + \phi_{e\mu}\right) \\
 & - 4\varepsilon_{e\tau} \frac{s_{213} c_{23} s_{23}^2}{1 - \frac{A}{\Delta_{31}}} \sin\left(\frac{AL}{2}\right) \cos\left(\frac{\pi + AL}{2} - \delta + \phi_{e\tau}\right)
 \end{aligned}$$

The longer baseline (higher energy), the better the physics reach as NSI effects become more important.

The HENF provides the best sensitivity to NSI:



Kopp, Ota, Winter, 0804.2261

This analysis assumes two MIND detectors and therefore the reach for  $E=5$  GeV is very limited.

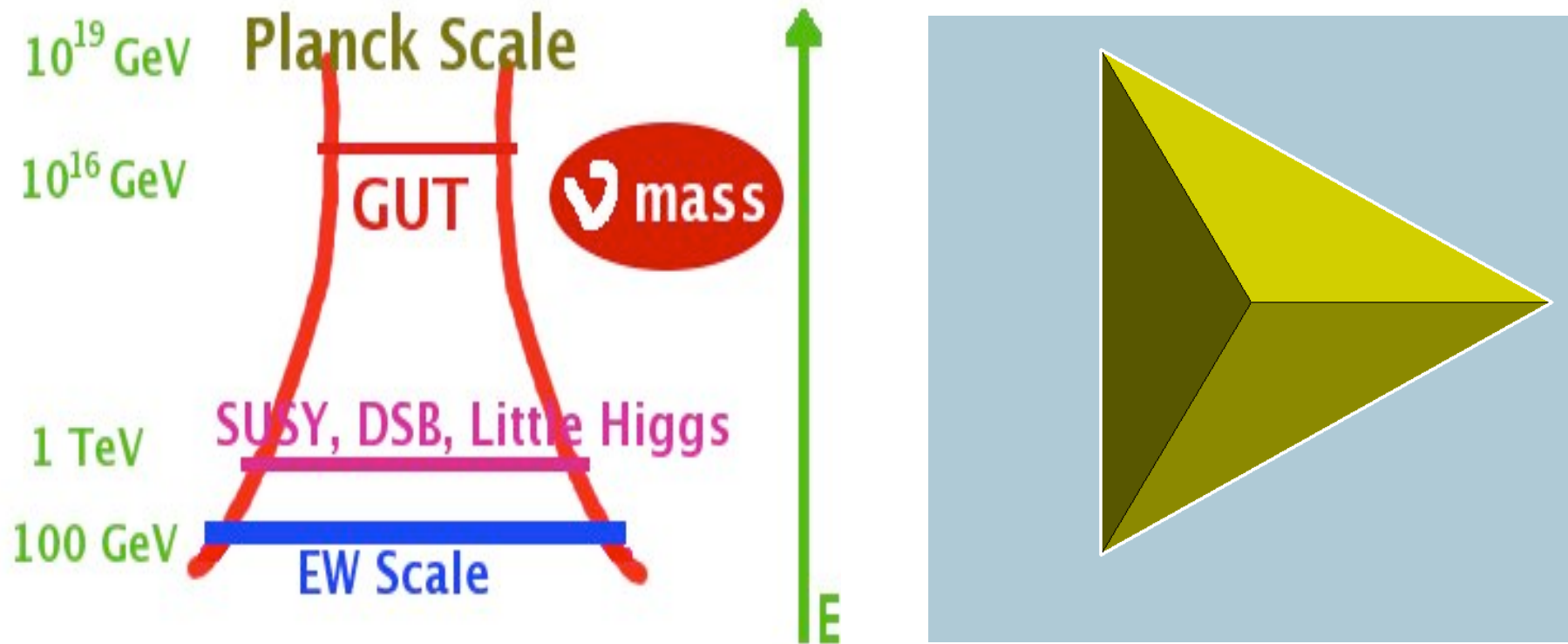
**Neutrino Physics** provides information  
on the **fundamental laws of Nature**  
and on the **evolution of the Universe**.

