# Benemérita Universidad Autónoma de Puebla 

and<br>Dual C-P Institute of High Energy Physics, México

Updating of 2HDM-III employing a four-zero texture in the Yukawa matrices and phenomenology of the charged Higgs

Present: Jaime Hernández-Sánchez

## Outline

- Brief introduction of 2HDM-III, employing four zero texture in the Yukawa matrices.
- As this version of 2HDM-III could contain the other versions of 2HDM.
- Flavor contraints at low energy processes.
- Phenomenology of charged Higgs could be quite different.
- Some interesting decays channels of $\mathrm{H}+$ :
$\mathrm{H}+\rightarrow \mathrm{cs}, \mathrm{cb}, \mathrm{ts}, \mathrm{W}$ gamma, W Z


## Versions of the 2HDM

Type I: one Higgs doublet provides masses to all quarks (up- and down-type quarks) (~SM).

Type II: one Higgs doublet provides masses for up-type quarks and the other for down-type quarks ( $\sim$ MSSM).

Type III: the two doublets provide masses for up and down type quarks, as well as charged leptons.
We could consider this model as a generic description of physics at a higher scale (i. e. Radiative corrections of the MSSM Higgs sector* or from extradimension**).
*J. L. Díaz-Cruz, R. Noriega-Papaqui and A. Rosado, Phys. Rev. D 71, 015014 (2005).
**A. Aranda, J.L. Díaz-Cruz, J. Hernández-Sánchez, R. Noriega-Papaqui, Phys. Lett. B 658, 57 (2007).

$$
\begin{aligned}
\mathcal{L}_{\text {yukawa }}^{\mathrm{THDM}}= & -\sum_{f=u, d, \ell}\left(\frac{m_{f}}{v} \xi_{h}^{f} \bar{f} f h+\frac{m_{f}}{v} \xi_{H}^{f} \bar{f} f H-i \frac{m_{f}}{v} \xi_{A}^{f} \bar{f} \gamma_{5} f A\right) \\
& -\left\{\frac{\sqrt{2} V_{u d}}{v} \bar{u}\left(m_{u} \xi_{A}^{u} \mathrm{P}_{L}+m_{d} \xi_{A}^{d} \mathrm{P}_{R}\right) d H^{+}+\frac{\sqrt{2} m_{\ell} \xi_{A}^{\ell}}{v} \overline{\nu_{L}} \ell_{R} H^{+}+\text {H.c. }\right\},
\end{aligned}
$$

|  | $\xi_{h}^{u}$ | $\xi_{h}^{d}$ | $\xi_{h}^{\ell}$ | $\xi_{H}^{u}$ | $\xi_{H}^{d}$ | $\xi_{H}^{\ell}$ | $\xi_{A}^{u}$ | $\xi_{A}^{d}$ | $\xi_{A}^{\ell}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Type-I | $c_{\alpha} / s_{\beta}$ | $c_{\alpha} / s_{\beta}$ | $c_{\alpha} / s_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $\cot \beta$ | $-\cot \beta$ | $-\cot \beta$ |
| Type-II | $c_{\alpha} / s_{\beta}$ | $-s_{\alpha} / c_{\beta}$ | $-s_{\alpha} / c_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $c_{\alpha} / c_{\beta}$ | $c_{\alpha} / c_{\beta}$ | $\cot \beta$ | $\tan \beta$ | $\tan \beta$ |
| Type-X | $c_{\alpha} / s_{\beta}$ | $c_{\alpha} / s_{\beta}$ | $-s_{\alpha} / c_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $c_{\alpha} / c_{\beta}$ | $\cot \beta$ | $-\cot \beta$ | $\tan \beta$ |
| Type-Y | $c_{\alpha} / s_{\beta}$ | $-s_{\alpha} / c_{\beta}$ | $c_{\alpha} / s_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $c_{\alpha} / c_{\beta}$ | $s_{\alpha} / s_{\beta}$ | $\cot \beta$ | $\tan \beta$ | $-\cot \beta$ |

TABLE II: The mixing factors in Yukawa interactions in Eq. (6)

Mayumi Aoki, Shinya Kanemura, Koji Tsumura, Kei Yagyu. Phys.Rev. D80 (2009) $0150 \not{ }^{\sharp} 7$

## Absence of (tree-level) FCNCs

$\rightarrow$ constraints on Higgs couplings

In SM FCNC automatically absent as same operation diagonalising the mass matrix automatically diagonalises the Higgs-fermion couplings.

- There are three ways:
- (1) Discrete symmetries. This choice is based on the Glashow-Weinberg's theorem concerning FCNC's in models with several Higgs doublets.
(MSSM: Y=-1 (+1) doublet copules to donw (up)-type fermion, as required by SUSY)
- (2) Radiative suppression. When a given set of Yukawa matrices are present at tree-level, but the other ones arise only as a radiative effect: i.e. the 2 HDM -II, it is transformed into 2HDM-III through loops-effects of sfermions and gauginos.
- (3) Flavor symmetries. Suppression of FCNC effects can also be achieved when a certain form of the Yukawa matrices that reproduce the observed fermion masses and mixing angles is implemented in the model, i.e. THDM-III. (Yukawa textures)
J.L. Diaz-Cruz, R Noriega-Papaqui, A. Rosado. Phys. Rev. D69,095002 (2004)


