

# Top Quark Properties



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Physics in Collision 2012

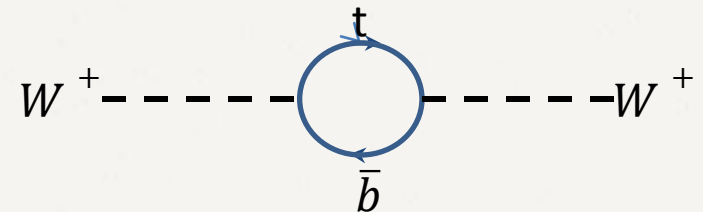
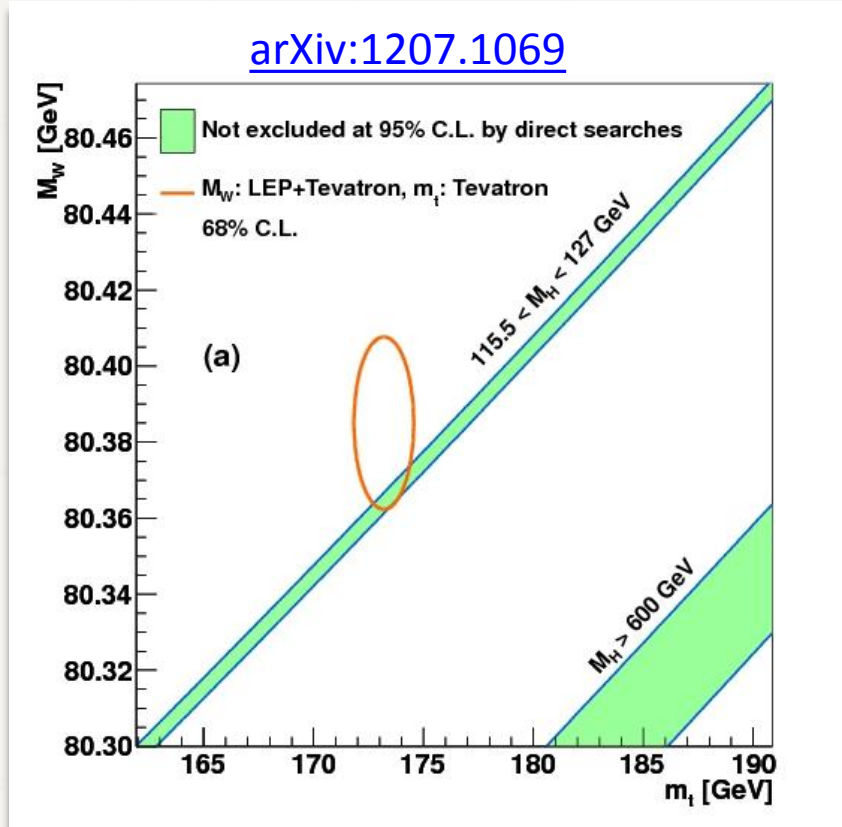
**Štrbské Pleso, Slovakia**

# Outline

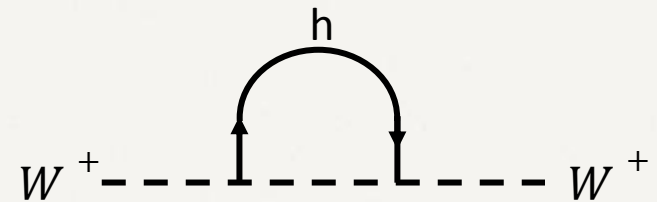
- Top Quark Mass
  - ❖  $M_t$
  - ❖  $M_t - M_{\bar{t}}$  mass *difference*
  
- Top Quark Width
  
- Top Quark Couplings
  - ❖  $t\bar{t}\gamma, t\bar{t}V$  cross section
  - ❖ W Helicity
  - ❖ Flavor-Changing Neutral Currents
  
- Spin Correlation

# The Mass

- The top quark plays an important role in electroweak radiative corrections, which are sensitive to its mass. The top quark mass becomes an important precision probe for physics beyond the SM.

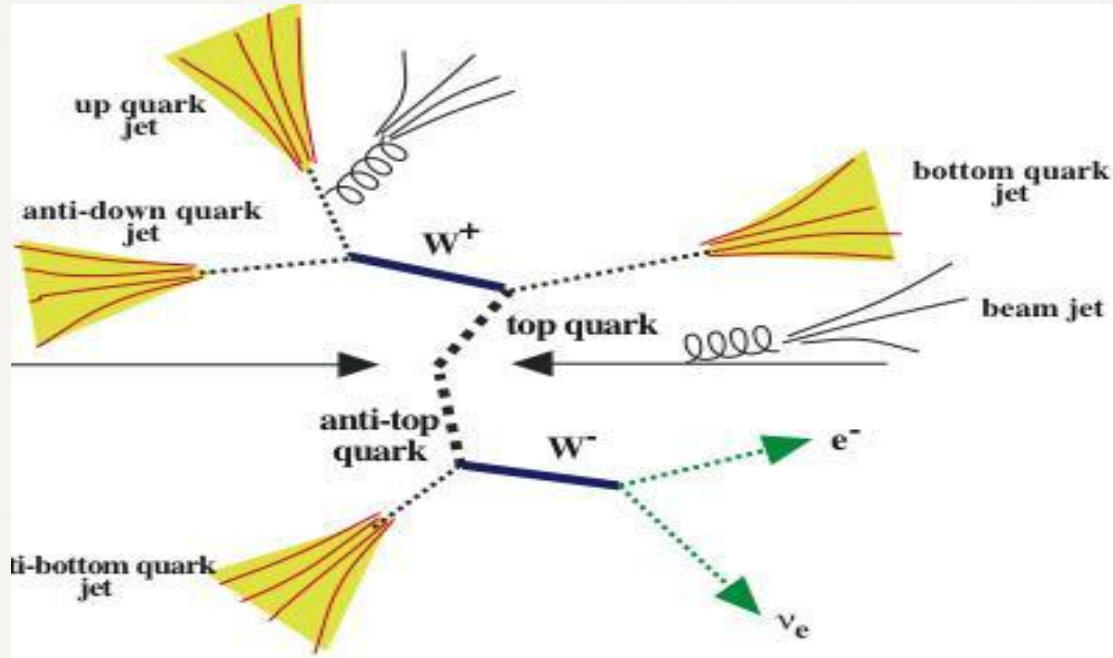


quadratic dependence on  $m_t$



logarithmic dependence on  $m_h$

# Mass Reconstruction



Challenges are to:

- Properly associate measured objects to initial state quarks and leptons (including neutrino(s)).
- Extract best possible four-vector for each (resolution). Jet energy scale (JES) uncertainty is most important.

# $M_t$ in lepton+jets -

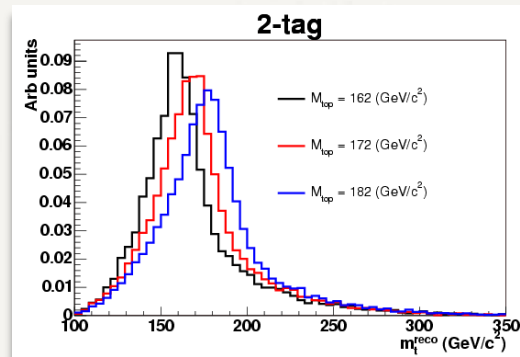


Minimize  $\chi^2$  for jet-parton assignment:

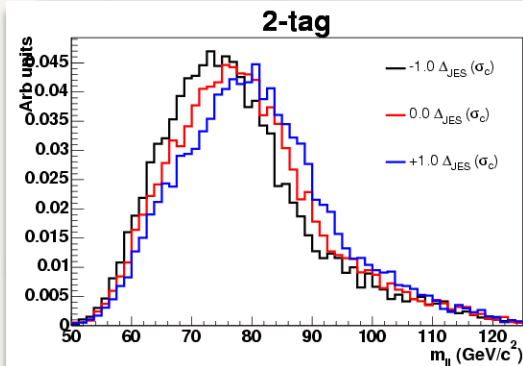
$$\chi^2 = \sum_{i=\ell, 4jets} \frac{(p_T^{i,fit} - p_T^{i,meas})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(U_j^{fit} - U_j^{meas})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{\ell\nu} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - m_t^{reco})^2}{\Gamma_t^2} + \frac{(M_{b\ell\nu} - m_t^{reco})^2}{\Gamma_t^2}$$

Measurement resolution terms

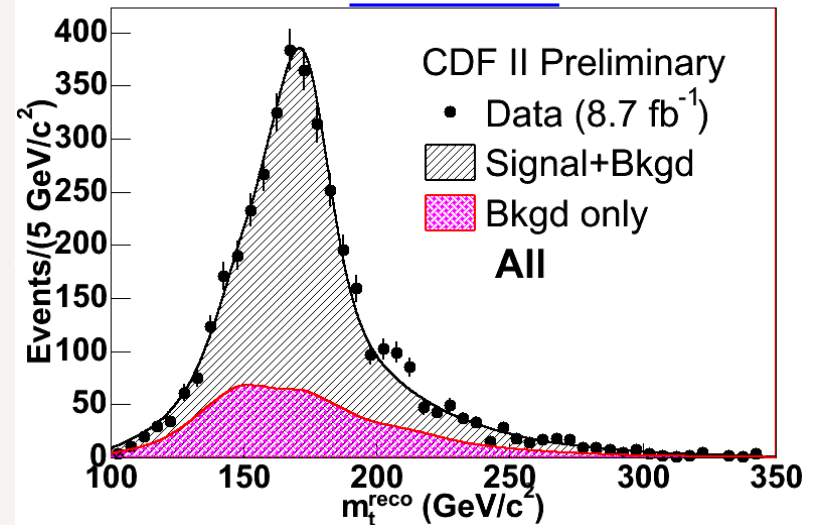
Distribution of  $m_t^{reco}$  fit with MC templates:



Constrain jet E scale with simultaneous fit to  $M_{jj}$ :



CDF 10761



$$M_t = 172.9 \pm 0.7 \text{ (JES+stat)} \pm 0.8 \text{ (syst)} \text{ GeV}$$

# $M_t$ in dileptons –

Under constrained system due to two neutrinos. Needs additional constraints to solve.