**Open window on  
the Physics beyond the  
SM at scales, possibly  
not otherwise  
reachable.**

**Neutrinos are  
messengers from  
the Early Universe and  
from Extreme  
Astrophysical  
Environments.**

# Open window on Physics beyond the SM

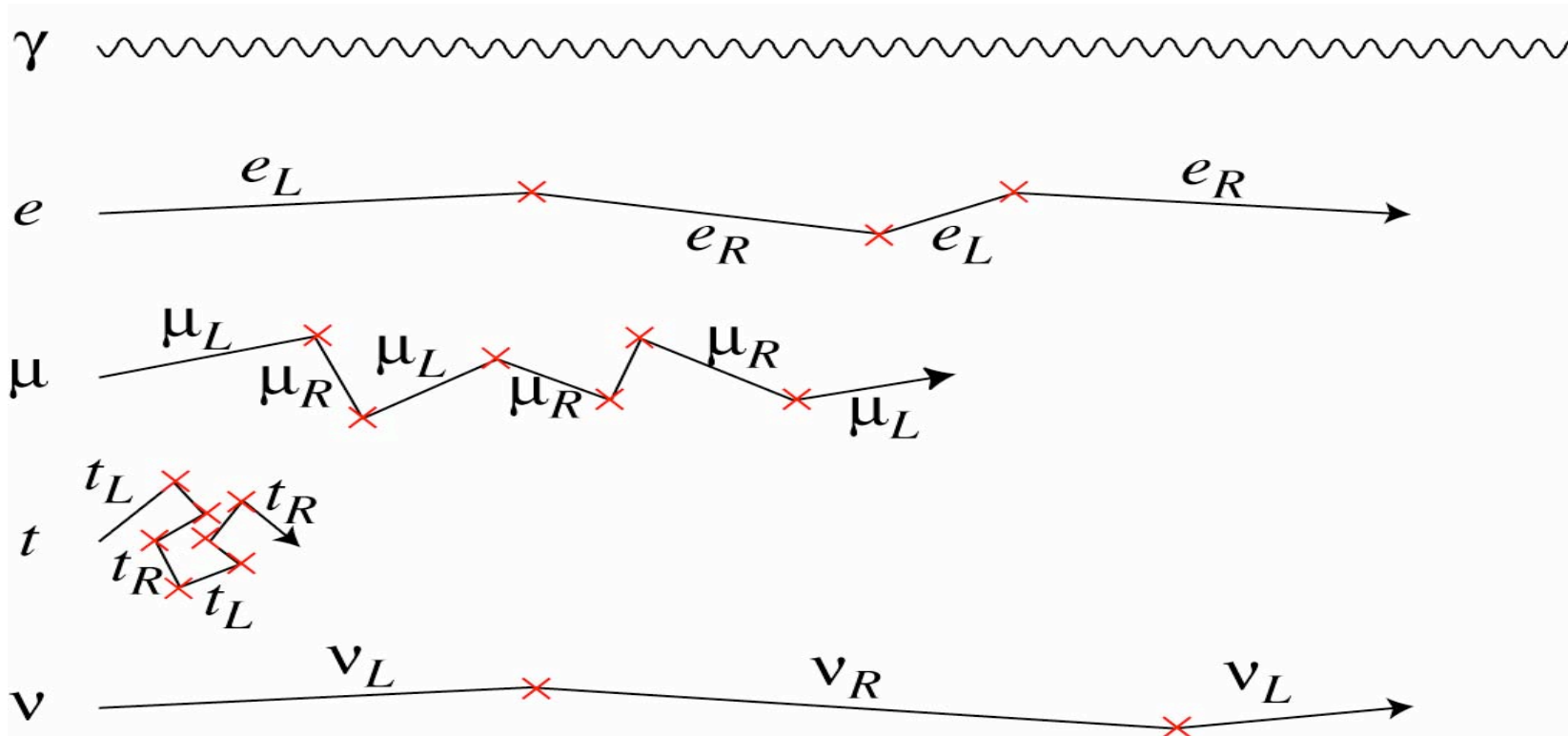
Neutrino physics gives a new perspective on physics BSM.



This information is **complementary** with the one which comes from flavour physics experiments and from colliders.



Neutrino masses in the sub-eV range cannot be explained naturally within the SM.