## Seesaw mechanism in MSSM

Flavor Violation among the Sleptons. In the leptonic sector, we begin with a Lagrangian:

$$
\begin{align*}
& -\mathcal{L}=\bar{E}_{R} Y_{E} L_{L} H_{d}+\bar{\nu}_{R} Y_{\nu} L_{L}+\frac{1}{2} \nu_{R}^{\top} M_{R} \nu_{R}  \tag{1}\\
\frac{d}{d \log Q}\left(m_{\tilde{L}}^{2}\right)_{i j}= & \left(\frac{d}{d \log Q}\left(m_{\tilde{L}}^{2}\right)_{i j}\right)  \tag{2}\\
& \left.+\frac{1}{16 \pi^{2}}\left[n_{\tilde{L}}^{2} Y_{\nu}^{\dagger} Y_{\nu}\right) Y_{\nu}^{\dagger} Y_{\nu} m_{\tilde{L}}^{2}+2\left(Y_{\nu}^{\dagger} m_{\tilde{\nu}_{R}}^{2} Y_{\nu}+m_{H_{u}}^{2} Y_{\nu}^{\dagger} Y_{\nu}+A_{\nu}^{\dagger} A_{\nu}\right)\right]_{i j} \\
& \left(\Delta m_{\tilde{L}}^{2}\right)_{i j} \simeq-\frac{\log \left(M / M_{R}\right)}{16 \pi^{2}}\left(6 m_{0}^{2}\left(Y_{\nu}^{\dagger} Y_{\nu}\right)_{i j}+2\left(A_{\nu}^{\dagger} A_{\nu}\right)_{i j}\right) \tag{3}
\end{align*}
$$

where $m_{0}$ is a common scalar mass evaluated at the scale $Q=M$, and $i \neq j$. If we further assume that the $A$-terms are proportional to Yukawa matrices, then:

$$
\begin{equation*}
\left(\Delta m_{\tilde{L}}^{2}\right)_{i j} \simeq \xi\left(Y_{\nu}^{\dagger} Y_{\nu}\right)_{i j} \tag{4}
\end{equation*}
$$

K.S. Babu, C. Kolda, Phys. Rev. Lett. 89,24I802 (2002).
2. Effective Lagrangians and branching ratios for LFV processes. We now present the calculational details we use in arriving at the approximate results of the previous Section and the numerical results to be presented in the next Section. We consider the $R$-parity conserving superpotential:

$$
W=\begin{align*}
& U_{i}^{c}\left(Y_{u}\right)_{i j} Q_{j} H_{2}-D_{i}^{c}\left(Y_{d}\right)_{i j} Q_{j} H_{1}+  \tag{8}\\
& N_{i}^{c}\left(Y_{\nu}\right)_{i j} L_{j} H_{2}-E_{i}^{c}\left(Y_{e}\right)_{i j} L_{j} H_{1}+\frac{1}{2} N^{c}{ }_{i}\left(M_{N}\right)_{i j} N_{j}^{c}+\mu H_{2} H_{1},
\end{align*}
$$

where the indices $i, j$ run over three generations and $M_{N}$ is the heavy singlet-neutrino mass matrix. We work in a basis where $\left(Y_{d}\right)_{i j},\left(Y_{e}\right)_{i j}$ and $\left(M_{N}\right)_{i j}$ are real and diagonal. At the one-loop level, this leads to the effective Lagrangian [3, 5, 8, 14].

$$
\begin{align*}
-\mathcal{L}^{e f f}= & \bar{d}_{R}^{i} Y_{d i}\left[\delta_{i j} H_{1}^{0}+\left(\epsilon_{0} \delta_{i j}+\epsilon_{Y}\left(Y_{u}^{\dagger} Y_{u}\right)_{i j}\right) H_{2}^{0 *}\right] d_{L}^{j}+h . c .+ \\
& \bar{l}_{R}^{i} Y_{e i}\left[\delta_{i j} H_{1}^{0}+\left(\epsilon_{1} \delta_{i j}+\epsilon_{2} E_{i j}\right) H_{2}^{0 *}\right] l_{L}^{j}+h . c ., \tag{9}
\end{align*}
$$

A. Dedes, J.R. Ellis, M. Raidal, Phys. Lett. B549, I59 (2002)

## Yukawa sector in 2HDM type III

$$
\begin{aligned}
& \mathcal{L}_{Y}=Y_{1}^{u} \bar{Q}_{L} \Phi_{1} u_{R}+Y_{2}^{u} \bar{Q}_{L} \Phi_{2} u_{R}+Y_{1}^{d} \bar{Q}_{L} \Phi_{1} d_{R}+Y_{2}^{d} \bar{Q}_{L} \Phi_{2} d_{R} \\
& Y_{1}^{u}=Y_{1}^{d}=0 \text { or } Y_{2}^{u}=Y_{2}^{d}=0 \longrightarrow 2 \text { HDM-I } \\
& Y_{1}^{u}=Y_{2}^{d}=0 \text { or } Y_{2}^{u}=Y_{1}^{d}=0 \longrightarrow 2 H D M-I I(M S S M)
\end{aligned}
$$

Yukawa sector of the 2HDM-III is similar to effective lagrangian of the MSSM with a seesaw mechanism.

This lagrangian contains loop effects of sfermions and gauginos.
2HDM type III could be a generic description of physics at higher scale (of order TeV o maybe higher)

## Yukawa textures

The structure of quarks mass matrices (quark flavor mixing) is unknown.

A theory more fundamental than SM could determine: 6 quark masses, 3 flavor mixing angles, one CP-violating phase.

Phenomenologically, it has introduced a common approach: simple textures of quarks mass matrices (called Yukawa textures).