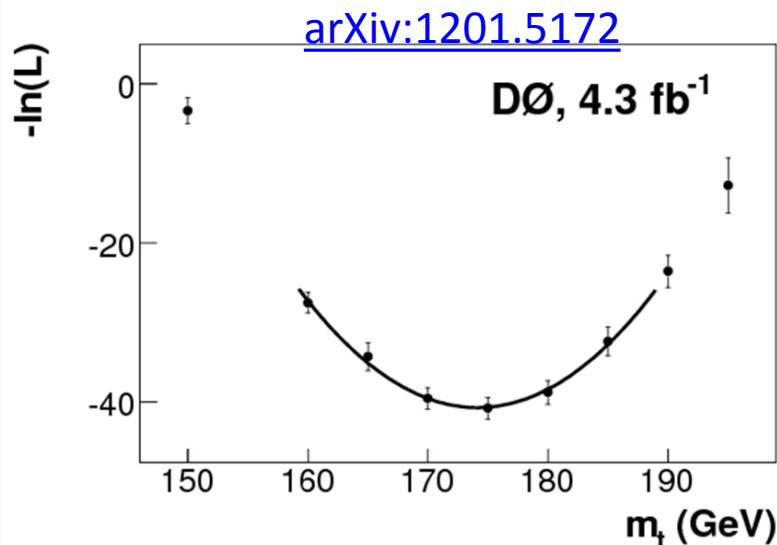
Neutrino weighting

Impose constraints:

$$m(\ell_1\nu_1) = m(\ell_2\nu_2) = m_W$$

$$m(\ell_1\nu_1 b_1) = m(\ell_2\nu_2 b_2)$$

- Integrate of  $\eta$  of both neutrinos
- Calculate neutrino momenta at each  $(\eta_1, \eta_2)$
- Compare measured missing  $E_T$  with missing  $E_T$  calculated from neutrino momenta
- Weight according to likelihood of calculated missing  $E_T \rightarrow$  measured missing  $E_T$

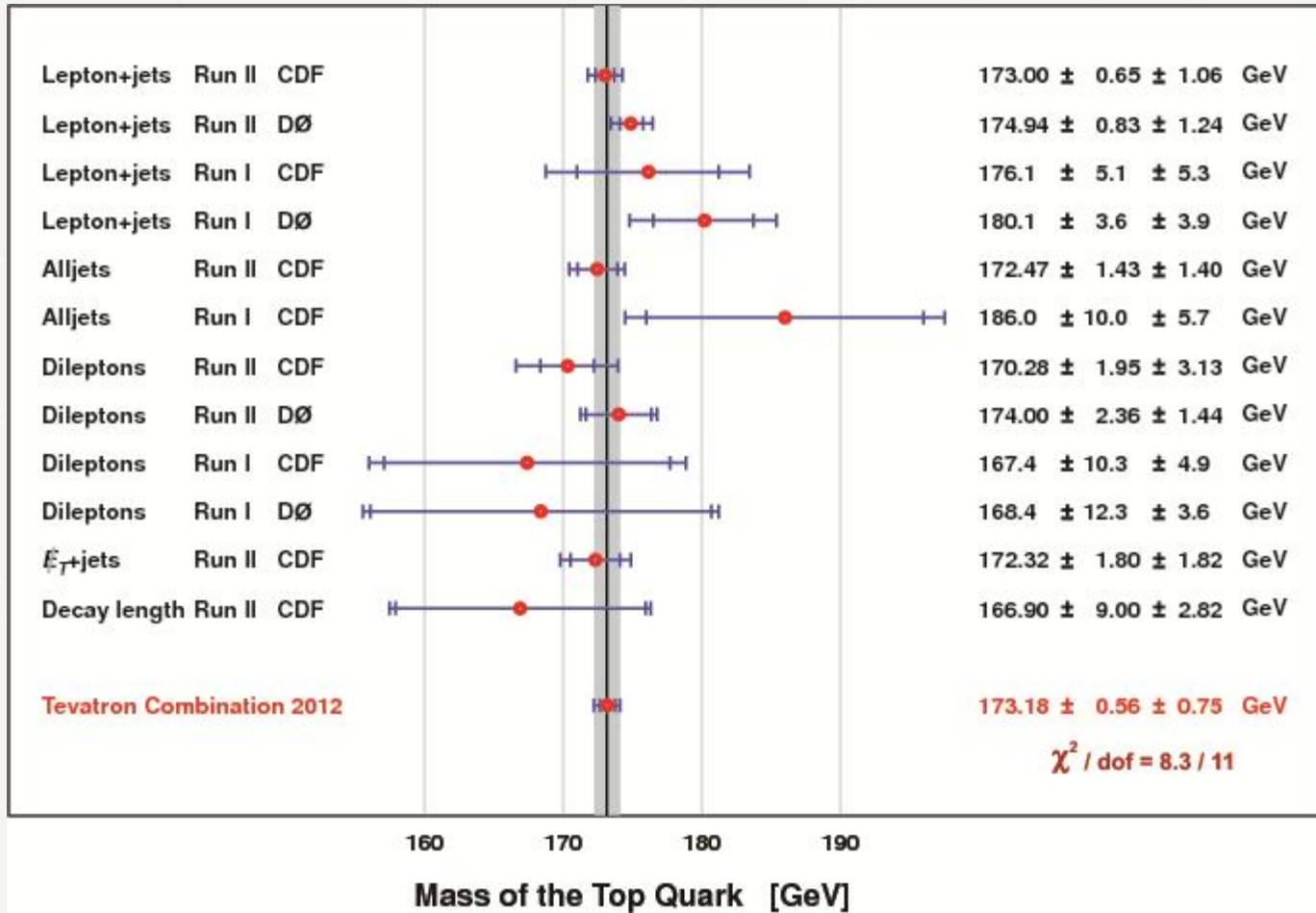
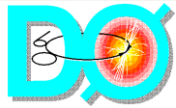


Max likelihood template fit to weight distribution.

$$M_t = 174.0 \pm 2.4 \text{ (stat)} \pm 1.4 \text{ (syst)} \text{ GeV}$$

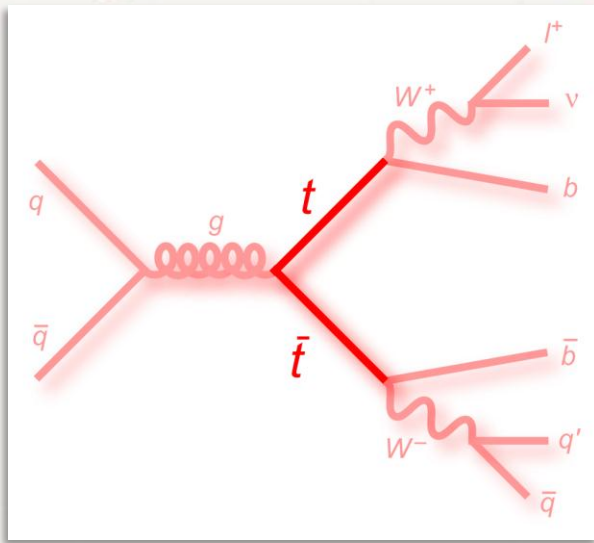
# Tevatron Combination

[arXiv:1207.1069](https://arxiv.org/abs/1207.1069)



$$M_t = 173.18 \pm 0.56 \text{ (stat)} \pm 0.75 \text{ (syst)} \text{ GeV}$$

# Top Mass @ LHC



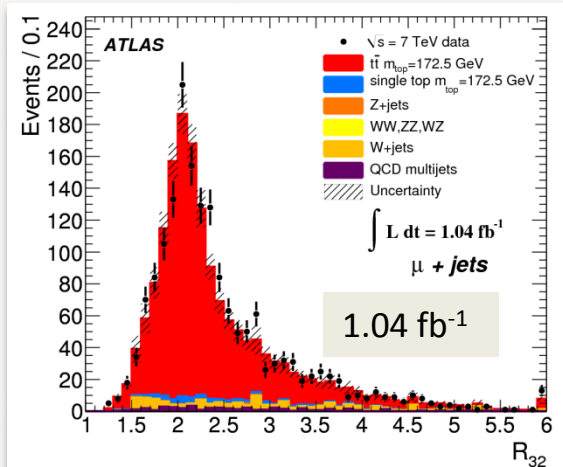
ATLAS 1-D: Measure  
[arXiv:1203.5755](https://arxiv.org/abs/1203.5755)

$$R_{32} = \frac{M(qqb)}{M(qq)}$$

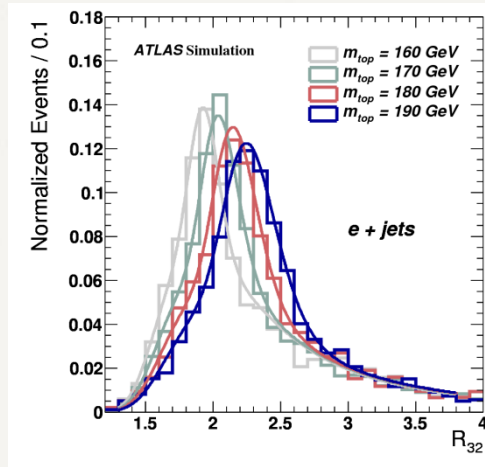
Uses just the hadronic side –  
 constrains JES with  $M(qq) \sim M_W$



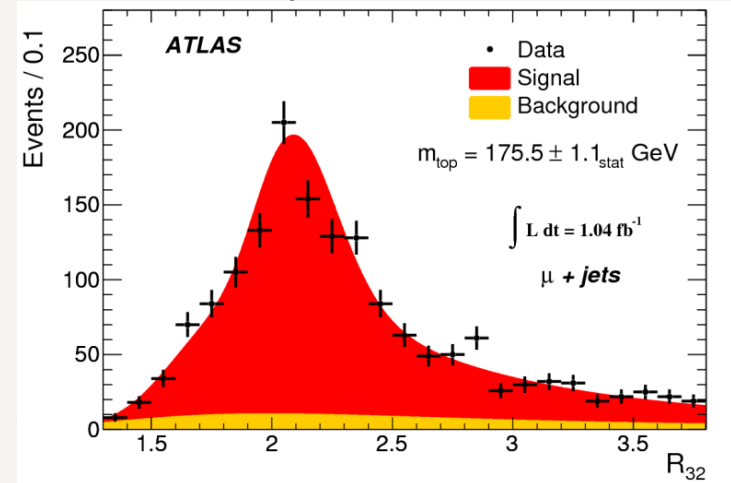
Reconstructed  $R_{32}$



Simulated  $R_{32}$  templates  
 for various  $M_t$



Extract  $M_t$  with template fit



$$m_t = 174.4 \pm 0.9 \pm 2.5 \text{ GeV } (e + \mu)$$



# Top Mass @ LHC - 2

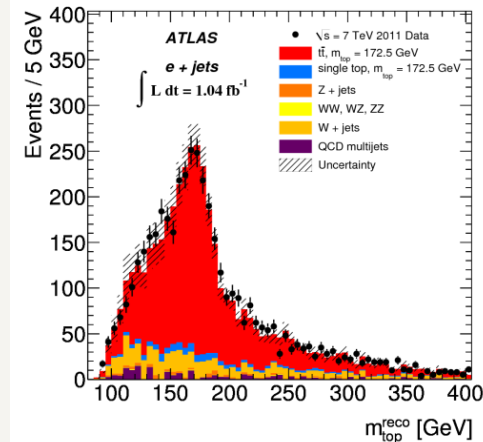
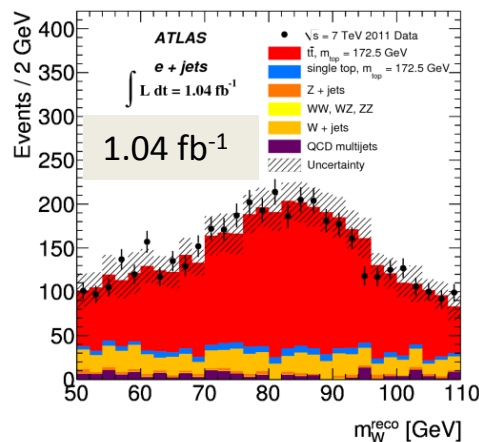
2D method: Measure  $M_{qq}$  and  $M_{qqb}$  simultaneously