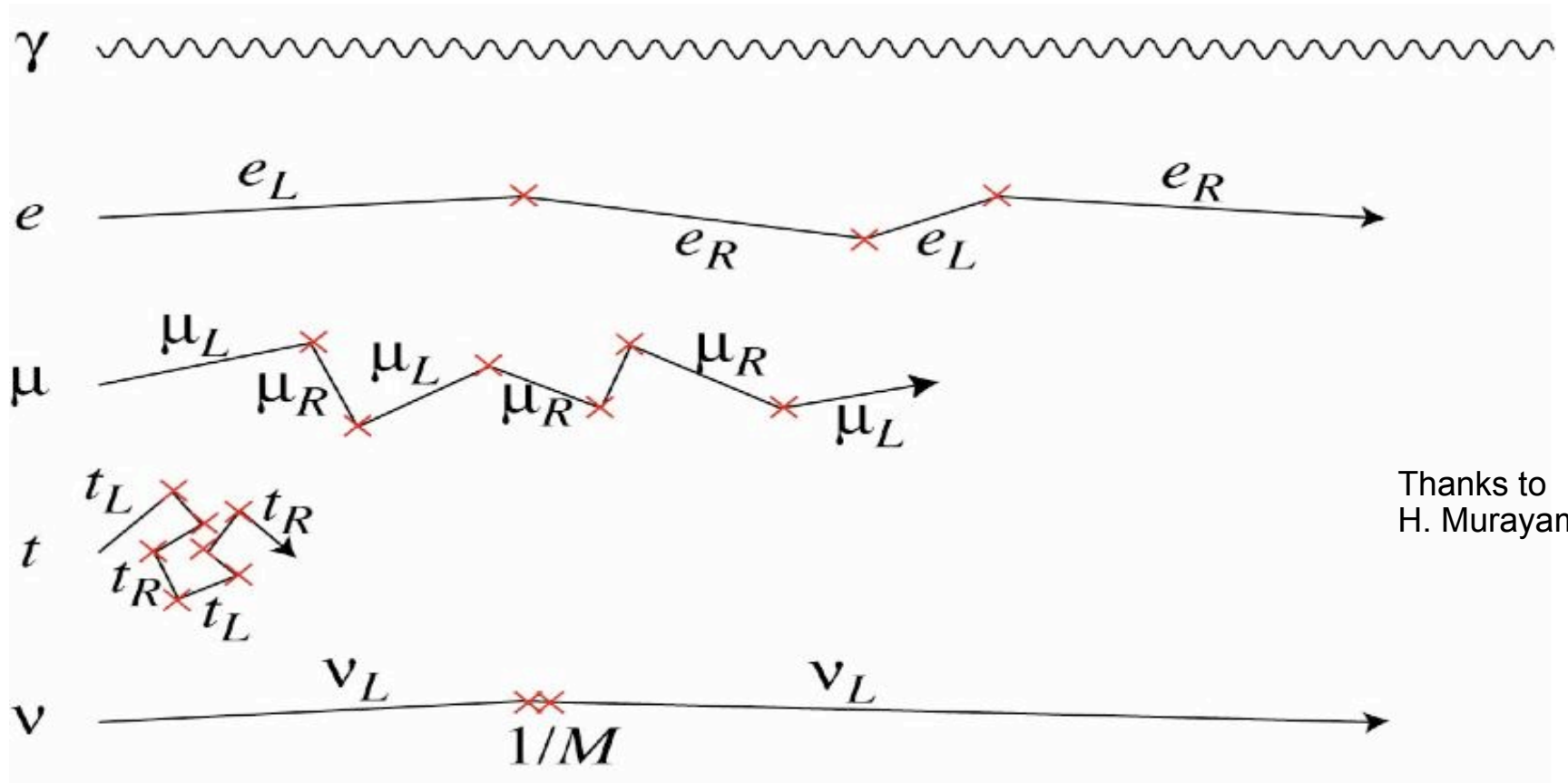


Thanks to  
H. Murayama

$$y_\nu = \frac{m_\nu}{v} = \frac{0.1 \text{ eV}}{250 \text{ GeV}} = 4 \times 10^{-13}$$

Many theorists consider this explanation of neutrino masses unnatural.

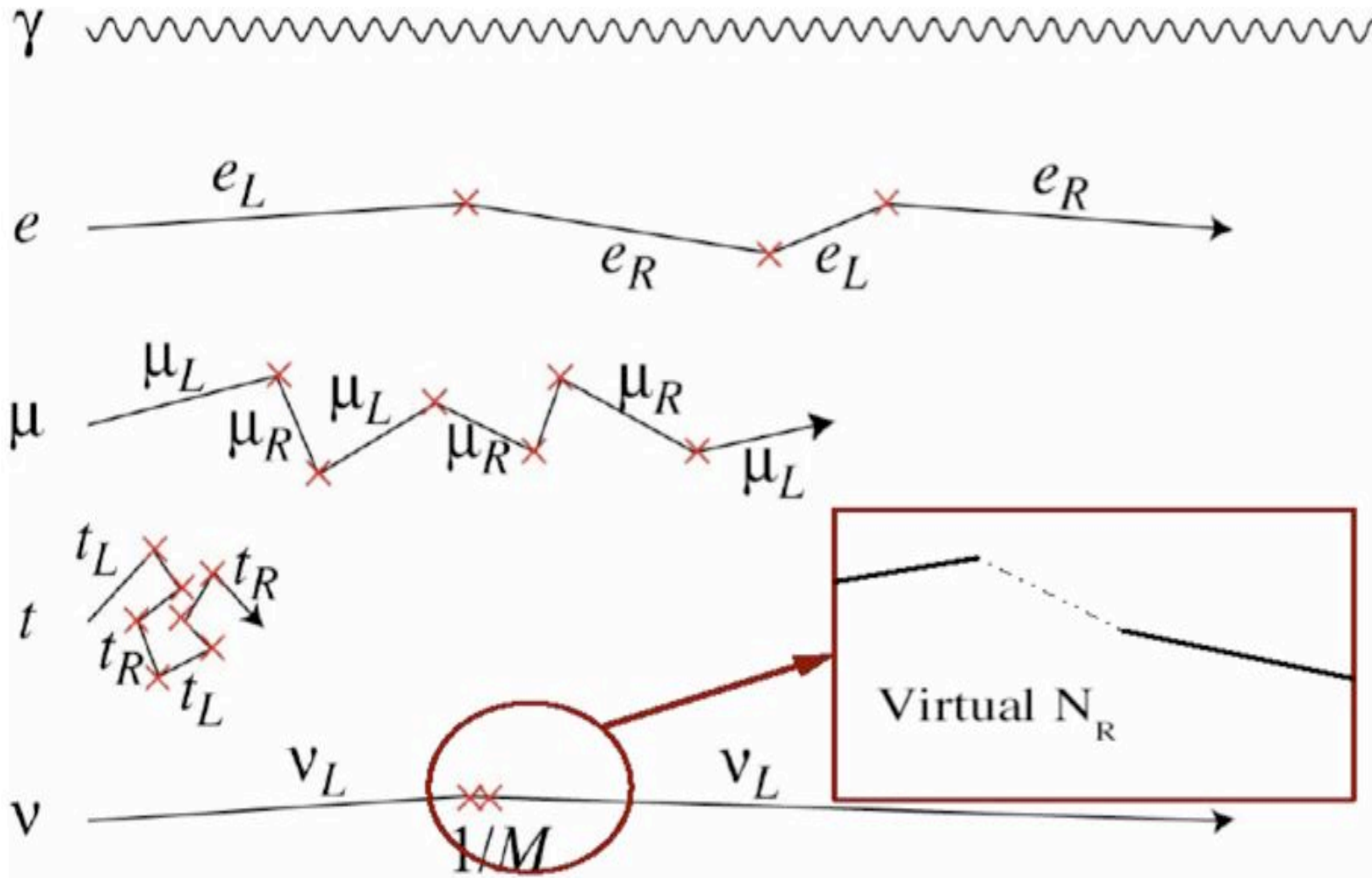
If neutrino are Majorana particles (neutrinos and antineutrinos are indistinguishable), a different type of neutrino mass can be generated (**Majorana mass**):