The Yukawa textures are consistents with the relations between quarks masses and flavor mixing parameters.

Yukawa textures could come of a theory more fundamental and it could be a flavor symmetry.
H. Fritzsch, Z. Z. Xing, Prog.Part. Nucl. Phys. 45 (2000) I .
H. Fritzsch, Z. Z. Xing, Phys. Lett. 555 (2003)63.

## 2HDM-III + Yukawa texture

 contain the following information:It could come from a more fundamental theory (susy models with seesaw mechanism).

$$
+
$$

Yukawa texture is the flavor symmetry of the model and do not require of the discrete flavor symmetry.

$$
+
$$

The Higgs potential must be expressed in the most general form.

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    T. P. Cheng, M. Sher, Phys. Rev. D33, II (1987)
J.L. Diaz-Cruz, R Noriega-Papaqui,A. Rosado. Phys. Rev. D69,095002 (2004)
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## Yukawa texture chosen

After SSB (Spontaneous Symmetry Breaking), one can derive the fermion mass matrices from eq. (1), namely

$$
\begin{equation*}
M_{f}=\frac{1}{\sqrt{2}}\left(v_{1} Y_{1}^{f}+v_{2} Y_{2}^{f}\right), \quad f=u, d, l, \tag{2}
\end{equation*}
$$

We will assume that both Yukawa matrices $Y_{1}^{f}$ and $Y_{2}^{f}$ have the four-texture form and Hermitic [22, 26]. Following this convention, the fermions masses matrices have the same form, which are written as:

$$
M_{f}=\left(\begin{array}{ccc}
0 & C_{f} & 0  \tag{3}\\
C_{f}^{*} & \tilde{B}_{f} & B_{f} \\
0 & B_{f}^{*} & A_{f}
\end{array}\right) .
$$

when $\tilde{B}_{q} \rightarrow 0$ one recovers the six-texture form. We also consider the hierarchy: $\left|A_{q}\right| \gg\left|\tilde{B}_{q}\right|,\left|B_{q}\right|,\left|C_{q}\right|$, which is supported by the observed fermion masses in the SM.

The mass matrix is diagonalized through the bi-unitary matrices $V_{L, R}$, though each Yukawa matrices are not diagonalized by this transformation. The diagonalization is performed in the following way

$$
\begin{equation*}
\bar{M}_{f}=V_{f L}^{\dagger} M_{f} V_{f R} \tag{4}
\end{equation*}
$$

$$
\begin{equation*}
\bar{M}_{f}=\frac{1}{\sqrt{2}}\left(v_{1} \tilde{Y}_{1}^{f}+v_{2} \tilde{Y}_{2}^{f}\right) \tag{6}
\end{equation*}
$$

where $\tilde{Y}_{i}^{f}=V_{f L}^{\dagger} Y_{i}^{f} V_{f R}$. In order to compare the new physics comes from Yukara texture with some traditional $2 H D M$ (in particular with $2 H D M-I I)$, in previous works $[22,23,28-30$, we have implemented the following redefinition ((a) like-2HDM-II):

$$
\begin{align*}
& \tilde{Y}_{1}^{d}=\frac{\sqrt{2}}{v \cos \beta} \bar{M}_{d}-\tan \beta \tilde{Y}_{2}^{d} \\
& \tilde{Y}_{2}^{u}=\frac{\sqrt{2}}{v \sin \beta} \bar{M}_{u}-\cot \beta \tilde{Y}_{1}^{u} \\
& \tilde{Y}_{1}^{\ell}=\tilde{Y}_{1}^{d}(d \rightarrow \ell) \tag{7}
\end{align*}
$$

(b) like-2HDM-I

$$
\begin{aligned}
\tilde{Y}_{2}^{d} & =\frac{\sqrt{2}}{v \sin \beta} \bar{M}_{d}-\cot \beta \tilde{Y}_{1}^{d} \\
\tilde{Y}_{2}^{u} & =\frac{\sqrt{2}}{v \sin \beta} \bar{M}_{u}-\cot \beta \tilde{Y}_{1}^{u} \\
\tilde{Y}_{2}^{\ell} & =\tilde{Y}_{2}^{d}(d \rightarrow \ell)
\end{aligned}
$$

(c) like-2HDM-X

$$
\begin{aligned}
\tilde{Y}_{2}^{d} & =\frac{\sqrt{2}}{v \sin \beta} \bar{M}_{d}-\cot \beta \tilde{Y}_{1}^{d} \\
\tilde{Y}_{2}^{u} & =\frac{\sqrt{2}}{v \sin \beta} \bar{M}_{u}-\cot \beta \tilde{Y}_{1}^{u} \\
\tilde{Y}_{1}^{\ell} & =\tilde{Y}_{1}^{d}(d \rightarrow \ell)
\end{aligned}
$$

(d) like-2HDM-Y

$$
\begin{aligned}
\tilde{Y}_{1}^{d} & =\frac{\sqrt{2}}{v \cos \beta} \bar{M}_{d}-\tan \beta \tilde{Y}_{2}^{d} \\
\tilde{Y}_{2}^{u} & =\frac{\sqrt{2}}{v \sin \beta} \bar{M}_{u}-\cot \beta \tilde{Y}_{1}^{u} \\
\tilde{Y}_{2}^{\ell} & =\tilde{Y}_{2}^{d}(d \rightarrow \ell)
\end{aligned}
$$