ATLAS: Template fit to *best* assignment

$$m_t = 174.5 \pm 0.6 \pm 2.3 \text{ GeV } (e + \mu)$$

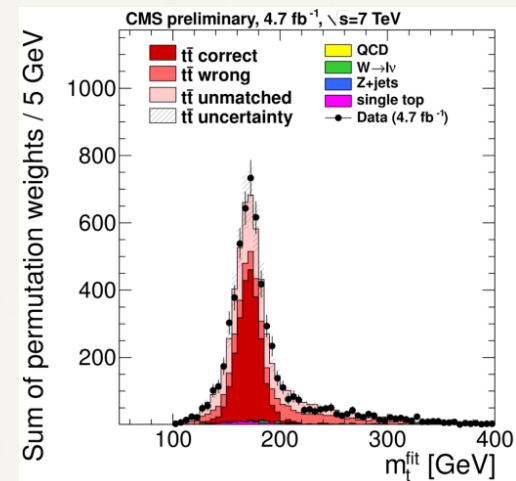
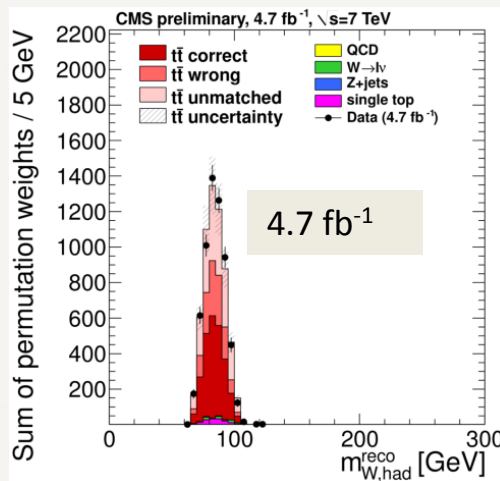
[arXiv:1203.5755](https://arxiv.org/abs/1203.5755)



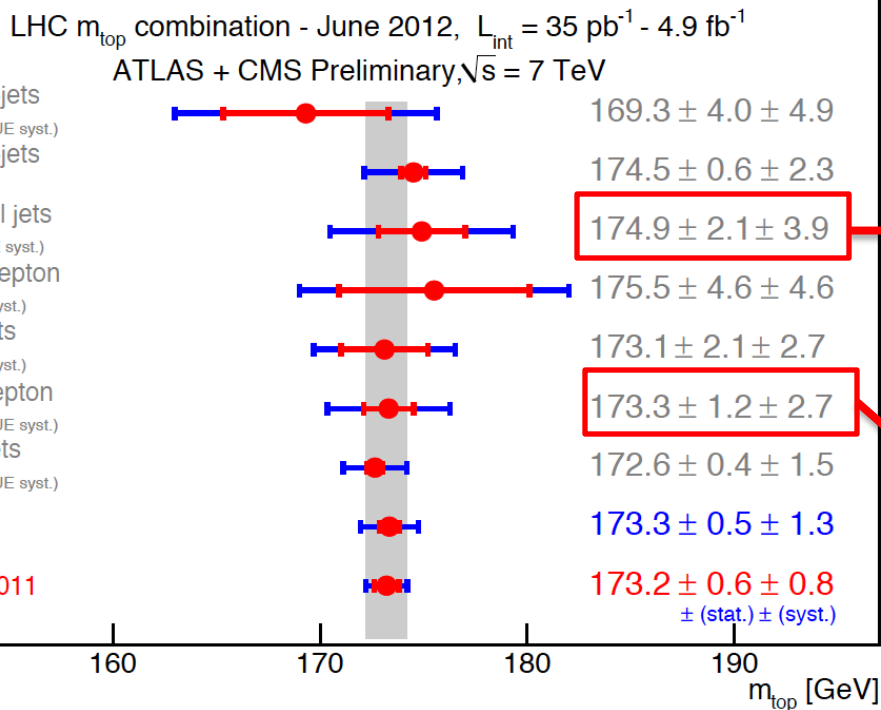
CMS: Use *all* jet-parton pairings, weight by probability (from MC) of pairing being correct (Ideogram method)

$$m_t = 172.6 \pm 0.6 \pm 1.2 \text{ GeV}$$

[CMS PAS TOP-11-015](https://arxiv.org/abs/1107.3164)

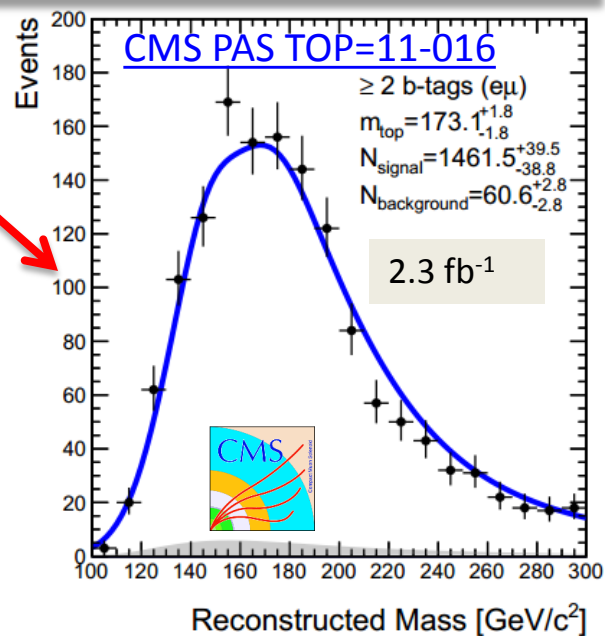
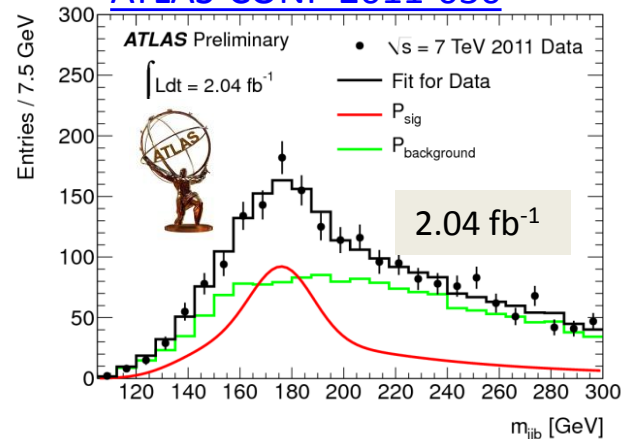


# Top Mass LHC



[CMS PAS TOP-12-001](#)  
[ATLAS-CONF-2012-095](#)

## ATLAS-CONF-2011-030

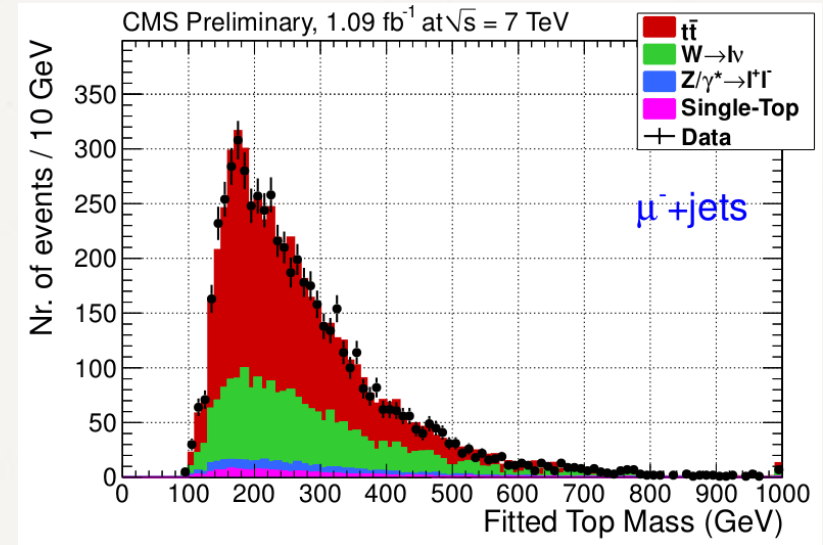
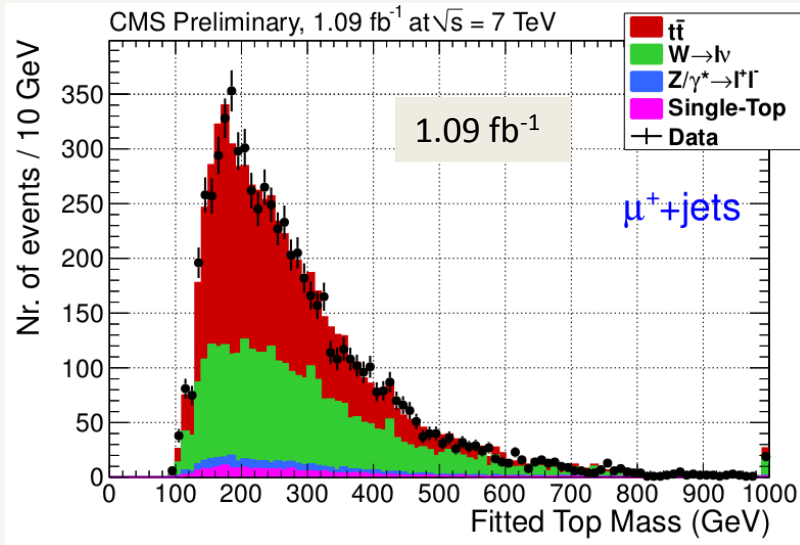


$$M_t - M_{\bar{t}}$$



If CPT is a good symmetry of nature, then  $\Delta M_t = M_t - M_{\bar{t}} = 0$

[arXiv:1204.2807](https://arxiv.org/abs/1204.2807)

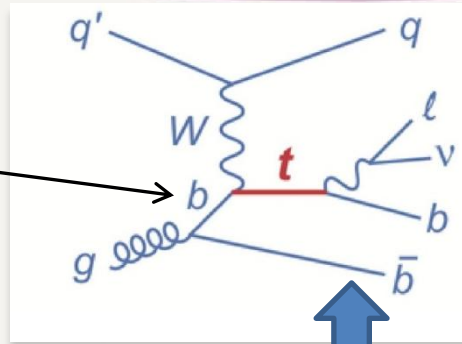


$$\Delta M_t = -0.44 \pm 0.46 \text{ (stat)} \pm 0.27 \text{ (syst)} \text{ GeV}$$

# Top Quark Width & $V_{tb}$

[PRD 85, 091104 \(2012\)](#)

$Wtb$  vertex  $\propto \Gamma(t \rightarrow Wb)$



**Inputs:**

$$\sigma(p\bar{p} \rightarrow tqb + X) = 2.90 \pm 0.59 \text{ pb}$$

$$R = B(t \rightarrow Wb) / B(t \rightarrow Wq) = 0.90 \pm 0.04$$

Measured in  $t\bar{t}$  events

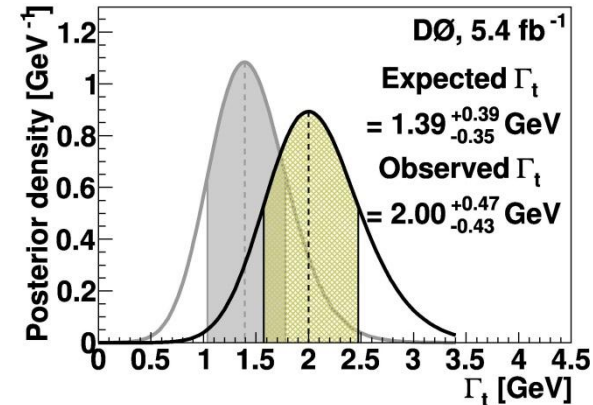
$$\Gamma(t \rightarrow Wb) = \frac{\sigma_{\text{meas}}(t\text{-chan})}{\sigma_{\text{SM}}(t\text{-chan})} \Gamma(t \rightarrow Wb)_{\text{SM}}$$

$$\Gamma_{\text{total}} = \frac{\Gamma(t \rightarrow Wb)}{B(t \rightarrow Wb)}$$



$$\Gamma_t = 2.00^{+0.47}_{-0.43} \text{ GeV} \Rightarrow \tau_t = \left(3.29^{+0.90}_{-0.63}\right) \times 10^{-25} \text{ s}$$