Thanks to  
H. Murayama

$$-\mathcal{L} = \lambda \frac{\nu_L H \nu_L H}{M} = \frac{\lambda v^2}{M} \nu_L^T C \nu_L$$

The Majorana mass term can arise as the **low energy realisation of a higher energy theory.**

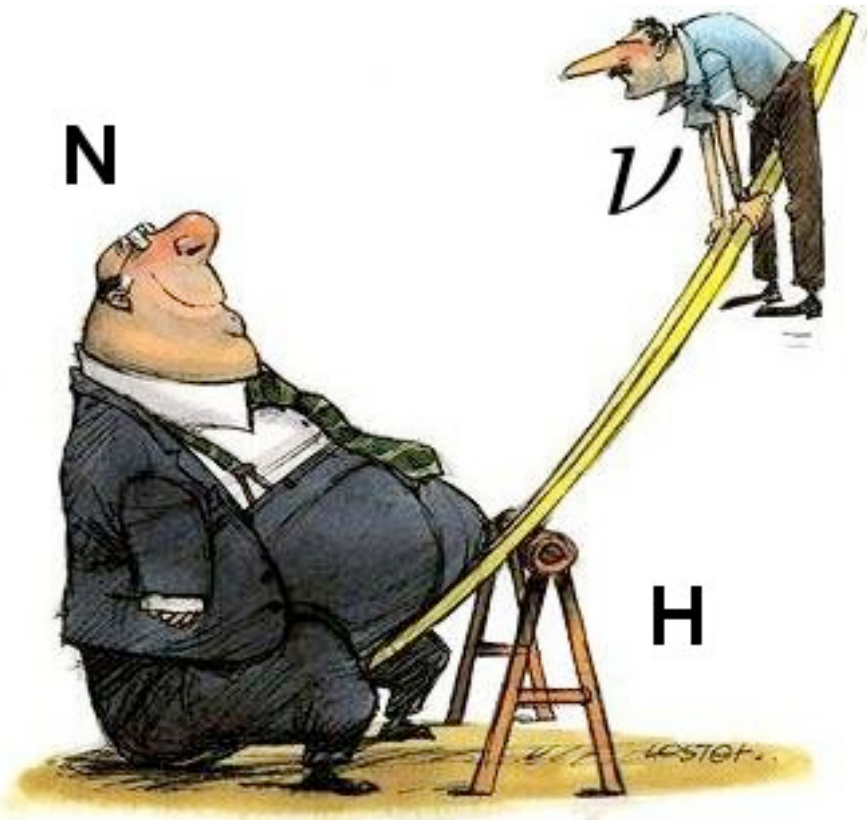


Thanks to  
H. Murayama

$$m_\nu = \frac{\lambda^2 v^2}{M} \rightarrow M \sim 10^{14} \text{ GeV}$$

# The see saw mechanism

In the **see-saw mechanism**, neutrinos acquire a very small mass due to their interactions. Minkowski; Yanagida; Gell-Mann, Ramond, Slansky.



- Introduce a right handed neutrino **N**
- Couple it to the Higgs and left handed neutrinos

$$m_{light} \simeq \frac{m_D^2}{M_R} \sim \frac{100 \text{ GeV}^2}{10^{14} \text{ GeV}} \sim 0.1 \text{ eV}$$

Other models have new particles at TeV scale, testable at the LHC.

# The flavour problem

Mixing is compatible with **tri-bi-maximal** pattern.

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} -\frac{2}{\sqrt{6}} & \frac{1}{\sqrt{3}} & 0 \\ \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Harrison, Perkins, Scott

This can arise from specific forms of the neutrino mass matrix with flavour symmetries (e.g. A4).

$$(M_{eff}^\nu)^{TBM} = \begin{pmatrix} a & b & b \\ \cdot & d & (a + b - d) \\ \cdot & \cdot & d \end{pmatrix}$$

Low, Volkas

Determining the deviations from TBM is important to understand the underlying flavour theory. Typically the deviations will be related together. For ex.

$$\sin^2 \theta_{13} = \frac{1}{3} \sin^2 \bar{\theta}, \quad \sin^2 \theta_{12} = \frac{\cos^2 \bar{\theta}}{3 - \sin^2 \bar{\theta}}, \quad \sin^2 \theta_{23} = \frac{3 \left| \cos \bar{\theta} - \sqrt{\frac{2}{3}} e^{i\gamma} \sin \bar{\theta} \right|^2}{3 - \sin^2 \bar{\theta}}$$

Ballett, King, Lhun, SP,  
Schmidt

In other models, e.g. GUTs, other connections between the values of the mixing angles can be found. For ex.