Then the rotated form $\tilde{Y}_{2}^{l}$ has the general form,

$$
\begin{aligned}
\tilde{Y}_{2}^{l} & =O^{T} P Y_{2}^{l} P^{\dagger} O \\
& =\left(\begin{array}{ccc}
\tilde{Y}_{211}^{l} & \tilde{Y}_{212}^{l} & \tilde{Y}_{213}^{l} \\
\tilde{Y}_{221}^{l} & \tilde{Y}_{222}^{l} & \tilde{Y}_{223}^{l} \\
\tilde{Y}_{231}^{l} & \tilde{Y}_{232}^{l} & \tilde{Y}_{233}^{l}
\end{array}\right) .
\end{aligned}
$$

$$
\begin{aligned}
\left(\tilde{Y}_{2}\right)_{22}^{l}= & \eta\left[C_{2}^{*} e^{i \Phi_{C}}+C_{2} e^{-i \Phi_{C}}\right] \frac{\left(A-\lambda_{2}\right)}{m_{3}-\lambda_{2}} \sqrt{\frac{m_{1} m_{3}}{A m_{2}}}+\tilde{B}_{2} \frac{A-\lambda_{2}}{m_{3}-\lambda_{2}} \\
& +A_{2} \frac{A-\lambda_{2}}{m_{3}-\lambda_{2}}-\left[B_{2}^{*} e^{i \Phi_{B}}+B_{2} e^{-i \Phi_{B}}\right] \sqrt{\frac{\left(A-\lambda_{2}\right)\left(m_{3}-A\right)}{m_{3}-\lambda_{2}}}
\end{aligned}
$$

$$
\begin{aligned}
\left(\tilde{Y}_{2}^{l}\right)_{11} & =\left(\tilde{b}_{2}-2 c_{2}\right) m_{1} / v \\
\left(\tilde{Y}_{2}^{l}\right)_{12} & =\left(c_{2}-\tilde{b}_{2}\right) \sqrt{m_{1} m_{2}} / v \\
\left(\tilde{Y}_{2}^{l}\right)_{13} & =\left(a_{2}-b_{2}\right) \sqrt{m_{1} m_{2}} / v \\
\left(\tilde{Y}_{2}^{l}\right)_{22} & =\tilde{b}_{2} m_{2} / v \\
\left(\tilde{Y}_{2}^{l}\right)_{23} & =\left(b_{2}-a_{2}\right) m_{2} / v \\
\left(\tilde{Y}_{2}^{l}\right)_{33} & =a_{2} m_{3} / v
\end{aligned}
$$

Then we introduce the matrix $\tilde{\chi}$ as follows:

$$
\begin{aligned}
\left(\widetilde{Y}_{2}^{l}\right)_{i j} & =\frac{\sqrt{m_{i} m_{j}}}{v} \widetilde{\chi}_{i j} \\
& =\frac{\sqrt{m_{i} m_{j}}}{v} \chi_{i j} e^{\vartheta_{i j}}
\end{aligned}
$$

which differs from the usual Cheng-Sher ansatz not only because of the appearance of the complex phases, but also in the form of the real parts $\chi_{i j}=\left|\tilde{\chi}_{i j}\right|$.

$$
\begin{aligned}
\tilde{\chi}_{11}= & {\left[\widetilde{b}_{2}-\left(c_{2}^{*} e^{\left.\left.i \Phi_{C}+c_{2} e^{-i \Phi_{C}}\right)\right] \eta} \begin{array}{rl} 
& +\left[a_{2}+\widetilde{b}_{2}-\left(b_{2}^{*} e^{\left.\left.i \Phi_{B}+b_{2} e^{-i \Phi_{B}}\right)\right] \beta,}\right.\right. \\
\tilde{\chi}_{12}= & \left(c_{2} e^{\left.-i \Phi_{C}-\widetilde{b}_{2}\right)}\right. \\
& -\eta\left[a_{2}+\widetilde{b}_{2}-\left(b_{2}^{*} e^{\left.\left.i \Phi_{B}+b_{2} e^{-i \Phi_{B}}\right)\right] \beta,}\right.\right. \\
\tilde{\chi}_{13}= & \left(a_{2}-b_{2} e^{-i \Phi_{B}}\right) \eta \sqrt{\beta}, \\
\tilde{\chi}_{22}= & \widetilde{b}_{2} \eta+\left[a_{2}+\widetilde{b}_{2}-\left(b_{2}^{*} e^{\left.\left.i \Phi_{B}+b_{2} e^{-i \Phi_{B}}\right)\right] \beta,}\right.\right. \\
\tilde{\chi}_{23}= & \left(b_{2} e^{\left.-i \Phi_{B}-a_{2}\right) \sqrt{\beta},}\right. \\
\tilde{\chi}_{33}= & a_{2} .
\end{array} .\right.\right.}
\end{aligned}
$$

Recently we are doing a $\mathrm{X}^{\wedge} 2$-fit with CKM and we have found $\mathrm{Xij} \mathrm{O}(1)$.
F.F. González-Canales, O. Félix-Beltrán, J. Hernández-Sánchez, S. Moretti, R. Noriega, A. Rosado, work in progress.