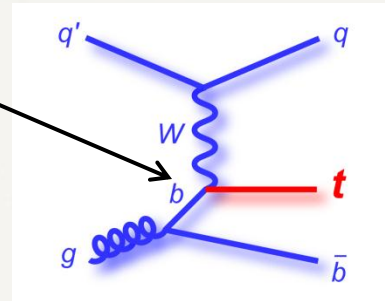
$$0.81 < |V_{tb}| < 1 \text{ @95\% C.L.}$$



# $V_{tb}$ from Single Top

Single-top cross section is  $\propto V_{tb}$

$$|V_{tb, \text{meas}}|^2 = \frac{\sigma_{\text{measured}}^{1t}}{\sigma_{\text{theory}}^{1t}} |V_{tb, \text{SM}}|^2$$



$|V_{tb}|$

ATLAS (1.04 fb <sup>-1</sup> )	<a href="https://arxiv.org/abs/1205.3130">arXiv:1205.3130</a>	$1.13^{+0.14}_{-0.13}$
CMS (1.1-1.5 fb <sup>-1</sup> )	<a href="https://arxiv.org/abs/1102.3567">CMS-PAS-TOP-11-021</a>	$1.04 \pm 0.09(\text{exp}) \pm 0.02(\text{th})$
CDF (7.5 fb <sup>-1</sup> )	<a href="https://arxiv.org/abs/1007.4096">CDF 10793</a>	$0.96 \pm 0.09(\text{exp}) \pm 0.05(\text{th})$
CDF+D0 (3.2, 2.3 fb <sup>-1</sup> )	<a href="https://arxiv.org/abs/0808.1798">Fermilab-TM-2440-E</a>	$0.88 \pm 0.07$

# $t\bar{t}\gamma$

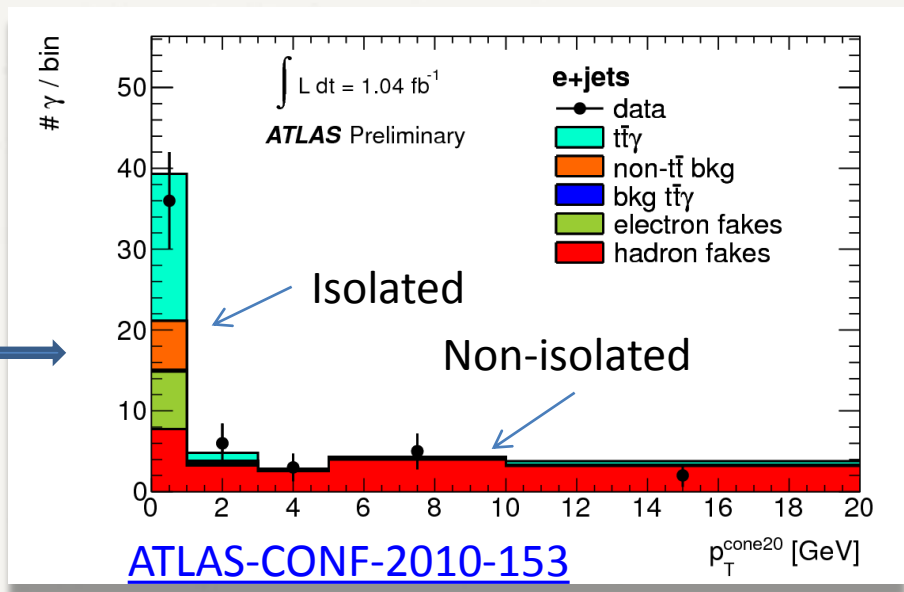
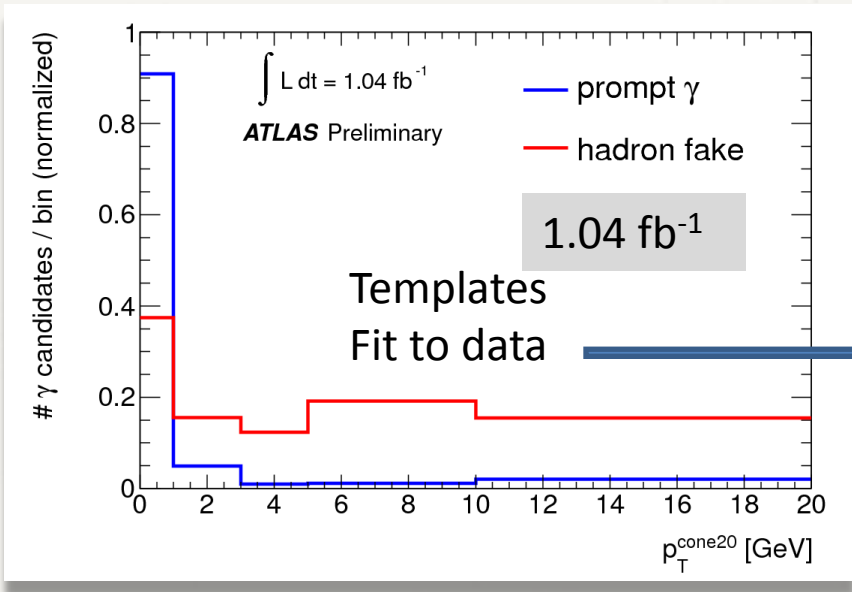
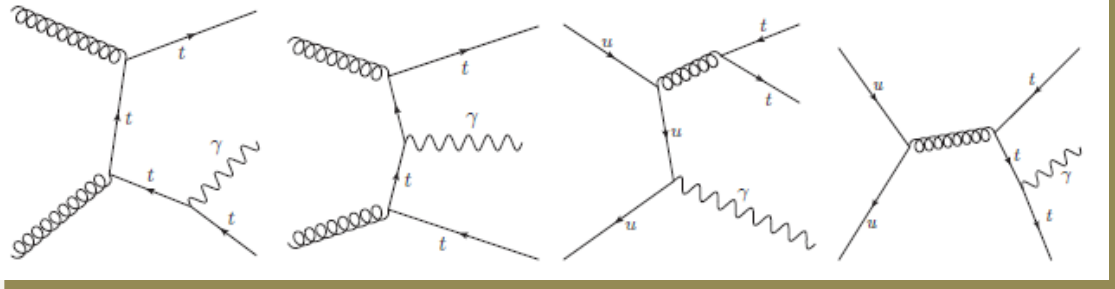


## Probe EWK couplings of the top quark

Sensitive to  $Q_{\text{top}}$  ( $Q_{\text{top}}$  also directly measured at Tevatron & LHC).

$P_T^\gamma > 8 \text{ GeV}$

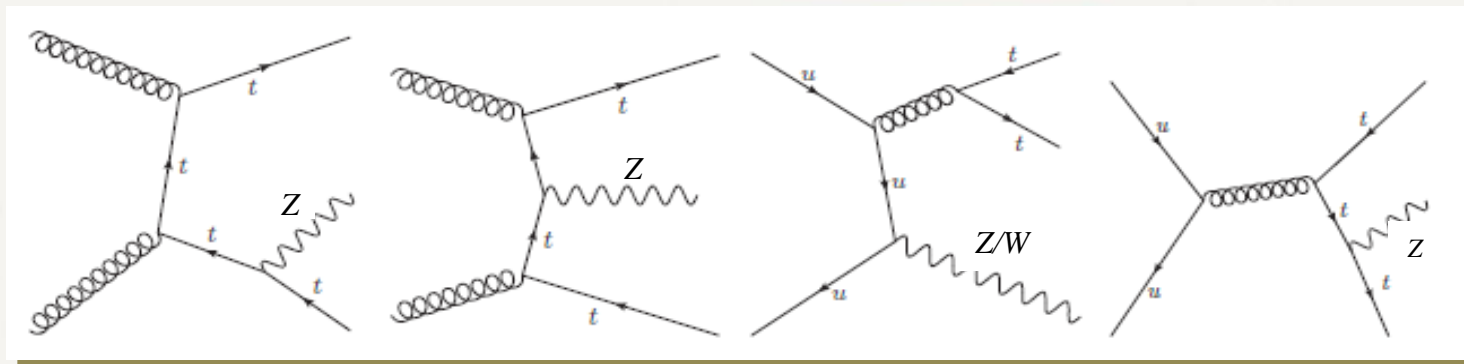
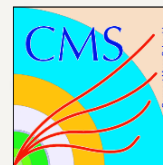
SM:  $2.1 \pm 0.4 \text{ pb}$



$\sigma_{t\bar{t}\gamma} * \text{BR} = 2.0 \pm 0.5 \text{ (stat)} \pm 0.7 \text{ (syst)} \pm 0.8 \text{ (lumi)} \text{ pb}$

See also P. Federic  
ATLAS  $Q_{\text{top}}$  Poster!

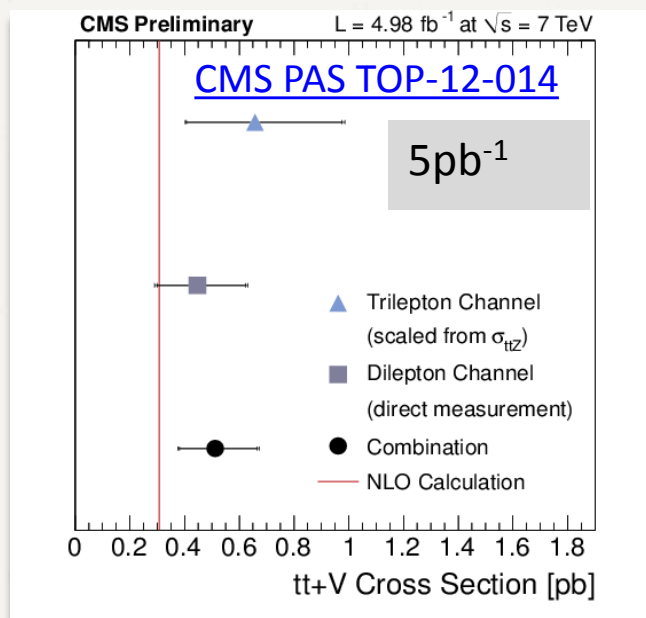
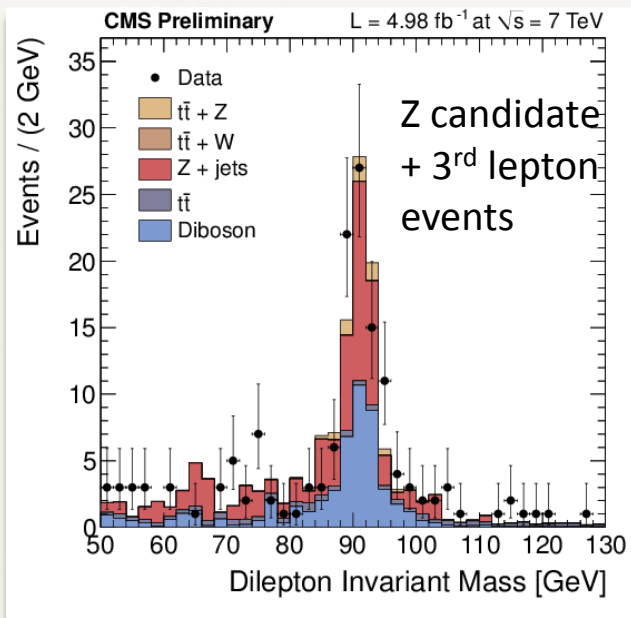
# $t\bar{t}V$