$$\theta_{12}^o = 35^\circ + \theta_{13}^o \cos \delta$$

King; Antusch, King; Masina

# Neutrinos are messengers from the Universe

**Supernovae**

**Dark Matter  
annihilations**

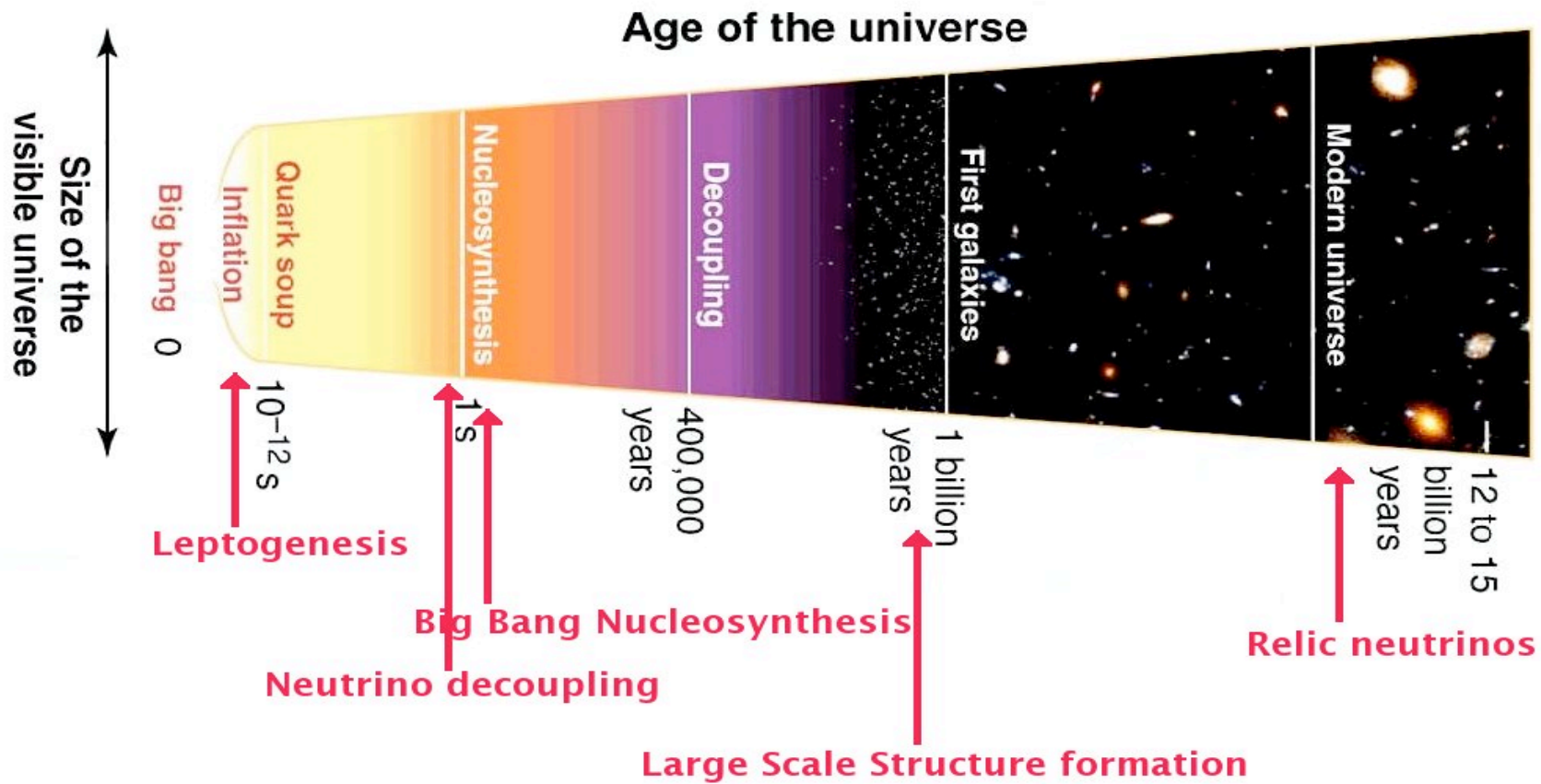
**Leptogenesis**

**Relic  
neutrinos**

**Big Bang  
Nucleosynthesis**

**Sterile  
Neutrinos as  
Dark Matter**

**HDM and structure  
formation**



Neutrinos constitute a **hot dark matter** component and affect the **formation of clusters of galaxies**.

Sterile neutrinos with  $m \sim eV$  behave as HDM and are severely constrained by cosmology.

Sterile neutrinos with  $m \sim keV$  are WDM.