## Another form to get the versions of 2HDM

- Partial Aligment 2HDM:
- J. Hernández-Sánchez, L. López-Lozano, R. Noriega-Papaqui. A. Rosado, PRD85, 071301(R) (2012)

$$
\tilde{Y}_{2}^{f}=\frac{1}{v} \tilde{A}_{L}^{f} \bar{M}_{f} \tilde{A}_{R}^{f},
$$

where $\tilde{A}_{L, R}^{f}=U_{L, R}^{f \dagger} A_{L, R}^{f} U_{L, R}^{f}, \bar{M}_{f}=\operatorname{Diag}\left[m_{f 1}, m_{f 2}, m_{f 3}\right]$, and $U_{L, R}^{f}$ are the matrices that diagonalize the mass matrix $M_{f}$. So, the contribution to fermion-fermion-Higgs bosons couplings is given by

$$
\begin{aligned}
\left(\tilde{Y}_{2}^{f}\right)_{i j}= & \frac{1}{v}\left(m_{f 1}\left(\tilde{A}_{L}^{f}\right)_{i 1}\left(\tilde{A}_{R}^{f}\right)_{1 j}+m_{f 2}\left(\tilde{A}_{L}^{f}\right)_{i 2}\left(\tilde{A}_{R}^{f}\right)_{2 j}\right. \\
& \left.+m_{f 3}\left(\tilde{A}_{L}^{f}\right)_{i 3}\left(\tilde{A}_{R}^{f}\right)_{3 j}\right) . \leq \sqrt{m_{f i} m_{f j}}\left|\tilde{\chi}_{i j}^{f}\right|
\end{aligned}
$$

TABLE I. Matrices that reproduce several versions of the Yukawa interactions for the 2 HDM in terms of $S U_{F}(3)$ generators. The $C^{\prime} s$ parameters are complex coefficients and they are proportional to the parameters $\tilde{\chi}_{i j}^{f}$ defined in Eq. (6).

|  | $A_{L}^{u}$ | $A_{R}^{u}$ | $A_{L}^{d}$ | $A_{R}^{d}$ |
| :--- | :---: | :---: | :---: | :---: |
| I | $\sqrt{\frac{3 m_{W}}{v}} \lambda_{0}$ | $\sqrt{\frac{3 m_{W}}{v}} \lambda_{0}$ | $\sqrt{\frac{3 m_{W}}{v}} \lambda_{0}$ | $\sqrt{\frac{3 m_{W}}{v}} \lambda_{0}$ |
| II | $\sqrt{\frac{3 m_{W}}{v}} \lambda_{0}$ | $\sqrt{\frac{3 m_{W}}{v}} \lambda_{0}$ | $0_{3 \times 3}$ | $0_{3 \times 3}$ |
| III-IV | $\sum_{a=0,3,8} C_{a}^{u} \lambda_{a}$ | $\left(\sum_{a=0,3,8} \tilde{C}_{a}^{u} \lambda_{a}\right)^{\dagger}$ | $\sum_{a=0,3,8} C_{a}^{d} \lambda_{a}$ | $\left(\sum_{a=0,3,8} \tilde{C}_{a}^{d} \lambda_{a}\right)^{\dagger}$ |
| A2HDM | $C_{0}^{u} \lambda_{0}$ | $\tilde{C}_{0}^{u_{0}^{* *}} \lambda_{0}$ | $C_{0}^{d} \lambda_{0}$ | $\tilde{C}_{0}^{d *} \lambda_{0}$ |

$$
\mathcal{L}^{\bar{f}_{i} f_{j} H^{+}}=-\left\{\frac{\sqrt{2}}{v} \bar{u}_{i}\left(m_{d_{j}} X_{i j} P_{R}+m_{u_{i}} Y_{i j} P_{L}\right) d_{j} H^{+}+\frac{\sqrt{2} m_{\ell_{j}}}{v} Z_{i j} \overline{\nu_{L}} \ell_{R} H^{+}+H . c .\right\}
$$

$$
\begin{aligned}
X_{i j} & =\sum_{l=1}^{3}\left(V_{\mathrm{CKM}}\right)_{i l}\left[X \frac{m_{d_{l}}}{m_{d_{j}}} \delta_{l j}-\frac{f(X)}{\sqrt{2}} \sqrt{\frac{m_{d_{l}}}{m_{d_{j}}}} \tilde{\chi}_{l j}^{d}\right], \begin{array}{r}
\text { Non-diagonal model (See } \\
\text { the talk of Jie Lu) }
\end{array} \\
Y_{i j} & =\sum_{l=1}^{3}\left[Y \delta_{i l}-\frac{f(Y)}{\sqrt{2}} \sqrt{\frac{m_{u_{l}}}{m_{u_{i}}}} \tilde{\chi}_{i l}^{u}\right]\left(V_{\mathrm{CKM}}\right)_{l j} . \\
Z_{i j}^{\ell} & =\left[Z \frac{m_{\ell_{i}}}{m_{\ell_{j}}} \delta_{i j}-\frac{f(Z)}{\sqrt{2}} \sqrt{\frac{m_{\ell_{i}}}{m_{\ell_{j}}}} \tilde{\chi}_{i j}^{\ell}\right], \quad \begin{array}{|c||c|c|c|}
\hline \text { like-2HDM-III } & X & Y & Z \\
\text { like-2HDM-II } & -\cot \beta & \cot \beta & -\cot \beta \\
\tan \beta & \cot \beta & \tan \beta \\
\text { like-2HDM-X } & -\cot \beta & \cot \beta & \tan \beta \\
\text { like-2HDM-Y } & \tan \beta & \cot \beta & -\cot \beta
\end{array}
\end{aligned}
$$

$$
\left(g_{2 H D M-I I I}^{f_{u} i f_{d} j H^{+}}=g_{2 H D M-a n y}^{f_{u} i f_{d} j H^{+}}+\Delta g^{f_{u} i f_{d j} j H^{+}}\right)
$$