CMS:

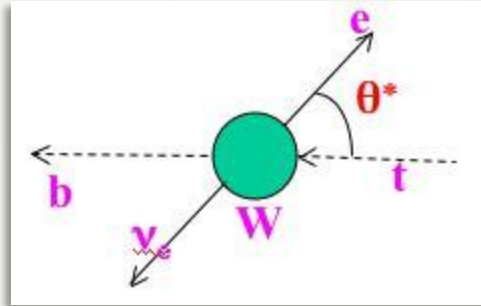
Trileptons ( $t\bar{t}Z$ )

Same-sign dileptons ( $t\bar{t}Z$  and  $t\bar{t}W$ )



ATLAS 4.7  $\text{fb}^{-1}$ :  
 $\sigma(t\bar{t}Z) < 0.71 \text{ pb}$

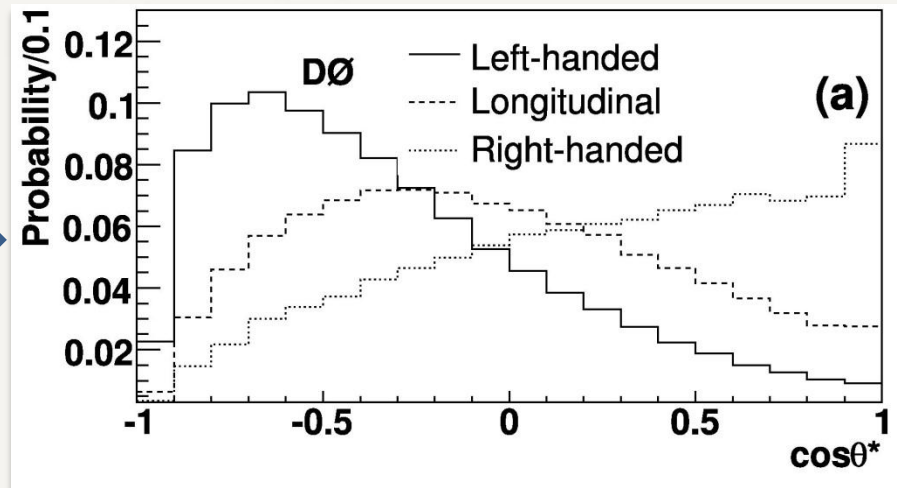
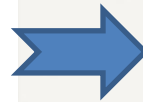
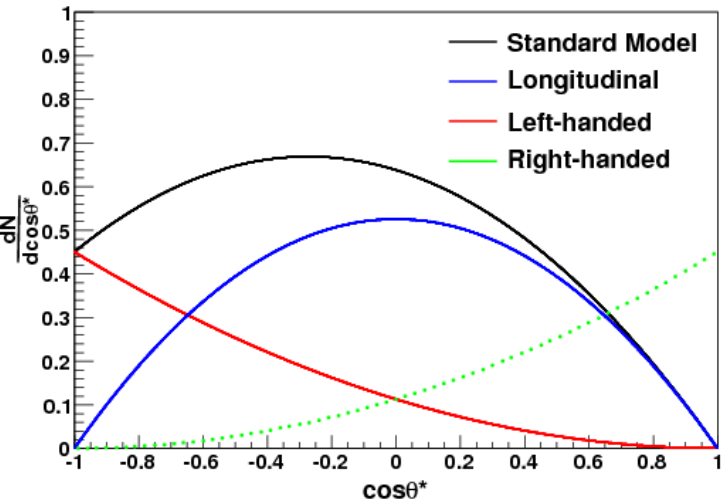
# W Helicity



IDEAL

RECONSTRUCTED

Theoretical  $\cos\theta^*$  distributions



$$(1/\Gamma) (d\Gamma/d\cos\theta^*) = f_- (3/8) (1 - \cos\theta^*)^2 + f_0 (3/4) (1 - \cos^2\theta^*) + f_+ (3/8) (1 + \cos\theta^*)^2$$

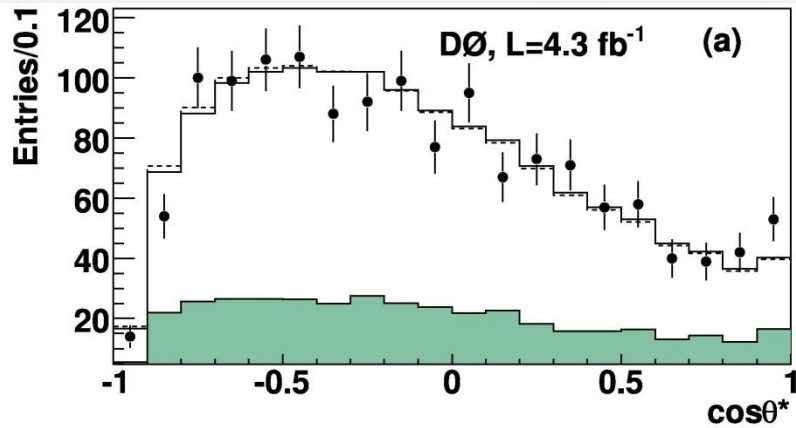
Left-handed, longitudinal, right-handed fractions



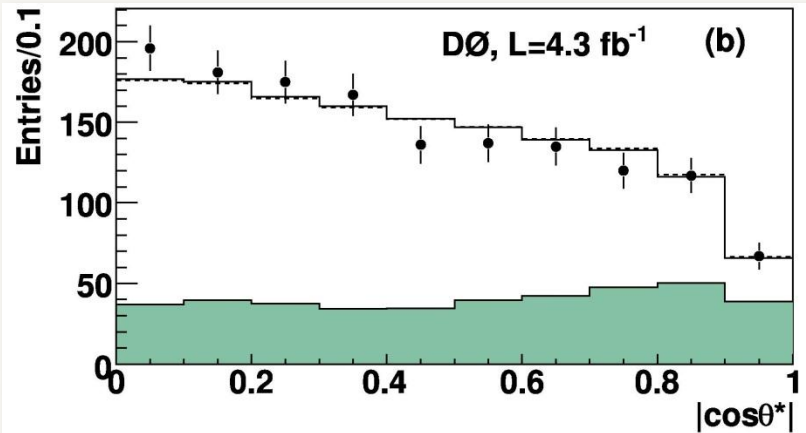
# W Helicity – D0

Template method

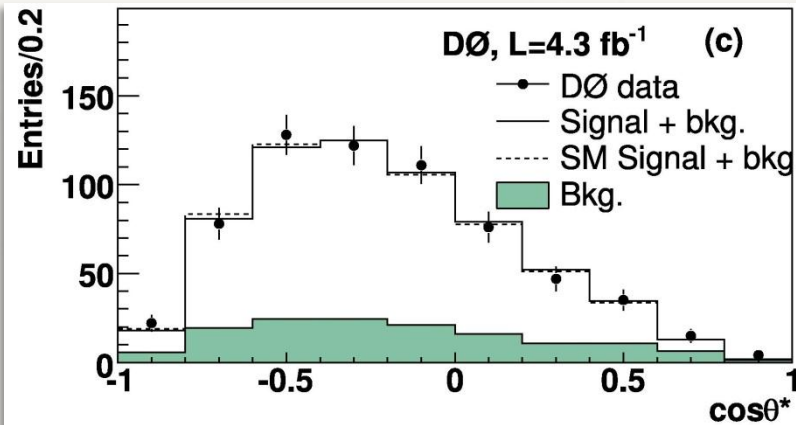
Leptonic W decay



Hadronic W decay



Dileptons



[PRD 83, 032009 \(2011\)](#)

$$f_0 = 0.669 \pm 0.078(\text{stat}) \pm 0.065(\text{syst})$$

$$f_+ = 0.023 \pm 0.041(\text{stat}) \pm 0.034(\text{syst})$$

# W Helicity - CDF

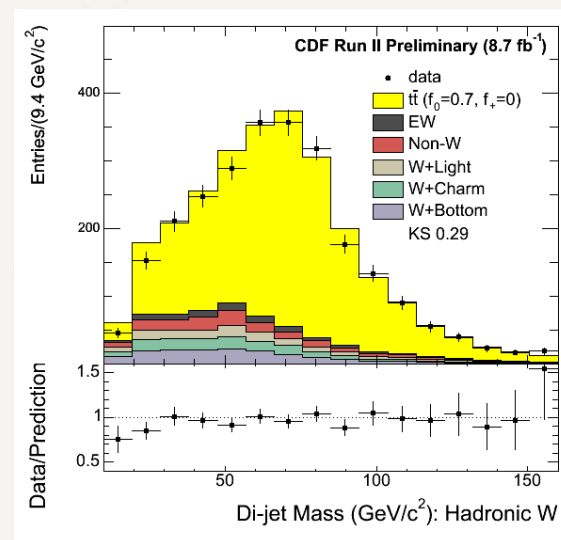
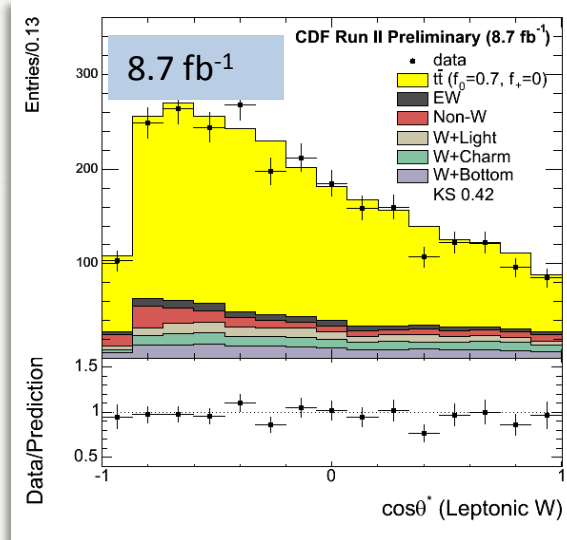
## Matrix element likelihood

$$\wp(x; f_0, f_+) = \frac{1}{\sigma_{\text{obs}}} \int d\sigma(y, f_0, f_+) f_{\text{PDF}}(q_1) f_{\text{PDF}}(q_2) W(x, y) dq_1 dq_2$$

$$\wp_{\text{evt}}(x; c_s, f_0, f_+) = c_s \wp_{t\bar{t}}(x; f_0, f_+) / A_s(x; f_0, f_+) + (1 - c_s) \wp_{\text{bkg}}(x) / A_b(x)$$

$A_s$  and  $A_b$  are signal and background acceptance terms

$$L(x; c_s, f_0, f_+) = \prod_{\text{events}} \wp_{\text{evt}}(x; c_s, f_0, f_+)$$



[CDF 10855](#)