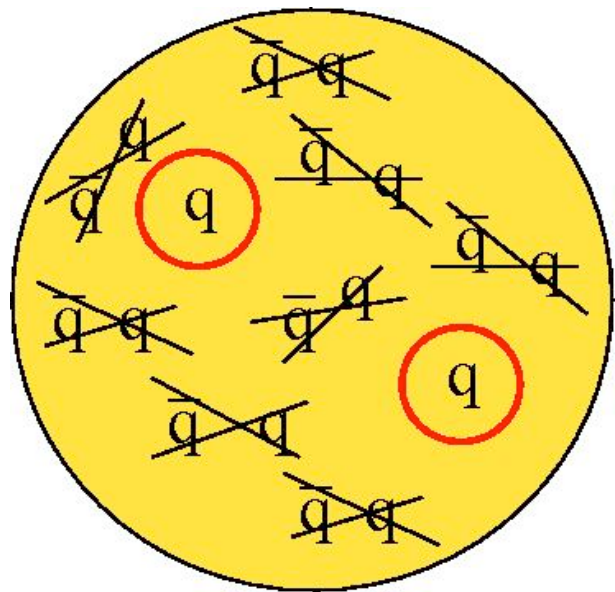


# Leptogenesis and the Baryon Asymmetry

1000000000  
quarks

In the Early  
Universe

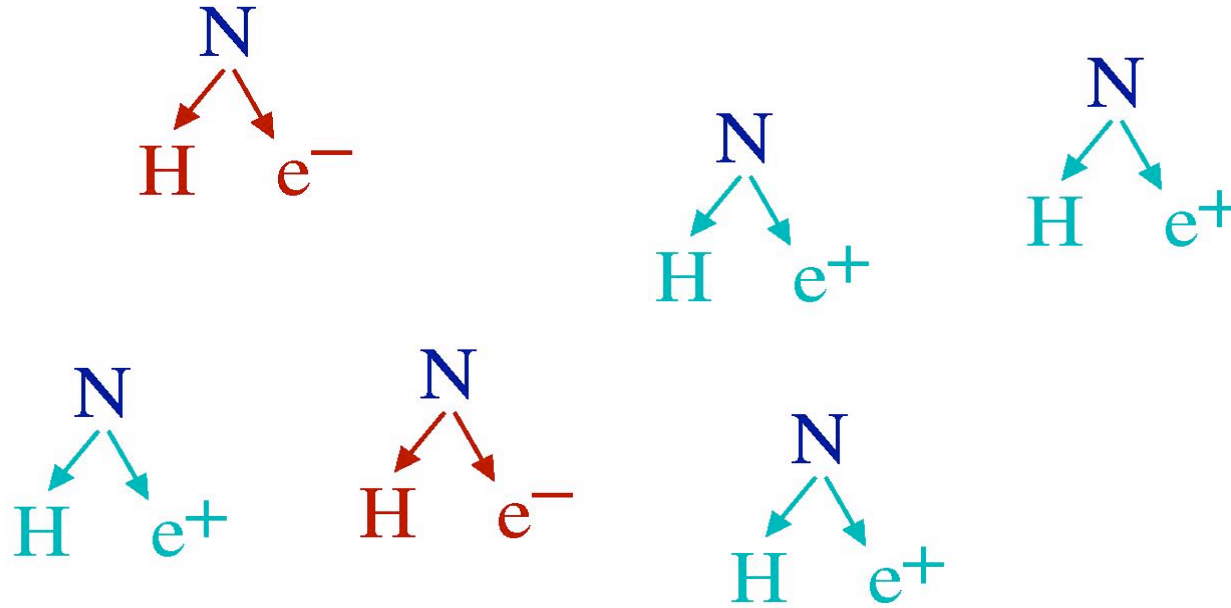
10000000000  
antiquarks



As the temperature drops,  
only quarks are left:

$$Y_B = \frac{n_B}{n_\gamma} = (6.0 \pm 0.2) \times 10^{-10}$$

The excess of quarks can be explained by **Leptogenesis** (Fukugita, Yanagida): the heavy  $N$  responsible for neutrino masses generate a lepton asymmetry.



Excess of  $e^+$   $\longrightarrow$  excess of  $q$  over  $\bar{q}$

This requires **L violation, CP-violation** and **non-equilibrium** (expansion of the EU).  
The lepton asymmetry is then converted into the baryon asymmetry.

The **see-saw mechanism** (type I) might be responsible for **neutrino masses** and the **baryon asymmetry**.

Is there a **connection** between the two?

- In general, there are more parameters at high energy (where leptogenesis happens) w.r.t. the ones we can measure in experiments at low energy.
- Due to **flavour effects**, if we **observe CPV at low energy** we know that generically a **baryon asymmetry** was generated.
- **Observing L violation and CPV** would constitute a **strong hint in favour of leptogenesis as the origin of the baryon asymmetry**.

# Conclusions

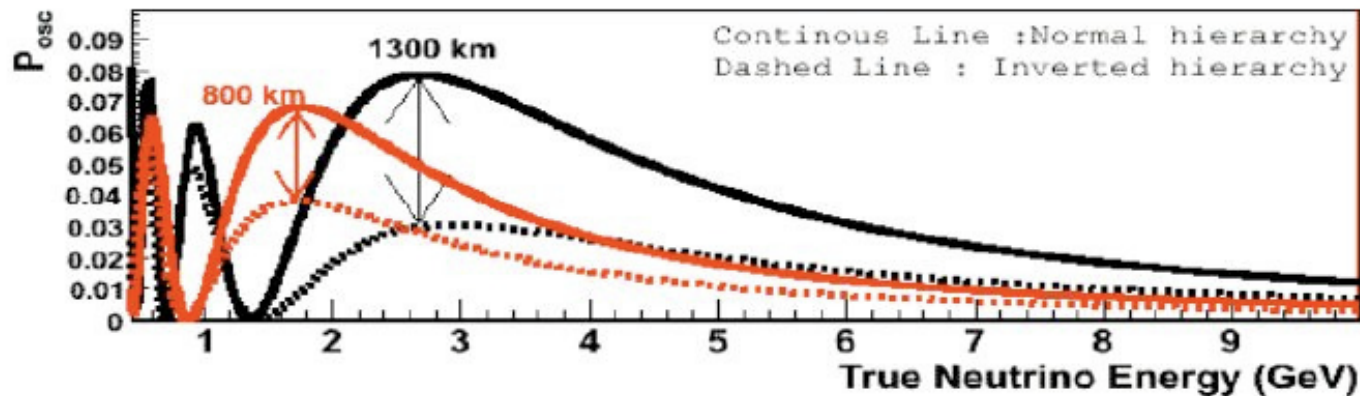
- In the past few years, the neutrino oscillation parameters have been measured with good precision. The (near) present experiments are going to improve the precision and possibly discover  $\theta_{13}$  .
- A wide future neutrino programme is planned: neutrinoless double beta decay and long baseline neutrino oscillation experiments.
- They will give crucial information on neutrino properties in order to understand the **origin of neutrino masses** and the **problem of flavour**. **Precision measurements** will be crucial.