A. Akeroyd, J. Hernandez-Sanchez, S. Moretti, R. Noriega- Papaqui, A. Rosado, work in progress

## For light charged Higgs

$$
\Gamma\left(H^{ \pm} \rightarrow u_{i} d_{j}\right)=\frac{3 G_{F} m_{H^{ \pm}}\left(m_{d_{j}}^{2}\left|X_{i j}\right|^{2}+m_{u_{i}}^{2}\left|Y_{i j}\right|^{2}\right)}{4 \pi \sqrt{2}}
$$

the case $Y \gg, X, Z$ the channel decay $H^{+} \rightarrow \bar{\square}$

$$
m_{c} Y_{c b}=m_{c} Y_{23}=V_{c b} m_{c}\left(Y-\frac{f(Y)}{\sqrt{2}} \chi_{22}^{u}\right)-V_{t b} \frac{f(Y)}{\sqrt{2}} \sqrt{m_{t} m_{c}} \chi_{23}^{u}
$$

$$
\left(H^{ \pm} \rightarrow c s\right)
$$

$$
m_{c} Y_{c s}=m_{c} Y_{22}=V_{c s} m_{c}\left(Y-\frac{f(Y)}{\sqrt{2}} \chi_{22}^{u}\right)-V_{t s} \frac{f(Y)}{\sqrt{2}} \sqrt{m_{t} m_{c}} \chi_{23}^{u}
$$

$$
\frac{\operatorname{BR}\left(H^{ \pm} \rightarrow c b\right)}{\operatorname{BR}\left(H^{ \pm} \rightarrow c s\right)}=R_{s b} \sim \frac{\left|V_{t b}\right|^{2}}{\left|V_{t s}\right|^{2}}
$$

## For light charged Higgs

Other case is when $X \gg, Y, Z$, we get the dominants terms $m_{b} X_{23}, m_{s} X_{22}$ :

$$
\begin{gathered}
m_{b} X_{c b}=m_{b} X_{23}=V_{c b} m_{b}\left(X-\frac{f(X)}{\sqrt{2}} \chi_{33}^{d}\right)-V_{c s} \frac{f(X)}{\sqrt{2}} \sqrt{m_{b} m_{s}} \chi_{23}^{d} \\
m_{s} X_{c s}=m_{s} X_{22}=V_{c s} m_{s}\left(X-\frac{f(X)}{\sqrt{2}} \chi_{22}^{d}\right)-V_{t s} \frac{f(X)}{\sqrt{2}} \sqrt{m_{b} m_{s}} \chi_{23}^{d} \\
\text { If } \chi=O(1) \text { and positive then }\left(X-\frac{f(X)}{\sqrt{2}} \chi_{33}^{d}\right) \text { is small and } R_{s b} \sim \frac{\mid V_{c s}{ }^{2}}{\left|{ }_{c c t}\right|^{2}}
\end{gathered}
$$

Other situation is when, $\chi=O(1)$ and negative, then $R_{s b} \sim \frac{m_{b}^{2}\left|V_{c b}\right|^{2}}{m_{s}^{2}\left|V_{c b}\right|^{2}}$.
A.G. Akeroyd, S. Moretti and J. Hernández-Sánchez, PRD85:115002 (2012)


FIG. 1: $B R\left(H^{ \pm} \rightarrow c b\right)$ and $B R\left(H^{ \pm} \rightarrow c s\right), Z=0.1, X \gg Y, \leq m H^{+} \leq 120 \mathrm{GeV}$ and $\chi=0.1$

## Others phenomenological consequences

- If we combine:
- The effects of texture in the coupling.
- The general Higgs potential.

It's possible to enhacement processes at one-loop-level, e.g.

- $\mathrm{H}, \mathrm{h} \rightarrow \mathrm{\gamma} \mathrm{\gamma}$
- $\mathrm{H}^{\wedge}+\rightarrow \mathrm{W}^{\wedge}+\mathrm{p}, \mathrm{W}^{\wedge}+\mathrm{Z}$
J. Hernández-Sánchez, C. G. Honoratp, M.A. Pérez, J.J. Toscano, PRD85:015020 (2012).
J.E. Barradas, F. Cazares-Bush, A. Cordero-Cid, O. Félix-Beltrán, J. Hernández-Sanchez, R. Noriega-Papaqui, J.Phys. G37 (2010) 115008


## Some constraints of processes to below energy

$\mu-e$ universality in $\tau$ decays

$$
\frac{B R\left(\tau \rightarrow \mu \bar{\nu}_{\mu} \nu_{\tau}\right)}{B R\left(\tau \rightarrow e \bar{\nu}_{e} \nu_{\tau}\right)} \frac{f\left(m_{e}^{2} / m_{\tau}^{2}\right)}{f\left(m_{\mu}^{2} / m_{\tau}^{2}\right.} \simeq 1+\frac{R^{2}}{4}-0.25 R .
$$

$R=\frac{m_{\tau} m_{\mu}}{M_{H^{+}}^{2}} Z_{33} Z_{22}=\frac{m_{\tau} m_{\mu}}{M_{H^{+}}^{2}}\left[Z-\frac{f(Z)}{\sqrt{2}} \chi_{33}^{l}\right]\left[Z-\frac{f(Z)}{\sqrt{2}} \chi_{22}^{l}\right]$.

$$
\frac{\left|Z_{22} Z_{33}\right|}{m_{H^{ \pm}}^{2}} \leq 0.16 \mathrm{GeV}^{-1}
$$