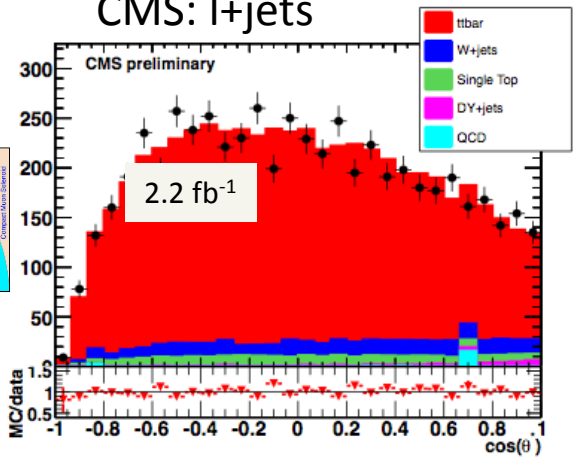
$$f_0 = 0.726 \pm 0.066 \text{ (stat)} \pm 0.067 \text{ (syst)}$$

$$f_+ = -0.045 \pm 0.043 \text{ (stat)} \pm 0.058 \text{ (syst)}$$

# W Helicity - CMS & ATLAS

## Template Method

CMS: l+jets

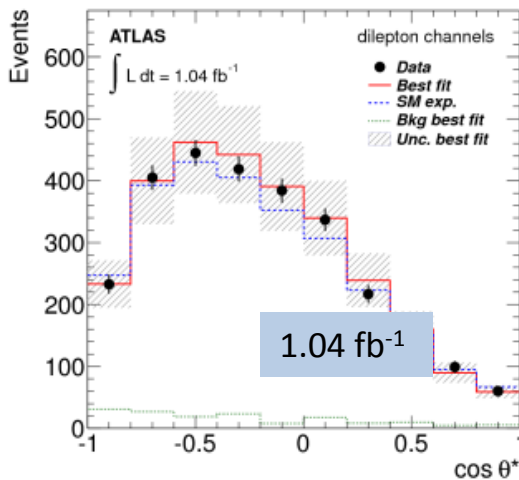


$$F_0 = 0.567 \pm 0.074(\text{stat.}) \pm 0.047(\text{syst.})$$

$$F_L = 0.393 \pm 0.045(\text{stat.}) \pm 0.029(\text{syst.}),$$

[CMS PAS TOP-11-020](#)

ATLAS: l+jets  
and dilepton (*shown*)



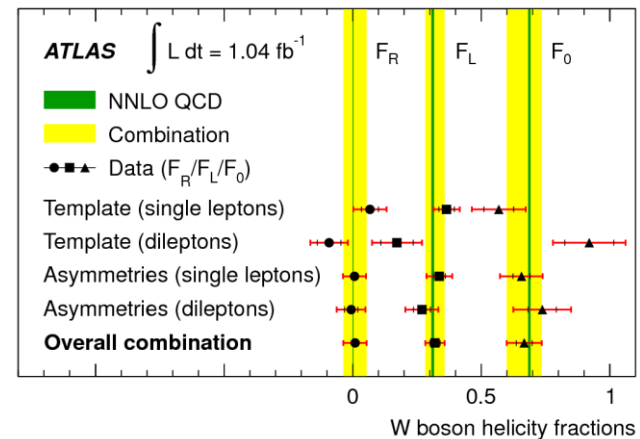
$$F_0 = 0.67 \pm 0.03 (\text{stat.}) \pm 0.06 (\text{syst.}),$$

$$F_L = 0.32 \pm 0.02 (\text{stat.}) \pm 0.03 (\text{syst.}),$$

$$F_R = 0.01 \pm 0.01 (\text{stat.}) \pm 0.04 (\text{syst.}).$$

Combine  
l+jets and dilepton

[JHEP 1206, 088 \(2012\)](#)



# Limits on Wtb Anomalous Couplings

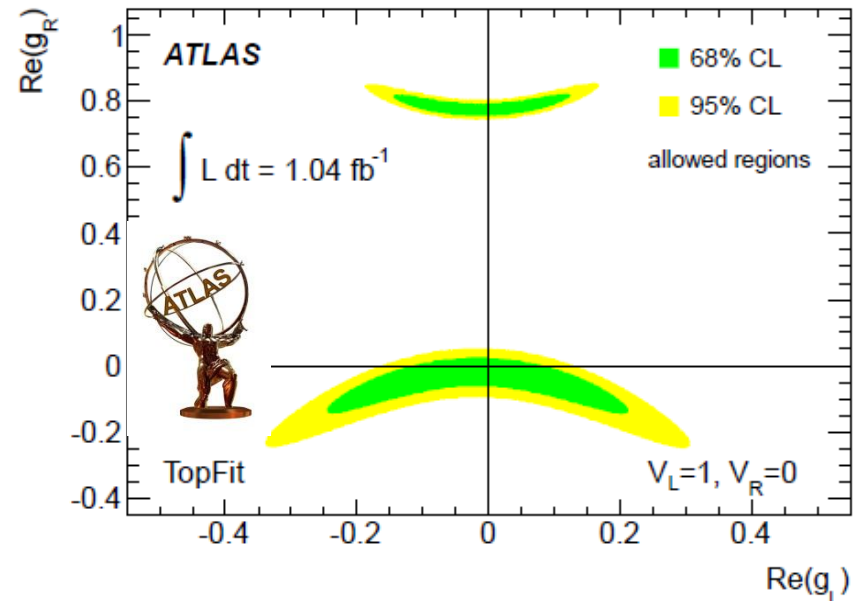
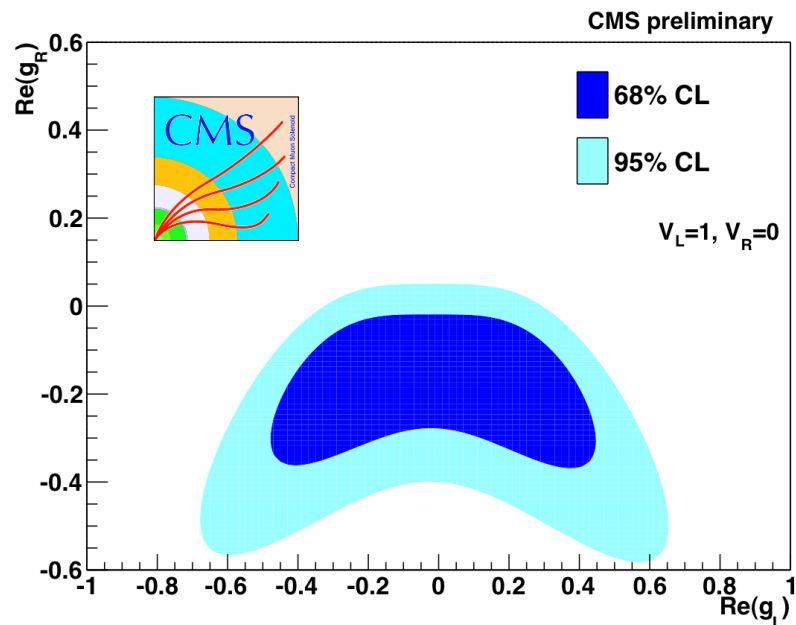
$$L_{Wtb} = \frac{g}{\sqrt{2}} \bar{b} \gamma^\mu \left( V_L (1 - \gamma^5) + V_R (1 + \gamma^5) \right) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} \left( g_L (1 - \gamma^5) + g_R (1 + \gamma^5) \right) t W_\mu^- + h.c.$$

All zero in SM at tree-level

[CMS PAS TOP-11-020](#)

Limits on  $g_R$  and  $g_L$  for  $V_R=0$

[JHEP 1206, 088 \(2012\)](#)

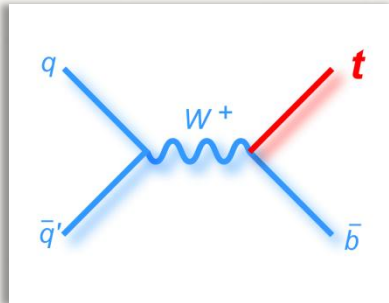


# Flavor-Changing Neutral Currents

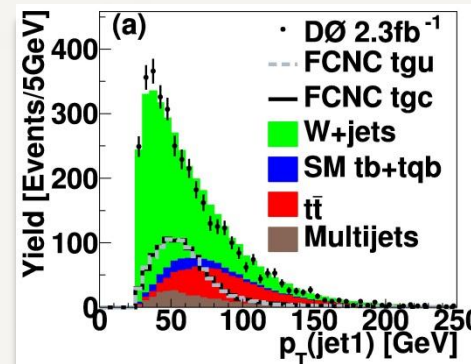
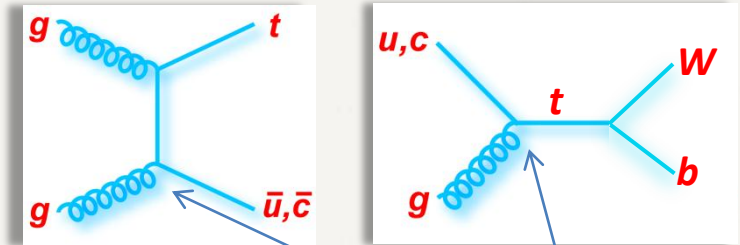
SM has no FCNC couplings at tree-level, and GIM mechanism causes almost perfect cancelation of FCNC at higher-order *if* quarks come in pairs (that's why bottom required top). Many BSM models include FCNC at  $\sim \text{few} \times 10^{-4}$  level.

The most sensitive tests in the top sector come from single-top production:

Subtle difference from SM production:



But kinematics are different:



Only sensitive to  $tgq$  coupling

Neural networks used for S/B discrimination

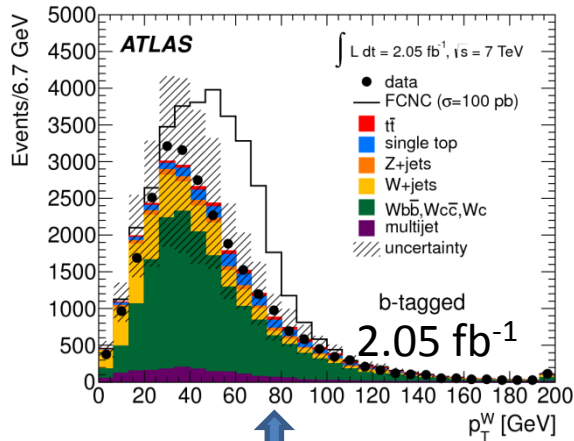
# FCNC Limits – Single Top

[PLB 712, 351 \(2012\)](#)