# LBNE



Wideband beam which exploits the rich oscillatory pattern.  
With Project X (from 700 kW to 2 MW), even better sensitivities could be obtained.

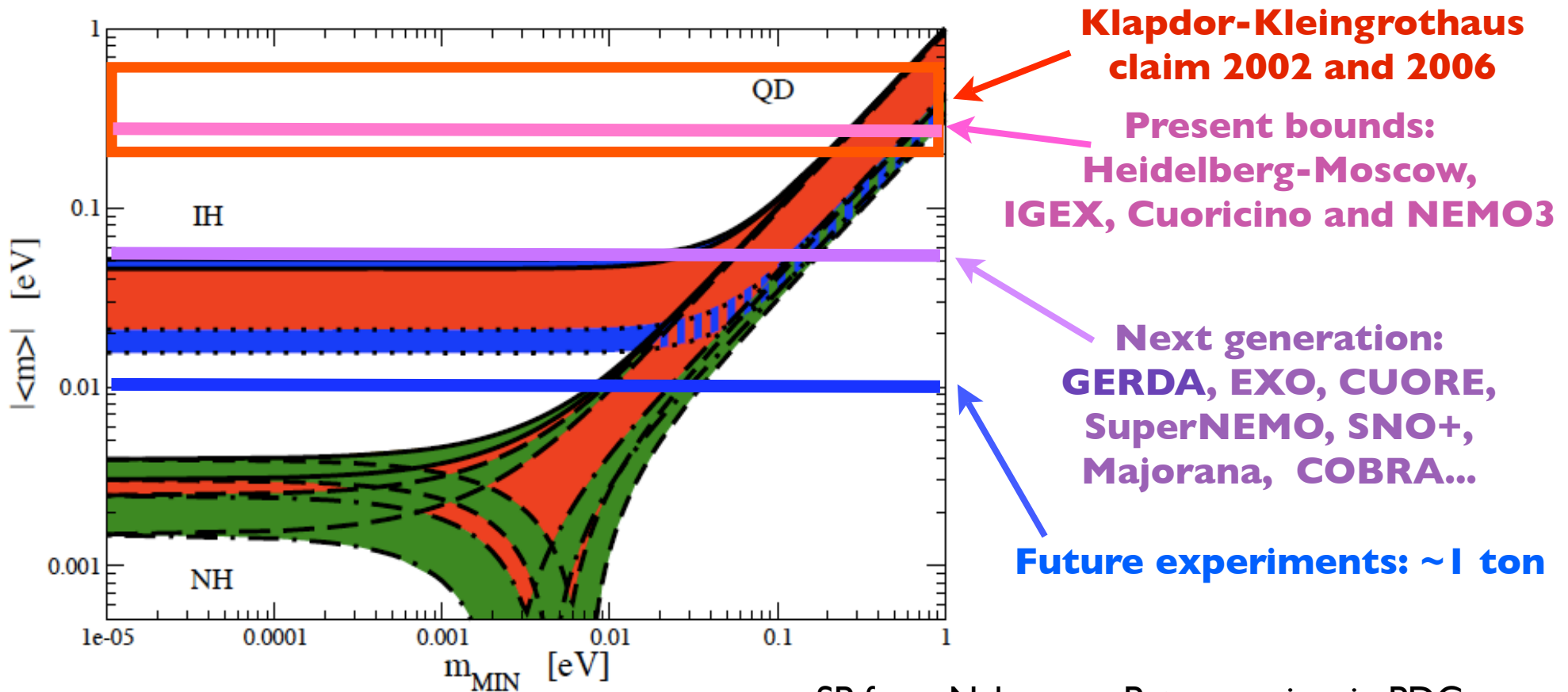
Presented by S. Parke at NeuTel 2011



# Neutrinoless double beta decay

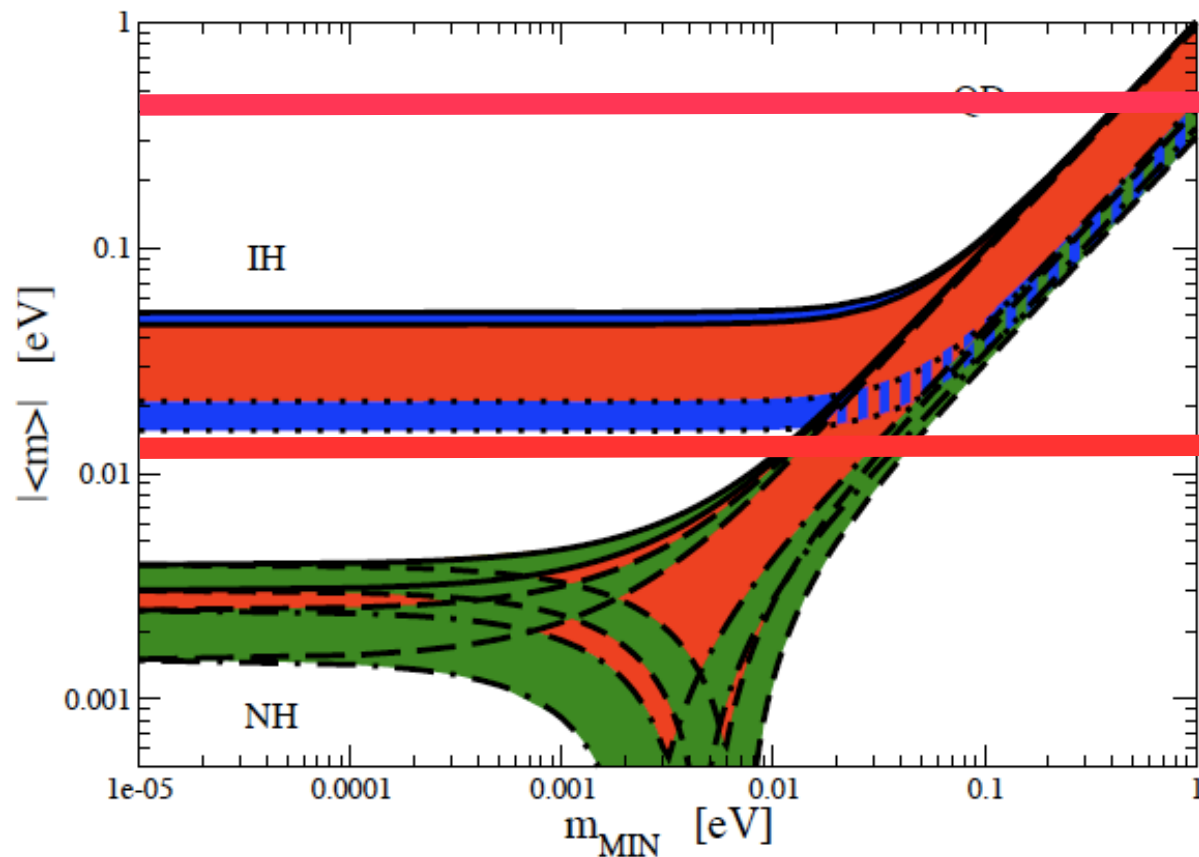
The half-life depends on neutrino properties through

$$|\langle m \rangle| \sim |m_1 \cos^2 \theta_{12} + m_2 \sin^2 \theta_{12} e^{i\alpha_{21}} + m_3 \sin^2 \theta_{13} e^{i\alpha_{31}}|$$



SP from Nakamura, Petcov review in PDG

Wide experimental program for the future:  
**a positive signal would indicate that L is violated!**  
It might give information on neutrino masses (and CPV).



It will be critical to establish the origin of the signal (light or heavy Majorana neutrinos, RV SUSY,...).