We use the analysis of Pich and Tuzon, JHEP11(2010)003


FIG. 2: Allowed region for $\chi_{22}^{\ell}$ and $\chi_{33}^{\ell}$ from $\mu-e$ universality in $\tau$ dēcays, $Z$ takes values of 0.5 to 80 , and $100 \mathrm{GeV} \leq m H^{+} \leq 150$ GeV

We consider $D \rightarrow \mu \nu, B \rightarrow \tau \nu, D_{s} \rightarrow \mu \nu, \tau \nu$

$$
\frac{B(M \rightarrow \ell \nu)}{B(M \rightarrow \ell \nu)_{S M}}=\left|1-\Delta_{i j}\right|^{2} \quad \Delta_{i j}=\left(\frac{m_{M}}{m_{H^{ \pm}}}\right)^{2} Z\left(\frac{Y_{i j} m_{u_{i}}+X_{i j} m_{d_{j}}}{m_{u_{i}}+m_{d_{j}}}\right)
$$


from $R_{D \rightarrow \mu \nu}, Z$ takes values of 0.5 to 80 and $Z \gg Y$,

We use the analysis of Pich and Tuzon, JHEP11(2010)003

from $R_{B \rightarrow \tau \nu}, Z$ takes values of 0.5 to 80 and $Z, X \gg Y$,


FIG. 1. The figure shows $X_{33}, Y_{33}, X_{23}$, and $Y_{23}$ vs $\tan \beta$, taking $\tilde{\chi}_{3,3}^{\mu, d}=1$ (solid line), $\tilde{\chi}_{3,3}^{\mu, d}=0.1$ (dashed line), $\tilde{\chi}_{3,3}^{u, d}=-0.1$ (dotted line), and $\tilde{\chi}_{3,3}^{n, d}=-1$ (dashed-dotted line).

Based on the analysis of $B \rightarrow X_{s} \gamma[36,37]$, it is claimed that $X \leq 20$ and $Y \leq 1.7$

## Phenomenology of $\mathrm{H}+$



Figure 1. Feynman diagrams contributing to the $H^{+} \rightarrow W^{+} \gamma$ decay in the nonlinear $R_{\xi}$-gauge. $\phi^{0}$ stands for $h^{0}$ and $H^{0}$, and $X^{+}$for $H^{+}$and $G_{W}^{+}$.

## Scenario with $\chi=1$, but $\alpha=\pi / 2+\beta$






## C. s-channel production of charged Higgs boson

Large flavor mixing coupling $H^{ \pm} \bar{q} q^{\prime}$ enables the possibility of studying the production of charged Higgs boson via the partonic $s$-channel production mechanism, $\bar{c} \bar{b}, \bar{c} b \rightarrow H^{ \pm}$. This mechanism was discussed first by He and Yuan

$$
\sigma\left(h_{1} h_{2}(\bar{c} \bar{b}) \rightarrow H^{+} X\right) \frac{\pi}{12 s}\left(\left|C_{L}\right|^{2}+\left|C_{R}\right|^{2}\right) I_{c, \bar{b}}^{h_{1}, h_{2}}
$$

where

$$
I_{c, \bar{b}}^{h_{1}, h_{2}}=\int_{\tau}^{1} d x\left[f_{c}^{h_{1}}\left(x, \tilde{Q}^{2}\right) f_{\bar{b}}^{h_{2}}\left(\tau / x, \tilde{Q}^{2}\right)+f_{\bar{b}}^{h_{1}}\left(x, \tilde{Q}^{2}\right) f_{c}^{h_{2}}\left(\tau / x, \tilde{Q}^{2}\right)\right] / x
$$

and $\tau=m_{H^{ \pm}}^{2} / s$. The parton distribution functions (PDFs) $f_{q}^{h_{i}}\left(x, \tilde{Q}^{2}\right)$ describe the quark $q$ content of the hadron $i$ at a scale interaction of $\tilde{Q}^{2}$. In other words, the PDFs $f_{q}^{h}\left(x, \tilde{Q}^{2}\right)$ give the probabilities to find a quark $q$ inside a hadron with the fraction $x$ of the hadron momentum, in a scattering process with momentum transfer square $\tilde{Q}^{2}$, in this case we will take $\tilde{Q}^{2}=m_{H^{+}}^{2}$
H. J. He and C.P. Yuan, Phys. Rev. Lett. 83, 28 (1999)

TABLE II: Summary of LHC event rates for some parameter combinations within Scenarios A, B, C, D with for an integrated luminosity of $10^{5} \mathrm{pb}^{-1}$, for several different signatures, through the channel $\bar{b} \rightarrow H^{+}+$ c.c.