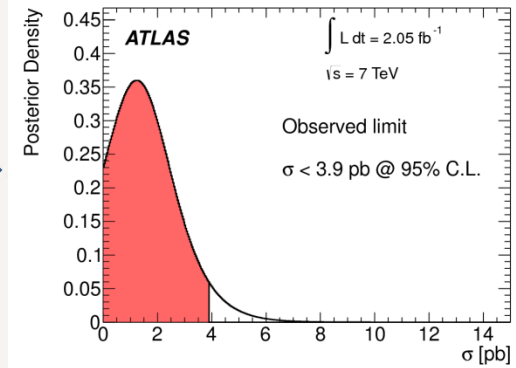
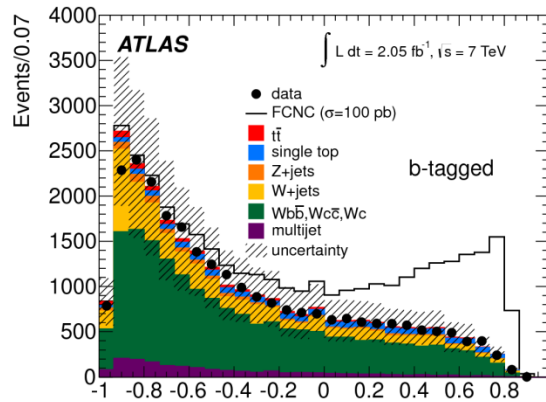
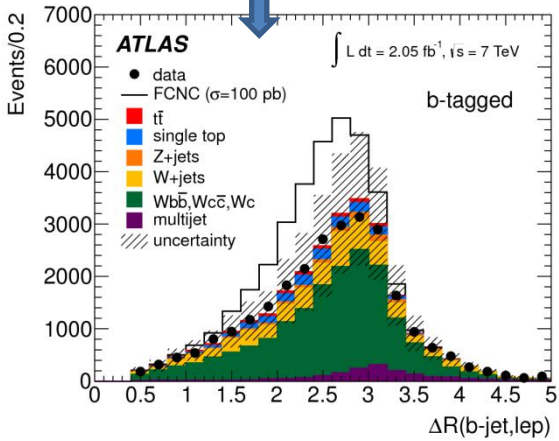
First limits from D0 and CDF:

$$B(t \rightarrow gu) < 2 \times 10^{-4} \quad B(t \rightarrow gc) < 3.9 \times 10^{-3} \quad (\text{D0})$$

$$\frac{K_{tgu}}{\Lambda} < 0.025 \text{ TeV} \quad \frac{K_{tgc}}{\Lambda} < 0.105 \text{ TeV} \quad (\text{CDF})$$



NN inputs (example)



$\sigma < 3.9 \text{ pb}$

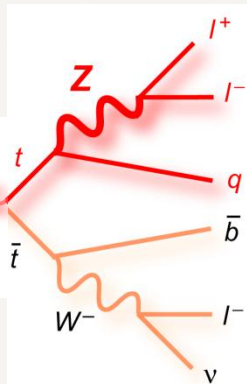
$$B(t \rightarrow ug) < 5.7 \cdot 10^{-5}$$

$$B(t \rightarrow cg) < 2.7 \cdot 10^{-4}$$

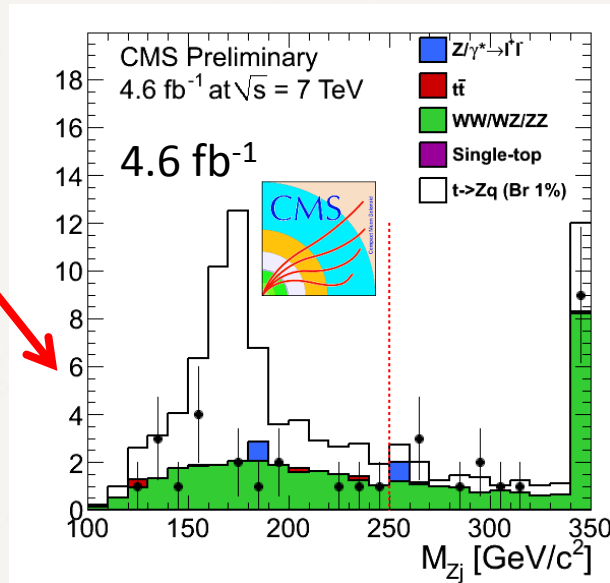
# FCNC - $t \rightarrow Zq$

Search for FCNC couplings to  $Zq$  through top decay.

Search for  $t\bar{t} \rightarrow WbZq$  - One SM decay to  $Wb$ , one FCNC decay to  $Zq$



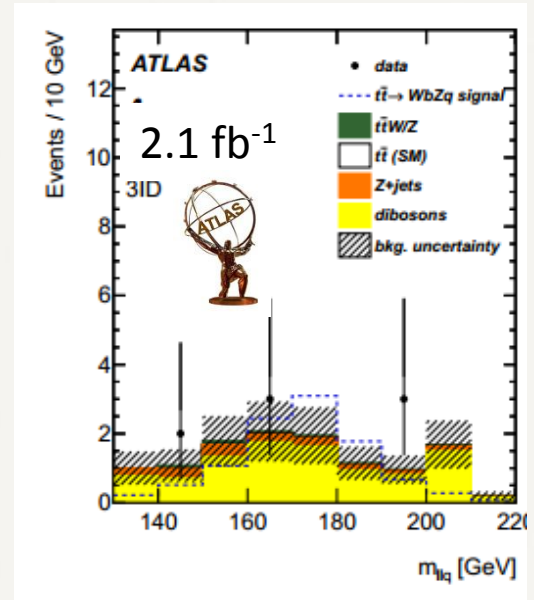
Tri-lepton signature



[CMS PAS TOP-11-028](#)

$Z$ +jet mass= $M_t$  for signal

[arXiv:1206.0257](#)



$\text{Br}(t \rightarrow qZ) < 0.34\%$  at 95% C.L.

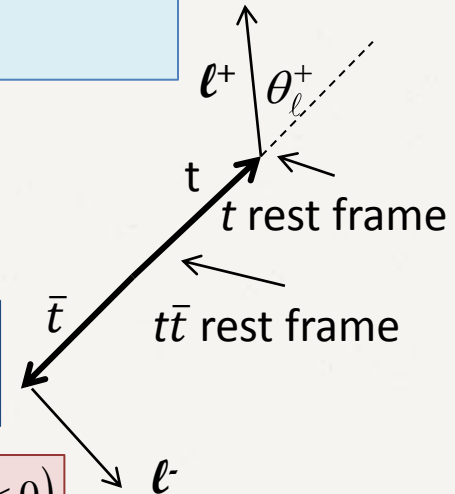
$\text{Br}(t \rightarrow qZ) < 0.73\%$  at 95% C.L.



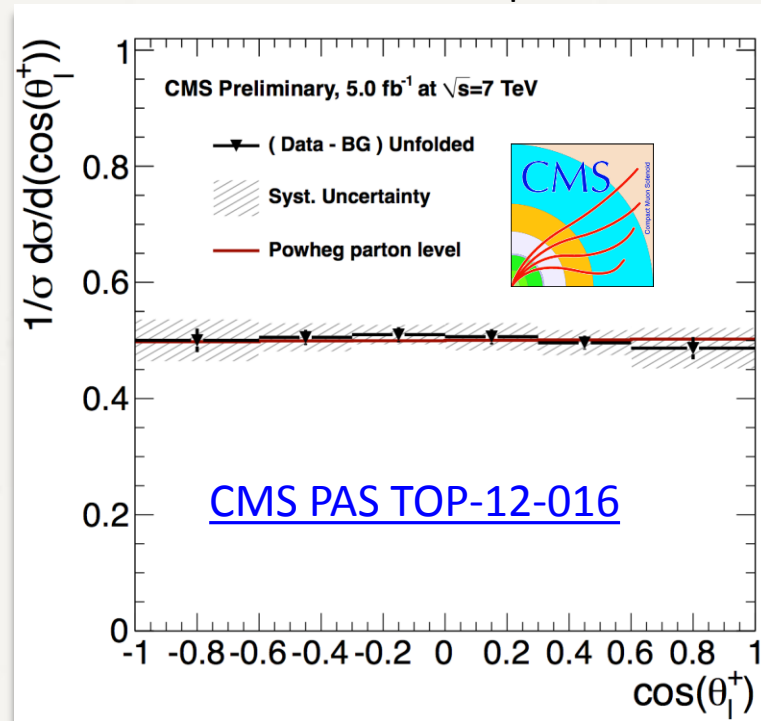
# Top quark polarization

Unlike other quarks, top decays before hadronization, and therefore its spin is preserved from production through decay.

$t\bar{t}$  pairs are produced via QCD and the spin is expected to be unpolarized (EWK corrections give a small net polarization).



Unfolded to account for acceptance effects



$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_\ell} = \frac{1}{2} (1 + 2P_n \cos \theta_\ell)$$

$$P_n = \frac{N(\cos \theta_\ell^+ > 0) - N(\cos \theta_\ell^+ < 0)}{N(\cos \theta_\ell^+ > 0) + N(\cos \theta_\ell^+ < 0)}$$

Analytical Matrix Weighting used to reconstruct dilepton system  
(L. Sonnenschein [PRD 73 054015 \(2006\)](#))

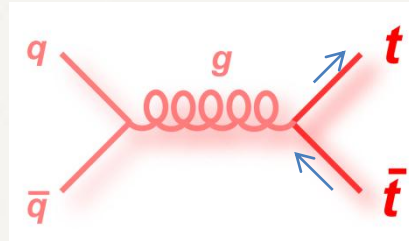
$$P_n = -0.009 \pm 0.029 \pm 0.041$$



# Spin Correlations

$t$  and  $\bar{t}$  may be unpolarized, but their spin directions are *correlated*.

Tevatron (dominant):



R

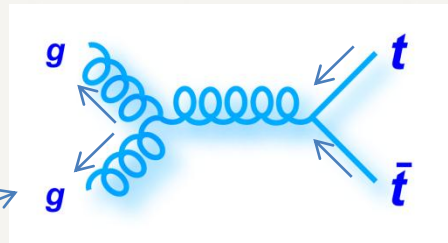
L

Opposite helicity (RL or LR)

Low  $M_{t\bar{t}}$

Like-helicity gluons

LHC (dominant):



L

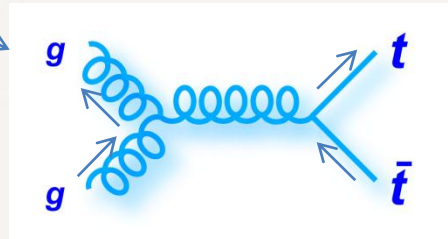
L

Like helicity (LL or RR)

Mahlon & Parke, PRD 81, 074024 (2010)

High  $M_{t\bar{t}}$

Opposite-helicity gluons



R

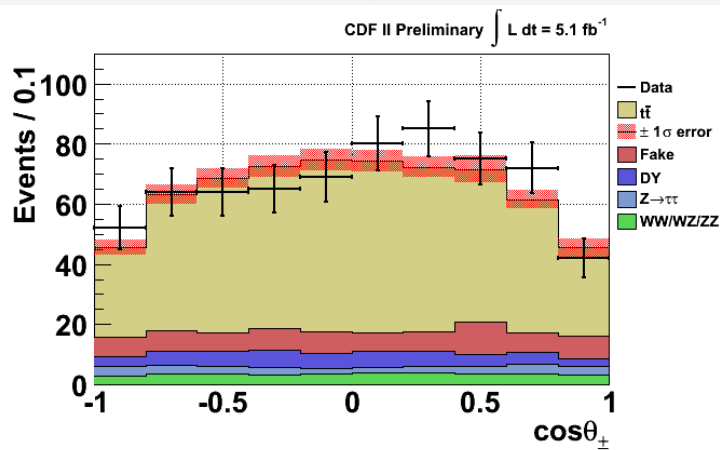
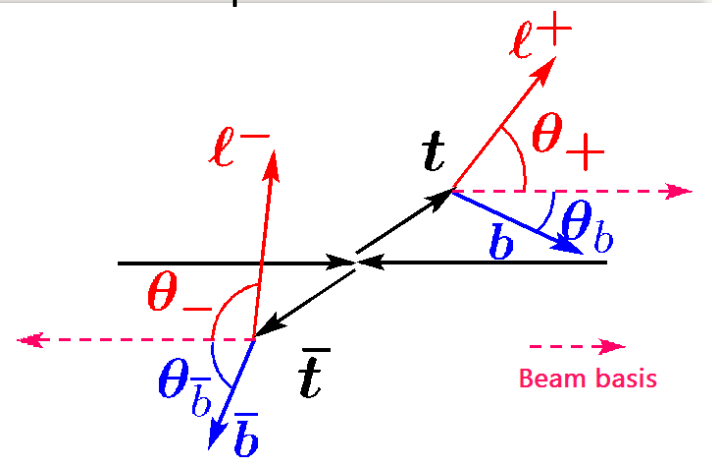
L