- $(\theta_{13}, \delta)$  degeneracy (Koike, Ota, Sato; Burguet-Castell et al.)

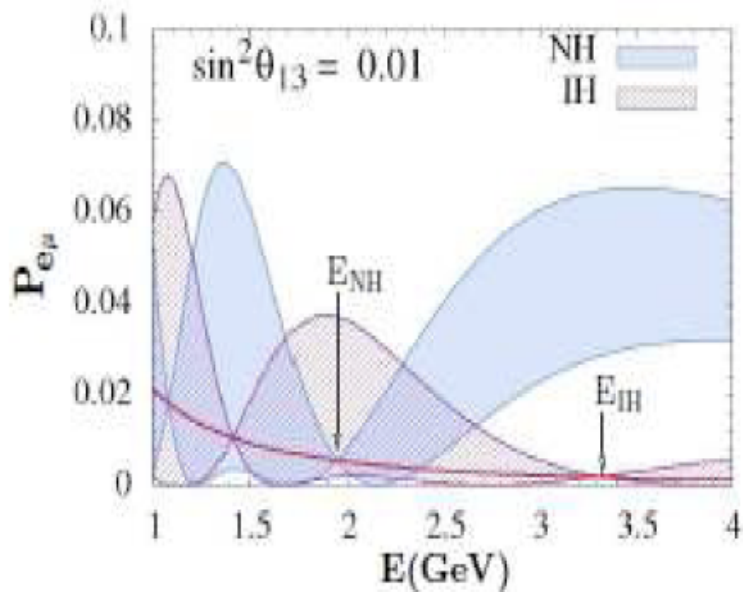
$$\delta' = \pi - \delta$$

$$\theta'_{13} = \theta_{13} + \cos \delta \sin 2\theta_{12} \frac{\Delta m_{12}^2 L}{4E} \cot \theta_{23} \cot \frac{\Delta m_{13}^2 L}{4E}$$

Having **information at different L/E** can resolve this.

- $\text{sign}(\Delta m_{31}^2)$  vs CPV (matter effects). In vacuum:

$$\delta' \rightarrow \pi - \delta \quad \text{sign}'(\Delta m_{13}^2) \rightarrow -\text{sign}(\Delta m_{13}^2)$$



This degeneracy is broken by matter effects.

For ex. Bimagic baseline at  $L=2540$  km  
Excellent sensitivity to the hierarchy

A. Dighe et al., 1009.1093; Raut et al. 0908.3741; Joglekar et al. 1011.1146

- the octant of  $\theta_{23}$  (low E data) (Fogli, Lisi)