| $\left(\tilde{\chi}_{i j}^{u}, \chi_{i j}^{d}\right)$ | $\tan \beta$ | $m_{H^{+}}$in GeV | $\mid \sigma\left(p p \rightarrow H^{+}+X\right)$ in pb | Relevant BRs | Nr. Events |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (1,1) | 15 | 400 | $1.14 \times 10^{-1}$ | $\operatorname{BR}\left(H^{+} \rightarrow t \bar{b}\right) \approx 3.2 \times 10^{-1}$ | 3648 |
|  |  |  |  | $\mathrm{BR}\left(H^{+} \rightarrow \tau^{+} \nu_{\tau}^{0}\right) \approx 2.1 \times 10^{-3}$ | 24 |
|  |  |  |  | $\mathrm{BR}\left(H^{+} \rightarrow W^{+} h^{0}\right) \approx 6.3 \times 10^{-1}$ | 7182 |
|  |  |  |  | $\mathrm{BR}\left(H_{2}^{+} \rightarrow W^{+} A^{0}\right) \approx 1.7 \times 10^{-2}$ | 194 |
| (1,1) | 70 | 400 | $1.25 \times 10^{-1}$ | $\operatorname{BR}\left(H^{+} \rightarrow t \bar{b}\right) \approx 3.5 \times 10^{-1}$ | 4375 |
|  |  |  |  | $\mathrm{BR}\left(\mathrm{H}^{+} \rightarrow \overline{\text { b }}\right) \approx 1.4 \times 10^{-2}$ | 175 |
|  |  |  |  | $\mathrm{BR}\left(H^{+} \rightarrow \tau^{+} \nu_{\tau}\right) \approx 2.5 \times 10^{-1}$ | 3125 |
|  |  |  |  | $\operatorname{BR}\left(H^{+} \rightarrow W^{+} h^{0}\right) \approx 3.6 \times 10^{-1}$ | 4500 |
| (0.1,1) | 1 | 600 | $3.41 \times 10^{-4}$ | $\mathrm{BR}\left(H^{+} \rightarrow+\overline{\text { b }}\right) \approx 3 \times 10^{-1}$ | 10 |
|  |  |  |  | $\mathrm{BR}\left(H^{+} \rightarrow t \bar{s}\right) \approx 9.1 \times 10^{-4}$ | 0 |
|  |  |  |  | $\operatorname{BR}\left(H^{+} \rightarrow W^{+} h^{0}\right) \approx 3.6 \times 10^{-1}$ | 12 |
|  |  |  |  | $\operatorname{BR}\left(H^{+} \rightarrow W^{+} A^{0}\right) \approx 3.2 \times 10^{-1}$ | 11 |

Table 1. Summary of LHC event rates for some parameter combinations within Scenario B $\left(\tilde{\chi}_{i j}^{u, d}=1\right)$ with an integrated luminosity of $10^{5} \mathrm{pb}^{-1}$, for the signal $H^{+} \rightarrow W^{+} \gamma$, through the channel $\bar{b} \rightarrow H^{+}+$c.c.

| $\alpha$ | $\tan \beta$ | $m_{H^{+}}$in GeV | $\sigma\left(p p \rightarrow H^{+}+X\right)$ in pb | $B R\left(H^{+} \rightarrow W^{+} \gamma\right)$ | $N_{S}$ | $\frac{N_{S}}{\sqrt{N_{B}}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\pi / 2$ | 0.3 | 200 | $2.1 \times 10^{2}$ | $2 \times 10^{-6}$ | 42 | 2.02 |
| $\pi / 2+\beta$ | 0.5 | 300 | $4.5 \times 10$ | $9 \times 10^{-7}$ | 4 | 0.223 |
| $\pi / 2$ | 1 | 200 | 4.5 | $1.4 \times 10^{-4}$ | 63 | 3.03 |
| $\pi / 2+\beta$ | 1 | 300 | 0.89 | $7 \times 10^{-4}$ | 62 | 3.46 |
| $\pi / 2$ | 10 | 200 | 2.5 | $2 \times 10^{-6}$ | 0 | 0 |
| $\pi / 2$ | 10 | 300 | $5.2 \times 10^{-1}$ | $1.5 \times 10^{-7}$ | 0 | 0 |

Table 2. Summary of LHC event rates for some parameter combinations within Scenarios B $\left(\tilde{\chi}_{i j}^{u, d}=1\right)$ with an integrated luminosity of $10^{5} \mathrm{pb}^{-1}$, for $H^{+} \rightarrow W^{+} \gamma$ signature, through the channel $q \bar{q}, g g \rightarrow \bar{t} b H^{+}+$c.c.

| $\alpha$ | $\tan \beta$ | $m_{H^{+}}$in GeV | $\sigma\left(p p \rightarrow H^{+} \bar{t} b\right)$ in pb | $\mathrm{BR}\left(H^{+} \rightarrow W^{+} \gamma\right)$ | $N_{S}$ | $\frac{N_{S}}{\sqrt{N_{B}}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\pi / 2$ | 0.3 | 200 | 25.8 | $2 \times 10^{-6}$ | 5 | 0.62 |
| $\pi / 2+\beta$ | 0.5 | 300 | 5 | $9 \times 10^{-7}$ | 0 | 0 |
| $\pi / 2$ | 1 | 200 | 2.3 | $1.4 \times 10^{-4}$ | 32 | 3.98 |
| $\pi / 2+\beta$ | 1 | 300 | 1.79 | $7 \times 10^{-4}$ | 125 | 18.04 |
| $\pi / 2$ | 10 | 200 | 2.4 | $2 \times 10^{-6}$ | 0 | 0 |
| $\pi / 2$ | 10 | 300 | 0.68 | $1.5 \times 10^{-7}$ | 0 | 0 |

## Conclusions

- 2HDM-III with a four-zero texture in the Yukawa matrices could contain the versions of 2HDM.
- The terms off-diagonal matrices Xij could be $\mathrm{O}(1)$ and cannot omitted, including some important constraints of processes to low energy.
- $\mathrm{H}+\rightarrow$ cb could be relevant.
- $\mathrm{H}+\rightarrow \mathrm{W}+$ gamma could enhance.
- Production $\mathrm{H}+$ could be quite different to the results of the others versions of 2 HDM .