Opposite helicity (RL or LR)

# Spin Correlations - CDF

$$\frac{1}{\sigma} \frac{d^2\sigma}{d\cos\theta_+ d\cos\theta_-} = \frac{1 + \kappa \cos\theta_+ \cos\theta_-}{4}$$

Dilepton channel

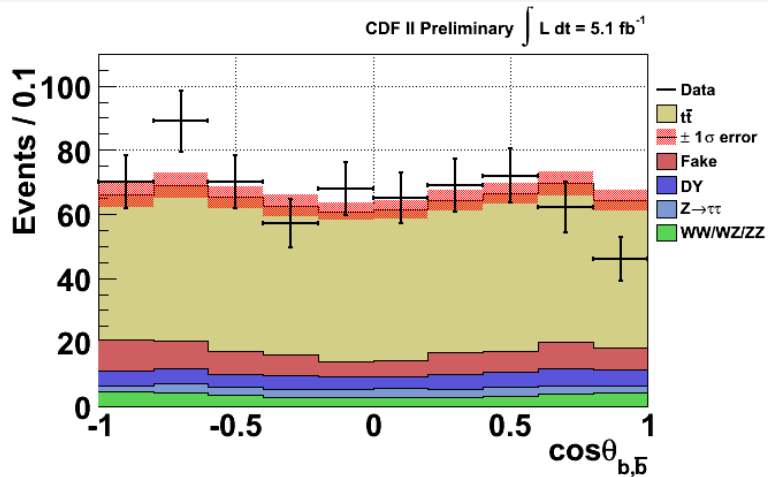


$$-0.520 < \kappa < 0.605 \text{ (68\% C.L.)}$$

OR

$$\kappa = 0.042^{+0.563}_{-0.562}$$

[CDF 10719](#)



# Spin Correlations – D0

Matrix element technique in lepton+jets events

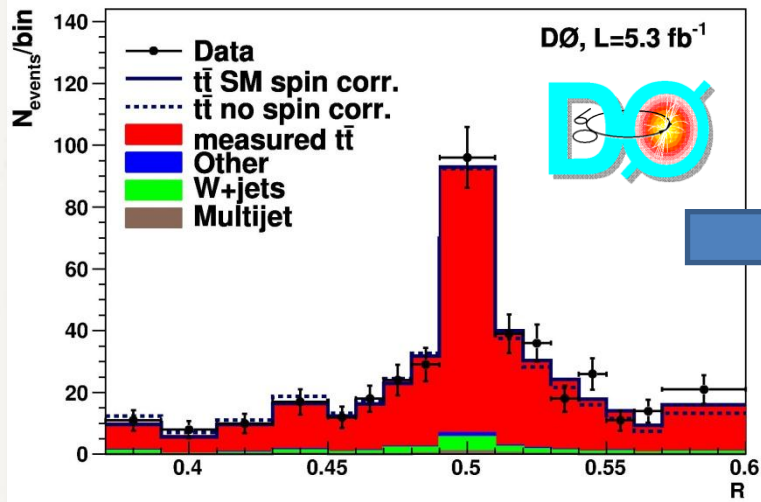
$$\wp(x; H) = \frac{1}{\sigma_{\text{obs}}} \int f_{\text{PDF}}(q_1) f_{\text{PDF}}(q_2) dq_1 dq_2 \frac{(2\pi)^4 |M(y, H)|^2}{q_1 q_2 s} W(x, y) d\Phi_6$$

$M(y, H)$  is LO matrix element with (H=c) or without (H=u) spin correlations.

Transfer function from partonic  $y$  to measured  $x$

Fit  $R$  dist. to  $f * R_{\text{corr}} + (1-f) * R_{\text{uncorr}}$

$$R = \frac{\wp(x; H=c)}{\wp(x; H=u) + \wp(x; H=c)}$$



Hard to see corr. vs. no corr. Difference. Tough measurement!

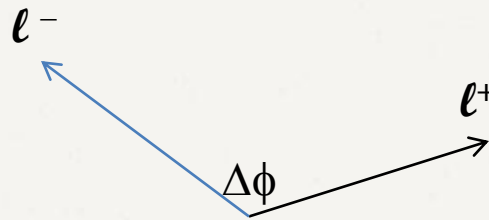
$$f = 1.15_{-0.43}^{+0.42} \text{ (stat+syst)}$$

Combined with result in dileptons:

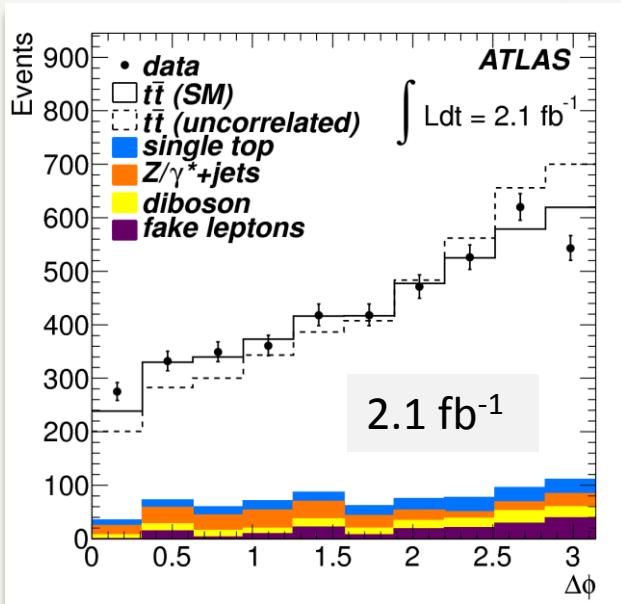
$$f = 0.85 \pm 0.29 \text{ (stat+syst)}$$

# Spin Correlations - ATLAS

$gg \rightarrow t\bar{t}$  is the dominant production mode at LHC  
 LL & RR  $t\bar{t}$  pairs produce charged leptons with correlated azimuthal angles



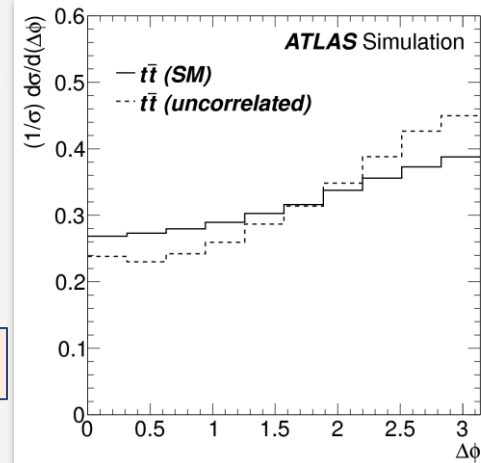
Straightforward measurement in dileptons!



Fit  $\Delta\phi$  dist. to  $f * \Delta\phi_{\text{corr}} + (1-f) * \Delta\phi_{\text{uncorr}}$

$$f = 1.30 \pm 0.14 (\text{stat}) \begin{matrix} +0.27 \\ -0.22 \end{matrix} (\text{syst})$$

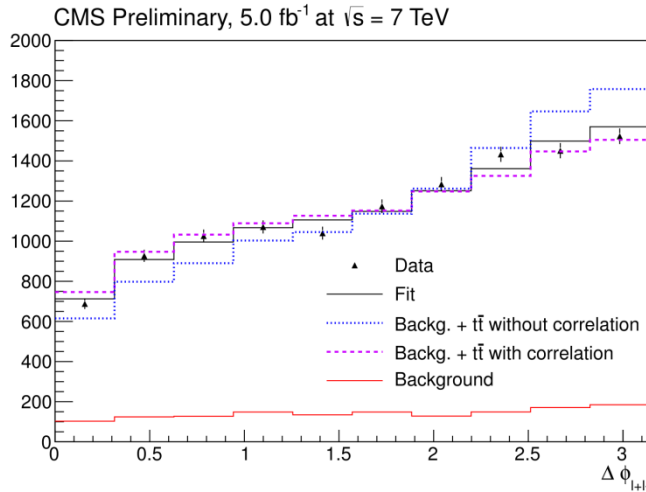
$f=0$  excluded at  $5.1\sigma$  level.



[PRL 108, 212001 \(2012\)](#)

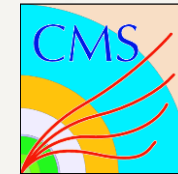
# Spin Correlations - CMS

Similar analysis to ATLAS, in  $5 \text{ fb}^{-1}$



$$f = 0.74 \pm 0.08(\text{stat}) \pm 0.24(\text{syst})$$

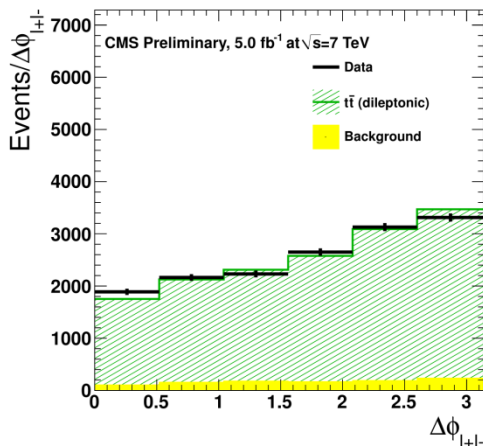
[CMS PAS TOP-12-004](#)



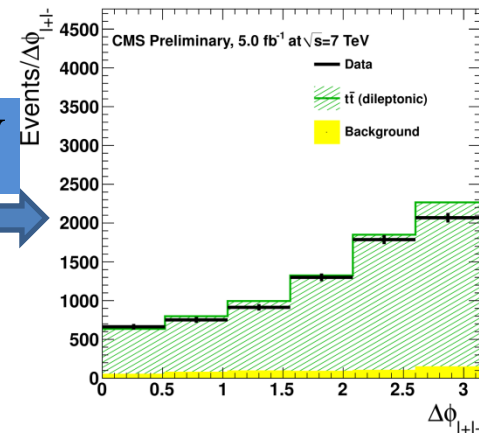
New physics at high  $M_{t\bar{t}}$ ?

Signal enhanced w/  $M_{t\bar{t}}$  cut:

But no sign of PBSM



$$M_{t\bar{t}} > 450 \text{ GeV}$$



# Conclusions

- Four experiments are now making relatively precise measurements of top quark properties:
  - Mass
  - Couplings
  - Rare decays
- Tevatron experiments have led the way with many advanced techniques
  - Matrix elements
  - Neural networks
- LHC experiments benefit from the large  $t\bar{t}$  and single top cross sections
  - Measurements are already systematics dominated
- So far, all top quark properties are consistent with SM expectations
  - Only the charge asymmetry at the Tevatron stands out as anomalous.
- Stay tuned.